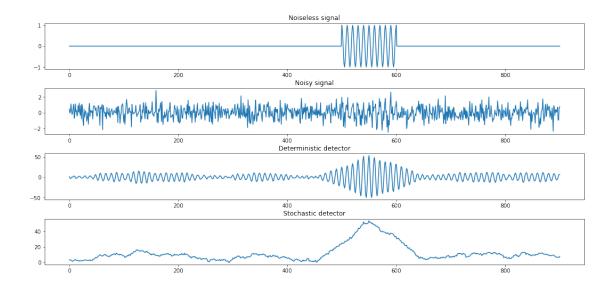
E2_Question_4_5

November 2, 2020

1 Answers to question 4

```
[1]: "Answers to question 4."
     import numpy as np
     import matplotlib.pyplot as plt
     # a) Create a vector of zero and sinusoidal components
     zeros = np.zeros(500)
     n = np.arange(500, 601)
     sinusoid = np.cos(2 * np.pi * 0.1 * n)
     y = np.concatenate([zeros, sinusoid])
     y = np.concatenate([y, np.zeros(300)])
     # b) Create a noisy version of the signal x[n]
     y_n = y + np.sqrt(0.5) * np.random.randn(y.size)
     # c) Implement the deterministic sinusoid detector
     y_d = np.convolve(sinusoid, y_n, 'same')
     # d) Implement the random signal version
     e = np.exp(-2 * np.pi * 1j * 0.1 * n)
     y_r = np.abs( np.convolve(e, y_n, 'same') )
     # e) Generate plots
     fig, ax = plt.subplots(4, 1, figsize=(15, 7))
     fig.tight_layout(pad=1.5)
     ax[0].plot(y)
     ax[0].title.set_text('Noiseless signal')
     ax[1].plot(y_n)
     ax[1].title.set_text('Noisy signal')
     ax[2].plot(y d)
     ax[2].title.set_text('Deterministic detector')
     ax[3].plot(y_r)
     ax[3].title.set_text('Stochastic detector')
```



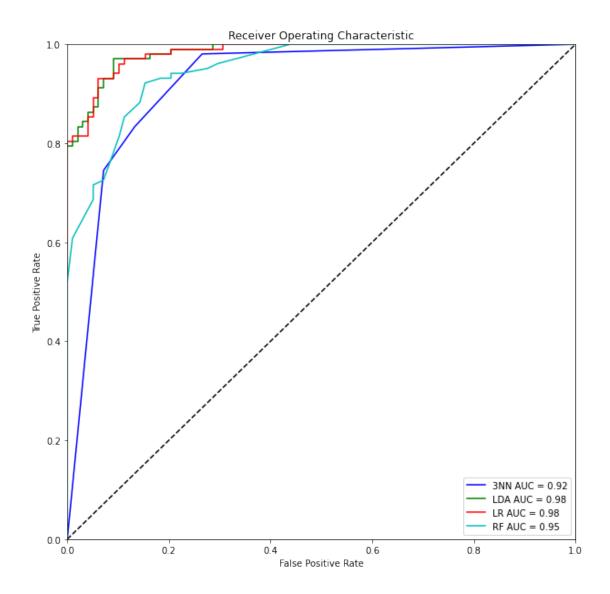
2 Answers to question 5

```
[2]: import numpy as np
     import scipy.io
     # a) Load data & split into training & testing samples
     root = '/home/tuomas/Python/DATA.ML.200/Ex2/'
     data = scipy.io.loadmat(root + 'twoClassData.mat')
     dataX = data['X']
     dataY = data['y'][0]
     trainX = dataX[:200,]
     trainY = dataY[:200]
     testX = dataX[200:,]
     testY = dataY[200:]
     # 3NN-classifier
     from sklearn.neighbors import KNeighborsClassifier
     K = 3
     KNN = KNeighborsClassifier(n_neighbors=K)
     KNN.fit(trainX, trainY)
     KNN_predY = KNN.predict(testX)
     KNN_probs = KNN.predict_proba(testX)
     KNN_acc = np.sum(testY==KNN_predY) / testY.size
     print("{}NN-accuracy: {}".format(K, KNN_acc))
```

```
# Linear Discriminant Analysis
from sklearn.discriminant_analysis import LinearDiscriminantAnalysis
LDA = LinearDiscriminantAnalysis(solver='svd')
LDA.fit(trainX, trainY)
LDA_predY = LDA.predict(testX)
LDA_probs = LDA.predict_proba(testX)
LDA_acc = np.sum(testY==LDA_predY) / testY.size
print("LDA-accuracy: {}".format(LDA_acc))
# Logistic Regression
from sklearn.linear_model import LogisticRegression
LR = LogisticRegression()
LR.fit(trainX, trainY)
LR_predY = LR.predict(testX)
LR_probs = LR.predict_proba(testX)
LR_acc = np.sum(testY==LR_predY) / testY.size
print("LR-accuracy: {}".format(LR_acc))
# Random Forest
from sklearn.ensemble import RandomForestClassifier
RF = RandomForestClassifier(n_estimators=20)
RF.fit(trainX, trainY)
RF_predY = RF.predict(testX)
RF_probs = RF.predict_proba(testX)
RF_acc = np.sum(testY==RF_predY) / testY.size
print("RF-accuracy: {}".format(RF_acc))
# ROC & AUC for each classifier
from sklearn import metrics
KNN_fpr, KNN_tpr, th = metrics.roc_curve(testY, KNN_probs[:,1])
KNN_auc = metrics.auc(KNN_fpr, KNN_tpr)
LDA_fpr, LDA_tpr, th = metrics.roc_curve(testY, LDA_probs[:,1], pos_label=1)
LDA_auc = metrics.auc(LDA_fpr, LDA_tpr)
LR_fpr, LR_tpr, th = metrics.roc_curve(testY, LR_probs[:,1], pos_label=1)
LR_auc = metrics.auc(LR_fpr, LR_tpr)
RF_fpr, RF_tpr, th = metrics.roc_curve(testY, RF_probs[:,1], pos_label=1)
```

```
RF_auc = metrics.auc(RF_fpr, RF_tpr)
import matplotlib.pyplot as plt
plt.figure(figsize=(10, 10))
plt.title('Receiver Operating Characteristic')
plt.plot(KNN_fpr, KNN_tpr, '-b', label = '3NN AUC = {}'.format(np.
→round(KNN_auc,2)))
plt.plot(LDA_fpr, LDA_tpr, '-g', label = 'LDA AUC = {}'.format(np.
→round(LDA_auc,2)))
plt.plot(LR_fpr, LR_tpr, '-r', label = 'LR AUC = {}'.format(np.round(LR_auc,2)))
plt.plot(RF_fpr, RF_tpr, '-c', label = 'RF AUC = {}'.format(np.round(RF_auc,2)))
plt.legend(loc = 'lower right')
plt.plot([0, 1], [0, 1], '--k')
plt.xlim([0, 1])
plt.ylim([0, 1])
plt.ylabel('True Positive Rate')
plt.xlabel('False Positive Rate')
plt.show()
```

3NN-accuracy: 0.85 LDA-accuracy: 0.91 LR-accuracy: 0.92 RF-accuracy: 0.87



```
[3]: # b) Fill in the attached table
import pandas as pd
import matplotlib.pyplot as plt

fig, ax = plt.subplots(figsize=(15,2))
ax.axis('off')
ax.axis('tight')

col_names = ['Model', 'Accuracy Score', 'ROC-AUC Score']
names = ['3-Nearest Neighbor', 'Linear Discriminant Analysis', 'Logistic
→Regression', 'Random Forest']
accs = [KNN_acc, LDA_acc, LR_acc, RF_acc]
roc_aucs = np.round([KNN_auc, LDA_auc, LR_auc, RF_auc], 2)
```

Model	Accuracy Score	ROC-AUC Score
3-Nearest Neighbor	0.85	0.92
Linear Discriminant Analysis	0.91	0.98
Logistic Regression	0.92	0.98
Random Forest	0.87	0.95