

EE2211 Tutorial 10

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- a) True
- b) False

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We have 3 parameter candidates for a classification model, and we would like to choose the optimal one for deployment. As such, we run 5-fold cross-validation.

Once we have completed the 5-fold cross-validation, in total, we have trained _____ classifiers. Note that, we treat models with different parameters as different classifiers.

- A) 10
- B) 20
- C) 25
- D) 15

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In each fold, we train 3 classifiers, so 5 folds give 15 classifiers.

Suppose the binary classification problem, which you are dealing with, has highly imbalanced classes. The majority class has 99 hundred samples and the minority class has 1 hundred samples. Which of the following metric(s) would you choose for assessing the classification performance?

- a) Classification Accuracy
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	$\widehat{\mathbf{P}}$ (predicted)	$\widehat{\mathbf{N}}$ (predicted)	
P (actual)	TP	FN	Recall TP/(TP+FN)
N (actual)	FP	TN	
	Precision TP/(TP+FP)	(TP+TN	Accuracy I)/(TP+TN+FP+FN)

Page 28, Lec 10

The goal is to highlight the problems of the results!

In this case, we shall

- 1) Use cost matrix, assign different costs for each entry
- 2) Use Precision and Recall! Precision = 0.5 and Recall = 0.5

Given below is a scenario for Training error rate Tr, and Validation error rate Va for a machine learning algorithm. You want to choose a hyperparameter (P) based on Tr and Va. Which value of P will you choose based on the above table?

- a) 10
- b) 9
- c) 8
- d) 7
- e) 6

Р	Tr	Va
10	0.10	0.25
9	0.30	0.35
8	0.22	0.15
7	0.15	0.25
6	0.18	0.15

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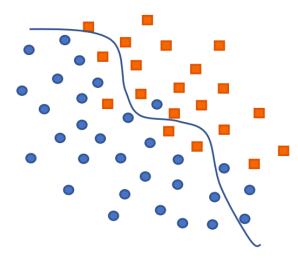
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(Binary and Multicategory Confusion Matrices)

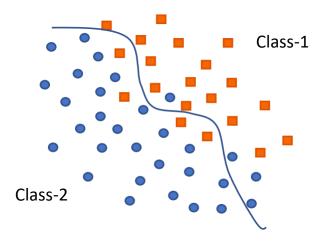
Tabulate the confusion matrices for the following classification problems.

a) Binary problem (the class-1 and class-2 data points are respectively indicated by squares and circles)



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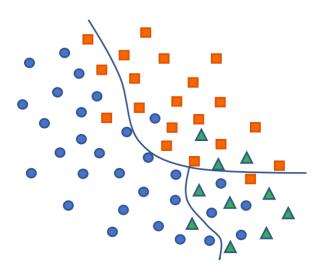
 a) Binary problem (the class-1 and class-2 data points are respectively indicated by squares and circles)



	$P_{\widehat{1}}$	$P_{\widehat{2}}$		
P_1	16	4		
P_2	4	26		

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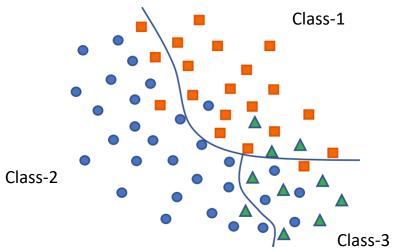
b) Three-category problem (the class-1, class-2 and class-3 data points are respectively indicated by squares, circles and triangles)



12

Tabulate the confusion matrices for the following classification problems.

b) Three-category problem (the class-1, class-2 and class-3 data points are respectively indicated by squares, circles and triangles)



	$P_{\widehat{1}}$	$P_{\widehat{2}}$	$P_{\widehat{3}}$
P_1	16	3	1
P_2	1	25	4
P_3	3	1	6

Q6 (python)

(5-fold Cross-Validation)

Get the data set "from sklearn.datasets import load_iris". Perform a 5-fold Cross-validation to observe the best polynomial order (among orders 1 to 10 and without regularization) for validation prediction. Note that, you will have to partition the whole dataset for training/validation/test parts, where the size of validation set is the same as that of test. Provide a plot of the average 5-fold training and validation error rates over the polynomial orders. The randomly partitioned data sets of the 5-fold shall be maintained for reuse in evaluation of future algorithms



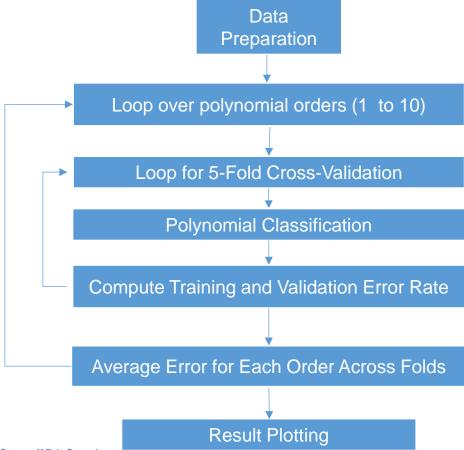
About this file

The dataset is a CSV file which contains a set of 150 records under 5 attributes - Petal Length, Petal Width, Sepal Length, Sepal width and Class(Species)

# sepal_length	=	# sepal_width	=	# petal_length	=	# petal_width	=	∆ species =
4.3	7.9		4.4		6.9	0.1	2.5	3 unique values
5.1		3.5		1.4		0.2		Iris-setosa
4.9		3		1.4		0.2		Iris-setosa
4.7		3.2		1.3		0.2		Iris-setosa
4.6		3.1		1.5		0.2		Iris-setosa
5		3.6		1.4		0.2		Iris-setosa
5.4		3.9		1.7		0.4		Iris-setosa
4.6		3.4		1.4		0.3		Iris-setosa
5		3.4		1.5		0.2		Iris-setosa
4.4		2.9		1.4		0.2		Iris-setosa
4.9		3.1		1.5		0.1		Iris-setosa
5.4		3.7		1.5		0.2		Iris-setosa
4.8		3.4		1.6		0.2		Iris-setosa
4.8		3		1.4		0.1		Iris-setosa
		9				0.1		V-1

Block diagram

Q6



- One-Hot Encoding
- Data Splitting

- 5-Fold Splitting
- Feature Expansion
- Least-Squares Solution

All Data

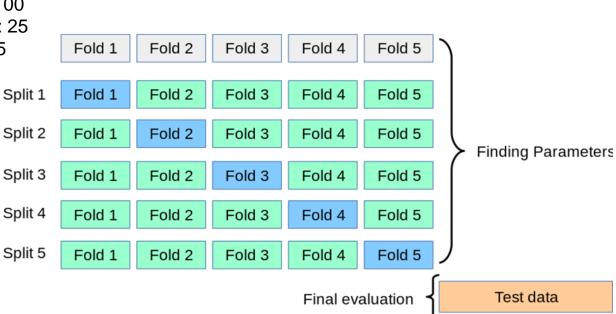
• Train : Validation : Test = 4 : 1 : 1

In total, we have 150 samples.

Number of Training Samples: 100

• Number of Validation Samples: 25

Number of Testing Samples: 25



Training data

https://scikit-learn.org/stable/modules/cross_validation.html

Test data

```
##--- load data from scikit ---##
import numpy as np
import pandas as pd
print("pandas version: {}".format(pd.__version__))
import sklearn
print("scikit-learn version: {}".format(sklearn. version ))
from sklearn.datasets import load iris
                                                    · Loads the Iris dataset, a classic dataset with three classes of flowers (Setosa,
iris dataset = load iris()
                                                       Versicolor, and Virginica).
X = np.array(iris dataset['data'])
                                                    • X: A NumPy array of shape (150, 4), containing four features for each sample.
y = np.array(iris_dataset['target'])
                                                    • y: A NumPy array of shape (150,), representing class labels (0, 1, or 2).
## one-hot encoding
Y = list()
for i in y:

    One-Hot Encoding: The target variable, y, is converted to a one-hot encoding format (Y) for

    letter = [0, 0, 0]
                                       each class (e.g., [1,0,0] for class 0, [0,1,0] for class 1, etc.).
    letter[i] = 1
    Y.append(letter)

    Y is now a NumPy array of shape (150, 3)

Y = np.array(Y)
test Idx = np.random.RandomState(seed=2).permutation(Y.shape[0])
X \text{ test} = X[\text{test } Idx[:25]]
                                      • Uses a fixed seed (2) to create a reproducible random permutation of indices for splitting data.
Y \text{ test} = Y[\text{test } Idx[:25]]

    Selects the first 25 samples for X_test and Y_test, leaving the remaining 125 samples in X and

X = X[\text{test Idx}[25:]]
                                         Y for training and validation.
Y = Y[test Idx[25:]]
```

```
from sklearn.preprocessing import PolynomialFeatures
error_rate_train_array = []
error rate val array = []
                                                       The code performs polynomial classification by expanding
##--- Loop for Polynomial orders 1 to 10 ---##
                                                       features to polynomial forms of varying degrees (1 to 10).
for order in range(1,11):
                                                       For each polynomial order, it uses 5-fold cross-validation:
    error rate train array fold = []
    error rate val array fold = []
    # Random permutation of data
                                                                    Creates a new random permutation of indices
    Idx = np.random.RandomState(seed=8).permutation(Y.shape[0])
                                                                    to assign data for 5-fold cross-validation.
    # Loop 5 times for 5-fold
    for k in range(0,5):
        ##--- Prepare training, validation, and test data for the 5-fold ---#
        # Prepare indexing for each fold
        X \text{ val} = X[Idx[k*25:(k+1)*25]]
                                                          Divides data into training and validation sets for each fold:
        Y \text{ val} = Y[Idx[k*25:(k+1)*25]]

    X val and Y val: Select the next 25 samples for validation.

        Idxtrn = np.setdiff1d(Idx, Idx[k*25:(k+1)*25])

    X_train and Y_train: Exclude the validation indices, using

        X train = X[Idxtrn]
                                                            the remaining samples for training.
        Y train = Y[Idxtrn]
```

```
##--- Polynomial Classification ---##
                   poly = PolynomialFeatures(order)
                   P = poly.fit transform(X train)
                   Pval = poly.fit transform(X val)
                   if P.shape[0] > P.shape[1]: # over-/under-determined cases
                         reg L = 0.00*np.identity(P.shape[1])
 \widehat{\mathbf{w}} = (\mathbf{P}^T \mathbf{P} + \lambda \mathbf{I})^{-1} \mathbf{P}^T \mathbf{y}
                        inv PTP = np.linalg.inv(P.transpose().dot(P)+reg L)
                        pinv L = inv PTP.dot(P.transpose())
                        wp = pinv L.dot(Y train)
                   else:
                         reg_R = 0.00*np.identity(P.shape[0])
                        inv_PPT = np.linalg.inv(P.dot(P.transpose())+reg_R)
\widehat{\mathbf{w}} = \mathbf{P}^T (\mathbf{P} \mathbf{P}^T + \lambda \mathbf{I})^{-1} \mathbf{y}
                         pinv R = P.transpose().dot(inv PPT)
                        wp = pinv_R.dot(Y_train)
```

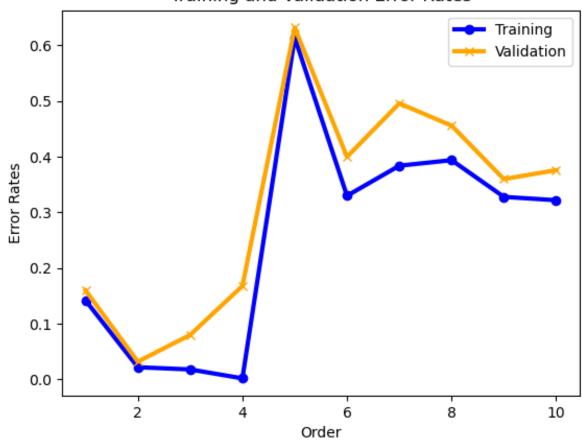
- Creates polynomial features of the specified order for X_train and X_val.
- P and Pval are the transformed features for training and validation, respectively.

- Checks if the system is over- or underdetermined (more rows than columns).
- Adds a small regularization term (reg_L or reg_R) for numerical stability in the pseudoinverse calculation.
- Least-Squares Solution: It calculates weights wp to fit the model by solving a system of equations based on whether the system is overdetermined or underdetermined.

```
##--- trained output ---##
                                       \hat{f}_{\mathbf{w}}(\mathbf{P}(\mathbf{X}_{new})) = \mathbf{P}_{new}\hat{\mathbf{w}}
    y_est_p = P.dot(wp);
    y_{cls_p} = [[1 \text{ if } y == max(x) \text{ else 0 for } y \text{ in } x] \text{ for } x \text{ in } y_{est_p}]
    m1tr = np.matrix(Y train)
    m2tr = np.matrix(y cls p)
    # training classification error count and rate computation
    difference = np.abs(m1tr - m2tr)
    error_train = np.where(difference.any(axis=1))[0]
    error_rate_train = len(error_train)/len(difference)
    error rate train array fold += [error rate train]
    ##--- validation output ---##
    yval est p = Pval.dot(wp);
    yval_cls_p = [[1 if y == max(x) else 0 for y in x] for x in yval_est_p ]
    m1 = np.matrix(Y val)
    m2 = np.matrix(yval cls p)
    # validation classification error count and rate computation
    difference = np.abs(m1 - m2)
    error val = np.where(difference.any(axis=1))[0]
    error rate val = len(error val)/len(difference)
    error_rate_val_array_fold += [error_rate_val]
# store results for each polynomial order
error rate train array += [np.mean(error rate train array fold)]
error_rate_val_array += [np.mean(error_rate_val_array_fold)]
```

- y_est_p: Predicts continuous outputs by applying wp to the training data.
- y_cls_p: Converts y_est_p to a binary onehot format for classification (1 for the maximum value, 0 elsewhere).
- m1tr and m2tr represent the true and predicted one-hot encoded labels as matrices for easy comparison.
- Computes the training error rate by comparing y_cls_p to Y_train, identifying misclassified samples in each fold.
- Applies the same classification process to the validation set.
- Appends the validation error rate for this fold to error_rate_val_array_fo
- Stores the average training and validation error rates across the 5 folds for each polynomiaborder.

Training and Validation Error Rates



THANK YOU