

EE2211 Pre-Tutorial 7

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Agenda

- Recap
- Self-learning
- Tutorial 7

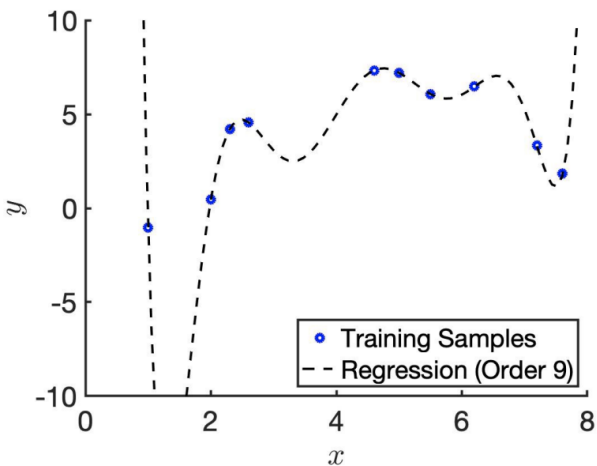
Recap

- Overfitting, underfitting & model complexity
 - Overfitting: low error in training set, high error in test set
 - Underfitting: high error in both training & test sets
 - Overly complex models can overfit; Overly simple models can underfit
- Feature selection
 - Extract useful features from training set
- Regularization (e.g., L2 regularization)
 - Solve “ill-posed” problem (e.g., more unknowns than data points)
 - Reduce overfitting
- Bias-Variance Decomposition Theorem
 - Test error = Bias Squared + Variance + Irreducible Noise
 - Can be interpreted as trading off bias & variance:
 - Overly complex models can have high variance, low bias
 - Overly simple models can have low variance, high bias

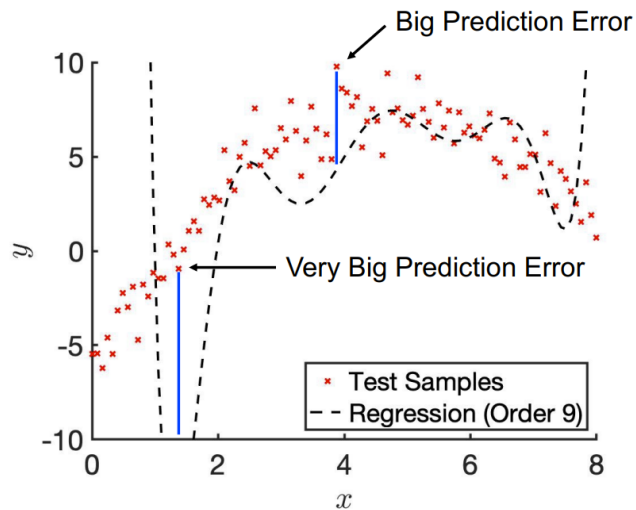
Overfitting

Training

Overfitting Example



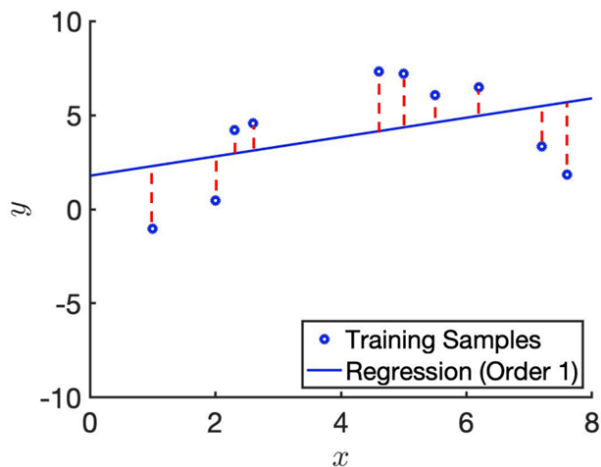
Overfitting Example



Underfitting

Training

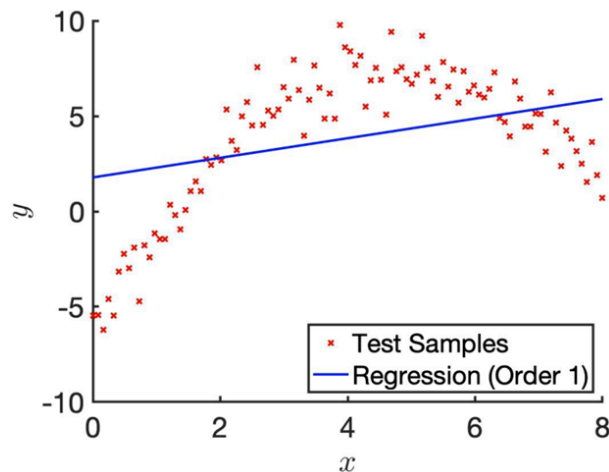
Underfitting Example



	Training Set Fit	Test Set Fit
Order 9	Good	Bad
Order 1	Bad	

Testing

Underfitting Example

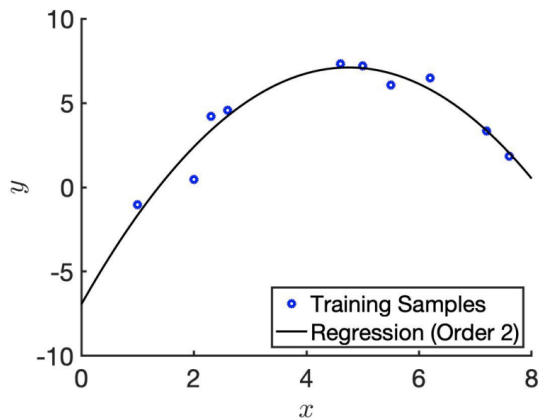


	Training Set Fit	Test Set Fit
Order 9	Good	Bad
Order 1	Bad	Bad

Perfect Fitting

Training

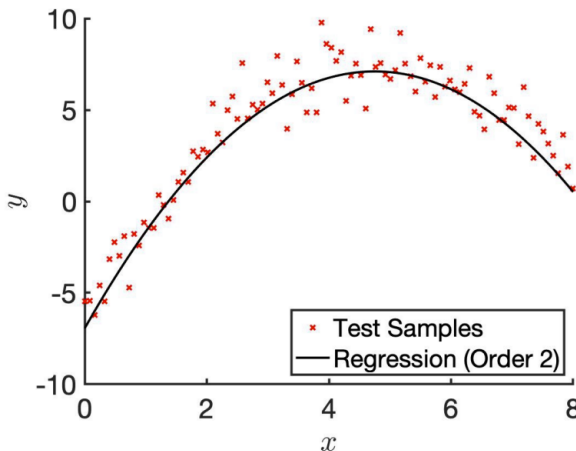
“Just Nice”



	Training Set Fit	Test Set Fit
Order 9	Good	Bad
Order 1	Bad	Bad
Order 2	Good	

Testing

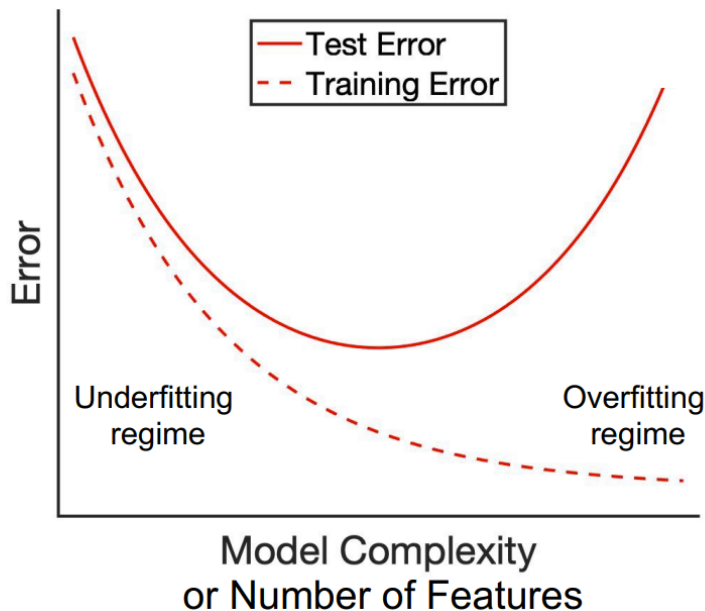
“Just Nice”



	Training Set Fit	Test Set Fit
Order 9	Good	Bad
Order 1	Bad	Bad
Order 2	Good	Good

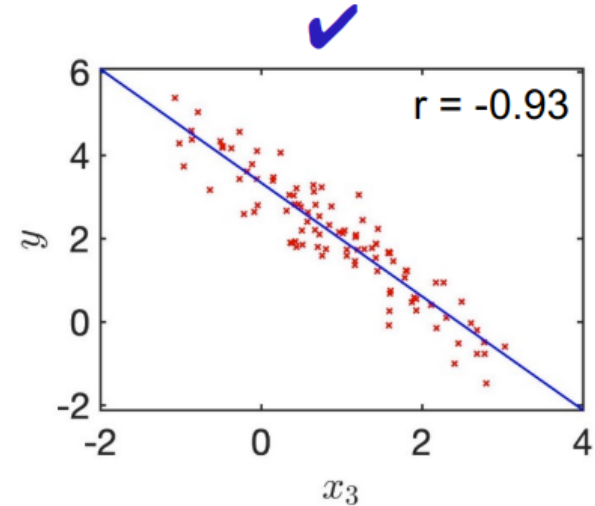
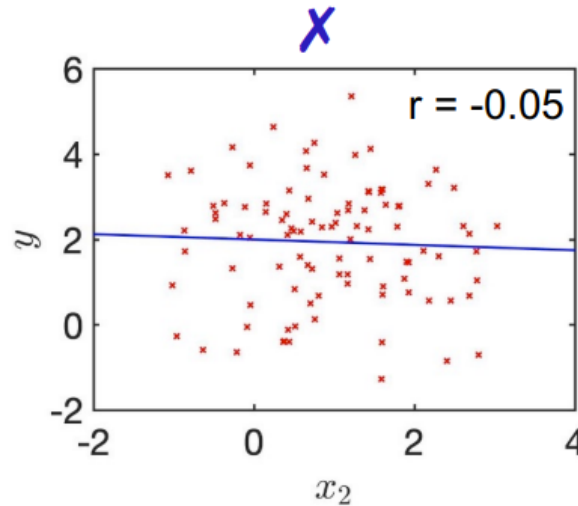
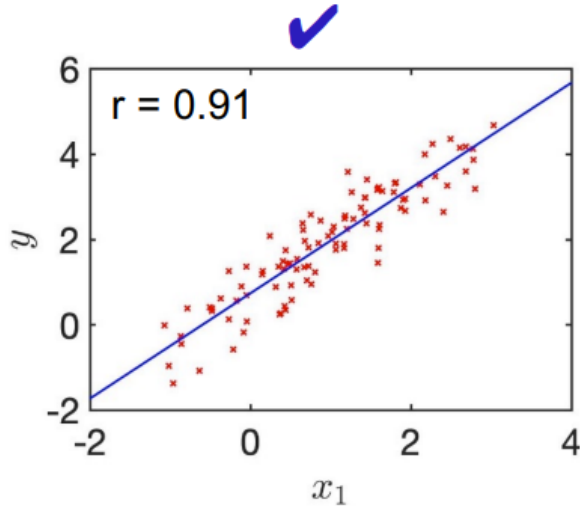
Fitting VS Model Complexity

Overfitting / Underfitting Schematic



Pearson's R

- Pearson's correlation r measures linear relationship between two variables

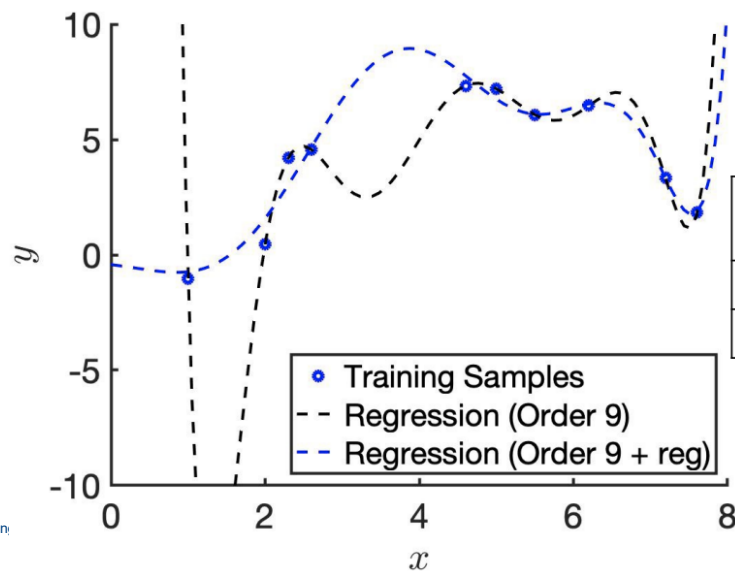


Regularization

$$\underset{\mathbf{w}}{\operatorname{argmin}} (\mathbf{P}\mathbf{w} - \mathbf{y})^T (\mathbf{P}\mathbf{w} - \mathbf{y}) + \lambda \mathbf{w}^T \mathbf{w}$$

Cost function quantifying data
fitting error in training set

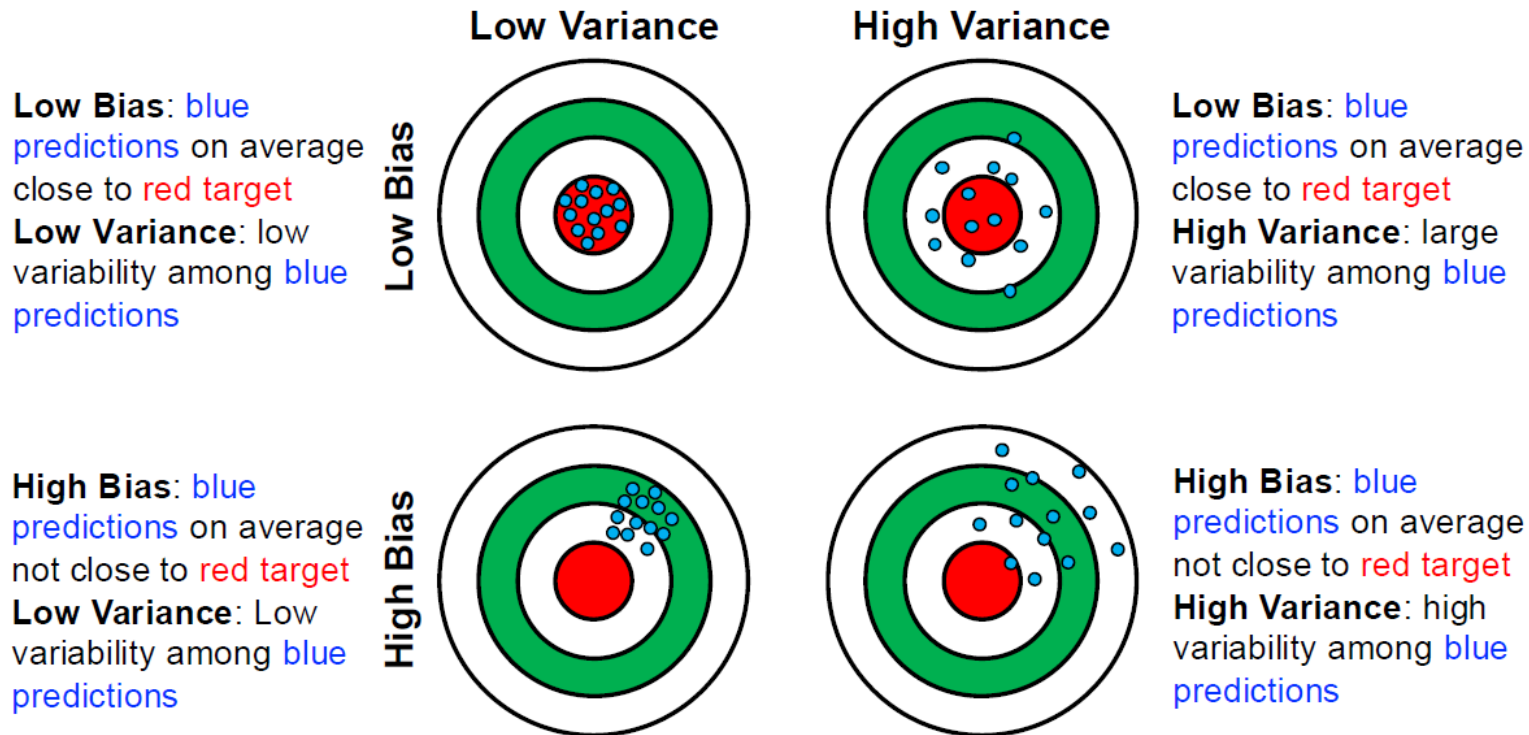
Regularization



	Training Set Fit	Test Set Fit
Order 9	Good	Bad
Order 9, $\lambda = 1$	Good	

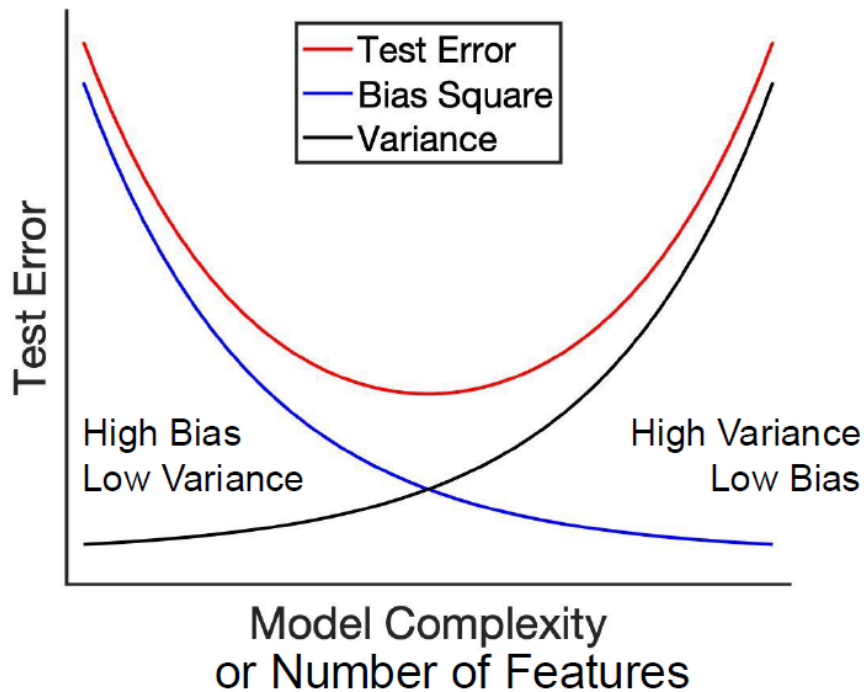
Bias vs Variance

- Suppose we are trying to predict **red target** below:



Bias + Variance Trade Off

- Test error = Bias Squared + Variance + Irreducible Noise



Bias-Variance Decomposition Theorem

- **Test error** = Bias Squared + Variance + Irreducible Noise
 - Mathematical details in optional uploaded material (won't be tested)
- **“Variance”** refers to variability of prediction models across different training sets
 - In previous example, every time the training set of 10 samples changes, the trained model changes
 - “Variance” quantifies variability across trained models
- **“Bias”** refers to how well an average prediction model will perform
 - In previous example, every time the training set of 10 samples changes, the trained model changes
 - If we average the trained models, how well will this average trained model perform?
- **“Irreducible Noise”** reflects the fact that even if we are perfect modelers, it might not be possible to predict target y with 100% accuracy from feature(s) x



THANK YOU