

CISP 440

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Homework 0 -

Positional Number Systems

## COMMON BASES

**1. 1234 decimal to binary: 0100 1101 0010**

$1234 \% 2 = 0$	$1234 / 2 = 617$
$617 \% 2 = 1$	$617 / 2 = 308$
$308 \% 2 = 0$	$308 / 2 = 154$
$154 \% 2 = 0$	$154 / 2 = 77$
$77 \% 2 = 1$	$77 / 2 = 38$
$38 / 2 = 0$	$38 / 2 = 19$
$19 \% 2 = 1$	$19 / 2 = 9$
$9 \% 2 = 1$	$9 / 2 = 4$
$4 \% 2 = 0$	$4 / 2 = 2$
$2 \% 2 = 0$	$2 / 2 = 1$
$1 \% 2 = 1$	$1 / 2 = 0$

**2. ABBA base 16 to decimal: 43,962**

A = 10	B = 11
$A * 16^3 + B * 16^2 + B * 16^1 + A * 16^0$	
$10 * 4096 + 11 * 256 + 11 * 16 + 10$	
43962	

**3. 1234 base 10 to hex: 4D2**

$1234 \% 16 = 2$	$1234 / 16 = 77$
$77 \% 16 = 13$	$77 / 16 = 4$
$4 \% 16 = 4$	$4 / 16 = 0$

**4. 1100 0001 binary to octal : 301**

$1 * 2^7 + 1 * 2^6 + 1 * 2^0$	
$1 * 128 + 1 * 64 + 1$	
193 in decimal	
$193 \% 8 = 1$	$193 / 8 = 24$
$24 \% 8 = 0$	$24 / 8 = 3$
$3 \% 8 = 3$	$3 / 8 = 0$

**5. 011 000 001 decimal to octal: 51 754 301**

$11,000,001 \% 8 = 1$	$11,000,001 / 8 = 1375000$
$1,375,000 \% 8 = 0$	$1,357,000 / 8 = 171875$
$171,875 \% 8 = 3$	$171,875 / 8 = 21484$
$21,484 \% 8 = 4$	$21,484 / 8 = 2685$
$2,685 \% 8 = 5$	$2,685 / 8 = 335$
$335 \% 8 = 7$	$335 / 8 = 41$
$41 \% 8 = 1$	$41 / 8 = 5$
$5 \% 8 = 5$	$5 / 8 = 0$

**6. 1234 octal to decimal: 668**

$$1 * 8^3 + 2 * 8^2 + 3 * 8^1 + 4 * 8^0$$

$$1 * 512 + 2 * 64 + 3 * 8 + 4 * 1$$

668

**7. 1234 octal to hex: 29C**

1234 octal is 668 decimal from problem 5

$668 \% 16 = \mathbf{12}$	$668 / 16 = 41$
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$41 \% 16 = \mathbf{9}$	$41 / 16 = 2$
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$2 \% 16 = \mathbf{2}$	$2 / 16 = 0$
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**8. 1234 octal to binary: 10 1001 1100**

1234 octal is 668 decimal from problem 5

$668 \% 2 = \mathbf{0}$	$668 / 2 = 334$
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$334 \% 2 = \mathbf{0}$	$334 / 2 = 167$
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$167 \% 2 = \mathbf{1}$	$167 / 2 = 83$
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$83 \% 2 = \mathbf{1}$	$83 / 2 = 41$
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$41 \% 2 = \mathbf{1}$	$41 / 2 = 20$
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$20 \% 2 = \mathbf{0}$	$20 / 2 = 10$
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$10 \% 2 = \mathbf{0}$	$10 / 2 = 5$
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$5 \% 2 = \mathbf{1}$	$5 / 2 = 2$
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$2 \% 2 = \mathbf{0}$	$2 / 2 = 1$
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$1 \% 2 = \mathbf{1}$	$1 / 2 = 0$
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## OTHER BASES

<b>9. 1234 base 10 to base 16: 4D2</b>	
$1234 \% 16 = \mathbf{2}$	$1234 / 16 = 77$
$77 \% 16 = \mathbf{13}$	$77 / 16 = 4$
$4 \% 16 = \mathbf{4}$	$4 / 16 = 0$
13 maps to D	

<b>10. 1234 base 16 to base 10: 4,660</b>	
$1 * 16^3 + 2 * 16^2 + 3 * 16^1 + 4 * 16^0$	
$1 * 4096 + 2 * 256 + 3 * 16 + 4 * 1$	
4660	

<b>11. 4567 base 10 to base 5: 121232</b>	
$4567 \% 5 = \mathbf{2}$	$4567 / 5 = 913$
$913 \% 5 = \mathbf{3}$	$913 / 5 = 182$
$182 \% 5 = \mathbf{2}$	$182 / 5 = 36$
$36 \% 5 = \mathbf{1}$	$36 / 5 = 7$
$7 \% 5 = \mathbf{2}$	$7 / 5 = 1$
$1 \% 5 = \mathbf{1}$	$1 / 5 = 0$

<b>12. 1234 base 5 to base 10: 194</b>	
$1 * 5^3 + 2 * 5^2 + 3 * 5^1 + 4 * 5^0$	
$1 * 125 + 2 * 25 + 3 * 5 + 4 * 1$	
194	

<b>13. 1234 base 7 to base 9: 567</b>	
$1 * 7^3 + 2 * 7^2 + 3 * 7^1 + 4 * 7^0$	
$1 * 343 + 2 * 49 + 3 * 7 + 4 * 1$	
466 in base 10	
$466 \% 9 = \mathbf{7}$	$466 / 9 = 51$
$51 \% 9 = \mathbf{6}$	$51 / 9 = 5$
$5 \% 9 = \mathbf{5}$	$5 / 9 = 0$

<b>14. 4567 base 10 to base 24 : 7L7</b>	
$4567 \% 24 = \mathbf{7}$	$4537 / 24 = 189$
$189 \% 24 = \mathbf{21}$	$189 / 24 = 7$
$7 \% 24 = \mathbf{7}$	$7 / 24 = 0$
21 maps to L	

<b>15. 4567 base 24 to base 2: 0110 1011 1101 0111</b>	
$4 * 24^3 + 5 * 24^2 + 6 * 24^1 + 7 * 24^0$	
$4 * 13824 + 5 * 576 + 6 * 24 + 7 * 1$	
58327 in decimal	
$58327 \% 2 = \mathbf{1}$	$58327 / 2 = 29163$
$29163 \% 2 = \mathbf{1}$	$29163 / 2 = 14581$
$14581 \% 2 = \mathbf{1}$	$14581 / 2 = 7290$
$7290 \% 2 = \mathbf{0}$	$7290 / 2 = 3645$
$3545 \% 2 = \mathbf{1}$	$3545 / 2 = 1822$
$1822 \% 2 = \mathbf{0}$	$1822 / 2 = 911$
$911 \% 2 = \mathbf{1}$	$911 / 2 = 455$
$455 \% 2 = \mathbf{1}$	$455 / 2 = 227$
$227 \% 2 = \mathbf{1}$	$227 / 2 = 113$
$113 \% 2 = \mathbf{1}$	$113 / 2 = 26$
$26 \% 2 = \mathbf{0}$	$26 / 2 = 13$
$13 \% 2 = \mathbf{1}$	$13 / 2 = 6$
$6 \% 2 = \mathbf{0}$	$6 / 2 = 3$
$3 \% 2 = \mathbf{1}$	$3 / 2 = 1$
$1 \% 2 = \mathbf{1}$	$1 / 2 = 0$

<b>16. FIVE base 36 to base 19: 58D8G</b>	
$F = 15 \ I = 18 \ V = 31 \ E = 14$	
$F * 36^3 + I * 36^2 + V * 36^1 + E * 36^0$	
$15 * 46656 + 18 * 576 + 31 * 36 + 14 * 1$	
711338 in decimal	
$711338 \% 19 = \mathbf{16}$	$711338 / 19 = 37438$
$37438 \% 19 = \mathbf{8}$	$37438 / 19 = 1970$
$1970 \% 19 = \mathbf{13}$	$1970 / 19 = 103$
$103 \% 19 = \mathbf{8}$	$103 / 19 = 5$
$5 \% 19 = \mathbf{5}$	$5 / 19 = 0$
$16 = G \ 13 = D$	

<b>17. THREE base 28 to base 10</b>
T would map to 29, which is out of bounds for base 28

<b>18. 1234 base 10 to base 36: YA</b>	
$1234 \% 36 = \mathbf{10}$	$1234 / 36 = 34$
$34 \% 36 = \mathbf{34}$	$34 / 36 = 0$
$34 = Y \ 10 = A$	

## ADDITION IN OTHER BASES

**19.** Add  $1234_5$  plus  $4321_5 = 11110_5$

1	1	1	1	0
	1	2	3	4
+	4	3	2	1
<b>1</b>	<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>

**20.** Add  $KETCHUP_{30}$  plus  $FRIES_{30} = KFFA6FN_{30}$

K	E	T	C	H	U	P
20	14	29	12	17	30	25
		F	R	I	E	S
		15	27	18	14	28
0	1	1	1	1	1	
20	14	29	12	17	30	25
+		15	27	18	14	28
20	15	15	10	6	15	23
<b>K</b>	<b>F</b>	<b>F</b>	<b>A</b>	<b>6</b>	<b>F</b>	<b>N</b>

**21.** Add  $FOUR_{36}$  plus  $TWO_{36} = GIRF_{36}$

F	O	U	R
15	24	30	27
	T	W	O
	29	32	24
1	1	1	
15	24	30	27
+	29	32	24
16	18	27	15
<b>G</b>	<b>I</b>	<b>R</b>	<b>F</b>

# DNA

<b>22. ACT to base 10: 33</b>
$A = 2 \ C = 0 \ T = 1$
$A * 4^2 + C * 4^1 + T * 4^0$
$2 * 16 + 0 * 4 + 1 * 1$
33

<b>23. ATTGCA to base 10: 2418</b>
$A = 2 \ T = 1 \ G = 3 \ C = 0$
$A * 4^5 + T * 4^4 + G * 4^3 + C * 4^2 + A * 4^1 + T * 4^0$
$2 * 1024 + 1 * 256 + 1 * 64 + 3 * 16 + 0 * 4 + 2 * 1$
2418

<b>24. TTAA to base 10: 90</b>
$T = 1 \ A = 2$
$T * 4^3 + T * 4^2 + A * 4^1 + A * 4^0$
$1 * 64 + 1 * 16 + 2 * 4 + 2 * 1$
90

<b>25. 1234 base 10 to DNA format: TCGTCA</b>	
$1234 \% 4 = 2$	$1234 / 4 = 308$
$308 \% 4 = 0$	$308 / 4 = 77$
$77 \% 4 = 1$	$77 / 4 = 19$
$19 \% 4 = 3$	$19 / 4 = 4$
$4 \% 4 = 0$	$4 / 4 = 1$
$1 \% 4 = 1$	$1 / 4 = 0$
1 = T 0 = C 3 = G 1 = T 0 = C 2 = A	

<b>26. 20 base ten to DNA format: TTC</b>	
$20 \% 4 = 0$	$20 / 4 = 5$
$5 \% 4 = 1$	$5 / 4 = 1$
$1 \% 4 = 1$	$1 / 4 = 0$

<b>27. Alanine = GCC convert to base 10: 48</b>	
$G = 3 \ C = 0$	
$G * 4^2 + C * 4^1 + C * 4^0$	
$3 * 16 + 0 * 4 + 0 * 1$	
48	

28. Explain how to group a binary string (1's and 0's) so that it can more easily be converted to DNA format. Give an example.

Groups of two would be best. C = 0 = 00    T = 1 = 01    A = 2 = 10    G = 3 = 11  
ACT = 10 00 01

## COLORS

<b>29. 1234 decimal to color code: TACCACT</b>	
$1234 \% 3 = \mathbf{1}$	$1234 / 3 = 411$
$411 \% 3 = \mathbf{0}$	$411 / 3 = 137$
$137 \% 3 = \mathbf{2}$	$137 / 3 = 45$
$45 \% 3 = \mathbf{0}$	$45 / 3 = 15$
$15 \% 3 = \mathbf{0}$	$15 / 3 = 5$
$5 \% 3 = \mathbf{2}$	$5 / 3 = 1$
$1 \% 3 = \mathbf{1}$	$1 / 3 = 0$
0 = C 1 = T 2 = A	

**30. Figure out and explain some way that yellow could be represented in this color code?**

Yellow could be represented by blue plus green, which sums to 10

Blue = 1 Green = 2

	1	0
		1
+		2
	<b>1</b>	<b>0</b>

**31. What is your favorite color, in this color code? There are no wrong answers to this one!**

My favorite color is blue, so the color code would be 1.