

Aerospace Vehicle Design And System Integration 3

CADE30007

(AVDASI 3 - Aircraft Propulsion, Performance and Sustainable Operations)

# Aircraft Performance

## Lecture 2

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# Overview



Performance in climb, cruise  
and descent



Useful parameters

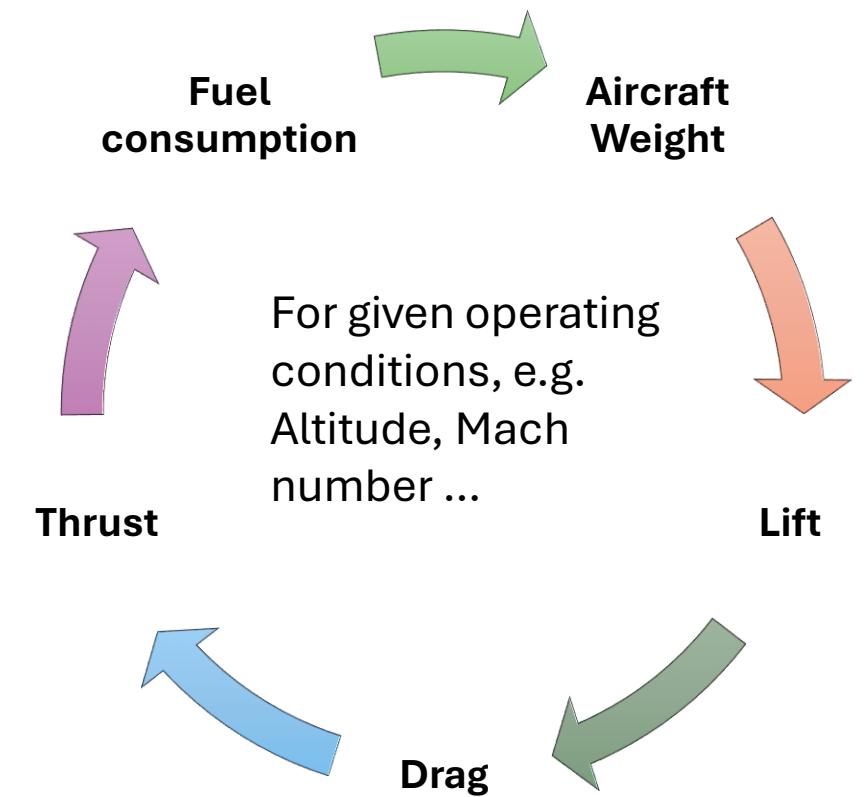
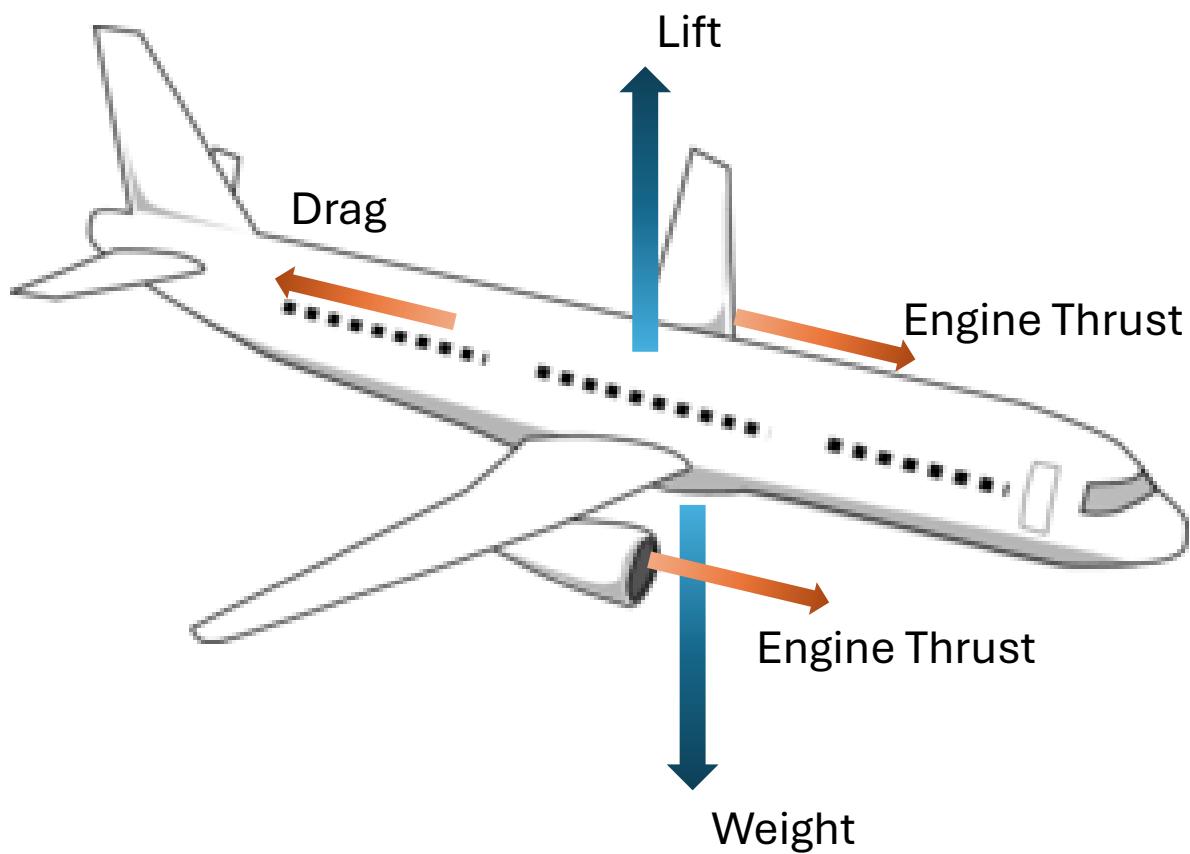


Fixed Wing Performance Tool



# Performance of Civil Airliners

# A Simplistic View of Performance Model



# Data required for an Aircraft Performance Calculation



## Mission Definition

Operating conditions  
Required range  
Take off and landing requirements



## Mass

Payload  
Fuel Load  
Operators Mass Empty  
Maximum Take-off Mass



## Drag Data

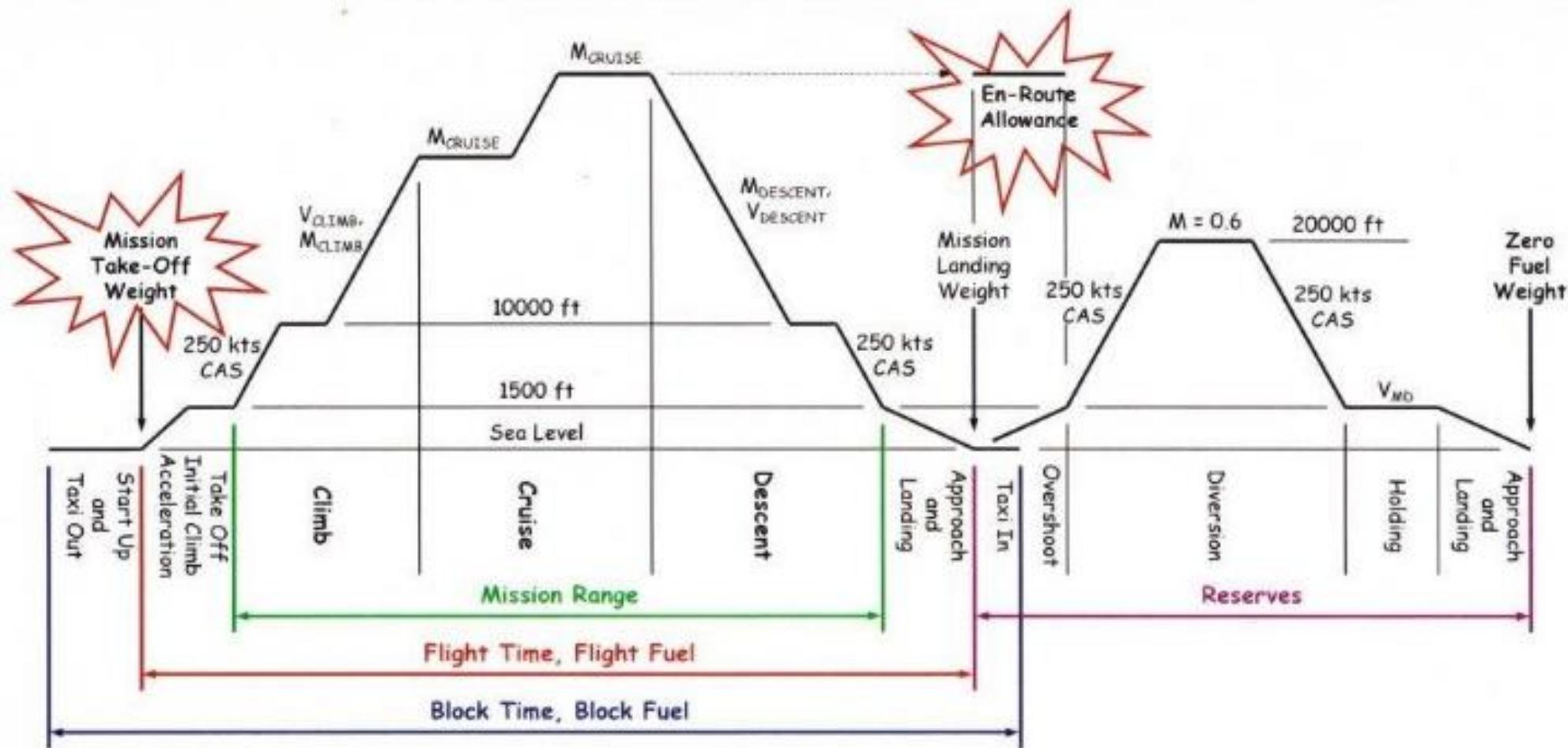
Zero Lift Drag  
Induced Drag  
“Wave Drag”  
Drag due to Reynolds Number

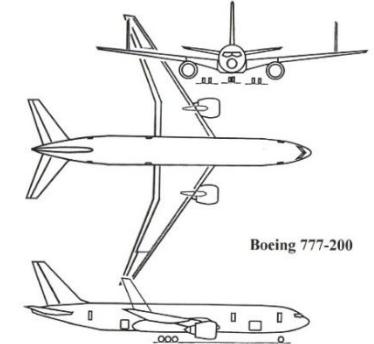


## Engine Data

Thrust & Fuel Flow across the Flight Envelope

# Typical Mission Profile for a Civil Airliner





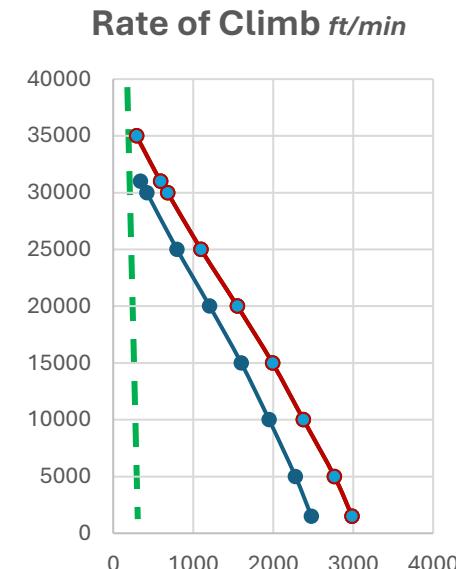
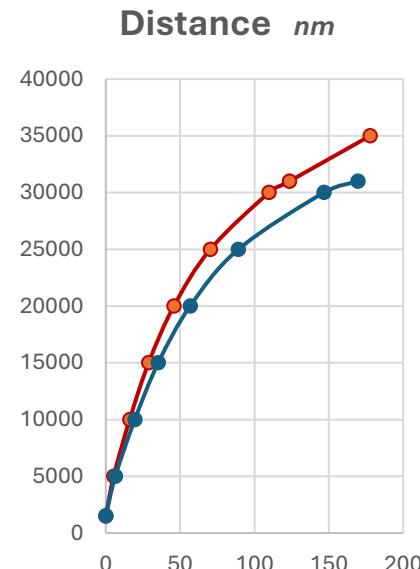
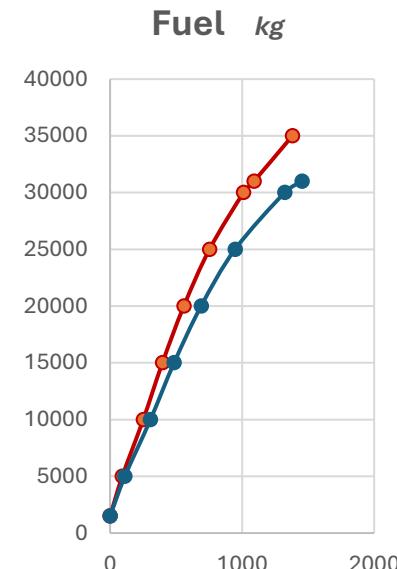
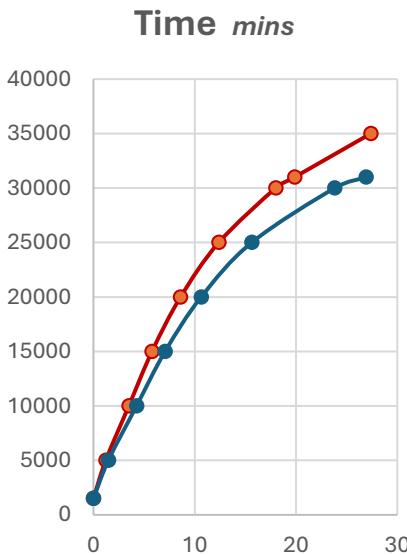
# Critical Sizing Conditions

## *Subsonic Transport Aircraft*

Fuselage	<ul style="list-style-type: none"> <li>• Payload</li> </ul>
Wing Area	<ul style="list-style-type: none"> <li>• Cruise Mach Number dependent on Range hence Wing Sweep.</li> <li>• Lift Coefficient at Top of Climb &amp; for Cruise</li> <li>• Aspect ratio for minimising Drag.</li> <li>• Lift Coefficient, with flaps for Take-off &amp; Landing (Approach Speed)</li> <li>• Sufficient Volume in wing for fuel.</li> </ul>
Control Surfaces	<ul style="list-style-type: none"> <li>• Balance, Engine out, Control (longitudinal &amp; lateral) etc.</li> </ul>
Engine	<ul style="list-style-type: none"> <li>• <b>Take-off</b> <ul style="list-style-type: none"> <li>• Sufficient thrust to meet take-off distance.</li> </ul> </li> <li>• <b>Climb</b> <ul style="list-style-type: none"> <li>• Sufficient thrust to give the aircraft a time to climb to at cruise altitude with a residual rate of climb of at least 300 ft/min.</li> </ul> </li> <li>• <b>Cruise</b> <ul style="list-style-type: none"> <li>• Sufficient thrust to sustain the cruise Mach Number following at take-off at Max Mass.</li> </ul> </li> <li>• <b>En-route clearance</b> <ul style="list-style-type: none"> <li>• Sufficient thrust to allow the aircraft to maintain altitude with an engine failed</li> </ul> </li> </ul>

# Climb Performance

**Climb Profile: 250/280 CAS / M = 0.76**



Key: — Take off Max ToM

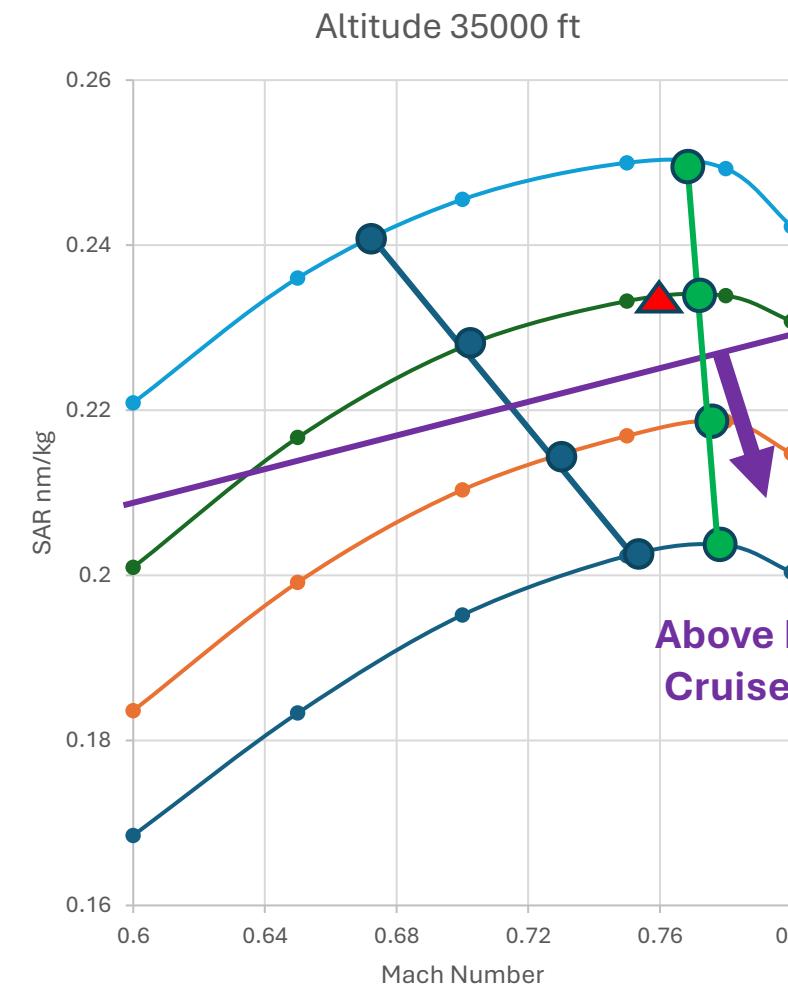
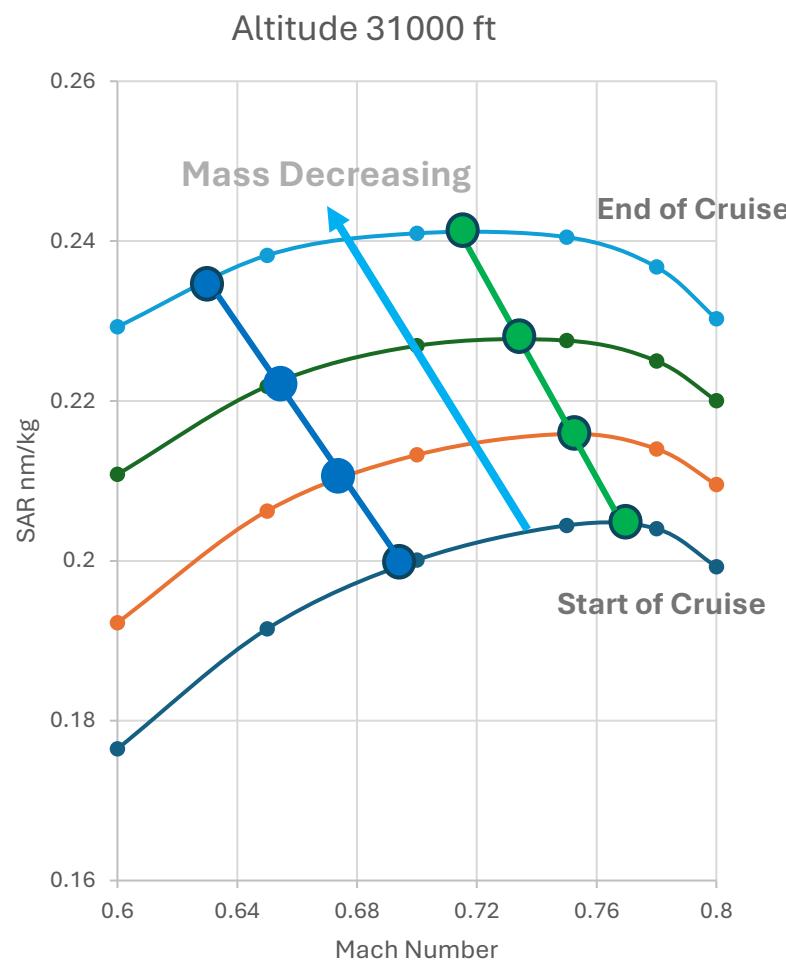
— Take off Reduced ToM (for half range)

- - - 300 ft/min Rate of Climb

**A useful empirical rule is that the top of climb Mach Number to be 0.02M less than the Cruise Mach Number**

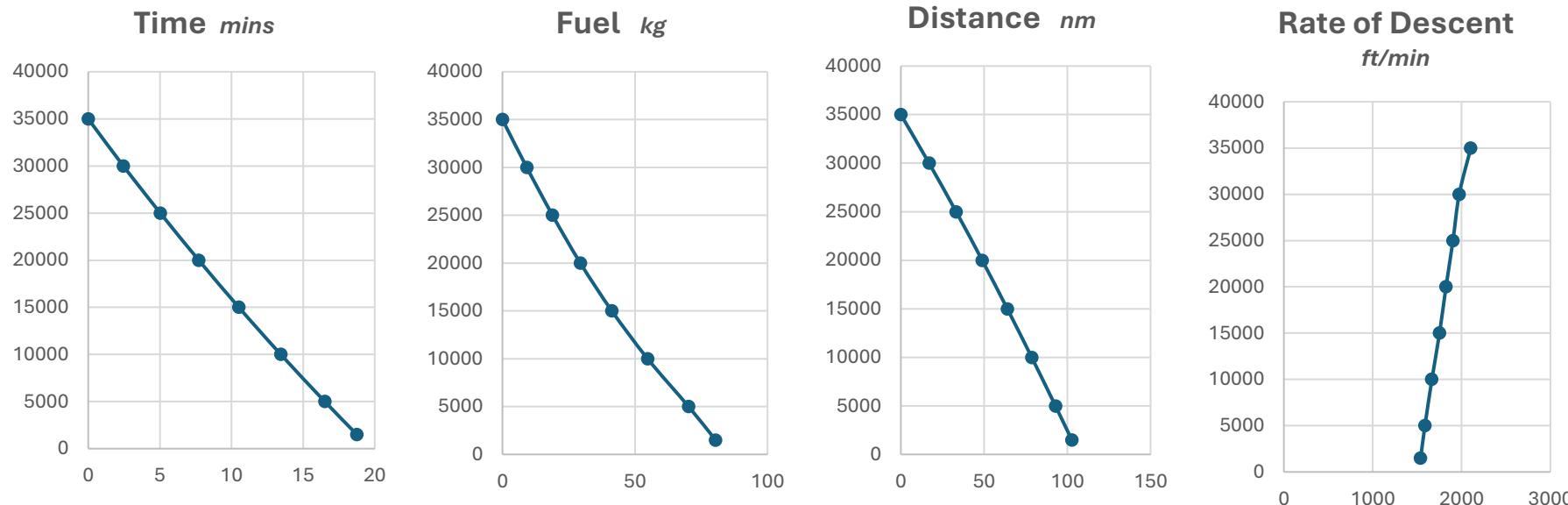
# Cruise Performance

## *Specific Air Range Plots*



Key: — Minimum Drag    — Maximum Specific Air Range    — Maximum Cruise Thrust    ▲ 300 ft/min Climb Thrust

# Descent Performance



Key: Descent Speed Profile 250 knots CAS Mass at end of cruise  
Cabin Altitude 8000 ft. The maximum rate of change of pressure in the Cabin must not exceed 300 ft/min. Hence Descent Time to 1500 ft should be > 22 mins.

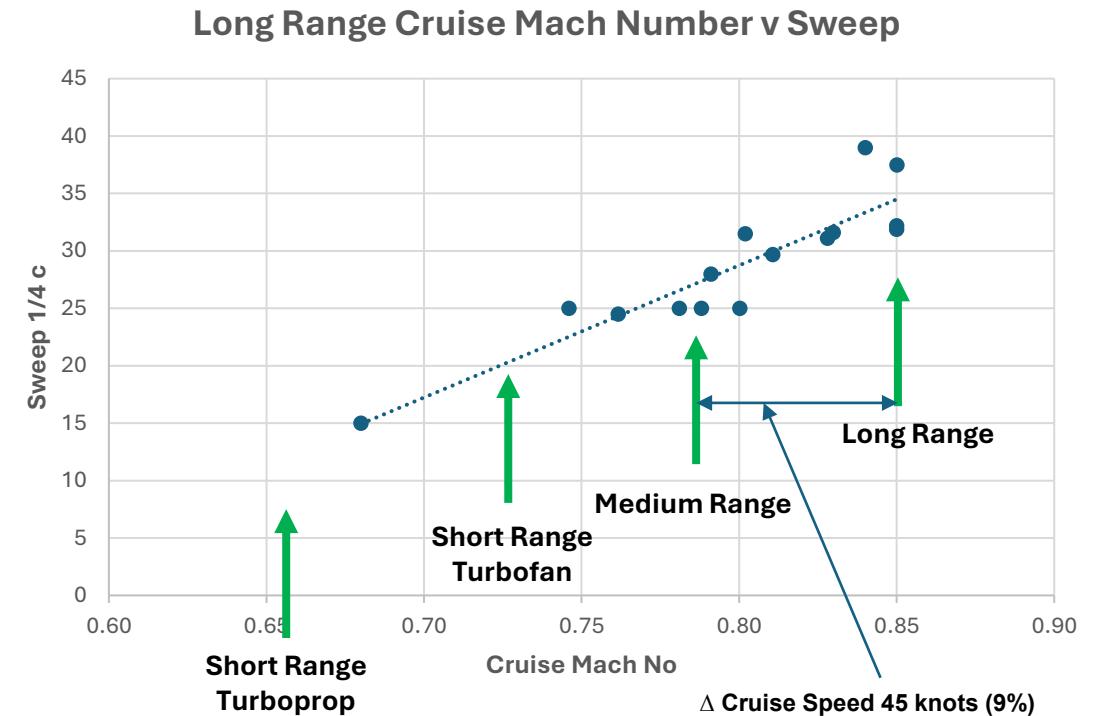
# Cruise Speed & Initial Cruise Altitude

The Airline Specification defines Cruise Speed & Initial Cruise Altitude (ICA):

- **Long Range Aircraft Twin Aisle (250 – 500 + seats) Range 5000 nm +**
  - *Long Range Cruise Speed  $M = 0.83 - 0.85$  ICA at least 35,000 ft*
- **Medium Range Single Aisle (150 - 250 seats) Range 3000 nm**
  - *Long Range Cruise Speed  $M = 0.76 - 0.80$ , ICA at least 35,000 ft*
- **Short Range Turbofan Single Aisle (70 – 150 seats) Range 1500 nm**
  - *Cruise Speed  $M = 0.7 - 0.76$  ICA at least 31,000 ft*
- **Short Range Turboprop Single Aisle (50 – 150 seats) Range 1200 nm**
  - *Cruise Speed  $0.5 - 0.7$ , ICA at least 25,000 ft*

# Wing Loading & Wing Sweep

- Wing loadings (at take-off mass) for a new design in the range 600–650 + kg / m<sup>2</sup> – derivative versions may be higher.
- Set by cruise performance & take-off & landing and type of flap system.
- Wing sweep largely set by cruise speed:



*Note: the higher the sweep the better the fuel burn at high Mach Numbers, at the expense of wing weight & low speed & take off performance.*

*Tendency for:*

*Long range – large airfields & long runways.*

*Short range small airfields & short runways.*

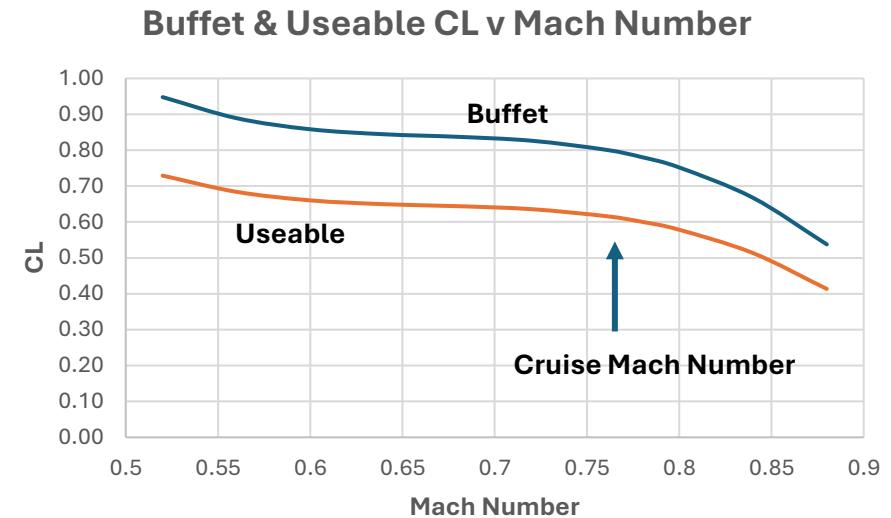
# Cruise Speed & Lift Co-efficient

➤ At typical start of cruise conditions:

- Altitude 35,000 ft
- Cruise Mach Number
- Mass 97% of take-off mass)

➤  $C_L$  needs to be within buffet boundary\*

\* *beginnings of wing stall*



**Example:**

Take-off Wing Loading  $640 \text{ kg/m}^2$

Cruise Mach Number = 0.78

$CL$  at 35000 ft:

Factor  $C_{L\text{Buff}} / C_{L\text{useable}} = 1.3$

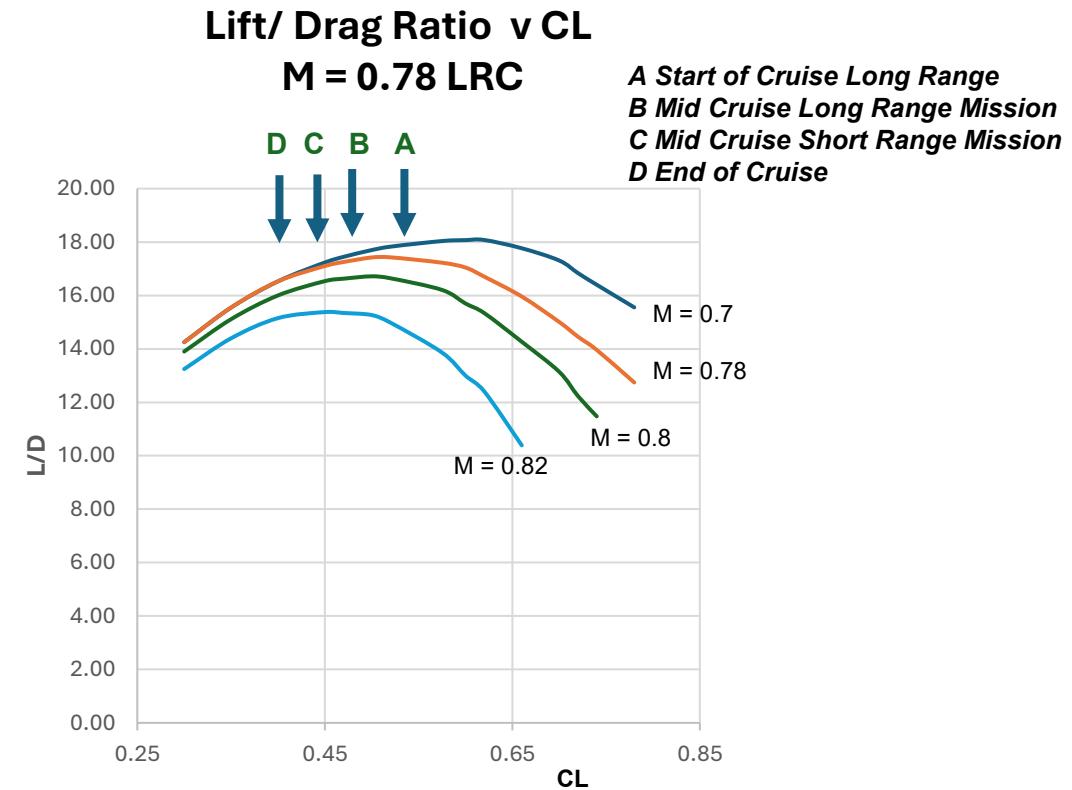
Buffet = 0.78

**Useable = 0.6**

# Drag Characteristics

$$C_{DTot} = C_{Do} + K C_L^2 + \Delta C_{Dw} + \Delta C_{DRe}$$

- $C_{DTot}$  = Total Drag Co-efficient
- $C_{Do}$  = Zero Lift Drag at a Reference Reynolds Number
- $K$  = Induced Drag Factor
- $C_L$  = Lift Coefficient
- $\Delta C_{Dw}$  = Increment in drag due to shock wave effects a function of  $C_L$  & Mach Number
- $\Delta C_{DRe}$  = Increment in Drag due to difference in  $R_e$  from Reference  $R_e$  ~ (can be ignored in these studies)

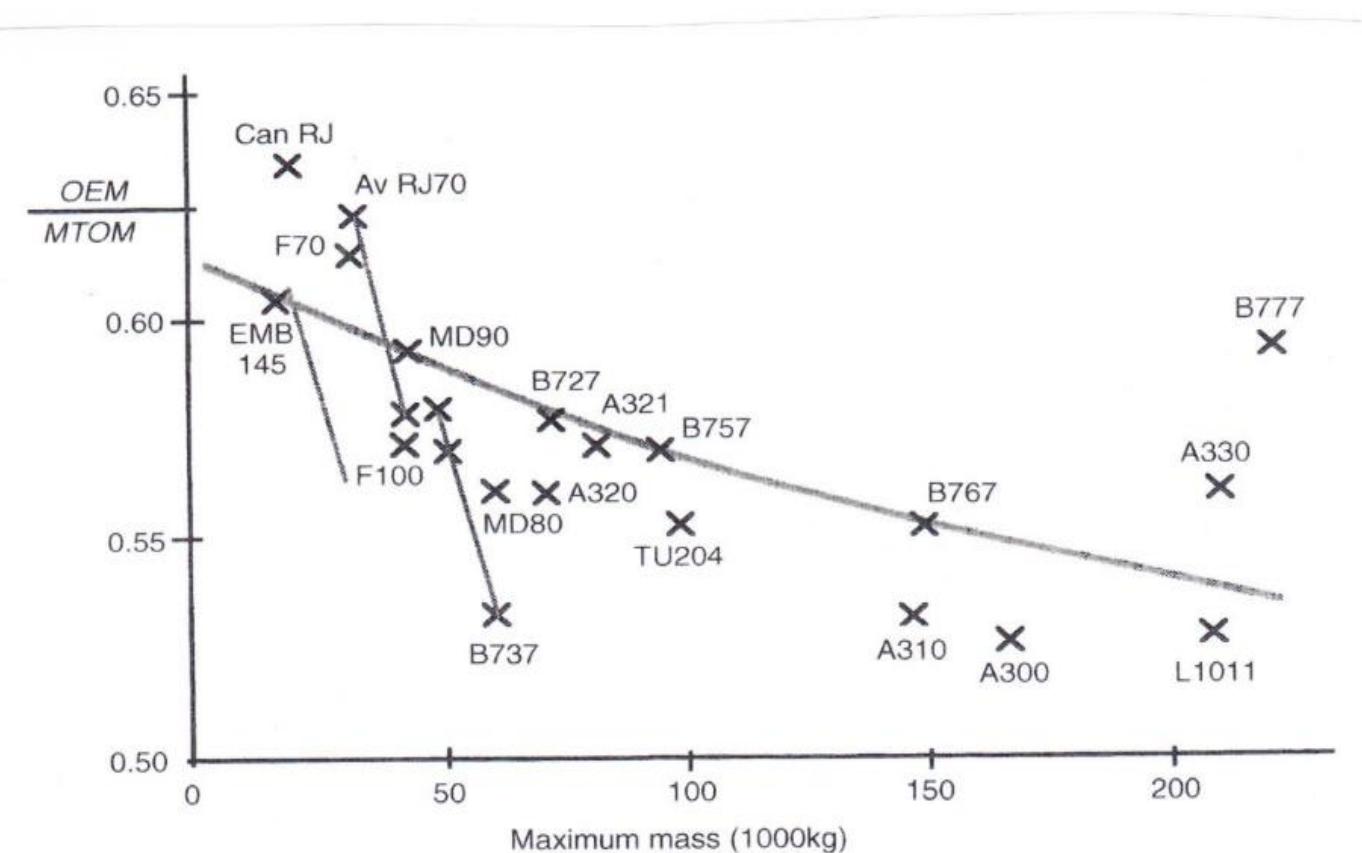


Note: with a take off wing loading in the range 600 - 650 kg/m<sup>2</sup>, the range of CL's (clean) that the aircraft will experience are in the range 0.3 to 0.6. For a modern wing, the max operating  $C_L$  to avoid buffet at the Long Range Cruise Mach Number will be of the order of 0.6.

# Some Useful Numbers

For a “conventional” Turbo-Fan powered Airliner  
there are a number of key parameters

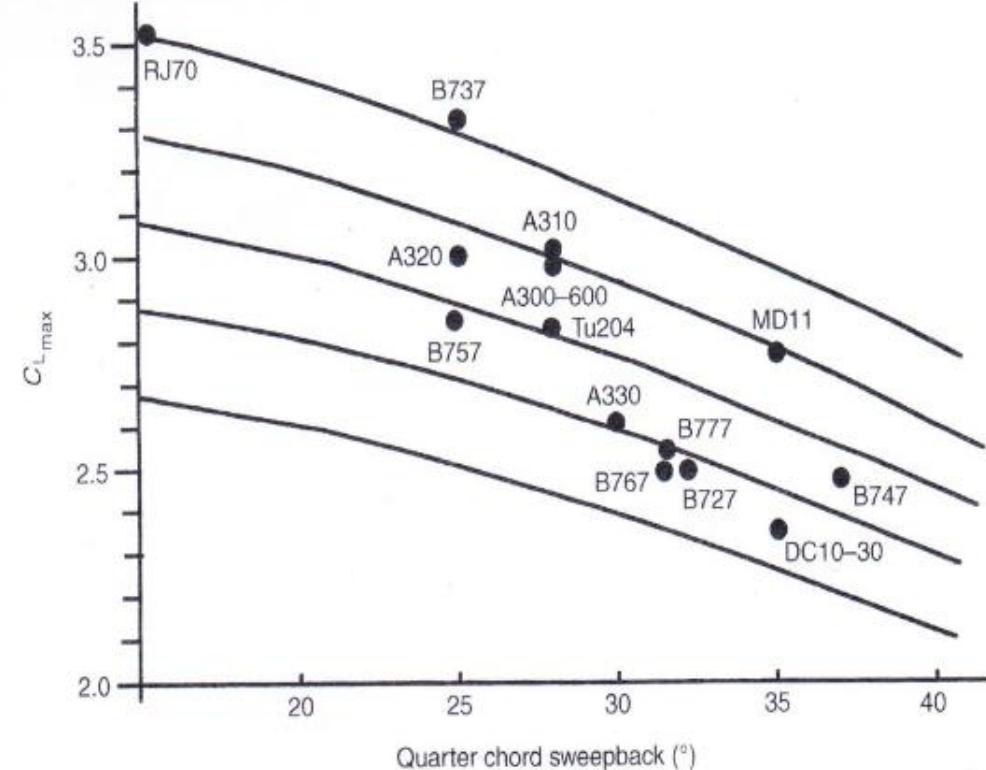
- Wing Loading:
  - 600 kg/m<sup>2</sup> (initial variant)
- Thrust/Weight Ratio
  - Four Engines ~ 0.25
  - Three Engines ~ 0.27
  - Two Engines ~ 0.3
- Empty Mass Fraction:
  - 0.53 to 0.57
- Cruise Mach Number:
  - 0.78 (medium range) to 0.84+ (long range)



# Some Useful Numbers

For a “conventional” Turbo-Fan powered Airliner  
there are a number of key parameters

- Quarter Chord Sweep
  - $25^\circ$  (medium range) :  $30^\circ+$  (long range)
- Aspect ratio
  - 9 to 11
- Lift Coefficient at start of Cruise
  - $C_L \sim 0.6$
- Lift/Drag Ratio
  - 18 (medium range) : 20+ (long range)
- Initial Cruise Altitude
  - 35,000 ft
- $C_{L\text{Max}}$  at for Take-off & Landing
  - 2.5 to 3.5



## Typical Drag Values

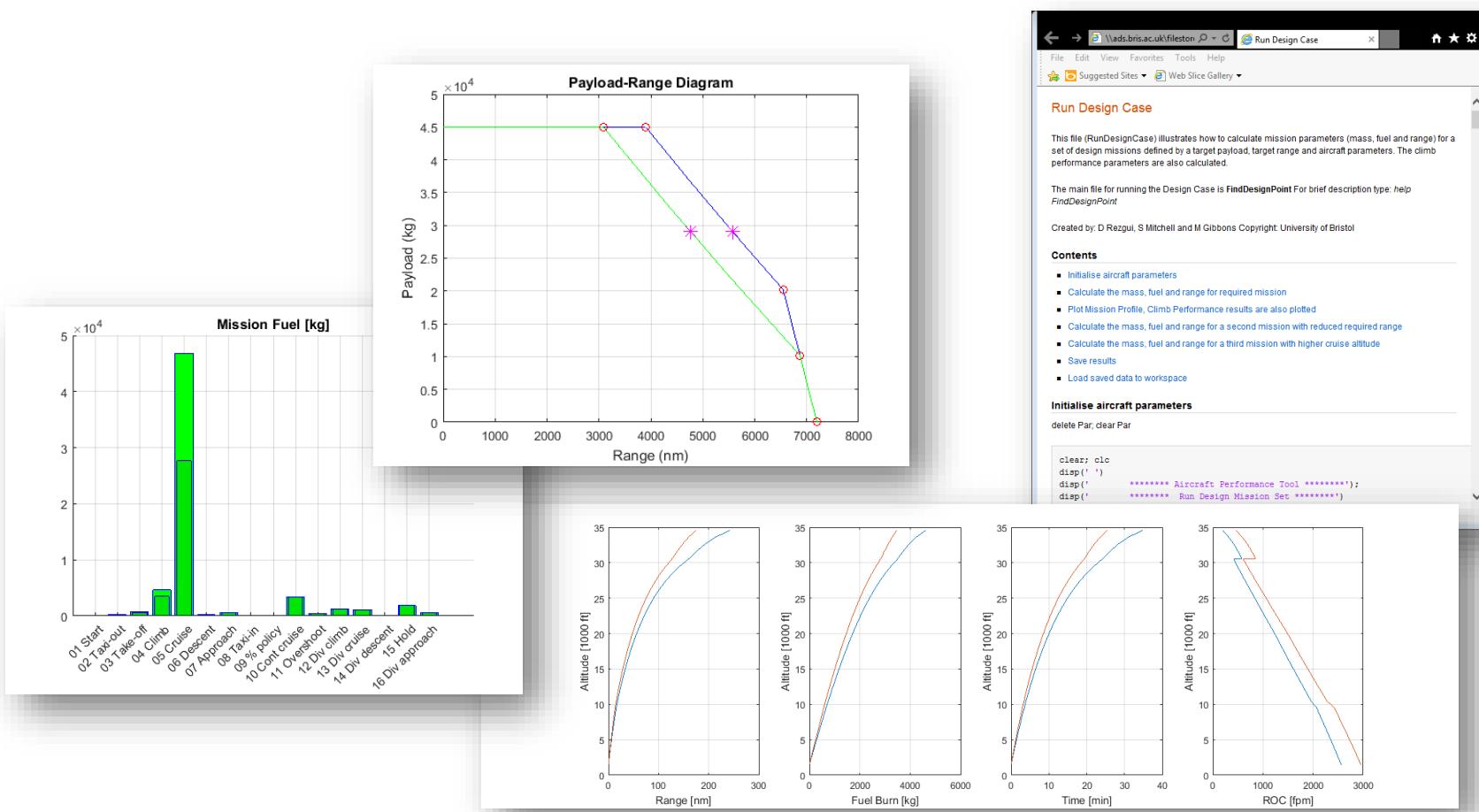
$$C_L = 0.6$$

$$L/D = 20$$

$$C_{D\text{tot}} = 0.03 \text{ (300 counts)}$$

$$\Delta C_{DW} = 5 + \text{counts}$$

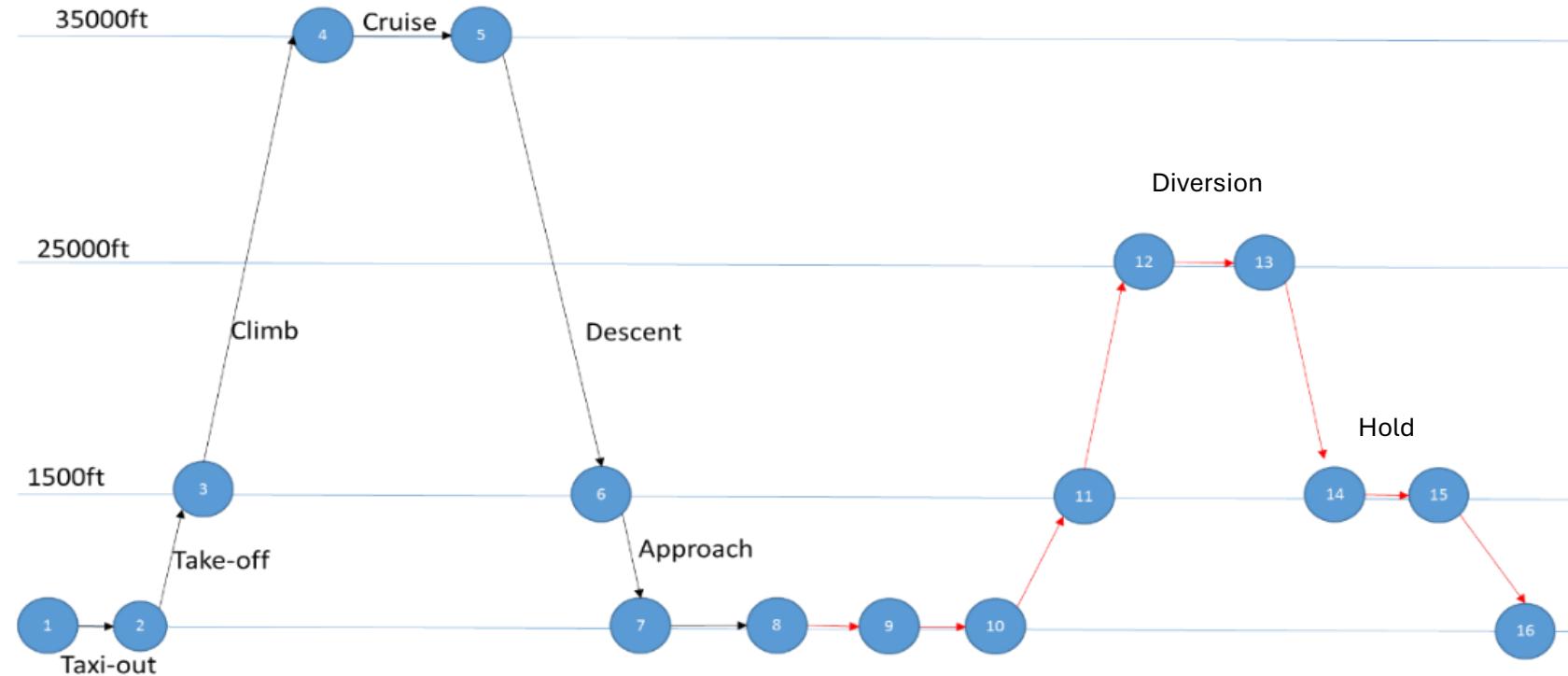
# Fixed Wing Performance Tool



# Fixed Wing Performance Tool

- In-house **MATLAB** tool created by **Rezgui, Mitchell and Gibbons**.
- Based largely on the reference aircraft in Chapter 10 of **Civil Aircraft Design** by Jenkinson, Simpkin & Rhodes, with a few modification from the Airbus design guides
- The tool generates the aircraft **Payload-Range Diagram** and calculate the **operational performance** for:
  - Given aircraft parameters (configuration, e.g. wing span, engine data, MTOM, empty mass, drag polar, ...)
  - Given aircraft mission (Mach number, altitude, required range, payload, ...)
- The tool is simple to use and allows flexibility to customise the run files and plotting functions
- Quick start guide available in the form of html and pdf demo files.

# Fixed Wing Performance Tool

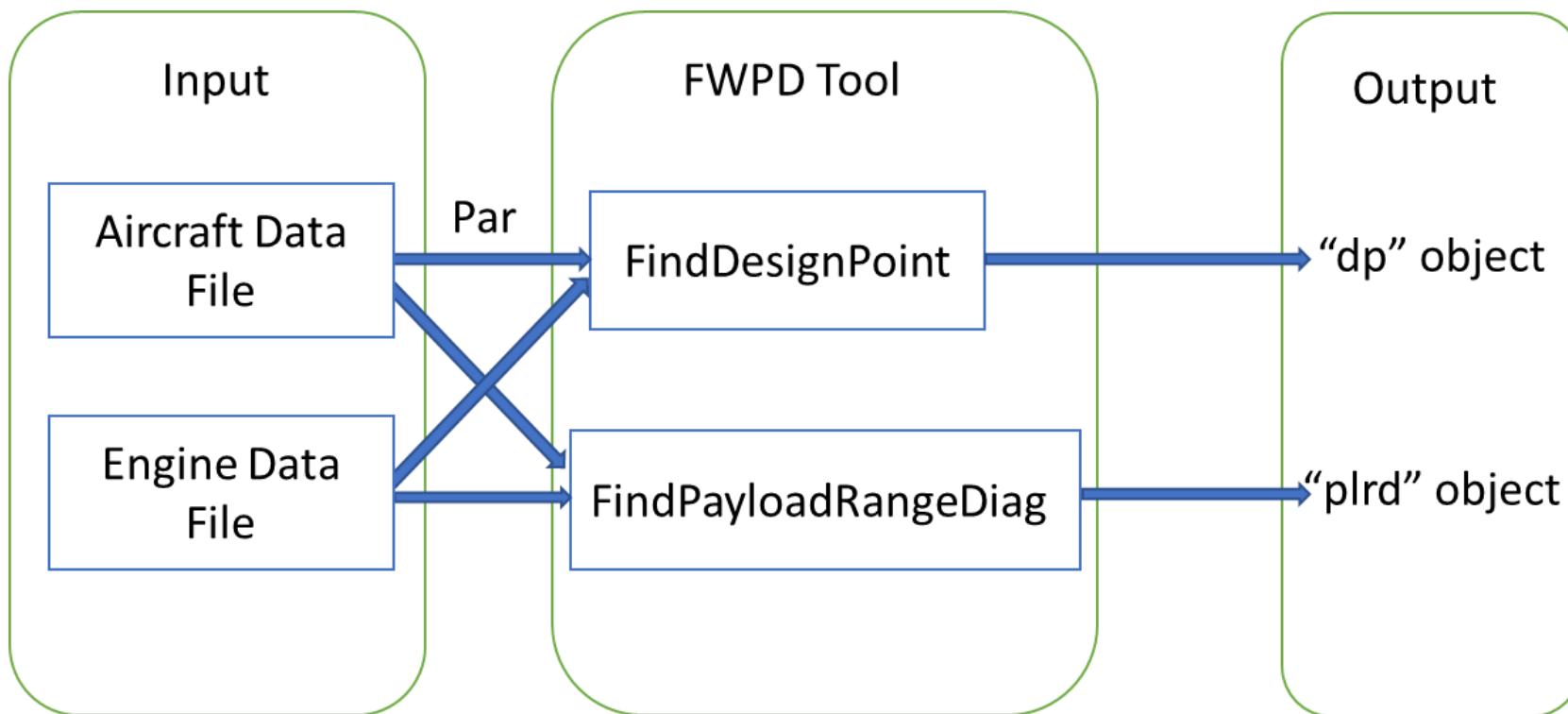


# Mission Phases

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1 - 2	Taxi out	Allowance
2 - 3	Take-off to 1500ft	Allowance
3 - 4	Climb 1500ft to Initial Cruise Altitude	Calculation
4 - 5	Cruise	Calculation
5 - 6	Descent final cruise altitude to 1500 ft.	Calculation
6 - 7	Approach	Allowance
7 - 8	Taxi in	Allowance
9	Overshoot / En route allowance	Allowance
10	Extended Cruise	Calculation
11 - 12	Diversion Climb	Calculation
12 - 13	Diversion Cruise	Calculation
13 - 14	Diversion Descent	Calculation
14 - 15	Diversion Hold	Allowance
15 - 16	Diversion Approach	Allowance

# Code Structure



# Function Calls

`dp = FindDesignPoint(Par, EngineData, TOM_0)`

## Input:

Par: Object of aircraft parameters

EngineData: Structure of aircraft engine data [optional]

TOM\_0: Initial value for TOM [optional]

## Output:

dp: object contains design point (dp) results

# Function Calls

**plrd = FindPayloadRangeDiag(Par, EngineData, Payload\_0)**

Par: Object of aircraft parameters

EngineData: Structure of aircraft engine data [optional]

Payload\_0: Initial value for payload [optional]

## Output:

plrd: object contains design point (dp) results

# Plotting

Plot mission:

**PlotMission(dp.Mission)**

Plot payload range diagram:

**PlotPLRD(plrd, marker)**

Marker: line colour and shape [optional]

# Run files

- RunDesignCase
- RunDesignSet
- RunPayloadRange

# Lab Tasks

Produce the Payload Range diagram for a notional 1990's twin engine, Airliner \*.

Show how the range at the “design case” varies with different cruise Mach Numbers & Cruise Altitudes.

Compare the block fuel & block time at a series of ranges (e.g. London to Beijing 4461 nm plus other ranges) for variations in Cruise Mach Number & altitude.

Carry out trade studies on the effect on block fuel at a fixed range for changes in OME, Drag & SFC.

\* Based largely on the reference aircraft in Chapter 10 of Civil Aircraft Design by Jenkinson, Simpkin & Rhodes.

# Getting Started with FW Performance Tool



Watch video on use of  
MATLAB tool



Download tool from  
Blackboard



Go through Quick Start-  
up Guide (run files and  
help documents)



Attempt the tutorial  
tasks



Attend labs for the FW  
Performance design  
exercise