

# Appendix 7: North American Aerodynamic Derivative Notation

**Table A7.1** Longitudinal Normalised Derivatives

Dimensionless Coefficient	Multiplier	Dimensional
$C_{x_u} = -(M_0 C_{D_M} + 2C_D)$	$\rho V_0 S / 2m$	$X_u$
$C_{x_u}^* = -(M_0 C_{D_M} + 2C_D) + M_0 C_{\tau_M} \cos \kappa$	$\rho V_0 S / 2m$	$X_u^*$
$C_{x_{\dot{w}}} = C_{x_{\dot{\alpha}}}$	$\rho S \bar{C} / 4m$	$X_{\dot{w}}$
$C_{x_w} = C_L - C_{D_\alpha}$	$\rho V_0 S / 2m$	$X_w$
$C_{x_q}$	$\rho V_0 S \bar{C} / 4m$	$X_q$
$C_{x_\delta}$	$\rho V_0^2 S / 2m$	$X_\delta$
$C_{z_u} = -(M_0 C_{L_M} + 2C_L)$	$\rho V_0 S / 2m$	$Z_u$
$C_{z_u}^* = -(M_0 C_{L_M} + 2C_L) - M_0 C_{\tau_M} \sin \kappa$	$\rho V_0 S / 2m$	$Z_u^*$
$C_{z_{\dot{w}}} = C_{z_{\dot{\alpha}}}$	$\rho S \bar{C} / 4m$	$Z_{\dot{w}}$
$C_{z_w} = -(C_D + C_{L_\alpha})$	$\rho V_0 S / 2m$	$Z_w$
$C_{z_q}$	$\rho V_0 S \bar{C} / 4m$	$Z_q$
$C_{z_\delta}$	$\rho V_0^2 S / 2m$	$Z_\delta$
$C_{m_u} = M_0 C_{m_M}$	$\rho V_0 S \bar{C} / 2I_y$	$M_u$
$C_{m_u}^* = M_0 C_{m_M} + M_0 \frac{z_\tau}{\bar{C}} C_{\tau_M} \cos \kappa$	$\rho V_0 S \bar{C} / 2I_y$	$M_u^*$
$C_{m_{\dot{w}}} = C_{m_{\dot{\alpha}}}$	$\rho S \bar{C} / 4I_y$	$M_{\dot{w}}$
$C_{m_w} = C_{m_\alpha}$	$\rho V_0 S \bar{C} / 2I_y$	$M_w$
$C_{m_q}$	$\rho V_0 S \bar{C}^2 / 4I_y$	$M_q$
$C_{m_\delta}$	$\rho V_0^2 S \bar{C} / 2I_y$	$M_\delta$

Notes: Thrust coefficient is defined as  $C_\tau = \tau / \frac{1}{2} \rho V_0^2 S$ . In the notational style,  $C_{\tau_M} = \partial C_\tau / \partial M$ ;  $\kappa$  is the (upward) inclination of the thrust line with respect to the  $x$  axis;  $z_\tau$  is the normal offset of the thrust line from the cg. It is assumed that  $x_\tau$ , the axial offset of the thrust line from the cg, is negligibly small.

**Table A7.2** Longitudinal Dimensionless Derivative Equivalents

American	British	American	British
$C_{x_u}$		$C_{z_\alpha}$	$Z_w$
$C_{x_u}^*$	$X_u$	$C_{z_q}$	$2Z_q$
$C_{x_{\dot{\alpha}}}$	$2X_{\dot{w}}$	$C_{z_\delta}$	$Z_{\eta\tau}$
$C_{x_\alpha}$	$X_w$	$C_{m_u}$	
$C_{x_q}$	$2X_q$	$C_{m_u}^*$	$M_u$

(Continued)

**Table A7.2** (Continued)

American	British	American	British
$C_{x_\delta}$	$X_{\eta, \tau}$	$C_{m_\alpha}$	$2M_{\dot{w}}$
$C_{z_u}$		$C_{m_\alpha}$	$M_w$
$C_{z_u}^*$	$Z_u$	$C_{m_q}$	$2M_q$
$C_{z_\alpha}$	$2Z_{\dot{w}}$	$C_{m_\delta}$	$M_{\eta, \tau}$

**Table A7.3** Lateral-Directional Normalised Derivatives

Dimensionless Coefficient	Multiplier	Dimensional
$C_{y_v}$	$\rho V_0 S / 2m$	$Y_v$
$C_{y_\beta}$	$\rho V_0^2 S / 2m$	$Y_\beta$
$C_{y_p}$	$\rho V_0 Sb / 4m$	$Y_p$
$C_{y_r}$	$\rho V_0 Sb / 4m$	$Y_r$
$C_{y_\delta}$	$\rho V_0^2 S / 2m$	$Y_\delta$
$C_{l_v}$	$\rho V_0 Sb / 2I_x$	$L_v$
$C_{l_\beta}$	$\rho V_0^2 Sb / 2I_x$	$L_\beta$
$C_{l_p}$	$\rho V_0 Sb^2 / 4I_x$	$L_p$
$C_{l_r}$	$\rho V_0 Sb^2 / 4I_x$	$L_r$
$C_{l_\delta}$	$\rho V_0^2 Sb / 2I_x$	$L_\delta$
$C_{n_v}$	$\rho V_0 Sb / 2I_z$	$N_v$
$C_{n_\beta}$	$\rho V_0^2 Sb / 2I_z$	$N_\beta$
$C_{n_p}$	$\rho V_0 Sb^2 / 4I_z$	$N_p$
$C_{n_r}$	$\rho V_0 Sb^2 / 4I_z$	$N_r$
$C_{n_\delta}$	$\rho V_0^2 Sb / 2I_z$	$N_\delta$

**Table A7.4** Lateral-Directional Dimensionless Derivative Equivalents

American	British	American	British
$C_{y_v}$	$Y_v$	$C_{l_r}$	$2L_r$
$C_{y_\beta}$		$C_{l_\delta}$	$L_{\xi, \zeta}$
$C_{y_p}$	$2Y_p$	$C_{n_v}$	$N_v$
$C_{y_r}$	$2Y_r$	$C_{n_\beta}$	
$C_{y_\delta}$	$Y_{\xi, \zeta}$	$C_{n_p}$	$2N_p$
$C_{l_v}$	$L_v$	$C_{n_r}$	$2N_r$
$C_{l_\beta}$		$C_{n_\delta}$	$N_{\xi, \zeta}$
$C_{l_p}$	$2L_p$		