



Fatigue

Samudra Dasgupta

Senior Lecturer in Aerospace Engineering
University of Bristol

bristol.ac.uk



Fatigue

Part-4: Aircraft level design considerations for fatigue

bristol.ac.uk



Airframe design considerations

Airframe
design
philosophies

Materials &
manufacturing

Operational
environments

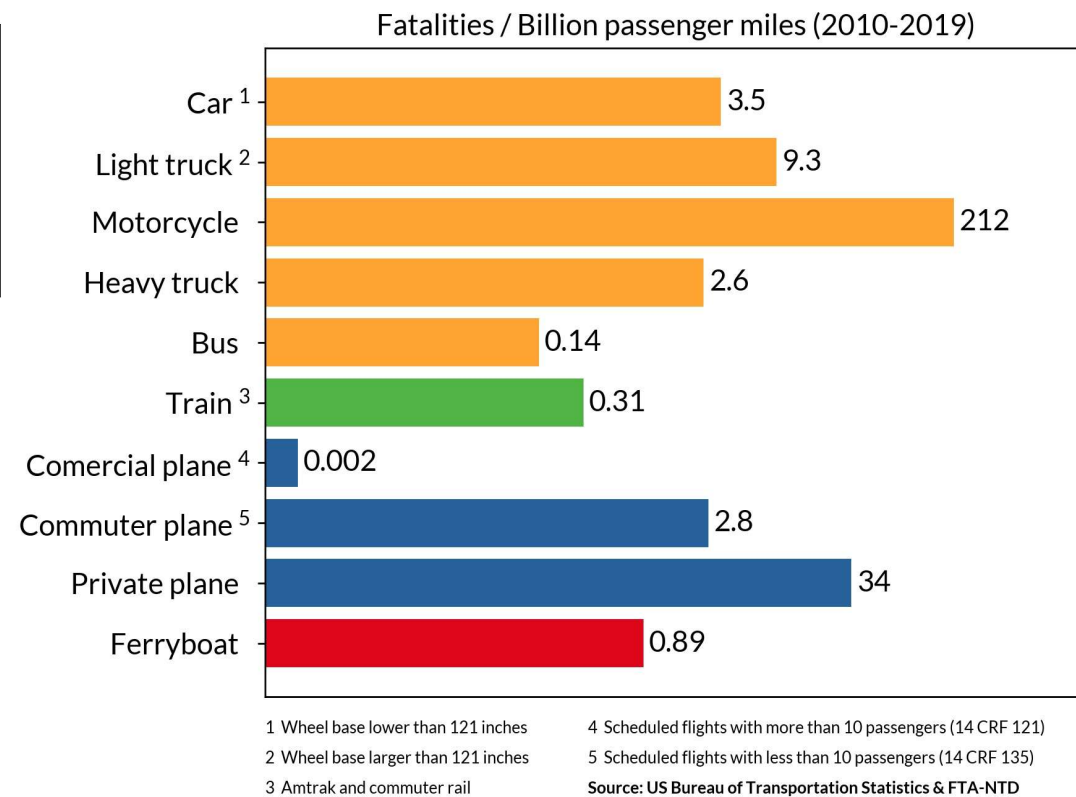
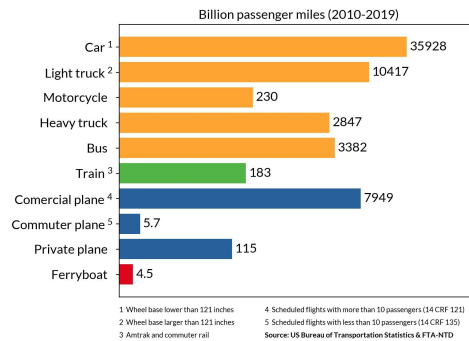
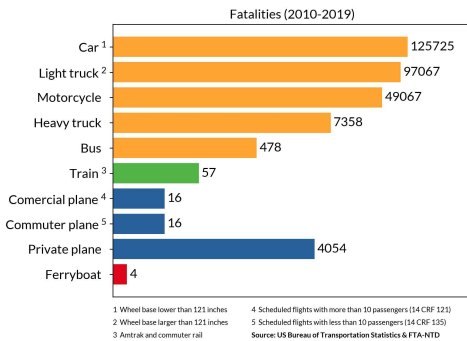
Detail designs

Airframe Design Philosophies

bristol.ac.uk



Aviation safety statistics



Fatal Airliner Accidents Per Year 1946-2019



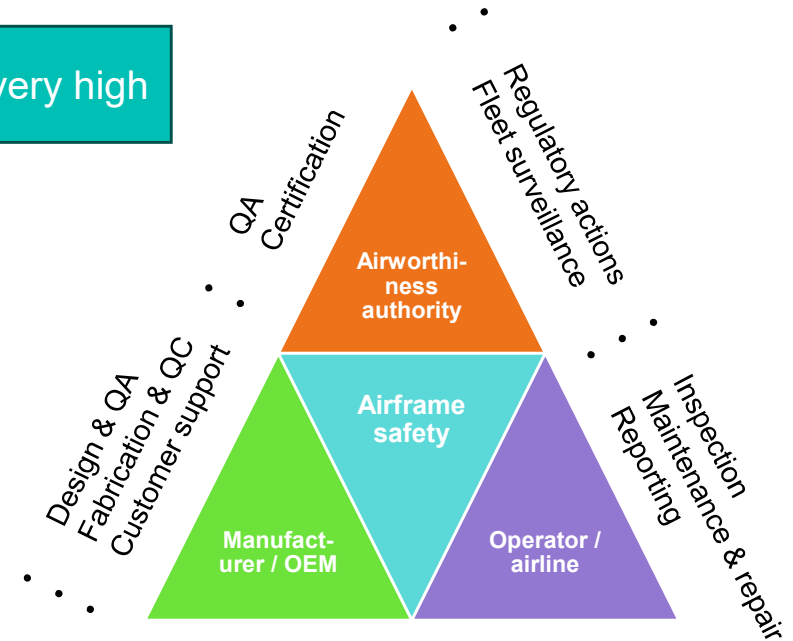
Design / safety philosophies

Crash due to structural failure is rare; reliability assumed to be very high



B747 cargo aircraft crash in Netherlands (1992) due to fatigue & overload failures in airframe

bristol.ac.uk



Safe life

Safety by retirement

Fail safe

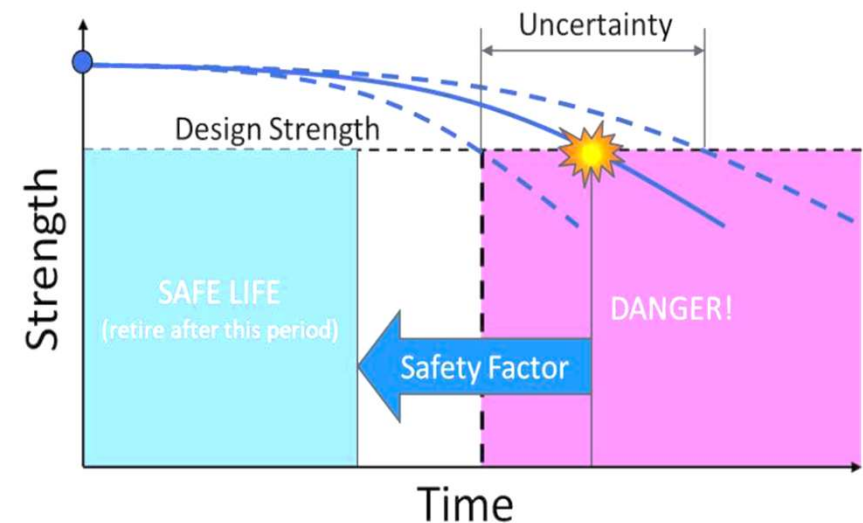
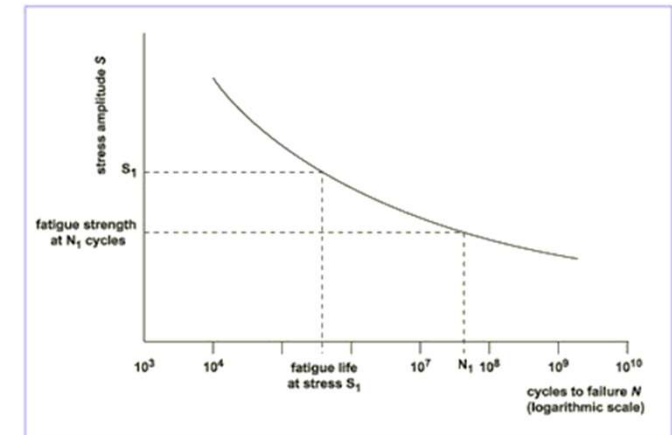
Safety by design

Damage tolerant

Safety by inspection

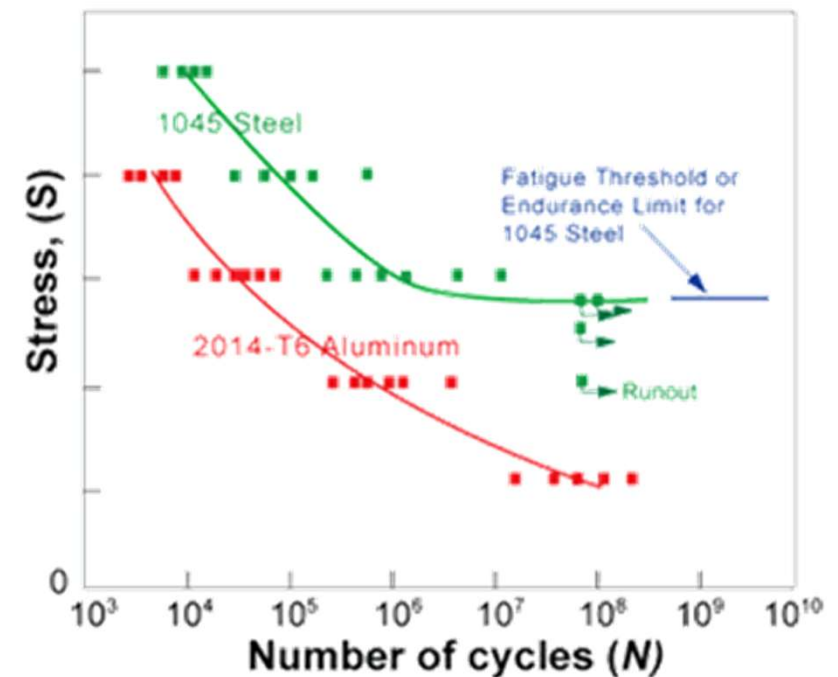
Safe life design

- Safe LIFE: Number of flights / landings / flight hours, during which there is a low probability that strength will degrade below design strength (1950s)
 - No. of flights: Pressurized fuselage
 - Distance traversed: Engine components
 - Calendar life: Rubber parts
- Design criteria
 - **Safety by retirement**
 - Fatigue failure is not likely to occur during design life (i.e. up to crack initiation stage)
 - Safe-life interval = projected lifetime of aircraft = crack free service life
- Challenges
 - Limitations of testing (La Havilland Comet 1)
 - 16000 as per test Vs. around 1000 in actual (3 crashes in 1 year)
 - Strain hardening @ window corners during static overload (2P) tests and same airframe used for fatigue
 - Life extension
 - Load increase (capacity extension)



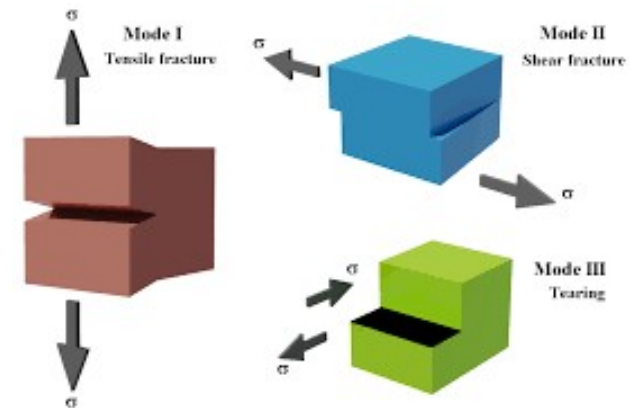
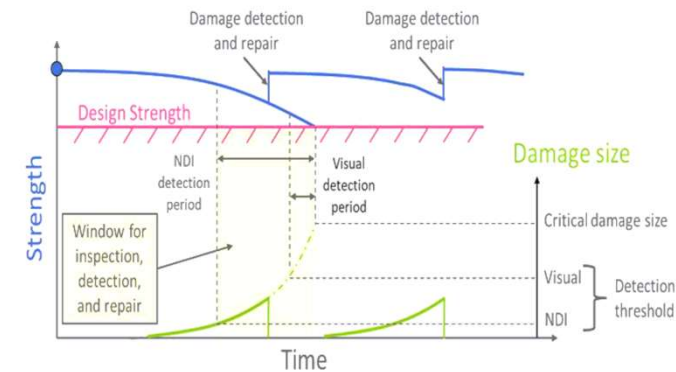
Fail safe design

- Designed NOT to fail (**safety by design**) (1970s)
 - Case 1: Infinite life
 - Case 2: Redundant load paths
 - Case 3: Residual strength-based design
- Design criteria
 - Max stress < FEL (fatigue crack propagation stage)
 - Multiple redundant spars in wing etc.
 - Compression after Impact (CAI) as design allowable for very conservative design
- Generally, economical & safer than safe life
- Challenges
 - Unforeseen damage
 - Multiple site damage
 - Gradual degradation of redundant member
 - **FMEA necessary**

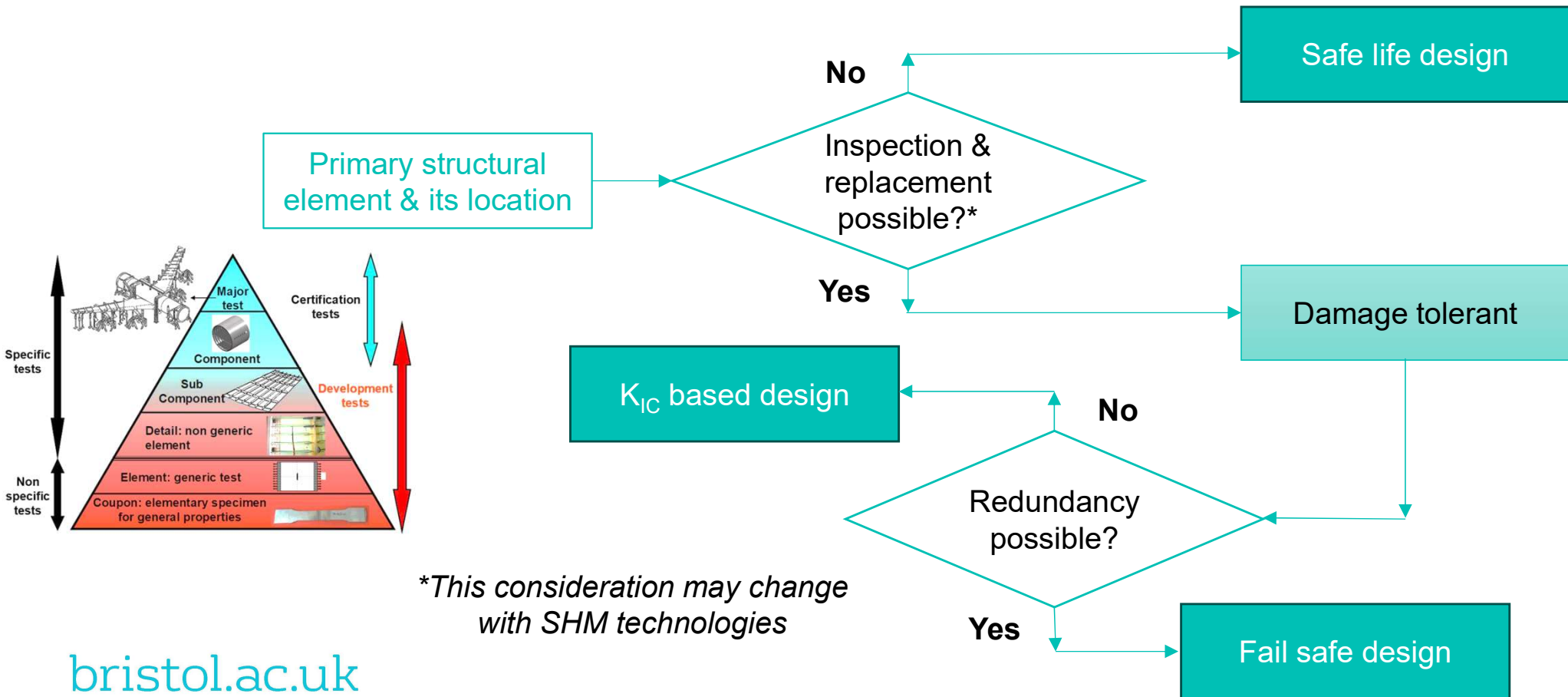


Damage tolerant design

- Designed with maintenance (detection capability & inspection schedule) in the loop (current)
 - Design assuming presence of damage (extension of fail safe)
 - Sustains loads till a critical size of the damage (extension of safe life)
 - Detect damages before they attain the critical size through inspection protocol, i.e. fail safe interval (**safety by inspection**)
 - Repair should restore original strength
- Design criteria
 - Stress conc. factor (K_t) = $\sigma(\text{peak})/\sigma(\text{nominal}) = 1 + 2(a/r)^{0.5}$ where a =damage size & r =damage radius, **not suitable for sharp defects**, but applicable for stress build-up from any repair
 - Stress intensity factor (K) = $\sigma \cdot (\pi \cdot a)^{0.5}$; $a_{\text{crit}} = (K_{IC}/\sigma_{\text{crit}})^2/\pi$ for sharp defects
 - Fracture toughness is a material property indicating the sensitivity for cracks under static loading
 - Related to material ductility and critical stress via geometry



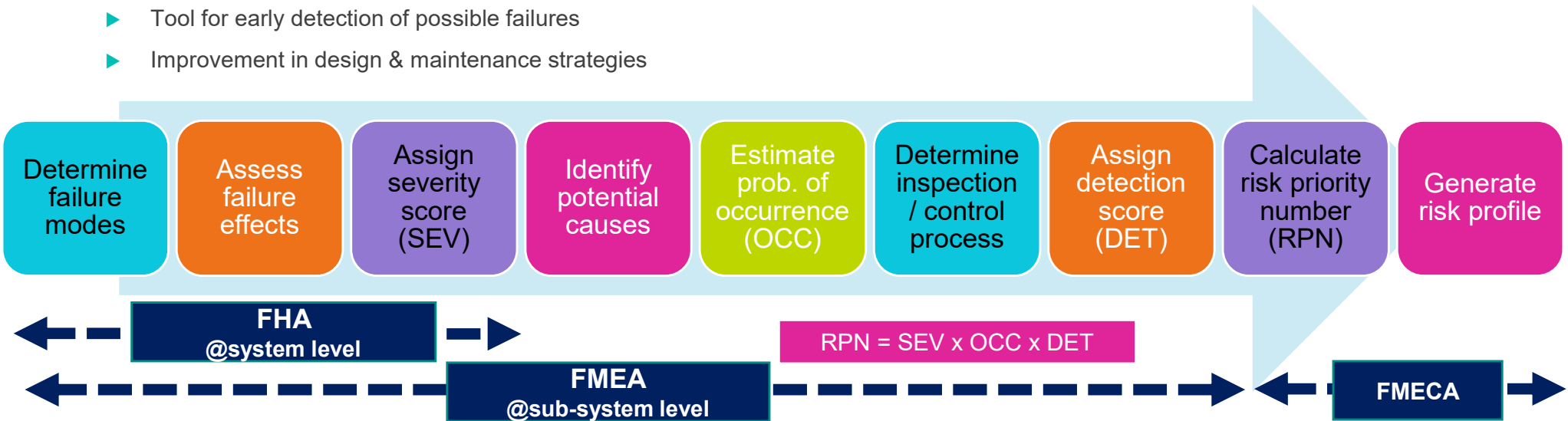
Safety design approach



FHA / FMEA / FMECA

► Structured engineering practice to analyze potential causes of operational failure

- Tool for early detection of possible failures
- Improvement in design & maintenance strategies



Scores	↓	1	2	3	4	5	6	7	8	9	10
SEV	Redundant / damage tol.	None	Very minor	Minor	Very low	Low	Moderate	High	Very high	Hazardous w warning	Hazardous w/o warning
OCC	More MTBF, MIL grade	Fail safe (P=0)	No failure / only isolated failures in identical system			Isolated / occasional / frequent failures in similar system			Possible / likely / inevitable failure in new design		New technology
DET	More O Level, IVHM	Almost certain	Very high	High	Moderately high	Moderate	Low	Very low	Remote	Very remote	Uncertain

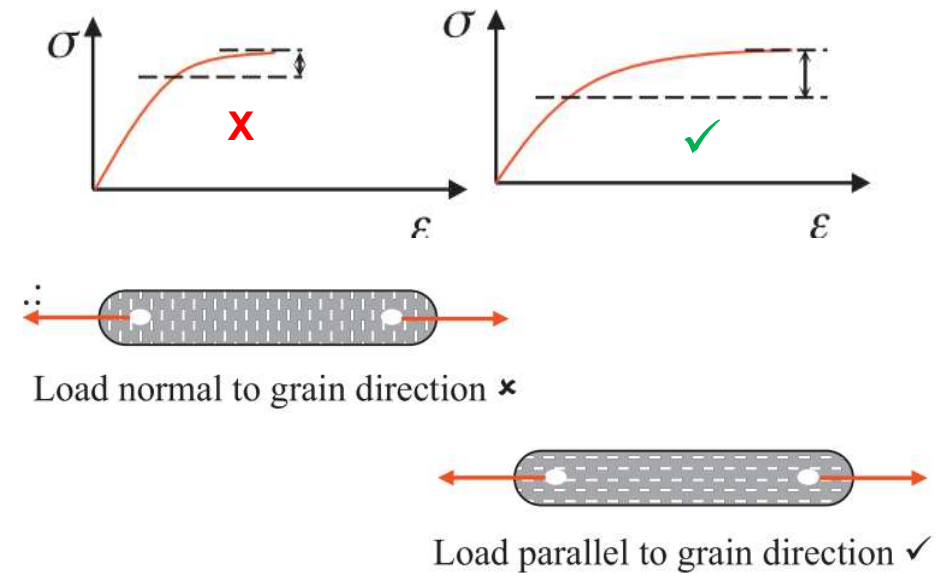
Materials & Manufacturing

bristol.ac.uk



Materials & processing

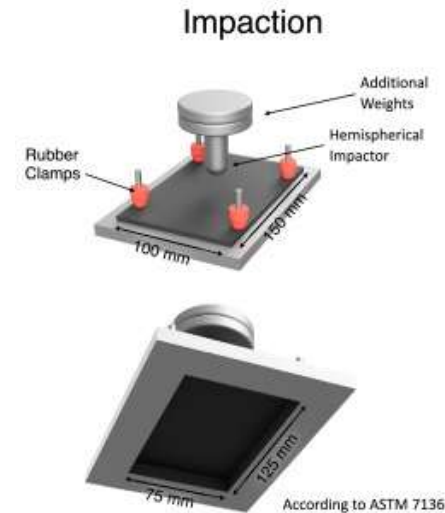
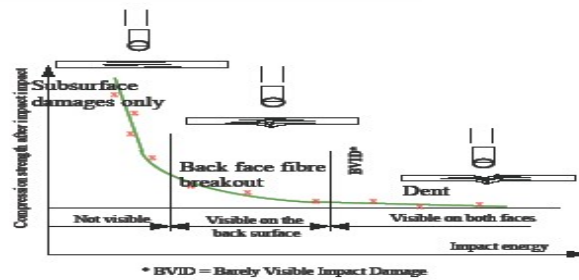
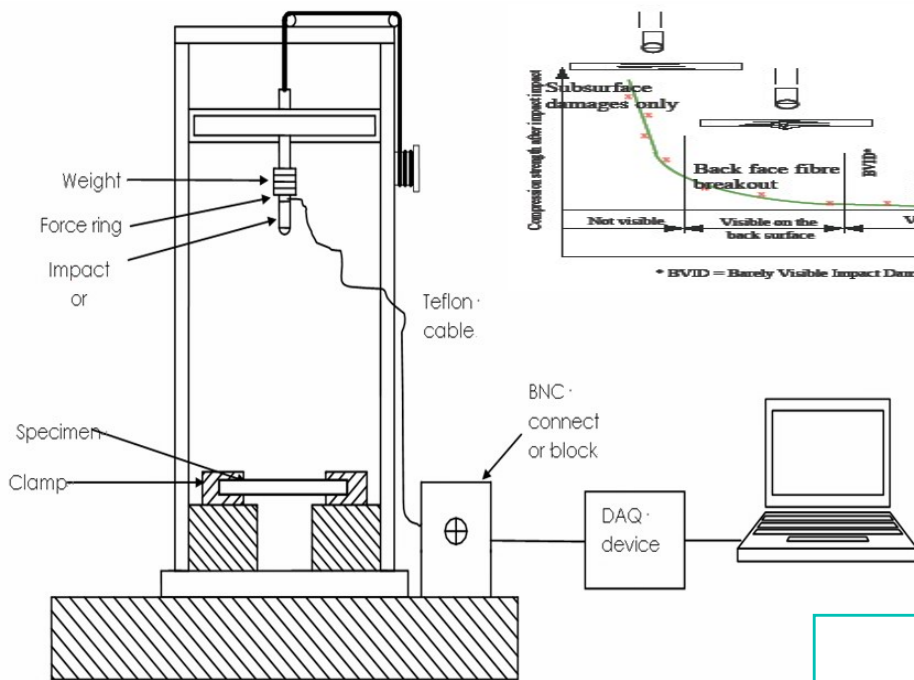
- Higher yield strength (improves N_i as well as N_{SP})
 - Al alloy 2024-T3 for tensile loading (lower wing skin, fuselage etc.)
 - Avoid Al alloy with high YS/UTS ratio (plastic safety margin)
 - Ensure proper heat treatment (T6 vs T3)
 - Grain boundaries vis-à-vis loading direction
- Case hardening after shot peening (improves N_{SP})
- Specific to composites
 - Ply drop protocols**
 - Use advanced processes ($V_0 < 2\%$)
 - Hand layup $\sim >10\%$
 - Autoclave molding of prepregs $\sim <0.5\%$
 - Residual compressive strength based design
 - 3d Composites



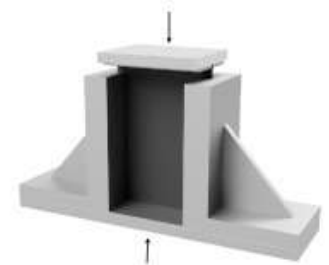
Ply-drop protocols (thumb-rules)

- For primary structures: Ply-drop length = $20 \times \text{CPT} \times n$
- For secondary structures: Ply-drop length = $10 \times \text{CPT} \times n$
- Only inner surface ply-drops allowed
- Symmetry & balance to be maintained in ply-drops

Compression after Impact



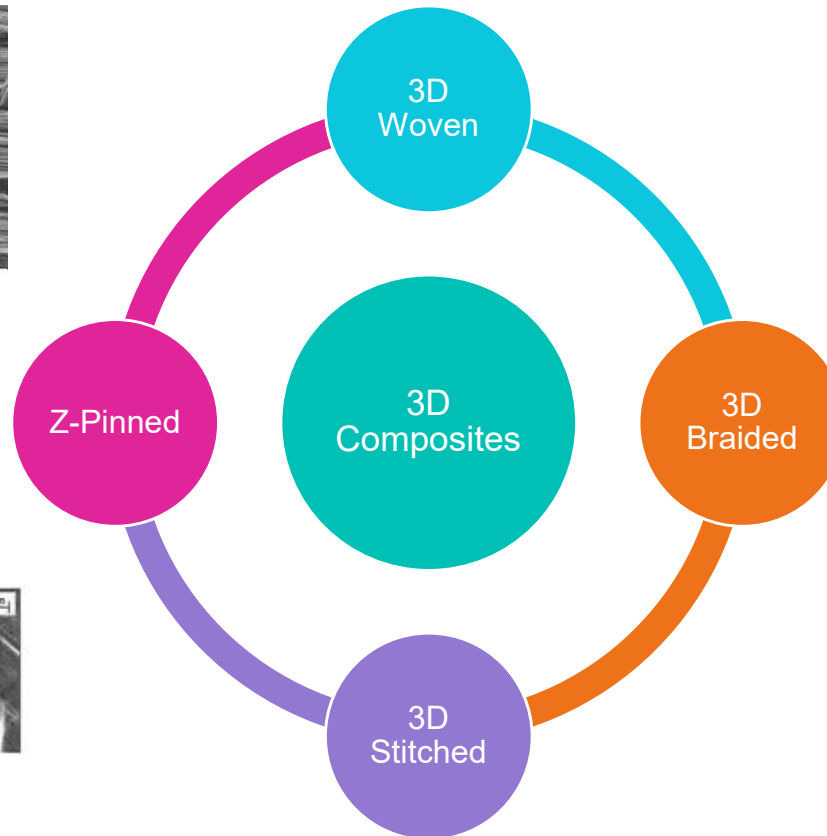
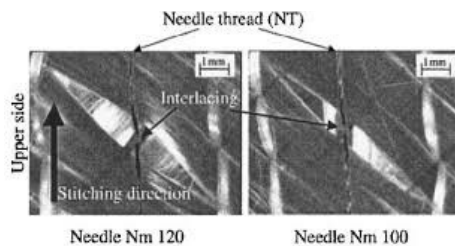
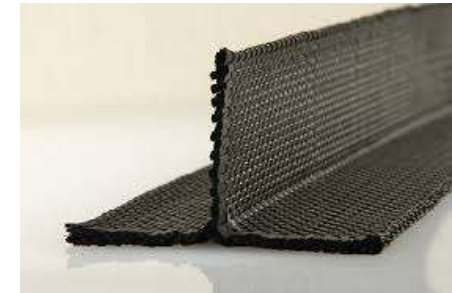
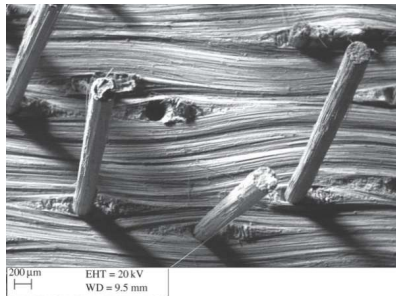
Compressive Test



According to ASTM 7137

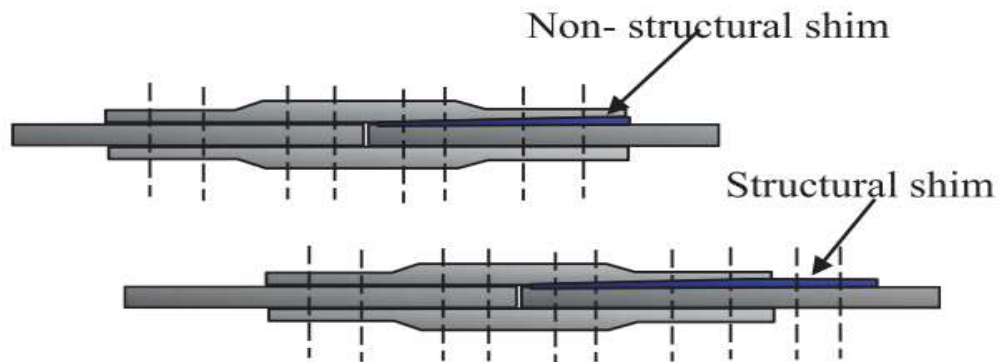
CAI: Very conservative design approach
(typically $1/3^{\text{rd}}$ of tensile strength)

Commonly used 3d composites

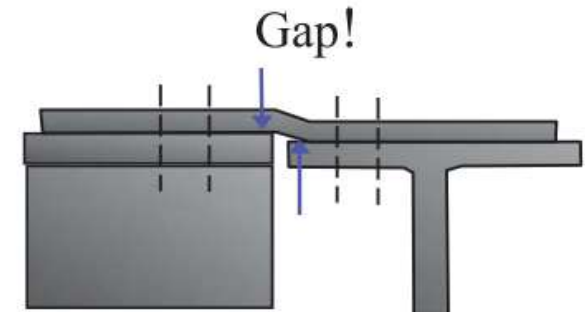
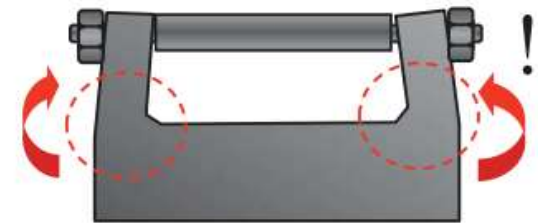
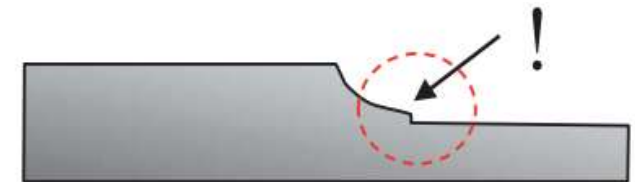


Manufacturing & assembly

- Minimize chances of stress raisers on surface (improves N_i)
 - Clean the surface off etchants, dye etc.
 - Protective finishing
- Minimize surface roughness and other discontinuities arising out of machining operations (improves N_i)
- Minimize gaps, check fit-up and use shims (improves N_i)



bristol.ac.uk



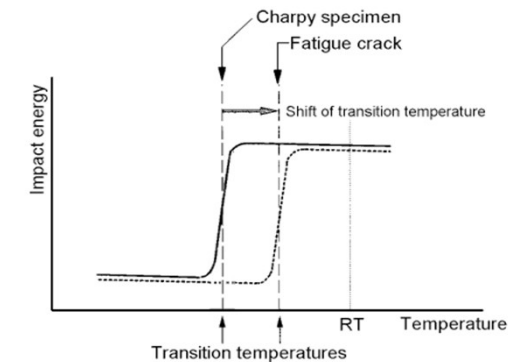
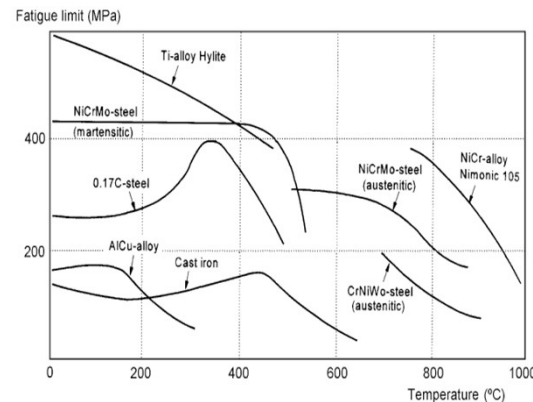
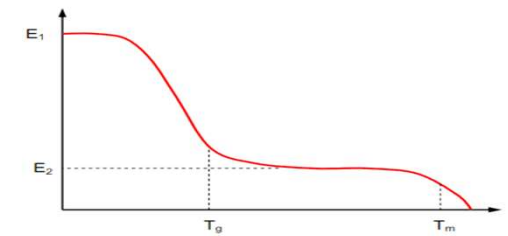
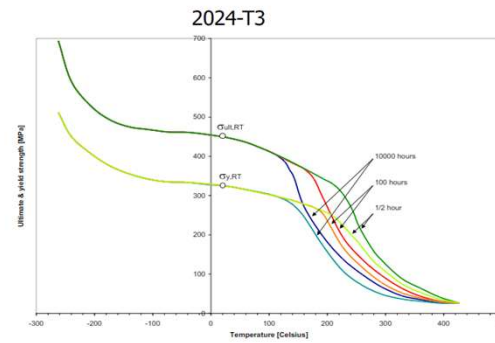
Operational Environments

bristol.ac.uk



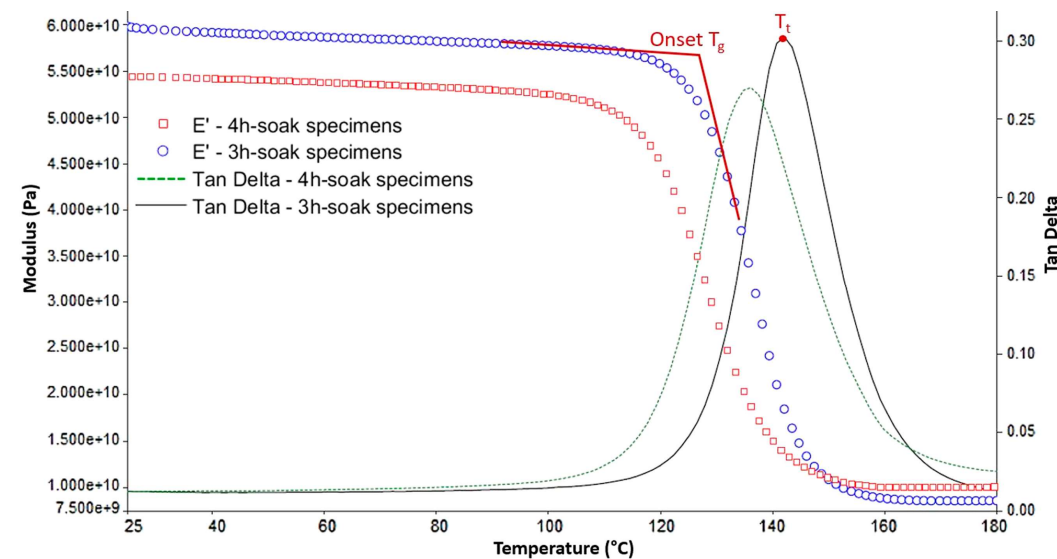
Effects of temperature

- High temperature
 - Caused by hot parts (engine) / skin friction (supersonic drag) / trajectory (re-entry) etc.
 - Creep
 - Decrease in strength & modulus
 - Glass transition
 - Melting
 - Thermal expansion
 - Fatigue life
- Low temperature
 - Caused by space / high altitudes / cryogenics etc.
 - Embrittlement (fracture toughness)



Material operational limits in composites

- Moisture saturation of samples in environmental chamber
 - Typically 70°C & 95% RH as per ASTM D5229
- Glass transition temperature (T_g) measurement (DMA / DSC etc.)
 - Identify onset of wet T_g from storage modulus tangents

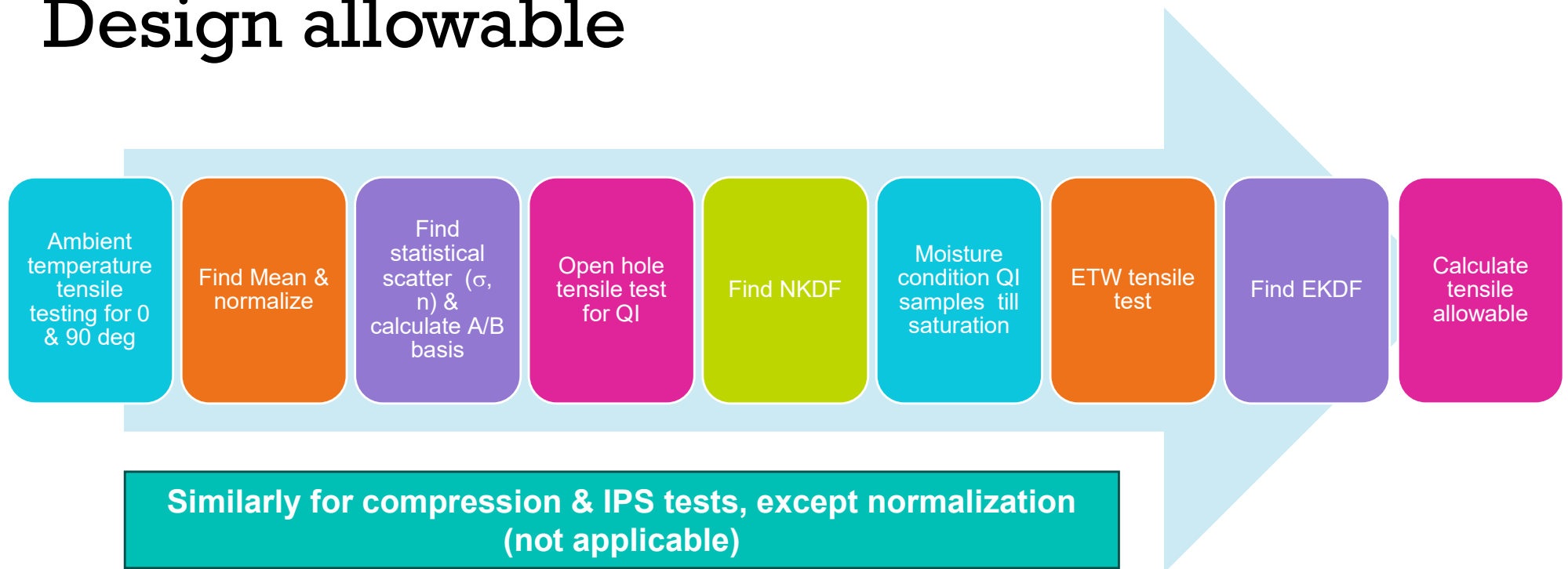


MOL = Onset of wet T_g - 28°C

Effects of other environments

- Humidity
 - Metal: Corrosion
 - Composites: Reduction in matrix cohesion, matrix to fibre adhesion and T_g
- Others
 - Salty / marine environment
 - Space (UV, Vacuum, Free radicals (O^+))
 - Fuel / hydraulic oil
 - Cleaning agents / solvents
- Galvanic corrosion (Del $V = 0.1$ V allowed; CFRP-Al = 1.2V, CFRP-Cu = 0.6V, CFRP-SS=0.1V)
 - Electrical isolation
 - Sacrificial anode (Zn for steel in marine env.)

Design allowable



B-basis calculations

- Method -1 (MIL/CMH HDBK 17F)

- The original method was developed for metallic materials (Ref: MIL-HDBK-5c) with the following assumptions.
 - Normal probability density function
 - All data belong to a single statistical population (no batch-to-batch variability).

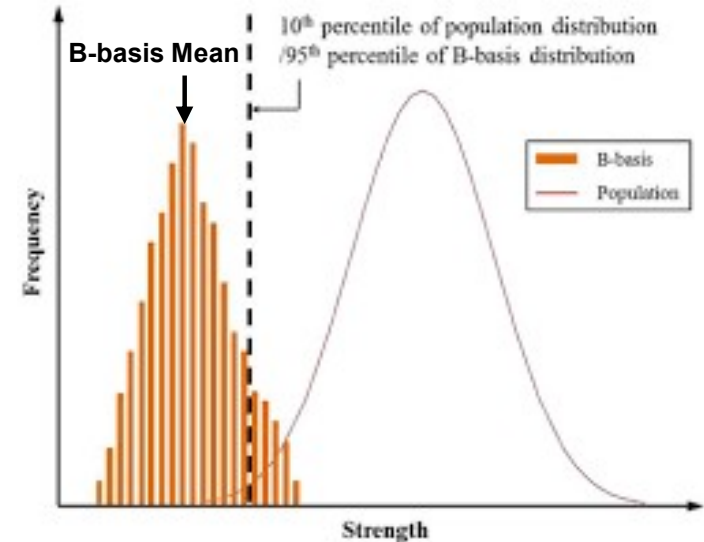
$$B - value = \bar{X} - K_b \cdot \sigma$$

- K_b = Function of sample size, as per Table 8.5.10 in MIL-HDBK-17-1F (copy of the same given at the end)
- σ = Standard deviation

- Method – 2 (Gökgöl method – Airbus Design Office, Germany)

$$B - value = \left[\frac{\{1 - (K_b \cdot CV)\}}{\left\{1 + \left(conf. \frac{CV}{\sqrt{n}}\right)\right\}} \right] \bar{X}$$

- $K_b = 1.2816$
- CV = Coefficient of variation = (Mean / Standard deviation)
- $Conf. = 1.6449$
- n = batch size of the sample



Carbon-epoxy allowables (typical)

Knock-downs	EKDF	NKDF
Tensile	0.96	0.60
Compressive	0.69	0.83
In-plane Shear	0.92	1.00
Poisson's ratio	0.3	
Density (Kg/m ³)	1.8	

Modulus	Orientation	Mean
Tensile (GPa)	0	130
	90	10
Compressive (GPa)	0	120
	90	15
Shear (GPa)	-	4.5

Test Details		Material / Design allowables @ $V_f = 60\%$ (MPa)				
Type	Orientation	Mean	Normalized @ 60% V_f	B-value-Gökgöl	After EKDF	After E&NKDF
Tensile	0	1850	1800	1600	1536	922
	90	100	97	80	77	46
Compression	0	1300	NA	1150	794	659
	90	200	NA	160	110	91
Shear (IPS)	± 45	85	NA	80	74	74

Detail Design

bristol.ac.uk



Stress levels

- Use high fidelity stress analysis to capture stress gradients and concentrations from holes, cut-outs, notches etc.
- Use actual loads if possible (from FTI or SHM)
- Use allowable strength values only
- Use local reinforcements wherever necessary (doubler plates, taper straps etc.)
- Limit fuselage hoop stress
- Design to allow for fuselage panel quilting or pillowing
- Avoid initial buckling of webs
 - No buckling up to 1g & 1.5 g for civilian and fighter A/c resp.
 - Use design ratio $\tau_{crit} / \tau_{ult} > 20\%$
 - Use limit minimum t/b panel sizing for lightly loaded webs (avoid in-plane shear)

Wing design - buckling

$$P_{cr} = \frac{\pi^2 EI}{(KL)^2}$$

where


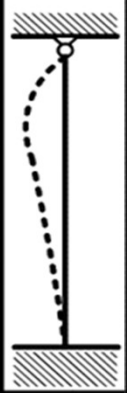


P_{cr} = Euler's critical load (longitudinal compression load on column),

E = modulus of elasticity of column material,

I = minimum area moment of inertia of the cross section of the column,

L = unsupported length of column,

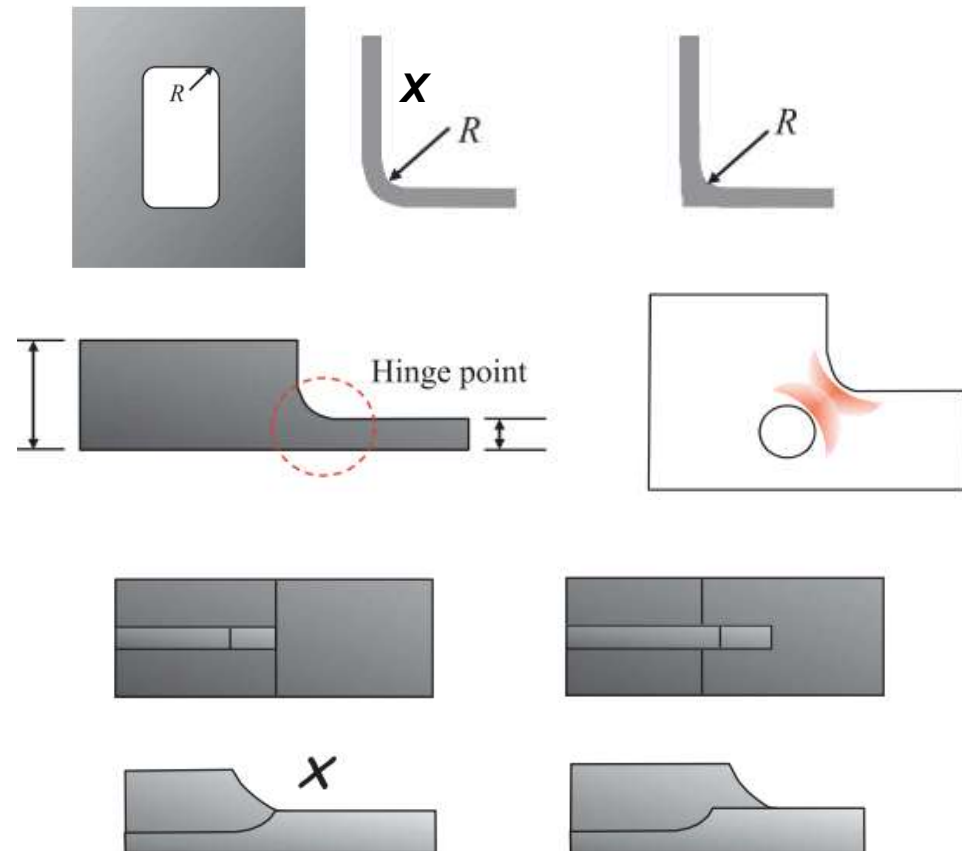
K = column effective length factor

Buckled shape of column shown by dashed line				
Theoretical K value	0.5	0.7	1.0	2.0
Recommended design value K	0.65	0.80	1.0	2.10
Boundary conditions	Fixed-Fixed	Fixed-Pinned	Pinned-Pinned	Fixed-Free

Detail engineering

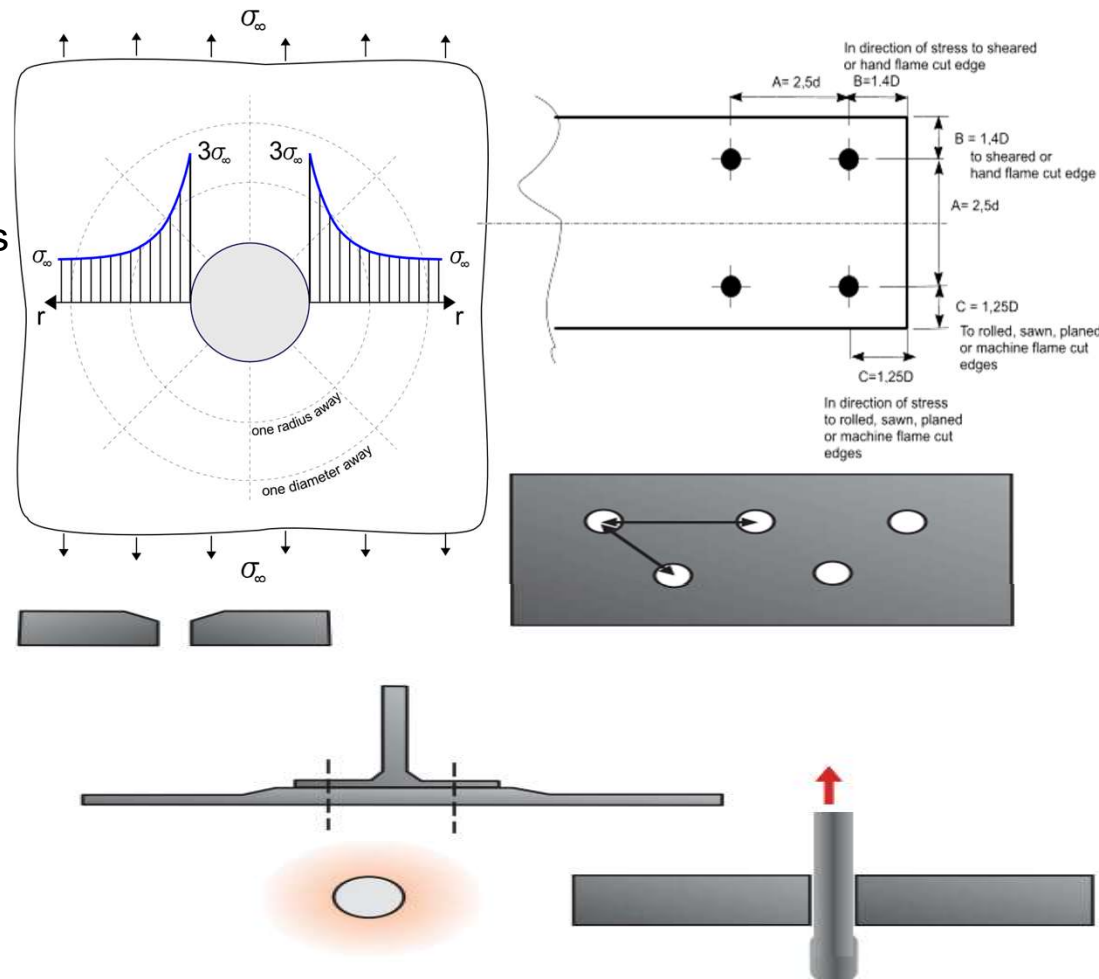
- Use large cut-out radii & corner / bend radii (min. $2t$)
- Avoid sudden discontinuities in sections
- Avoid interacting stress concentrations
- Avoid change in sections at same location
 - Example: Stringer run-outs
- Use fatigue quality index
 - Proprietary index capturing previous experience
 - Embed manufacturing damages, holes, scratches, repairs in design process
- Composite lay-ups ply drops

bristol.ac.uk



Joint & edge design

- Use sufficient pitch between fastener holes & edge distances
 - To prevent stress concentration interactions
- Limit counter sink depth
 - Increase edge distance to cater for CSKs
- Use thickening / pad-up
 - To reduce stress levels
- Use cold worked holes
 - For residual compressive stress
- Use correct fastener & installation
- Avoid blind areas
- Avoid eccentricities



End of Part-4

Fatigue

bristol.ac.uk



Thank you

samudra.dasgupta@bristol.ac.uk

<https://in.linkedin.com/in/samudradg>

bristol.ac.uk

