

# REVIEW & STATE SPACE INTRO

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# Feedback (from you)

- 10/158 responses
- More guidance
- I'm still unsure what I should be doing
- More coverage of basic control concepts
- More linking back to previous learning
- I appreciate the mixture of theory and MATLAB
- Please be clear of when coursework is set
  - the lecturer has said it will be set on a certain day but it has not



SB



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(Start of lecture) Current feeling/comments...

fast bold  
inspiration creative  
leader focus  
transpiration

Mentimeter

Menti

Control L3



Choose a slide to present

Current feeling...

(After concept outline) Current feeling...

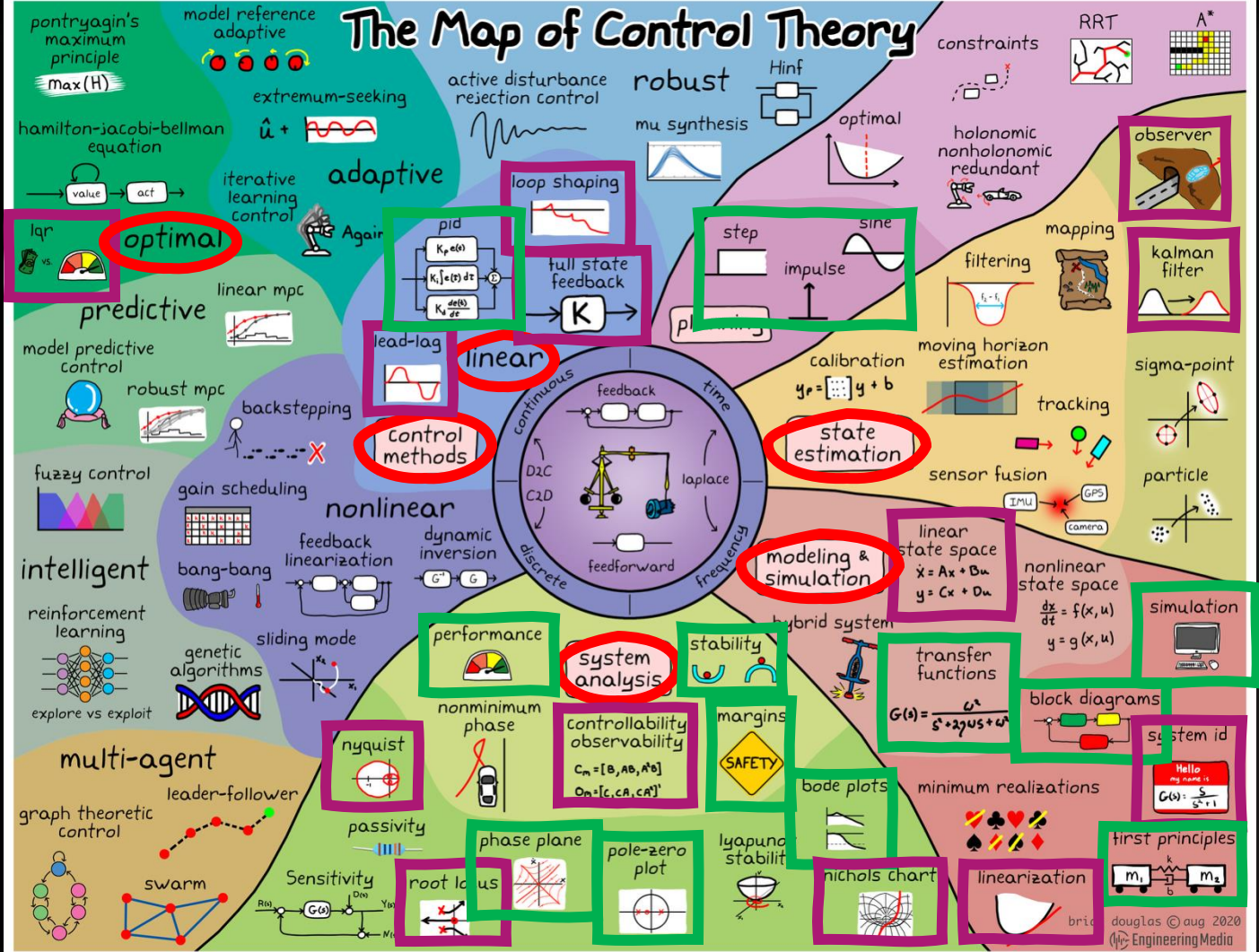
(After recap) Current feeling/comments...



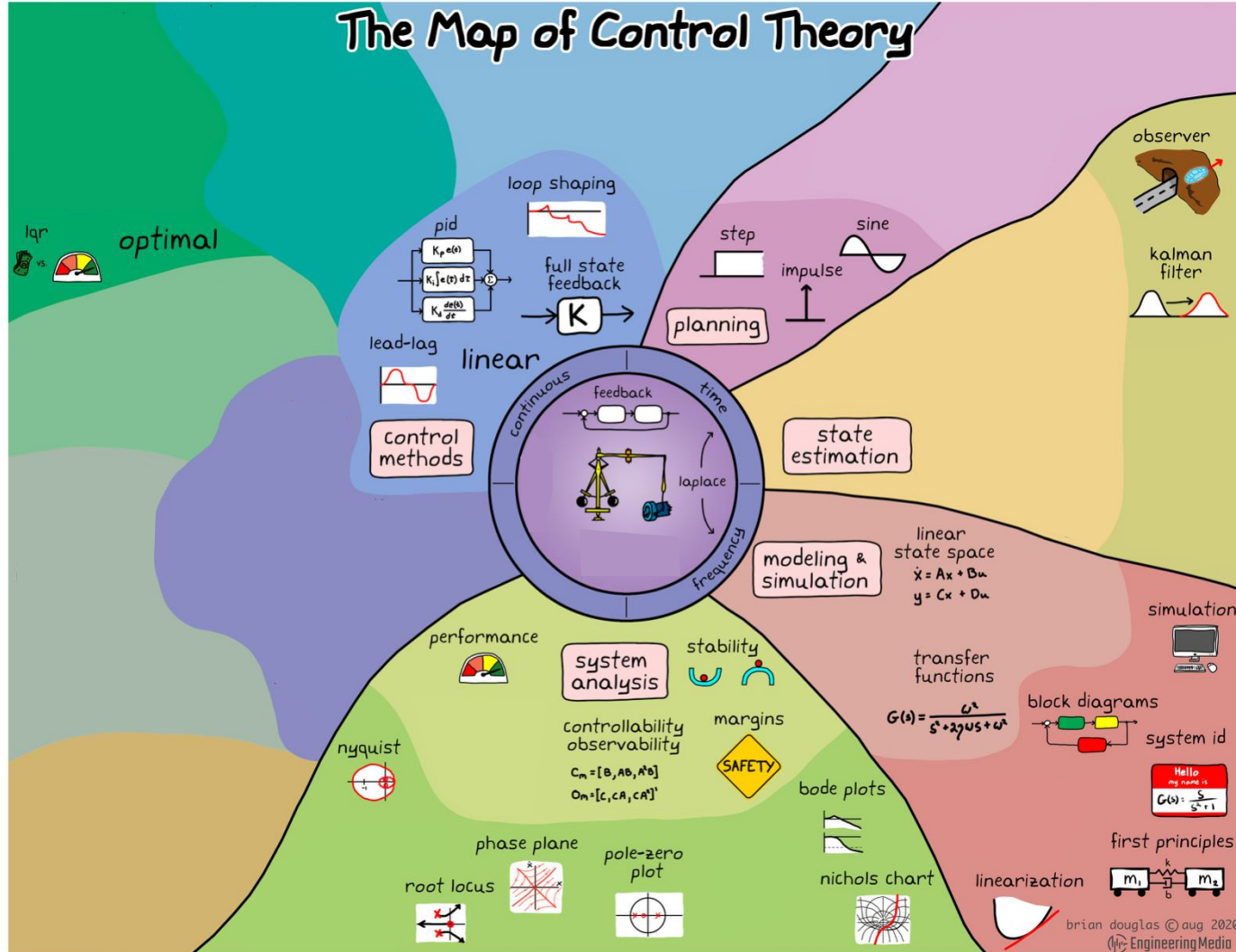
# Today

- Review syllabus
  - What did I assume you knew?
  - What did you actually know?
  - What do you want a refresher on?
  - What else do you want clarity on?
- Review delivery approach
  - What do you think so far? (Be honest).
  - How shall we proceed?
- Review and recap as necessary
- Introduce State Space models and control

# The Map of Control Theory



# The Map of Control Theory

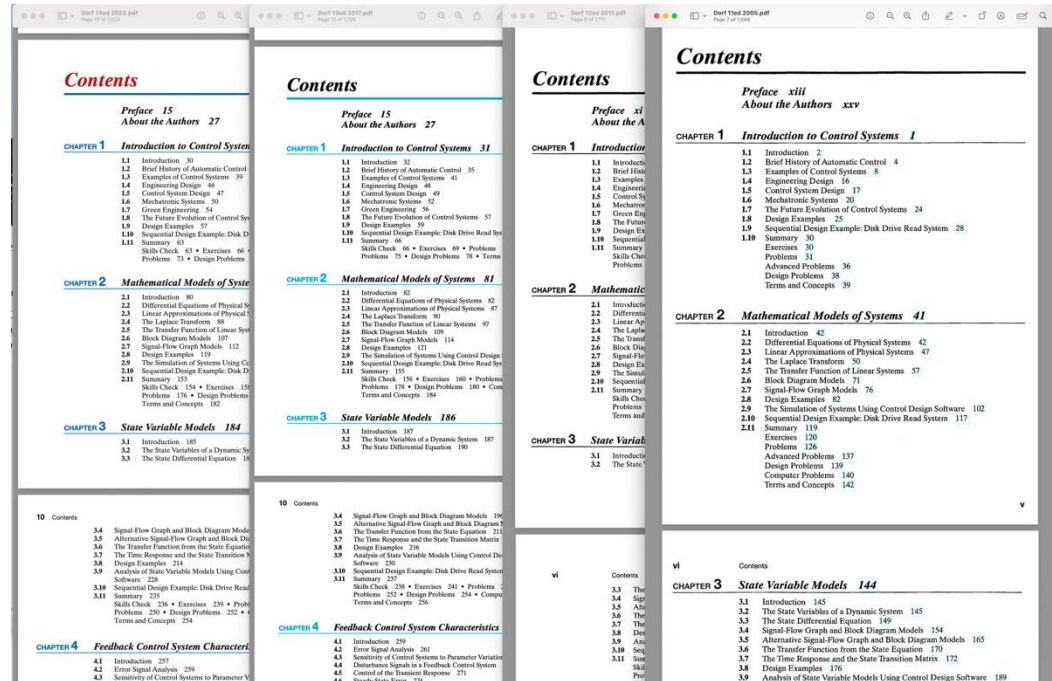




# Recommended text: access and mapping

- Dorf mapping doc on Bb
  - But last 4 versions (and more?) are largely identical
- Doc includes access and etiquette guidance

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*Of the greater teachers—  
when they are gone,  
their students will say:  
we did it ourselves.*

*Dedicated to*  
Lynda Ferrera Bishop  
  
and  
  
Joy MacDonald Dorf  
*In grateful appreciation*

---

*Dedicated to the memory of*  
Professor Richard C. Dorf





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# This hour - recap

- 1. Mathematical modelling
  - ODEs
  - LTI ODEs
  - Linearisation
  - Frequency domain methods
- 2. Feedback control
  - PID control
  - Block diagrams

- In Bb/Control/Recaps/link
  - Recap slides
  - Problem sheets
  - MATLAB code

**See slides and code in MATLAB drive**

## More practice:

- Modelling (ODEs  $\rightarrow$  TFs): Dorf ch2 (any version!)
- PID control: Brian Douglas – [Understanding PID control](#)



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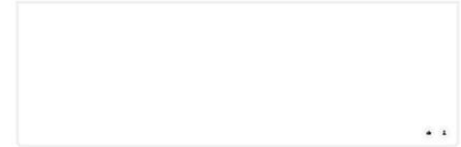
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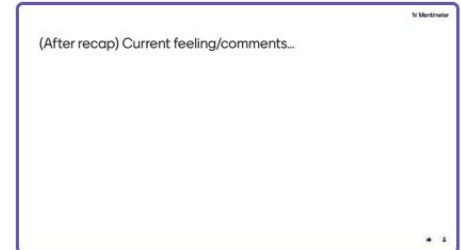
Control L3



(After concept outline) Current feeling...



(After recap) Current feeling/comments...



# STATE SPACE MODELS

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# Overview

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**See slides and code in MATLAB drive**

# **State Space – Steve's version**

$$\dot{\mathbf{x}}(t) = \mathbf{A}(t)\mathbf{x}(t) + \mathbf{B}(t)\mathbf{u}(t)$$

$$\mathbf{y}(t) = \mathbf{C}(t)\mathbf{x}(t) + \mathbf{D}(t)\mathbf{u}(t)$$

where:

$\mathbf{x}(\cdot)$  is called the "state vector",  $\mathbf{x}(t) \in \mathbb{R}^n$ ;

$\mathbf{y}(\cdot)$  is called the "output vector",  $\mathbf{y}(t) \in \mathbb{R}^q$ ;

$\mathbf{u}(\cdot)$  is called the "input (or control) vector",  $\mathbf{u}(t) \in \mathbb{R}^p$ ;

$\mathbf{A}(\cdot)$  is the "state (or system) matrix",  $\dim[\mathbf{A}(\cdot)] = n \times n$ ,

$\mathbf{B}(\cdot)$  is the "input matrix",  $\dim[\mathbf{B}(\cdot)] = n \times p$ ,

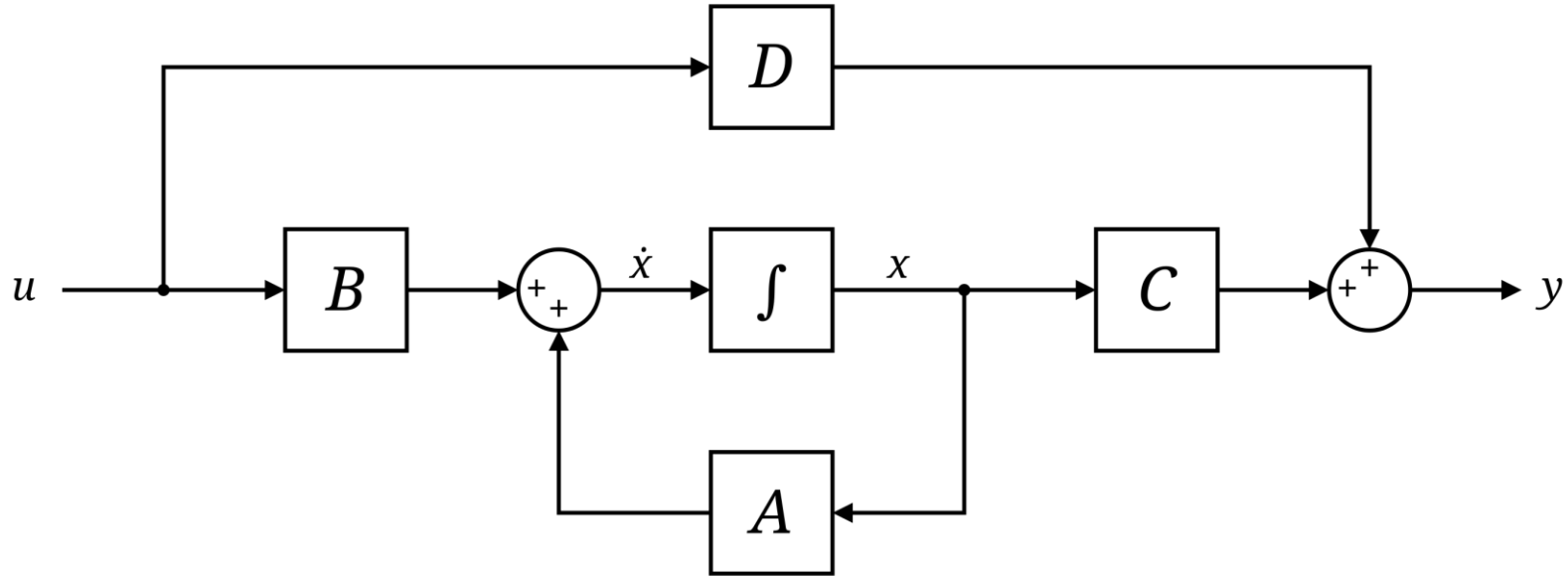
$\mathbf{C}(\cdot)$  is the "output matrix",  $\dim[\mathbf{C}(\cdot)] = q \times n$ ,

$\mathbf{D}(\cdot)$  is the "feedthrough (or feedforward) matrix" (in cases where the system model does not have a direct feedthrough,  $\mathbf{D}(\cdot)$  is the zero matrix),  $\dim[\mathbf{D}(\cdot)] = q \times p$ ,

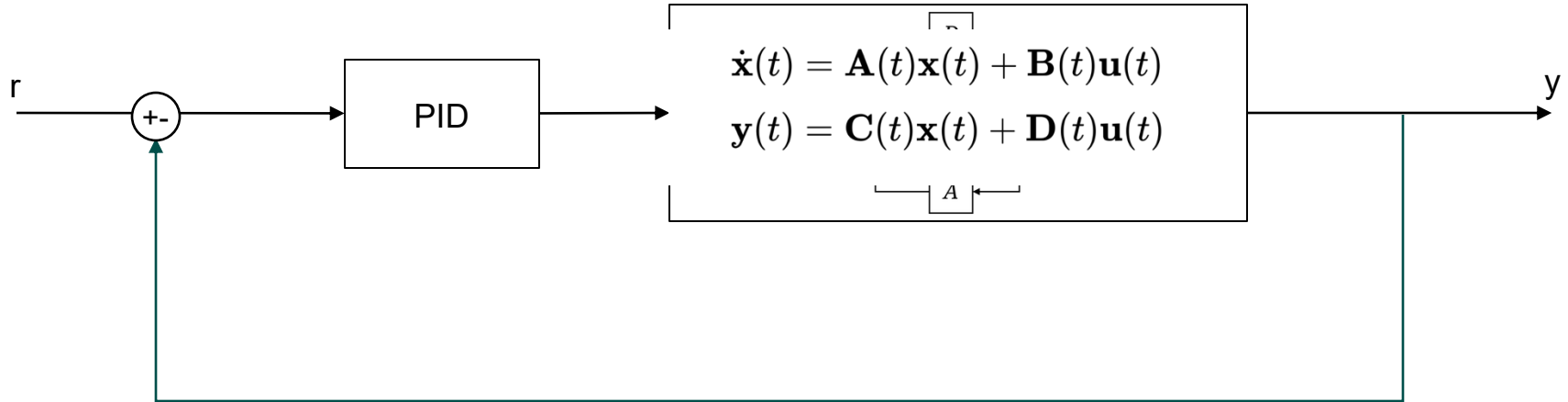
$$\dot{\mathbf{x}}(t) := \frac{d}{dt}\mathbf{x}(t).$$

Continuous time-invariant

$$\dot{\mathbf{x}}(t) = \mathbf{A}\mathbf{x}(t) + \mathbf{B}\mathbf{u}(t)$$
$$\mathbf{y}(t) = \mathbf{C}\mathbf{x}(t) + \mathbf{D}\mathbf{u}(t)$$



Remember! This is the dynamics of whatever system you put into it.  
Could be a 'plant' on its own, i.e.:



# What does it look like?

$$\dot{\mathbf{x}}(t) = \mathbf{A}(t)\mathbf{x}(t) + \mathbf{B}(t)\mathbf{u}(t)$$

$$\mathbf{y}(t) = \mathbf{C}(t)\mathbf{x}(t) + \mathbf{D}(t)\mathbf{u}(t)$$

$$\begin{bmatrix} \dot{\alpha} \\ \dot{q} \\ \dot{\theta} \end{bmatrix} = \begin{bmatrix} -0.313 & 56.7 & 0 \\ -0.0139 & -0.426 & 0 \\ 0 & 56.7 & 0 \end{bmatrix} \begin{bmatrix} \alpha \\ q \\ \theta \end{bmatrix} + \begin{bmatrix} 0.232 \\ 0.0203 \\ 0 \end{bmatrix} [\delta]$$

$$y = \begin{bmatrix} 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \alpha \\ q \\ \theta \end{bmatrix}$$

# What does it look like?

- Quanser model on MATLAB Drive



# Looking ahead

