

# **Design of Experiments for Engineers and Scientists**

# **Design of Experiments for Engineers and Scientists**

**Third Edition**

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# **Dedication**

This book is dedicated to my wife, Frenie, and my daughter, Evelyn,  
for always inspiring my work.

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# About the author

**Professor Jiju Antony** is recognised worldwide as a leader in Lean Six Sigma methodology for achieving and sustaining process excellence. He is currently serving as a professor of Operations and Supply Chain Management in Newcastle Business School at Northumbria University, Newcastle, England, United Kingdom. He worked as a professor of industrial and systems engineering at Khalifa University in Abu Dhabi, UAE. He is a Fellow of the Royal Statistical Society (United Kingdom), Fellow of the Chartered Quality Institute (CQI), Fellow of the Institute of Operations Management (FIOM), Fellow of the American Society for Quality (ASQ), Fellow of the Higher Education Academy, Fellow of the International Lean Six Sigma Institute, Fellow of the Institute of the Six Sigma Professionals (ISSP) and an academician of the International Academy of Quality (IAQ). He is a certified Lean Six Sigma Master Black Belt and has trained more than 1200 people as Lean Six Sigma Yellow, Green and Black Belts from more than 20 countries representing more than 180 organisations in the last 15 years. Professor Antony has coached and mentored several Lean Six Sigma projects from various companies in the United Kingdom ranging from manufacturing, service to public sector organisations, including the NHS, City Councils, NHS 24, Police Scotland, ACCESS, Business Stream, and a number of universities. He has authored more than 500 journal, conference and white papers and 14 text books. He has won the outstanding contribution to Quality Management Practice Award in 2019 from the Chartered Quality Institute (United Kingdom), Lifetime Achievement Award for his contribution to Lean Six Sigma from the International Lean Six Sigma Institute (United Kingdom) in 2020 and Outstanding Contribution to Six Sigma Practice award from the Institute of Six Sigma Professionals (United Kingdom) in 2021. His book 'Ten Commandments of Lean Six Sigma: A Practical Guide for Senior Managers' has won Walter Mazing Book Price in 2021 (International Academy of Quality, United States) and Crosby Medal (American Society of Quality, United States) in 2022. He has published more than 500 papers on various quality-related topics and is considered to be one of the highest in the world for the number of publications with more than 31,000 citations according to Google Scholar with an H-index of 91 and an i10-index of 300. He is the founder of the International Conference on Lean Six Sigma for Higher Education. He is currently serving as the editor of the International Journal of Lean Six Sigma and the International Journal of Quality and Reliability Management and an associate editor of the TQM and Business Excellence Journal (Europe's top-ranked Quality

Management Journal) and the TQM Journal (Emerald). He has worked as a strategic advisor for several companies especially on their journey of operational excellence. He has supervised more than 20 PhD students, among whom more than 12 were senior managers from world-class companies.

# Preface

Design of Experiments (DOE) is a powerful technique used for both exploring new processes and gaining increased knowledge of existing processes, followed by optimising these processes for achieving world-class performance. My involvement in promoting and training in the use of DOE dates back to the mid-1990s. There are plenty of books available in the market today on this subject written by classic statisticians, although the majority of them are better suited to other statisticians than to run-of-the-mill industrial engineers and business managers with limited mathematical and statistical skills.

DOE never has been a favourite technique for many of today's engineers and managers in organisations due to the number crunching involved and the statistical jargon incorporated into the teaching mode by many statisticians. This book is targeted to people who have either been intimidated by their attempts to learn about DOE or who have never appreciated the true potential of DOE for achieving breakthrough improvements in product quality and process efficiency.

This book gives a solid introduction to the technique through a myriad of practical examples and case studies. The third edition of the book has incorporated two new chapters and both cover the status of DOE in the service environment. In addition to the two new chapters, two new case studies on DoE in non-manufacturing settings have been included. Readers of this book will develop a sound understanding of the theory of DOE and practical aspects of how to design, analyse and interpret the results of a designed experiment. Throughout this book, the emphasis is on the simple but powerful graphical tools available for data analysis and interpretation. All of the graphs and figures in this book were created using Minitab for Windows.

I sincerely hope that practising industrial engineers and managers as well as researchers in academic world will find this book useful in learning how to apply DOE in their own work environment. The book will also be a useful resource for people involved in Six Sigma training and projects related to design optimisation and process performance improvements. In fact, I have personally observed that the number of applications of DOE in non-manufacturing sectors has increased significantly because of the methodology taught to Six Sigma professionals such as Six Sigma Green Belts and Black Belts. However, the applications of DOE in the service sector are still under-researched and under-reported in the extant literature. This situation would change in the service industry due to the evolution of Industry 4.0 where practitioners and researchers can integrate AI, machine learning with DOE in the near future.

The third edition has more chapters dedicated to DOE for non-manufacturing processes. As a mechanical engineer, I was not convinced about the application of DOE in the context of the service industry and public sector organisations including higher education. I have included one more case study from the higher education sector. I firmly believe that DOE can be applied to any industrial setting, although there will be more challenges and barriers in the non-manufacturing sector compared to traditional manufacturing companies.

I hope that this book inspires readers to get into the habit of applying DOE for problem-solving and process troubleshooting. I strongly recommend that readers of this book continue on a more advanced reference to learn about topics which are not covered here. I am indebted to many contributors and gurus for the development of various experimental design techniques, especially Sir Ronald Fisher, Plackett and Burman, Professor George Box, Professor Douglas Montgomery, Dr. Genichi Taguchi and Dr. Dorian Shainin.

**Jiju Antony**

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I would like to express my deepest appreciation to Hayley Grey and Cari Owen for their incessant support and forbearance during the course of this project. Finally, I express my sincere thanks to my wife, Frenie, and daughter, Evelyn, for their encouragement and patience as the book stole countless hours away from our family activities.

# Introduction to industrial experimentation

1

## 1.1 Introduction

Experiments are performed today in many manufacturing organisations to increase our understanding and knowledge of various manufacturing processes. Experiments in manufacturing companies are often conducted in a series of trials or tests which produce quantifiable outcomes. For continuous improvement in product/process quality, it is fundamental to understand the process behaviour; the amount of variability and its impact on processes. In an engineering environment, experiments are often conducted to explore, estimate or confirm. Exploration refers to understanding the data from the process. Estimation refers to determining the effects of process variables or factors on the output performance characteristic. Confirmation implies verifying the predicted results obtained from the experiment.

In manufacturing processes, it is often of primary interest to explore the relationships between the key input process variables (or factors) and the output performance characteristics (or quality characteristics). For example, in a metal cutting operation, cutting speed, feed rate, type of coolant, depth of cut, etc. can be treated as input variables and the surface finish of the finished part can be considered as an output performance characteristic. In service processes, it is often more difficult to understand what is to be measured; moreover, the process variability in the service context may be attributed to human factors, which are difficult to control. Furthermore, the delivery of service quality is heavily dependent on the situational influences of the person who provides the service.

One of the common approaches employed by many engineers today in manufacturing companies is One-Variable-At-a-Time (OVAT), where we vary one variable at a time and keep all other variables in the experiment fixed. This approach depends upon guesswork, luck, experience and intuition for its success. Moreover, this type of experimentation requires large quantities of resources to obtain a limited amount of information about the process. OVAT experiments often are unreliable, inefficient and time consuming and may yield false optimum conditions for the process.

Statistical thinking and statistical methods play an important role in planning, conducting, analysing and interpreting the data from engineering experiments. Statistical thinking tells us how to deal with variability, and how to collect and use data so that effective decisions can be made about the processes or systems we deal with every day. When several variables influence a certain characteristic of a product, the best strategy is then to design an experiment so that valid, reliable and sound conclusions can be drawn effectively, efficiently and economically. In a

designed experiment we often make deliberate changes in the input variables (or factors) and then determine how the output functional performance varies accordingly. It is important to note that not all variables affect the performance in the same manner. Some may have strong influences on the output performance, some may have medium influences and some may have no influence at all. Therefore the objective of a carefully planned designed experiment is to understand which set of variables in a process affect the performance most and then determine the best levels for these variables to obtain satisfactory output functional performance in products. Moreover, we can also set the levels of unimportant variables to their most economic settings. This would have an immense impact on financial savings to a company's bottom line ([Clements, 1995](#)).

Design of Experiments (DOE) was developed in the early 1920s by Sir Ronald Fisher at the Rothamsted Agricultural Field Research Station in London, England. His initial experiments were concerned with determining the effect of various fertilisers on different plots of land. The final condition of the crop was dependent not only on the fertiliser but also on a number of other factors (such as underlying soil condition, moisture content of the soil, etc.) of each of the respective plots. Fisher used DOE that could differentiate the effect of fertiliser from the effects of other factors. Since then, DOE has been widely accepted and applied in biological and agricultural fields. A number of successful applications of DOE have been reported by many US and European manufacturers over the last 15 years or so. The potential applications of DOE in manufacturing processes include ([Montgomery et al., 1998](#)):

- improved process yield and stability
- improved profits and return on investment
- improved process capability
- reduced process variability and hence better product performance consistency
- reduced manufacturing costs
- reduced process design and development time
- heightened engineers' morale with success in solving chronic problems
- increased understanding of the relationship between key process inputs and output(s)
- increased business profitability by reducing scrap rate, defect rate, rework, retest, etc.

Similarly, the potential applications of DOE in service processes include:

- identifying the key service process or system variables which influence the process or system performance
- identifying the service design parameters which influence the service quality characteristics in the eyes of customers
- minimising the time to respond to customer complaints
- minimising errors on service orders
- reducing the service delivery time to customers (e.g., banks, restaurants)
- reducing the turn-around time in producing reports to patients in a healthcare environment, and so on.

Industrial experiments involve a sequence of activities:

1. *Hypothesis* – an assumption that motivates the experiment
2. *Experiment* – a series of tests conducted to investigate the hypothesis

3. *Analysis* – understanding the nature of data and performing statistical analysis of the collected data from the experiment
4. *Interpretation* – understanding the results of the experimental analysis
5. *Conclusion* – stating whether or not the original set hypothesis is true or false. Very often more experiments are to be performed to test the hypothesis and sometimes we establish a new hypothesis that requires more experiments.

Consider a welding process where the primary concern of interest to engineers is the strength of the weld and the variation in the weld strength values. Through scientific experimentation, we can determine what factors mostly affect the mean weld strength and the variation in weld strength. Through experimentation, one can also predict the weld strength under various conditions of key input welding machine parameters or factors (e.g., weld speed, voltage, welding time, weld position, etc.).

For the successful application of an industrial designed experiment, we generally require the following skills:

- *Planning skills*: Understanding the significance of experimentation for a particular problem, time and experimental budget required for the experiment, how many people are involved with the experimentation, establishing who is doing what, etc.
- *Statistical skills*: The statistical analysis of data obtained from the experiment, assignment of factors and interactions to various columns of the design matrix (or experimental layout), interpretation of results from the experiment for making sound and valid decisions for improvement, etc.
- *Teamwork skills*: Understanding the objectives of the experiment and having a shared understanding of the experimental goals to be achieved, better communication among people with different skills and learning from one another, brainstorming of factors for the experiment by team members, etc.
- *Engineering skills*: Determination of the number of levels of each factor and the range at which each factor can be varied, determination of what to measure within the experiment, determination of the capability of the measurement system in place, determination of what factors can be controlled and what cannot be controlled for the experiment, etc.

## 1.2 Some fundamental and practical issues in industrial experimentation

An engineer is interested in measuring the yield of a chemical process, which is influenced by two key process variables (or control factors). The engineer decides to perform an experiment to study the effects of these two variables on the process yield. The engineer uses an OVAT approach to experimentation. The first step is to keep the temperature constant ( $T_1$ ) and vary the pressure from  $P_1$  to  $P_2$ . The experiment is repeated twice and the results are illustrated in [Table 1.1](#). The engineer conducts four experimental trials.

The next step is to keep the pressure constant ( $P_1$ ) and vary the temperature from  $T_1$  to  $T_2$ . The results of the experiment are given in [Table 1.2](#).

The engineer has calculated the average yield values for only three combinations of temperature and pressure:  $(T_1, P_1)$ ,  $(T_1, P_2)$  and  $(T_2, P_1)$ . The engineer concludes

**Table 1.1** The effects of varying pressure on process yield.

Trial	Temperature	Pressure	Yield	Average yield (%)
1	$T_1$	$P_1$	55, 57	56
2	$T_1$	$P_2$	63, 65	64

**Table 1.2** The effects of varying temperature on process yield.

Trial	Temperature	Pressure	Yield	Average yield (%)
3	$T_1$	$P_1$	55, 57	56
4	$T_2$	$P_1$	60, 62	61

from the experiment that the maximum yield of the process can be attained by corresponding to  $(T_1, P_2)$ . The question then arises as to what should be the average yield corresponding to the combination  $(T_2, P_2)$ ? The engineer was unable to study this combination as well as the interaction between temperature and pressure. *Interaction between two factors exists when the effect of one factor on the response or output is different at different levels of the other factor.* The difference in the average yield between the trials one and two provides an estimate of the effect of pressure. Similarly, the difference in the average yield between trials three and four provide an estimate of the effect of temperature. *An effect of a factor is the change in the average response due to a change in the levels of a factor.* The effect of pressure was estimated to be 8% (i.e.  $64 - 56$ ) when temperature was kept constant at ' $T_1$ '.' There is no guarantee whatsoever that the effect of pressure will be the same when the conditions of temperature change. Similarly the effect of temperature was estimated to be 5% (i.e.  $61 - 56$ ) when pressure was kept constant at ' $P_1$ '.' It is reasonable to say that we do not get the same effect of temperature when the conditions of pressure change. Therefore the OVAT approach to experimentation can be misleading and may lead to unsatisfactory experimental conclusions in real-life situations. Moreover, the success of the OVAT approach to experimentation relies on guesswork, luck, experience and intuition ([Antony, 1997](#)). This type of experimentation is inefficient in that it requires large resources to obtain a limited amount of information about the process. In order to obtain a reliable and predictable estimate of factor effects, it is important that we vary the factors simultaneously at their respective levels. In the above example, the engineer should have varied the levels of temperature and pressure simultaneously to obtain reliable estimates of the effects of temperature and pressure. The focus of this book is to explain the rationale behind such carefully planned and well-designed experiments.

A study carried out at the University of Navarra, Spain, has shown that 80% of the companies (sample size of 128) in the Basque Country conduct experimentation using the OVAT strategy. Moreover, it was found that only 20% of companies carry out experimentation with a pre-established statistical methodology ([Tanco et al., 2008](#)).

The findings of Tanco et al. have also revealed that the size of the industry plays a large part in DOE awareness; only 22% of small companies are familiar with DOE, as compared with 43% of medium-sized companies and 76% of large companies (sample size of 133).

## 1.3 Statistical thinking and its role within DOE

One of the success factors for the effective deployment of DOE in any organisation is the uncompromising commitment of the senior management team and visionary leadership. However, it is not essential that the senior managers have a good technical knowledge of the working mechanisms of DOE, although the author argues that they should have a good understanding of the term ‘statistical thinking.’ Statistical thinking is a philosophy of learning and action based on the following three fundamental principles (Snee, 1990):

1. All work occurs in a system of interconnected processes.
2. Variation exists in all processes.
3. Understanding and reducing variation are the key to success.

The importance of statistical thinking derives from the fundamental principle of quality put forth by Deming: ‘*Reduce variation and you improve quality.*’ Customers of today and tomorrow value products and services that have consistent performance, which can be achieved by systematically eliminating variation in business processes (American Society of Quality, 1996). However, our managers lack statistical thinking and some of the possible reasons for this are as follows:

- *A shift in the organisation’s priorities* – Global competition has forced managers to rethink how organisations are run and to search for better ways to manage. Problem solving in manufacturing and R&D, while important, is not seen as particularly relevant to the needs of management.
- *Managers view statistics as a tool for ‘fire fighting’ actions* – One of the most difficult challenges for every manager is to figure out how to use statistical thinking effectively to help them make effective decisions. When a problem arises in the business, managers want to fix it as soon as possible so that they can deal with their day-to-day activities. However, what they do not realise is that the majority of problems are in systems or processes that can only be tackled with the support of senior management team. The result is that management spends too much time ‘fire fighting,’ solving the same problem again and again because the system was not changed. These scenarios are as follows:
- *A change in the mindset of people in the enterprise* – Philosopher George Bernard Shaw once said, ‘If you cannot change your mind, you cannot change anything.’ It is clear that managers, quality professionals and statisticians all have new roles that require new skills. Change implies discontinuity and the destruction of familiar structures and relationships. Change can be resisted because it involves confrontation of the unknown and loss of the familiar (Huczynski and Buchanan, 2001).
- *Fear of statistics by managers* – Even if managers were taught statistics at university, it was usually focused on complex maths and formulas rather than the application of statistical tools for problem solving and an effective decision-making process. Usually managers have

their first experience with statistical thinking in a workshop inside the company, applying some tools with the guidance of an expert. Although this is the best learning method for understanding and experiencing statistical thinking, managers may still struggle to apply the principles to a different problem. This fundamental problem can be tackled by teaching usable and practical statistical techniques through real case studies at the university level.

## Exercises

1. Why do we need to perform experiments in organisations?
2. What are the limitations of the OVAT approach to experimentation?
3. What types of skills are required to make an experiment successful in organisations?
4. Why is statistical thinking highly desirable for senior managers and leaders of organisations?

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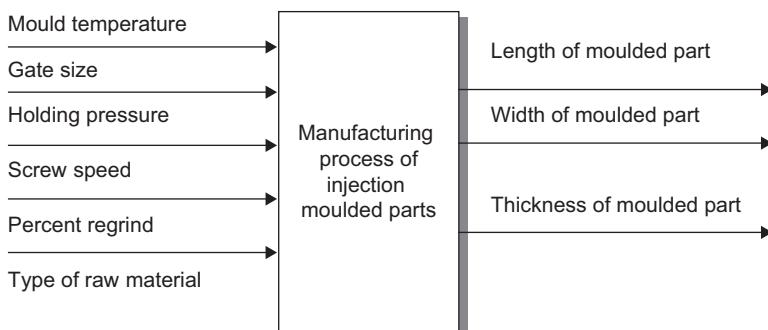
# Fundamentals of design of experiments

2

## 2.1 Introduction

In order to properly understand a designed experiment, it is essential to have a good understanding of the process. A process is the transformation of inputs into outputs. In the context of manufacturing, inputs are factors or process variables such as people, materials, methods, environment, machines, procedures, etc. and outputs can be performance characteristics or quality characteristics of a product. Sometimes, an output can also be referred to as response. In the context of Six Sigma, this is often referred to as critical-to-quality characteristics.

In performing a designed experiment, we will intentionally make changes to the input process or machine variables (or factors) in order to observe corresponding changes in the process output. If we are dealing with a new product development process, we will make changes to the design parameters in order to make the design performance insensitive to all sources of variation (Montgomery, 2001). The information gained from properly planned, executed and analysed experiments can be used to improve functional performance of products, to reduce the scrap rate or rework rate, to reduce product development cycle time, to reduce excessive variability in production processes, to improve throughput yield of processes, to improve the capability of processes, etc. Let us suppose that an experimenter wishes to study the influence of five variables or factors on an injection moulding process. Fig. 2.1 illustrates an example of an injection moulding process with possible inputs and outputs. The typical outputs of an injection moulding process can be length, thickness, width etc. of an injection moulded part. However, these outputs can be dependant on a



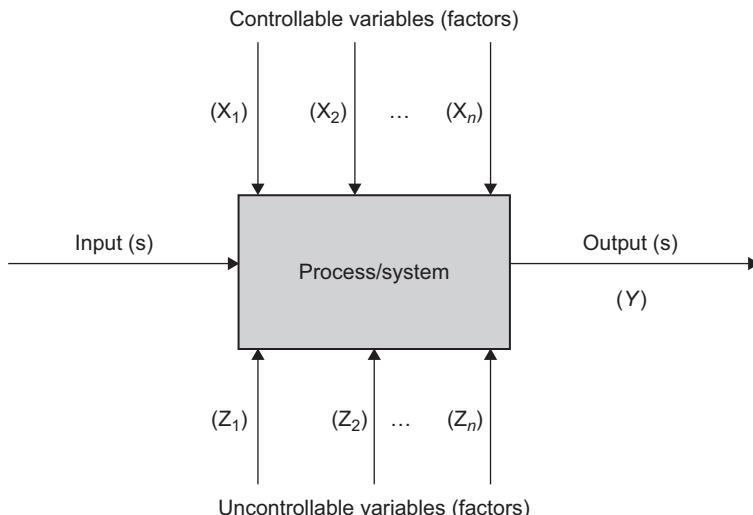
**Figure 2.1** Illustration of an injection moulding process.

number of input variables such as mould temperature, injection pressure, injection speed, etc. which could have an impact on the above mentioned outputs. The purpose of a designed experiment is to understand the relationship between a set of input variables and an output or outputs.

Now consider a wave soldering process where the output is the number of solder defects. The possible input variables which might influence the number of solder defects are type of flux, type of solder, flux coating depth, solder temperature, etc. More recently, DOE has been accepted as a powerful technique in the service industry and there have been some major achievements. For instance, a credit card company in the US has used DOE to increase the response rate to their mailings. They have changed the colour, envelope size, character type and text within the experiment.

In real-life situations, some of the process variables or factors can be controlled fairly easily and some of them are difficult or expensive to control during normal production or standard conditions. Fig. 2.2 illustrates a general model of a process or system.

In Fig. 2.2, output(s) are performance characteristics which are measured to assess process/product performance. Controllable variables (represented by  $X$ 's) can be varied easily during an experiment and such variables have a key role to play in the process characterisation. Uncontrollable variables (represented by  $Z$ 's) are difficult to control during an experiment. These variables or factors are responsible for variability in product performance or product performance inconsistency. It is important to determine the optimal settings of  $X$ 's in order to minimise the effects of  $Z$ 's. This is the fundamental strategy of robust design (Roy, 2001).



**Figure 2.2** General model of a process/system.

## 2.2 Basic principles of DOE

DOE refers to the process of planning, designing and analysing the experiment so that valid and objective conclusions can be drawn effectively and efficiently. In order to draw statistically sound conclusions from the experiment, it is necessary to integrate simple and powerful statistical methods into the experimental design methodology (Vecchio, 1997). The success of any industrially designed experiment depends on sound planning, appropriate choice of design, statistical analysis of data and teamwork skills.

In the context of DOE in manufacturing, one may come across two types of process variables or factors: qualitative and quantitative. For quantitative factors, one must decide on the range of settings and how they are to be measured and controlled during the experiment. For example, in the above injection moulding process, screw speed, mould temperature, etc. are examples of quantitative factors. Qualitative factors are discrete in nature. Type of raw material, type of catalyst, type of supplier, etc. are examples of qualitative factors. A factor may take different levels, depending on the nature of the factor – quantitative or qualitative. A qualitative factor generally requires more levels when compared to a quantitative factor. Here the term ‘level’ refers to a specified value or setting of the factor being examined in the experiment. For instance, if the experiment is to be performed using three different types of raw materials, then we can say that the factor – the type of raw material – has three levels.

In the DOE terminology, a trial or run is a certain combination of factor levels whose effect on the output (or performance characteristic) is of interest.

The three principles of experimental design, namely randomisation, replication and blocking, can be utilised in industrial experiments to improve the efficiency of experimentation (Antony, 1997). These principles of experimental design are applied to reduce or even remove experimental bias. It is important to note that large experimental bias could result in wrong optimal settings or, in some cases, could mask the effect of the really significant factors. Thus an opportunity for gaining process understanding is lost, and a primary element for process improvement is overlooked.

### 2.2.1 Randomisation

We all live in a non-stationary world, a world in which noise factors (or external disturbances) will never stay still. For instance, the manufacture of a metal part is an operation involving people, machines, measurement, environment, etc. The parts of the machine are not fixed entities; they wear out over a period of time and their accuracy is not constant over time. The attitudes of the people who operate the machines vary from time to time. If you believe your system or process is stable, you do not then need to randomise the experimental trials. On the other hand, if you believe your process is unstable and without randomisation, the results will be meaningless and misleading; you then need to think about randomisation of experimental trials (Box, 1990). If the process is very unstable and randomisation would make your

experiment impossible, then do not run the experiment. You may have to look at process control methods to bring your process into a state of statistical control.

While designing industrial experiments, there are factors, such as power surges, operator errors, fluctuations in ambient temperature and humidity, raw material variations, etc. which may influence the process output performance because they are often expensive or difficult to control. Such factors can adversely affect the experimental results and therefore must be either minimised or removed from the experiment. Randomisation is one of the methods experimenters often rely on to reduce the effect of experimental bias. The purpose of randomisation is to remove all sources of extraneous variation which are not controllable in real-life settings ([Leon et al., 1993](#)). By properly randomising the experiment, we assist in averaging out the effects of noise factors that may be present in the process. In other words, randomisation can ensure that all levels of a factor have an equal chance of being affected by noise factors ([Barker, 1990](#)). Dorian Shainin accentuates the importance of randomisation as ‘experimenters’ insurance policy’. He pointed out that *‘failure to randomise the trial conditions mitigates the statistical validity of an experiment’*. Randomisation is usually done by drawing numbered cards from a well-shuffled pack of cards, by drawing numbered balls from a well-shaken container or by using tables of random numbers.

Sometimes experimenters encounter situations where randomisation of experimental trials is difficult to perform due to cost and time constraints. For instance, temperature in a chemical process may be a hard-to-change factor, making complete randomisation of this factor almost impossible. Under such circumstances, it might be desirable to change the factor levels of temperature less frequently than others. In such situations, *restricted randomisation* can be employed.

It is important to note that in a classical DOE approach, complete randomisation of the experimental trials is advocated, whereas in the Taguchi approach to experimentation, the incorporation of noise factors into the experimental layout will supersede the need for randomisation. The following questions are useful if you decide to apply randomisation strategy to your experiment.

- What is the cost associated with change of factor levels?
- Have we incorporated any noise factors in the experimental layout?
- What is the set-up time between trials?
- How many factors in the experiment are expensive or difficult to control?
- Where do we assign factors whose levels are difficult to change from one to another level?

### **2.2.2 Replication**

In all industrial designed experiments, some variation is introduced because of the fact that the experimental units such as people, batches of materials, machines, etc. cannot be physically identical. Replication is a process of running the experimental trials in a random sequence. Replication means repetitions of an entire experiment or a portion of it, under more than one condition. Replication has three important

properties. The first property is that it allows the experimenter to obtain a more accurate estimate of the experimental error, a term which represents the differences that would be observed if the same experimental settings were applied several times to the same experimental units (operator, machine, material, gauges, etc.). The second property is that it permits the experimenter to obtain a more precise estimate of the factor/interaction effect. The third property is that replication can decrease the experimental error and thereby increase precision. If the number of replicates is equal to one or unity, we would not then be able to make satisfactory conclusions about the effect of either factors or interactions. The factor or interaction effect could be significant due to experimental error. On the other hand, if we have a sufficient number of replicates, we would safely be making satisfactory inferences about the effect of factors/interactions.

Replication can result in a substantial increase in the time needed to conduct an experiment. Moreover, if the material is expensive, replication may lead to exorbitant material costs. Any bias or experimental error associated with set-up changes will be distributed evenly across the experimental runs or trials using replication. The use of replication in real life must be justified in terms of time and cost.

Many experimenters use the terms ‘repetition’ and ‘replication’ interchangeably. Technically speaking, however, they are not the same. In repetition, an experimenter may repeat an experimental trial condition a number of times as planned, before proceeding to the next trial in the experimental layout. The advantage of this approach is that the experimental set-up cost should be minimal. However, a set-up error is unlikely to be detected or identified.

### 2.2.3 Blocking

Blocking is a method of eliminating the effects of extraneous variation due to noise factors and thereby improving the efficiency of experimental design. The main objective is to eliminate unwanted sources of variability such as batch-to-batch, day-to-day, shift-to-shift, etc. The idea is to arrange similar or homogenous experimental runs into blocks (or groups). Generally, a block is a set of relatively homogeneous experimental conditions (Bisgaard, 1994). The blocks can be batches of raw materials, different operators, different vendors, etc. Observations collected under the same experimental conditions (i.e. same day, same shift, etc.) are said to be in the same block. Variability between blocks must be eliminated from the experimental error, which leads to an increase in the precision of the experiment. The following two examples illustrate the role of blocking in industrial designed experiments.

#### Example 2.1

A metallurgist wants to improve the strength of a steel product. Four factors are being considered for the experiment, which might have some impact on the strength. It is decided to study each factor at 2-levels (i.e. a low setting  
*(Continued)*

**(cont'd)**

and a high setting). An eight-trial experiment is chosen by the experimenter but it is possible to run only four trials per day. Here each day can be treated as a separate block.

**Example 2.2**

An experiment in a chemical process requires two batches of raw material for conducting the entire experimental runs. In order to minimise the effect of batch-to-batch material variability, we need to treat batch of raw material as a noise factor. In other words, each batch of raw material would form a block.

## 2.3 Degrees of freedom

In the context of statistics, the term ‘degrees of freedom’ is the number of independent and fair comparisons that can be made in a set of data. For example, consider the heights of two students, say John and Kevin. If the height of John is  $H_J$  and that of Kevin is  $H_K$ , then we can make only one fair comparison ( $H_J - H_K$ ).

In the context of DOE, the number of degrees of freedom associated with a process variable is equal to one less than the number of levels for that factor (Belavendram, 1995). For example, an engineer wishes to study the effects of reaction temperature and reaction time on the yield of a chemical process. Assume each factor was studied at 2-levels. The number of degrees of freedom associated with each factor is equal to unity or 1 (i.e.  $2 - 1 = 1$ ).

$$\therefore \text{Degrees of freedom for a main effects} = \text{number of levels}-1$$

The number of degrees of freedom for the entire experiment is equal to one less than the total number of data points or observations. Assume that you have performed an eight-trial experiment and that each trial condition was replicated twice. The total number of observations in this case is equal to 16 and therefore the total degrees of freedom for the experiment is equal to 15 (i.e.  $16 - 1$ ).

The degrees of freedom for an interaction is equal to the product of the degrees of freedom associated with each factor involved in that particular interaction effect. For instance, in the above yield example, the degrees of freedom for both reaction temperature and reaction time are equal to one and therefore, the degrees of freedom for its interaction effect is also equal to unity.

Assume that an experimenter wishes to study the effect of four process or design parameters at 3-levels. The degrees of freedom required for studying all the main effects is equal to  $8((3 - 1) \times 4 = 8)$ . The degrees of freedom for studying one

interaction in this case is equal to  $4((3 - 1) \times (3 - 1) = 4)$ . The degrees of freedom therefore required for studying all six interactions (i.e. AB, AC, BC, BD, AD and CD) is equal to 24.

## 2.4 Confounding

The term ‘confounding’ refers to the combining influences of two or more factor effects in one measured effect. In other words, one cannot estimate factor effects and their interaction effects independently. Effects which are confounded are called aliases. A list of the confoundings which occur in an experimental design is called an alias structure or a confounding pattern. The confounding of effects is simple to illustrate. Suppose two factors, say mould temperature and injection speed, are investigated at 2-levels. Five response values are taken when both factors are at their lower levels and high levels, respectively. The results of the experiment (i.e. mean response) are given in [Table 2.1](#).

The effect of mould temperature is equal to  $82.75 - 75.67 = 7.08$ . Here effect refers to the change in mean response due to a change in the levels of a factor.

The effect of injection speed is also the same as that of mould temperature (i.e.  $82.75 - 75.67$ ). So is the calculated effect actually due to injection speed or to mould temperature? One cannot simply tell this as the effects are confounded.

### 2.4.1 Design resolution

Design resolution ( $R$ ) is a summary characteristic of aliasing or confounding patterns. The degree to which the main effects are aliased with the interaction effects (two-factor or higher) is represented by the resolution of the corresponding design. Obviously, we don't prefer the main effects to be aliased with other main effects. A design is of resolution  $R$  if no  $p$ -factor effect is aliased with another effect containing less than  $(R - p)$  factors. For designed experiments, designs of resolution III, IV and V are particularly important.

Design resolution identifies for a specific design the order of confounding of the main effects and their interactions. It is a key tool for determining what fractional factorial design will be the best choice for a given problem ([Kolarik, 1995](#)). More information on full and fractional factorial designs can be seen in the later chapters of this book.

**Table 2.1** Example of confounding.

Mould temperature	Injection speed	Mean response
Low level	Low level	75.67
High level	High level	82.75

*Resolution III designs:* These are designs in which no main effects are confounded with any other main effect, but main effects are confounded with two-factor interactions and two-factor interactions may be confounded with each other. For example, studying three factors or process parameters at 2-levels in four trials or runs is a resolution III design. In this case, each main effect is confounded with two-factor or second-order interactions.

*Resolution IV designs:* These are designs in which no main effects are confounded with any other main effect or with any two-factor interaction effects, but two-factor interaction effects are confounded with each other. For example, studying four factors or process parameters at 2-levels in eight trials or runs is a resolution IV design. In this case, each two-factor interaction is confounded with other two-factor interactions.

*Resolution V designs:* These are designs in which main effects are not confounded with other main effects, two-factor interactions or three-factor interactions, but two-factor interactions are confounded with three-factor interactions. For example, studying 5 factors or process parameters at 2-levels in 16 trials or runs is a resolution V design. In this case, each two-factor interaction is confounded with three-factor or third-order interactions.

## **2.4.2 Metrology considerations for industrial designed experiments**

For industrial experiments, the response or quality characteristic will have to be measured either by direct or indirect methods. These measurement methods produce variation in the response. Measurement is a process and varies, just as all processes vary. Identifying, separating and removing the measurement variation leads to improvements to the actual measured values obtained from the use of the measurement process.

The following characteristics need to be considered for a measurement system:

- *Accuracy:* It refers to the degree of closeness between the measured value and the true value or reference value.
- *Precision:* It is a measure of the scatter of results of several observations and is not related to the true value. It is a comparative measure of the observed values and is only a measure of the random errors. It is expressed quantitatively as the standard deviation of observed values from repeated results under identical conditions.
- *Stability:* A measurement system is said to be stable if the measurements do not change over time. In other words, they should not be adversely influenced by operator and environmental changes.
- *Capability:* A measurement system is capable if the measurements are free from bias (accurate) and sensitive. A capable measurement system requires sensitivity (the variation around the average should be small compared to the specification limits or process spread and accuracy).

## **2.4.3 Measurement system capability**

The goal of a measurement system capability study is to understand and quantify the sources of variability present in the measurement system. Repeatability and Reproducibility (R&R) studies analyse the variation of measurements of a gauge and the variation of measurements by operators, respectively. Repeatability refers

to the variation in measurements obtained when an operator uses the same gauge several times for measuring the identical characteristic on the same part. Reproducibility, on the other hand, refers to the variation in measurements when several operators use the same gauge for measuring the identical characteristic on the same part. It is important to note that total variability in a process can be broken down into variability due to product (or parts variability) and variability due to measurement system. The variability due to measurement system is further broken into variability due to gauge (i.e. repeatability) and reproducibility. Reproducibility can be further broken into variability due to operators and variability due to (part  $\times$  operator) interaction ([Montgomery and Runger, 1993](#)).

A measurement system is considered to be capable and adequate if it satisfies the following criterion:

$$\frac{P}{T} \leq 10\% \quad (2.1)$$

where  $P/T$  = Precision-to-Tolerance ratio, which is given by

$$\frac{P}{T} = \frac{6\hat{\sigma}_{\text{measurement error}}}{\text{USL}-\text{LSL}} \quad (2.2)$$

where USL = Upper Specification Limit of a quality characteristic, LSL = Lower Specification Limit of a quality characteristic

$$\hat{\sigma}_{\text{measurement error}}^2 = \hat{\sigma}_{\text{repeatability}}^2 + \hat{\sigma}_{\text{reproducibility}}^2$$

Moreover,

There are obvious dangers in relying too much on the  $P/T$  ratio. For example, the  $P/T$  ratio may be made arbitrarily small by increasing the width of the specification of tolerance band. The gauge must be able to have sufficient capability to detect meaningful variation in the product. The contribution of gauge variability (or measurement error) to the total variability is a much more useful criterion for determining the measurement system capability. So one may look at the following equation to see whether the given measurement system is capable or not.

$$\frac{\hat{\sigma}_{\text{measurement error}}^2}{\hat{\sigma}_{\text{total}}^2} \leq 10\% \quad (2.3)$$

Another useful gauge to evaluate a measurement system is to see whether or not the measurement process is able to detect product variation. If the amount of measurement system variability is high, it will obscure the product variation. It is important to be able to separate out measurement variability from product variability. Donald J. Wheeler uses discrimination ratio as an indicator of whether the measurement process is able to detect product variation ([Wheeler and Lynday, 1989](#)).

For more information on discrimination ratio and its use in gauge capability analysis, I would advise readers to refer to his book entitled *Evaluating the Measurement Process* (see reference list).

#### **2.4.4 Some tips for the development of a measurement system**

The key to managing processes is measurement. Engineers and managers, therefore, must strive to develop useful measurements of their processes. The following tips are useful when developing a measurement system for industrial experiments.

1. *Select the process you want to measure:* This involves process definition and determination of recipients of the information on measurements, and how that information will be used.
2. *Define the characteristic that needs to be measured within the process:* This involves identification and definition of suitable characteristics that reflect customer needs and expectations. It is always best to have a team of people comprising members from quality engineering, process engineering and operators in defining the key characteristics that need to be measured within a process.
3. *Perform a quality check:* It is quite important to address the following questions during the development of a measurement system:
  - How accurately can we measure the product characteristics?
  - What is the error in our measurement system? Is it acceptable?
  - Is our measurement system stable and capable?
  - What is the contribution of our measurement system variability to the total variation? Is it acceptable?

### **2.5 Selection of quality characteristics for industrial experiments**

The selection of an appropriate quality characteristic is vital for the success of an industrial experiment. To identify a good quality characteristic, it is suggested to start with the engineering or economic goal. Having determined this goal, identify the fundamental mechanisms and the physical laws affecting this goal. Finally, choose the quality characteristics to increase the understanding of these mechanisms and physical laws. The following points are useful in selecting the quality characteristics for industrial experiments (Antony, 1998):

- Try to use quality characteristics that are easy to measure.
- Quality characteristics should, as far as possible, be continuous variables.
- Use quality characteristics which can be measured precisely, accurately and with stability.
- For complex processes, it is best to select quality characteristics at the sub-system level and perform experiments at this level prior to attempting overall process optimisation.
- Quality characteristics should cover all dimensions of the ideal function or the input–output relationship.
- Quality characteristics should preferably be additive (i.e. no interaction exists among the quality characteristics) and monotonic (i.e. the effect of each factor on robustness should be in a consistent direction, even when the settings of factors are changed).

Consider a certain painting process which results in various problems such as orange peel, poor appearance, voids, etc. Too often, experimenters measure these characteristics as data and try to optimise the quality characteristic. It is not the function of the coating process to produce an orange peel. The problem could be due to excess variability of the coating process due to noise factors such as variability in viscosity, ambient temperature, etc. We should make every effort to gather data that relate to the engineering function itself and not to the symptom of variability. One fairly good characteristic to measure for the coating process is the coating thickness. It is important to understand that excess variability of coating thickness from its target value could lead to problems such as orange peel or voids. The sound engineering strategy is to design and analyse an experiment so that best process parameter settings can be determined in order to yield a minimum variability of coating thickness around the specified target thickness.

In the context of service organisations, the selection of quality characteristics is not very straightforward due to the human behavioural characteristics present in the delivery of the service. However, it is essential to understand what characteristics can be efficiently and effectively measured. For instance, in the banking sector, one may measure the number of processing errors, the processing time for certain transactions, the waiting time to open a bank account, etc. It is important to measure those quality characteristics which have an impact on customer satisfaction. In the context of health care services, one can measure the proportion or fraction of medication errors, the proportion of cases with inaccurate diagnosis, the waiting time to get a treatment, the waiting time to be admitted to an A&E department, the number of malpractice claims in a hospital every week or month, etc.

## Exercises

1. What are the three basic principles of DOE?
2. Explain the role of randomisation in industrial experiments. What are the limitations of randomisation in experiments?
3. What is replication? Why do we need to replicate experimental trials?
4. What is the fundamental difference between repetition and replication?
5. Explain the term ‘degrees of freedom’.
6. An experimenter wants to study five process parameters at 2-levels and has decided to use eight trials. How many degrees of freedom are required for studying all five process parameters?
7. What is confounding and what is its role in the selection of a particular design matrix or experimental layout?
8. What is design resolution? Briefly illustrate its significance in industrial experiments.
9. What is the role of a measurement system in the context of industrial experimentation?
10. State three key factors for the selection of quality characteristics for the success of an industrial experiment.
11. What are the three Critical-to-Quality (CTQ) characteristics which you believe to be critical in the eyes of international students who are pursuing a post-graduate course at the University?

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# Understanding key interactions in processes

3

## 3.1 Introduction

For modern industrial processes, the interactions between the factors or process parameters are a major concern to many engineers and managers, and therefore should be studied, analysed and understood properly for problem solving and process optimisation problems. For many process optimisation problems in industries, the root cause of the problem is sometimes due to the interaction between the factors rather than the individual effect of each factor on the output performance characteristic (or response). Here performance characteristic is the characteristic of a product/service which is most critical to customers (Logothetis, 1994).

The significance of interactions in manufacturing processes can be illustrated by the following example taken from a wave-soldering process of a PCB assembly line in a certain electronic industry. The engineering team of the company was interested in reducing the number of defective solder joints obtained from the soldering process. The average defect rate based on the existing conditions is 410 ppm (parts per million). The team has decided to perform a simple experiment to understand the influence of wave-soldering process parameters on the number of defective solder joints.

The team initially utilised an OVAT approach to experimentation. Each process parameter (or process variable) was studied at 2-levels – low level (represented by  $-1$ ) and high level (represented by  $+1$ ). The parameters and their levels are given in [Table 3.1](#). The experimental layout (or design matrix) for the experiment is given in [Table 3.2](#). The design matrix shows all the possible combinations of factors at their respective levels.

In the experimental layout, the actual process parameter settings are replaced by  $-1$  and  $+1$ . The first trial in [Table 3.2](#) represents the current process settings, with each process parameter kept at low level. In the second trial, the team has changed the level of factor ‘A’ from low to high, keeping the levels of other two factors constant. The engineer notices from this experiment that the defect rate is minimum, corresponding to trial condition 4, and thereby conclude that the optimal setting is the one corresponding to the fourth trial.

The difference in the responses between the trials 1 and 2 provides an estimate of the effect of process parameter ‘A’. From [Table 3.2](#), the effect of ‘A’ ( $370 - 420 = -50$ ) was estimated when the levels of ‘B’ and ‘C’ were at low levels. There is no guarantee whatsoever that ‘A’ will have the same effect for different conditions of ‘B’ and ‘C’. Similarly, the effects of ‘B’ and ‘C’ can be estimated. In the above experiment, the response values corresponding to the combinations A ( $-1$ ) B ( $+1$ ), A ( $-1$ ) C ( $+1$ ) and

**Table 3.1** List of process parameters and their levels.

Labels	Process parameters	Units	Low level (-1)	High level (+1)
A	Flux density	g/c/c	0.85	0.90
B	Conveyor speed	ft/min	4.5	5.5
C	Solder temperature	°C	230	260

**Table 3.2** OVAT approach to wave-soldering process.

Run	A	B	C	Response (ppm)
1	-1	-1	-1	420
2	+1	-1	-1	370
3	+1	+1	-1	410
4	+1	+1	+1	350

**Table 3.3** Results from a  $2^3$  FFE.

Run (standard order)	Run (randomised order)	A	B	C	Response (ppm)
1	5	-1	-1	-1	420, 412
2	7	+1	-1	-1	370, 375
3	4	-1	+1	-1	310, 289
4	1	+1	+1	-1	410, 415
5	8	-1	-1	+1	375, 388
6	3	+1	-1	+1	450, 442
7	2	-1	+1	+1	325, 322
8	6	+1	+1	+1	350, 340

B (-1) C (+1) are missing. Therefore OVAT to experimentation can lead to unsatisfactory conclusions and in many cases it would even lead to false optimum conditions. In this case, the team failed to study the effect of each factor at different conditions of other factors. In other words, the team failed to study the interaction between the process parameters.

Interactions occur when the effect of one process parameter depends on the level of the other process parameter. In other words, the effect of one process parameter on the response is different at different levels of the other process parameter. In order to study interaction effects among the process parameters, we need to vary all the factors simultaneously ([Anderson and Whitcomb, 2000](#)). For the above wave-soldering process, the engineering team employed a Full Factorial Experiment (FFE) and each trial or run condition was replicated twice to observe variation in results within the experimental trials. The results of the FFE are given in [Table 3.3](#). Each trial condition was randomised to minimise the effect of undesirable disturbances or external factors which were uncontrollable or expensive to control during the experiment.

As it is an FFE, it is possible to study all the interactions among the factors A, B and C. The interaction between two process parameters (say, A and B) can be computed using the following equation:

$$I_{A,B} = \frac{1}{2} (E_{A,B(+L)} - E_{A,B(-L)}) \quad (3.1)$$

where  $E_{A,B(+1)}$  is the effect of factor ‘A’ at high level of factor ‘B’ and where  $E_{A,B(-1)}$  is the effect of factor ‘A’ at low level of factor ‘B’.

For the above example, three two-order interactions and a third-order interaction can be studied. Third-order and higher order interactions are not often important for process optimisation problems and therefore not necessary to be studied. In order to study the interaction between A (flux density) and B (conveyor speed), it is important to form a table ([Table 3.4](#)) for average ppm values at the four possible combinations of A and B (i.e.  $A_{(-1)} B_{(-1)}$ ,  $A_{(-1)} B_{(+1)}$ ,  $A_{(+1)} B_{(-1)}$  and  $A_{(+1)} B_{(+1)}$ ).

From [Table 3.4](#), the effect of ‘A’ (i.e., going from low level (−1) to high level

$$\begin{aligned} (+1) \text{ at high level of } B \text{ (i.e. +1)} &= 378.75 - 311.50 \\ &= 67.25 \text{ ppm} \end{aligned}$$

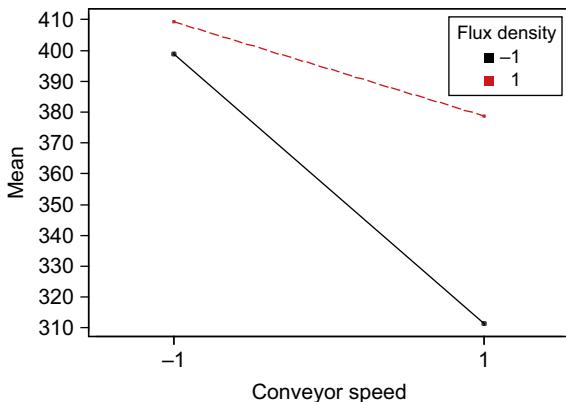
$$\begin{aligned} \text{Similarly, the effect of } A \text{ at low level of } B &= 409.25 - 398.75 \\ &= 10.5 \text{ ppm} \end{aligned}$$

$$\begin{aligned} \text{Interaction between } A \text{ and } B &= \frac{1}{2} [67.25 - 10.5] \\ &= 28.375 \end{aligned}$$

In order to determine whether two process parameters are interacting or not, one can use a simple but powerful graphical tool called interaction graphs. If the lines in the interaction plot are parallel, there is no interaction between the process parameters ([Barton, 1990](#)). This implies that the change in the mean response from low to high level of a factor does not depend on the level of the other factor. On the other hand, if the lines are non-parallel, an interaction exists between the factors. The greater the degree of departure from being parallel, the stronger the interaction effect ([Antony and Kaye, 1998](#)). [Fig. 3.1](#) illustrates the interaction plot between ‘A’ (flux density) and ‘B’ (conveyor speed).

**Table 3.4** Average ppm values.

Run (standard order)	A	B	Average ppm
1, 5	−1	−1	398.75
3, 7	−1	+1	311.50
2, 6	+1	−1	409.25
4, 8	+1	+1	378.75



**Figure 3.1** Interaction plot between flux density and conveyor speed.

The interaction graph between flux density and conveyor speed shows that the effect of conveyor speed on ppm at two different levels of flux density is not the same. This implies that there is an interaction between these two process parameters. The defect rate (in ppm) is minimum when the conveyor speed is at high level and flux density at low level.

## 3.2 Alternative method for calculating the two-order interaction effect

In order to compute the interaction effect between flux density and conveyor speed, we need to first multiply columns 2 and 3 in [Table 3.4](#). This is illustrated in [Table 3.5](#). In [Table 3.5](#), column 3 yields the interaction between flux density (A) and conveyor speed (B).

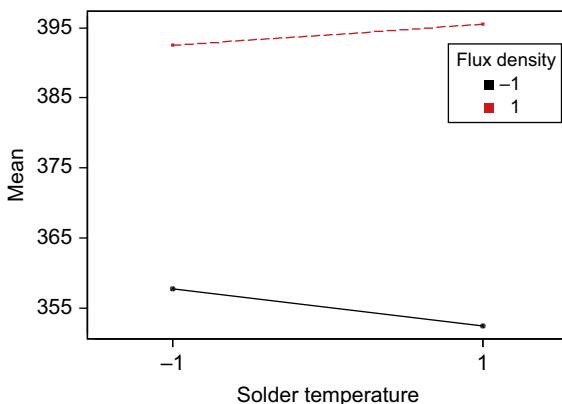
Having obtained column 3, we then need to calculate the average ppm at high level of  $(A \times B)$  and low level of  $(A \times B)$ . The difference between these will provide an estimate of the interaction effect.

$$\begin{aligned}
 A \times B &= \text{Average ppm at high level of } (A \times B) \\
 &\quad - \text{Average ppm at low level of } (A \times B) \\
 &= \frac{1}{2} (398.75 + 378.75) - \frac{1}{2} (311.50 + 409.25) \\
 &= 388.75 - 360.375 \\
 &= 28.375
 \end{aligned}$$

Now consider the interaction between flux density (A) and solder temperature. The interaction graph is shown in [Fig. 3.2](#). The graph shows that the effect of solder temperature at different levels of flux density is almost the same. Moreover, the

**Table 3.5** Alternative method to compute the interaction effect.

A	B	$A \times B$	Average ppm
-1	-1	+1	398.75
-1	+1	-1	311.50
+1	-1	-1	409.25
+1	+1	+1	378.75

**Figure 3.2** Interaction plot between solder temperature and flux density.

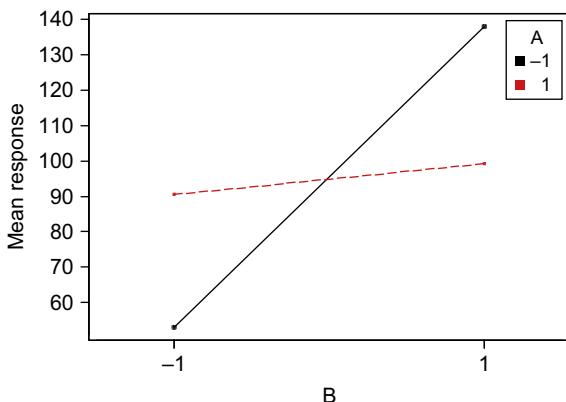
lines are almost parallel, which indicates that there is little interaction between these two factors.

The interaction plot suggests that the mean solder defect rate is minimum when solder temperature is at high level and flux density at low level.

*Note:* Non-parallel lines are an indicator of the existence of interactions between two factors and parallel lines indicate no interactions between the factors.

### 3.3 Synergistic interaction versus antagonistic interaction

The effects of process parameters can be either fixed or random. Fixed process parameter effects occur when the process parameter levels included in the experiment are controllable and specifically chosen because they are the only ones for which inferences are desired. For example, if you want to determine the effect of temperature at 2-levels ( $180^{\circ}\text{F}$  and  $210^{\circ}\text{F}$ ) on the viscosity of a fluid, then both  $180^{\circ}\text{F}$  and  $210^{\circ}\text{F}$  are considered to be fixed parameter levels. On the other hand, random process parameter effects are associated with those parameters whose levels are randomly chosen from a large population of possible levels.



**Figure 3.3** Antagonistic interaction between two factors A and B.

Inferences are not usually desired on the specific parameter levels included in an experiment, but rather on the population of levels represented by those in the experiment. Factor levels represented by batches of raw materials drawn from a large population are examples of random process parameter levels. In this book, only fixed process parameter effects are considered.

For synergistic interaction, the lines on the plot do not cross each other (Gunst and Mason, 1991). For example, Fig. 3.1 is an example of synergistic interaction. In contrast, for antagonistic interaction, the lines on the plot cross each other. This is illustrated in Fig. 3.3. In this case, the change in mean response for factor B at low level (represented by  $-1$ ) is noticeably high compared to high level. In other words, factor B is less sensitive to variation in mean response at high level of factor A.

In order to have a greater understanding of the analysis and interpretation of interaction effects, the following two scenarios can be considered.

### 3.4 Scenario 1

In an established baking school, the students had failed to produce uniform-sized cakes, despite their continuous efforts. The engineering team of the company was looking for the key factors or interactions which were most responsible for the variation in the weight of cakes. Here the weight of the cakes was considered to be the critical characteristic to the customers. A project was initiated to understand the nature of the problem and come up with a possible solution to identify the causes of variation and, if possible, eliminate them for greater consistency in the weights of these cakes. Further to a thorough brainstorming session, six process variables (or factors) and a possible interaction ( $B \times M$ ) were considered for the experiment. The factors and their levels are given in Table 3.6.

Each process variable was kept at 2-levels and the objective of the experiment was to determine the optimum combination of process variables which yield

**Table 3.6** List of baking process variables for the experiment.

Factors	Label	Low level	High level
Butter (cups)	B	$\frac{1}{4}$	$\frac{1}{2}$
Milk (cups)	M	$\frac{1}{4}$	$\frac{1}{2}$
Flour (cups)	F	$\frac{3}{4}$	1
Sugar (cups)	S	$\frac{1}{2}$	$\frac{3}{4}$
Oven temperature (°C)	O	200	225
Eggs	E	2	3

**Table 3.7** Response table for the cake baking experiment.

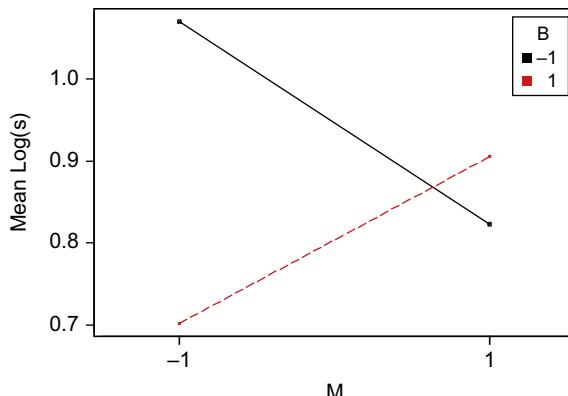
Run	B	M	B × M	O	F	S	E	Weight (g)	log(SD)
1	-1	-1	+1	-1	+1	+1	-1	102.3, 117.6	1.034
2	+1	-1	-1	-1	-1	+1	+1	114.6, 120.3	0.605
3	-1	+1	-1	-1	+1	-1	+1	134.6, 126.7	0.747
4	+1	+1	+1	-1	-1	-1	-1	116.4, 123.9	0.725
5	-1	-1	+1	+1	-1	-1	+1	112.6, 130.6	1.105
6	+1	-1	-1	+1	+1	-1	-1	150.6, 141.7	0.799
7	-1	+1	-1	+1	-1	+1	-1	133.6, 122.4	0.899
8	+1	+1	+1	+1	+1	+1	+1	155.8, 138.6	1.085

minimum variation in the weight of cakes. An FFE would have required 64 experimental runs. Due to limited time and experimental budget, it was decided to select a  $2^{(6-3)}$  fractional factorial experiment (i.e. eight trials or runs). Each trial condition was replicated twice to obtain sufficient degrees of freedom for the error term. Because we are analysing variation, the minimum number of replicates per trial condition is two. [Table 3.7](#) presents the experimental layout or design matrix for the cake baking experiment. According to the Central Limit Theorem (CLT), if you repeatedly take large random samples from a stable process and display the averages of each sample in a frequency diagram, the diagram will be approximately bell-shaped. In other words, the sampling distribution of means is roughly normal, according to CLT. It is quite interesting to note that the distribution of sample standard deviations (SDs) does not follow a normal distribution. However, if we transform the sample SDs by taking their logarithms, the logarithms of the SDs will be much closer to being normally distributed. The last column in [Table 3.7](#) gives the logarithmic transformation of sample SD. The SDs and log(SD) can easily be obtained by using a scientific calculator or Microsoft Excel spreadsheet. Here our interest is to analyse the interaction between the process variables butter (B) and milk (M) rather than the individual effect of each process variable on the variability of cake weights.

In order to analyse the interaction effect between butter and milk, we form a table for average log(SD) values corresponding to all of the four possible combinations of B and M. The results are given in [Table 3.8](#).

**Table 3.8** Interaction table for log(SD).

B	M	Average log(SD)
-1	-1	1.0695
-1	+1	0.823
+1	-1	0.702
+1	+1	0.905

**Figure 3.4** Interaction plot between milk and butter.

Calculation of interaction effect ( $B \times M$ ):

$$\text{Effect of butter } (B) \text{ at high level of milk } (M) = 0.905 - 0.823 = 0.082$$

$$\text{Effect of butter } (B) \text{ at low level of milk } (M) = 0.702 - 1.0695 = -0.3675$$

Using Eq. (4.1),

$$B \times M = \frac{1}{2}[0.082 - (-0.3675)] = 1/2[0.082 + 0.3675] = 0.225$$

**Fig. 3.4** illustrates the interaction plot between the process variables ‘B’ and ‘M’.

**Fig. 3.4** clearly indicates the existence of interaction between the factors butter and milk. The interaction plot shows that variability in the weight of cakes is minimum when the level of butter is kept at high level and milk at low level.

## 3.5 Scenario 2

In this scenario, we illustrate an experiment conducted by a chemical engineer to study the effect of three process variables (temperature, catalyst and pH) on the chemical yield.

The results of the experiment are given in [Table 3.9](#). The engineer was interested in studying the effect of three process variables and the interaction between temperature and catalyst. The engineer has replicated each trial condition three times to obtain sufficient degrees of freedom for the experimental error. Moreover, replication increases the precision of the experiment by reducing the SDs used to estimate the process parameter (or factor) effects.

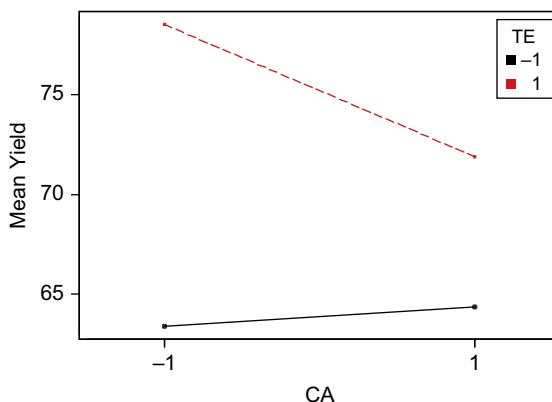
The first step was to construct a table ([Table 3.10](#)) for interaction between TE and CA. The mean chemical yield at all four combinations of TE and CA was estimated. In order to determine whether or not these variables are interacting, an interaction plot was constructed ([Fig. 3.5](#)).

**Table 3.9** Experimental layout for the yield experiment.

Trial	TE	CA	pH	Chemical yield (%)
1	-1	-1	-1	60.4, 62.1, 63.4
2	+1	-1	-1	64.1, 79.4, 74.0
3	-1	+1	-1	59.6, 61.2, 57.5
4	+1	+1	-1	66.7, 67.3, 68.9
5	-1	-1	+1	63.3, 66.0, 65.3
6	+1	-1	+1	91.2, 77.4, 84.9
7	-1	+1	+1	68.1, 71.3, 68.6
8	+1	+1	+1	75.3, 77.1, 76.1

**Table 3.10** TE  $\times$  CA interaction table.

TE	CA	Mean chemical yield
-1	-1	63.42
+1	-1	78.50
-1	+1	64.38
+1	+1	71.90



**Figure 3.5** Interaction plot between CA and TE.

As the lines are not parallel, there is an interaction between the process variables CA and TE. The graph indicates that the effect of CA is insensitive to mean yield at low level of TE. However, maximum yield is obtained when temperature is kept at a high level. Maximum yield is obtained when temperature is set at a high level and CA at a low level. The interaction effect can be computed in the following manner.

$$\text{Effect of CA at high level of TE} = 71.90 - 78.50 = -6.60$$

$$\text{Effect of CA at low level of TE} = 64.38 - 63.42 = 0.96$$

$$\text{CA} \times \text{TE} = \frac{1}{2}[-6.60 - 0.96] = -3.78$$

### 3.6 Scenario 3

In this scenario, we share the results of an experiment carried out in a certain grinding process to reduce common-cause variation (random in nature and expensive to control in many cases). The primary purpose of the experiment in this case was to reduce variation in the outer diameter produced by a grinding operation. The following factors and their effects were of interest to the experimenter.

1. Feed Rate – Factor A – labelled as FR
2. Wheel Speed – Factor B – labelled as WHS
3. Work Speed – Factor C – labelled as WOS
4. Wheel Grade – Factor D – labelled as WG
5. Interaction between WHS and WOS
6. Interaction between WHS and WG

The results of the experiment are given in [Table 3.11](#). The response of interest for this experiment was Signal-to-Noise ratio (SNR). SNR is a performance statistic recommended by Dr Taguchi in order to make the process insensitive to undesirable disturbances called noise factors ([Gijo, 2005; Lochner and Matar, 1990](#)). The purpose of the SNR is to maximise the signal while minimising the impact of noise. The whole idea is to achieve robustness, and the higher the SNR, the greater the robustness will be.

The mean SNR at high level (+1) of  $\text{WHS} \times \text{WOS}$  = 51.11

The mean SNR at low level (-1) of  $\text{WHS} \times \text{WOS}$  = 48.054

Therefore, interaction effect = 3.056

Similarly, the mean SNR at high level of  $\text{WHS} \times \text{WG}$  = 49.409

The mean SNR at low level of  $\text{WHS} \times \text{WG}$  = 49.754

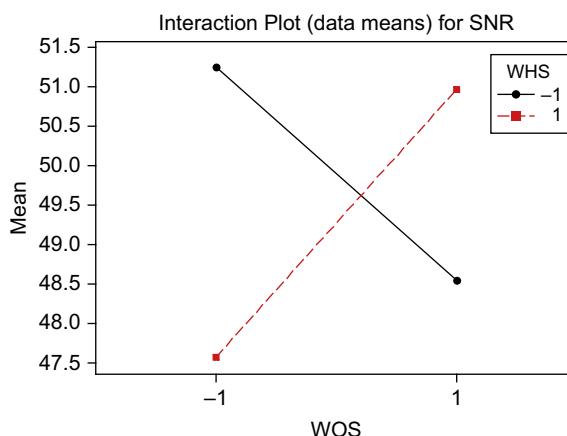
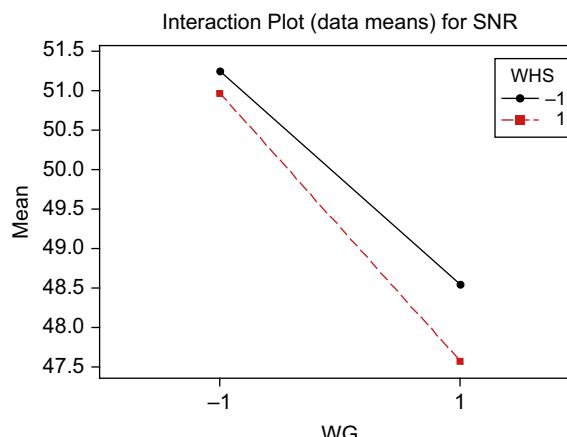
Therefore, interaction effect = -0.345

[Fig. 3.6](#) illustrates the interaction plot between the WHS and WOS. As the lines are non-parallel, there is a strong interaction between those two factors.

[Fig. 3.6](#) shows that the effect of WOS on SNR at different levels of WHS is not the same. As SNR needs to be maximised, the optimum combination is when WOS and WHS are kept at a low level. [Fig. 3.7](#) illustrates the interaction plot between the WHS and WG. As the lines exhibit near parallelism, there is no interaction between those two factors.

**Table 3.11** SNR values and interactions.

Trial	WHS × WOS	WHS × WG	Response (SNR)
1	+1	+1	53.469
2	-1	-1	50.970
3	-1	+1	49.030
4	+1	-1	56.991
5	+1	+1	49.030
6	-1	-1	46.108
7	-1	+1	46.108
8	+1	-1	44.948

**Figure 3.6** Interaction plot between WOS and WHS.**Figure 3.7** Interaction plot between WG and WHS.

## Exercises

1. In a certain casting process for manufacturing jet engine turbine blades, the objective of the experiment is to determine the most important interaction effects (if there are any) that affect part shrinkage. The experimenter has selected three process parameters: pour speed (A), metal temperature (B) and mould temperature(C), each factor being kept at two levels for the study. The response table, together with the response values, is shown below. Calculate and analyse the two-factor interactions among the three process variables. Each run was replicated three times to have adequate degrees of freedom for error.

Run	A	B	C	Shrinkage
1	-1	-1	-1	2.22, 2.11, 2.14
2	+1	-1	-1	1.42, 1.54, 1.05
3	-1	+1	-1	2.25, 2.31, 2.21
4	+1	+1	-1	1.00, 1.38, 1.19
5	-1	-1	+1	1.73, 1.86, 1.79
6	+1	-1	+1	2.71, 2.45, 2.46
7	-1	+1	+1	1.84, 1.76, 1.70
8	+1	+1	+1	2.27, 2.69, 2.71

2. A company that manufactures can-forming equipment wants to set up an experiment to help understand the factors influencing surface finish on a particular steel subassembly. The company decides to perform an eight-trial experiment with three factors at 2-levels. A brainstorming session conducted with people within the organisation –operator, supervisor and engineer –resulted in the finished part being measured at four places. The list of factors (A: tool radius, B: feed rate and C: Revolutions per Minute (RPM)) and the response (surface finish) is shown in the following experimental layout. Generate an interaction plot for any two-way interactions with large effects.

Run	A	B	C	Surface finish
1	-1	-1	-1	50, 50, 55, 50
2	+1	-1	-1	145, 150, 100, 110
3	-1	+1	-1	160, 165, 155, 160
4	+1	+1	-1	180, 200, 190, 195
5	-1	-1	+1	60, 65, 55, 60
6	+1	-1	+1	25, 35, 35, 30
7	-1	+1	+1	160, 160, 150, 165
8	+1	+1	+1	80, 70, 75, 80

3. Assume you are planning to carry out an experiment to investigate the sensitivity of an amplifier to process variation. The response of interest for the experiment is the gain of the amplifier measured in decibels (dB). You would like to evaluate the effects of three factors: resistor (R), width of the microstrip lines (W) and a capacitor (C). Each factor was studied at 2-levels and a simulation was conducted for studying all the combinations of factors at their respective levels. The coded matrix is shown below.

<b>Run</b>	<b>W</b>	<b>R</b>	<b>C</b>	<b>Gain (dB)</b>
1	-1	-1	-1	12.85
2	+1	-1	-1	13.01
3	-1	+1	-1	14.52
4	+1	+1	-1	14.71
5	-1	-1	+1	12.93
6	+1	-1	+1	13.09
7	-1	+1	+1	14.61
8	+1	+1	+1	14.81

Calculate and analyse all the two-factor interactions  $W \times R$ ,  $R \times C$  and  $W \times C$ . Also construct an interaction graph between W and R. How would you interpret this graph?

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# A systematic methodology for design of experiments

4

## 4.1 Introduction

It is widely considered that DOE (or experimental design) forms an essential part of the quest for effective improvement in process performance or product/service quality. This chapter discusses the barriers and cognitive gaps in the statistical knowledge required by industrial engineers for tackling process and quality-related problems using DOE technique. This chapter also presents a systematic methodology to guide people in organisations with limited statistical ability for solving manufacturing process-related problems in real-life situations.

## 4.2 Barriers in the successful application of DOE

Although DOE has been around for nearly 100 years, research has clearly demonstrated that less than 30% of people are knowledgeable about DOE. Despite every effort by specialists and practitioners in quality and statistics, DOE has yet to be applied as widely as it could and should be. A study carried out in Sweden has shown that only 18% of Swedish companies are using the Robust Parameter Design (RPD) methodology advocated by Dr Taguchi. These results were part of a large study carried out as part of a European project which looked into the use of RPD methodology across five countries (Germany, Ireland, The Netherlands, Spain and Sweden). It was also found that the application of Six Sigma methodology has a positive influence on the application of DOE. A recent study has shown that over 60% of companies that apply DOE frequently are knowledgeable about Six Sigma as a problem-solving methodology. It has been observed over the years that companies utilising Six Sigma and Design for Six Sigma (DFSS) methodologies are using DOE more frequently than those companies which are not. The ‘effective’ application of DOE by industrial engineers is limited in many manufacturing organisations ([Antony and Kaye, 1995](#)). Some noticeable barriers are as follows:

- *Educational barriers:* The word ‘statistics’ invokes fear in many industrial engineers. The fundamental problem begins with the current statistical education for the engineering community in their academic curriculum. The courses currently available in ‘engineering statistics’ often tend to concentrate on the theory of probability, probability distributions and more mathematical aspects of the subject, rather than practically useful techniques such as DOE, Taguchi method, robust design, gauge capability studies, Statistical Process Control (SPC), etc. It was found from various sources of literature that DOE is rarely taught at universities or at company-provided training sessions. The best way to

tackle this issue is through incessant cooperation between industry and academia. In the context of small and medium enterprises (SMEs), engineers typically do not have access to books and case studies which demonstrate the power of DOE. In addition, most of the DOE material is available in English but many engineers and scientists in the developing world lack adequate English reading skills and therefore cannot use such materials. Another study has shown that the only experiments students participate in, if any, are based on demonstration and are often of limited educational value. Although DOE is a very powerful technique for problem solving in manufacturing companies, it was observed that both engineers and scientists receive little or no training in DOE at the university level. The most common criticisms of the teaching of DOE in many schools are that it is too academic in focus and that most examples taught to engineers are far too theoretical and do not represent real-world problems. There is a clear consensus that academics needs to change the way it teaches business statistics ([Bisgaard, 1991](#)). Engineers must be taught these powerful techniques in the academic world with a number of supporting case studies. This will ensure a better understanding of the application of statistical techniques before they enter the job market.

- *Management barriers:* Managers often don't understand the importance of DOE in problem solving or don't appreciate the competitive value it brings into the organisation. In many organisations, managers encourage their engineers to use the so-called 'home-grown' solutions for process- and quality-related problems. These 'home-grown' solutions are consistent with the OVAT approach to experimentation, as managers are always after quick-fix solutions which yield short-term benefits to their organisations. Responses from managers with high resistance to change may include the following:
  - DOE tells me what I already know.
  - It sounds good, but it is not applicable to my job.
  - I need to make additional effort to prove what I already know.

Many managers do not instinctively think statistically, mainly because they are not convinced that statistical thinking adds any value to management and decision-making. Managers in organisations believe that DOE is very demanding of resources.

- *Cultural barriers:* Cultural barriers are one of the principal reasons why DOE is not commonly used in many organisations. The management should be prepared to address all cultural barrier issues that might be present within the organisation, plus any fear of training or reluctance to embrace the application of DOE. Many organisations are not culturally ready for the introduction and implementation of advanced quality improvement techniques such as DOE and Taguchi. The best way to overcome this barrier is through intensive training programs and by demonstrating the successful application of such techniques by other organisations during the training. The culture of the company is very much reliant on the style of leadership. If the leaders are not committed to the idea of performing industrially designed experiments for improving quality and process efficiency, then the concept of DOE becomes just 'lip service' on the part of the senior management team and will never be a reality ([Tanco et al., 2009](#)).
- *Communication barriers:* Research has indicated that there is very little communication between the academic and industrial worlds. Moreover, the communication among industrial engineers, managers and statisticians in many organisations is limited. For the successful initiative of any quality improvement programme, these communities should work together and make this barrier less formidable. For example, lack of statistical knowledge for engineers could lead to problems such as misinterpretation of historical data or misunderstanding of the nature of interactions among factors under consideration for a given experiment. Similarly, academic statisticians' lack of engineering knowledge could lead

to problems such as undesirable selection of process variables and quality characteristics for the experiment, lack of measurement system precision and accuracy, etc. Managers' lack of basic knowledge in engineering and statistics could lead to problems such as high quality costs, poor quality and therefore lost competitiveness in the world marketplace and so on and so forth.

- *Other barriers:* Negative experiences with DOE may make companies reluctant to use DOE again. The majority of negative DOE experiences can be classified into two groups. The first relates to technical issues and the second to non-technical issues. Technical issues include
  - choosing unreasonably large or small designs;
  - inadequate or even poor measurement of quality characteristics;
  - not choosing the appropriate levels for the process variables, etc. Non-linearity or curvature effects of process variables should be explored to determine the best operating process conditions;
  - assessing the impact of 'uncontrolled variables' which can influence the output of the process. Experimenters should try to understand how the 'uncontrolled variables' influence the process behaviour and devise strategies to minimise their impact as much as possible; and
  - lacking awareness of assumptions: data analysis, awareness of different alternatives when they are needed, etc.

Some of the non-technical issues include

- lack of experimental planning;
- executing one-shot experimentation instead of adopting sequential, adaptive and iterative nature of experimentation and
- not choosing the right process variables or design variables for the experiment in the first round of experimentation, etc.

Commercial software systems and expert systems in DOE provide no guidance whatsoever in classifying and analysing manufacturing process quality-related problems from which a suitable approach (Taguchi, Classical or Shainin's approach) can be selected. Very little research has been done on this particular aspect and from the author's standpoint, this is probably the most important part of DOE. The selection of a particular approach to experimentation (i.e. Taguchi, Classical or Shainin) is dependent upon a number of criteria: the complexity involved, the degree of optimisation required by the experimenter, the time required for completion of the experiment, cost issues associated with the experiment, the allowed response time to report back to management, etc. Moreover, many software systems in DOE stress data analysis and do not properly address data interpretation. Thus, many engineers, having performed the statistical analysis using such software systems, would not know how to effectively utilise the results of the analysis without assistance from statisticians.

### 4.3 A practical methodology for DOE

The methodology of DOE is fundamentally divided into four phases. These are:

1. planning phase
2. designing phase

3. conducting phase
4. analysing phase.

### **4.3.1 Planning phase**

The planning phase is made up of the following steps. Many engineers pay special attention on the statistical details of DOE and very little attention to the non-statistical details. According to [Peace \(1993\)](#), experimental studies may fail not only as a result of lack of technical knowledge of the process under study or wrong use of statistical techniques but also due to lack of planning. It is the responsibility of the senior management team in the organisation to create an environment that stimulates a culture of using experimental design techniques for process optimisation problems, product and process development projects, improving process capability through systematically reducing excessive variation in processes, etc.

#### **4.3.1.1 Problem recognition and formulation**

A clear and succinct statement of the problem can create a better understanding of what needs to be done. The statement should contain an objective that is specific, measurable and which can yield practical value to the company ([Kumar and Tobin, 1990](#)). The creation of a multidisciplinary team in order to have a shared understanding of the problem is critical in the planning phase. The multidisciplinary team should be led by someone with good knowledge of the process (a DOE specialist), good communication skills, good interpersonal skills and awareness of team dynamics. Other team members may include process engineers, a quality engineer/manager, a machine operator, a management representative and manufacturing/production engineers/managers. Sharing experiences and individual knowledge is critical to assure a deeper understanding of the process providing more efficient ways to design experiments ([Romeu, 2006](#)). Some manufacturing problems that can be addressed using an experimental approach include

- development of new products; improvement of existing processes or products;
- improvement of the process/product performance relative to the needs and demands of customers;
- reduction of existing process spread, which leads to poor capability.

The objective of the experiment must be clearly specified and has to be measurable. Objectives can be either short term or long term. A short-term objective could be to fix a problem related to a high scrap rate. However, this objective is not at all specific and not measured in a true sense. What is ‘high,’ for instance? What particular process causes a high scrap rate? Some aspects of Six Sigma thinking would be very beneficial to help the team convert this engineering or manufacturing problem into a statistical problem.

#### ***4.3.1.2 Selection of response or quality characteristic***

The selection of a suitable response for the experiment is critical to the success of any industrially designed experiment. Time spent in establishing a meaningful response variable before a well-planned experiment is rarely wasted. The response can be variable or attribute in nature. Variable responses such as length, thickness, diameter, viscosity, strength, etc. generally provide more information than attribute responses such as good/bad, pass/fail or yes/no. Moreover, variable characteristics or responses require fewer samples than attributes to achieve the same level of statistical significance. It is also not unusual to have several responses requiring simultaneous optimisation, which can be quite challenging at times.

Experimenters should define the measurement system prior to performing the experiment in order to understand what to measure, where to measure and who is doing the measurements, etc. so that various components of variation (measurement system variability, operator variability, part variability, etc.) can be evaluated. Defining a measurement system, including human resources, equipments and measurement methods, is a fundamental aspect in planning experimental studies. It is important to ensure that equipment exists and is suitable, accessible and calibrated. The quality of a measurement system is usually determined by the statistical properties of the data it generates over a period of time which captures both long- and short-term variation. Experimenters should be aware of the repeatability, reproducibility and uncertainty of the measurements prior to the execution of industrial experiments ([Launsby and Weese, 1995](#)). It is advisable to make sure that the measurement system is capable, stable, robust and insensitive to environmental changes.

#### ***4.3.1.3 Selection of process variables or design parameters***

Some possible ways to identify potential process variables are the use of engineering knowledge of the process, historical data, cause-and-effect analysis and brainstorming. This is a very important step of the experimental design procedure. If important factors are left out of the experiment, then the results of the experiment are not accurate or useful for any improvement actions. It is a good practice to conduct a screening experiment in the first phase of any experimental investigation to identify the most important design parameters or process variables. More information on screening experiments/designs can be obtained from Chapter 5.

#### ***4.3.1.4 Classification of process variables***

Having identified the process variables, the next step is to classify them into controllable and uncontrollable variables. Control variables are those which can be controlled by a process engineer/production engineer in a production environment. Uncontrollable variables (or noise variables) are those which are difficult or expensive to control in actual production environments. Variables such as ambient temperature fluctuations, humidity fluctuations, raw material variations, etc. are examples of noise variables. These variables may have an immense impact on the

process variability and therefore must be dealt with for enhanced understanding of our process. The effect of such nuisance variables can be minimised by the effective application of DOE principles such as blocking, randomisation and replication. (For more information on these three principles, refer to Chapter 8.)

#### **4.3.1.5 Determining the levels of process variables**

A level is the value that a process variable holds in an experiment. For example, a car's gas mileage is influenced by such levels as tyre pressure, speed, etc. The number of levels depends on the nature of the process variable to be studied for the experiment and whether or not the chosen process variable is qualitative (type of catalyst, type of material, etc.) or quantitative (temperature, speed, pressure, etc.). For quantitative process variables, two levels are generally required in the early stages of experimentation. However, for qualitative variables, more than two levels may be required. If a non-linear function is expected by the experimenter, then it is advisable to study variables at three or more levels. This would assist in quantifying the non-linear (or curvature) effect of the process variable on the response function.

#### **4.3.1.6 List all the interactions of interest**

Interaction among variables is quite common in industrial experiments. In order to effectively interpret the results of the experiment, it is highly desirable to have a good understanding of the interaction between two process variables (Marilyn, 1993). The best way to relate to interaction is to view it as an effect, just like a factor or process variable effect. Since it is not an input you can control, unlike factors or process variables, interactions do not enter into descriptions of trial conditions. In the context of DOE, we generally study two-order interactions. The number of two-order interactions within an experiment can be easily obtained by using a simple equation:

$$N = \frac{n \times (n - 1)}{2} \quad (4.1)$$

where  $n$  is the number of factors.

For example, if you consider four factors in an experiment, the number of two-order interactions can be equal to six.

The questions to ask include 'Do we need to study the interactions in the initial phase of experimentation?' and 'How many two-order interactions are of interest to the experimenter?' The size of the experiment is dependent on the number of factors to be studied and the number of interactions, which are of great concern to the experimenter.

#### **4.3.2 Designing phase**

In this phase, one may select the most appropriate design for the experiment. Some DOE practitioners would argue that proper experimental design is often more

important than sophisticated statistical analysis. The author would agree with this point as the damage caused by poor experimental design is irreparable. The choice of design depends upon a number of factors such as the number of factors to be studied, the number of levels at which the factors are to be explored, the resources and budget allocated for the experiment, the nature of the problem and objectives to be achieved, etc. Experiments can be statistically designed using the classical approach advocated by Sir Ronald Fisher, the orthogonal array approach advocated by Dr Genichi Taguchi or the variables search approach promoted by Dr Dorian Shainin. This book is focused on the classical DOE approach advocated by Sir Ronald Fisher. Within this approach, one can choose full factorial, fractional factorial or screening designs (such as Plackett–Burmann designs). These designs are introduced to the reader in the subsequent chapters.

During the design stage, it is quite important to consider the confounding structure and resolution of the design ([Minitab, 2000](#)). It is good practice to have the design matrix ready for the team prior to executing the experiment. The design matrix generally reveals all the settings of factors at different levels and the order of running a particular experiment. Experimenters are advised to carefully consider the three principles of experimental design prior to conducting the real experiment. The principles of randomisation, replication and blocking should be carefully taken into account but depending upon the nature of the problem and the objectives set for the experiment ([Montgomery, 2001](#)). These principles will be explained in detail at a later stage of the book.

### **4.3.3 Conducting phase**

This is the phase in which the planned experiment is carried out and the results are evaluated. Several considerations are recognised as being recommended prior to executing an experiment, such as

- selection of a suitable location for carrying out the experiment. It is important to ensure that the location is not affected by any external sources of noise (vibration, humidity, etc.);
- availability of materials/parts, operators, machines, etc. required for carrying out the experiment;
- assessment of the viability of an action in monetary terms by utilising cost–benefit analysis. A simple evaluation must also be carried out in order to verify that the experiment is the only possible solution for the problem at hand and justify that the benefits to be gained from the experiment will exceed the cost of the experiment.

The following steps may be useful while performing the experiment in order to ensure that it is performed according to the prepared experimental design matrix (or layout).

- The person responsible for the experiment should be present throughout the experiment. In order to reduce the operator-to-operator variability, it is best to use the same operator for the entire experiment.

- Monitor the experimental trials. This is to find any discrepancies while running the experiment. It is advisable to stop running the experiment if any discrepancies are found.
- Record the observed response values on the prepared data sheet or directly into the computer.
- Any experiment deviations and unusual occurrences must be recorded and analysed.

#### **4.3.4 Analysing phase**

It has been quite interesting to observe over the years that many engineers rush into the conducting and analysing phases of DOE and pay little attention to the planning and designing phases. My personal message, as a mechanical engineer, to the engineering fraternity is that it is the planning and designing phases that are crucial to the success of the experiment and not the executing and analysing phases. I am not suggesting that conducting and analysing the phases of DOE are unimportant but if we do not plan and design an experiment correctly the first time, there is no way to save the experiment with a sophisticated statistical analysis.

Having performed the experiment, the next phase is to analyse and interpret the results so that valid and sound conclusions can be derived. In DOE, the following are the possible objectives to be achieved from this phase:

- Determine the design parameters or process variables that affect the mean process performance.
- Determine the design parameters or process variables that influence performance variability.
- Determine the design parameter levels that yield the optimum performance.
- Determine whether further improvement is possible.

The following tools can be used for the analysis of experimental results. As the focus of this book is to ‘Keep It Statistically Simple’ for the readers, the author will be introducing only simple but powerful tools for the analysis and interpretation of results. There are a number of DOE books available on the market that cover more sophisticated statistical methods for the analysis. The author encourages readers to use Minitab software for the analysis of experimental results.

### **4.4 Analytical tools of DOE**

#### **4.4.1 Main effects plot**

A main effects plot is a plot of the mean response values at each level of a design parameter or process variable. One can use this plot to compare the relative strength of the effects of various factors. The sign and magnitude of a main effect would tell us the following:

- The sign of a main effect tells us of the direction of the effect, that is, whether the average response value increases or decreases.
- The magnitude tells us of the strength of the effect.

If the effect of a design or process parameter is positive, it implies that the average response is higher at a high level rather than a low level of the parameter setting. In contrast, if the effect is negative, it means that the average response at the low-level setting of the parameter is more than at the high level. Fig. 4.1 illustrates the main effect of temperature on the tensile strength of a steel specimen. As you can see from the figure, tensile strength increases when the temperature setting varies from low to high (i.e.  $-1$  to  $1$ ).

The effect of a process or design parameter (or factor) can be mathematically calculated using the following simple equation:

$$E_f = \bar{F}_{(+L)} + \bar{F}_{(-L)} \quad (4.2)$$

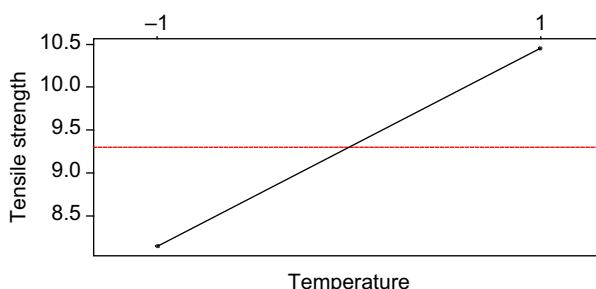
where  $\bar{F}_{(+L)}$  = average response at high-level setting of a factor, and  $\bar{F}_{(-L)}$  = average response at low-level setting of a factor.

#### 4.4.2 Interactions plots

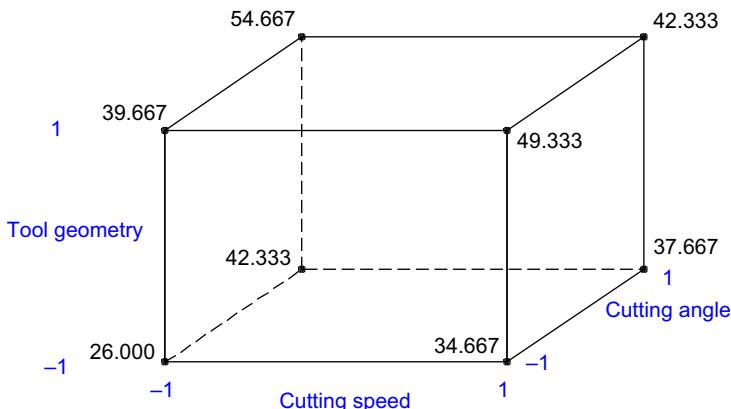
An interactions plot is a powerful graphical tool which plots the mean response of two factors at all possible combinations of their settings. If the lines are parallel, this indicates that there is an interaction between the factors. Non-parallel lines are an indication of the presence of interaction between the factors. More information on interactions and how to interpret them can be seen in Chapter 3.

#### 4.4.3 Cube plots

Cube plots display the average response values at all combinations of process or design parameter settings. One can easily determine the best and worst combinations of factor levels for achieving the desired optimum response. A cube plot is useful to determine the path of steepest ascent or descent for optimisation problems. Fig. 4.2 illustrates an example of a cube plot for a cutting tool life optimisation study with three tool parameters: cutting speed, tool geometry and cutting angle.



**Figure 4.1** Main effect plot of temperature on tensile strength.



**Figure 4.2** Example of a cube plot for cutting tool optimisation study.

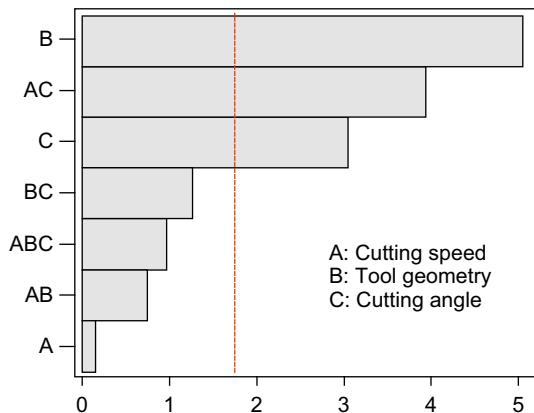
The graph indicates that tool life increases when cutting speed is set at low level and cutting angle and tool geometry are set at high levels. The worst condition occurs when all factors are set at low levels.

#### 4.4.4 Pareto plot of factor effects

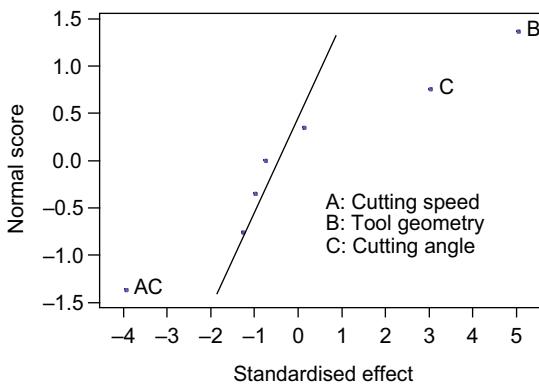
The Pareto plot allows one to detect the factor and interaction effects that are most important to the process or design optimisation study one has to deal with. It displays the absolute values of the effects, and draws a reference line on the chart. Any effect that extends past this reference line is potentially important. For example, for the above tool life experiment, a Pareto plot is constructed (Fig. 4.3). The graph shows that factors B and C and interaction AC are most important. Minitab displays the absolute value of the standardised effects of factors when there is an error term. It is always a good practice to check the findings from a Pareto chart with Normal Probability Plot (NPP) of the estimates of the effects (refer to NPP in the following section).

#### 4.4.5 NPP of factor effects

For NPPs, the main and interaction effects of factors or process (or design) parameters should be plotted against cumulative probability (%). Inactive main and interaction effects tend to fall roughly along a straight line, whereas active effects tend to appear as extreme points falling off each end of the straight line (Benski, 1989). These active effects are judged to be statistically significant. Fig. 4.4 shows an NPP of effects of factors for the above cutting tool optimisation example at a 5% significance level. Here the significance level is the risk of saying that a factor is significant when in fact it is not. In other words, it is the probability of the observed significant effect being due to pure chance. The results are absolutely identical to that of a Pareto plot of factor/interaction effects.



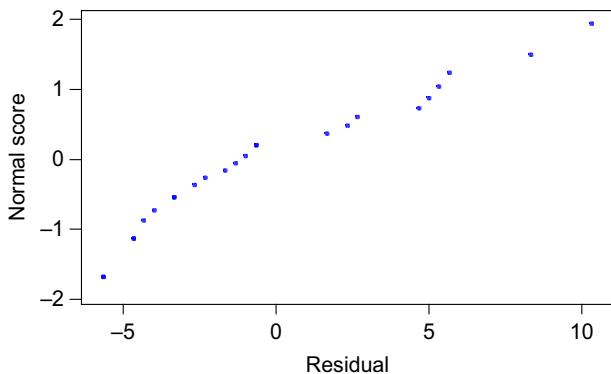
**Figure 4.3** Pareto plot of the standardised effects.



**Figure 4.4** NPP of effects for cutting tool optimisation example.

#### 4.4.6 NPP of residuals

One of the key assumptions for the statistical analysis of data from industrial experiments is that the data come from a normal distribution. The appearance of a moderate departure from normality does not necessarily imply a serious violation of the assumptions. Gross deviations from normality are potentially serious and require further analysis. In order to check the data for normality, it is best to construct an NPP of the residuals. NPPs are useful for evaluating the normality of a data set, even when there is a fairly small number of observations. Here residual is the mean difference between the observed value (obtained from the experiment) and the predicted or fitted value. If the residuals fall approximately along a straight line, they are then normally distributed. In contrast, if the residuals do not fall fairly close to



**Figure 4.5** NPP of residuals for the cutting tool example.

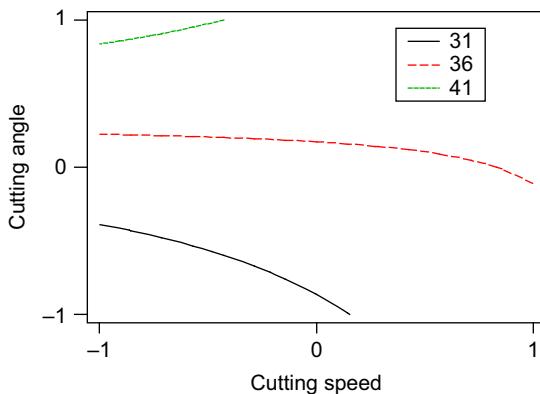
a straight line, they are then not normally distributed and hence the data do not come from a normal population.

The general approach to dealing with non-normality situations is to apply variance-stabilising transformation on the data. An explanation on data transformation is beyond the scope of this book and therefore readers are advised to refer to [Montgomery \(2001\)](#), which covers the use of data transformation and how to perform data transformation in a detailed manner. [Fig. 4.5](#) illustrates the NPP of residuals for the cutting tool optimisation example. The graph shows that the points fall fairly close to a straight line, indicating that the data are approximately normal.

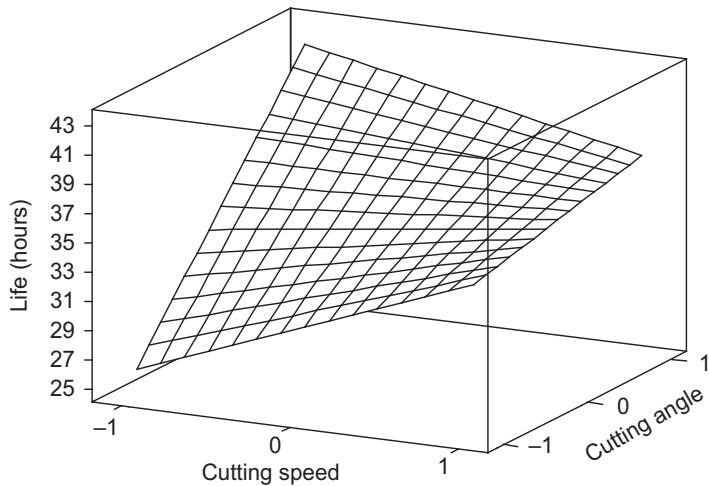
#### 4.4.7 Response surface plots and regression models

Response surface plots such as contour and surface plots are useful for establishing desirable response values and operating conditions. In a contour plot, the response surface is viewed as a two-dimensional plane where all points that have the same response are connected to produce contour lines of constant responses. A surface plot generally displays a three-dimensional view that may provide a clearer picture of the response. If the regression model (i.e. first-order model) contains only the main effects and no interaction effect, the fitted response surface will be a plane (i.e. contour lines will be straight). If the model contains interaction effects, the contour lines will be curved and not straight. The contours produced by a second-order model will be elliptical in nature. [Figs. 4.6 and 4.7](#) illustrate the contour and surface plots of cutting tool life (hours).

Both contour and surface plots help experimenters to understand the nature of the relationship between the two factors (cutting speed and cutting angle) and the response (life in hours). As can be seen in [Figs. 4.6 and 4.7](#), the tool life increases with an increase in cutting angle and a decrease in cutting speed. Moreover, we have used a fitted surface ([Fig. 4.7](#)) to find a direction of potential improvement for a process. A formal way to seek the direction of improvement in process



**Figure 4.6** Contour plot of cutting tool life.



**Figure 4.7** Surface plot of cutting tool life.

optimisation problems is called the method of steepest ascent or descent (depending on the nature of the problem at hand, i.e. whether one needs to maximise or minimise the response of interest).

## 4.5 Model building for predicting response function

This section is focused on the model building and prediction of response function at various operating conditions of the process. Here the author uses a regression model approach to illustrate the relationship between a response and a set of process parameters (or design parameters) which affect the response. The use of this regression

model is to predict the response for different combinations of process parameters (or design parameters) at their best levels. In order to develop a regression model based on the significant effects (either main or interaction), the first step is to determine the regression coefficients. For factors at 2-levels, the regression coefficients are obtained by dividing the estimates of effects by 2. The reason is that a two-unit change (i.e. low-level setting  $(-1)$  to a high-level setting  $(+1)$ ) in a process parameter (or factor) produces a change in the response function. A regression model for factors at 2-levels is usually of the form

$$\hat{y} = \beta_0 + \beta_L x_L + \beta_2 x_2 + \dots + \beta_{L2} x_L x_2 + \beta_{L3} x_L x_3 + \dots + \varepsilon \quad (4.3)$$

where  $\beta_L$ ,  $\beta_2$  are the regression coefficients and  $\beta_0$  is the average response in a factorial experiment. The term ' $\varepsilon$ ' is the random error component which is approximately normal and independently distributed with mean zero and constant variance  $\sigma^2$ . The regression coefficient  $\beta_{L2}$  corresponds to the interaction between the process parameters  $x_1$  and  $x_2$ . For example, the regression model for the cutting tool life optimisation study is given by

$$\hat{y} = 40.833 + 5.667(B) + 3.417(C) - 4.717(AC) \quad (4.4)$$

The response values obtained from Eq. (4.4) are called predicted values and the actual response values obtained from the experiment are called observed values. Residuals can be obtained by taking the difference of observed and predicted (or fitted) values. Eq. (4.4) provides us with a tool that can be used to study the response as a function of three tool life parameters: cutting speed, tool geometry and cutting angle. We can predict the cutting tool life for various combinations of these tool parameters. For instance, if all the cutting tool life parameters are kept at low-level settings, the predicted tool life then would be

$$\begin{aligned}\hat{y} &= 40.833 + 5.667(B) + 3.417(C) - 4.417(AC) \\ &= 40.833 + 5.667(-1) + 3.417(-1) - 4.417(-1) \times (-1) \\ &= 27.332\end{aligned}$$

The observed value of tool life (refer to cube plot) is 26 h. The difference between the observed value and predicted value (i.e. residual) is  $-1.332$ . Similarly, if all the cutting tool life parameters are kept at the optimal condition (i.e. cutting speed = low, tool geometry = high and cutting angle = high), the predicted tool life would then be

$$\begin{aligned}\hat{y} &= 40.833 + 5.667(+1) + 3.417(+1) - \{4.417(-1) \times (+1)\} \\ &= 54.384\end{aligned}$$

Once the statistical analysis is performed on the experimental data, it is important to verify the results by means of confirmatory experiments or trials. The number of confirmatory runs at the optimal settings can vary from 4 to 20 (4 runs if expensive, 20 runs if cheap).

## 4.6 Confidence interval for the mean response

The statistical confidence interval (CI) (at 99% confidence limit) for the mean response can be computed using the equation

$$CI = \bar{y} \pm 3 \left\{ \frac{SD}{\sqrt{n}} \right\} \quad (4.5)$$

where  $\bar{y}$  = mean response obtained from confirmation trials or runs, SD = standard deviation of response obtained from confirmation trials,  $n$  = number of samples (or confirmation runs).

For the cutting tool life example, five samples were collected from the process at the optimal condition (i.e. cutting speed = low, tool geometry = high and cutting angle = high). The results of the confirmation trials are illustrated in [Table 4.1](#).

$$\bar{y} = 53.71 \text{ h and } SD = 0.654 \text{ h}$$

Ninety-nine per cent CI for the mean response is given by:

$$\begin{aligned} CI &= 53.71 \pm 3 \left\{ \frac{0.654}{\sqrt{5}} \right\} \\ &= 53.71 \pm 0.877 = (54.55, 52.83) \end{aligned}$$

As the predicted value based on the regression model falls within the statistical CI, we will consider our model good.

If the results from the confirmation trials or runs fall outside the statistical CI, possible causes must be identified. Some of the possible causes may be

- incorrect choice of experimental design for the problem at hand
- improper choice of response(s) for the experiment
- inadequate control of noise factors, which cause excessive variation
- omission of some important process or design parameters in the first rounds of experimentation
- measurement error
- wrong assumptions regarding interactions
- errors in conducting the experiment, etc.

**Table 4.1** Confirmation trials.

Results from confirmation trials
53.48
52.69
53.88
54.12
54.36

If the results from the confirmatory trials or runs are within the CI, then improvement action on the process is recommended. The new process or design parameters should be implemented with the involvement of top management. After the solution has been implemented, control charts on the response(s) or key process parameters should be constructed for constantly monitoring, analysing, managing and improving the process performance.

## 4.7 Statistical, technical and sociological dimensions of DOE

### 4.7.1 Statistical dimension of DOE

This dimension refers to all statistical assumptions and mathematical methods that validate the application of DOE. Some of the key aspects one may consider include ([Tanco, 2008](#)) the following:

- *Low precision of the experiment due to inadequate samples collected per experimental run* – Quite often engineers in organisations rush into experiments without having a good understanding of the number of replicates they need to have per trial condition. The levels of  $\alpha$  and  $\beta$  risks should be understood in the planning phase. Here  $\alpha$  is the risk of wrongly deciding that a process variable is a signal in our process when in reality it is not. On the other hand,  $\beta$  represents the risk of missing a signal and considering it as underlying noise. The levels of both risks should be chosen in a way that is both technically acceptable and economically feasible. The number of replicates is related to its power or capability to detect signals; as each experimental run requires resources, there is a trade-off between precision and the allocated budget for the experiment.
- *Randomisation is difficult as some of the factors were hard to change* – When some of the factors are hard to change, it is good practice to look into ‘split-plot’ design. It is common to forget the split-plot structure of the design and analyse the data as a full factorial design, but this can lead to erroneous conclusions on the determination of significant factors and their interactions.
- *Lack of proper analysis of residuals* – Some assumptions before we carry out proper statistical analysis must be verified to validate the results of the analysis. Emphasis must be given to independence of the residuals, the variance stability and normality assumption of data.
- *Data transformation before the identification of factor effects on the response variable* – In DOE, we transform the response variable to stabilise the variance of the residuals and Box–Cox transformation is very useful when little is known about the behaviour of the process.
- *Proper analysis of interactions and the confounding pattern* – Many engineers in organisations do not have a good understanding of how to analyse interactions and how to interpret the confounding structure provided by statistical software systems. This scenario is very much applicable when engineers are trying to characterise a process using low-resolution design where main effects are confounded with two interaction effects.

### 4.7.2 Technical dimension of DOE

Technical dimension refers to the way experiments are executed as well as all activities involved in experimental planning until some realistic conclusions are derived. Technical dimensions include

- *Process stability before conducting DOE* – A number of scholars debate the point as though experimenters need to achieve process stability prior to performing a designed experiment ([Costa et al., 2006](#)). Although randomisation and blocking are principles used to reduce suspected noises in the process, it is advisable to achieve process stability (as much as possible) so that noise factors will not prevent the identification of important factor and interaction effects.
- *Involvement of key players for identification of factors* – It is absolutely critical to involve all the stakeholders at the planning phase in order to reach a consensus on which factors should be included in the experiment. Experiments are always very expensive and time consuming and therefore it is advisable to clearly define the team formation and the roles and responsibilities of all team members.
- *Selection of wrong levels and not taking time to explore curvature effects* – Selecting the right process variables and choosing the appropriate levels for the process variables is not a straightforward process in industrially designed experiments. Experimenters should be able to explore the curvature effects of process variables to determine if non-linear effects are present. This can be achieved by adding centre points. It is often a good practice to start with  $2k$  factorial or  $2(k-p)$  fractional factorial experiments and then add centre points to determine the presence of curvature effects of process variables on the response or quality characteristic of interest ([Anderson and Kraber, 1999](#)).

### 4.7.3 Sociological and managerial dimensions of DOE

- DOE in an industrial context is always an iterative process; each experiment answers some questions and triggers new ones, and so on until the team concludes that the full knowledge required is sufficient to reach the expected degree of excellence of the process. Some of the sociological and managerial dimensions include
- *Communicating the need for DOE at the Senior Management level* – Clear and open communication to the senior management team about the need for DOE is a critical factor. It is absolutely essential to share world-class examples to gain the attention of the senior management team.
- *Communicating the need for DOE at the shop floor level* – Process improvement techniques such as DOE are not meant just for senior- and middle-level managers. For DOE to be successful, it is absolutely critical to involve people on the shop floor to identify the potential process variables or factors which are believed to have an impact on the response or quality characteristic. Operators and supervisors on the shop floor can also give good input into the selection of levels for each process variable.
- *Using the DOE project charter as a tool to develop a good business case for the problem* – Many Six Sigma-related projects in organisations begin with a project charter which encompasses the cost-benefits, the nature of the problem, what to measure in order to describe the problem, how to measure, etc. I do think it might be a good practice for engineers and experimenters to develop a DOE project charter at the planning phase and present it to the senior management team for approval.

## Exercises

1. What are the common barriers to the successful application of DOE?
2. Discuss the four phases in the methodology of DOE.
3. What are the criteria for the selection of an experimental design?
4. Explain the key considerations which need to be taken into account prior to executing an experiment.
5. What is the purpose of NPP of residuals?
6. Explain the role of Response Surface Plots in industrial experiments.
7. Why do we need to develop regression models?
8. What are the possible causes of experiments being unsuccessful?
9. What are the statistical dimensions of the execution of an industrially designed experiment?
10. What are the technical dimensions of the execution of an industrially designed experiment?
11. What are the managerial and sociological dimensions of the execution of an industrially designed experiment?

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# Screening designs

5

## 5.1 Introduction

In many process development and manufacturing applications, the number of potential process or design variables or parameters (or factors) is large. Screening is used to reduce the number of process or design parameters (or factors) by identifying the key ones that affect the product quality or process performance. This reduction allows one to focus process improvement efforts on the few really important factors, or the ‘vital few’.

Screening designs provide an effective way to consider a large number of process or design parameters (or factors) in a minimum number of experimental runs or trials (i.e. with minimum resources and budget). The purpose of screening designs is to identify and separate out those factors that demand further investigation. This chapter is focused on the Screening Designs expounded by [Plackett and Burman \(1946\)](#) —hence the name Plackett–Burman designs (P–B designs). P–B designs are based on Hadamard matrices in which the number of experimental runs or trials is a multiple of four, i.e.  $N = 4, 8, 12, 16$  and so on, where  $N$  is the number of trials/runs ([Plackett and Burmann, 1946](#)).

P–B designs are suitable for studying up to  $k = (N - 1)/(L - 1)$  factors, where  $L$  is the number of levels and  $k$  is the number of factors. For instance, using a 12-run experiment, it is possible to study up to 11 process or design parameters at 2-levels. One of the interesting properties of P–B designs is that all main effects are estimated with the same precision. This implies that one does not have to anticipate which factors are most likely to be important when setting up the study. For screening designs, experimenters are generally not interested in investigating the nature of interactions among the factors ([Antony, 2002](#)). The aim is to study as many factors as possible in a minimum number of trials and to identify those that need to be studied in further rounds of experimentation in which interactions can be more thoroughly assessed.

## 5.2 Geometric and non-geometric P–B designs

Geometric P–B designs are those in which  $N$  is a power of two. The number of runs can be 4, 8, 16, 32, etc. Geometric designs are identical to fractional factorial designs (refer to Chapter 7) in which one may be able to study the interactions

**Table 5.1** An eight-run geometric P–B design.

A	B	C	D	E	F	G
+1	-1	-1	+1	-1	+1	+1
+1	+1	-1	-1	+1	-1	+1
+1	+1	+1	-1	-1	+1	-1
-1	+1	+1	+1	-1	-1	+1
+1	-1	+1	+1	+1	-1	-1
-1	+1	-1	+1	+1	+1	-1
-1	-1	+1	-1	+1	+1	+1
-1	-1	-1	-1	-1	-1	-1

**Table 5.2** Design matrix for a four-run geometric P–B design.

A	B	C
-1	+1	+1
+1	-1	+1
+1	+1	-1
-1	-1	-1

between factors. For example, an eight-run geometric P–B design is presented in [Table 5.1](#). This allows one to study up to seven factors at 2-levels.

Each P–B design can be constructed easily using a ‘generating vector’ which, for example, in the case of  $N=4$  has the form  $(-1 +1 +1 +1)$ . The design matrix or experimental layout is obtained by arranging the vector as the first column and offsetting by one vector element for each new column. In other words, a new column is generated from the previous one by moving the elements of the previous column down once and placing the last element in the first position. The matrix is completed by a row of ones. [Table 5.2](#) illustrates the completed design matrix for a four-run P–B design ( $N=4$ ) using the above generating vector.

Non-geometric P–B designs are designs which are multiples of four but are not powers of two. Such designs have runs of 12, 20, 24, 28, etc. These designs do not have complete confounding of effects. For non-geometric P–B designs, each main effect is partially confounded with all interactions that do not contain the main effect ([Wheeler, 1988](#)). If the interaction effect is suspected to be large, then the interaction may distort the estimated effects of several process or design parameters, since each interaction is partially confounded with all main effects except the two interacting factors. [Table 5.3](#) illustrates the design matrix for a 12-run non-geometric P–B design with generating vector  $(+1 +1 -1 +1 +1 +1 -1 -1 -1 +1 -1)$ . This design should not be used to analyse interactions. A 12-run P–B design is generally used for studying 11 main effects. There is nothing wrong with having fewer than 11 factors. If the process is

**Table 5.3** A 12-run non-geometric P–B design.

A	B	C	D	E	F	G	H	I	J	K
+1	-1	+1	-1	-1	-1	+1	+1	+1	-1	+1
+1	+1	-1	+1	-1	-1	-1	+1	+1	+1	-1
-1	+1	+1	-1	+1	-1	-1	-1	+1	+1	+1
+1	-1	+1	+1	-1	+1	-1	-1	-1	+1	+1
+1	+1	-1	+1	+1	-1	+1	-1	-1	-1	+1
+1	+1	+1	-1	+1	+1	-1	+1	-1	-1	-1
-1	+1	+1	+1	-1	+1	+1	-1	+1	-1	-1
-1	-1	+1	+1	+1	-1	+1	+1	-1	+1	-1
-1	-1	-1	+1	+1	+1	-1	+1	+1	-1	+1
+1	-1	-1	-1	+1	+1	+1	-1	+1	+1	-1
-1	+1	-1	-1	-1	+1	+1	+1	-1	+1	+1
-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1

suspected to be highly interactive, it would be better to use a geometric design as opposed to a non-geometric design. In contrast, if interactions are of no concern to the experimenter, it is advisable to use a non-geometric design.

The generating vectors for P–B designs are as follows:

$$N = 4 (-1 + 1 + 1)$$

$$N = 8 (+1 + 1 + 1 - 1 + 1 - 1 - 1)$$

$$N = 12 (+1 + 1 - 1 + 1 + 1 + 1 - 1 - 1 + 1 - 1)$$

$$N = 16 (+1 + 1 + 1 + 1 - 1 + 1 - 1 + 1 + 1 - 1 - 1 + 1 - 1 - 1 - 1)$$

$$N = 20 (+1 + 1 - 1 - 1 + 1 + 1 + 1 - 1 + 1 - 1 + 1 + 1 - 1 - 1 + 1 + 1 - 1)$$

The obvious advantage of P–B designs is the limited number of runs to evaluate large number of factors. Since interactions are not of interest to the experimenter for P–B designs, the important main effects can be selected for more in-depth study. The obvious disadvantage of P–B designs is tied to the assumption required to evaluate up to  $k = (N - 1)$  factors in  $N$  runs. It is important to note that one can study fewer than  $(N - 1)$  factors in  $N$  runs. The unused columns can be used to estimate experimental error (Barrentine, 1999). Geometric P–B designs are resolution III designs and therefore these designs can be folded over to achieve a design resolution IV.

### Example 5.1

In this section, the author would like to illustrate a simple example with an eight-run P–B design which has been used for studying seven factors. The data for this example is taken from Barrentine's book *An introduction to Design of Experiments: A Simplified Approach*. This example is based on the manufacturing process of a paperboard product. The objective of the experiment was to increase the puncture resistance of this paperboard product. The

(Continued)

**(cont'd)**

response or quality characteristic of interest to the team conducting the experiment was the force required to penetrate the material. The objective was to maximise the mean force required to penetrate the material. Seven factors at 2-levels were studied using an eight-run geometric P–B design. [Table 5.4](#) presents the factors selected from the brainstorming session and their levels.

[Table 5.5](#) presents the results of an eight-run geometric P–B design experiment with two replicates per experimental trial condition.

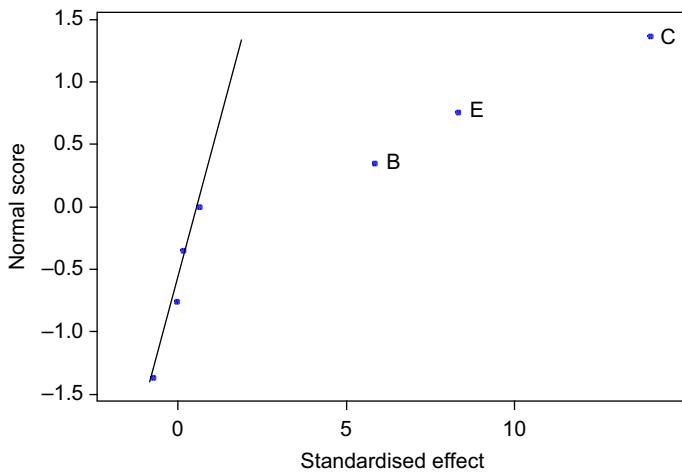
The data was analysed using Minitab software and the results are illustrated below. The first task was to identify the key main effects that were most influential on the response (i.e. force). [Fig. 5.1](#) presents a standardised normal plot of effects for the above experiment. Effects C, E and B fall away from the straight line, which implies that they are statistically significant at 5% significance level. Effects A, D, F and G fall along the straight line and therefore can be treated as inactive effects. It is important to note that one can consider even a 10% significance level for

**Table 5.4** List of factors and their levels for the experiment.

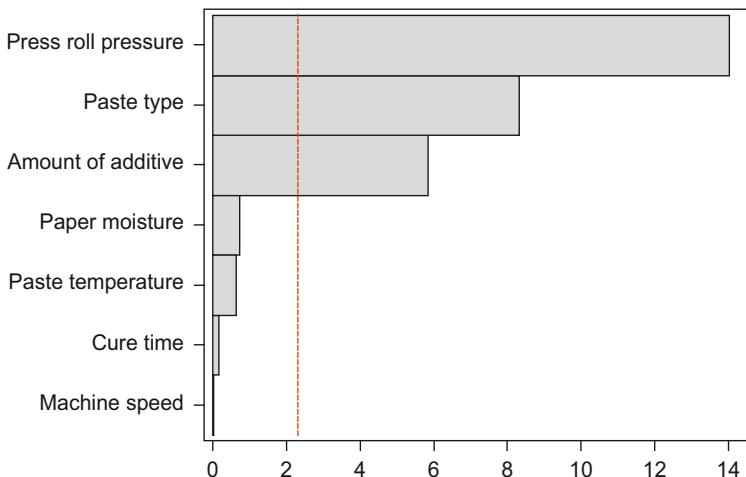
Factors	Labels	Low-level setting	High-level setting
Paste temperature	A	130°F	160°F
Amount of additive	B	0.2%	0.5%
Press roll pressure	C	40 psi	80 psi
Paper moisture	D	Low	High
Paste type	E	No clay	With clay
Cure time	F	10 days	5 days
Machine speed	G	120 fpm	200 fpm

**Table 5.5** Design matrix of an eight-run geometric P–B design for the experiment.

A	B	C	D	E	F	G	R1	R2
+1	-1	-1	+1	-1	+1	+1	12.5	16.84
+1	+1	-1	-1	+1	-1	+1	42.44	39.29
+1	+1	+1	-1	-1	+1	-1	55.08	47.57
-1	+1	+1	+1	-1	-1	+1	49.37	47.69
+1	-1	+1	+1	+1	-1	-1	55.43	52.80
-1	+1	-1	+1	+1	+1	-1	42.51	35.02
-1	-1	+1	-1	+1	+1	+1	51.13	57.92
-1	-1	-1	-1	-1	-1	-1	15.61	13.65



**Figure 5.1** NPP of standardised effects.

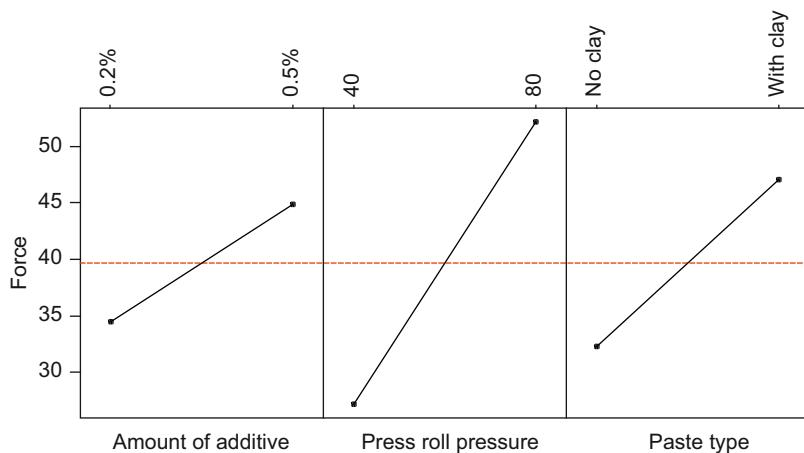


**Figure 5.2** Pareto plot of the effects for the experiment.

screening designs in order to ensure that no important factor effects or parameters are omitted in the first round of experimentation.

In order to substantiate the findings of normal plot, the author have used the Pareto plot of effects. The Pareto plot (Fig. 5.2) shows that effects C (press roll pressure), E (paste type) and B (amount of additive) are most important to the process and therefore should be studied in greater depth. The effect plot of the significant effects is shown in Fig. 5.3.

From the above results, one may conclude that main effects C (press roll pressure), E (paste type) and B (amount of additive) are found to have significant



**Figure 5.3** Main effects plot of the significant effects.

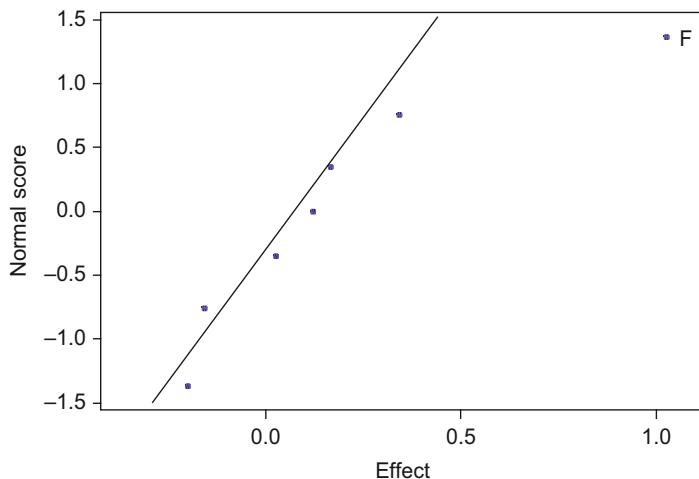
**Table 5.6** Design matrix of an eight-run geometric P–B design with standard deviation values.

A	B	C	D	E	F	G	s	ln (SD)
+1	-1	-1	+1	-1	+1	+1	3.07	1.122
+1	+1	-1	-1	+1	-1	+1	2.23	0.802
+1	+1	+1	-1	-1	+1	-1	5.31	1.670
-1	+1	+1	+1	-1	-1	+1	1.18	0.166
+1	-1	+1	+1	+1	-1	-1	1.86	0.621
-1	+1	-1	+1	+1	+1	-1	5.30	1.668
-1	-1	+1	-1	+1	+1	+1	4.80	1.569
-1	-1	-1	-1	-1	-1	-1	1.39	0.329

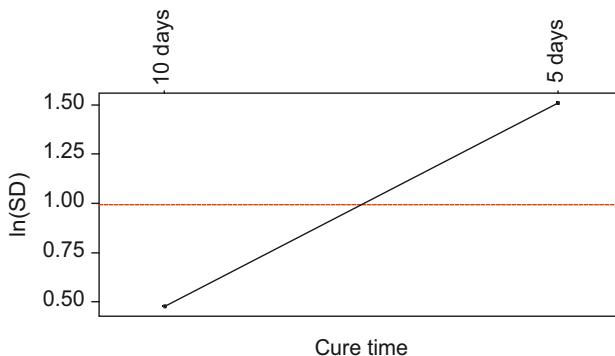
impact on the mean puncture resistance (i.e. the force required to penetrate the paper board).

In order to analyse the factors affecting variability in force, we need to calculate the SD of observations at each experimental design point. The results are given in **Table 5.6**. As we have seen before in the cake baking example (refer to Chapter 3), the SD of observations do not follow a normal distribution. Therefore we transform the sample SD by taking their logarithms, as the logarithms of the SD will be much closer to being normally distributed (refer to Chapter 3). It is important to note that SD can be computed using any scientific calculator.

**Fig. 5.4** shows a standardised normal plot of effects affecting ln(SD). The normal plot indicates that only factor F (cure time) influenced the variation in the puncture resistance (i.e. force). Further analysis of factor F has revealed that variability is maximum when cure time is set at high level (i.e. 5 days). This can be seen in **Fig. 5.5**.



**Figure 5.4** Normal plot of effects affecting variability in puncture resistance.



**Figure 5.5** Main effects plot for  $\ln(\text{SD})$ .

The conclusions are that factors C, B and E have a significant impact on process average, whereas factor F has a significant impact on process variability. The other factors such as A, D and G can be set at their economic levels since they do not appear to influence either the process average or the process variability. The next stage of the experimentation would be to consider the interaction among the factors and select the optimal settings from the experiment that yields maximum force with minimum variability. This can be accomplished by utilising more powerful designs such as full factorials or fractional factorial designs with resolution IV (i.e. main effects are free of third-order interactions or two-factor interactions are confounded with other two-factor interactions).

### Example 5.2

In this example, we consider a plastic foam extrusion process. A process improvement team was formed to investigate what affects the porosity of plastic parts. After a thorough brainstorming session with quality engineers, the process manager and the operators, it was identified that eight process parameters might have some impact on porosity. [Table 5.7](#) presents the list of parameters and their levels for the experiment. Each factor was studied at 2-levels. As the total degrees of freedom for studying eight factors at 2-levels is equal to 8, it was decided to choose a non-geometric 12-run P–B design with 11 degrees of freedom. The extra 3 degrees of freedom can be used to estimate experimental error. [Table 5.8](#) presents the experimental layout with response values in both standard and random order.

The objective of the experiment was to determine the key parameters that affect percentage porosity. The Minitab software system was used for analysis purposes. [Fig. 5.6](#) illustrates a standardised Pareto plot of effects for the experiment.

[Fig. 5.6](#) shows that process parameters such as G (adhesive coating temperature), E (extrusion speed) and F (adhesive coating thickness) have significant impact on porosity. These parameters should be further explored using full fractional designs and more advanced methods such as response surface methods, if necessary. In the next stage of experimentation, one should analyse the interactions among the parameters E, F and G. In order to identify which levels of these parameters yield minimum porosity, we may consider an effects plot ([Fig. 5.7](#)). [Fig. 5.7](#) shows that E at high level, F at low level and G at high level yields minimum porosity.

[Fig. 5.7](#) shows that porosity will decrease when temperature is kept at high level (100°C). Similarly, porosity decreases as extrusion speed is kept at high level (4.5 m/min) and coating thickness at low level (0.7 mm).

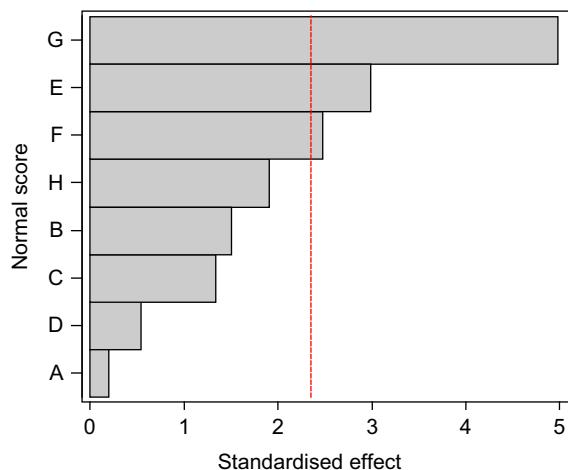
**Table 5.7** List of process parameters and their levels for the experiment.

Process parameters	Labels	Low level (-1)	High level (+1)
Temperature profile	A	1	2
Temperature after heating	B	210°C	170°C
Temperature after expansion	C	170°C	150°C
Temperature before coating die	D	130°C	115°C
Extrusion speed	E	6 m/min	4.5 m/min
Adhesive coating thickness	F	0.7 mm	0.4 mm
Adhesive coating temperature	G	115°C	100°C
Expansion angle	H	Max	Min

**Table 5.8** Experimental layout for 12-run P–B design with response values.

Run	A	B	C	D	E	F	G	H	Porosity (%)
1 (6)	+1	+1	-1	+1	+1	+1	-1	-1	44.8
2 (11)	+1	-1	+1	+1	+1	-1	-1	-1	37.2
3 (9)	-1	+1	+1	+1	-1	-1	-1	+1	36.0
4 (7)	+1	+1	+1	-1	-1	-1	+1	-1	34.8
5 (2)	+1	+1	-1	-1	-1	+1	-1	+1	46.4
6 (1)	+1	-1	-1	-1	+1	-1	+1	+1	24.8
7 (5)	-1	-1	-1	+1	-1	+1	+1	-1	43.6
8 (12)	-1	-1	+1	-1	+1	+1	-1	+1	44.8
9 (3)	-1	+1	-1	+1	+1	-1	+1	+1	24.0
10 (8)	+1	-1	+1	+1	-1	+1	+1	+1	34.4
11 (4)	-1	+1	+1	-1	+1	+1	+1	-1	27.2
12 (10)	-1	-1	-1	-1	-1	-1	-1	-1	49.6

Note: Numbers in parentheses represent the random order of experimental runs or trials.

**Figure 5.6** Standardised Pareto plot of Effects for the plastic foam extrusion process.

### Example 5.3

In this section, the author would like to illustrate an example with a 12-run Taguchi Orthogonal Array which has been used for studying seven factors. The data for this example is taken from [Kiemele et al. \(2000\)](#). In this example, we consider a process of producing the small cylindrical protective (Continued)

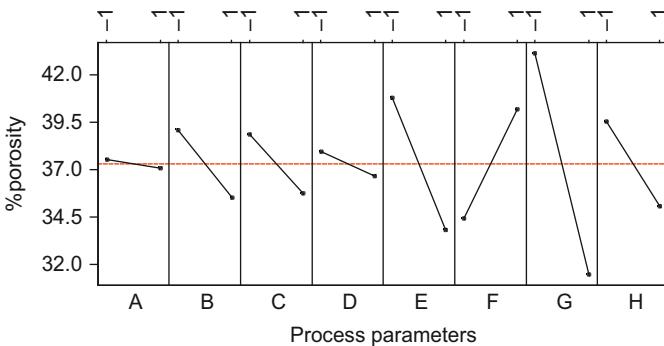


Figure 5.7 Main effects plot for the experiment.

**(cont'd)**

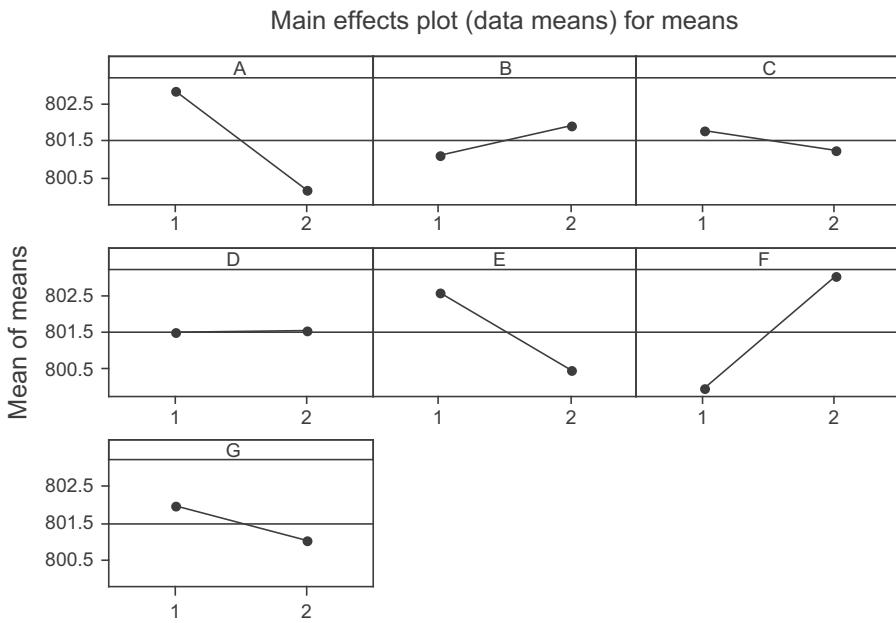
mechanism that houses the solid explosive material used to inflate the air bag in an automobile. Each trial condition was replicated four times to observe variation within the trials. The response of interest for the experiment was the diameter of cylinder and the target value for diameter was 800. Table 5.9 presents the experimental layout with the factors and the results. The last two columns represent the mean ( $\bar{y}$ ) and SD of diameter of the cylinder.

The first part of the analysis is to determine the most important factors that influence the mean diameter of the cylinder. Obviously, not all seven factors would have an equal impact on the diameter. So we may use a simple main effects plot to screen the most important ones from the unimportant ones. Fig. 5.8 shows the main effects plot. Fig. 5.8 shows that factors A, E and F are the most important ones that can be used to adjust the diameter to the target value of 800. The most interesting feature of DOE is that it can not only identify the most important factors but also understand the unimportant factors. The levels of unimportant factors can be set at their most economical levels. This would save significant cash in certain cases of industrial experiments.

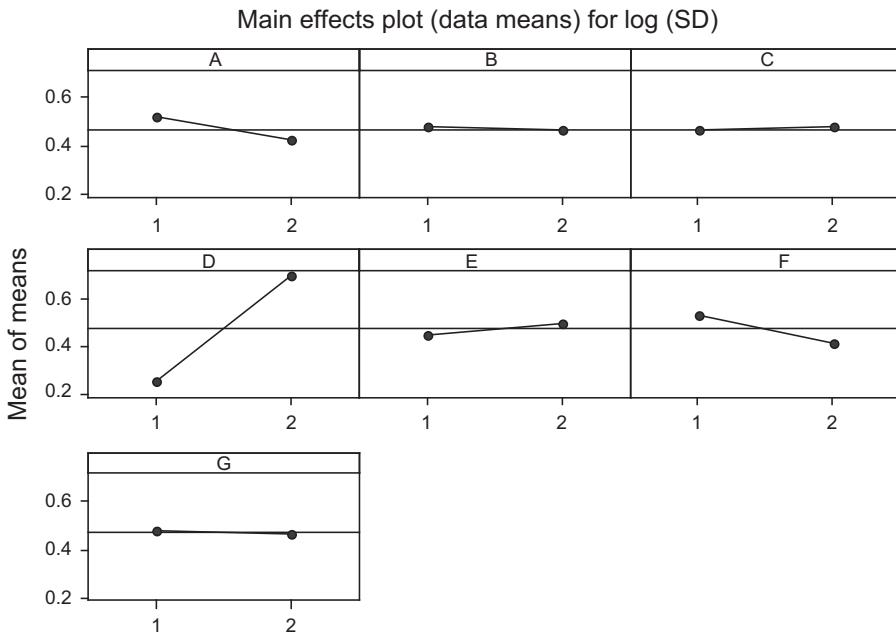
The next part of the analysis is to understand the factors which influence variability in diameter. In this instance, it is not only important to achieve a mean diameter closer to the target of 800 but also to achieve consistent diameter values closer to 800. In order to analyse variability, we compute SD at each experimental design point and use logarithmic transformation for validating normal distribution assumptions. This point is very well covered in [Lochner and Matar \(1990\)](#). It was a surprise to observe from Fig. 5.9 that factor D is the only factor which causes variation in the diameter of the cylinder. Moreover, it points out that minimum variation is obtained when we keep this factor at its low-level setting. This is a very useful piece of information for any designed experiment.

**Table 5.9** Experimental layout for screening seven factors at 2-levels.

Run	A	B	C	D	E	F	G	Y <sub>1</sub>	Y <sub>2</sub>	Y <sub>3</sub>	Y <sub>4</sub>	y-bar	SD
1	-1	-1	-1	-1	-1	-1	-1	803.00	800.77	804.64	799.34	801.94	2.35
2	-1	-1	-1	-1	-1	+1	+1	806.31	804.80	807.19	803.80	805.53	1.52
3	-1	-1	+1	+1	+1	-1	-1	806.89	795.18	797.31	809.94	802.33	7.19
4	-1	+1	-1	+1	+1	-1	+1	805.49	795.47	794.50	804.59	800.01	5.83
5	-1	+1	+1	-1	+1	+1	-1	802.29	801.69	799.96	802.94	801.72	1.28
6	-1	+1	+1	+1	-1	+1	+1	811.38	798.87	811.01	800.78	805.51	6.61
7	+1	-1	+1	+1	-1	-1	+1	795.73	794.57	801.15	794.03	796.37	3.26
8	+1	-1	+1	-1	+1	+1	+1	801.36	802.22	798.58	800.09	800.56	1.59
9	+1	-1	-1	+1	+1	+1	-1	792.32	799.13	803.69	804.33	799.87	5.54
10	+1	+1	+1	-1	-1	-1	-1	803.23	802.30	798.00	800.21	800.94	2.33
11	+1	+1	-1	+1	-1	+1	-1	806.09	801.04	806.97	805.88	804.99	2.68
12	+1	+1	-1	-1	+1	-1	+1	799.02	796.58	796.61	800.55	798.19	1.95



**Figure 5.8** Main effects plot for the experiment (mean diameter).



**Figure 5.9** Main effects plot for the experiment (analysis of diameter variability).

## Exercises

1. What are screening designs?
2. Compare geometric and non-geometric P–B designs.
3. What are the strengths and limitations of P–B designs?
4. When would you utilise screening designs in real-life situations?
5. Explain how to overcome the problem of low resolution in a screening design.

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# Full factorial designs

6

## 6.1 Introduction

It is widely accepted that the most commonly used experimental designs in manufacturing companies are full and fractional factorial designs at 2-levels and 3-levels. Factorial designs would enable an experimenter to study the joint effect of the factors (or process/design parameters) on a response. A factorial design can be either full or fractional factorial. This chapter is primarily focused on full factorial designs at 2-levels only. Factors at 3-levels are beyond the scope of this book. However, if readers wish to learn about experimental design for factors at 3-levels, the author would suggest them to refer to [Montgomery \(2001\)](#).

A full factorial designed experiment consists of all possible combinations of levels for all factors. The total number of experiments for studying  $k$  factors at 2-levels is  $2k$ . The  $2k$  full factorial design is particularly useful in the early stages of experimental work, especially when the number of process parameters or design parameters (or factors) is less than or equal to 4. One of the assumptions we make for factors at 2-levels is that the response is approximately linear over the range of the factor settings chosen. The first design in the  $2k$  series is one with only two factors, say, A and B, each factor to be studied at 2-levels. This is called a  $2^2$  full factorial design.

## 6.2 Example of a $2^2$ full factorial design

Here we consider a simple nickel plating process with two plating process parameters: plating time and plating solution temperature ([Kiemele et al., 1997](#)). Each process parameter is studied at 2-levels. The response of interest to the experimenters was plating thickness. [Table 6.1](#) illustrates the two process parameters and their chosen levels for the experiment.

[Table 6.2](#) shows the design layout of the experiment with response values. Each experimental condition was replicated five times so that a reasonable estimate of error variance (or experimental error) could be obtained.

The following are the four objectives set by the experimenter:

1. Which main effects or interactions might affect the mean plating thickness?
2. Which main effects or interactions might influence variability in plating thickness?
3. What is the best setting of factors to minimise variability in thickness?
4. How can a target plating thickness of 120 units be achieved?

**Table 6.1** Process parameters and their levels for the experiment.

Process parameters	Labels	Low level	High level
Plating time	A	4 s	12 s
Plating solution temperature	B	16°C	32°C

**Table 6.2** Design layout of the experiment with response values.

Trial number	A	B	Plating thickness				
1	4	16	116.1	116.9	112.6	118.7	114.9
2	4	32	106.7	107.5	105.9	107.1	106.5
3	12	16	116.5	115.5	119.2	114.7	118.3
4	12	32	123.2	125.1	124.5	124.0	124.7

**Table 6.3** Coded design matrix with mean plating thickness values.

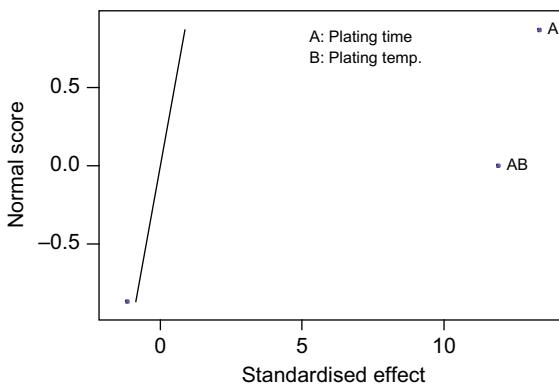
A	B	AB	Mean plating thickness
-1	-1	1	115.84
-1	1	-1	106.74
1	-1	-1	116.84
1	1	1	124.30

### 6.2.1 Objective 1: Determination of main/interaction effects that influence mean plating thickness

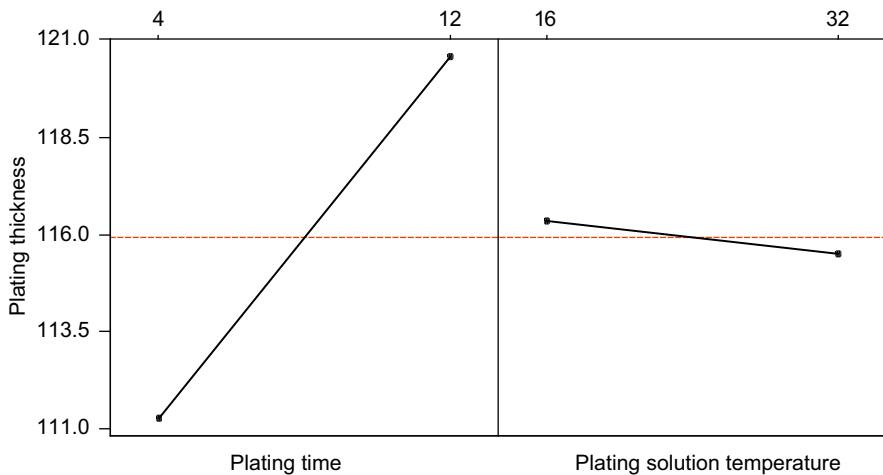
In order to determine the effect of process parameters A and B and its interaction AB, we need to construct a coded design matrix with mean plating thickness values as shown in [Table 6.3](#).

The column AB is obtained by simply multiplying the coded values in columns A and B. Interaction AB yields a combined effect of two factors, A and B. The results from Minitab software are shown below. [Fig. 6.1](#) illustrates the normal plot of effects. The graph illustrates that process parameter ‘plating time’ and the interaction between ‘plating time and plating solution temperature’ are statistically significant at 5% significance level. In other words, these effects have a large impact on the mean plating thickness, though plating solution temperature has very little impact on the mean plating thickness. This finding can be further supported by considering the main effects plot and interaction plot (see [Figs. 6.2 and 6.3](#), respectively).

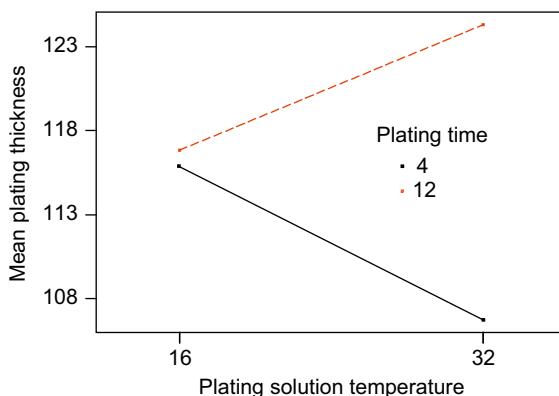
It can be seen from [Fig. 6.2](#) that plating time has a huge impact on plating thickness, whereas plating solution temperature has no impact on plating thickness whatsoever. However, it is interesting to note that plating solution temperature has a lower sensitivity to variability in plating thickness when compared to plating time. [Fig. 6.3](#) indicates that there is a strong interaction between plating time and plating thickness. Plating thickness is maximum when plating time is kept at high level



**Figure 6.1** NPP of effects for the plating experiment.



**Figure 6.2** Main effects plot for the plating experiment.



**Figure 6.3** Interaction plot – plating time  $\times$  plating solution temperature.

(12 s) and plating solution temperature is kept at high level ( $32^{\circ}\text{C}$ ). Similarly, plating thickness is minimum when plating solution temperature is kept at high level ( $32^{\circ}\text{C}$ ) and plating time is kept at low level (4 s).

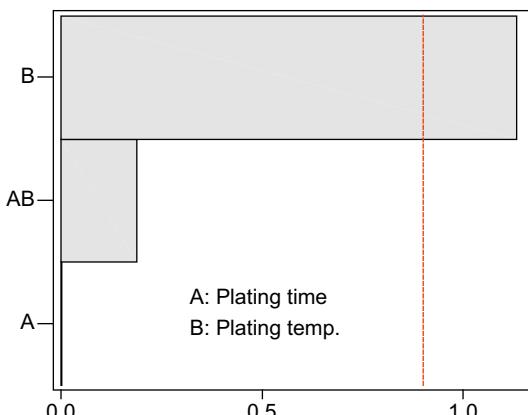
### 6.2.2 Objective 2: Determination of main/interaction effects that influence variability in plating thickness

In order to determine the effect of A, B and interaction AB on process variability, we need to construct a coded design matrix with response as variability in plating thickness (Table 6.4).

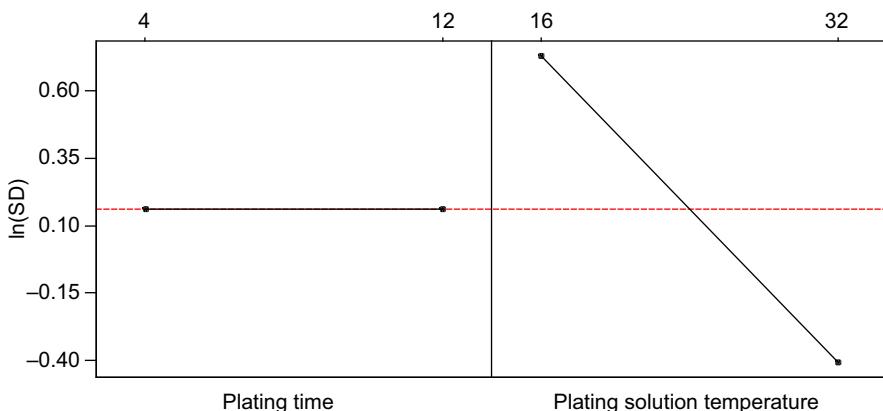
Minitab software is used to identify which effects are most important to process variability. Fig. 6.4 shows a Pareto plot of the effects on variability [ $\ln(\text{SD})$ ]. It is quite clear from the graph that process parameter plating solution temperature (B) has a significant effect on plating thickness variability, whereas plating time (A) has no impact on plating thickness variability. Interaction AB has again very little impact on variability. Fig. 6.5 shows that variability is minimum when the plating solution temperature is set at high level ( $32^{\circ}\text{C}$ ). This finding provides the answer to our objective 3, set out earlier in this chapter.

**Table 6.4** Coded design matrix with variability as response.

A	B	AB	Variability in plating thickness (SD)	$\ln(\text{SD})$
-1	-1	1	2.278	0.823
-1	1	-1	0.607	-0.499
1	-1	-1	1.884	0.633
1	1	1	0.731	-0.313



**Figure 6.4** Pareto plot of effects on plating thickness variability.



**Figure 6.5** Main effects plot with variability as response.

### 6.2.3 Objective 4: How to achieve a target plating thickness of 120 units?

In order to achieve a target plating thickness of 120 units, we need to initially develop a simple regression model (or mathematical model) which connects the response of interest (i.e., plating thickness) and the significant process parameters. In order to develop a regression model, we need to construct a table of effects and regression coefficients (Kiemele et al., 1997). It is important to recall that regression coefficients for factors at 2-levels are just half the estimate of effect. A sample calculation of how to estimate the effect of paste time and the interaction between time and temperature is shown below (Table 6.3).

#### 6.2.3.1 Effect of plating time on plating thickness

$$\begin{aligned} \text{Mean plating thickness at high level of plating time} &= (116.84 + 124.30)/2 \\ &= 120.57 \end{aligned}$$

$$\begin{aligned} \text{Mean plating thickness at low level of plating time} &= (115.84 + 106.74)/2 \\ &= 111.29 \end{aligned}$$

$$\begin{aligned} \text{Effect of plating time on plating thickness} &= (120.57 - 111.29) \\ &= 9.28 \end{aligned}$$

$$\begin{aligned} \text{Regression coefficient of plating time (A)} &= 9.28/2 \\ &= 4.64 \end{aligned}$$

#### 6.2.3.2 Interaction effect between plating time and plating solution temperature (AB)

$$\begin{aligned} \text{Referring to Column 3 in Table 7.3, the mean plating thickness at low level of AB} &= (106.74 + 116.84)/2 \\ &= 111.79 \end{aligned}$$

$$\begin{aligned} \text{Similarly, the mean plating thickness at high level of AB} &= (115.84 + 124.30)/2 \\ &= 120.07 \end{aligned}$$

$$\begin{aligned}\text{Therefore, interaction AB} &= 120.07 - 111.79 \\ &= 8.28\end{aligned}$$

Regression coefficient of the interaction term (AB) = 4.14

The regression model for the plating thickness can be therefore written as

$$\hat{y} = \beta_0 + \beta_L(A) + \beta_{L2}(AB) \quad (6.1)$$

where  $\beta_0$  = overall mean plating thickness = 115.93;  $\beta_L$  = regression coefficient of factor A (plating time);  $\beta_{L2}$  = regression coefficient of interaction AB (plating time  $\times$  plating solution temperature).

The predicted model for plating thickness is therefore given by

$$\hat{y} = 115.93 + 4.64(A) + 4.14(AB)$$

Using the above predicted model, we need to determine the settings of parameters which give a target thickness of 120 units (i.e.  $\hat{y} = 120$ ). Moreover, we know that a high level of plating solution temperature (factor B) yields minimum variability. Therefore, we can set B at a low level (i.e., 1).

$$\text{Now, we can write, } 120 = 115.93 + 4.64(A) + 4.14(A)$$

$$= 115.93 + 4.64A + 4.14A$$

$$= 115.93 + 8.78A$$

$$4.07 = 8.78A$$

$$A = 0.463 \text{ (in coded terms)}$$

$$= 8.28$$

$$= 8.28$$

$$= 8.28$$

$$= 8.28$$

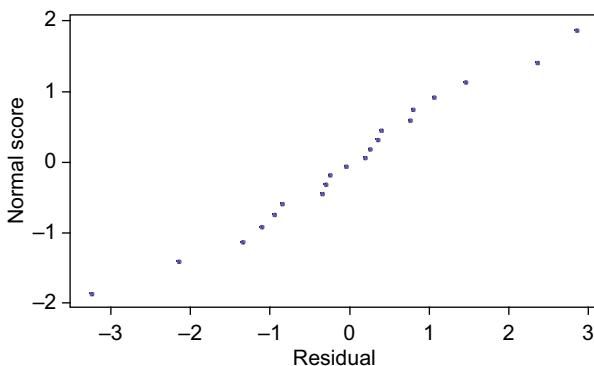
The following equation can be used to convert the coded values into actual parameter values (or vice versa).

$$\text{Actual} = \left[ \frac{\text{High} + \text{Low}}{2} \right] + \left[ \frac{\text{High} - \text{Low}}{2} \right] \cdot \text{Coded} \quad (6.2)$$

For example, for factor A, high-level setting = 12 s, low-level setting = 4 s, coded value = 0.463:

$$\begin{aligned}\text{Actual} &= \{(12 + 4)/2\} + \{((12 - 4)/2) \cdot 0.463\} \\ &= 8 + 4(0.463) \\ &= 9.85 \text{ s}\end{aligned}$$

Therefore, to achieve a target plate thickness of 120 units, we need to set the plating time for 9.85 s at a temperature of 32°C. We need to perform confirmation experiments or runs to verify the results of our analysis. If the results of the confirmation experiments or runs (i.e., each observation from the trials) fall within the interval of  $\hat{y} \pm 3$  (s.e.), then the results are satisfactory. Here s.e. refers to standard



**Figure 6.6** NPP of residuals for the plating experiment.

error and is obtained by  $s/\sqrt{n}$ , where SD is the sample standard deviation and  $n$  is sample size.

The analysis of a  $2k$  factorial design assumes that the observations are normally and independently distributed (Logothetis, 1992). The best way to check the normality assumption is by constructing an NPP of residuals (Box et al., 1978). Fig. 6.6 presents the normal probability of residuals for the plating experiment. As the residuals fall approximately along a straight line, we can conclude that the data come from a normal population.

### 6.3 Example of a $2^3$ full factorial design

Now we consider an experiment with three factors at 2-levels. The response of interest for the experiment was yield of a chemical process. The list of process parameters and their levels are presented in Table 6.5.

It was important to analyse all the two-factor interactions and therefore a  $2^3$  full factorial design was chosen. Each trial condition was replicated three times in order to obtain an accurate estimate of experimental error (or error variance). The following objectives were set prior to performing the experiment.

1. Which main effects or interactions might affect the average process yield?
2. Which main effects or interactions might influence variability in process yield?
3. What is the optimal process condition?

**Table 6.5** List of process parameters and their levels.

Process parameters	Labels	Low level	High level
Temperature	T	80°C	120°C
Pressure	P	50 psi	70 psi
Reaction time	R	5 min	15 min

### 6.3.1 Objective 1: To identify the significant main/interaction effects that affect the process yield

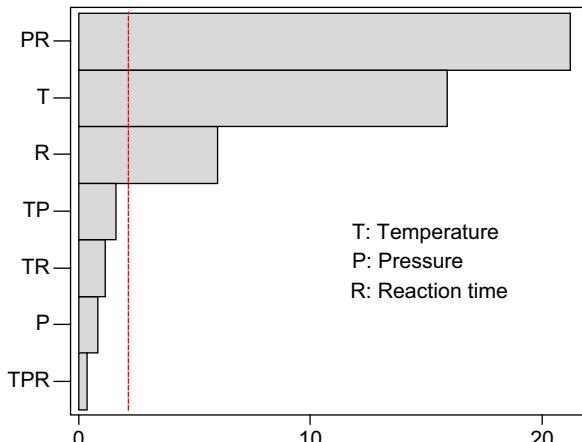
In order to identify the significant main/interaction effects, it was decided to construct an experimental layout (Table 6.6), which shows all the combinations of process parameters at their respective levels. The table shows the actual settings of the process parameters with the response values (i.e., yield) recorded at each trial condition.

Fig. 6.7 illustrates the Pareto plot of effects. The graph shows that main effects T (temperature) and R (reaction time), and interaction between pressure (P) and reaction time (R), are significant at 5% significance level. It is quite interesting to note that pressure (P) on its own has no significant impact on the process yield. It is important to analyse the interaction between P and R for determining the best settings for optimising the chemical process yield.

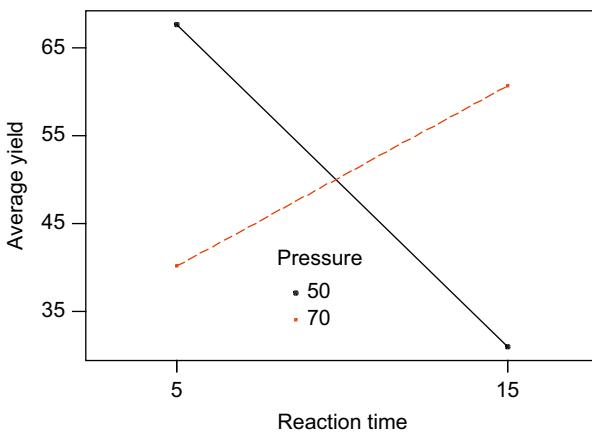
Fig. 6.8 indicates that there exists a strong interaction between pressure and reaction time. It is clear that the effects of reaction time at different levels of pressure are different. Yield is minimum when the pressure is kept at a low level (50 psi)

**Table 6.6** Experimental layout with response values.

Run/trial	T	P	R	Yield 1 (%)	Yield 2 (%)	Yield 3 (%)
1	80	50	5	61.43	58.58	57.07
2	120	50	5	75.62	77.57	75.75
3	80	70	5	27.51	34.03	25.07
4	120	70	5	51.37	48.49	54.37
5	80	50	15	24.80	20.69	15.41
6	120	50	15	43.58	44.31	36.99
7	80	70	15	45.20	49.53	50.29
8	120	70	15	70.51	74.00	74.68



**Figure 6.7** Pareto plot of effects for the yield example.



**Figure 6.8** Interaction plot – pressure  $\times$  reaction time.

**Table 6.7** Design matrix with variability as response of interest.

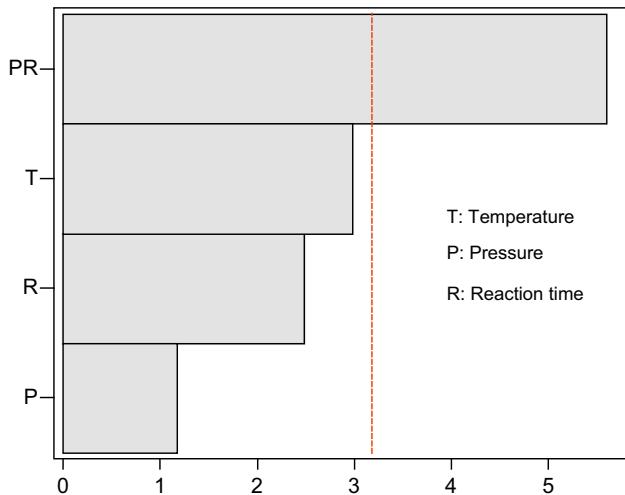
Run	T	P	R	SD	ln(SD)
1	-1	-1	-1	2.214	0.795
2	1	-1	-1	1.090	0.086
3	-1	1	-1	4.632	1.533
4	1	1	-1	2.940	1.078
5	-1	-1	1	4.707	1.549
6	1	-1	1	4.032	1.394
7	-1	1	1	2.746	1.010
8	1	1	1	2.237	0.805

and reaction time at high level (15 min). Maximum yield is obtained when the pressure and reaction time are kept at low levels.

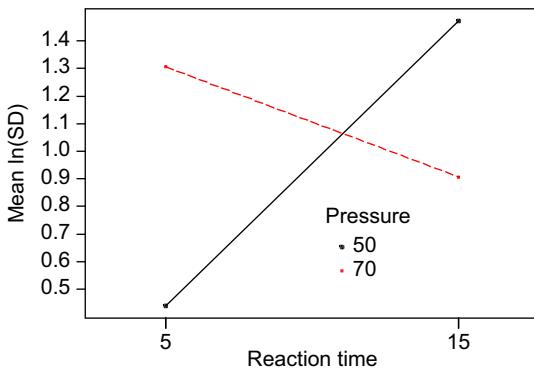
### 6.3.2 Objective 2: To identify the significant main/interaction effects that affect the variability in process yield

In order to identify the significant main/interaction effects that affect process variability, we need to construct a coded design matrix with  $\ln(\text{SD})$  as the response of interest. **Table 6.7** illustrates the design matrix with variability as the response. Due to zero degrees of freedom for the error term, we need to rely on a procedure called ‘pooling’ of insignificant effects (Taguchi, 1987). Pooling is a process of obtaining a more accurate estimate of error variance. Taguchi advocates pooling effects until the degrees of freedom for the error term is approximately equal to half the total degrees of freedom for the experiment.

For the present example, the author has pooled interactions TR, TP and TPR so that three degrees of freedom have been created for the error term. A Pareto plot of the effects is shown in [Fig. 6.9](#). The figure shows that none of the main effects have



**Figure 6.9** Pareto plot of effects with  $\ln(\text{SD})$  as response of interest.



**Figure 6.10** Interaction plot of  $\ln(\text{SD})$  – pressure  $\times$  reaction time.

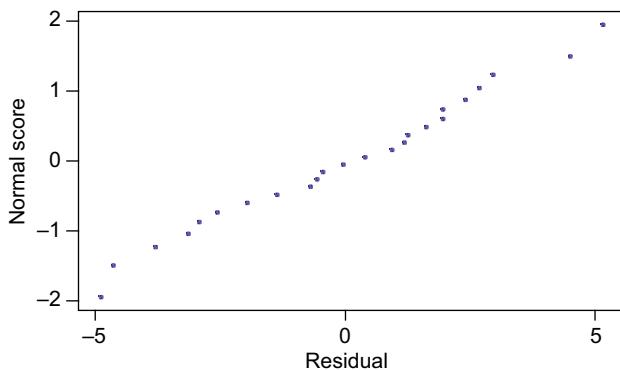
any impact on variability. Interaction between pressure (P) and reaction time (R) seems to have some impact on variability (Fig. 6.10). It can be seen that variability is minimum when pressure is kept at low level and reaction time at low level.

### 6.3.3 Objective 3: What is the optimal process condition?

In order to determine the optimal condition for the process, it is important that we need to analyse both response mean and variability. The best settings for maximising the process yield are as follows:

Temperature (T) – High level ( $120^{\circ}\text{C}$ )

Pressure (P) – Low level (50 psi)



**Figure 6.11** NPP of residuals for the yield experiment.

Reaction time (R) — Low level (5 min)

Similarly, the best settings for minimising response variability are:

Temperature (T) — High level (120°C)

Pressure (P) — Low level (50 psi)

Reaction time (R) — Low level (5 min)

The above settings can be easily obtained by analysing the mean process yield and mean  $\ln(\text{SD})$  values at both low- and high-level settings of T, P and R.

For normality assumption of data, it is best to construct an NPP of residuals (Fig. 6.11). The graph indicates that the data come from a normal population.

## 6.4 Example of a $2^4$ full factorial design

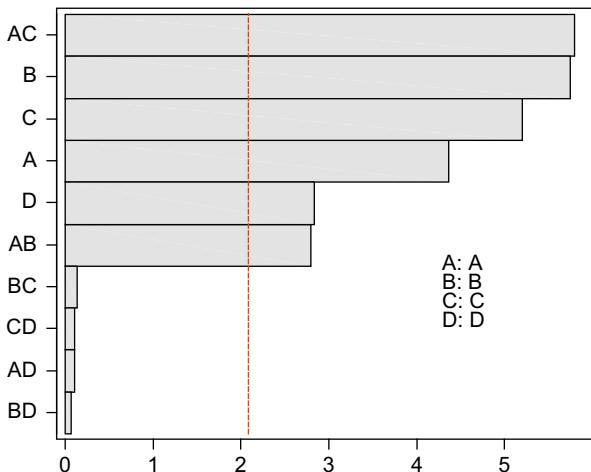
In the last example, the author will consider an example with four factors. This example shows the results of an experiment to study the effect of four factors on a cracking problem. A nickel–titanium alloy is used to make components for jet turbine aircraft engines. Cracking is a potentially serious problem in the final part, because it can lead to non-recoverable failure and subsequent rejection of the part, thereby causing waste. The objective of the experiment was therefore to identify the key factors and their interactions (if existing) which have effect on cracks. Four factors were considered: pouring temperature (A), titanium content (B), heat treatment method (C) and the amount of grain refiner used (D). Each factor was studied at 2-levels and a  $2^4$  full factorial design was selected. Table 6.8 presents the experimental layout used for this experiment to minimise cracks. The response of interest to the experimenter was the length of crack (in  $\text{mm} \times 10^{-2}$ ). Each trial condition was replicated twice to estimate error variance.

The following are the objectives of the experiment:

1. Which of the main/interaction effects affect mean crack length?
2. Which main effects or interactions might influence variability in crack length?
3. What is the optimal process condition to minimise mean crack length?

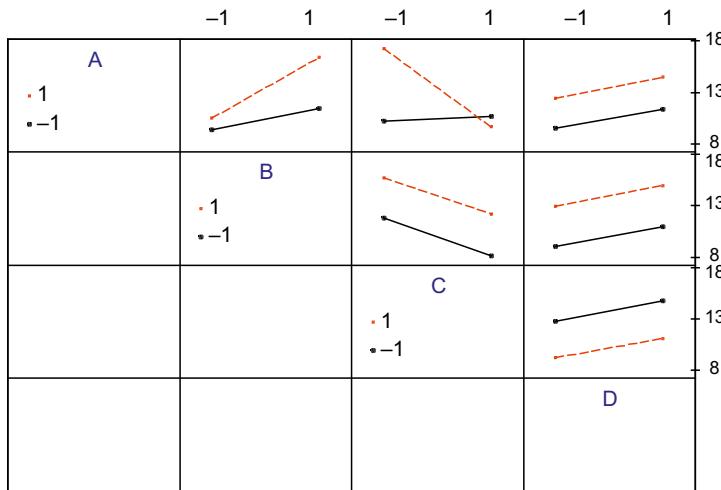
**Table 6.8** Experimental layout with response values.

Run	A	B	C	D	Crack length	
1	-1	-1	-1	-1	7.037	6.376
2	1	-1	-1	-1	14.707	15.219
3	-1	1	-1	-1	11.635	12.089
4	1	1	-1	-1	17.273	17.815
5	-1	-1	1	-1	10.403	10.151
6	1	-1	1	-1	4.368	4.098
7	-1	1	1	-1	9.360	9.253
8	1	1	1	-1	13.440	12.923
9	-1	-1	-1	1	8.561	8.951
10	1	-1	-1	1	16.867	17.052
11	-1	1	-1	1	13.876	13.658
12	1	1	-1	1	19.824	19.639
13	-1	-1	1	1	11.846	12.337
14	1	-1	1	1	6.125	5.904
15	-1	1	1	1	11.190	10.935
16	1	1	1	1	15.653	15.053

**Figure 6.12** Pareto plot of effects for the above example.

#### 6.4.1 Objective 1: Which of the main/interaction effects affect mean crack length?

In order to identify the key main and interaction effects that affect crack length, a Pareto plot of effects (Fig. 6.12) was constructed. The Pareto plot clearly indicates that all the main effects (A, B, C and D) and two two-factor interactions (AB and AC) are statistically significant at 5% significance level. In order to understand the



**Figure 6.13** Interactions graph for the experiment.

nature of interactions among the factors, the author would suggest that readers refer to Fig. 6.13.

Fig. 6.13 indicates that there is a strong interaction between A and B; and A and C (due to non-parallel lines). We don't generally study three-factor (or three-way) interactions as they are not important in real-life settings.

#### 6.4.2 Objective 2: Which of the main/interaction effects affect variability in crack length?

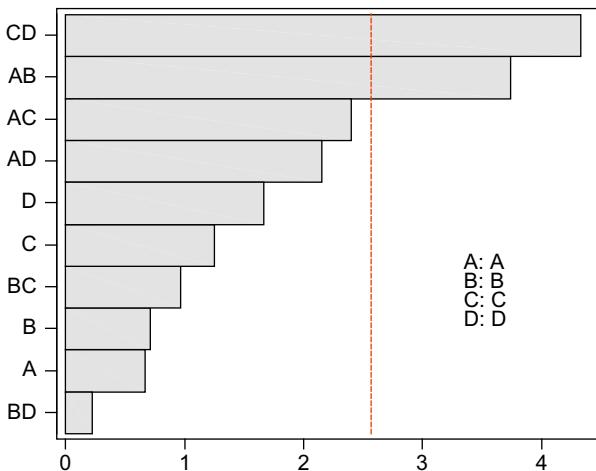
For many industrial experiments, it is important to understand which factors affect mean response and which ones affect response variability. For optimisation problems, we need to minimise response variability around the target performance (Dean and Voss, 1999). This is one of the fundamental objectives of robust design methodology.

In order to analyse which factors affect variability in crack length, we need to construct a design matrix with  $\ln(\text{SD})$  as the response. Table 6.9 presents the design matrix with  $\ln(\text{SD})$  as the response of interest.

In order to identify the factors/interactions that affect variability in crack length, a Pareto plot of effects was constructed (Fig. 6.14). The Pareto plot has shown that none of the main effects has a significant effect on variability in crack length. Two interactions (AB and CD) are believed to have significant impact on the variability. Fig. 6.15 illustrates the interaction plot between factors A and B. It is quite clear from the graph that there exists a strong interaction between factors A and B. The variability in crack length is minimum when A is kept at low level and B at high level. Similarly, C at low level and D at high level yield minimum variability in crack length. However, it is interesting to observe that factor D is less sensitive to variability when C is kept at high level.

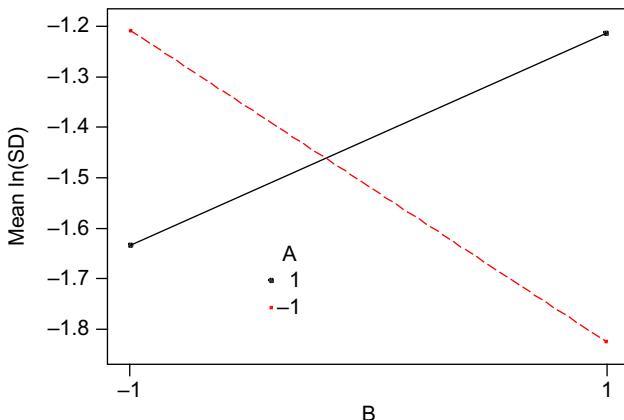
**Table 6.9** Experimental layout with response values.

Run	A	B	C	D	SD	ln(SD)
1	-1	-1	-1	-1	0.467	-0.761
2	1	-1	-1	-1	0.362	-1.016
3	-1	1	-1	-1	0.321	-1.136
4	1	1	-1	-1	0.383	-0.960
5	-1	-1	1	-1	0.178	-1.726
6	1	-1	1	-1	0.191	-1.655
7	-1	1	1	-1	0.076	-2.577
8	1	1	1	-1	0.366	-1.005
9	-1	-1	-1	1	0.276	-1.287
10	1	-1	-1	1	0.131	-2.033
11	-1	1	-1	1	0.154	-1.871
12	1	1	-1	1	0.131	-2.033
13	-1	-1	1	1	0.347	-1.058
14	1	-1	1	1	0.156	-1.858
15	-1	1	1	1	0.180	-1.715
16	1	1	1	1	0.424	-0.858

**Figure 6.14** Pareto plot for ln(SD).

### 6.4.3 Objective 3: What is the optimal process condition to minimise mean crack length?

In this section, the author will demonstrate how to determine the settings of A, B, C and D to minimise mean crack length. As interactions AB and AC have a significant impact on mean crack length, we need to analyse the mean crack length for all the four combinations between these two factors. [Tables 6.10 and 6.11](#) present the

**Figure 6.15** Interaction between A and B (response:  $\ln(\text{SD})$ ).**Table 6.10** Mean crack length for all combinations of A and B.

A	B	Mean crack length
-1	-1	9.458
1	-1	10.542
-1	1	11.5
1	1	16.453

**Table 6.11** Mean crack length for all combinations of A and C.

A	C	Mean crack length
-1	-1	10.273
1	-1	17.300
-1	1	10.684
1	1	9.696

mean crack length at all combinations of factor levels of A and B and A and C, respectively.

It is also observed that factor D at low level yields minimum crack length. Therefore, the optimal condition of the process to minimise crack length is as follows:

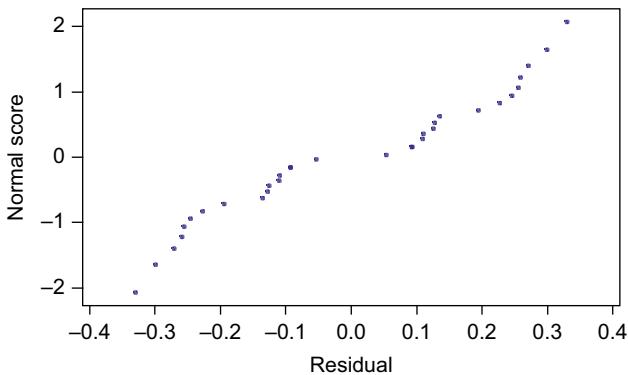
Factor A – Low level (-1)

Factor B – Low level (-1)

Factor C – High level (1)

Factor D – Low level (-1)

The NPP of residuals (Fig. 6.16) shows that the data comes from a normal population.



**Figure 6.16** NPP of residuals for the above data.

**Table 6.12** List of process variables and their levels for the experiment.

Process variables	Labels	Low level	High level
Carbonation	A	10%	12%
Operating pressure	B	25 psi	30 psi
Line speed	C	200 bottles per minute (bpm)	250 bottles per minute (bpm)

#### 6.4.4 More examples of FFEs

In this section, we consider a couple of examples to help you understand the use of FFEs in two different contexts. The first example is about obtaining more uniform fill heights in soft drink bottles. The filling machine theoretically fills each bottle to the correct target height. However, the bottle manufacturer was experiencing variation in fill heights and it was quite important for the company to reduce variation around the target height. The engineering team of the company identified three process variables that could influence the fill heights during the filling process. It was decided to keep each process variable at 2-levels. This would lead to eight experimental trials or runs. [Table 6.12](#) presents the list of process variables (or factors) and their respective levels for the experiment.

[Table 6.13](#) shows the experimental layout with the list of process variables and the possible combinations.

The response or quality characteristic of interest for the experiment was deviation from the target fill height. [Table 6.14](#) presents the coded layout with the response values.

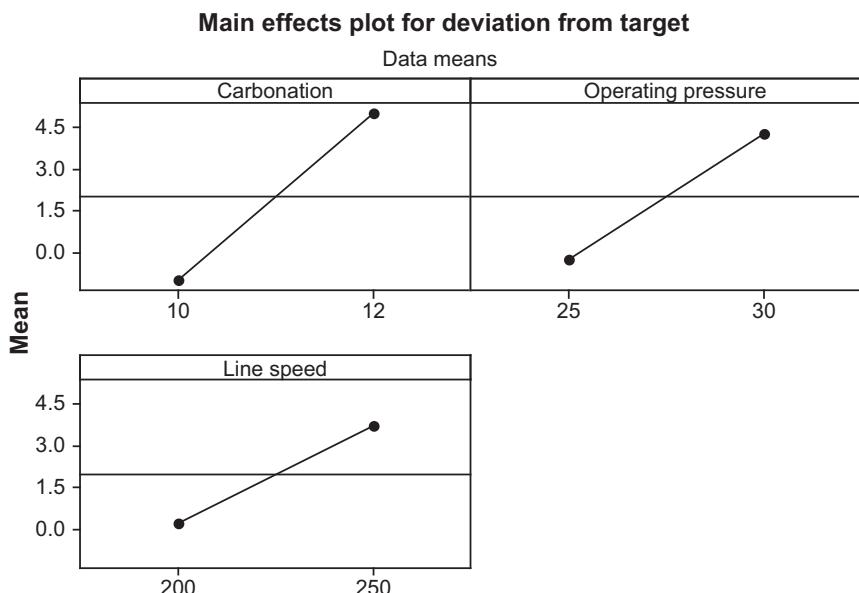
[Fig. 6.17](#) shows a main effects plot for the process variables. The main effects plot shows that carbonation is the most important factor, followed by operating pressure and finally line speed. We also look at the interaction graph to determine if any interaction exists among these process variables. [Fig. 6.18](#) shows the interaction graph for all three process variables. It was found that there is no interaction

**Table 6.13** Experimental layout with all the process variables.

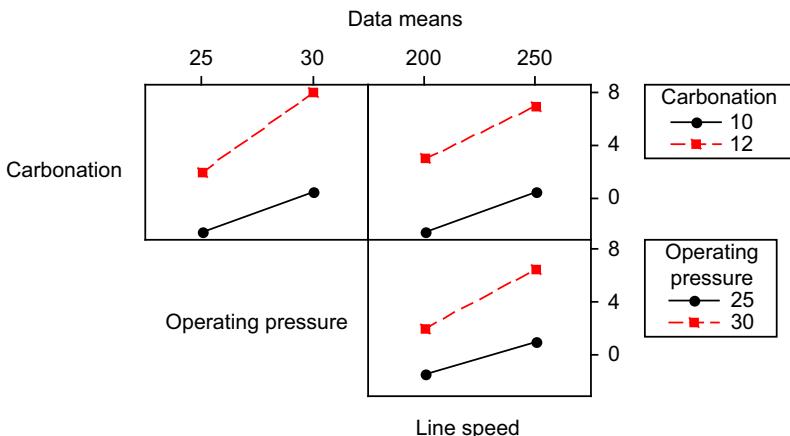
Experimental run	A (%)	B	C
1	10	25	200
2	12	25	200
3	10	30	200
4	12	30	200
5	10	25	250
6	12	25	250
7	10	30	250
8	12	30	250

**Table 6.14** Coded experimental layout with response values.

Experimental run	A	B	C	Deviation from the target fill height (y)
1	-1	-1	-1	-4
2	+1	-1	-1	1
3	-1	+1	-1	-1
4	+1	+1	-1	5
5	-1	-1	+1	-1
6	+1	-1	+1	3
7	-1	+1	+1	2
8	+1	+1	+1	11

**Figure 6.17** Main effects for the process variables.

### Interaction plot for deviation from target



**Figure 6.18** Interaction plot (carbonation, operating pressure and line speed).

**Table 6.15** Factors and their levels for the reactor experiment.

Factors	Labels	Units	Low level (-1)	High level (+)
Temperature	A	°C	24	35
Pressure	B	psig	10	15
Concentration	C	%	2	4
Stir rate	D	rpm	15	30

between carbonation and line speed. However, there was some interaction between the operating pressure and carbonation as well as operating pressure and line speed (Oehlert, 2000).

The second example describes a designed experiment executed to study the influence of four factors on the filtration rate of a high-pressure chemical reactor. Table 6.15 presents the list of factors and levels for the chemical reactor experiment.

The response of interest in this experiment was filtration rate measured in gallons per hour. The objective of the experiment was to understand which factors and their interactions (if any) are influencing the response. We also needed to maximise the filtration rate. In other words, we needed to determine the levels of factors that maximise the filtration rate.

It was decided to perform a  $2^4$  FFE with no replicates. Table 6.16 illustrates the results of the 16-run experiment. The table is a coded design matrix showing all the possible combinations of factors at their respective levels. Table 6.16 shows that trial number or run number 12 has provided the experimenters with the highest filtration rate. The lowest filtration is obtained for trial number 9. Having collected the data, the next step was to understand which factors and their interactions have an impact on the filtration rate.

**Table 6.16** Experimental design layout with the results for reactor study.

Trials	A	B	C	D	Filtration rate (gallons per hour)
1	-1	-1	-1	-1	45.0
2	+1	-1	-1	-1	71.0
3	-1	+1	-1	-1	48.0
4	+1	+1	-1	-1	65.0
5	-1	-1	+1	-1	68.0
6	+1	-1	+1	-1	60.0
7	-1	+1	+1	-1	80.0
8	+1	+1	+1	-1	65.0
9	-1	-1	-1	+1	43.0
10	+1	-1	-1	+1	100.0
11	-1	+1	-1	+1	45.0
12	+1	+1	-1	+1	104.0
13	-1	-1	+1	+1	75.0
14	+1	-1	+1	+1	86.0
15	-1	+1	+1	+1	70.0
16	+1	+1	+1	+1	96.0

Source: Data from Montgomery, D.C., 2001. Design and Analysis of Experiments, fifth ed. John Wiley & Sons, New York.

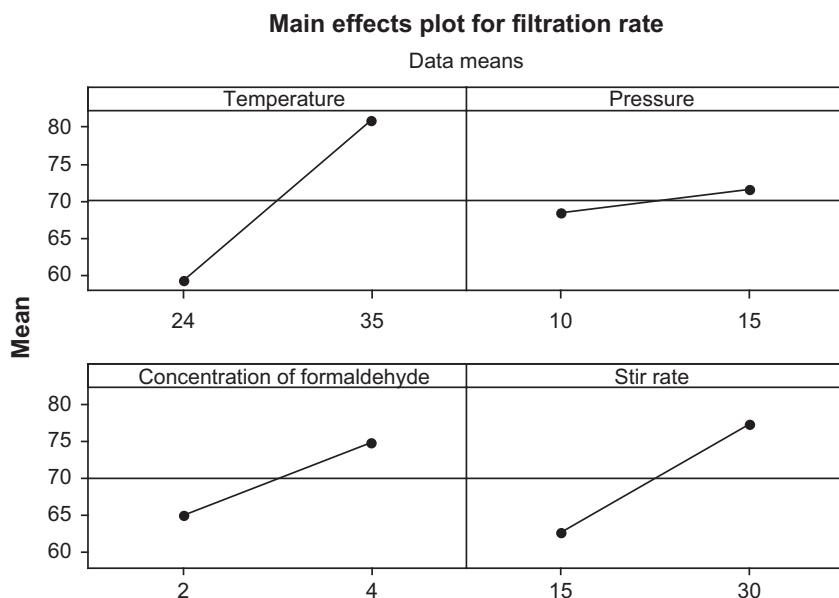
**Figure 6.19** Main effects plot for the reactor experiment.

Fig. 6.19 shows the main effects plot for the reactor experiment. The main effects plot indicates that temperature and stir rate are the most influential factors, followed by concentration of formaldehyde and pressure. It was interesting to note

that pressure has very little influence on the filtration rate and the level of pressure can be kept at either 10 or 15 psig. The experimenters also wanted to minimise the concentration of formaldehyde and hence we needed to determine the best level of this factor to give the maximum infiltration rate. As this factor did not appear to be the most important factor, and moreover since trials 10 and 12 gave the highest filtration rates at low levels of concentration, we could safely keep this factor at a low-level setting (that is, 2% concentration of formaldehyde). The best possible settings for maximising the filtration rate, therefore, are as follows (based on main effects plot):

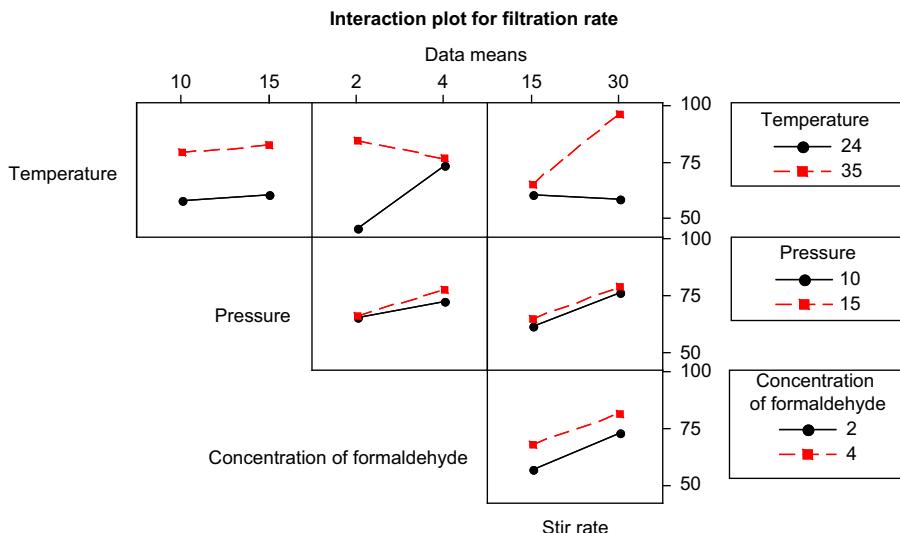
Temperature – High level – 35°C

Pressure – High level – 15 psig

Concentration of formaldehyde – Low level – 2%

Stir rate – High level – 30 rpm

We also explored the nature of interactions among the factors to make sure that levels were chosen correctly for maximising the filtration rate. Fig. 6.20 depicts the interaction plot among all the factors. It is clear from the interaction graph that there are some strong interactions between temperature and concentration of formaldehyde as well as temperature and stir rate. However, there was no interaction between temperature and pressure, pressure and stir rate or stir rate and concentration of formaldehyde. Further analysis of the interaction graph between temperature and concentration reveals that the filtration rate is highest when temperature is kept at high level and concentration at low level. Also, the interaction graph between temperature and stir rate clearly indicates that the filtration rate is maximum when temperature and stir rate are kept at high levels.



**Figure 6.20** Interaction plot for the reactor experiment.

## Exercises

1. An engineer is interested in the effects of cutting speed (CS), tool geometry (TG), and cutting angle (CA) on the life (in hours) of a machine tool. A  $2^3$  full factorial design was chosen and the results are shown below. Each trial condition was replicated twice.

Run	CS	TG	CA	Life	
1	-1	-1	-1	22	31
2	1	-1	-1	32	43
3	-1	1	-1	35	34
4	1	1	-1	55	47
5	-1	-1	1	44	45
6	1	-1	1	40	37
7	-1	1	1	60	50
8	1	1	1	39	41

- a. Which effects appear to have a significant effect on the tool life?
  - b. What is the optimal condition if the objective of the experiment is to maximise tool life?
  - c. How do you validate the assumption of normality?
2. In a certain casting process for manufacturing jet engine turbine blades, the objective of the experiment is to determine the most significant main and interaction effects that affect part shrinkage. Three factors [mould temperature (A), metal temperature (B) and pour speed (C)] were studied at 2-levels using a  $2^3$  FFE. The following table presents the results of the experiment. Each trial condition was replicated three times to obtain sufficient degrees of freedom for the error term.

Run	C	B	A	Shrinkage values (%)		
1	-1	-1	-1	2.22	2.11	2.14
2	1	-1	-1	1.42	1.54	1.05
3	-1	1	-1	2.25	2.31	2.21
4	1	1	-1	1.00	1.38	1.19
5	-1	-1	1	1.73	1.86	1.79
6	1	-1	1	2.71	2.45	2.46
7	-1	1	1	1.84	1.76	1.70
8	1	1	1	2.27	2.69	2.71

- a. Which effects appear to have a significant effect on the percentage of shrinkage?
  - b. Which effects appear to have a significant effect on variability in shrinkage?
3. A  $2^3$  FFE was conducted to study the influence of temperature (A), pressure (B) and cycle time (C) on the occurrence of splay in an injection moulding process. For each of the eight unique trials, 50 parts were made and the response of interest to the experimenter was the number of incidences of the occurrence of splay on the surface of the part across all 50 parts. The following table shows the experimental layout with the data.

Run	A	B	C	Response
1	-1	-1	-1	12
2	1	-1	-1	15

(Continued)

(Continued)

Run	A	B	C	Response
3	-1	1	-1	24
4	1	1	-1	17
5	-1	-1	1	24
6	1	-1	1	16
7	-1	1	1	24
8	1	1	1	28

- a. Compute all the main and interaction effects.
- b. Construct a Pareto plot of the effect estimates. Which of the effects appear to be statistically significant?
4. A  $2^3$  FFE was performed in a packaging industry offering food service products, consumer packaging and packaging machinery. The following table shows the results of the experiment with dry crush being the response of the experiment. It was decided to keep the belt tension constant throughout the experiment. Moreover, each trial or run was replicated to capture variability due to process, machine set-up, operator, etc.
- a. Which effects appear to have a significant influence on dry crush?
- b. Construct an interaction graph and identify which of the effects interact.

Run	Score depth	Speed	Temperature	Dry crush
1	High	18	75	311.5
2	Low	18	75	315.1
3	High	22	75	261.6
4	Low	22	75	353.8
5	High	18	145	280.6
6	Low	18	145	335.2
7	High	22	145	353.2
8	Low	22	145	352.4
9	High	18	75	299.5
10	Low	18	75	295.1
11	High	22	75	286.4
12	Low	22	75	319.0
13	High	18	145	271.2
14	Low	18	145	329.4
15	High	22	145	312.4
16	Low	22	145	365.6

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# Fractional factorial designs

7

## 7.1 Introduction

Very often experimenters do not have adequate time, resources or budget to carry out FFEs. If the experimenters can reasonably assume that certain higher-order interactions (third order and higher) are not important, then information on the main effects and two-order interactions can be obtained by running only a fraction of the FFE. A type of orthogonal array design which allows experimenters to study main effects and desired interaction effects in a minimum number of trials or experimental runs is called a fractional factorial design. These fractional factorial designs are the most widely and commonly used types of design in industry. These designs are generally represented in the form  $2(k-p)$ , where  $k$  is the number of factors and  $1/2^p$  represents the fraction of the full factorial  $2k$  (Box et al., 1978). For example,  $2^{(5-2)}$  is a 1/4th fraction of a  $2^5$  FFE. This means that one may be able to study 5 factors at 2-levels in just 8 experimental trials instead of 32 trials.

## 7.2 Construction of half-fractional factorial designs

The construction of half-fractions of a FFE is simple and straightforward. Consider a simple experiment with three factors. Table 7.1 presents the design matrix with all the main and interaction effects assigned to various columns of the matrix. Based on our assumption about three-factor (or third-order) and higher-order interactions being negligible, one could use the ABC interaction column in Table 7.1 to generate settings for the fourth factor D. In other words, we would be able to study

**Table 7.1** Design matrix of an eight-run experiment with three factors.

Run	A	B	AB	C	AC	BC	ABC
1	-1	-1	1	-1	1	1	-1
2	1	-1	-1	-1	-1	1	1
3	-1	1	-1	-1	1	-1	1
4	1	1	1	-1	-1	-1	-1
5	-1	-1	1	1	-1	-1	1
6	1	-1	-1	1	1	-1	-1
7	-1	1	-1	1	-1	1	-1
8	1	1	1	1	1	1	1

four factors using eight runs by deliberately aliasing factor D with ABC interaction. This is referred to as a  $2^{(4-1)}$  factorial design ([Table 7.2](#)).

In [Table 7.2](#),  $D = ABC$  implies that main effect D is confounded (or aliased) with a third-order interaction ABC. However, a third-order interaction is of no interest to experimenters. The ‘design generator’ of this design is given by  $D = ABC$ . We refer to design generator as a word. The defining relation of this design is given by  $D \cdot D^2 = ABCD = I$ , where ‘I’ is the identity element. Once we know the defining relation of a design, we can then generate the alias structure for that particular design.

In the above experiment,  $I = ABCD$  (defining relation)

In order to determine the alias of A, we multiply both sides of the defining relation by ‘A’. This yields the following:

$$A \times I = A = A \times ABCD = A^2BCD = BCD, \text{ as } A^2 = 1.$$

We can now generate aliases of B and C as follows:

$$B \times I = B = ACD$$

$$C \times I = C = ABD$$

Because we are generally interested in two-factor interactions, we can also generate aliases for all two-factor interactions as follows:

$$I \times AB = A^2B^2CD = CD$$

$$I \times AC = A^2C^2BD = BD$$

$$I \times BC = B^2C^2AD = AD$$

$$I \times AD = A^2D^2CB = BC$$

$$I \times BD = B^2D^2CA = AC$$

$$I \times CD = C^2D^2AB = AB$$

**Table 7.2** Design matrix of a  $2^{(4-1)}$  factorial design.

Run	A	B	AB	C	AC	BC	D = ABC
1	-1	-1	1	-1	1	1	-1
2	1	-1	-1	-1	-1	1	1
3	-1	1	-1	-1	1	-1	1
4	1	1	1	-1	-1	-1	-1
5	-1	-1	1	1	-1	-1	1
6	1	-1	-1	1	1	-1	-1
7	-1	1	-1	1	-1	1	-1
8	1	1	1	1	1	1	1

Similarly, we can generate aliases for three-factor interactions as follows:

$$\begin{aligned}I \times ABC &= A^2B^2C^2D = D \\I \times ABD &= A^2B^2D^2C = C \\I \times ACD &= A^2C^2D^2B = B \\I \times BCD &= B^2C^2D^2A = A\end{aligned}$$

**Table 7.3** presents the complete aliasing pattern (or confounding pattern) for four factors in eight runs. Minitab software generates the confounding pattern for various types of designs involving up to 15 factors at 2-levels.

For the above design, the resolution is IV (as main effects are confounded with three-factor interactions and two-factor interactions are confounded with other two-factor interactions). In real-life situations, certain two-factor interactions may be confounded with other two-factor interactions, and hence we cannot determine which of the two-factor interactions are important to that process. Under such circumstances we may use ‘fold-over designs’. Fold-over designs are used to reduce confounding when one or more effects cannot be estimated independently or separately. In other words, the effects are said to be aliased. However, fold-over designs are used in resolution III designs to break the links between main effects and two-factor interaction effects. For example, if you fold on one factor, say A, then A and all its two-factor interactions will be free from other main effects and two-factor interactions. If you fold on all factors, then all main effects will be free from each other and from all two-factor interactions.

In a fold-over design, one may perform a second experiment where the factor levels are all the opposite of what they were in the first experiment. That is, interchange the  $-1$ s and  $+1$ s before carrying out the second experiment. However, such designs are not recommended when limited time and resources are available

**Table 7.3** Aliasing pattern for  $2^{(4-1)}$  factorial experiment.

Effect	Alias
A	BCD
B	ACD
C	ABD
D	ABC
AB	CD
AC	BD
BC	CD
AD	BC
BD	AC
CD	AB
ABC	D
ABD	C
ACD	B
BCD	A

for industrial designed experiments. Under such circumstances, sound engineering judgements coupled with knowledge in the subject matter would be of great help to experimenters in separating out the main effects from confounded interaction effects.

### 7.3 Example of a $2^{(7-4)}$ factorial design

The following section describes an example of a fractional factorial design with resolution III. The example is adapted from Box et al. (1978). This example involves an experiment to study the effect of seven factors at 2-levels using eight trials. The response of interest for the experiment was the time (seconds) taken to climb a hill for a particular person on a bicycle. Table 7.4 illustrates the list of factors and their levels used for the experiment.

**Table 7.5** presents the experimental layout with the response values. The runs were performed in random order on eight successive days. This is a  $2^{(7-4)}$  factorial design with a design resolution III (i.e. main effects are confounded with two-factor interactions).

**Table 7.4** List of factors and their levels for the experiment.

Factors	Labels	Low level	High level
Seat	A	Up	Down
Dynamo	B	Off	On
Handlebars	C	Up	Down
Gear	D	Low	Medium
Raincoat	E	On	Off
Breakfast	F	Yes	No
Tyres	G	Hard	Soft

**Table 7.5** Experimental design layout of the experiment.

Minitab software is used for the statistical analysis of data. The first step in the analysis is to identify the most important factors which influence the time to cycle up the hill (seconds). A Pareto plot is constructed to identify the key factors (Fig. 7.1). The graph shows that the positions of the gear (D) and the dynamo (B) have a significant effect on the time.

The design generators of the above design are as follows:

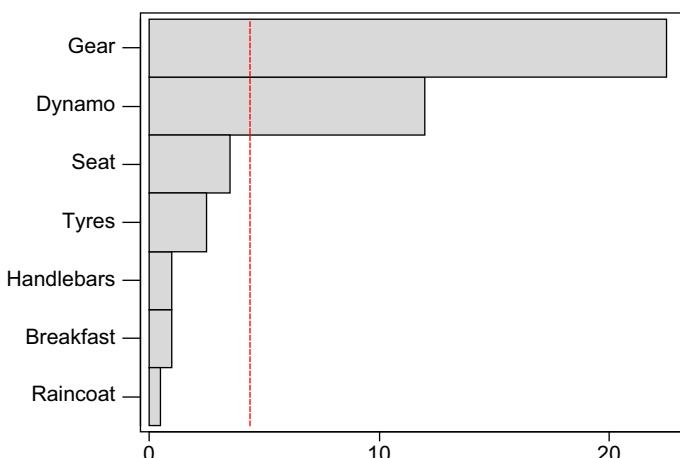
$$D = AB, E = AC, F = BC \text{ and } G = ABC$$

Therefore defining relation can be obtained as follows:

$$\begin{aligned} I &= ABD = ACE = BCF = ABCG = BCDE = ACDF = ABEF \\ &= CDG = BEG = AFG = DEF = ADEG = BDFG = ABCDEFG \end{aligned}$$

As we are interested in only main effects and two-factor interactions, the seven main effects and their aliases can be generated in the following manner. As all factors were studied at 2-levels, we estimate only the linear effects of the factors which are confounded with two-factor interactions. For instance, the linear effect of A ( $\ell_A$ ) is estimated to be 3.5. However, factor A is confounded with three two-factor interactions such as BD, CE and FG.

$$\begin{aligned} \ell_A &= 3.5 \rightarrow A + BD + CE + FG \\ \ell_B &= 12.0 \rightarrow B + AD + CF + EG \\ \ell_C &= 1.0 \rightarrow C + AE + BF + DG \\ \ell_D &= 22.5 \rightarrow D + AB + CG + EF \\ \ell_E &= 0.50 \rightarrow E + AC + BG + DF \\ \ell_F &= 1.0 \rightarrow F + AG + BC + DE \\ \ell_G &= 2.5 \rightarrow G + AF + BE + CD \end{aligned}$$

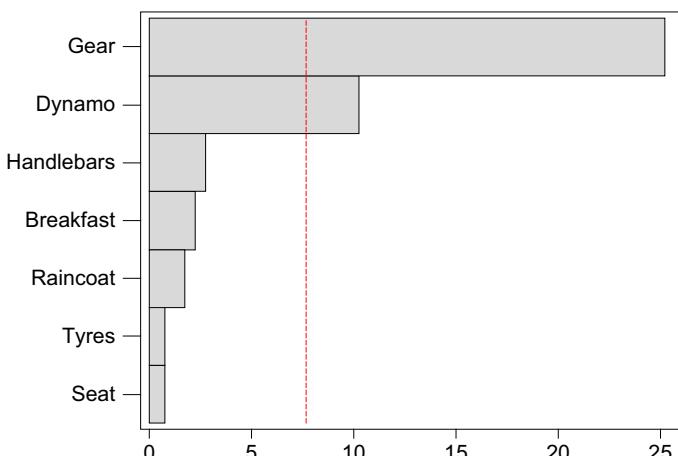


**Figure 7.1** Pareto plot of effects for the bicycle data.

As only B and D are two significant effects, we need to analyse them further as D is confounded with B and A, and B is confounded with A and D. Here the largest effect is due to factor D and it is not easy to conclude that the effect of D is large just because of factor D or the confounded two-factor interactions. This problem can be tackled by folding on factor D and by reversing the signs of column containing factor D. This fold-over design is given in [Table 7.6](#) along with the observed responses. It is quite interesting to observe that both factors B and D turn out to be significant again ([Fig. 7.2](#)).

**Table 7.6** Fold-over design by folding on just one factor.

Run	A	B	C	D = -AB	E = AC	F = BC	G = ABC	Time to climb hill (s)
1	-1	-1	-1	-1	1	1	-1	47
2	1	-1	-1	1	-1	1	1	74
3	-1	1	-1	1	1	-1	1	84
4	1	1	-1	-1	-1	-1	-1	62
5	-1	-1	1	-1	-1	-1	1	53
6	1	-1	1	1	1	-1	-1	78
7	-1	1	1	1	-1	1	-1	87
8	1	1	1	-1	1	1	1	60



**Figure 7.2** Pareto plot of effects for the fold-over design data.

The effects estimated by the second fraction are as follows:

$$\begin{aligned}\ell_{A*} &= 0.750 \rightarrow A - BD + CE + FG \\ \ell_{B*} &= 10.25 \rightarrow B - AD + CF + EG \\ \ell_{C*} &= 2.75 \rightarrow C + AE + BF - DG \\ \ell_{D*} &= 25.25 \rightarrow D - AB - CG - EF \\ \ell_{E*} &= -1.75 \rightarrow E + AC + BG - DF \\ \ell_{F*} &= -2.25 \rightarrow F + AG + BC - DE \\ \ell_{G*} &= -0.75 \rightarrow G + AF + BE - CD\end{aligned}$$

By combining the effect estimates from this second fraction with the effect estimates from the original eight runs, we obtain the following estimates of the effects:

$$\begin{aligned}\ell_A + \ell_{A*} &= 2(A + CE + FG) \text{ or } \frac{1}{2}(\ell_A + \ell_{A*}) = A + CE + FG \\ \text{i.e. } \frac{1}{2}(3.5 + 0.750) &= 2.125 = A + CE + FG\end{aligned}$$

Similarly,

$$\begin{aligned}\frac{1}{2}(10.25 + 12.0) &= 11.125 = B + CF + EG \\ \frac{1}{2}(2.75 + 1.0) &= 1.875 = C + AE + BF \\ \frac{1}{2}(25.25 + 22.5) &= 23.875 = D \\ \frac{1}{2}(-1.75 + 0.5) &= -0.625 = E + AC + BG \\ \frac{1}{2}(-2.25 + 1.0) &= -0.625 = F + AG + BC \\ \frac{1}{2}(-0.75 + 2.5) &= 0.75 = G + AF + BE\end{aligned}$$

We may also write

$$\begin{aligned}\ell_A - \ell_{A*} &= 2 \times BD \text{ or } \frac{1}{2}(\ell_A - \ell_{A*}) = BD \\ \text{i.e. } \frac{1}{2}(3.5 - 0.750) &= BD \text{ or } BD = 1.38\end{aligned}$$

Similarly,

$$\frac{1}{2}(12.0 - 10.25) = AD \text{ or } AD = 0.88$$

$$\frac{1}{2}(1.0 - 2.75) = DG \text{ or } DG = -0.88$$

$$\frac{1}{2}(22.5 - 25.25) = AB + CG + EF \text{ or } AB + CG + EF = -1.38$$

$$\frac{1}{2}(0.50 + 1.75) = DF = 1.13$$

$$\frac{1}{2}(1.0 + 2.25) = DE = 1.625$$

$$\frac{1}{2}(2.5 + 0.75) = CD = 1.625$$

It can be concluded from the above results that the large main effect due to the ‘gear’ (factor D) is now estimated to be free of bias from two-factor interactions. The joint effect of three second-order interactions (i.e. AB + EF + CG) appears to be small. Moreover, all the two-factor interactions involving the factor D are now free of aliases. Similarly, we can conclude that the effect of 2 two-factor interactions (CF and EG), which are aliased with main effect B, is shown to be small. Therefore it is safe to say that it is the effect of B which is important in this experiment and has significant impact on the response (i.e. time to climb up the hill).

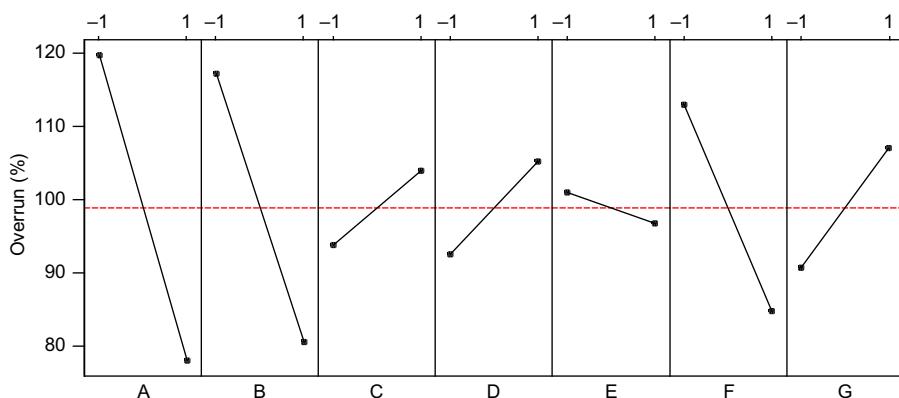
## 7.4 An application of 2-level fractional factorial design

In this section, the author will now demonstrate another application of a 2-level fractional factorial design in the development of a soybean whipped topping. This example is adapted from [Chow et al. \(1983\)](#) published in the *Journal of Food Science*. Non-dairy whipped topping is a fabricated food product that serves as a substitute for whipped cream dessert topping. It is generally formulated with sodium caseinate, vegetable fat, carbohydrates and emulsifiers. The response of interest for this experiment was percentage overrun (or whipability). Seven process variables (or factors) at 2-levels were studied using eight runs. The idea was to separate out the key process variables from the unimportant ones. The experimental layout with responses is given in [Table 7.7](#). Each trial condition was randomised to minimise the effect of any noise (or hidden variables) induced into the experiment.

[Fig. 7.3](#) presents the main effects plot for the experiment. Main effects A, B, F and G appear to be important, whereas main effects due to C, D and E do not appear to be important to the process. These effects have been pooled to generate

**Table 7.7** Experimental layout for the soybean whipped topping experiment.

Run	A	B	C	D = AB	E = AC	F = BC	G = ABC	Overrun (%)
1	-1	-1	-1	1	1	1	-1	115
2	1	-1	-1	-1	-1	1	1	81
3	-1	1	-1	-1	1	-1	1	110
4	1	1	-1	1	-1	-1	-1	69
5	-1	-1	1	1	-1	-1	1	174
6	1	-1	1	-1	1	-1	-1	99
7	-1	1	1	-1	-1	1	-1	80
8	1	1	1	1	1	1	1	63

**Figure 7.3** Main effects plot for the soybean whipped topping experiment.

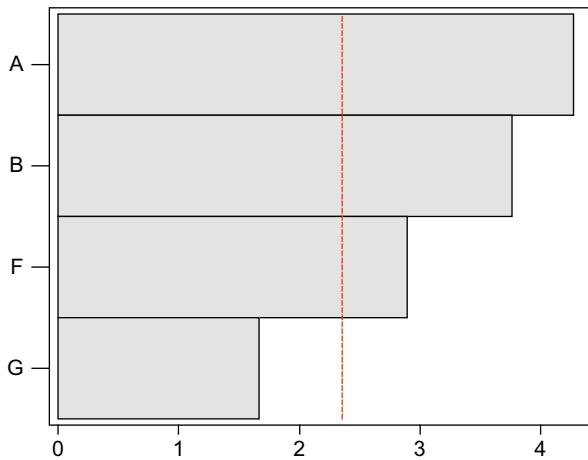
adequate degrees of freedom for the error term. Fig. 7.4 illustrates the Pareto plot of effects which implies that factors A (soybean emulsion), B (vegetable fat) and F (carbohydrates) are statistically significant and therefore should be studied in detail. The next section will look into the design generators, defining relation and confounding or aliasing pattern for the experiment.

The design generators of the design are as follows:

$$D = AB, E = AC, F = BC \text{ and } G = ABC$$

The defining relationship for this design is therefore obtained by adding to the generators all of their products taken two, three and four at a time. The complete defining relation is therefore generated as

$$\begin{aligned} I &= ABD = ACE = BCF = ABCG = BCDE = ACDF = CDG = ABEF \\ &= AFG = BEG = DEF = CEFG = ADEG = BDFG = ABCDEFG \end{aligned}$$



**Figure 7.4** Pareto plot of effects for the experiment.

Based on the above defining relations, one can generate the following linear combinations of confounded effects.

$$\ell_A = -41.75 \rightarrow A + BD + CE + FG$$

$$\ell_B = -36.75 \rightarrow B + AD + CF + EG$$

$$\ell_C = 10.25 \rightarrow C + AE + BF + DG$$

$$\ell_D = 12.75 \rightarrow D + AB + CG + EF$$

$$\ell_E = -4.25 \rightarrow E + AC + BG - DF$$

$$\ell_F = -28.25 \rightarrow F + AG + BC + DE$$

$$\ell_G = 16.25 \rightarrow G + AF + BE + CD$$

From the Pareto plot, we might conclude that the three main effects (A, B and F) are the important variables which affect whipability. But we cannot make any valid conclusions at this point as the main effects due to A, B and F are confounded with a number of two-factor interactions. For example, we cannot conclude that factor A is significant due to its true effect on whipability; rather, it is significant due to interactions BD/CE or FG. In order to remove the ambiguity surrounding the results of this experiment, one could perform a fold-over (or mirror image) design. In this case, we have folded on all factors in order to make the main effects free from each other and from two-factor interactions. Therefore a second  $2^{(7-4)}$  fractional factorial design is performed by switching the signs from  $-1$  to  $1$  and vice versa for all of the columns in the original experimental layout given in [Table 7.7](#) (Drain, 1997). The results of the fold-over experiment are given in [Table 7.8](#).

The design generators of the second fraction are as follows:

$$D = -AB, E = -AC, F = -BC \text{ and } G = ABC$$

In other words, column for process variable D is obtained by multiplying columns with process variables A and B and the resultant by  $(-1)$ . Similarly, column

**Table 7.8** Experimental layout for the soybean whipped topping experiment.

E is obtained by multiplying A and C first and then the resultant by  $(-1)$ . The same process is repeated for process variable F.

The defining relationship for the folded design is therefore obtained by adding to the generators all of their products taken two, three and four at a time. The complete defining relation for the folded (or mirror image) design is therefore generated as

$$\begin{aligned} I &= -ABD = -ACE = -BCF = ABCG = BCDE = ACDF = -CDG = ABEF \\ &= -AFG = -BEG = -DEF = CEFG = ADEG = BDFG = -ABCDEF \end{aligned}$$

Based on the above defining relations, one can generate the following linear combinations of confounded effects (assuming that third- and higher-order interactions can be neglected).

$$\begin{aligned} \ell_{A*} &= -47.5 \rightarrow A - BD - CE - FG \\ \ell_{B*} &= 67.00 \rightarrow B - AD - CF - EG \\ \ell_{C*} &= 6.50 \rightarrow C - AE - BF - DG \\ \ell_{D*} &= 63.00 \rightarrow AB - D + CG + EF \\ \ell_{E*} &= -2.50 \rightarrow AC - E + BG + DF \\ \ell_{F*} &= -35.00 \rightarrow BC - F + AG + DE \\ \ell_{G*} &= -3.00 \rightarrow G - AF - BE - CD \end{aligned}$$

By combining the effect estimates from this second fraction with the effect estimates from the original eight runs, we obtain the following estimates of the effects:

$$\begin{aligned} \ell_A + \ell_{A*} &= 2A \text{ or } \frac{1}{2}(\ell_A + \ell_{A*}) \\ \text{i.e. } \frac{1}{2}(-41.75 + 47.5) &= -44.625 = A \end{aligned}$$

Similarly,

$$\begin{aligned} \frac{1}{2}(-67.0 + -36.75) &= -51.875 = B \\ \frac{1}{2}(10.25 + -6.50) &= 1.875 = C \\ \frac{1}{2}(12.75 + 63) &= 37.875 = (AB + CG + EF) \\ \frac{1}{2}(2.50 - 4.25) &= -0.875 = (AC + BG + DF) \\ \frac{1}{2}(35.00 - 28.25) &= 3.375 = (BC + AG + DF) \\ \frac{1}{2}(16.25 - 3.00) &= 6.625 = G \end{aligned}$$

Similarly,

$$\frac{1}{2}(-41.750 - (-47.50)) = 2.875 = BD + CE + FG$$

$$\frac{1}{2}(-36.750 - (-67.00)) = 15.125 = AD + CF + EG$$

$$\frac{1}{2}(10.25 - (-6.50)) = -8.375 = AE + BF + DG$$

$$\frac{1}{2}(12.75 - 63.00) = -25.125 = D$$

$$\frac{1}{2}(-4.25 - 2.50) = -3.375 = E$$

$$\frac{1}{2}(-28.25 - 35.00) = -31.625 = F$$

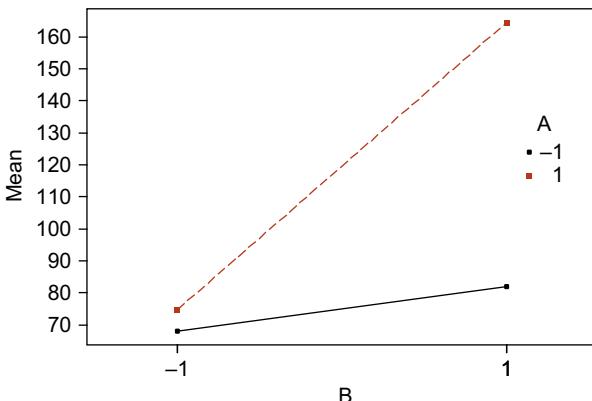
$$\frac{1}{2}(16.25 - (-3.00)) = 9.625 = AF + BE + CD$$

The estimates of the main effects and sets of three two-factor interactions are summarised in [Table 7.9](#).

An examination of [Table 7.9](#) shows that main effects A, B, D and F and the linear combination of three two-factor interactions (AB, CG and EF) appear to be important. However, we cannot tell which of the above three-factor interactions is responsible. It is clear from [Table 7.9](#) that factors C, E and G have no impact on the percentage overrun. Hence it can be concluded that it is AB interaction which is important with respect to the overrun, as both factors A and B have a

**Table 7.9** Estimates of effects from combined designs.

Estimate of effect A = -44.625
Estimate of effect B = -51.875
Estimate of effect C = 1.875
Estimate of effect D = -25.125
Estimate of effect E = -3.375
Estimate of effect F = -31.625
Estimate of effect G = 6.625
Estimate of AB + CG + EF = 37.875
Estimate of AC + BG + DF = -0.875
Estimate of BC + AG + DE = 3.375
Estimate of BD + CE + FG = 2.875
Estimate of AD + CF + EG = 15.125
Estimate of AE + BF + DG = 8.375
Estimate of AF + BE + CD = 9.625



**Figure 7.5** Interaction between A and B.

significant influence on the overrun. Fig. 7.5 illustrates the interaction graph between A and B. The graph shows that there exists a strong interaction between A and B.

#### 7.4.1 Example of a $2^{(5-1)}$ factorial design

The next example is about the investigation of the effect of five factors on the free height of leaf springs used in an automotive application (for more information on the case study, the readers may refer to the *Journal of Quality Technology*, Vol. 17, pp. 198–206, 1985). Table 7.10 presents the experimental layout and the recorded values of free height. Each trial condition was replicated three times to determine the variability within the trial conditions. The five factors used for the experiment are A = furnace temperature, B = heating time, C = transfer time, D = hold down time and E = quench oil temperature. This is a  $2^{(5-1)}$  fractional factorial design with design generator D = ABC. In other words, the design resolution of the experiment is IV. This implies that main effects are confounded with three-factor interactions or that two-factor interactions are confounded with other two-factor interactions.

The defining relation is given by I = ABCD. The aliasing or confounding structure is shown below.

$$A = BCD, B = ACD, C = ABD, D = ABC$$

$$AB = CD, AC = BD, AD = BC$$

$$ABC = D, ABD = C, ACD = B, BCD = A$$

The following are the objectives of this experiment.

1. What factors influence the mean free height?
2. What factors affect variability in the free height of springs?

**Table 7.10** Experimental layout with response values.

Run	A	B	C	D	E	Free height values		
1	-1	-1	-1	-1	-1	7.78	7.81	7.78
2	1	-1	-1	1	-1	8.15	7.88	8.18
3	-1	1	-1	1	-1	7.50	7.56	7.50
4	1	1	-1	-1	-1	7.59	7.75	7.56
5	-1	-1	1	1	-1	7.54	8.00	7.88
6	1	-1	1	-1	-1	7.69	8.06	8.09
7	-1	1	1	-1	-1	7.44	7.52	7.56
8	1	1	1	1	-1	7.56	7.69	7.81
9	-1	-1	-1	-1	1	7.50	7.25	7.12
10	1	-1	-1	1	1	7.44	7.88	7.88
11	-1	1	-1	1	1	7.50	7.56	7.50
12	1	1	-1	-1	1	7.56	7.63	7.75
13	-1	-1	1	1	1	7.32	7.44	7.44
14	1	-1	1	-1	1	7.69	7.56	7.62
15	-1	1	1	-1	1	7.18	7.25	7.18
16	1	1	1	1	1	7.50	7.81	7.59

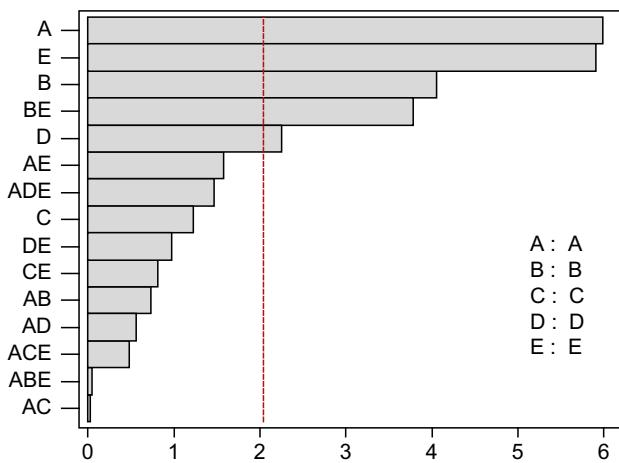
#### 7.4.2 Objective 1: To identify the factors which influence the mean free height

Minitab software is used to identify the factors which influence the mean free height of leaf springs. Fig. 7.6 illustrates a Pareto plot of effects which indicate that main effects A, B, D and E and a two-factor interaction BE are considered to have significant impact on mean height at 5% significance level. In order to validate the assumption of normality, the author has constructed a normal probability of residuals (Fig. 7.7). The normal plot has shown that the residuals fall approximately along a straight line and hence we may conclude that the data come from a normal population.

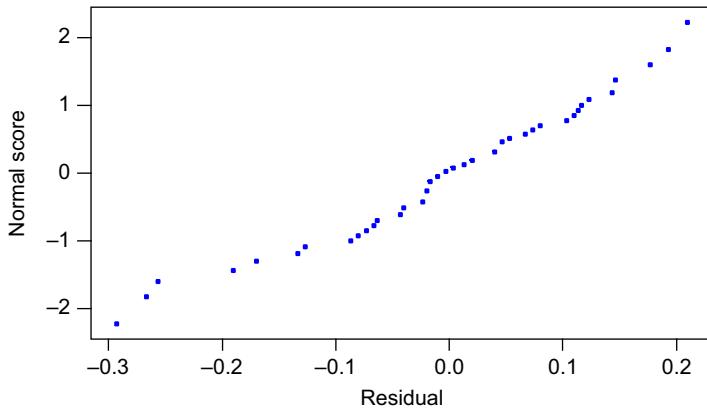
#### 7.4.3 Objective 2: To identify the factors which affect variability in the free height of leaf springs

In order to determine which of the factors or interaction effects have a significant influence on the variability, it was decided to construct a Pareto plot of effects (Fig. 7.8). Due to insufficient degrees of freedom for the error term, it was decided to pool the effects with low magnitude.

The Pareto plot has indicated that main effect A and interaction effect CE appear to have a significant impact on variability at 10% significance level. The interaction plot (Fig. 7.9) implies that there is a strong interaction between the factors C (transfer time) and E (quench oil temperature). It can be observed from the plot that variability in the free height of leaf springs is minimum when both C and E are kept at low levels. Moreover, it can be seen that variability is high when E is kept at low



**Figure 7.6** Pareto plot of effects for the leaf spring experiment.

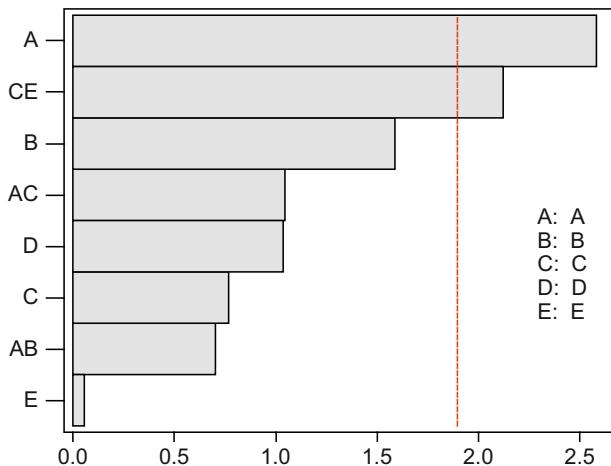


**Figure 7.7** NPP of residuals for the leaf spring example.

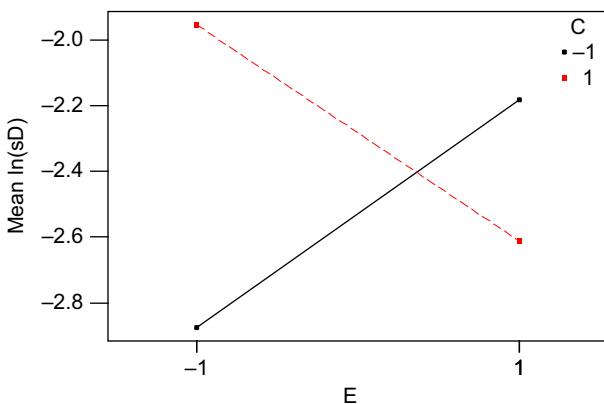
level and C at high level. As main effect C is confounded with a third-order interaction, it is fair to conclude that it is the interaction CE which causes variability in the free height of leaf springs.

#### 7.4.4 How do we select the optimal factor settings to minimise variability in free height?

For any process optimisation problems, it is important to determine the optimal factor settings which meet the experimental objectives. Here we need to determine the best factor settings which yield minimum variability in the free height of leaf



**Figure 7.8** Pareto plot of effects which influence variability.



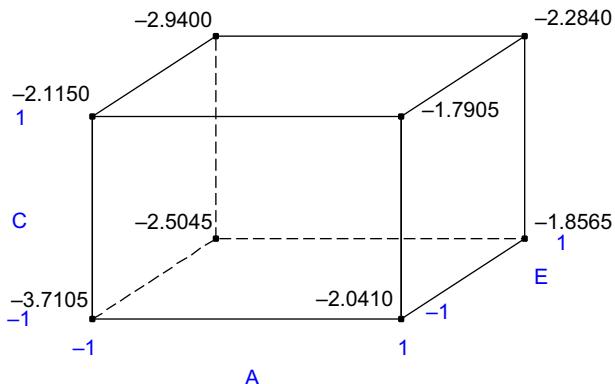
**Figure 7.9** Interaction plot between quench oil temperature and transfer time.

springs. A cube plot was constructed with factors A, C and E (Fig. 7.10). The cube plot clearly shows that minimum variability is obtained when all the factors are kept at low levels. It can be concluded that the optimal settings for minimising variability are as follows (Fig. 7.11):

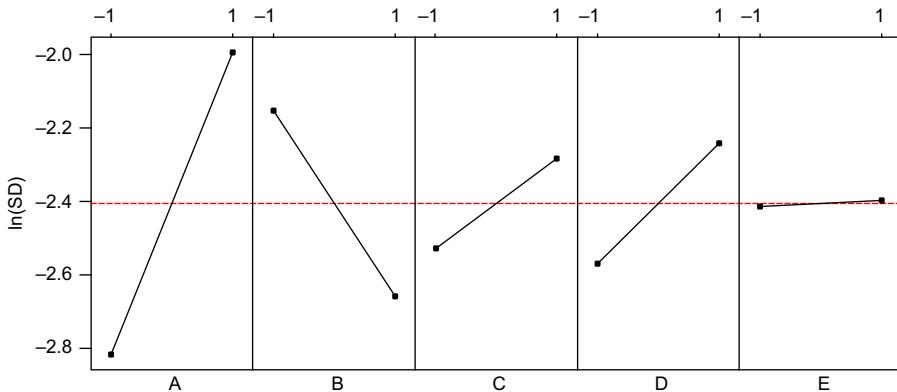
Factor A – Low level (-1), Factor B – High level (1), Factor C – Low level (-1), Factor D – Low level (-1), Factor E – Low level (-1)

#### 7.4.5 Another example of a $2^{(5-1)}$ factorial design

The next example is about the investigation of the effect of five factors on the process yield of an IC manufacturing process (for more information on the case study,



**Figure 7.10** Cube plot of effects.



**Figure 7.11** Main effects plot for  $\ln(\text{SD})$ .

the readers may refer to Montgomery, D.C., *Design and Analysis of Experiments*, 5th Edition, John Wiley and Sons, 2001). As it was too expensive to run an FFE, the engineers decided to run a half-fractional factorial design. Each factor was studied at 2-levels. The trial conditions were not replicated as the engineers were keen to increase the yield of the process only in the initial phase of this experimentation. Table 7.11 shows the experimental layout and the recorded yield values. The five factors used for the experiment were A = aperture setting, B = exposure time, C = develop time, D = mask dimension and E = etch time. This is a  $2^{(5-1)}$  fractional factorial design with design generator E = ABCD. In other words, the design resolution of the experiment is V. This implies that main effects are confounded with a fourth-order or four-factor interaction or that two-factor interactions are confounded with three-factor interactions.

**Table 7.11** Experimental layout with yield values for the IC manufacturing process.

Run order	A	B (min)	C (s)	D	E (min)	Yield (%)
1	Small	20	30	Small	15.5	8
2	Large	20	30	Small	14.5	9
3	Small	40	30	Small	14.5	34
4	Large	40	30	Small	15.5	52
5	Small	20	45	Small	14.5	16
6	Large	20	45	Small	15.5	22
7	Small	40	45	Small	15.5	45
8	Large	40	45	Small	14.5	60
9	Small	20	30	Large	14.5	6
10	Large	20	30	Large	15.5	10
11	Small	40	30	Large	15.5	30
12	Large	40	30	Large	14.5	50
13	Small	20	45	Large	15.5	15
14	Large	20	45	Large	14.5	21
15	Small	40	45	Large	14.5	44
16	Large	40	45	Large	15.5	63

The defining relation is given by  $I = ABCDE$ . The aliasing or confounding structure is shown below.

$$A = BCDE, B = ACDE, C = ABDE, D = ABCE, E = ABCD$$

Also,

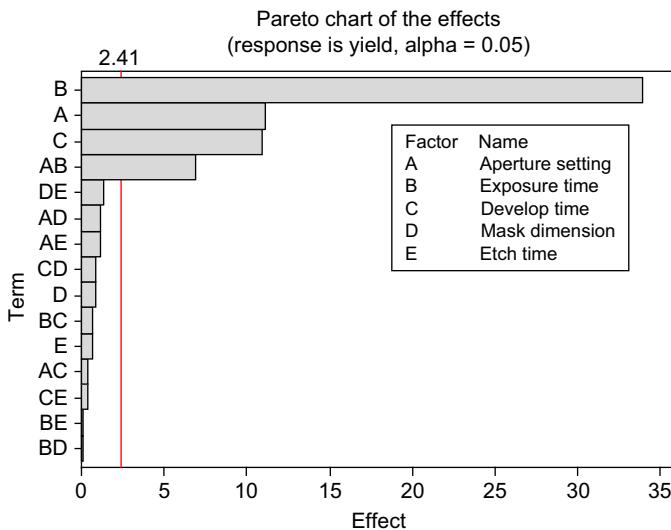
$$AB = CDE, AC = BDE, AD = BCE, AE = BCD$$

$$BC = ADE, BD = ACE, BE = ACD$$

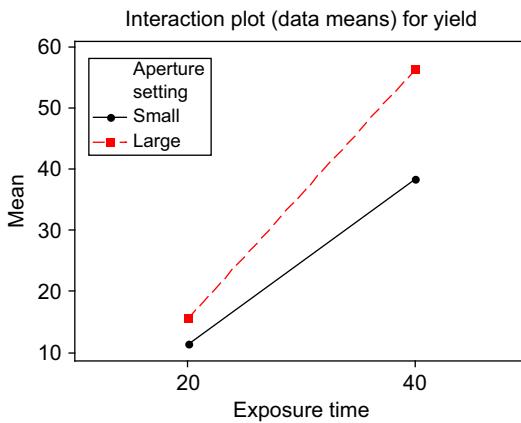
$$CD = ABE, CE = ABD \text{ and, } DE = ABC$$

The objective of the experiment was to determine which factors influence the yield (%) and which settings would provide us with the highest yield. In order to determine the most significant effects (main or interaction effects), it was decided to use a Pareto plot (Fig. 7.12). Fig. 7.12 reveals that main effects B = exposure time, A = aperture setting and C = develop time appeared to be statistically significant at 5% significance level. Moreover, it was found that there is a strong interaction between aperture setting and exposure time. Fig. 7.13 shows that the effect of exposure time at different levels of aperture setting is not the same. In addition, the interaction graph clearly indicates that yield is maximum when exposure time is kept at a high level (40 min) and aperture setting was also kept at a high level (high).

It was quite interesting to observe that factor D (mask dimension) and factor E (etch time) had no effect on yield. The levels of these factors can be set at their



**Figure 7.12** Pareto plot of effects for the yield from IC manufacturing process.



**Figure 7.13** Interaction plot between aperture setting and exposure time.

most economical levels. In order to improve the yield, the high-level setting of factors A, B and C should be applied.

#### 7.4.6 Example of a $2^{(7-4)}$ factorial design

In this example, we look at a case study from Box et al. (1978, p. 424). In a new chemical plant, the filtration step takes nearly twice as long as it did at the older plant, resulting in serious process delays. A brainstorming session produces seven

**Table 7.12** List of factors and their respective levels used for the experiment.

Factors	Labels	Low-level setting	High-level setting
Water supply	A	Town	Well
Raw material	B	On site	Other
Temperature	C	Low	High
Recycle	D	Yes	No
Caustic soda	E	Fast	Slow
Filter cloth	F	New	Old
Holdup time	G	Low	High

factors thought to affect filtration time. [Table 7.12](#) presents the list of factors and their respective levels which are thought to influence filtration time.

The confounding structure or aliasing pattern for the experiment is as follows. We have not taken third-order and higher-order interactions into account here as they are usually negligible compared to the main and second-order interaction effects ([Bisgaard, 1988](#)).

$$A = BD + CE + FG; B = AD + CF + EG$$

$$C = AE + BF + DG; D = AB + CG + EF$$

$$E = AC + BG + DF; F = AG + BC + DE$$

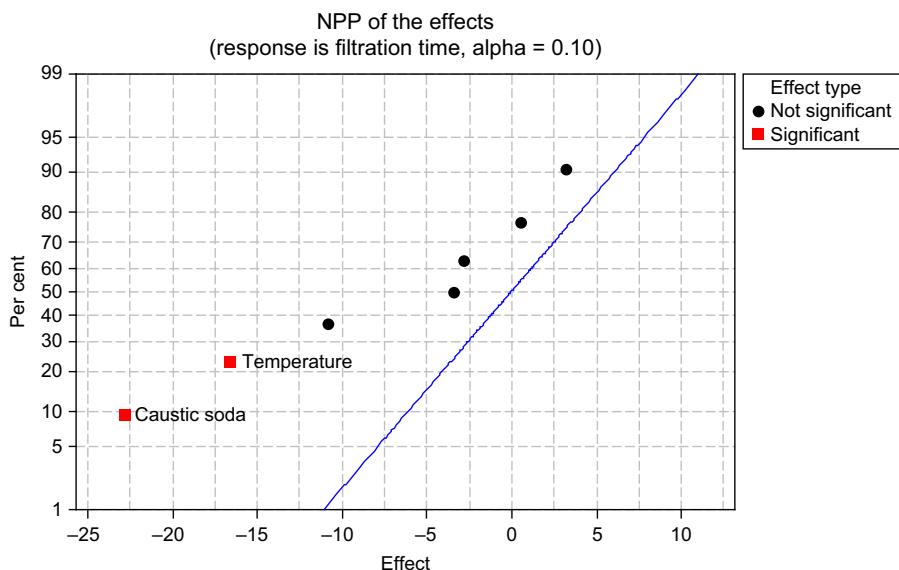
$$G = AF + BE + CD$$

Each factor was studied at 2-levels. Due to time and cost constraints, it was decided to perform a  $2^{(7-4)}$  factorial design which is 1/16th fractional of a full factorial design. This clearly implies that we are studying 7 factors in 8 trials instead of 128 trials. [Table 7.13](#) presents the experimental layout for the experiment.

[Fig. 7.14](#) shows a normal plot of all main effects ([Daniel, 1976](#)) which indicated that factors E and C appeared to have a significant effect on filtration time. However, factor E is confounded with two-order or second-order interactions such as AC, BG and DF. Similarly, factor C is confounded with AE, BF and DG. In such circumstances, we need to perform a fold-over design to separate out the main effects from interaction effects; this way we would know if it is the main effects or the interaction effects which influence the filtration time. The results of the fold-over design are given in [Table 7.14](#). By using a fold-over design, we can de-alias the main effects. After the fold-over design was created and executed based on [Table 7.14](#), the main effects were no longer confounded with second-order or two-factor interactions. However, two-factor interactions were still confounded with each other. Further analysis has showed that two effects appeared to be significant: the main effect due to factor E and the two-factor interaction AE. It was quite interesting to observe that temperature (factor C) was not a significant factor after all. One of the key findings of the experiment was that temperature had no significant effect on filtration time.

**Table 7.13** Experimental layout for the filtration time experiment.

Trial no.	A	B	C	D	E	F	G	Filtration time
1	Town	On site	Low	No	Slow	Old	Low	68.4
2	Well	On site	Low	Yes	Fast	Old	High	77.7
3	Town	Other	Low	Yes	Slow	New	High	66.4
4	Well	Other	Low	No	Fast	New	Low	81.0
5	Town	On site	High	No	Fast	New	High	78.6
6	Well	On site	High	Yes	Slow	New	Low	41.2
7	Town	Other	High	Yes	Fast	Old	Low	68.7
8	Well	Other	High	No	Slow	Old	High	38.7

**Figure 7.14** NPP of effects.

#### 7.4.7 Another example of a $2^{(7-4)}$ factorial design

The determination of the moulding condition in an injection moulding process is very complicated. Typical injection moulding machines have many adjustable parameters

**Table 7.14** Results of fold-over design.

Trial no.	A	B	C	D	E	F	G	Filtration time
1	Well	Other	High	Yes	Fast	New	High	66.7
2	Town	Other	High	No	Slow	New	Low	65.0
3	Well	On site	High	No	Fast	Old	Low	86.4
4	Town	On site	High	Yes	Slow	Old	High	61.9
5	Well	Other	Low	Yes	Slow	Old	Low	47.8
6	Town	Other	Low	No	Fast	Old	High	59.0
7	Well	On site	Low	No	Slow	New	High	42.6
8	Town	On site	Low	Yes	Fast	New	Low	67.6

which could potentially influence the quality of finished plastic parts. Quality can be determined in terms of dimensional conformity, appearance of the finished product or even mechanical characteristics. The traditional approach to determine the best moulding condition has been through trial and error which is time consuming and not cost effective. One of the most efficient methods of process optimisation and systematic investigation of the process is through the utilisation of DOE. The plastic part for this example is the closure for infusion bottles. For more information about the case study, please refer to Azeredo et al. (2003), Improve moulded part quality, *Quality Progress*, July, pp. 72–76. The closure is moulded in high-density polyethylene and has complex geometry plus many functional properties. For this experiment, the mould engineers were interested to understand the influence of moulding process parameters on the force needed to open the closure. Extremely high forces make it difficult to open the closure and low forces can result in damage during shipping or handling.

A brainstorming session was conducted to list the potential process parameters which could influence the force needed to open the closure. The team had to study the impact of seven process parameters at 2-levels and a  $2^{(7-4)}$  factorial design was selected in order to minimise the cost and time factors. Each trial condition was replicated three times to understand the variation within the experimental runs and between the experimental trials. The engineering team used a tensile device to measure the force needed to open the closure. [Table 7.15](#) presents the list of process parameters and their respective levels used for the experiment. [Table 7.16](#) presents the experimental layout with uncoded process parameters along with the response values.

[Fig. 7.15](#) shows a Pareto plot of the effects. It is clear from the plot that process parameters A (injection speed), B (mould temperature), C (melt temperature), G (ejection speed) and F (cooling time) appeared to be statistically significant at 5% significance level. Holding pressure and holding time had no impact on the force needed to open the closure.

**Table 7.15** List of process parameters and their levels used for the experiment.

Process parameters	Labels	Low level	High level
Injection speed (percentage setting)	A	40	75
Mould temperature (Celsius)	B	25	45
Melt temperature (Celsius)	C	205	235
Holding pressure (bar)	D	25	45
Holding time	E	2	3
Cooling time	F	10	25
Ejection speed (percentage setting)	G	5	25

## Exercises

1. A  $2^{(7-4)}$  fractional factorial design was conducted on a chemical process to evaluate the effect of seven process variables which might influence the yield (%) of the process. The list of variables and their levels used for the experiment are shown below.

Variable	Low level	High level
Temperature (A)	150	200
Pressure (B)	Low	High
Concentration of chemical A (C)	3%	5%
Concentration of chemical B (D)	2%	8%
Type of catalyst (E)	A	B
Reaction time (F)	Low	High
Flow rate (G)	Low	High

*Source:* Data from, DeVor et al., 1992. Statistical Quality Design and Control. Macmillan Publishing Company, New York.

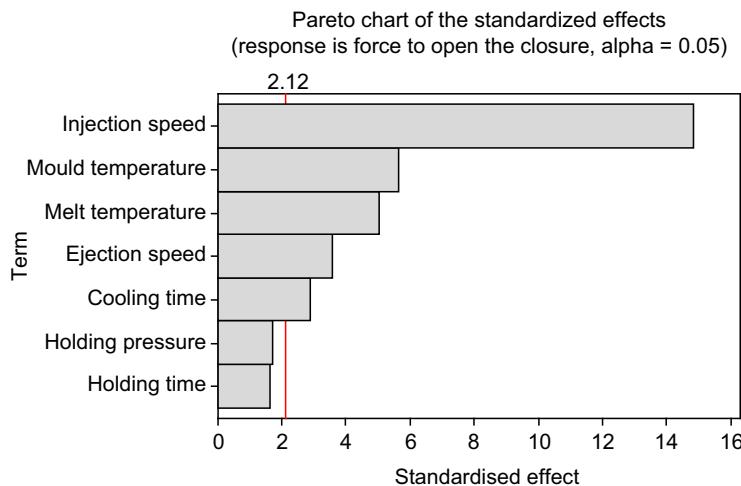
The results of the experiment are shown below. The response for the experiment is per cent yield. Note that the tests are displayed in the order in which they were carried out.

Run	A	B	C	D	E	F	G	Yield (%)
1	-1	1	1	-1	-1	1	-1	66.1
2	-1	1	-1	1	-1	-1	1	59.6
3	1	-1	1	1	-1	-1	-1	62.3
4	1	1	-1	-1	1	-1	-1	67.1
5	-1	-1	1	-1	1	-1	1	21.1
6	1	1	1	1	1	1	1	57.8
7	-1	-1	-1	1	1	1	-1	59.7
8	1	-1	-1	-1	-1	1	1	22.5

**Table 7.16** Results of the injection moulding experiment.

Run	A	B	C	D	E	F	G	Y1	Y2	Y3
1	40	25	205	45	3	25	5	41.04	44.02	41.89
2	75	25	205	25	2	25	25	68.59	70.89	71.53
3	40	45	205	25	3	10	25	44.12	46.46	32.33
4	75	45	205	45	2	10	5	63.02	64.12	62.67
5	40	25	235	45	2	10	25	65.51	62.48	59.05
6	75	25	235	25	3	10	5	71.62	78.44	73.96
7	40	45	235	25	2	25	5	42.77	41.55	39.49
8	75	45	235	45	3	25	25	64.33	73.43	70.95

Y1, Y2 and Y3 = force needed to open the closure.

**Figure 7.15** Pareto plot of effects for the injection moulding experiment.

- What are the generators and defining relation for this experiment?
- Illustrate the complete confounding structure for the design, assuming third-order and higher-order interactions are negligible.
- Which factor or interaction effects appear to have a significant impact on percentage yield?
- Construct a Pareto plot of effects and determine the optimal settings of the variables which give maximum yield.
- How do you validate the assumption of normality?
- An experimenter decided to study the effect of four process parameters for an injection moulding process. The experimenter was interested in both main and two-factor interactions. The response of interest was the width of the injected part (accuracy is up to four decimal places), which is critical to customers. The results of the experiment are given in the following table. The experiment was repeated twice to create sufficient degrees of

freedom for the error term. The four process variables are D = mould temperature, A = injection speed, E = hold pressure and B = cooling time.

Trial no.	D	A	E	B = DAE	Width	
1	-1	-1	-1	-1	9.3415	9.3416
2	-1	-1	1	1	9.3691	9.3692
3	-1	1	-1	-1	9.3467	9.3466
4	-1	1	1	-1	9.3680	9.3681
5	1	-1	-1	1	9.3679	9.3680
6	1	-1	1	-1	9.3493	9.3494
7	1	1	-1	1	9.3668	9.3669
8	1	1	1	1	9.3544	9.3545

Source: Data from, Schmidt, S.R., Launsby, R.G., 1992. Understanding Industrial Designed Experiments. Air Academy Press, Colorado Springs, CO.

- a. What is the resolution of this design?
- b. Display the complete confounding structure.
- c. Which effects appear to have a significant effect on the width?
- d. What are the best settings of the parameters to achieve a target width of 9.380?
- 3. An experimenter is interested in studying the effect of five welding process parameters. The results of the experiment are illustrated below. The response of interest to the experimenter is heat input (measured in watts) for welding. The welding parameters considered for the experiment are A = open-circuit voltage, B = slope, C = electrode melt-off rate, D = electrode diameter and E = electrode extension. The design matrix of the experiment with response is given in the following table.

Trial no.	A	B	C	D	E	Heat input (W)
1 (12)	-1	-1	-1	-1	1	3318
2 (1)	1	-1	-1	-1	-1	4141
3 (2)	-1	1	-1	-1	-1	3790
4 (6)	1	1	-1	-1	1	4061
5 (15)	-1	-1	1	-1	-1	3431
6 (8)	1	-1	1	-1	1	3425
7 (7)	-1	1	1	-1	1	3507
8 (4)	1	1	1	-1	-1	3765
9 (11)	-1	-1	-1	1	-1	2580
10 (14)	1	-1	-1	1	1	2450
11 (3)	-1	1	-1	1	1	2319
12 (16)	1	1	-1	1	-1	3067
13 (13)	-1	-1	1	1	1	1925
14 (10)	1	-1	1	1	-1	2466
15 (5)	-1	1	1	1	-1	2485
16 (9)	1	1	1	1	1	2450

Note: ( ) implies the order in which the experimental trials were carried out.

Source: Data from, Stegner, D.A.J., et al., 1967. Prediction of heat input for welding. Welding J. Res. (Suppl. 1).

- a. What is the defining relation of this design?
  - b. Display the complete confounding structure and determine the design resolution.
  - c. Which effects appear to have a significant effect on heat input?
  - d. Construct an NPP of residuals for validating normality assumptions.
4. As a reliability engineer, you have been asked to weed out infancy failures in component-populated printed circuit boards. The four factors of interest are as follows:

Label	Process variable	Low level	High level
A	Stress temperature	80°C	125°C
B	Thermo cycle rate	5°C/min	20°C/min
C	Humidity	15%	95%
D	g level for a 10 min sinusoid random variation	3	6

The response is the number of electrical defects per board, each of which contains 1000 bonds. Given the following design matrix and response data, determine the optimal screening method. The more failures found, the better.

Trial	A	B	AB	C	AC	BC	D	Response		
Y1	Y2	Y3								
1	-1	-1	1	-1	1	1	-1	9	17	12
2	-1	-1	1	1	-1	-1	1	21	37	42
3	-1	1	-1	-1	1	-1	1	29	35	48
4	-1	1	-1	1	-1	1	-1	17	10	15
5	1	-1	-1	-1	-1	1	1	32	41	33
6	1	-1	-1	1	1	-1	-1	21	17	19
7	1	1	1	-1	-1	-1	-1	12	14	18
8	1	1	1	1	1	1	1	33	27	47

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## Further reading

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# Some useful and practical tips for making your industrial experiments successful

8

## 8.1 Introduction

Experimental Design (ED), or DOE, is a powerful approach to achieve increased understanding of your process, leading to significant improvements in product quality, decreased manufacturing costs and potentially thousands of dollars of savings for organisations. So why don't more manufacturers use ED? Why do some manufacturing companies try ED, and then abandon it, saying 'It won't work for us'? Inadequate training, demanding production schedules or time pressures, cost and resources required for the execution of an experiment or a series of experiments are often cited as the principal reasons. Moreover, fear of statistics is widespread, even among many educated scientists and managers in organisations. This chapter provides some useful and practical tips for industrial engineers and managers with limited knowledge of ED or DOE for making industrial experiments successful in their own organisations. The purpose of this chapter is to stimulate the engineering community to start applying ED for tackling quality control problems in key processes they deal with everyday.

Industrial experiments are fundamental to and crucial for increasing the understanding of a process and of product behaviour. The success of any industrial experiment depends on a number of key factors such as statistical skills, engineering skills, planning skills, communication skills, teamwork skills and so on. Many scientists and engineers perform industrial experiments based on full and fractional factorial designs (Montgomery, 1991) or Orthogonal Array (OA) designs (Taguchi, 1986) for improving product quality and process efficiency. In other words, engineers and managers of today's modern industrial world have placed an increased emphasis on achieving breakthrough improvements in product and process quality using DOE/ED. DOE/ED is essentially a strategy of industrial experimentation whereby one may vary a number of factors in a process/system simultaneously to study their effect on the process/system output (Antony, 1996). DOE/ED is a direct replacement of traditional One-Factor-At-A-Time (OFAT) or the 'Hit or Miss' approach to experimentation (Antony, 1998). It is important to note that these tips were developed strictly on the basis of author's experience and expertise in the field of study and also by reviewing many industrial case studies and literature in the subject matter.

### 8.1.1 Get a clear understanding of the problem

One of the key reasons for an industrial experiment to be unsuccessful is due to lack of understanding of the problem itself. The nature of the experiment to be

conducted is heavily dependent on the nature of the problem and the objective of the experiment. Therefore, it is absolutely essential to have a clear definition of both before one embarks on to any kind of experimentation. A well-defined objective leads the experimenter to the correct choice of ED. If you incorrectly state the objective(s) of an experiment, you may have to face the consequences – trying to study too many or too few factors for the experiment, not measuring the right quality characteristics or responses, or arriving at conclusions which are already known to the team conducting the experiment. In other words, unclear objectives can lead to lost time and money, as well as lack of appreciation and feelings of frustration for all involved in the study ([Antony, 1997](#)). Industrial experiments are generally a team effort; a typical team includes people from design and from the quality and production department as well as an operator. It is quite important that everyone on the team have a clear understanding of the objective of the experiment and also of their role in experimentation. If there is more than one objective, it is then important to assign a relative weight to the objectives and establish ways in which each will be evaluated.

### ***8.1.2 Project selection***

Selection of the right project will either assure you of success or guarantee an opportunity to try it again a second time. Many companies are continuously engaged in a number of ED projects and it is important to identify the projects that can return the most savings. In situations where you have a number of experiments to be performed for a variety of problems, it is worthwhile to keep the following factors in mind.

#### ***8.1.2.1 Management involvement and commitment***

Management must be involved in the project right from the beginning. You need their support and commitment when you need to take actions to improve a process or system. There is no point in pursuing a DOE/ED project if you do not have 100% backup from senior management team. Moreover, the purpose of the DOE/ED project must be clearly communicated to the senior management team and expectations regarding their involvement and commitment should be explicitly stated up front ([Anderson and Kraber, 1999](#)).

#### ***8.1.2.2 Return on investment***

Experimentation in general is not a priority for many senior managers in organisations. In fact, it is not an easy task for engineers to suggest DOE/ED to senior management as the solution to a particular problem. When you have a number of experiments to be carried out, consider the return on investment. Savings from reduced warranty costs, reduced customer complaints and increased customer satisfaction may produce a higher return in the long term. It is strongly advisable to present successful case studies of DOE from other businesses similar to yours.

### **8.1.2.3 Project scope**

If the system or process you deal with for experimentation purposes is too intricate in nature, it is best to break it down into sub-systems or sub-processes. For example, in the case of automobiles, rather than optimising the entire vehicle, it is better to start optimising the braking or suspension system. If it is feasible and practical, you may break the braking system into many sub-systems and seek to optimise the surface finish of the rotor disk. Moreover, it is quite important to understand the boundaries of the project before it turns into a ‘boiling-the-ocean’ project.

### **8.1.2.4 Time required to complete the project**

An unfinished experiment is a waste of time and resources, and this can be quite detrimental to all future initiatives. Therefore, it is important to start off with projects that bring quick wins to the organisation in a short time. This helps to boost the morale of the team and helps them to become more confident in undertaking more and more projects across the organisation.

### **8.1.2.5 Value to your organisation**

You should select a project that adds long-term value to the future of your organisation. Carry out DOE/ED projects (in the form of experiments) to achieve greater product performance that your customers may not be asking for now but may ask for soon. It is also highly desirable to select a project that is aligned with the strategic objectives of the business; this gives you a competitive advantage. For instance, select DOE/ED projects so that products can be introduced to market faster than those of your competitors. Understanding what makes the customer tick, anticipating his needs and behaviours and then optimising products and service levels to meet all of these is the way ahead in business.

## **8.1.3 Conduct exhaustive and detailed brainstorming sessions**

Many DOE/ED training courses and textbooks spend as much as 70%–80% of their time in the analysis of experimental data gathered by the experimenter (i.e. statistical skills). The successful application of DOE/ED in today’s industrial environment requires a mixture of statistical, planning, engineering, communication and teamwork skills. Brainstorming must be treated as an integral part of the planning and design of effective experiments ([Bhote, 1988](#)). There is no standard procedure on how to perform a typical brainstorming session that is applicable to all industrial situations. The nature and content of each brainstorming session will rely heavily on the nature of the problem under investigation. In the context of DOE/ED, brainstorming is performed with the following purposes and questions in mind:

- Identification of the factors, the number of levels and other relevant information about the experiment.
- Development of team spirit and positive attitude in order to assure greater participation of the team members.

- How well does the experiment simulate the customers or users conditions?
- Who will do what and how? For example, who will be responsible for data analysis?
- How quickly does the experimenter need to provide the results to the management?
- Is experimentation the only way to tackle the problem at hand?

### **8.1.4 Teamwork and selection of a team for experimentation**

For ED projects, it is good practice to have a project owner who is responsible for team formation. In selecting team members, the following criteria may be considered:

- *Project beneficiaries* – These are people who must accept your recommendation for improvement further to key findings from the experiment. They may not be directly involved in the project, but it is important to bring them in the loop somehow.
- *Parts/materials supplier* – If the parts/materials supplier is a factor in the experiment, it is best to consult with them and include them on the experimentation team.
- *Direct involvement* – When planning and conducting an experiment, it is important to include people who can provide input into the identification of factors for the experiment. For a typical industrial designed experiment, personnel involved in design, validation, quality and production, as well as operators, are likely candidates ([Anderson, 2000](#)).

### **8.1.5 Select the continuous measurable quality characteristics or responses for the experiment**

A quality characteristic or response is the performance characteristic of a product that is most critical to customers and often reflects the product quality. Selecting the right quality characteristic (or response) is critical to the success of any industrial designed experiment ([Antony, 1998](#)). Many DOE programs fail because their responses cannot be measured quantitatively. A classic example can be found with the traditional approach to evaluating quality, where an inspector uses a subjective judgement based on his experience to determine whether a product or unit passes or fails the test. Pass/fail data can be used in DOE, but it is very crude and inefficient. For example, if your process typically produces a 0.5% defect rate, you would expect to find 5 out of 1000 parts defective. If you perform a 16-trial experiment, you would then require a minimum of 16,000 parts ( $16 \times 1000$ ). This poses the question, ‘*Can we afford the cost associated with the parts?*’

The following guidelines may be useful to engineers in selecting the quality characteristics or responses for industrial experiments:

- Use quality characteristics (or responses) that can be measured accurately and with stability.
- Use quality characteristics that can be measured quantitatively.
- Use quality characteristics which are directly related to the energy transfer associated with the fundamental mechanism of the product or the process.
- Use quality characteristics which are complete, i.e. they should cover the input–output relationship for the product or the process.
- For complex systems or processes, select quality characteristics at the sub-system level and perform experiments at this level before trying to optimise the overall system.

Consider a coating process which results in various problems such as poor appearance, low yield, orange peel and voids. Too often, experimenters measure these characteristics as data and try to optimise the response. This is not sound engineering, because these are the symptoms of poor function. It is not the function of the coating process to produce an orange peel. Problems such as orange peel are due to excessive variability of the coating process caused by noise factors such as variability in viscosity, ambient temperature, etc. We should measure data that relate to the function itself, not the symptom of variability. One fairly good characteristic to measure for the coating process is the coating thickness. The aim of the coating process is to form the coating layer; effects such as orange peel result from excessive variability of coating thickness from its target. A sound engineering approach is to measure the coating thickness and determine the best settings of the coating process that will minimise the coating thickness variability around its target value. [Table 8.1](#) provides a framework covering a variety of manufacturing process problems and the suitable response of interest to experimenters for each associated process.

In essence, the selection of attribute quality characteristics (e.g. good/bad, defective/non-defective, etc.) for industrial experiments is not a good practice. This does not mean that experimenters should measure only continuous measurable quality characteristics. The author nevertheless recommends choosing continuous characteristics over attributes. One of the limitations with the attribute characteristic is its poor additivity. It means that many main effects will be confounded with two-factor interactions or that two-factor interactions will be confounded with other two-factor interactions. Attribute characteristics also require a large number of samples and therefore experiments involving such characteristics are costly and time consuming.

**Table 8.1** Examples of quality characteristics for various manufacturing processes.

Type of process	Objective of the experiment	Appropriate response
Extrusion	To reduce the post extrusion shrinkage of a speedometer cable casing	Shrinkage
Coil spring manufacturing	To reduce variability in the tension of coil springs	Spring tension
TV picture tube manufacturing	To reduce performance variation of TV electron guns	Cut-off voltage
Surface mounting	To improve field reliability	Shear strength
Gold plating	To reduce variation in gold plating thickness	Plating thickness
Die-casting process	To increase the hardness of a die-cast engine component	Rockwell hardness
MIG welding	To reduce the high scrap rate due to poor welded joints	Weld strength
Wire bonding	To reduce the defect rate from broken wires	Wire pull strength

### **8.1.6 Choice of an appropriate ED**

The choice of ED is very important for the success of any industrial experiment as it depends on various factors which include the nature of the problem at hand, the number of factors to be studied, resources available for the experiment, time needed to complete the experiment and the resolution of the design. We can use either Classical ED (full and fractional factorial designs), advocated by Sir Ronald Fisher, or OA designs, recommended by Dr Taguchi ([Antony, 1999](#)). In Classical ED, the focus is on the study of product and process behaviour, followed by the development of a mathematical model which explicitly illustrates the relationship between a dependent variable and a set of independent variables. Experiments based on OA designs, promoted by Taguchi, are focused on product and process robustness. Here robustness refers to reducing the process/product performance to noise sensitivity. Taguchi recommends the use of the SNR to estimate the performance sensitivity of a product to noise. The choice of any of these designs will be dependent upon the following factors:

- degree of optimisation required for the chosen quality characteristic
- number of factors and interactions (if any) to be studied
- complexity of using each design
- statistical validity and effectiveness of each design
- degree of product/process functional performance robustness to be attained from the experiment
- ease of understanding and implementation
- nature of the problem (or objective of the experiment)
- cost and time constraints.

The interesting thing is that many companies the author has visited rely on just one approach of DOE. So whenever the author approaches the Engineering Director, Operations Director or Manufacturing Director in local companies, the author often gets the response, ‘Our employees have been trained on Taguchi or Classical DOE.’ As mentioned above, you cannot use the same approach for all problems in the business. The solution to a problem depends upon the nature of the problem. For instance, if a company wants to achieve robust performance due to inconsistency issues from the presence of noise factors in the process, it is best to look into an RPD, as expounded by Dr Taguchi. On the other hand, if your objective is to predict performance based on a regression model with quadratic effects (non-linear effects), it is probably best to look into Classical DOE followed by the use of Response Surface Methodology (RSM) ([Box et al., 1978](#)).

### **8.1.7 Iterative experimentation**

Experiments should be conducted in an iterative manner so that information gained from one experiment can be applied to the next. It is best to run a number of smaller and sequential experiments rather than running a large experiment with several factors and using up the majority of resources assigned to the experimentation process. If none of the factors or process variables is significant, the experiment would then be a waste of time and money. The first step in any experimentation process is

to ‘separate out the vital few from the trivial many’. Screening experiments are generally performed to reduce the number of factors or key process variables to a manageable number in a limited number of experimental trials (Hansen, 1996).

It is advisable not to invest more than 25% of the experimental budget in the first phase of any experimentation, such as screening (Montgomery, 1991). Once the key factors have been identified, the interactions among them can be studied using full or fractional factorial experiments. Once you identify the key variables and interactions for a process, you may then want to perform an RSM, which allows you to model the process behaviour over its entire operating region. Using RSM, one may be able to develop a second-order mathematical model that depicts the relationship between the key process variables and the process response. This model can then be used to predict the values of the responses at different variable settings.

### ***8.1.8 Randomise the experimental trial order***

In the context of ED, randomisation is a process of performing experimental trials in a random order in which they are logically listed. This is a very important concept in any ED because an experimenter cannot always be certain that all important factors affecting a response have been included and considered in the experiment. The purpose of randomisation is to reduce the systematic bias that is induced into the experiment (Kraber, 1998). The bias may be due to the effect of uncontrolled factors or noise, such as machine ageing, changes in raw material, tool wear, change of relative humidity, power surges, change of ambient temperature and so on. These changes, which often are time related, can significantly influence the response. For example, assume that an experiment is performed so that all the low levels of factor A are run first, followed by the high levels of factor A. During the course of the experiment, the humidity in the workplace changes by 50%, creating a significant effect on the response. The analysis may reveal that factor A is statistically significant. In reality factor A is not significant; it is the change in humidity level that caused the factor effect to be significant. Randomisation would have prevented this confusion.

Whilst conducting an experiment, do not underestimate the background noise inherent in the experiment. Characterisation of the noise variables allows an engineer to understand their effect and minimise their influence on the process performance. A factor may turn out to be significant due to the influence of the lurking variables (or noise variables), which often are uncontrollable. Randomisation will minimise the effect of a factor which has been confounded with the effect of noise. The author therefore recommends that the experimenters randomise (if possible) the trials.

### ***8.1.9 Replicate to dampen the effect of noise or uncontrolled variation***

Replication improves the chance of detecting a statistically significant effect (i.e. signal) in the midst of natural process variation. In some processes, the amount of

natural process variation is very large. This can mitigate your chances of detecting a significant factor or interaction effect. One of the common queries before conducting experiments in organisations is ‘How many experimental runs are required to identify significant effect(s), given the current process variation?’ SNRs help to determine the minimum number of experimental runs needed to achieve a given power for your ED ([Taguchi and Yokoyama, 1993](#)). The signal is the change in response that you want to detect. You need to determine the smallest change you want to detect. Once the signal is detected, you may then estimate the noise. Here noise is the random variation that occurs in the response during standard operating conditions. The noise (i.e. measure of variation) can be estimated from either control charts (using the equation  $\sigma = d_2/R$ ) or the Analysis of Variance (ANOVA) table from a designed experiment (refer to the value of Root Mean Square Error (RMSE)).

The number of replications is a direct function of the size of the experiment. [Table 8.1](#) provides some guidance on to determine how many experimental runs are required to be conducted for the desired detectable signal. If you cannot afford to perform the necessary runs, then you must find some way to minimise the noise or random variation. The number of runs is given by the following formula:

$$N = \frac{(4r)^2}{(\Delta/\sigma)^2} \quad (8.1)$$

where  $N$  = total number of experiments,  $r$  is the number of levels of the factors,  $\Delta$  is the size of the effect to detect and  $\sigma$  is the noise level. The derivation of the above equation is based on providing approximately a 90% confidence of finding an active effect of size  $\Delta$ . For example, for an injection moulding process, the management would like to reduce the shrinkage by 0.85% (i.e.  $\Delta = 0.85$ ). The SD of the process is known to be about 0.60% (i.e.  $\sigma = 0.60$ ). Assume that each factor is studied at 2-levels. The total number of experiments in this case can be computed (using [Eq. \(8.1\)](#)) as 32.

Consider another example where the objective of the experiment is to improve the yield of a chemical process by 1%. The SD of the process is estimated to be 0.5%. The minimum number of experiments to detect an effect of 1% is 16 ([Table 8.2](#)).

Many process engineers engaged in industrial experiments are not sure of the difference between repetition and replication. Replication is a process of running

**Table 8.2** Number of experiments as a function of SNR.

SNR ( $\Delta/\sigma$ )	Minimum number of experiments
1.0	64
1.4	32
2.0	16
2.8	8

the experimental trials in a random fashion. In contrast, repetition is a process of running the experimental trials under the same set-up of machine parameters ([Versepuit, 1998](#)). In other words, the variation due to machine set-up cannot be captured using repetition. Replication requires resetting of each trial condition and therefore the cost of the experiment and also the time taken to complete the experiment may be increased to some extent. Replication increases the precision of an experiment by reducing the SDs used to estimate factor effects. Increasing the number of replicates will decrease the error variance or mean square due to error ([Schmidt and Launsby, 1992](#)). Replication will yield better results in the long run. Therefore, it is always best to remember the following maxim: ‘Do it right the first time or you’ll just have to do it later!’

### **8.1.10 Improve the efficiency of experimentation using a blocking strategy**

Blocking can be used to minimise the chances of experimental results being influenced by variations from shift to shift, day to day or machine to machine. By dividing your experimental runs into homogeneous blocks and then arithmetically removing the difference, you increase the sensitivity of your experiment. Do not block on anything that you want to study. For example, if you want to measure the difference in the quality of materials provided by three suppliers, then you have to include ‘supplier’ as a factor in your experiment. When blocking occurs, one or more of the interactions is likely to be confounded with the block effects; however, a good choice of blocking should ensure that it is a higher-order interaction (one that would be challenging to interpret or is not be expected to be important) that is confounded.

The blocks can be batches of different shifts, different machines, raw materials and so on. Shainin’s Multi-variate charts can be a useful tool for identifying those variables that cause unwanted sources of variability. For example, a metallurgist wishes to improve the strength of a certain steel component. Four factors at 2-levels each were considered for the experiment. An eight-trial experiment was chosen, but it was possible to run only four experimental trials per day. Hence each day was treated as a separate block, with the purpose of reducing day-to-day variation. It is important that the experimental trials within the block be as homogeneous as possible.

In the context of ED, one usually has to obtain blocking generator(s) prior to applying a blocking strategy. In order to obtain the blocking generators, it is advised to decide on the number of blocks needed for the experiment as well as the block size. It is important to ensure that the block generators are not confounded with the main effects or with two-factor interaction effects. [Box et al. \(1978\)](#) provide a useful table which illustrates the number of blocks, block size, recommended block generators, the number of experimental trials and the resolutions of the blocked design.

### **8.1.11 Understanding the confounding pattern of factor effects**

The confounding pattern is often overlooked by many experimenters who use Taguchi OA designs, Plackett–Burmann designs or highly fractionated factorial designs. If we study three factors at 2-levels using four runs, the main effects will be confounded with two-factor interactions. In other words, the estimates of main effects cannot be separated out from the interactions. It is always dangerous to run such a low-resolution fractional factorial design. In the above case, we generally assign factor A to column 1, factor B to column 2 and factor C to column 3. In fact, column 3 can also be obtained due to the interaction between factors A and B. In other words, main effect C is confounded with interaction AB. If column 3 is significant from the statistical analysis, then we don't know whether the effect is the result of C, AB or both.

Confounding can be avoided by carefully choosing high-resolution fractional designs, but the cost factor will go up due to the large size of the experiment. The challenge here is to find the balance between the size of the experiment and the information gained from the experiment. An understanding of confounding structures (also called alias structures) can be a tremendous asset to the experimenter.

### **8.1.12 Perform confirmatory runs/experiments**

There is a tendency to eagerly grab the results, rush out to production and say, ‘We have the answer! This will solve the problem!’ Before doing that, it is important to take the time to verify the outcome of your experiment using confirmatory runs. A confirmatory run or experiment is necessary in order to verify the results of the experiment from the statistical analysis. If conclusive results have been obtained, it is then recommended to take improvement actions on the process under investigation. In contrast, if the results do not turn out as expected, further investigation would then be required (Taguchi, 1986). Some of the possible causes for not achieving the objective of the experiment include the following:

- wrong choice of ED for the experiment
- incorrect choice of quality characteristic (or response) for the experiment
- important factors that influence the response of interest are not as yet identified
- presence of non-linear or curvature effect of factors on the response of interest
- inadequate control of noise factors, causing unpleasant variation in the process under investigation
- measurement system error is very high
- rushing into data analysis without understanding the details of assumptions behind the data analysis
- problem scope was not clearly understood by the team
- lack of expertise on the part of the user in the statistical analysis.

## **Exercises**

1. Explain why unclear experimental objectives can lead to lost time and money.
2. What factors should be considered for the selection of an ED project?

3. Why is brainstorming important in the context of ED?
4. What are the advantages of choosing measurable quality characteristics over attribute characteristics?
5. Why must experiments be conducted in an iterative manner?
6. Why is blocking important in industrial designed experiments?
7. Why do we need to perform confirmatory runs/experiments?
8. How do you differentiate between replication and repetition?
9. What are the pros and cons of randomisation as a principle of ED?

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## 9.1 Introduction

This chapter presents a collection of real industrial case studies. The case studies illustrated in this chapter are well-planned experiments and not simply a few experimental trials to explore the effects of varying one or more factors at a time. The case studies will provide a good foundation for students, researchers and practitioners on how to go about carrying out an experiment in real industrial settings. The case studies will cover the nature of the problem or objective of the experiment, list of factors, their levels, response of interest, choice of a particular design (i.e. number of trials used), analysis using Minitab software, interpretation of results and benefits gained from the experiment. These case studies will increase the awareness of the application of experimental design (ED) techniques in industries and its potential in tackling process optimisation and variability problems.

## 9.2 Case studies

### 9.2.1 Optimisation of a radiographic quality welding of cast iron

#### 9.2.1.1 Objective of the experiment

The objective of the experiment was to identify the significant welding parameters and to determine the optimal parameter settings which gave minimum crack length.

#### 9.2.1.2 Selection of the response function

The response of interest for the experiment was crack length measured in centimetres.

#### 9.2.1.3 List of factors and interactions of interest for the experiment

Five main effects and two two-order interactions were identified from a thorough brainstorming session. The list of main and interaction effects is shown below.

*Main effects:* current (A), bead length (B), electrode make (C), V-groove angle (D) and welding method (E)

*Interaction effects:* A  $\times$  B and B  $\times$  C

### 9.2.1.4 Levels of parameters and their ranges

Each parameter was studied at 2-levels. The ranges of welding parameters are given in [Table 9.1](#).

### 9.2.1.5 Choice of design and number of experimental trials

As the number of factors is more than four, it was decided to select a fractional factorial design rather than a full factorial design. The number of degrees of freedom for studying both main effects and interactions is equal to 7. The closest number of experimental trials that can be employed for this study is 8. This means it is a  $2^{(5-2)}$  fractional factorial design in which main effects are confounded with two-factor interactions. In other words, the design resolution of this design is III.

### 9.2.1.6 Design generators and the confounding structure of the design

Design generators: D = AC and E = ABC

Defining relationship: I = ACD, I = ABCE and I = BDE

$$A = CD = BCE$$

$$B = ACE = DE$$

$$C = AD = ABE$$

Confounding pattern: D = AC = BE

$$E = ABC = BD$$

$$AB = CE = ADE = BCD$$

$$AC = BE, \quad BC = AE = ABD = CDE$$

### 9.2.1.7 Uncoded design matrix with response values

The uncoded design matrix showing all the real factor settings, along with the respective response values, is given in [Table 9.2](#). Each trial condition was replicated

**Table 9.1** List of factors and their ranges for the experiment.

Welding parameters	Labels	Low level	High level
Current	A	110	135
Bead length	B	20	30
Electrode make	C	X	Y
V-groove angle	D	45	60
Welding method	E	1	2

**Table 9.2** Uncoded design matrix with response values.

Standard order	C	B	A	D = AC	E = ABC	Crack length (cm)
1 (5)	X	20	110	60	1	9, 12
2 (3)	Y	20	110	45	2	7, 8
3 (8)	X	30	110	60	2	7, 5
4 (2)	Y	30	110	45	1	13.5, 12.0
5 (6)	X	20	135	45	2	10, 9
6 (1)	Y	20	135	60	1	6.5, 8
7 (7)	X	20	135	45	1	7, 6
8 (4)	Y	20	135	60	2	7.5, 8

Note: () represents the order in which the experimental runs were carried out.

twice to create adequate degrees of freedom for the error term. Randomisation strategy was employed to minimise the effect of lurking variables and undesirable external influences induced into the experiment. As we can see from [Table 9.2](#), welding parameter C (electrode make) was assigned to column 1 as it was not practical to change the levels of this factor frequently.

### 9.2.1.8 Analysis and interpretation of results

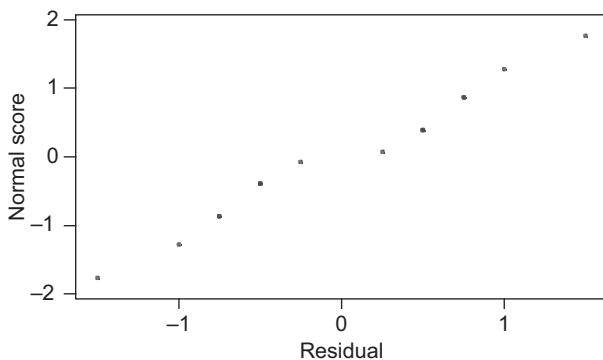
The first step was to check the data for normality assumptions. This was achieved by constructing normal probability plot (NPP) of residuals ([Fig. 9.1](#)). The plot suggests that the data follow a normal distribution. The analysis part involves the determination of significant main and interaction effects, followed by the selection of optimal welding parameter settings which yield minimum crack length. In order to identify the most important main and interaction effects, it was decided to use a Pareto plot of effects ([Fig. 9.2](#)). [Fig. 9.2](#) indicates that main effects A and E and interaction effect BC were considered to be real (or active). In order to analyse interaction between B and C, it was decided to use an interaction plot, shown in [Fig. 9.3](#).

[Fig. 9.3](#) indicates that there is a strong interaction between B and C. Moreover, it can be observed from [Fig. 9.3](#) that crack length is minimum when B is kept at a high-level setting and C at a low-level setting. In order to determine the optimal welding parameter settings that yield minimum crack length, a main effects plot is constructed ([Fig. 9.4](#)). The optimal settings for minimising crack length are as follows:

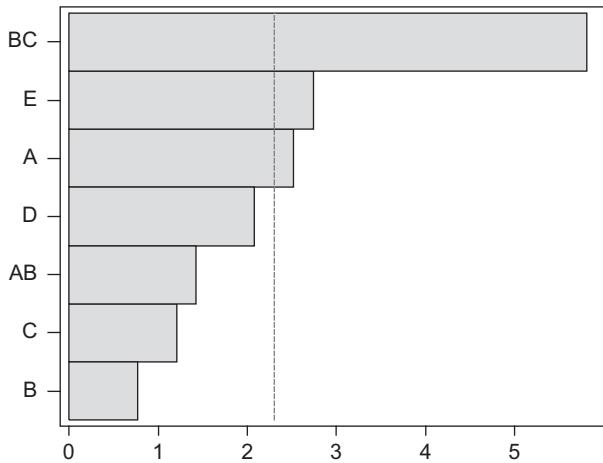
- A: + 1 (high level)
- B: + 1 (high level)
- C: - 1 (low level)
- D: + 1 (high level)
- E: + 1 (high level)

### 9.2.1.9 Confirmatory trials

Three confirmatory trials based on the optimal settings were performed and crack lengths of 0.31, 0.46 and 0.32 mm were observed. The results of the study have



**Figure 9.1** NPP of residuals. *NPP*, Normal probability plot.



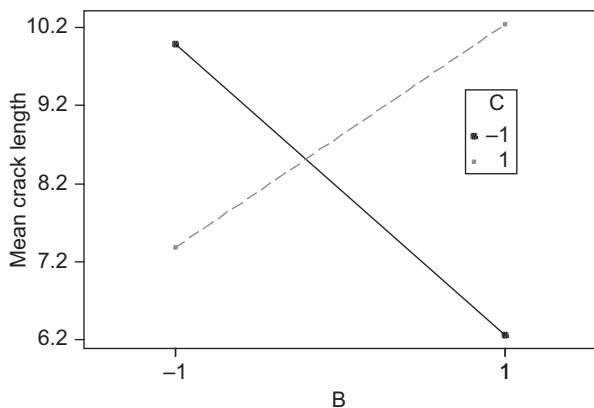
**Figure 9.2** Pareto plot of effects from the experiment.

demonstrated a significant improvement to the process and a significant reduction in scrap and rework was achieved.

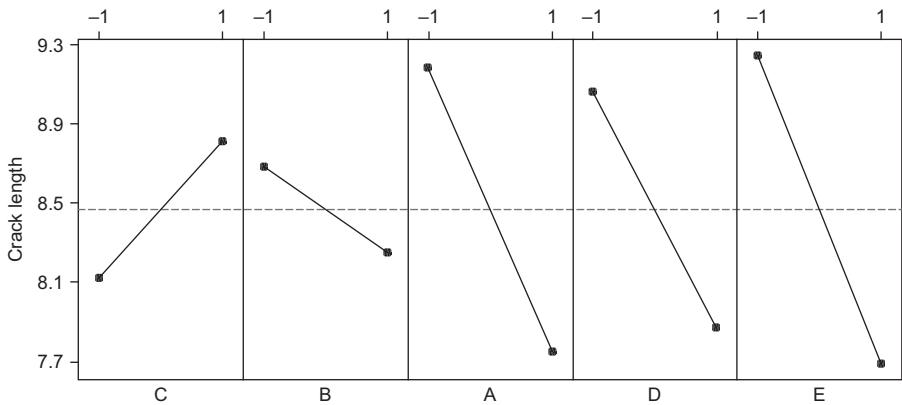
## 9.2.2 Reducing process variability using experimental design technique

### 9.2.2.1 Objective of the experiment

The objective of the experiment was to identify the most important process parameters that affect variability in response.



**Figure 9.3** Interaction plot of B versus C.



**Figure 9.4** Main effects plot for crack length.

### 9.2.2.2 Selection of the response

The response of interest for the experiment was expulsion force measured in kilograms (kg). Here expulsion force is the force required to expel the device or component from a certain tube.

### 9.2.2.3 List of process parameters and their levels

Seven process parameters were identified from a brainstorming session with people from production, maintenance, quality, design and the shop floor. As part of the initial investigation of the study, it was decided to study the main effects on variability in expulsion force. The parameters used for the experiment and their levels are illustrated in [Table 9.3](#).

**Table 9.3** List of process parameters and their levels.

Process parameters	Labels	Low level	High level
Position of the cam	A	Forward (F)	Backward (B)
Drum temperature	B	84	104
Time	C	68	72
Type of material	D	1	2
Clearance	E	0.006	0.012
Machine alignment	F	134	130
Header temperature	G	190	210

#### 9.2.2.4 Choice of design and number of experimental trials required for the experiment

For this study, seven factors were thought to have some impact on variability in expulsion force. A full factorial experiment (FFE) would require a total of 128 experimental trials. Owing to limited budget and the top management needing a speedy response to this investigation, it was decided to use a highly fractionated factorial design. Here the objective was to identify the key process parameters so that further smaller experiments could be carried out to study the interactions among the key parameters. The number of degrees of freedom associated with seven factors at 2-levels is equal to 7. Hence, the number of degrees of freedom required for the experiment must be greater than 7. The closest number of experimental trials that can be employed for this study is 8, that is a  $2^{(7-4)}$  fractional factorial design was selected.

#### 9.2.2.5 Design generators and resolution

$$C = -AB$$

$$E = -AD$$

$$F = -BD$$

$$G = ABC$$

As the main effects are confounded with two-factor interactions, the resolution of this design is III.

#### 9.2.2.6 Coded and uncoded design matrix with response values

The uncoded and coded design matrices with response values are given in [Tables 9.4](#) and [9.5](#). Each trial condition was repeated five times to analyse variability.

#### 9.2.2.7 Analysis and interpretation of results

As the objective of the experiment is to reduce variability in expulsion force, the first step is to identify which of the seven factors have an impact on variability. In

**Table 9.4** Uncoded design matrix with response values.

Run	A	B	C	D	E	F	G	Expulsion force (kg)
1	F	84	68	1	0.006	134	190	0.990, 1.037, 0.965, 0.860, 1.086
2	B	84	72	1	0.012	134	210	0.875, 0.748, 0.959, 0.600, 0.807
3	F	104	72	1	0.006	130	210	0.924, 0.881, 0.733, 0.767, 0.873
4	B	104	68	1	0.012	130	190	0.760, 0.620, 0.669, 0.632, 0.605
5	F	84	68	2	0.012	130	210	0.741, 0.455, 0.549, 0.468, 0.646
6	B	84	72	2	0.006	130	190	0.787, 1.061, 0.607, 1.168, 0.878
7	F	104	72	2	0.012	134	190	0.508, 0.446, 0.351, 0.419, 0.421
8	B	104	68	2	0.006	134	210	0.691, 0.771, 0.940, 0.743, 0.675

**Table 9.5** Coded design matrix with response values.

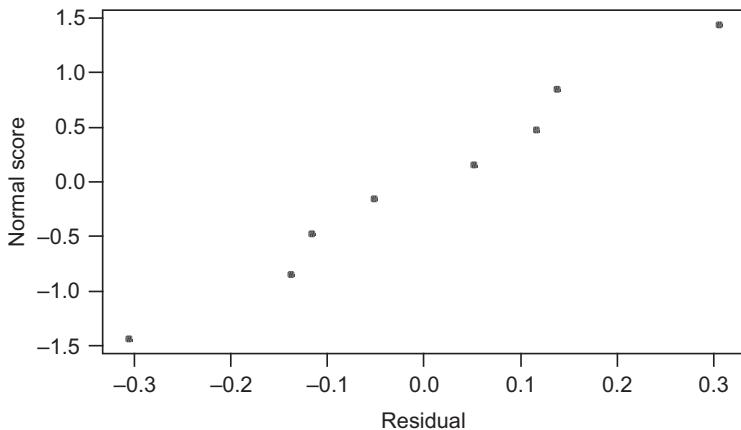
Run	A	B	C	D	E	F	G	Expulsion force (kg)
1	-1	-1	-1	-1	-1	-1	-1	0.990, 1.037, 0.965, 0.860, 1.086
2	1	-1	1	-1	1	-1	1	0.875, 0.748, 0.959, 0.600, 0.807
3	-1	1	1	-1	-1	1	1	0.924, 0.881, 0.733, 0.767, 0.873
4	1	1	-1	-1	1	1	-1	0.760, 0.620, 0.669, 0.632, 0.605
5	-1	-1	-1	1	1	1	1	0.741, 0.455, 0.549, 0.468, 0.646
6	1	-1	1	1	-1	1	-1	0.787, 1.061, 0.607, 1.168, 0.878
7	-1	1	1	1	1	-1	-1	0.508, 0.446, 0.351, 0.419, 0.421
8	1	1	-1	1	-1	-1	1	0.691, 0.771, 0.940, 0.743, 0.675

order to analyse variability, both standard deviation (SD) and  $\ln(\text{SD})$  (natural logarithms of SD) were computed at each ED point. The results are given in [Table 9.6](#).

An NPP of residuals was constructed for the validity of normality assumptions ([Fig. 9.5](#)). [Fig. 9.5](#) shows that the data come from a normal population. Having checked

**Table 9.6** Standard deviation (SD) and  $\ln(\text{SD})$  values.

Run	A	B	C	D	E	F	G	S	$\ln(\text{SD})$
1	-1	-1	-1	-1	-1	-1	-1	0.085	-2.465
2	1	-1	1	-1	1	-1	1	0.136	-1.995
3	-1	1	1	-1	-1	1	1	0.081	-2.513
4	1	1	-1	-1	1	1	-1	0.0621	-2.779
5	-1	-1	-1	1	1	1	1	0.122	-2.104
6	1	-1	1	1	-1	1	-1	0.222	-1.505
7	-1	1	1	1	1	-1	-1	0.057	-2.865
8	1	1	-1	1	-1	-1	1	0.106	-2.244

**Figure 9.5** NPP of residuals for  $\ln(\text{SD})$ . *NPP*, Normal probability plot.

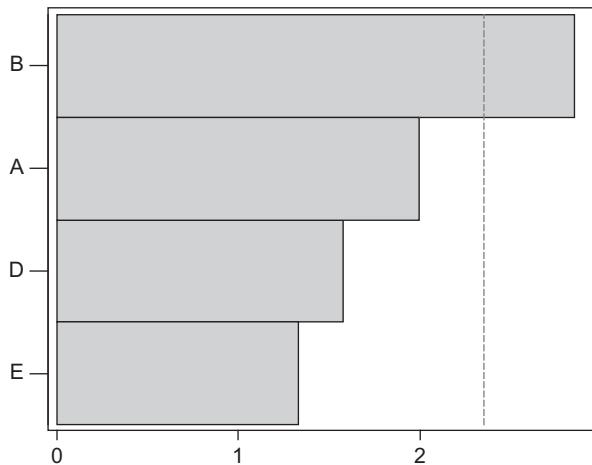
the data for normality, the next step was to identify the factors which influence variability in expulsion force. Both a main effects plot and a Pareto plot are used to identify the key process parameters or factors which have an impact on variability. The graphs (Figs. 9.6 and 9.7) indicate that factor B has a significant impact on variation. In order to obtain adequate degrees of freedom for the error variance term, a pooling strategy was utilised. The rule of thumb is to pool the effects with low magnitude till the error degrees of freedom is nearly half the total degrees of freedom. It was interesting to note that variability is minimum when factor B is kept at high level (Fig. 9.7).

#### 9.2.2.8 Determination of optimal settings to minimise variability

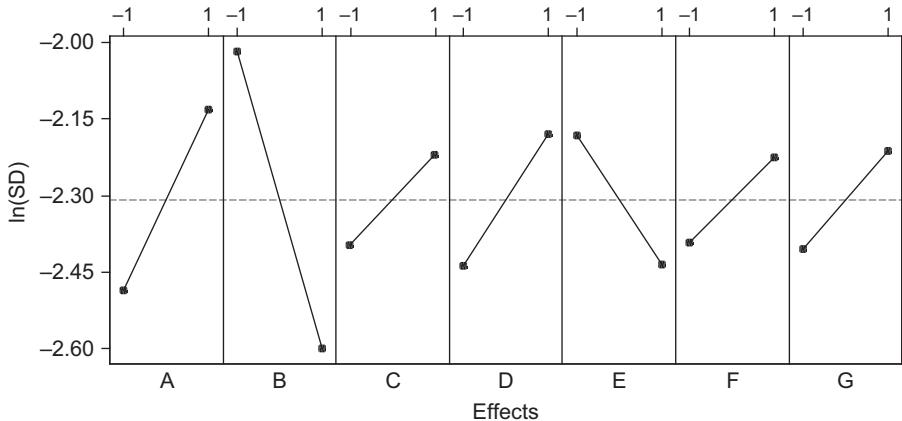
In order to determine the optimal settings to minimise variability, the first step was to rank the factors (in descending order of importance) that influence variability in expulsion force.

Factor B – Rank 1

Factor A – Rank 2



**Figure 9.6** Pareto plot of effects for  $\ln(\text{SD})$ .



**Figure 9.7** Main effects plot for  $\ln(\text{SD})$ .

Factor D – Rank 3

Factor E – Rank 4

Factor G – Rank 5

Factor C – Rank 6

Factor F – Rank 7

The optimal condition based on the main effects plot was obtained as follows:

$$\mathbf{B}_{(1)}\mathbf{A}_{(-1)}\mathbf{D}_{(-1)}\mathbf{E}_{(1)}\mathbf{G}_{(-1)}\mathbf{C}_{(-1)}\mathbf{F}_{(-1)}$$

### **9.2.2.9 Confirmation trials**

Fifteen samples were produced under the optimal conditions and compared against the samples produced under standard production conditions. The sample SD at the optimal settings was reduced to 0.042 kg as opposed to 0.125 kg under normal production conditions. The reduction in SD was therefore estimated to be approximately 66%.

### **9.2.2.10 Significance of the work**

Due to the significant reduction in process variability, the actual capability of the process has increased from 0.86 to over 1.78. This clearly demonstrates a dramatic improvement in the process performance and thereby more reliable and consistent products can be produced by determining the optimal condition of the process under study. The benefits from this study include increased customer satisfaction, reduced warranty costs, reduced customer complaints, reduced scrap and rework, improved market share, improved process control and so forth. The engineering team, including production personnel, quality engineers and managers of the company, are now well aware of the benefits that can be gained from the application of ED methods. Moreover, the awareness that has been established within the organisation has built confidence among the engineers, managers and front-line workers in other areas facing similar difficulties.

## **9.2.3 Slashing scrap rate using fractional factorial experiments**

### **9.2.3.1 Nature of the problem**

This case study describes the application of a highly fractionated factorial design to a manufacturing process that makes electromagnetic clutch coils. The coils were made of about 0.75-mm diameter copper wire. When the coil is wound to form into a solenoid, the wire is heated to around 180°C, which turns the insulation into an adhesive that bonds the wires together. However, the company that produces these coils was facing a quality problem in the form of high scrap rate, rework etc. which resulted in huge failure costs for the company. Hence, it was important for the company to find out what was causing this.

### **9.2.3.2 Objective of the experiment**

The objective of the experiment was to identify the most important machine parameters that gave the minimum scrap rate (%).

### **9.2.3.3 Selection of the response**

The response of interest for the experiment was the percentage of rejects.

### 9.2.3.4 List of process parameters and their levels

With limited budget and resources, it was important to study the effect of seven parameters on the percentage of rejects. To minimise the number of experimental trials, each factor was studied at 2-levels: low and high. The process (or machine) parameters and their levels are given in [Table 9.7](#).

### 9.2.3.5 Coded design matrix with response values for the experiment

The coded design matrix describes all the process parameter combinations at their respective levels and the order in which the runs or experimental trials were performed. A total of 2500 samples were used for each trial condition, and the percentage of rejects recorded for the analysis. In order to minimise the effect of lurking variables, randomisation strategy was employed. The results of the experiment are given in [Table 9.8](#).

### 9.2.3.6 Analysis and interpretation of results

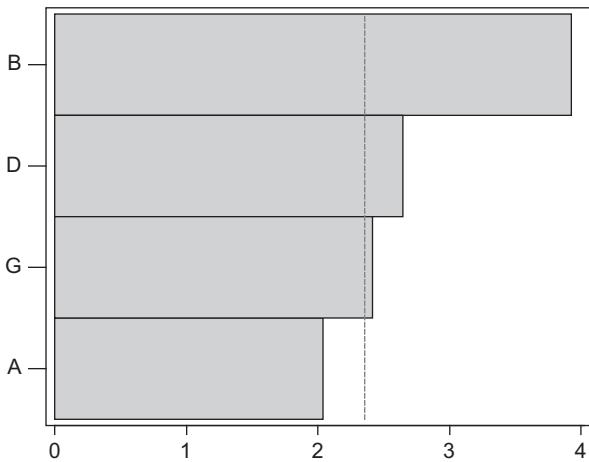
The analysis part involves the identification of the most important machine (or process) parameters that likely cause the problem. In order to identify the key parameters, a Pareto plot was used ([Fig. 9.8](#)).

**Table 9.7** List of parameters and their levels used for the experiment.

Process parameters	Labels	Low level	High level
Felt lubrication	A	Dry	Soaked
Wire diameter	B	0.75 mm	0.76 mm
Friction on pulley	C	Low	High
Brake tension	D	1.5 kg	2 kg
Winding width	E	High	Low
Dirt buildup	F	Unclean	Clean
Axial start position	G	A	B

**Table 9.8** Experimental layout with response values.

Standard Order	A	B	C	D	E	F	G	Rejects (%)
1	-1	-1	-1	-1	-1	-1	-1	1.08
2	1	-1	1	-1	1	-1	1	2.52
3	-1	1	1	-1	-1	1	1	1.12
4	1	1	-1	-1	1	1	-1	1.20
5	-1	-1	-1	1	1	1	1	3.04
6	1	-1	1	1	-1	1	-1	2.76
7	-1	1	1	1	1	-1	-1	1.00
8	1	1	-1	1	-1	-1	1	1.92



**Figure 9.8** Pareto plot of effects for the experiment.

**Fig. 9.8** shows that machine parameters B, D and G are statistically significant at the 10% significance level. Machine parameters A, C, E and F have a relatively trivial effect. Having identified the key parameters, the next step was to determine the settings that yield the best performance. For the present study, a main effects plot was constructed (**Fig. 9.9**). The graph clearly shows that the optimal level of all the parameters except B (the most important) is  $-1$  (low-level setting). The optimal settings for the parameters were obtained as follows:

$$A_{(-1)}B_{(1)}C_{(-1)}D_{(-1)}E_{(-1)}F_{(-1)}G_{(-1)}$$

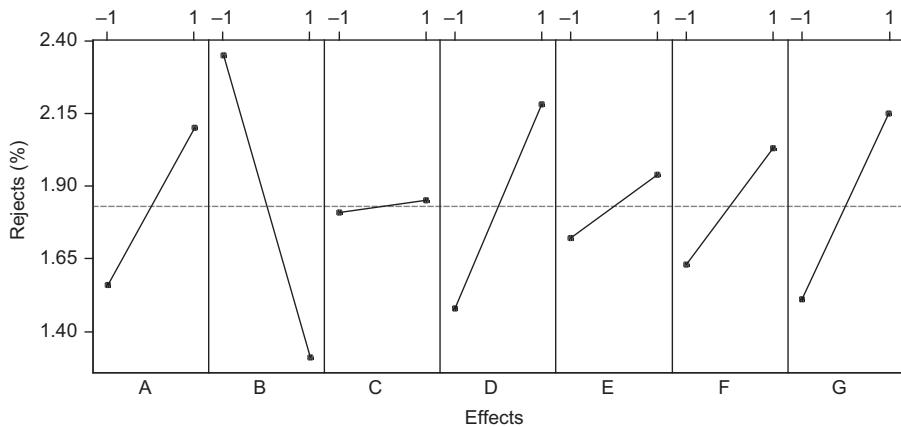
### 9.2.3.7 Confirmation runs

For confirmation runs, five batches of 500 samples were used. The results of the confirmation runs were remarkable due to a very significant reduction in the scrap rate of only 0.37%. As a result of this significant reduction in scrap, the company expects to save more than \$120,000 per annum. Moreover, the quality and production personnel of the organisation have been persuaded to extend the application of simple ED methods to other core processes.

## 9.2.4 Optimising the time of flight of a paper helicopter

### 9.2.4.1 Objective of the experiment

The objective of the experiment was to determine the optimal settings of the design parameters which would maximise the time of flight of a paper helicopter.



**Figure 9.9** Main effects plot for the experiment.

#### 9.2.4.2 Description of the experiment

The experiment was carried out by the author in a classroom for a postgraduate course in quality management with the aim of demonstrating how the DoE can be employed for optimising the design parameters of a simple paper helicopter. The experiment requires paper, scissors, a ruler, paper clips, measuring tape and a stopwatch. It would take approximately 5–6 h to design, conduct and analyse the results of the experiment. The model of a paper helicopter design is shown in Fig. 9.10.

#### 9.2.4.3 Selection of the response

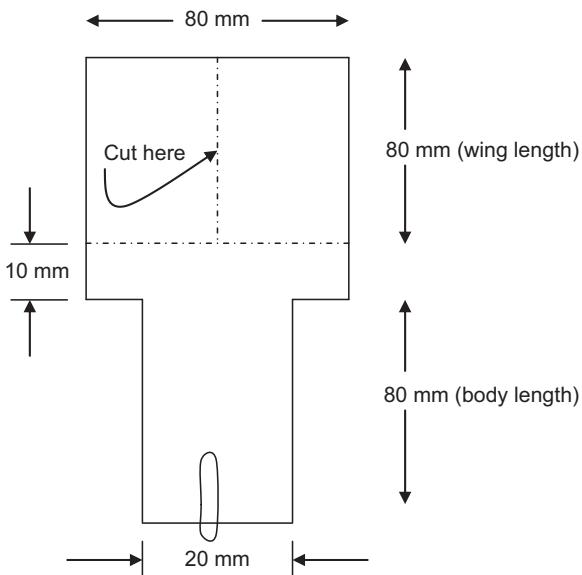
The response of interest to the experimenter in this case was the time of flight measured in seconds.

#### 9.2.4.4 List of design parameters and their levels

Six design parameters were chosen for this experiment. In order to make the experiment simple, it was decided to study each design parameter at 2-levels. Design parameters at 3-levels are more complicated to teach in the first place and moreover the author strongly believes that it might discourage engineers from further learning DoE. The logic behind a simple but practical experiment of this nature is to demonstrate the importance of ED and to illustrate how it works in real-life situations. Table 9.9 presents the design parameters and their levels selected for the experiment.

Apart from the main effects, three interaction effects were also of interest to analyse for the experiment. These are as follows:

1.  $B \times C$
2.  $B \times D$
3.  $A \times E$



**Figure 9.10** Model of a paper helicopter design.

**Table 9.9** List of design parameters and their levels.

Design parameters	Labels	Low level (-1)	High level (+1)
Paper type	A	Normal	Bond
Body length	B	80 mm	130 mm
Wing length	C	80 mm	130 mm
Body width	D	20 mm	35 mm
Number of clips	E	1	2
Wing shape	F	Flat	Angled 45 degrees up

In order to minimise the effect of noise parameters such as draft and operator on the time of flight, extra caution was taken during the experiment. The experiment was conducted in a closed room to dampen the effect of draft. The same operator was responsible in all instances for minimising the reaction time of hitting the stopwatch when the helicopter was released and when it hit the floor.

#### 9.2.4.5 Choice of design and design matrix for the experiment

As we are interested in studying six main effects and three interaction effects, the total degrees of freedom are equal to 9. The closest number of experimental trials that can be employed for the experiment is 16 (i.e.  $2^{(6-2)}$  fractional factorial design). This means that only a quarter replicate of an FFE is needed for the study.

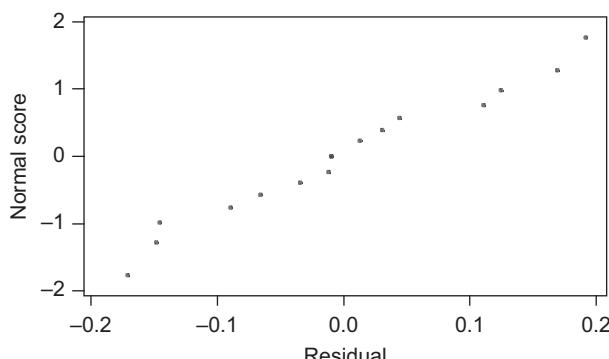
The uncoded design matrix for the experiment, along with recorded response values corresponding to each trial condition, is presented in [Table 9.10](#).

#### 9.2.4.6 Statistical analysis and interpretation of results

Prior to carrying out any statistical analysis, the first step was to check the data for normality assumptions. An NPP of residuals was constructed ([Fig. 9.11](#)) which indicates that the data come from a normal population ([William, 1990](#)). The next stage of the analysis was to identify which of the main or/and interaction effects have

**Table 9.10** Uncoded design matrix with response values.

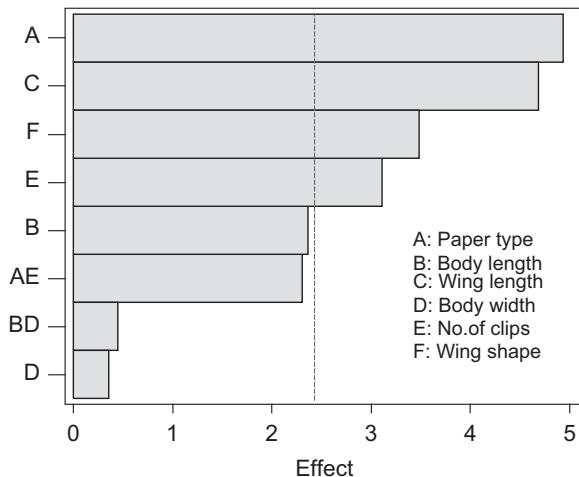
Run	A	B	C	D	E	F	Time of flight (s)
1 (6)	Normal	80	80	20	1	Flat	2.49
2 (9)	Bond	80	80	20	2	Flat	1.80
3 (11)	Normal	130	80	20	2	Angled	1.82
4 (15)	Bond	130	80	20	1	Angled	1.99
5 (12)	Normal	80	130	20	2	Angled	2.11
6 (2)	Bond	80	130	20	1	Angled	1.96
7 (16)	Normal	130	130	20	1	Flat	3.19
8 (14)	Bond	130	130	20	2	Flat	2.27
9 (10)	Normal	80	80	35	1	Angled	2.12
10 (1)	Bond	80	80	35	2	Angled	1.58
11 (7)	Normal	130	80	35	2	Flat	2.15
12 (3)	Bond	130	80	35	1	Flat	2.05
13 (8)	Normal	80	130	35	2	Flat	2.60
14 (4)	Bond	80	130	35	1	Flat	2.09
15 (5)	Normal	130	130	35	1	Angled	2.63
16 (13)	Bond	130	130	35	2	Angled	2.18



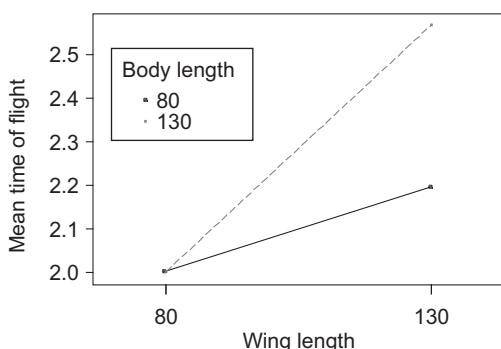
**Figure 9.11** NPP of residuals. *NPP*, Normal probability plot.

significant impact on the time of flight. It was decided to use a Pareto plot using Minitab software. Minitab plots the effects in decreasing order of the absolute value of the standardised effects and draws a reference line on the chart. Any effect that extends the reference line appears to be statistically significant. The Pareto plot of the effects (Fig. 9.12) show that the main effects (A, C, F and E) are statistically significant (assume 5% significance level).

None of the interactions appears to be statistically significant. The interaction between B and C was not statistically significant at 5% significance level, though it appeared to be important in the interaction graph (Fig. 9.13). It was rather interesting to observe that body width has no influence on the time of flight.



**Figure 9.12** Pareto plot of the effects from the experiment.



**Figure 9.13** Interaction plot between wing length and body length.

### 9.2.4.7 Determination of optimal design parameters

Having identified the significant design parameters that influence the time of flight, the next step is to determine the optimal settings that will maximise the time of flight. As none of the interaction effects were statistically significant, the best levels of each parameter can readily be obtained from a main effects plot (Fig. 9.14). The final optimal settings of the design parameters are as follows:

- Design parameter A – low level (normal paper)
- Design parameter B – high level (130 mm)
- Design parameter C – high level (130 mm)
- Design parameter D – low level (20 mm)
- Design parameter E – low level (no. of clips = 1)
- Design parameter F – low level (flat)

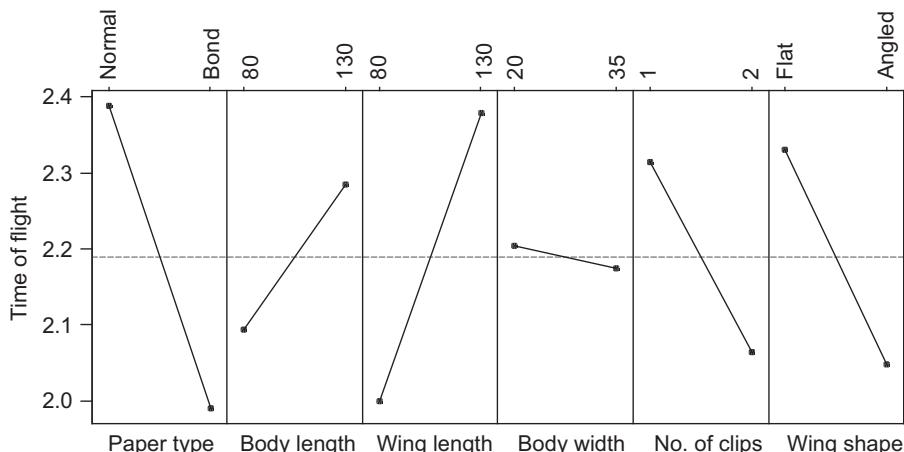
It was quite interesting to note that the time of flight was maximum when wing length and body length were kept at high levels.

### 9.2.4.8 Predicted model for time of flight

A simple regression model is developed based on the significant effects. It is important to note that the regression coefficients in the model are half the estimates of the effects. The regression model for the time of flight can be therefore written as

$$\hat{y} = \beta_0 + \beta_1(A) + \beta_2(C) + \beta_3(F) + \beta_4(E) \quad (9.1)$$

where  $\beta_0$  = overall mean time of flight = 2.19,  $\beta_1$  = regression coefficient of factor A (paper type),  $\beta_2$  = regression coefficient of factor C (wing length),  $\beta_3$  = regression coefficient of factor F (wing shape),  $\beta_4$  = regression coefficient of factor E (no. of clips).



**Figure 9.14** Main effects plot of the design parameters.

The predicted model for time of flight is therefore given by

$$\hat{y} = 2.19 + (-0.20 \times -1) + (0.19 \times 1) + (-0.14 \times -1) + (-0.13 \times -1) \quad \hat{y} = 2.85 \text{ s}$$

#### **9.2.4.9 Confirmatory runs**

A confirmatory experiment was carried out to verify the results from the analysis. Ten helicopters were made based on the optimal settings of the design parameters. The average flight time was estimated to be 3.09 s with an SD of 0.35 s.

CI (based on 95% confidence level) =  $\bar{y} + 3 \times \frac{SD}{\sqrt{n}}$ , where “SD” is the sample SD,  $\bar{y}$  is the sample mean and  $n$  is the sample size.

Therefore

$$\begin{aligned}\text{confidence interval} &= 3.09 \pm 3 \times 0.11 \\ &= 3.09 \pm 0.33 \\ &= (2.76, 3.42)\end{aligned}$$

As the predicted value (2.85 s) for the optimal settings falls within the above CI, we can conclude that the predicted model is sound.

#### **9.2.4.10 Significance of the work**

The purpose of this case study is to demonstrate the importance of teaching ED methods to people with limited skills in statistics for tackling variability and poor process performance problems. This experiment is quite old in its nature and has been widely used for some time by many statisticians for teaching purposes. Nevertheless the focus here was to minimise the statistical jargon associated with the technique and bring modern graphical tools for better and rapid understanding of the results to non-statisticians. The students of the class found this experiment very interesting specifically in terms of selecting the design, conducting the experiment and interpreting the results. Many students were quite astounded by the use of simple but powerful graphical tools and their reduced involvement of number crunching.

### **9.2.5 Optimising a wire bonding process using DoE**

#### **9.2.5.1 Objective of the experiment**

The following are the objectives of the experiment:

- to determine the optimal process parameter settings for enhanced strength.
- to develop a mathematical model which relates the wire pull strength and the key process parameters which influence the strength.

### 9.2.5.2 Description of the experiment

This case study illustrates a wire bonding process making a physical connection between the die and the lead. The purpose of this study was to increase the wire pull strength due to an increased number of customer complaints on broken wires (Green and Launsby, 1995).

### 9.2.5.3 Selection of the response

The response of interest to the experimenter was wire pull strength expressed in grams.

### 9.2.5.4 Identification of Process Variables for Experimentation

The following process variables were identified from a thorough brainstorming session. People from the quality department and the production department as well as operators were involved in the session. Each process variable was studied at 2-levels as part of the initial investigation. Table 9.11 presents the list of parameters used for the experiment.

The following interactions were of interest to the experimenter:

1.  $B \times C$
2.  $A \times C$
3.  $A \times D$
4.  $A \times B$

All three-order and higher order interactions are neglected.

### 9.2.5.5 Choice of design and experimental layout

The choice of design is dependent on the number of main and interaction effects to be studied, cost and time constraints, required design resolution etc. As the total degrees of freedom required for studying the four main effects and four interaction effects is equal to 8, the most suitable design for this experiment was a  $2^4$  FFE (Antony, 1999). This allows one to estimate all the main effects and interactions independently. Each trial condition was randomised to minimise the effect of lurking variables. The uncoded design matrix along with response values is shown in Table 9.12. The next step illustrates how the results of the experiment have been analysed.

**Table 9.11** List of process parameters used for the experiment.

Process variables	Labels	Low level	High level	Unit
Power	A	100	150	mW
Temperature	B	140	200	°C
Bonding time	C	15	25	ms
Bonding force	D	3	9	g

**Table 9.12** Uncoded design matrix for the experiment.

Trial no.	A	B	C	D	Pull strength
1 (7)	-1	-1	-1	-1	7.4
2 (11)	1	-1	-1	-1	6.5
3 (5)	-1	1	-1	-1	8.2
4 (15)	1	1	-1	-1	8.8
5 (2)	-1	-1	1	-1	7.6
6 (9)	1	-1	1	-1	6.8
7 (10)	-1	1	1	-1	8.4
8 (16)	1	1	1	-1	8.6
9 (3)	-1	-1	-1	1	9.4
10 (13)	1	-1	-1	1	8.0
11 (4)	-1	1	-1	1	9.8
12 (1)	1	1	-1	1	8.9
13 (6)	-1	-1	1	1	9.0
14 (12)	-1	-1	1	1	7.9
15 (8)	1	1	1	1	10.1
16 (14)	-1	1	1	1	9.1

### 9.2.5.6 Statistical analysis and interpretation

In order to identify the significant main effects and interaction effects, it was decided to use an NPP of effects. Those effects that fall off the straight line are deemed to be statistically significant and those that fall along the straight line are deemed to be statistically insignificant. The NPP of effects is shown in Fig. 9.15. Fig. 9.15 shows that main effects A, B, D and interaction effect AD are statistically significant at 5% significance level. In order to determine the best levels for A and D, it was important to analyse the interaction effect ( $A \times D$ ). Fig. 9.16 illustrates the interaction plot between A and D.

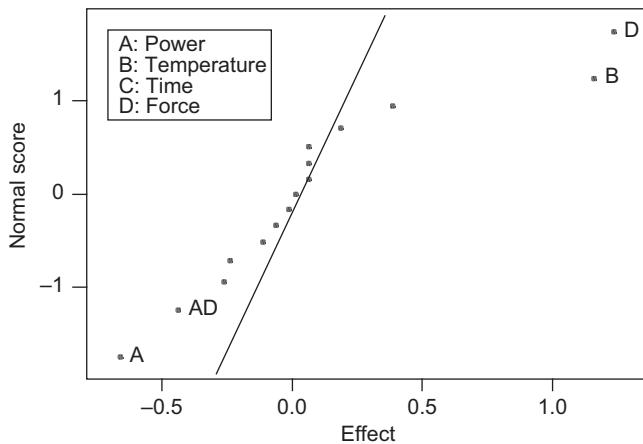
The non-parallel lines indicate that there is a strong interaction between the process variables A and D. As we can observe from the plot, the effect of bonding force on the pull strength is different at low and high levels of power. Minimum variability in pull strength is observed at a high level of power. On the other hand, mean strength is higher at a high level of bonding force (9 g) and a low level of power (100 mW).

In order to identify the optimal settings of process parameters which give maximum pull strength, a main effects plot was constructed (Fig. 9.17).

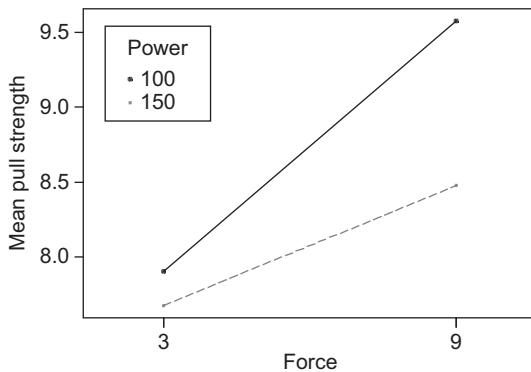
Table 9.13 presents the optimal settings of bonding process parameters that would yield maximum strength. It is important to note that bonding time has no influence whatsoever on the pull strength. Hence, it was decided to select 15 ms as the optimal value rather than 25 ms. Here, bonding time can be treated as a cost adjustment factor.

### 9.2.5.7 Model development based on the significant factor/interaction effects

Having identified the significant main and interaction effects which influence the pull strength, it was considered important to develop a simple regression model



**Figure 9.15** NPP of effects. *NPP*, Normal probability plot.



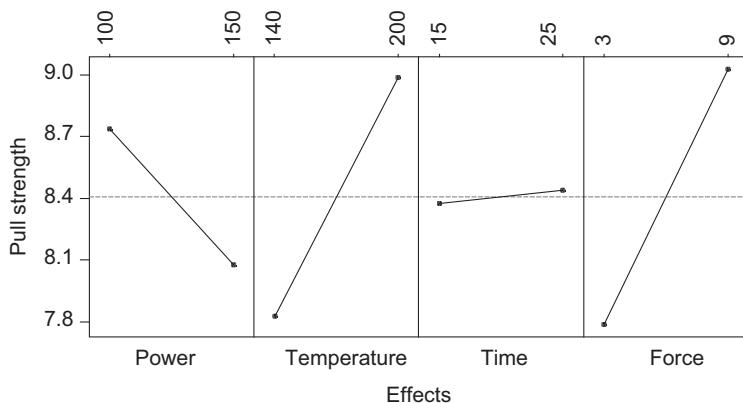
**Figure 9.16** Interaction between power (A) and force (D).

which provides the relationship between the pull strength and the critical effects (Hamada, 1995). The use of this model is to predict the pull strength for different combinations of wire bonding process parameters at their best levels. It is important to note that for process parameters at 2-levels, the regression coefficients are half the estimates of the effects. **Table 9.14** presents the estimates of significant effects and regression coefficients. The regression model for the wire bonding process as a function of significant main and interaction effects is given by

$$\hat{y} = \beta_0 + \beta_1(A) + \beta_2(B) + \beta_4(D) + \beta_{14}(A \times D)$$

$$\hat{y} = 8.41 - 0.33 A + 0.58 B + 0.62 D - 0.22 AD$$

where  $\hat{y}$  is the predicted pull strength.



**Figure 9.17** Main effects plot of wire bonding experiment.

**Table 9.13** Optimal condition of the wire bonding process.

Process parameters	Uncoded level	Coded level
Power	100 mW	-1
Temperature	200°C	1
Bonding time	15 ms	-1
Bonding force	9 g	1

**Table 9.14** Estimates of effects and regression coefficients.

Process parameters/interactions	Estimate of effects	Regression coefficients
A	-0.663	-0.33
B	1.162	0.58
D	1.237	0.62
AD	-0.438	-0.22

The predicted pull strength based on the significant factor and interaction effects (based on the optimal condition) is hence given by

$$\hat{y} = 8.41 - 0.33(-1) + 0.58(1) + 0.62(1) - 0.22(-1)(1) \quad \hat{y} = 10.16$$

Confirmation trials at the optimal condition have yielded a mean pull strength of 10.25 g. A 95% CI of the mean pull strength is given by

$$\begin{aligned} 95\% \text{ CI} &= \bar{y} \pm 3(\text{s.e.}), \text{ where s.e. is the standard error} \\ &= 10.25 \pm 3(0.19) \\ &= (9.68, 10.82) \end{aligned}$$

As the predicted value falls within this interval, it is fair to conclude that the predicted model for pull strength is sound and practical.

### 9.2.5.8 Conclusion

This case study presents a study performed on a certain wire bonding process using DoE with two objectives in mind. The first objective of the experiment is to understand the process by identifying the key wire bonding process parameters and the interactions of interest. The second objective was to develop a regression model for predicting the pull strength at the optimal condition of the process. The results of the study have shown an improvement in pull strength by more than 20% over the existing production conditions.

## 9.2.6 Training for DoE using a catapult

The purpose of this case study was to provide an insight into the process of understanding the role of DoE as part of a training programme to a group of engineers and managers in a world-class company. The results of the experiment have been extracted from a simple FFE performed using a catapult. The results of the experiment were analysed using Minitab software for rapid and easier understanding of the results.

### 9.2.6.1 Objective of the experiment

The objective of the experiment was to maximise the in-flight distance.

### 9.2.6.2 Selection of response

The response of interest to the team was in-flight distance measured in metres.

### 9.2.6.3 List of factors and their levels used for the experiment

Four factors (stop position (SP), peg height (PH), release angle (RA) and hook position (HP)) were studied at 2-levels. These factors were identified from a brainstorming session facilitated by the author. The levels for factors such as type of ball, type of rubber band and cup position were kept constant. This implies that a pink ball, the sixth cup position and a brown rubber band were used throughout the experiment. [Table 9.15](#) presents the list of factors and their levels used for the experiment.

**Table 9.15** List of factors and their levels for catapult experiment.

Factors	Labels	Low level	High level
Release angle	RA	180	Full
Peg height	PH	3	4
Stop position	SP	3	5
Hook position	HP	3	5

### 9.2.6.4 Choice of design and experimental layout for the experiment

It was decided to perform an FFE to allow us to study all the main and interaction effects. The experiment was replicated twice to capture the variation due to experimental set-up and air flow in the room. Each trial condition was randomised to minimise the bias induced into the experiment. The results of the experiment along with response values are given in [Table 9.16](#).

After the experiment was performed, the next step was to analyse and interpret the results so that necessary actions could be taken accordingly. The analysis of the experiment is often dependent on its objective. In this case, the objective was to identify the factors which affect the in-flight distance. The team used Minitab to analyse the data from the experiment. This is the focus of the next section.

### 9.2.6.5 Statistical analysis and interpretation of results

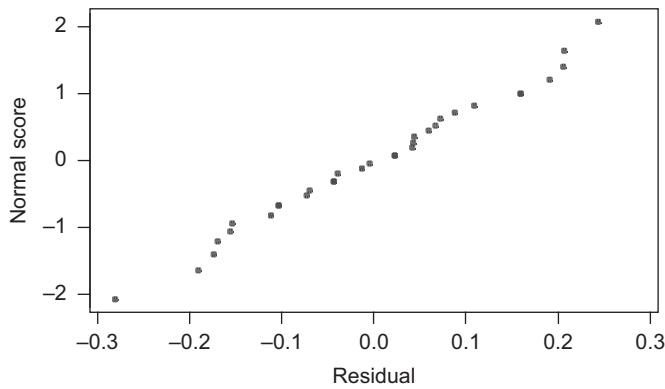
Prior to carrying out the statistical analysis, the first step was to check the data for normality assumptions. An NPP of residuals ([Fig. 9.18](#)) was constructed using Minitab software ([Minitab, 2000](#)). It can be seen in [Fig. 9.18](#) that all the points on the normal plot come close to forming a straight line. This implies that the data are fairly normal. The next step was to identify the most significant main and interaction effects which influence the distance.

**Table 9.16** Results of the FFE.

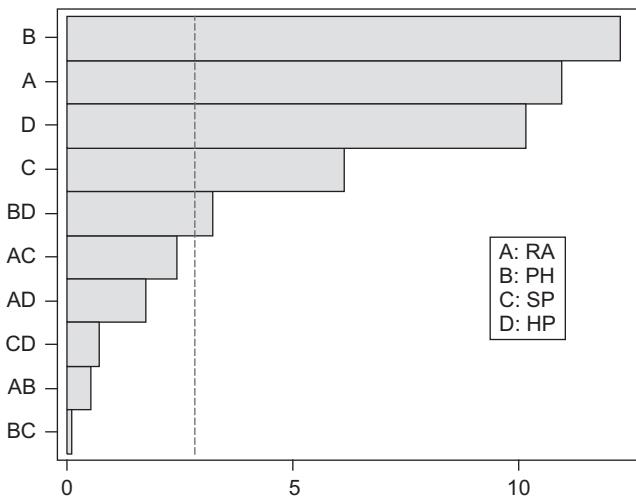
Trial no.	RA	PH	SP	HP	Distance (m)
1 (4)	-1	-1	-1	-1	3.62, 3.64
2 (8)	1	-1	-1	-1	4.01, 4.06
3 (11)	-1	1	-1	-1	4.16, 4.60
4 (7)	1	1	-1	-1	4.70, 4.90
5 (1)	-1	-1	1	-1	3.80, 3.83
6 (10)	1	-1	1	-1	4.37, 4.40
7 (3)	-1	1	1	-1	4.74, 4.77
8 (15)	1	1	1	-1	5.32, 5.58
9 (2)	-1	-1	-1	1	4.26, 4.13
10 (14)	1	-1	-1	1	4.74, 4.94
11 (6)	-1	1	-1	1	4.80, 5.02
12 (13)	1	1	-1	1	5.20, 5.55
13 (16)	-1	-1	1	1	4.46, 4.67
14 (5)	1	-1	1	1	5.12, 5.50
15 (12)	-1	1	1	1	4.80, 4.85
16 (9)	1	1	1	1	5.80, 5.91

FFE, Full factorial experiment.

Note: () represents the experimental trials/runs in random order.



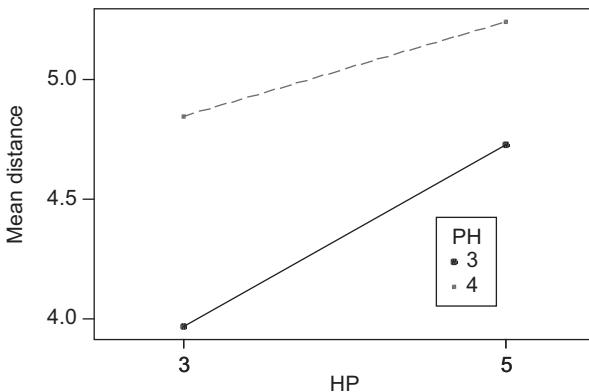
**Figure 9.18** Normal probability plot of residuals.



**Figure 9.19** Pareto plot of effects from a catapult experiment.

In order to identify the most important effects, it was decided to use a Pareto plot. The Pareto plot (Fig. 9.19) shows that all the main effects (RA, PH, HP and SP) and one interaction effect ( $\text{PH} \times \text{HP}$ ) are deemed to be active. In order to interpret the interaction between PH and HP effectively, an interaction plot was constructed (Fig. 9.20).

The interaction plot indicates that the effect of HP at different levels of PH is not the same. This implies that there is a strong interaction between these two factors. The graph also shows that maximum distance was achieved when HP was kept at position 5 and PH at position 4.



**Figure 9.20** Interaction plot – HP  $\times$  PH.

#### 9.2.6.6 Determination of optimal factor settings

In order to arrive at the optimal condition, the mean distance at each level of the control factor was analysed. A main effects plot was constructed to identify the best levels of the factors (Fig. 9.21). The best settings of the factors for maximising the in-flight distance are (Fig. 9.21):

RA – Full

PH – Position 4

SP – Position 5

Hook position – Position 5

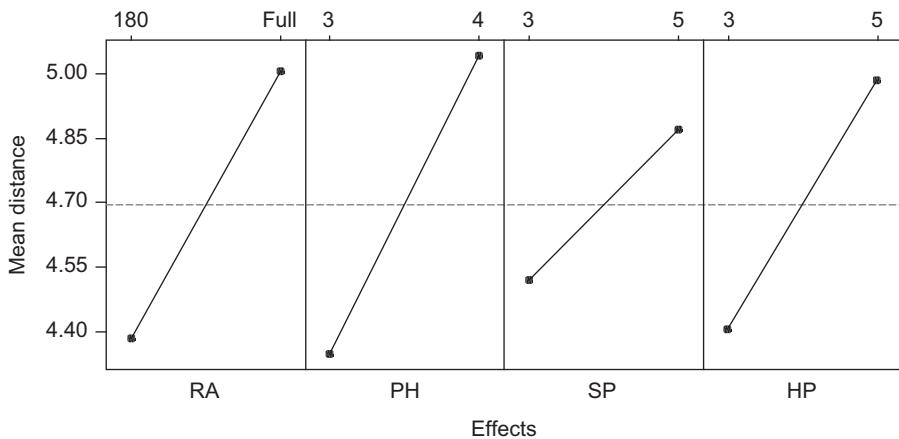
It is worthwhile noting that the optimal condition is one which corresponds to trial condition 16 (Table 9.16). This is due to the fact that it is an FFE, which shows all the possible combinations. This is not necessarily the case in many industrial experiments due to various constraints (time, cost, objective of the experiment, degree of resolution required, etc.).

#### 9.2.6.7 Confirmatory experiment

A confirmatory experiment was carried out to verify the results from the analysis. Five observations were made at the optimal condition. The average in-flight distance was estimated to be 5.84 m. It was also observed that a change of SP from 5 to 4 yielded even better average results in distance (i.e. 5.96 m).

#### 9.2.6.8 Significance of the work

The purpose of this case study was to bring the importance of teaching DoE to a group of engineers and managers in a world-class organisation using simple but powerful graphical tools. The focus of this study was to minimise the statistical jargon associated with DoE and to use modern graphical tools for a rapid decision-making process. The results of this experiment have provided a greater



**Figure 9.21** Main effects plot for the catapult experiment.

stimulus for the wider application of DoE by engineers within this organisation in other core processes for tackling variability-related and process optimisation problems.

### 9.2.7 Optimisation of core tube life using designed experiments

This case study presents two different experiments: the first was performed by the engineering team within the company and the second was performed by the author with the help of operations personnel within the company. The product of concern in this case study was a core tube used within a solenoid-operated directional control valve. The problem with this product was that its life was short when subjected to hydraulic fatigue test. The core tube assembly is welded and then machined prior to final assembly of the system. The company uses laser welding for core tube assembly and therefore most of the factors affecting the life of these core tubes were related to the laser welding process. Laser welding was chosen for the core tube assembly because the technique affords a high degree of repeatability and predictability and good control of penetration depth (Crafer and Oakley, 1981).

#### 9.2.7.1 Company's first attempt to experimental approach

The first experiment was performed by the engineering team, which consisted of a quality engineer, a design engineer, a production engineer and an operator. In order to keep the experimental budget to a minimum, it was decided to study all factors (or process parameters) at 2-levels. Three process parameters, which were believed to have some impact on the life of the core tube, were chosen by the team. The response of interest to the team was the fatigue life of the core tube, expressed in number of cycles (in millions).

The team decided to study only the effects of three laser welding process parameters. Interactions among the parameters were of interest to the team. A  $2^{(3-1)}$

fractional factorial design was chosen for the experiment. **Table 9.17** illustrates the list of welding process parameters used for the experiment.

**Table 9.18** presents the experimental layout for the optimisation of core tube life. The experimental layout displays the number of experimental trials, the process parameters and the response values corresponding to each ED point.

The desired number of cycles on average is about 8.5. This is to conform to the requirements of the National Fluid Power Association Standards. None of the above trial conditions yielded a value of more than 7 million cycles. The analysis of results indicates that weld speed has the highest impact on core tube life and ramp in has the least influence. **Table 9.19** presents the effects of the laser welding process parameters.

The objective of the experiment was to maximise the life of the core tube and hence it was important to determine the settings of the parameters which yield the maximum life of core tubes. The optimal settings were determined as follows:

Weld speed – high level (2 rev./s)

Ramp out – high level (2 s)

Ramp in – high level (1.5 s)

**Table 9.17** Process parameters for the experiment.

Process parameter	Label	Low level	High level	Units
Weld speed	A	1.5	2.0	Rev./s
Ramp out	B	1	2	Seconds
Ramp in	C	0.5	1.5	Seconds

**Table 9.18** Experimental layout for the experiment.

Run	A	B	C	No. of cycles (in millions)
1	1.5	1	1.5	1.92
2	2.0	1	0.5	4.80
3	1.5	2	0.5	2.24
4	2.0	2	1.5	6.93

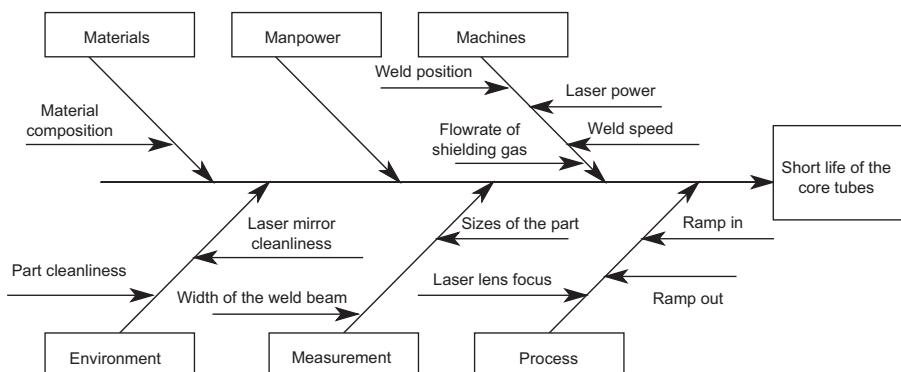
**Table 9.19** Effects of process parameters on core tube life.

Process parameter	Average response at Level 1	Average response at Level 2	Effect
Weld speed	2.08	5.865	3.785
Ramp out	3.36	4.585	1.225
Ramp in	3.52	4.425	0.905

The engineering team concluded that trial condition 4 (Table 9.18) gives the maximum core tube life. However, the desired value of the core tube was at least 8.5 million cycles. The above study conducted by the engineering team did not reveal any significant improvement to the process under investigation. Therefore a second case study was proposed with the aim of achieving better and more satisfactory results.

### 9.2.7.2 Company's second attempt to use designed experiments

The second attempt was made with the assistance of the author's skills and expertise in the area of study. A fishbone diagram (Fig. 9.22) was constructed to identify the process parameters which influence the life of the core tubes. Twelve process parameters were initially thought to have some impact on the life. Further to a number of iterations, it was decided to select 5 out of 12 process parameters. Table 9.20 lists the process parameters along with their ranges of settings. The ranges of these parameter settings were determined after a thorough brainstorming session with people from design, manufacturing, quality and the shop floor.



**Figure 9.22** Fishbone analysis of the problem.

**Table 9.20** List of process parameters and their ranges used for the second experiment.

Process parameters	Label	Units	Low level	High level
Weld speed	A	Rev./s	1.5	2.2
Ramp in	B	Seconds	1.0	2.0
Ramp out	C	Seconds	2.0	3.0
Laser power	D	Watts	950	1100
Lens focus	E	—	Position 1	Position 2

The following objectives were set by the company for the second round of experimentation. The objectives were determined by the team members and were as follows:

- to identify the laser welding process parameters which affect the mean fatigue life of core tubes,
- to identify the process parameters which influence variability in life and
- to determine the optimal settings of the process parameters which give maximum life with minimum variability.

For the second round of experimentation, the team decided to study the following interactions:

1.  $C \times D$
2.  $A \times C$
3.  $A \times D$

### **9.2.7.3 Choice of experimental layout for the experiment**

For the second experiment, five main effects and three interactions were of interest to the team. The number of degrees of freedom for studying five main effects and three interactions (each parameter at 2-levels) is equal to 8. The best possible design matrix or experimental layout for this experiment was a  $2^{(5-1)}$  fractional factorial experiment. This means that both main and interactions could be studied independently. The resolution of this design is V (i.e. main effects are clear of confoundings with two-way interactions and two-way interactions are free of confoundings with other two-way interactions). The following section explains the design generator and the confounding pattern of the design.

Design generator:  $E = ABCD$

Defining relationship = ABCDE

Confounding pattern:  $A = BCDE$ ,  $B = ACDE$ ,  $C = ABDE$ ,  $D = ABCE$ ,  $E = ABCD$ ,  $AB = CDE$ ,  $AC = BDE$ ,  $AD = BCE$ ,  $AE = BCD$ ,  $BC = ADE$ ,  $BD = ACE$ ,  $BE = ACD$ ,  $CD = ABC$ ,  $CE = ABD$ ,  $DE = ABC$ .

[Table 9.21](#) displays the results of the second experiment with response values. Each ED point was replicated twice to increase the precision of the experiment. Moreover, the trial condition was also randomised to minimise the effect of bias induced into the experiment.

### **9.2.7.4 Statistical analysis and interpretation**

In order to meet the objectives set at the outset of the project, it was important to perform statistical analysis of the data generated from the experiment. If the experiment was planned, designed, conducted and analysed correctly, then statistical analysis would provide sound and valid conclusions. The first step was to estimate the main and interaction effects of interest. [Table 9.22](#) presents the table of effects and regression coefficients.

**Table 9.21** Experimental layout and the response values for the experiment.

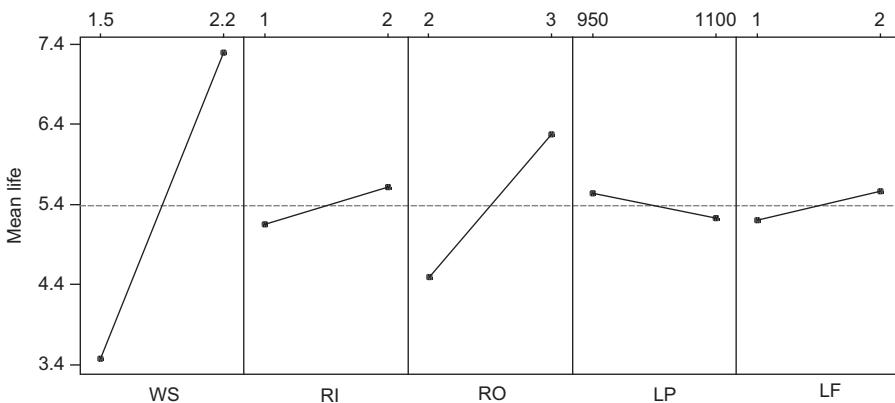
Standard order	Weld speed	Ramp in	Ramp out	Laser power	Lens focus	Fatigue life (million cycles)
1 (7)	1.50	1.0	2.0	950	2.0	4.8, 1.3
2 (3)	2.20	1.0	2.0	950	1.0	6.3, 5.5
3 (10)	1.50	2.0	2.0	950	1.0	5.6, 4.8
4 (2)	2.20	2.0	2.0	950	2.0	9.0, 5.6
5 (15)	1.50	1.0	3.0	950	1.0	1.6, 2.9
6 (1)	2.20	1.0	3.0	950	2.0	8.4, 11.5
7 (9)	1.50	2.0	3.0	950	2.0	0.8, 4.1
8 (4)	2.20	2.0	3.0	950	1.0	8.3, 8.1
9 (14)	1.50	1.0	2.0	1100	1.0	2.0, 2.8
10 (5)	2.20	1.0	2.0	1100	2.0	4.8, 5.1
11 (12)	1.50	2.0	2.0	1100	2.0	4.7, 1.0
12 (8)	2.20	2.0	2.0	1100	1.0	5.0, 3.7
13 (16)	1.50	1.0	3.0	1100	2.0	4.6, 4.4
14 (6)	2.20	1.0	3.0	1100	1.0	8.0, 8.4
15 (11)	1.50	2.0	3.0	1100	1.0	5.0, 5.2
16 (13)	2.20	2.0	3.0	1100	2.0	10.8, 8.2

**Table 9.22** Table of effects and regression coefficients.

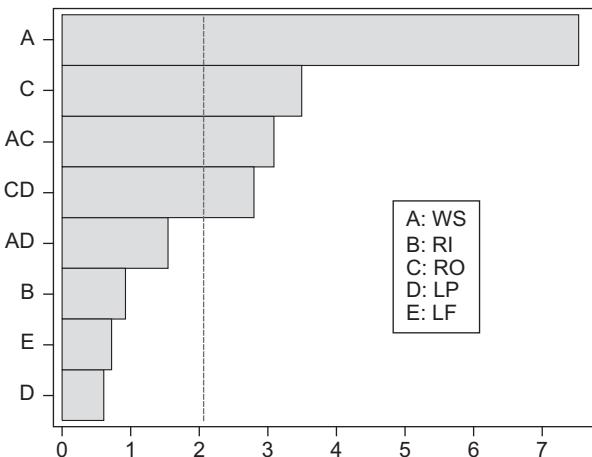
Term	Effect	Coefficient
A (WS)	3.819	1.595
B (RI)	0.469	0.235
C (RO)	1.769	0.885
D (LP)	-0.306	-0.153
E (LF)	0.369	0.185
A × C (WS × RO)	1.569	0.785
A × D (WS × LP)	-0.781	-0.391
C × D (RO × LP)	1.419	0.709

The identification of active and real effects is obtained with the help of Pareto and main effect plots. Figs. 9.23 and 9.24 present these. Figs. 9.23 and 9.24 indicate that two main effects (WS and RO) and two interaction effects (WS × RO) and (RO × LP) are found to be statistically significant at 5% significance level. Here significance level is the risk of saying that a factor effect or an interaction is significant when in fact it is not. The main effect and Pareto plots indicate that weld speed is the most active factor effect, followed by ramp out. The interaction between ramp out and laser power is shown in Fig. 9.25. The interaction plot shows that life increases when both laser power and ramp out are at high level.

It is quite interesting to note that although laser power on its own has very little impact on the life of core tubes, its effect on life is dependent on ramp out



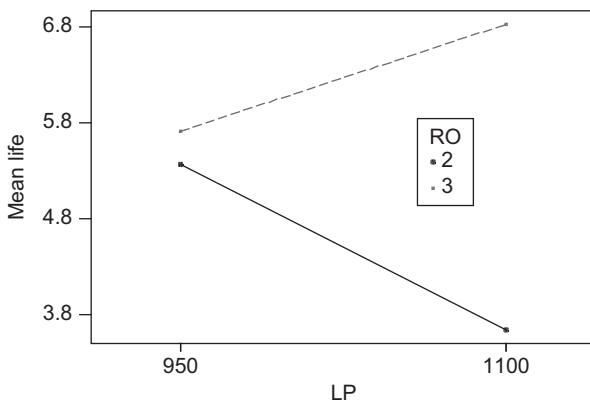
**Figure 9.23** Main effects plot for the experiment.



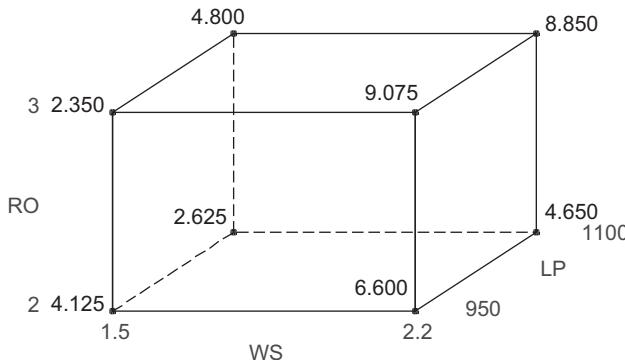
**Figure 9.24** Pareto plot of effects affecting mean life.

(Fig. 9.25). In order to observe the effect of three factors on the mean life of core tubes, a cube plot is constructed (Fig. 9.26). It is quite apparent in the cube plot that a high level of weld speed will yield a higher life. Similarly, it is fair to say that life increases with increase in ramp out.

The next step in the analysis was to identify the factors which influence fatigue life variability (Sirvanci and Durmaz, 1993). To analyse variability, SD was calculated at each ED point. As log(SD) values will tend to be normally distributed, a log transformation on SD values was essential. Table 9.23 displays the log(SD) values corresponding to each experimental trial condition. Due to insufficient degrees of freedom for the error term, it was decided to pool those effects with low



**Figure 9.25** Interaction plot – ramp out  $\times$  laser power.



**Figure 9.26** Cube plot of factors with mean life of core tubes.

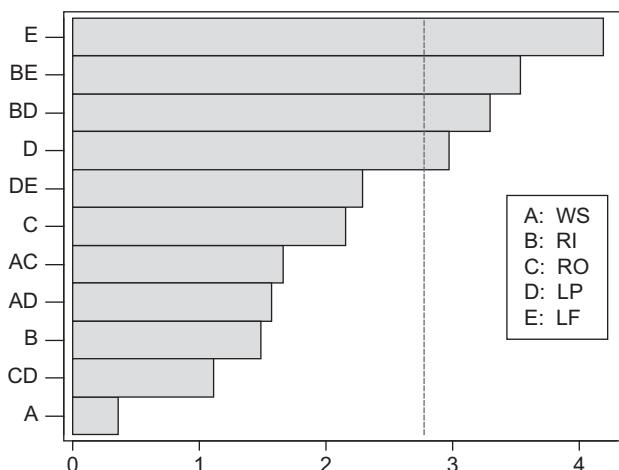
magnitude. The Pareto chart (Fig. 9.27) shows that the main effects lens position and laser power are significant at 5% significance level. Similarly, it was also found that the interactions between lens focus and ramp in and laser power and ramp in were significant. Similar results can be obtained using analytical tools such as ANOVA. For more information on the ANOVA, readers are encouraged to refer to Montgomery's book, *Design and Analysis of Experiments*. Having identified the process parameters which influence the mean and variability, the next stage was to determine the optimal process parameter settings that would maximise the core tube life with minimum variability.

#### 9.2.7.5 Determination of the optimal process parameter settings

The selection of optimal settings of the process parameters depends a great deal on the objectives to be achieved from the experiment and the nature of the problem to

**Table 9.23** Table of log(SD) Values.

Trial No.	log (SD)
1	0.394
2	-0.247
3	-0.247
4	0.381
5	-0.037
6	0.341
7	0.368
8	-0.851
9	-0.247
10	-0.674
11	0.418
12	-0.037
13	-0.851
14	-0.548
15	-0.851
16	0.264

**Figure 9.27** Pareto plot of effects influencing variability.

be tackled. For the present study, the engineering team within the company want to discover the settings of the key process parameters that will not only maximise the core tube mean life but also reduce variability in core tube life so that more consistent and reliable products can be produced by the manufacturer (Montgomery, 1992).

To identify the process parameter settings which maximise the life, it was important to select the best levels of those parameters which yield maximum core tube

life. This information can be easily generated from the main effects plot (Fig. 9.23). The interaction plot between ramp out (C) and laser power (D) suggests that (Fig. 9.25) the core tube life is maximum when the laser power is set at its high level. Therefore the optimal settings for maximising the core tube life are as follows:

- Weld speed (A) – level 2 (2.2 rev./s)
- Ramp out (C) – level 2 (3.0 s)
- Laser power (D) – level 2 (1100 W)

In essence, the maximum core tube life was achieved only when all of the above process parameters were kept at high levels.

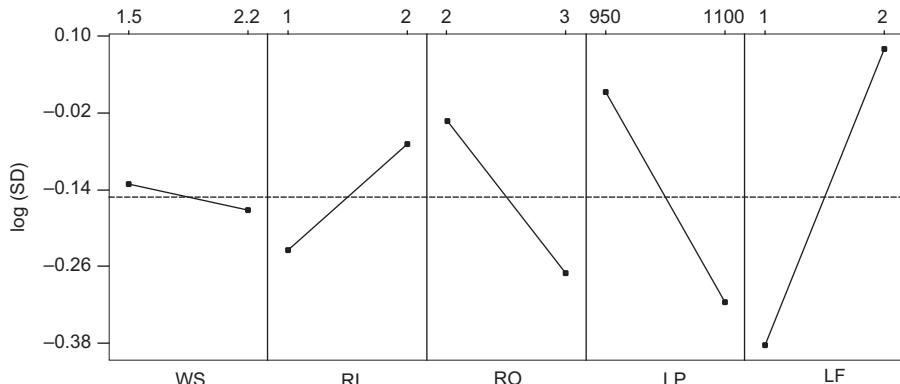
In order to determine the best levels of process parameters which yield minimum variability, it was decided to construct a main effects plot on variability (using  $\log(\text{SD})$  as the response of interest). Fig. 9.28 presents the main effects plot of process parameters for variability ( $\log(\text{SD})$ ) as the response).

The optimal settings for the significant process parameters which influence variability in core tube life are as follows:

- Ramp in (B) – Level 1 (1 s)
- Laser power (D) – Level 2 (1100 W)
- Lens focus (E) – Level 1 (Position 1)

As there was no trade-off in the levels of the process parameters, the final settings were determined by combining the above two. The final optimal condition is therefore given by

- Weld speed (A) – Level 2 (2.2 rev./s)
- Ramp in (B) – Level 1 (1 s)
- Ramp out (C) – Level 2 (3.0 s)
- Laser power (D) – Level 2 (1100 W)
- Lens focus (E) – Level 1 (Position 1)



**Figure 9.28** Main effects plot on variability ( $\log(\text{SD})$ ).

### **9.2.7.6 Confirmation trials**

Confirmation trials were performed in order to verify the results of the analysis. Five samples were produced at the optimal condition of the process. The mean life of the core tubes and tube life variance were 10.25 and 0.551, as opposed to 6.75 and 1.6 at the normal production settings in the company. This showed an improvement of over 50% in the life of the core tubes and a 65% reduction in core tube life variability.

### **9.2.7.7 Significance of the study**

Due to the significant reduction in process variability, the costs due to poor quality such as scrap, rework, replacement, re-test etc. were reduced by over 20%. This shows a dramatic improvement in the performance of the process and thereby more consistent and higher quality core tubes could be produced using the optimised process. The engineering team within the company are now well aware of the dos and don'ts of ED. Moreover, the awareness of DoE that has been established within the organisation has built confidence among the engineers and among front-line workers in other areas facing similar difficulties. The author believes that it is important to teach a case study of this nature in order to learn the common pitfalls when applying DoE to a specific problem. The experiment also helped the engineering team within the company to understand not only the fundamental mistakes they were making but also the key features of making an industrial experiment a successful event.

## **9.2.8 Optimisation of a spot welding process using DoE**

This case study presents the application of DoE to a spot welding process in order to discover the key process parameters which influence the tensile strength of welded joints. Spot welding is the most commonly used form of resistance welding. The metal to be joined is placed between two electrodes, pressure applied and a current turned on. The electrodes pass an electric current through the work pieces. As the welding current is passed through the material via the electrodes, heat is generated, mainly in the material at the interface between the sheets. As time progresses, the heating effect creates a molten pool at the joint interface which is contained by the pressure at the electrode tip. Once the welding current is switched off, the molten pool cools under the continued pressure of the electrodes to produce a weld nugget.

The heat generated depends on the electrical resistance and thermal conductivity of the metal, and the time at which the current is applied. The electrodes are held under a controlled pressure or force during the welding process. The amount of pressure affects the resistance across the interfaces between the work pieces and the electrodes. If the applied pressure is too low, weld splash (a common defect in spot resistance welding) may occur.

There are three stages to the welding cycle: squeeze time, weld time and hold time. The squeeze time is the period from when the pressure is applied until the current is turned on. The weld time is the duration of the current flow. If the weld current is high, this may again lead to weld splash. The hold time is the time for which the metal is held together after the current is stopped.

As part of initial investigation and because no experiments have been performed on the spot welding machine before, the engineers within the company were more interested in understanding the process itself, including the key welding process parameters, which affect the mean strength of the weld, and the process parameters, which affect the variability in weld strength.

The following objectives therefore were set by a team of people within the company consisting of quality improvement engineers, a process manager, two operators, a production engineer and a DoE facilitator who is an expert in the subject matter. The objectives of the experiment were as follows:

1. to identify the key welding process parameters which influence the strength of the weld and
2. to identify the key welding process parameters which influence variability in weld strength.

**Table 9.24** presents the list of process parameters along with their levels used for the experiment. As part of the initial investigation, it was decided to study the process parameters at 2-levels. Owing to the non-disclosure agreement between the company and the author, certain information relating to the case study (process parameters, levels and original data) cannot be revealed. However, the data have not been manipulated or modified as a consequence of this agreement.

### 9.2.8.1 *Interactions of interest*

Further to a thorough brainstorming session, the team has identified the following interactions of interest:

1. A × B
2. B × D
3. C × D
4. D × E

**Table 9.24** List of process parameters used for the experiment.

Process parameter	Label	Low-level setting	High-level setting
Stroke distance	A	-1	1
Weld time	B	-1	1
Electrode diameter	C	-1	1
Welding current	D	-1	1
Electrode pressure	E	-1	1

The quality characteristic of interest for this study was weld strength measured in kilograms. Having identified the quality characteristic and the list of process parameters, the next step was to select an appropriate design matrix for the experiment. The design matrix shows all the possible combinations of process parameters at their respective levels. The choice of design matrix or experimental layout is based on the degrees of freedom required for studying the main and interaction effects (Bullington et al., 1993). The total degrees of freedom required for studying five main effects and four interaction effects is equal to 9. A  $2^{(5-1)}$  fractional factorial design was selected to study all the main and interaction effects stated above. The degrees of freedom associated with this design is 15 (i.e. 16 – 1).

In order to minimise the effect of noise factors induced into the experiment, each trial condition was randomised. Randomisation is a process of performing experimental trials in a random order in which they are logically listed. The idea is to evenly distribute the effect of noise (factors which are difficult or expensive to control under standard production conditions) across the total number of experimental trials. Moreover, each design point was replicated five times to improve the efficiency of experimentation. The purpose of replication is to capture variation due to machine set-up, operator error etc. Moreover, replications generally provide estimates of error variability for the factors (or process parameters). Table 9.25 illustrates the results of the experiment.

#### 9.2.8.2 Statistical analysis of experimental results

Statistical analysis and interpretation of results are imperative steps for DoE to meet the objectives of the experiment. A well-planned and well-designed experiment will

**Table 9.25** Results of the experiment.

Run	A	B	C	D	E	Mean weld strength
1	-1	-1	-1	-1	-1	5.4
2	1	-1	-1	-1	1	20.4
3	-1	1	-1	-1	1	243.0
4	1	1	-1	-1	-1	109.0
5	-1	-1	1	-1	-1	48
6	1	-1	1	-1	1	104
7	-1	1	1	-1	1	23.6
8	1	1	1	-1	-1	3.40
9	-1	-1	-1	1	-1	763
10	1	-1	-1	1	1	750
11	-1	1	-1	1	1	553
12	1	1	-1	1	-1	279
13	-1	-1	1	1	-1	462
14	1	-1	1	1	1	610
15	-1	1	1	1	1	747
16	1	1	1	1	-1	576

provide effective and statistically valid conclusions. The first step in this particular analysis was to identify the factors and interactions which influence the mean weld strength. The results of the analysis are shown in Fig. 9.29. The Pareto plot (Fig. 9.29) shows that main effects D (welding current) and E (electrode pressure) have significant influence on mean weld strength. Moreover, two interactions A  $\times$  B (stroke distance  $\times$  weld time) and B  $\times$  D (weld time  $\times$  welding current) are also found to be statistically significant. Main effects A, C and B did not have any influence on the mean weld strength.

In order to analyse the strength of the interaction among the process parameters, such as stroke distance, weld time and welding current, it was decided to construct interaction graphs (Figs. 9.30 and 9.31).

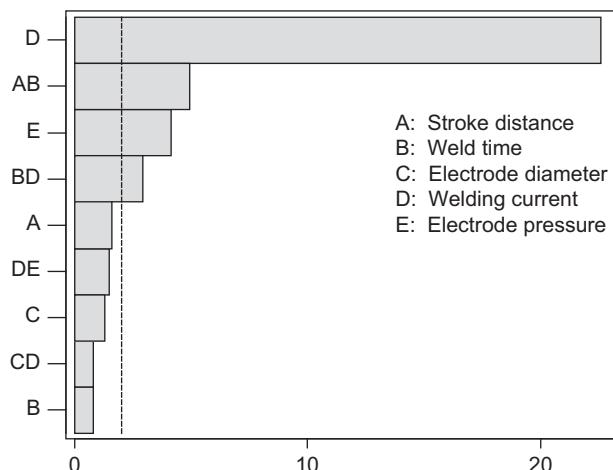


Figure 9.29 Pareto plot of main and interaction effects from the experiment.

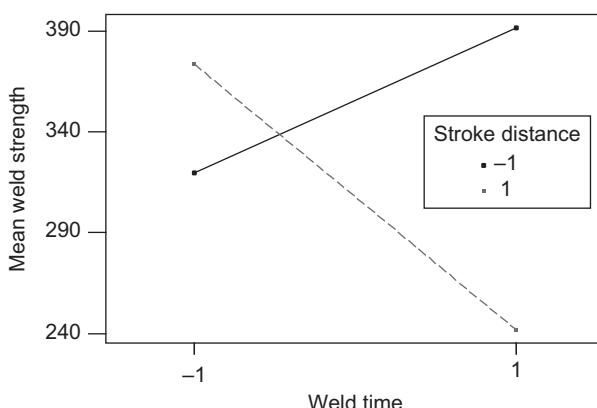
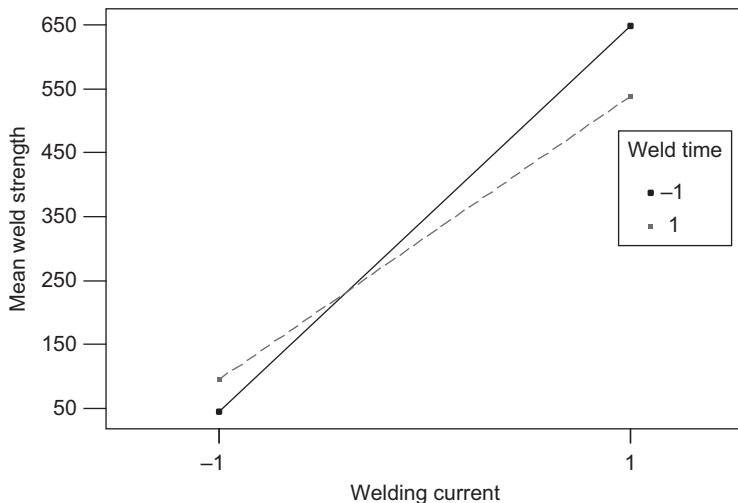


Figure 9.30 Interaction graph for weld time and stroke distance.



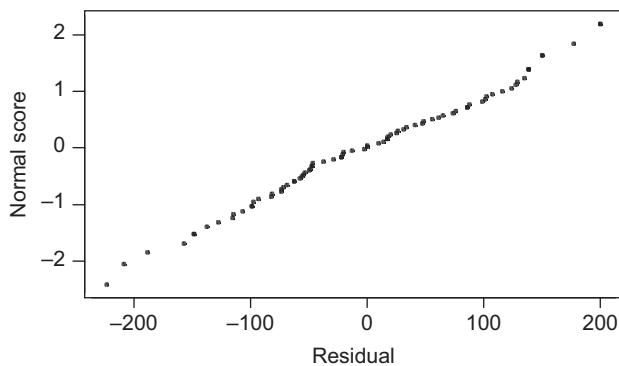
**Figure 9.31** Interaction graph for welding current and weld time.

[Fig. 9.30](#) shows that high weld time and low stroke distance yield the highest weld strength, whereas high weld time and high stroke distance yield the lowest weld strength. Similarly, [Fig. 9.31](#) indicates that high welding current and low weld time yield the highest weld strength. Here, there is a trade-off in the selection of factor levels for weld time. However, further studies showed that the combination of high weld time and high welding current produces the highest weld strength.

One of the assumptions experimenters generally make in the analysis part is that the data come from a normal population. In order to verify that the data follow a normal distribution in this instance, it was decided to construct an NPP of residuals (residual = observed value – predicted value). [Fig. 9.32](#) presents an NPP of residuals which clearly indicates that all the points on the plot come close to forming a straight line. This implies that the data are fairly normal.

The next step in the analysis was to identify the key process parameters which affect variability in weld strength. To analyse variability, SD was calculated at each experimental trial condition ([Logothetis and Wynn, 1989](#)). As  $\ln(\text{SD})$  values will tend to be normally distributed, a log transformation was carried out on the data. The results are given in [Table 9.26](#).

In order to identify which of the factors or interactions have a significant impact on variability in weld strength, it was decided to construct a Pareto plot ([Fig. 9.33](#)). The graph shows that only welding current has a significant impact on variability in the strength of the weld. In order to generate adequate degrees of freedom for analysing variability, pooling was performed (by combining the degrees of freedom associated with those effects which are comparatively low in magnitude). In order to support the procedure of pooling, an NPP of effects was also constructed. It was interesting to note that variability in the strength was minimum when the welding



**Figure 9.32** NPP of residuals. *NPP*, Normal probability plot.

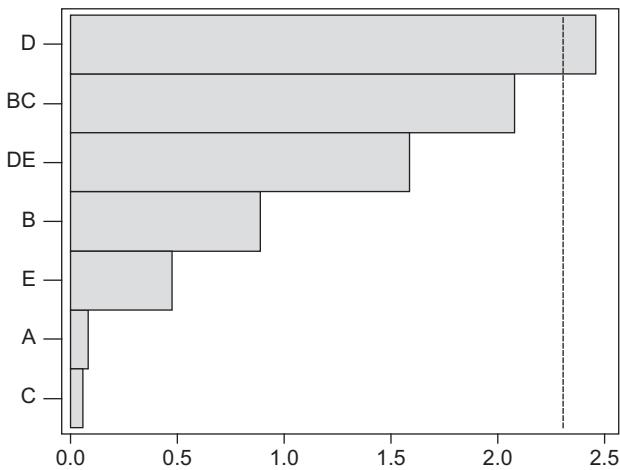
**Table 9.26**  $\ln(\text{SD})$  values from the experiment.

Trial no.	$\ln(\text{SD})$
1	1.086
2	2.961
3	3.642
4	3.713
5	4.008
6	3.481
7	3.379
8	1.329
9	4.011
10	3.379
11	3.931
12	4.937
13	3.646
14	3.560
15	4.000
16	4.070

current was set at a low level. As there was a trade-off in one of the factor levels (factor D), it was decided to perform the loss-function analysis promoted by Dr. Taguchi.

### 9.2.8.3 Loss-function analysis for larger-the-better characteristics

This analysis is used when there is a trade-off in the selection of process parameter levels. As the performance characteristic of interest in this case is the strength of the weld, it was decided to perform the loss-function analysis for larger-the-better



**Figure 9.33** Pareto plot of effects on variability in weld strength.

(LTB) performance characteristics. The average loss function for LTB quality characteristic is given by

$$L = k \left[ \frac{1}{\bar{y}^2} \right] \left\{ 1 + \left( \frac{3s^2}{\bar{y}^2} \right) \right\} \quad (9.2)$$

where  $k$  = cost constant or quality loss coefficient,  $\bar{y}$  = mean performance characteristic (i.e. mean strength),  $SD$  = standard deviation in the strength of the weld corresponding to each trial condition,  $L$  = average loss associated with the performance characteristic per trial condition.

Eq. (9.2) is applied to all 16 trial conditions. It was found that trial condition 10 yields minimum loss. For trial condition 10, factor D was set at high level and therefore the high-level setting for D was chosen for the model development and prediction of weld strength.

#### 9.2.8.4 Significance of the study

The purpose of this chapter is to illustrate an application of DoE to a spot welding process. The objectives of the experiment in this study were twofold. The first objective was to identify the critical welding process parameters which influence the strength of the weld. The second objective was to identify the process parameters which affect variability in the weld strength. A trade-off in one of the factor levels (factor D) was observed. This problem was rectified with the use of Taguchi's loss-function analysis. The strength of the weld was increased by around 25%. The next phase of the research is to perform more advanced methods such as RSM by adding centre points and axial points to the current design. The results of

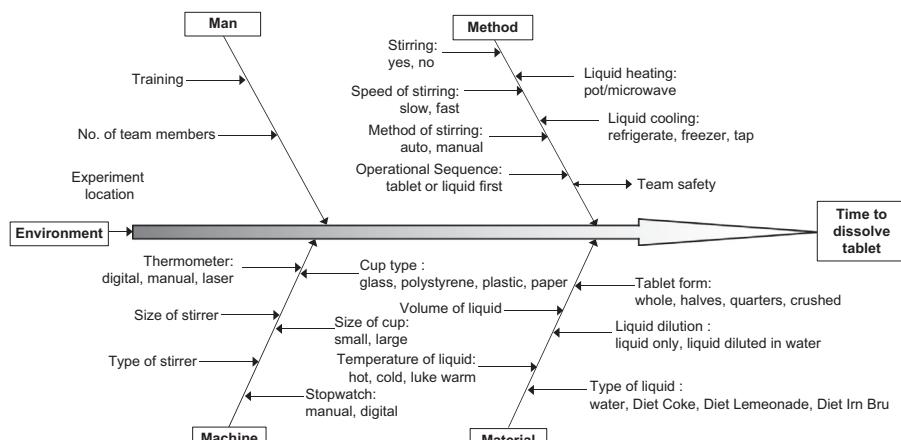
the experiment have stimulated the engineering team within the company to extend the applications of DoE in other core processes for performance improvement and variability reduction activities.

### 9.2.9 DoE applied to a fizz-flop experiment

The purpose of this experiment was to determine which factors influence the mean response and variation of response of an effervescent pain relief tablet (hereafter referred to as a *tablet*) being dissolved in a liquid. The time taken to completely dissolve one tablet will be measured and recorded in seconds. This experiment was given out to a group of students pursuing a Masters Programme on Lean Six Sigma at the University of Strathclyde, Scotland.

By means of a brainstorming session, the team (consists of five students) considered potential factors and how they might affect the time needed to dissolve a single tablet. As this is a commercially available product which is taken orally, process parameters were limited to those which would not affect consumer safety. As the team members had no previous experience of the process under investigation, we used six tablets to help with the brainstorming. Fig. 9.34 illustrates the Cause and Effect diagram produced during the brainstorming. Team discussions led to further consideration of the factors which were considered to affect the response. Table 9.27 gives the final output which was to be used in the ED. This included the following information:

- *Factor*: process parameters selected to be considered during the experiment.
- *Possible levels*: levels selected to give as wide a scope as reasonably possible.
- *Group thinking*: the thoughts of the team with regards to factors and why specific levels were chosen.
- *Considered for experiment*: the 2-levels chosen for each factor.
- *Considered as key factor*: the thoughts of the team prior to carrying out the experiments as to whether a particular factor would influence the response.



**Figure 9.34** Cause and Effect diagram.

**Table 9.27** Final output from brainstorming.

Factor	Possible levels	Group thinking	Chosen for experiment	Considered as key factor in response
Type of cup	Paper	No chemical reaction with cup material is expected in either case. Possible difference in heat loss characteristics, particularly with hot water. Plastic and glass were chosen as these allowed good visibility of the table during dissolving process.	✗	No
	Plastic		✓	
	Polystyrene		✗	
	Glass		✓	
Size of cup	1/2 pint	The size of cup is not expected to affect the response but must be able to hold the specified volume and temperature of liquid.	✓	No
	Pint		✓	
Volume of liquid	4 fl. oz.	4 fl. oz. is the supplier-recommended volume. Additional volume may allow a greater chemical reaction in the creation of carbon dioxide and therefore speed up the dissolving process.	✓	Possible
	8 fl. oz.		✓	
Liquid temperature	Cold (40°F)	The dissolving process is likely to be affected by significant change in water temperature, with higher temperatures speeding up the time to dissolve a tablet.	✓	Yes
	Hot (175°F)		✓	
Type of liquid	Water	The supplier recommends using water as the solvent. Using a carbonated soft drink as an additive could have two effects: (1) lower pH value which may speed up response time of the chemical reaction and (2) increase carbon dioxide content which may increase time to dissolve a tablet. Diet Lemonade was chosen as it was found to be easier to view the tablet during the experiments.	✓	Yes

Tablet size	Diet Lemonade		✓ ✗ ✗ ✓	Yes
	Diet Irn Bru Diet Coke Full			
Operational sequence	Halves Quarters Crushed		✗ ✓ ✗ ✓	No
	Liquid then tablet Tablet then liquid			
Stirring	No		✓ ✓	Yes
	Yes			

### 9.2.9.1 Hypotheses

Prior to the experiment, hypotheses were considered by every team member regarding which factors would make the tablet dissolve the fastest, as this would provide evidence as to what potential outcomes were perceived to happen. The hypotheses perceived prior to experimentation were the following:

- Mr. A – hot water and stirring whilst dissolving
- Mr. B – hot water and the tablet being crushed prior to being put in water
- Ms. C – cold water and a wide-rimmed cup
- Ms. D – hot water and a glass
- Mr. E – cold sparkling water with salt added to the solution.

The team consisted of four people who performed all aspects of the experiment without additional resources. [Table 9.28](#) lists materials and resources that were used during the experiment.

### 9.2.9.2 Experimental plan

The output of the brainstorming session suggested eight possible factors which could affect the response (i.e. time to dissolve tablet). It was decided to study each

**Table 9.28** List of available materials.

Description	Quantity	Purpose/comment
Measuring jug (0–16 fl. oz.)	1	To calibrate the amount of liquid used in each experiment
Thermometer (manual)	1	To measure the liquid temperature
Stopwatch	1	To measure the time to dissolve the tablet during each experiment
Effervescent pain relief tablets	30	6 × tablets were used for pre-experiment investigation 24 × tablets were used during the experiments
Plastic cup (1/2 pint)	6	To hold hot and cold liquids and have the capacity to hold the desired volume levels
Plastic cup (pint)	6	
Glass cup (1/2 pint)	6	
Glass cup (pint)	6	
Diet Lemonade	6 L	Liquids to be chilled to 40°F and heated to 175°F based on experimental design
Water	6 L	
Pan	1	To heat liquid for high-level temperature experiments
Measuring spoon (1 tsp.)	1	To stir solution for appropriate experiments

factor at 2-levels in the initial part of the investigation. For an FFE, this would require 256 experiments or trials (e.g.  $2^8 = 256$ ). As the first objective of the experiment was to determine the main factors which affected the mean response, the team decided to carry out a screening experiment. Furthermore, as the second objective was to determine which factors affected the variability of response, it was decided to replicate each trial condition. Based on the these objectives, the limited availability of tablets, the relatively low cost of the materials and the time required to carry out the experiments, the team decided to carry out a PB-12 trial experiment with two replicates. It was also decided that the experiments would be randomised in order to distribute the random effects of noise (if any).

A PB-12 experiment allows for up to 11 factors at 2-levels to be considered and offers 11 degrees of freedom. As we were only considering eight factors, this allowed us to create 3 degrees of freedom for the error term.

The measurement system to be used by the team was agreed and consisted mainly of the following:

- liquid volume measured using a measuring jug,
- liquid temperature measured by an analogue thermometer and
- time to dissolve (response) measured by a stopwatch.

As these were all manual and open to judgement and error, the capability and stability of the measurement system could not be guaranteed. [Table 9.29](#) gives the final list of factors, with their low and high levels, to be used during the experimentation.

The following information was entered into Minitab along with the following:

- Number of experiments = 12
- Experimental method = Plackett–Burman
- Replicates = 2
- Randomisation = Yes

[Table 9.30](#) presents the P–B experimental layout used for the experiment.

**Table 9.29** List of factors and their respective levels.

Factor ID	Description	Low level (-)	High level (+)
A	Type of cup	Plastic	Glass
B	Cup size	1/2 pint	Pint
C	Volume of liquid	4 fl. oz.	8 fl. oz.
D	Liquid temperature	40°F	175°F
E	Type of liquid	Water	Diet Lemonade
F	Tablet size	Quarters	Full
G	Operational sequence	Tablet then liquid	Liquid then tablet
H	Stirring	No	Yes

**Table 9.30** Experimental layout for the fizz-flop experiment.

Exp. no.	Factor							
	A	B	C	D	E	F	G	H
1	-	+	+	-	+	-	-	-
2	-	+	+	+	-	+	+	-
3	+	-	+	+	-	+	-	-
4	+	-	-	-	+	+	+	-
5	-	+	+	+	-	+	+	-
6	-	-	-	+	+	+	-	+
7	-	-	-	+	+	+	-	+
8	+	+	+	-	+	+	-	+
9	+	+	-	+	-	-	-	+
10	+	+	-	+	-	-	-	+
11	-	-	+	+	+	-	+	+
12	-	+	+	-	+	-	-	-
13	+	+	-	+	+	-	+	-
14	-	+	-	-	-	+	+	+
15	+	+	+	-	+	+	-	+
16	+	-	+	+	-	+	-	-
17	+	-	-	-	+	+	+	-
18	-	-	-	-	-	-	-	-
19	+	+	-	+	+	-	+	-
20	+	-	+	-	-	-	+	+
21	+	-	+	-	-	-	+	+
22	-	+	-	-	-	+	+	+
23	-	-	+	+	+	-	+	+
24	-	-	-	-	-	-	-	-

### 9.2.9.3 Execution of experiment

To minimise the effect of manual error during the experiments, the following approach was taken:

- Person 1: prepared the cup and liquid for each experiment and added tablet to experiments with in the order of *Liquid then Tablet* and
- Person 2: stirred the solution for appropriate experiments and measured time to dissolve each tablet (response) with stopwatch.

This ensured that Person 1 would be responsible for the measurement of the two quantitative characteristics (liquid volume and temperature) and Person 2 would be responsible for the measurement of the response time. This was expected to reduce the level of operator error, as this was not considered a key factor in our experiments.

The experiments were set up, executed and recorded on an individual basis, based on the randomised design stated by Minitab.

The 40°F liquids were refrigerated and the 175°F liquids were heated in a pan in advance of the experiments.

#### 9.2.9.4 Data collection, analysis and interpretation

##### 9.2.9.4.1 Data collection

The 24 experiments were conducted and the responses (time to dissolve each tablet) were recorded as given in [Table 9.31](#).

##### 9.2.9.4.2 Analysis of data

The first part of the analysis was to determine which of the factors in the experiment had the highest impact on the response. For simplicity reasons, it was decided to construct a main effects plot ([Fig. 9.35](#)). [Fig. 9.35](#) clearly shows that all factors apart from liquid temperature do not greatly affect the response. Obviously, the graph shows that when liquid temperature increased from 40°F to 175°F, the time taken for the tablet to dissolve is reduced significantly. In order to determine the statistical significance, it was decided to use both a normal plot and a Pareto plot so that valid and robust conclusions could be drawn from the experiment. Both plots ([Figs. 9.36 and 9.37](#)) suggested that liquid temperature is the only factor which appeared to be statistically significant at the 5% significance level.

The second phase of the analysis was focused on the factors which influence the response variability, that is variability in the time taken for the tablets to dissolve. In order to analyse variability, we have computed the SD at each ED point ([Table 9.31](#)). An NPP of effects for variability, In(SD), was constructed. The graph ([Fig. 9.38](#)) has shown that both liquid temperature and liquid type have an impact on the response variability. It was also observed from further analysis that higher liquid temperature gave less variability in response and Diet Lemonade provided the team with minimal variability in response compared to water.

##### 9.2.9.4.3 Experimental conclusions

From the experiments carried out and analysis of the results, the following conclusions were drawn by the team:

- Only factor D (liquid temperature) has a significant effect on the mean time to dissolve a tablet.
- Factor D (liquid temperature) and factor E (liquid type) have a significant effect on the variability of time needed to dissolve a tablet.
- All other factors can be set at economical or customer-defined levels as they do not influence either the mean time or variability of time needed to dissolve a tablet.
- Interactions between factors were not considered and could be included in further rounds of experimentation.

##### 9.2.9.4.4 Key lessons learned

*Mr. A:* This exercise confirmed my view that DoE is an extremely powerful tool within Six Sigma. We carried out only a basic screening exercise but I will pursue further opportunities to learn and practice further DoE with a view to expanding my knowledge and understanding and introducing it within my workplace.

**Table 9.31** Results of the P-B 12 experiment with response values.

Run order R1/R2	A Cup type	B Cup size	C Volume of liquid (fl.oz.)	D Liquid temperature (°F)	E Liquid type	F Tablet size	G Operational sequence	H Stirring	Response (s)		Analysis		
									R1	R2	Mean	SD	In (SD)
1/12	Plastic	1	8	40	Diet Lemonade	Quarters	Tablet then liquid	No	109.84	90.00	99.92	14.03	2.64
2/5	Plastic	1	8	175	Water	Whole	Liquid then tablet	No	19.94	24.69	22.32	3.36	1.21
3/16	Glass	0.5	8	175	Water	Whole	Tablet then liquid	No	19.34	22.04	20.69	1.91	0.65
4/17	Glass	0.5	4	40	Diet Lemonade	Whole	Liquid then tablet	No	91.50	76.97	84.24	10.27	2.33
6/7	Plastic	0.5	4	175	Diet Lemonade	Whole	Tablet then liquid	Yes	16.09	17.56	16.83	1.04	0.04
8/15	Glass	1	8	40	Diet Lemonade	Whole	Tablet then liquid	Yes	92.75	70.10	81.43	16.02	2.77
9/10	Glass	1	4	175	Water	Quarters	Tablet then liquid	Yes	17.78	14.94	16.36	2.01	0.70
11/23	Plastic	0.5	8	175	Diet Lemonade	Quarters	Liquid then tablet	Yes	17.37	16.41	16.89	0.68	-0.39
13/19	Glass	1	4	175	Diet Lemonade	Quarters	Liquid then tablet	No	15.10	16.19	15.65	0.77	-0.26
14/22	Plastic	1	4	40	Water	Whole	Liquid then tablet	Yes	101.60	65.32	83.46	25.65	3.24
18/24	Plastic	0.5	4	40	Water	Quarters	Tablet then liquid	No	111.41	79.38	95.40	22.65	3.12
20/21	Glass	0.5	8	40	Water	Quarters	Liquid then tablet	Yes	81.00	56.62	68.81	17.24	2.85

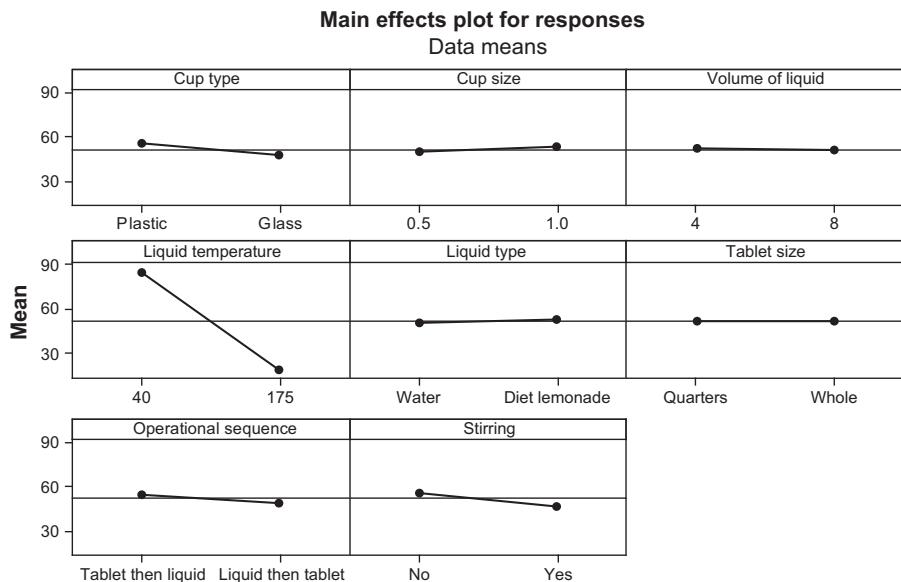


Figure 9.35 Main effects plot for the Fizz-Flop experiment.

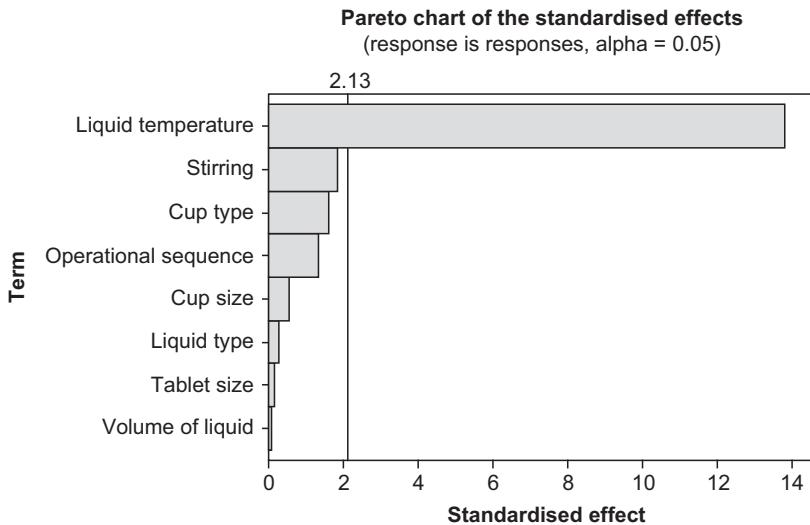
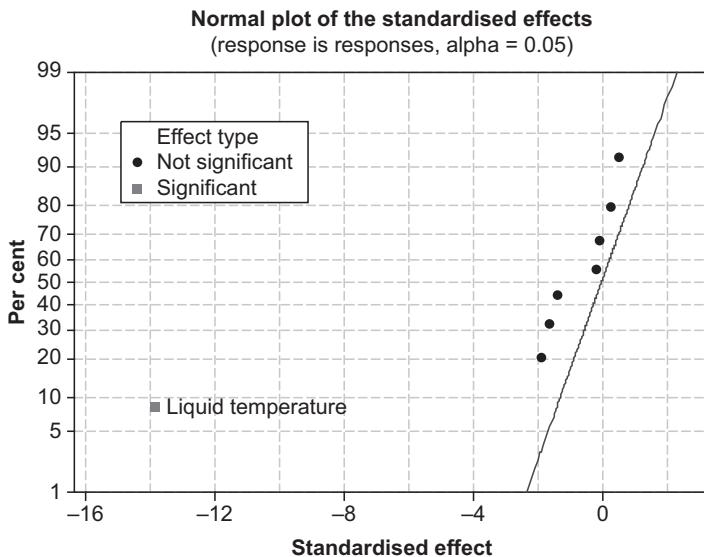
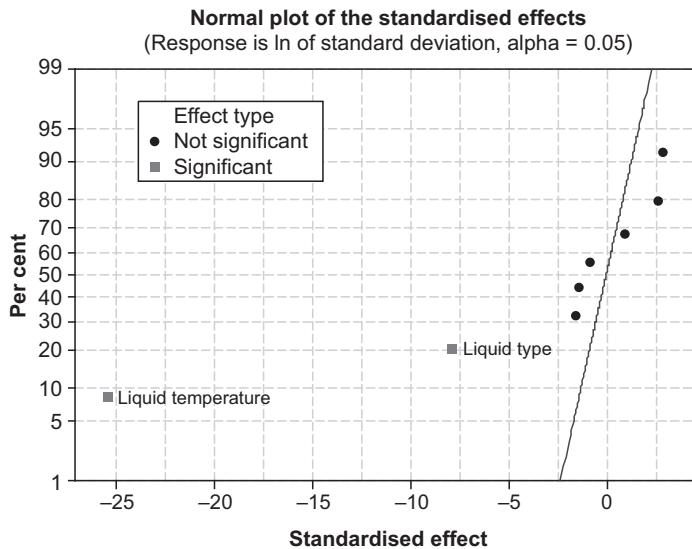


Figure 9.36 Pareto plot of the effects for the Fizz-Flop experiment.

*Mr. B:* DoE was an eye-opener for me. It encouraged me to approach the experiments in a more scientific manner. As an engineer, it has also motivated me to avoid making judgments based on the one-factor-at-a-time approach to experimentation.



**Figure 9.37** NPP of effects (mean response). *NPP*, Normal probability plot.



**Figure 9.38** NPP of effects (response variability). *NPP*, Normal probability plot.

I feel my hypothesis was really out of place; the lesson here was to study more about the actual process that you are going to experiment on. The beauty of this technique was its foundations and solutions based on data and facts. Moreover, this assignment

has been a really interesting team bonding experience, full of enthusiasm and shared knowledge.

*Ms. C:* The use of brainstorming was very important. I believe that had this been an individual exercise a lot of factors would never have come to light.

Understanding and interpreting data and statistics have proved to be a very important aspect in the use of DoE. I would have expected stirring to have a greater effect on the experiment and the result achieved was surprising which suggests that gut instinct is not always correct. This experiment also highlighted how time-consuming and complex experimentation can be, even in a very simple experiment, which explains why companies are so hesitant to conduct designed experiments and also exemplifies how beneficial DoE can be in reducing the size of the experiment but still allowing us to understand the process more efficiently and effectively.

*Ms. D:* ED appears complicated and requires a good grasp of basic statistics in order to successfully apply this technique in real-world scenarios. It is easy to see why it is used so little in industry. Partial knowledge could lead to misinterpretation of results or incorrectly applying the method, leading to frustration and even avoidance of the technique. In my opinion, a good coach is vital in order to steer you through the potential pitfalls.

I believe once you have completed three to four experiments and have gained experience and confidence, this would be a powerful tool. At this particular time, I believe I require further coaching and would benefit from being involved in a complete experiment (screening, characterisation and optimisation) with a good practitioner.

Using a good screening experimentation such as Plackett–Burman, one could save hundreds of pounds and time associated with experimentation. I was unaware of this technique before and the knowledge gained from this experiment will benefit me greatly in the future.

*Mr. E:* This was an extremely interesting experiment to me as the outcome was different to the original thinking of many in the group. This showed how assumptions can be incorrect from the outset. Team working is the key to achieve great results. When everybody has clear roles and responsibilities, the team functions more effectively and achieves the goal in less time than expected.

#### 9.2.9.4.5 Significance of the study

Team work was found to be vital. This exercise has confirmed the importance of having the right people in attendance at the initial brainstorming. Even carrying out a basic screening experiment highlighted the benefits a knowledgeable team would bring. We had no prior knowledge of the product or process under investigation and may have missed some important factors, or deemed them to be unimportant. Our chosen DoE approach did not consider factor interaction and we did not have enough tablets to carry out further testing. We would welcome the opportunity to be involved in further experimentation, particularly for process characterisation and optimisation.

### **9.2.10 DoE applied to a higher education context**

This case study was executed to remove the myth that DoE is purely confined to manufacturing processes. This case study basically encompasses delivery of a course to both undergraduate and postgraduate students in the Faculty of Engineering at a UK-based university. One of the key outputs of teaching is how well the students have learned the topic and how useful and relevant the topics and contents of the course are to them. In the initial phase of the case study, we asked a number of students to identify the potential factors which could influence the teaching performance of the course leader. So the objective of the experiment was to have a bigger picture of the potential factors which influence the teaching performance. It was observed that the teaching performance is dependent on the content style, the presentation style and the way things were delivered during the course leader's allocated time. A thorough brainstorming was performed with students (approximately 10 students representing different cultural backgrounds) and identified the following factors of interest which could influence the content style, the presentation style and the way things were delivered. We have included both undergraduate and postgraduate students for this experiment.

1. Type of presentation – overhead, data projector, board style etc.
2. Class timing – morning session, afternoon session and evening session.
3. People involved in the delivery of the module (number of speakers) – class registrar, involvement of PhD students, people from external organisations etc.
4. Content of presentation – just a general overview of each topic with no specific case studies, specific case studies related to each topic throughout the module.
5. Time for each session allocated – presenter can deliver a lecture with no exercises and discussion or deliver a lecture with some exercises followed by a discussion session.
6. Type of exercise in the class – individual, group etc.
7. Presentation style of the class registrar or module tutor – loud, clear speech; pace of the presentation; tone and pitch; passion/enthusiasm of the speaker etc.
8. Duration of the class – 1, 2, 4 h etc.

*Note: The factors do not include the method of assessment of the module. This case study is primarily focused on the delivery of the class.*

One of the challenges in a service context is the identification of what to measure in order to describe the problem and how to measure the characteristic (Ledolter and Swersey, 2007). Moreover, the performance measurement can be heavily dependent on the person who provides the service. Moreover, variation due to human nature cannot be easily controlled as service processes always have human interventions in the delivery of the service. Each factor was studied at 2-levels in order to minimise the size of the experiment. A total of 25 students (14 postgraduate and 11 undergraduate) participated in the initial investigation. Students were asked to complete a design layout with different combinations of factors provided. The objective here was to rate, on a scale of 1–10, each combination of factor settings in the design layout, with 1 being the least preferred combination in their eyes and 10 being the most preferred combination.

In order to make things simpler, the author will be presenting the results of the experiment on content style and the way things were delivered during the tutor's allocated time (we shall call this time distribution from now onwards). It was found from brainstorming that the content style can be influenced by three factors: class timing, content of presentation and number of speakers. [Table 9.32](#) presents the factors and levels used for the experiment.

It was decided to carry out a  $2^3$  FFE to study all the possible combinations and their respective interactions. For a  $2^3$  FFE, we have three main effects to be evaluated ( $P$ ,  $S$  and  $T$  – see [Table 9.32](#)) and their two-way or second-order interactions such as  $P \times S$ ,  $P \times T$  and  $S \times T$ . Third-order interactions are generally ignored in industrial designed experiments. [Table 9.33](#) presents the experimental layout in coded form for this experiment. All the factor combinations are presented in coded format and this means low levels of all factors are represented by “ $-1$ ” and all the high levels of factors are represented by “ $+1$ .” The last two columns represent the average scores provided by undergraduate (*coded by US*) and postgraduate (*coded by PS*) students. The average scores are based on the number of participants for the experiment (i.e. 11 undergraduate and 14 postgraduate students).

The next part of the case study involves the basic analysis using Minitab software to evaluate the influence of main effects and interaction effects (if any). The effect of a factor is the difference between the average scores at high and low

**Table 9.32** Factors and levels used for the experiment.

Factors	Labels	Low level – represented by $-1$	High level – represented by $+1$
Presentation content	P	General overview of the topic only	Overview plus specific case studies
Number of speakers	S	One speaker	Multiple speakers
Time of delivering the class	T	Morning	Afternoon

**Table 9.33** Experimental layout with the results.

Runs	P	S	T	US (average score)	PS (average score)
1	$-1$	$-1$	$-1$	3.2	6.3
2	$+1$	$-1$	$-1$	5.2	7.8
3	$-1$	$+1$	$-1$	4.3	6.6
4	$+1$	$+1$	$-1$	6.6	8.4
5	$-1$	$-1$	$+1$	6.3	4.8
6	$+1$	$-1$	$+1$	7.0	5.6
7	$-1$	$+1$	$+1$	6.4	6.5
8	$+1$	$+1$	$+1$	8.5	7.2

levels. For example, the average score at a high level of presentation content for US (undergraduate students) is calculated as

$$P_{(+)} = \frac{1}{4}(5.2 + 6.6 + 7.0 + 8.5) = 6.83$$

Similarly, the average score at a low level of presentation content for PS (post-graduate students) is calculated as

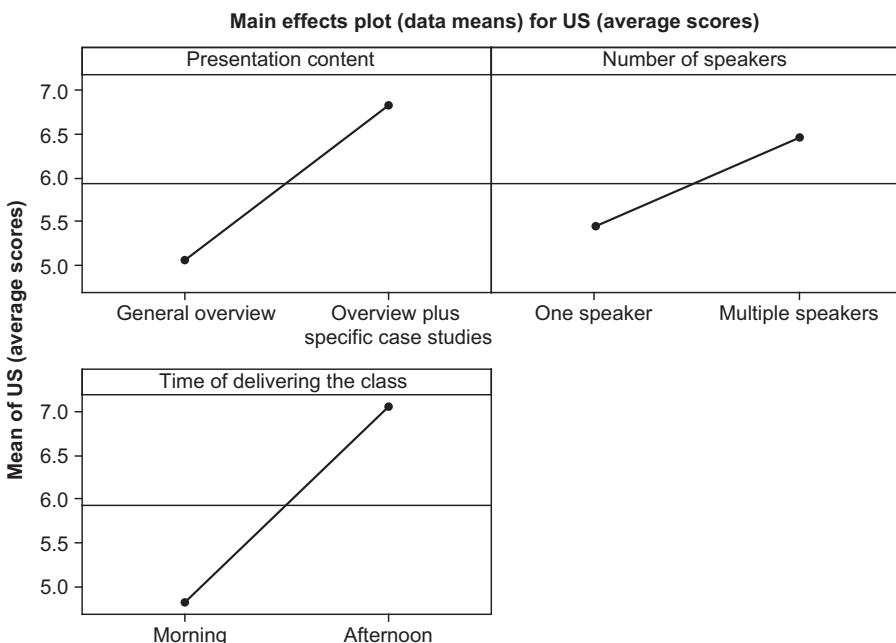
$$P_{(-)} = \frac{1}{4}(3.2 + 4.3 + 6.3 + 6.4) = 5.05$$

$$\text{Effect of presentation content} = 6.83 - 5.05 = 1.78.$$

In a similar manner, we can work out the effects of other factors such as number of speakers and time of delivering the class for both undergraduate and postgraduate students. Fig. 9.39 illustrates the main effects plot for the undergraduate students (US).

We found that the time of delivery and presentation contents are the two most important factors. The best combinations of factors for the content style in the case of US were as follows:

*Presentation content – general overview + specific case studies*



**Figure 9.39** Main effects plot for content style (undergraduate students).

Number of speakers – *multiple speakers*  
 Time of delivering the class – *afternoon*

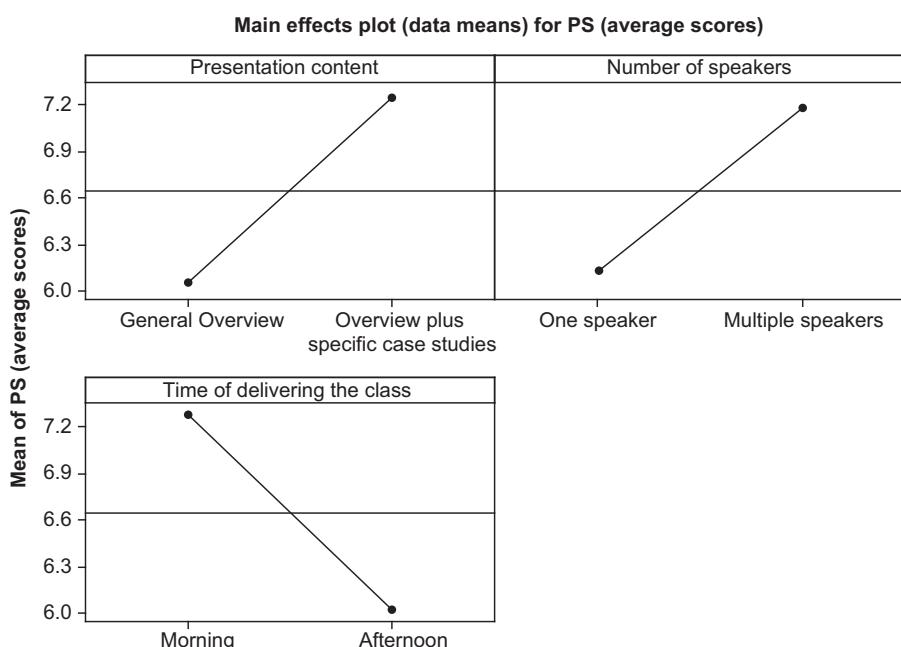
Now we analyse the influence of these factors for the postgraduate students (PS). Fig. 9.40 shows the main effects plot for the PS.

The best combinations of factors for the content style in the case of PS were as follows:

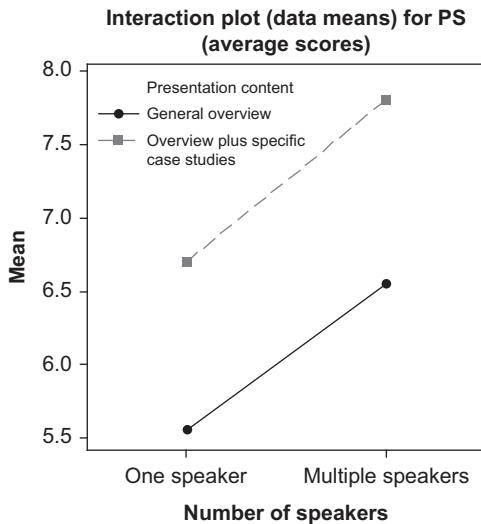
Presentation content – *general overview + specific case studies*  
 Number of speakers – *multiple speakers*  
 Time of delivering the class – *morning*

It was quite interesting to note that the postgraduate students prefer their classes in the morning, whereas undergraduate students prefer their classes in the afternoon.

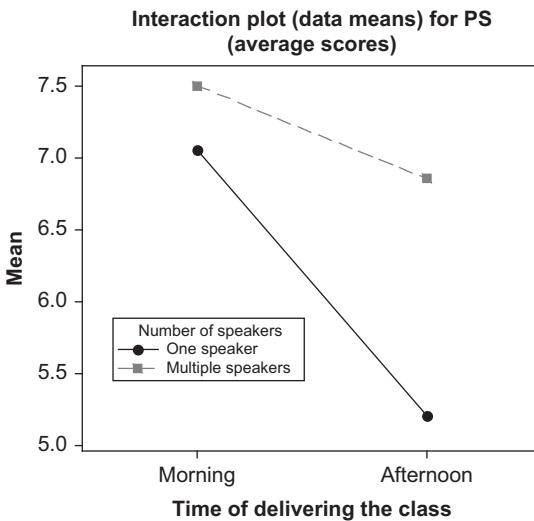
Figs. 9.41 and 9.42 show the interaction plots for content style in the case of PS. Fig. 9.41 shows the interaction between presentation content and the number of speakers. The effect of the number of speakers at different levels of presentation content is the same in this case and this is represented by the parallel lines. In other words, parallel lines are an indication of non-interaction between two factors. Now we analyse the interaction between the number of speakers and the time of delivering the class in the case of PS. Fig. 9.42 shows the interaction plot. The graph



**Figure 9.40** Main effects plot for content style (postgraduate students).



**Figure 9.41** Interaction plot for presentation content and number of speakers.



**Figure 9.42** Interaction plot for number of speakers and time of delivery.

shows that the effect of time of delivering the class at different levels of the number of speakers is not the same. Non-parallel lines are an indication of interaction.

The next part of the case study will be looking into the experimental layout for time distribution (how time has been allocated within the delivery of a class). For convenience purposes, we are going to focus on PS. The time distribution is

dependent upon the length of the lecture, time allocated for exercises (or case studies) and time allocated for discussion after the exercise or case study. This clearly tells us that three independent factors may influence the time distribution. The factors and their levels are given in [Table 9.34](#). Please note that low levels add up to a 1-h lecture session and high levels add up to a 2-h lecture session.

Once the levels and factors were determined, it was decided to design the experimental layout. This is again a  $2^3$  full factorial design where one can study all the main and interaction effects. The average scores along with the layout of the experiment for PS are given in [Table 9.35](#).

[Fig. 9.43](#) shows the main effects plot. The main effects plot indicates that duration of the talk is the most dominant factor as far as postgraduate students are concerned. Further analysis shows that the students prefer a 30-min introduction to the topic in a 1-h lecture. Moreover, the students prefer more time to be spent on the exercises and less time on the discussion. This clearly tells us that the postgraduate students would like to have a good exercise session in the form of a case study followed by a quick discussion after the delivery of a particular topic or subject.

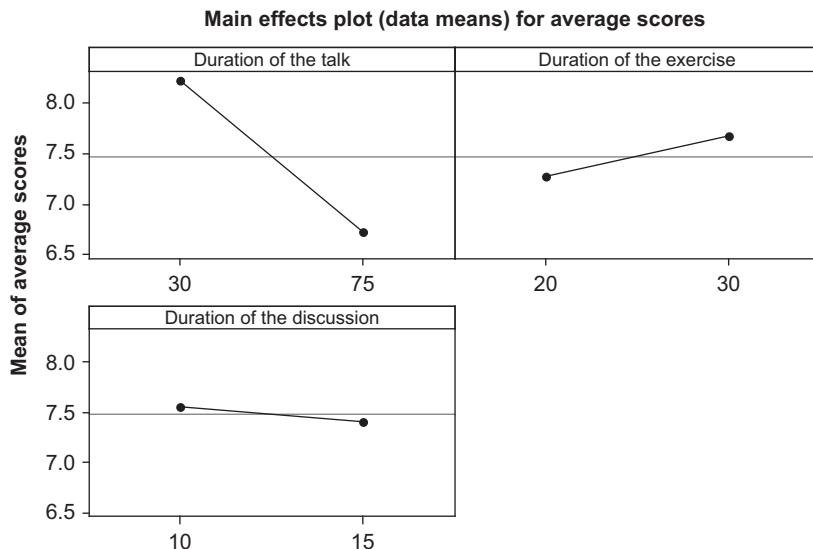
[Fig. 9.44](#) shows the interaction among all the three factors studied. As we can see from [Fig. 9.44](#), there is very little interaction among all the factors due to parallelism properties.

**Table 9.34** Factors and levels for the first experiment.

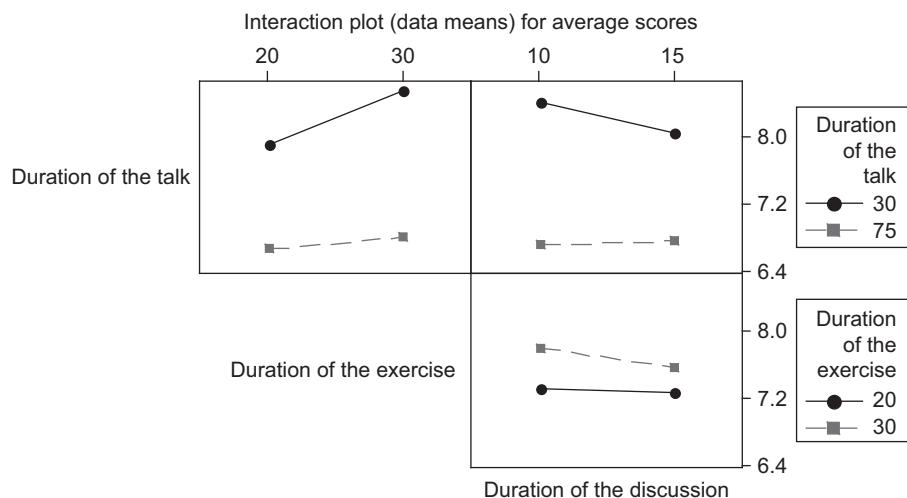
Factors	Labels	Low level – represented by -1	High level – represented by +1
Duration of the talk prior to exercise	T	30 min	75 min
Duration of the exercise	E	20 min	30 min
Duration of the discussion	D	10 min	15 min

**Table 9.35** Experimental layout with the results (coded form).

Runs	T	E	D	Average score (PS)
1	-1	-1	-1	8.2
2	+1	-1	-1	6.4
3	-1	+1	-1	8.6
4	+1	+1	-1	7.0
5	-1	-1	+1	7.6
6	+1	-1	+1	6.9
7	-1	+1	+1	8.5
8	+1	+1	+1	6.6



**Figure 9.43** Main effects plot for time distribution (postgraduate students).



**Figure 9.44** Interaction plot – duration of the talk, duration of the exercise and duration of the discussion.

### 9.2.10.1 Significance of the study

This case study clearly shows the power of DoE and what it can reveal in terms of the students' needs and their choices for a particular course taught at both undergraduate and postgraduate levels. There has been a clear misconception that DoE is

primarily confined to manufacturing processes and that it is not applicable to service and higher education processes. The author is making an attempt to remove this myth and illustrate how DoE can be applied through a simple case study. This case study shows how DoE as a pure manufacturing technique can be extended to a higher education setting. The results of this study were quite an eye-opener for the author in terms of understanding the key factors which influence any process irrespective of the sector. One of the limitations of this study is that the experiment was confined to one course and the number of students that participated in the study was relatively small. The author is planning to extend this study to a number of courses across the university.

### **9.2.11 DoE applied to a transactional process**

A large company was having a problem with receivables. The average age of receivables due was 200 days after delivery of the material. The company had \$130 million that was 30 days or older after receipt by the customer. The cost of this delay was significant. Moreover, the delay was causing a cash flow problem. The several options available that might have further reduced billing time were as follows:

- Bill directly on the invoice.
- Automate the billing and invoicing systems.
- Provide follow-up to the customers by management at 30–45 days by telephone or in writing.
- Contract out the billing department to a professional billing agency.

These options lend themselves to evaluation using a designed experiment. The factors and their levels for the designed experiment are shown below.

#### Factor A – Billing

- Bill directly on the invoice with the shipment (low level – represented by – 1).
- Mail bill from the billing department separately from the shipment (high level – represented by + 1).

#### Factor B – Automation

- Automate the complete billing process with all billing generated automatically on shipment (low level – represented by – 1).
- Maintain the current system in which the generation of billing is automated but the bills and invoices are transmitted and routed in hard copy (high level – represented by + 1).

#### Factor C – Follow up

- Follow up by letter at 45 and 60 days (low level – represented by – 1).
- Follow up by telephone at 45 and 60 days (high level – represented by + 1).

#### Factor D – Contract

- Contract out the billing and follow-up (low level – represented by – 1).
- Keep the billing and follow-up in house (high level – represented by + 1).

In order to minimise the size of the experiment, a half fractional factorial experiment was selected. The trials took place over a 6-month period. **Table 9.36** presents the uncoded design matrix with average age of receivables in the last column. Each

**Table 9.36** Uncoded design matrix with results.

Trial no.	A	B	C	D	Average age of receivables
1	Invoice	Complete	Letter	Contract	50
2	Separate	Complete	Letter	In house	84
3	Invoice	Partial	Letter	In house	58
4	Separate	Partial	Letter	Contract	86
5	Invoice	Complete	Telephone	In house	46
6	Separate	Complete	Telephone	Contract	62
7	Invoice	Partial	Telephone	Contract	51
8	Separate	Partial	Telephone	In house	64

design point was replicated six times to understand the variation in the process. The following objectives were set for this experiment:

- to identify the factors which influence the average age of receivables,
- to determine the optimal settings of factors which yields minimum age of receivables and
- to detect if any interactions exist among the factors under study.

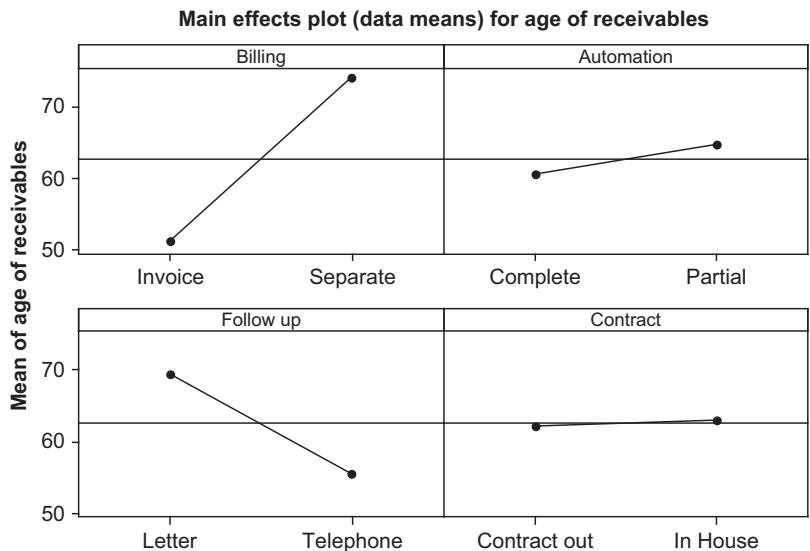
#### 9.2.11.1 Data analysis

The Minitab software system was used to analyse the data. The first objective was to understand what factors affect the average age of receivables. A main effects plot was constructed (Fig. 9.45). The main effects plot clearly indicated that factors A, C and B, in that order, are the most important ones. Factor D has no impact on the age of receivables. This factor can be set at its most economical level. The main effects plot also tells us that factor A must be kept at its low level (directly on the invoice with the shipment), factor B must be kept at its low level (automate the complete billing process) and factor C must be kept at its high level (use telephone as a follow-up).

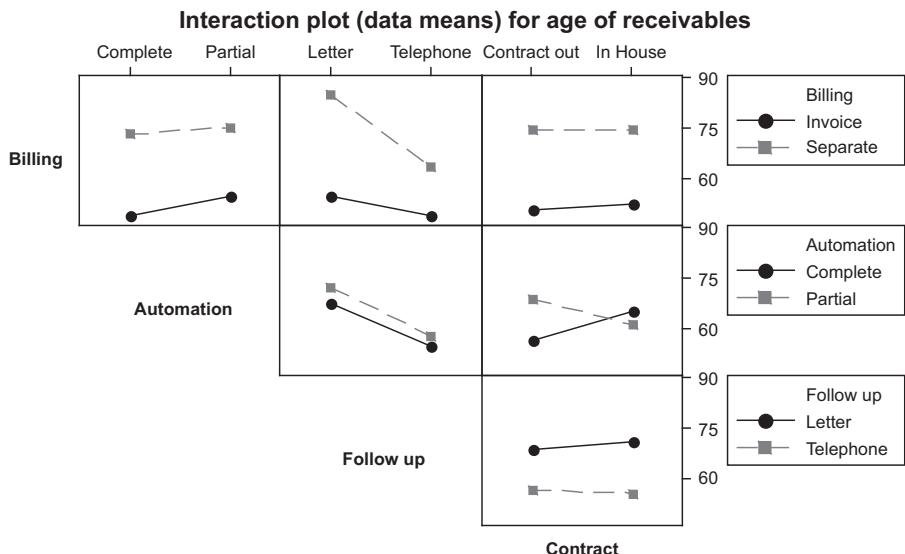
In order to detect any interaction between the factors, an interaction plot was constructed (Fig. 9.46). It is clear from the graph that there is a strong interaction between billing and follow-up as well as between automation and contract. For instance, when we analyse the interaction between billing and follow-up, it was evident that billing directly on the invoice with the shipment and telephone follow-up yields the minimum age of receivables. Similarly, when we analyse the interaction between automation and contract, it was evident that automating the complete billing process with all billing generated automatically on shipment and contracting out the billing and follow-up yield the minimum age of receivables. There were a couple of marginal interactions between factors and there was no interaction between billing and automation or between billing and contract.

#### 9.2.12 DoE applied to a banking operation

This case study is an application of DoE within a banking industry showing how DoE has been useful in improving its application process. The bank was experiencing



**Figure 9.45** Main effects plot for average age of receivables.



**Figure 9.46** Interaction effects plot for average age of receivables.

a 60% reprocessing rate on applications due to incomplete information provided by the customer. A project team was formed to tackle this problem and it was observed that three potential factors might affect a completed application:

1. the type of application

2. how much detail was provided in the instructions
3. whether additional examples were provided.

It was decided to perform an experiment in two locations to understand the application process. The team identified five factors and in order to minimise the size of the experiment, it was decided to study each factor at 2-levels. A fractional factorial experiment ( $2^{(5-1)}$ ) was also executed. The list of factors and their levels are given in [Table 9.37](#).

The response of interest in the case study was the percentage completeness of each application. [Table 9.38](#) gives the results of the experiment. Without performing a scientific approach to experiment, it is difficult to say which factors from the above five are critical to the application process, or which factors are unimportant. Where do we set the factors so that we can achieve the minimum number of errors? A systematic and disciplined approach such as DoE is an extremely powerful tool under these circumstances, as it can help him to understand the process better and in the most efficient manner.

[Fig. 9.47](#) shows the main effects plot. It was quite interesting to note that only two factors appeared to be very important (factor D – whether an example was provided and factor C – how much description was provided). The region, application type and negative example did not appear to be important at all. We also found that an enhanced example as well as an enhanced description would provide the process with a higher completion rate. The next stage of the analysis was to explore the interactions among the factors. [Fig. 9.48](#) shows an interaction graph among all the studied variables.

From the results of the analysis, the team concluded that

- the same forms and processes should be used in both regions, since the results were the same and
- it would help to provide enhanced descriptions and examples for certain fields.

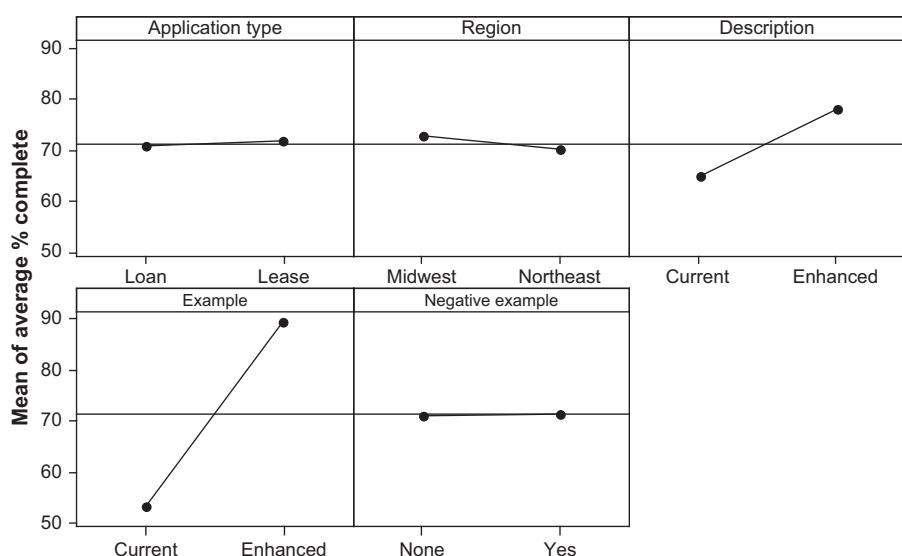
By analysing the interactions among the factors, the team determined that negative examples did not help significantly when there were positive examples. Moreover, as the team decided to use the positive examples, it would not be worthwhile to also develop negative examples. The new forms increased the application completion rate from 60% to over 95%.

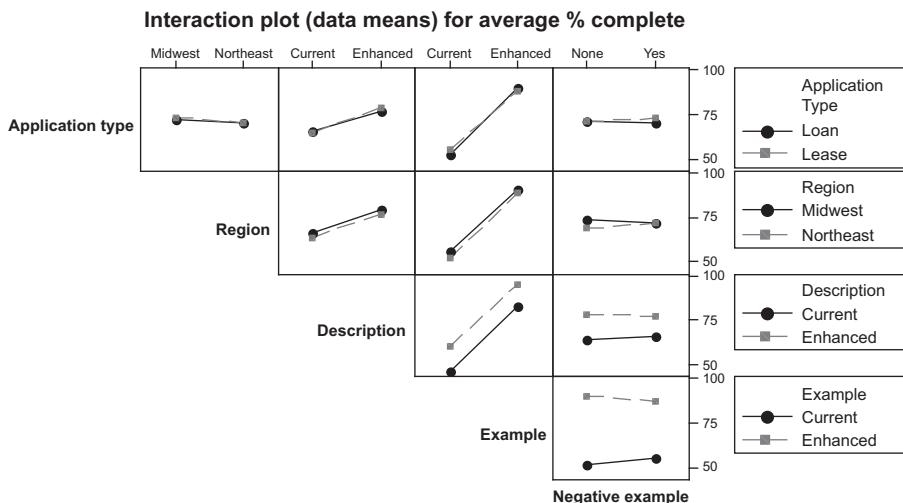
**Table 9.37** Factors and their respective levels for the experiment.

Factors	Labels	Low level	High level
Application type	A	Loan	Lease
Region	B	Midwest	Northeast
Description	C	Current	Enhanced (additional explanation provided)
Example	D	Current	Enhanced (additional examples provided)
Negative example	E	None	Yes

**Table 9.38** Results of the experiment from a banking process.

Run order	A	B	C	D	E	Average percentage complete
1	Loan	Midwest	Current	Current	Yes	46.5
2	Lease	Midwest	Current	Current	None	47.2
3	Loan	Northeast	Current	Current	None	40.5
4	Lease	Northeast	Current	Current	Yes	49.8
5	Loan	Midwest	Enhanced	Current	None	60.2
6	Lease	Midwest	Enhanced	Current	Yes	65.8
7	Loan	Northeast	Enhanced	Current	Yes	58.5
8	Lease	Northeast	Enhanced	Current	None	57.2
9	Loan	Midwest	Current	Enhanced	None	88.7
10	Lease	Midwest	Current	Enhanced	Yes	81.4
11	Loan	Northeast	Current	Enhanced	Yes	83.9
12	Lease	Northeast	Current	Enhanced	None	79.3
13	Loan	Midwest	Enhanced	Enhanced	Yes	91.6
14	Lease	Midwest	Enhanced	Enhanced	None	99.3
15	Loan	Northeast	Enhanced	Enhanced	None	96.3
16	Lease	Northeast	Enhanced	Enhanced	Yes	94.2

**Main effects plot (data means) for average % complete****Figure 9.47** Main effects plot for the bank application process.



**Figure 9.48** Interaction effects plot for the bank application process.

### 9.2.13 DoE applied to a transactional process

A global telecommunications company in the United States launched a major initiative to improve its customer service. This case study discusses the use of a screening experiment to determine which process factors have the largest effects on the performance of the repair ordering process in the above company. Phone equipment and lines need repairs for many reasons which are typically initiated with a service order. The ordering process is not perfect, resulting in corrections for many reasons: incorrect information, customers change their minds, and the company cannot meet their commitment to the customer and the repair must be rescheduled. Not meeting commitments to customers was important. This issue consistently showed up as the largest source of customer dissatisfaction.

The financial and process improvement opportunities associated with the repair process are large. At the time of this study the company was issuing over 700,000 service order corrections per month. A 10% reduction in corrections amounted to more than \$10.9 million per year. This savings does not include the costs associated with decreased customer satisfaction as well as increased employee anxiety associated with fixing errors. These costs are unknown and unknowable. The factors to be tested were brainstormed by the team. The 41 “fixes” identified that could be tested were reduced to 15 which could be evaluated in a 16 run screening design. A sampling of six locations across the company was selected to run the test. In some of the larger sites, a 32-run experiment design was used to estimate some of the interactions between the factors studied.

The list of the 15 factors studied is shown in [Table 9.39](#). Each factor is evaluated at two levels; low (−) and high (+). The design used was the 16-run Plackett–Burman design shown in [Table 9.40](#). It is important to note that Test

**Table 9.39** Factors studied in repair order corrections reduction experiment.

Code	Factor	Low level	High level
X1	Call recap	As is	All orders recapped
X2	Agree on due date	First available date	What date would you like?
X3	Feature exchange	As is	Job aid provided
X4	Order flow process	As is	Process map provided
X5	Correction cost impact	As Is	Handout provided
X6	Test dial customer number	As Is	Instructions provided
X7	Facilities reuse training	As is	Instructions provided
X8	Dual service policy clarification	As Is	Training on policy provided
X9	Correct field identifier usage	As Is	Instructions provided
X10	Caller ID information	As is	Information provided
X11	Eliminate pregreen dates	As Is	Ignore approved usage dates
X12	Sales literature	As is	Caller ID packet provided
X13	Order facts identification	As is	Tip sheet provided
X14	Check switch	As is	Information provided
X15	Abbrev dialing list accuracy	As Is	Correct entries: how to

16 is the current settings of the 15 process variables being studied. A different CSR (Customer Sales Representative) was assigned to complete each test run. In effect, each test run in the design represents the recipe the CSR should use to operate the repair order process during the test period. The CSRs were assigned to the different runs at random. The results for each of the 16 tests are shown in [Table 9.41](#). The response measured is the number of order corrections per 1000 orders.

The effects of the 15 factors are shown in [Table 9.42](#) and [Fig. 9.49](#). The factor effects are the difference between the average responses at the high (+) and low (−) levels of the factors. We see in [Table 9.42](#) and [Fig. 9.50](#) that four factors have statistically significant effects: X1, X4, X8 and X15. The confidence limits for the factor effects of + / − 31.4 shown in [Fig. 9.2](#) were computed by using the residual SD of the four-factor model (X1, X4, X8 and X15).

In [Table 9.43](#), the direction (positive or negative) of the effects is taken into consideration to develop the recommended settings for factors to reduce service order corrections. The four-factor model predicted that an order correction rate = 25 corrections per 1000 orders at the recommended factor levels (+, −, +, −). In [Table 9.41](#), we see that the lowest correction rates observed in the design were 65 and 69 for Tests 1 and 6, respectively. Test 15 which is the current operating conditions (all factors at low levels) had a correction rate of 136 per 1000 orders. These results together with the findings at the other locations led to the assignment of a

**Table 9.40** Repair order process screening design—factor levels for each of 16 tests.

Test	X1	X2	X3	X4	X5	X6	X7	X8	X9	X10	X11	X12	X13	X14	X15
1	+	-	-	-	+	-	-	+	+	-	+	-	+	+	+
2	+	+	-	-	-	+	-	-	+	+	-	+	-	+	+
3	+	+	+	-	-	-	+	-	-	+	-	-	+	-	+
4	+	+	+	+	-	-	-	+	-	-	+	+	-	+	-
5	-	+	+	+	+	-	-	-	+	-	-	+	+	-	+
6	+	-	+	+	+	+	-	-	-	+	-	-	+	+	-
7	-	+	-	+	+	+	+	-	-	-	+	-	-	+	+
8	+	-	+	-	+	+	+	+	-	-	-	+	-	-	+
9	+	+	-	+	-	+	+	+	+	-	-	-	+	-	-
10	-	+	+	-	+	-	+	+	+	+	-	-	-	+	-
11	-	-	+	+	-	+	-	+	+	+	+	-	-	-	+
12	+	-	-	+	+	-	+	-	+	+	+	+	-	-	-
13	-	+	-	-	+	+	-	+	-	+	+	+	+	-	-
14	-	-	+	-	-	+	+	-	+	-	+	+	+	+	-
15	-	-	-	+	-	-	+	+	-	+	-	+	+	+	+
16	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-

Note: Test 16 is current levels of the 15 process variables being studied.

**Table 9.41** Repair order process responses—correction errors per 1000 orders.

Test	Rate	Test	Rate	Test	Rate	Test	Rate
1	65	5	231	9	78	13	75
2	140	6	69	10	81	14	122
3	121	7	216	11	129	15	131
4	97	8	82	12	85	16	136

**Table 9.42** Repair order process factor effects.

Code	Factor	Average low level	Average high level	Effect
X1	<b>Call recap</b>	<b>152.6</b>	<b>92.1</b>	<b>- 60.5</b>
X2	Agree on due date	114.9	129.9	15.0
X3	Feature exchange	128.3	116.5	- 11.8
<b>X4</b>	<b>Order flow process</b>	<b>102.8</b>	<b>142.0</b>	<b>39.2</b>
X5	Correction cost impact	131.8	113.0	- 18.8
X6	Test dial customer number	130.9	113.9	- 17.0
X7	Facilities reuse training	117.8	127.0	9.2
<b>X8</b>	<b>Dual service policy clarification</b>	<b>140.0</b>	<b>104.8</b>	<b>- 35.2</b>
X9	Correct field identifier usage	128.4	116.4	- 12.0
X10	Caller ID information	128.4	116.4	- 12.0
X11	Eliminate pregreen dates	131.0	113.8	- 17.2
X12	Sales literature	111.9	132.9	21.0
X13	Order facts identification	120.8	124.0	3.2
X14	Check switch	117.1	127.6	10.5
<b>X15</b>	<b>Abbreviated dialing list accuracy</b>	<b>92.9</b>	<b>151.9</b>	<b>59.0</b>

team to study the repair ordering process further, including the refinement of the findings identified in the screening experiments. This work involved a number of additional experiments. Problems are rarely solved in a single experiment.

This study highlights some important considerations regarding experimentation with service and other processes. First, it is important to have a strategy to follow. We have found the strategy of screening experiments followed by characterisation experiments (also referred to as refining experiments), and as appropriate optimisation experiments to be broadly useful (Snee, 2009; Antony, 2014). Next, it is important to note that in this study only 4 of the 15 factors had significant effects. This result is consistent with the general finding that typically 3–6 factors drive a process (Snee, 2009). This is also consistent with the Pareto principle and its 80/20 rule that 80% of the variation is due to 20% causes (Juran and Godfrey, 1999). Using screening experiments, we can “cast your net wide,” testing many factors at

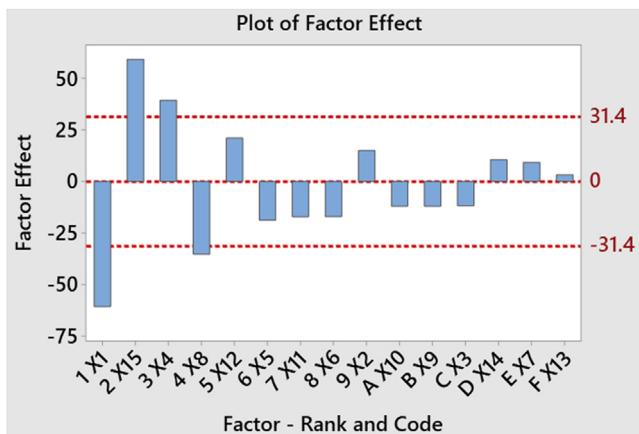


Figure 9.49 Repair ordering process factor effects and 95% confidence limits.

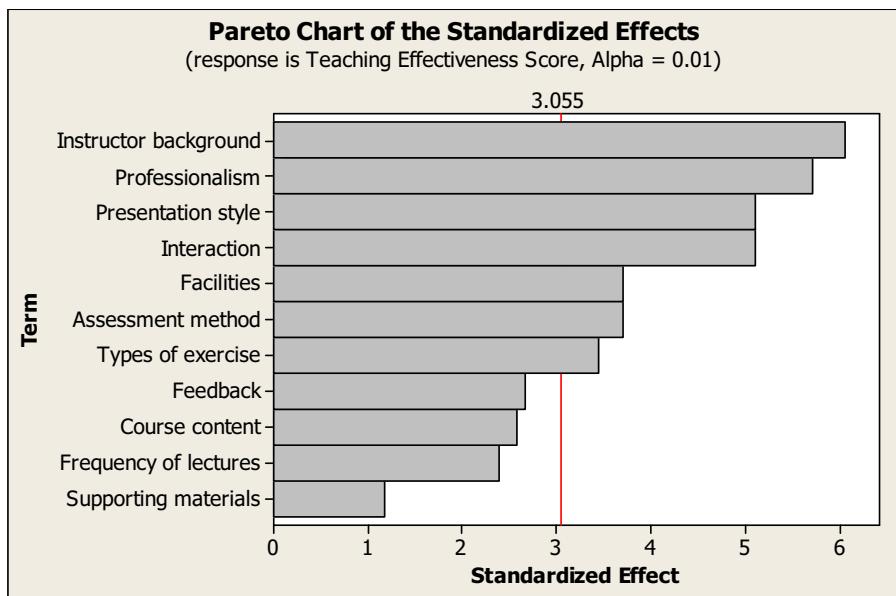


Figure 9.50 Pareto plot of the effects for the screening experiment.

the same time and increasing the likelihood of identifying the most important factors which influence the output of a process.

This experiment tested 15 factors in 16 tests. Such a design is called a *saturated design*. The strategy here is to test as large a number of factors as possible (Antony, 2014;

**Table 9.43** Recommended settings for the significant factors.

Code	Factor	Average low level	Average high level	Effect	Recommended level
X1	Call recap	152.6	92.1	- 60.5	Recap all orders
X4	Order flow process	102.8	142.0	39.2	As is, no change
X8	Dual service policy clarification	140.0	104.8	- 35.2	Provide training on policy
X15	Abbreviated dialing list accuracy	92.9	151.9	59.0	As is, no change
	All other factors				As is, no change

(Antony and Kaye, 2012). Time is the essence and in the screening phase we like to test as many factors as possible in each experiment. The downside to this strategy is that there are no repeat runs to estimate the experimental variation due to inadequate degrees of freedom. This potential problem is handled by using the small effects to estimate the experimental variation. As mentioned earlier, experience consistent with the Pareto principle has shown that only a few factors will have large effects. In this case the 11 factors with insignificant effects were used to estimate the experimental variation which was used to calculate the factor effect confidence limits shown in Fig. 9.49.

Several Important lessons were learned from this case study. We have seen that screening designs such as the Plackett–Burman design can be very effective in testing a large number of factors in a single experiment. Even with a saturated design, the Pareto principle tells us that only a few factors (e.g. 3–6) will be important. The team that carried out this experiment received some training on the *what, why and how of conducting screening experiments*. This training was very helpful in assuring the success to the experiment. Graphical displays such as Fig. 9.49 are very useful in communicating the results of the study without learning mathematical equations and various statistical hypotheses tests for identifying the most important factors. Management and others see the effects which stimulate discussion and decisions regarding what actions to take. It is important to recall John W. Tukey's admonishment: "*the greatest value of a picture is when it forces us to notice what we never expected to see.*"

### 9.2.13.1 Significance of the study

This case study illustrates the power of DoE in a telecommunications company aimed at improving the customer service. A number of service improvement managers were sceptical about the application of DoE at the outset. This is due to the lack of awareness on the benefits of this powerful technique as well as lack of

continuous improvement mindset. In addition, a few business leaders had a pre-conceived idea that DoE is useful for manufacturing companies and not so helpful in the service context. The results of this study were quite an eye-opener for many managers and many of them stated that it certainly can deliver great value to service processes, in particular to understand many unknown facts.

### **9.2.14 *Design of experiments in understanding and evaluating teaching effectiveness in UK higher education***

This case study is published in the International Journal of Quality and Reliability Management by the author and the author would like to take this opportunity to thank Emerald Publishers in granting the permission to reproduce the case study for the book (refer to the following hyperlink <https://doi.org/10.1108/IJQRM-01-2018-0011>) for more information.

The author has identified a few papers on the use of ED methodology applied to HE environment and this clearly indicates a research gap and more potential opportunities in its applications in various business processes within the HE setting. [Barone and Lo Franco \(2009\)](#) undertook an ED approach in combination with the service quality model in an environmental engineering degree programme at the University of Palermo, Italy. The authors found that teacher–student interaction is the most influential factor on student satisfaction during two academic statistical courses over a period of two years when they gathered data from 24 students who had been attending the course regularly. [Ree et al. \(2014\)](#) presented a very interesting case study on ED to improve teaching quality at one of the universities in Seoul, South Korea. This study quantitatively and qualitatively analysed the factors that affect lecture quality and selected two control factors that can be controlled by the lecturer and three noise factors that cannot be controlled by the lecturer. The result was analysed to propose the optimum lecturing method. The result of analysis showed that it is more effective when the effort to form closeness with students is carried out at the beginning of the lecture, and when student presentations are held once every two months.

In the case study, the author followed the definition provided by [Seidel and Shavelson \(2007, p. 456\)](#) “We speak of teaching effects or teaching effectiveness when referring to the effects of teaching on student learning and how satisfied are students from their learning experience.” According to [Seidel and Shavelson \(2007\)](#), studies conducted in the past decade related to teaching effectiveness were dominated by correlational survey studies, but they were proven distant from the teaching–learning process. The majority of teaching effectiveness studies is based on correlational survey studies ([Seidel and Shavelson, 2007](#)). In a study carried out by [Marsh and Hattie \(2002\)](#), they used “student perception” of teaching as the measure of teaching effectiveness, rather than an assessment that attempts to directly measure student-learning outcomes. The authors are using similar approach in this case study and a scientific experiment is executed purely based on students’ perception on teaching effectiveness. Teaching effectiveness obviously is a highly

complex and very personal process of evaluation which includes multitude of variables (Galbraith and Merrill, 2012). The quality of teaching effectiveness has been reported to have a direct relationship with the student learning outcomes (Darling-Hammond and Young, 2002).

The case study encompasses delivery of a postgraduate course to postgraduate students from 26 countries at one of the higher education institutions in the United Kingdom. The case study was carried out in four different phases.

#### 9.2.14.1 Phase 1: Planning of the experiment

In the planning phase, the students were asked to define teaching effectiveness in their own perspective. The study was carried out in two successive years (2015 and 2016) attended by over 100 postgraduate students. The students were put in groups and each group had not more than 8 students. In students' perspective, it was apparent that there were two components which constitute teaching effectiveness. The first component was: *the content of the course taught by the tutor or instructor has to be practical and can be readily applied to a business context*. The second component was: *the course material can be easily understood and can be learned efficiently and effectively*. The tutor of the class has 20-year experience with a good background and gained 10-year industrial experience on the topic. The tutor has asked the students to identify the potential factors or process variables which could influence teaching effectiveness. In this study, the response or quality characteristic of interest is the teaching effectiveness. For simplicity reasons, the students were asked to keep each factor at 2-levels. This assumes the property of linearity for each factor and the definitions of each level for each factor were determined by the students in groups and the tutor was involved in guiding them to come up with a definition which was agreeable to everyone in the classroom. From a thorough brainstorming for an hour, the students have initially identified 20 potential factors and their levels as defined below.

**1. Number of speakers in the delivery of lectures**

*Low level = instructor on his or her own*

*High level = instructor + guest speakers*

**2. Background of the instructor**

*Low level = instructor who has recently completed a PhD with little exposure to industry*

*High level = instructor with rich industrial and teaching experience*

**3. Method of assessment for the course**

*Low level = examination on its own*

*High level = coursework on its own*

**4. Interaction during the delivery of lecture**

*Low level = no discussion/Q & A sessions*

*High level = healthy discussions plus Q & A sessions*

**5. Content of the course**

*Low level = heavy theoretical with a few case studies*

*High level = less theoretical with more practical case studies*

- 6. Frequency of lectures**  
*Low level = 3 h per week*  
*High level = 6 hours fortnightly*
- 7. Feedback**  
*Low level = no feedback for course works and other related works relevant to assessment*  
*High level = have feedback for course works and other related works relevant to assessment*
- 8. Students' background**  
*Low level = students with no previous knowledge and experience in the field*  
*High level = students with some knowledge on the topic and experience in the field*
- 9. Students' attitude towards learning**  
*Low level = negative*  
*High level = positive*
- 10. Types of exercise in the classroom**  
*Low level = individual exercise*  
*High level = group exercise*
- 11. Presentation style of the instructor**  
*Low level = lack of clarity in speaking, monotonous tone and pitch*  
*High level = clarity of speech, passionate speaker with varied tone and pitch*
- 12. Time of delivery of the lecture**  
*Low level = morning*  
*High level = afternoon*
- 13. Field trip associated with the course**  
*Low level = unavailable*  
*High level = available*
- 14. Facilities of the room where the teaching is delivered**  
*Low level = poor*  
*High level = good*
- 15. Supporting materials**  
*Low level = insufficient information*  
*High level = sufficient information*
- 16. Coherence**  
*Low level = no structure, random*  
*High level = logical and structured*
- 17. Professionalism**  
*Low level = unfamiliarity of materials, topic, unprepared, not handling questions professionally*  
*High level = familiarity of materials, topic, explaining complex things, handling questions professionally*
- 18. Support after lectures**  
*Low level = no support*  
*High level = good support*
- 19. Approachability**  
*Low level = students cannot approach lecturer*  
*High level = students can approach lecturer with confidence*
- 20. Behaviour of lecturer**  
*Low level = less caring, rude, not helpful*  
*High level = caring, nice, helpful*

The students in groups have been then asked to utilise a simple tool called multi-voting to reduce the number of factors to a manageable number. All students have participated in this exercise and identified top 11 factors from the 20 so that a screening design could be utilised to identify the most important factors from the study. Table 9.44 presents the list of factors which have been included in the screening experiment. In order to study 11 factors at 2-levels, a non-geometric Plackett–Burman (P–B) 12-trial design was utilised. There were 14 groups for year 2015 and 2016 and each group had 7–8 students. Each group has been asked to rate teaching effectiveness on a Likert scale of 1–10; 1 being the lowest score and 10 is the maximum possible score. The average teaching effectiveness for year 2015 for all possible combinations of factors were recorded and similarly the same exercise has been repeated in 2016 for repeatability. The data collection and the experimental layout will be discussed in the next phase.

#### **9.2.14.2 Phase 2: Designing the experimental layout**

In this phase, one should design the experimental layout showing the experimental trials to be conducted based on various combinations of factors selected from the brainstorming. In this phase, the authors present the layout of Plackett–Burman (P–B) screening design with 12 trials. In Plackett–Burman designs, main effects have a complicated confounding relationship with 2-factor interactions. Therefore these designs should be used to study main effects only and not when strong interactions are to be studied or analysed in an experiment. However, Plackett–Burman

**Table 9.44** List of factors and their levels chosen for the screening experiment.

<b>Factor name</b>	<b>Label</b>	<b>Low level ( – 1)</b>	<b>High level ( + 1)</b>
Course content	A	Heavy theory	Less theory
Presentation style	B	Monotonous tone	Varied tone
Interaction	C	No (no discussion)	Yes (healthy discussion)
Feedback	D	No	Yes (Have feedback)
Instructor background	E	Inexperienced	Experienced
Frequency of lectures	F	Weekly	Fortnightly
Professionalism	G	Unprofessional (unfamiliarity of materials)	Professional (familiarity of materials)
Assessment method	H	Exam on its own	Coursework on its own
Types of exercise	I	Individual	Group
Facilities	J	Poor	Well equipped
Supporting materials	K	Insufficient	Sufficient

designs are very powerful in identifying the most important factors in a minimum number of experimental runs or trials. For instance, if a full factorial design is utilised for studying 11 factors at 2-levels, the total number of experimental trials or runs would have been  $2^{11} = 2048$ . This huge number of trials will be time-consuming in our investigation and was not at all feasible to execute. **Table 9.45** presents the design matrix or experimental layout in coded format (showing all the factor levels in coded form). The low level of each factor in the experimental layout will be replaced by “– 1” and high level by “+ 1.”

### 9.2.14.3 Phase 3: Conducting the experiment

The author has collected the data during the second semester of 2015 and 2016 from over 100 postgraduate students representing 26 countries. The same factors have been studied using the P–B design for repeatability purposes and average teaching effectiveness in both years have been recorded by the course tutor. This has resulted in 24 data points from 12 experimental trials. This allows an experimenter to create enough degrees of freedom to work out the experimental error or error variance. The average scores for teaching effectiveness for year 2015 and 2016 have been entered into the last column of **Table 9.46**. It was quite interesting to observe some variation in the average scores between the years at each trial condition. The next phase is about analysis of the results and therefore the key objectives from the analysis have to be discussed with the students. The following objectives were set by the tutor so that students can perform statistical analysis on the collected data.

1. *What are the most important factors (from a statistical perspective) which influence the average teaching effectiveness?*
2. *What are the least important factors which influence the average teaching effectiveness?*
3. *What are the best settings of the factors to maximise teaching effectiveness?*

**Table 9.45** Plackett–Burman experimental layout.

Runs	A	B	C	D	E	F	G	H	I	J	K
1	+ 1	– 1	+ 1	– 1	– 1	– 1	+ 1	+ 1	+ 1	– 1	+ 1
2	+ 1	+ 1	– 1	+ 1	– 1	– 1	– 1	+ 1	+ 1	+ 1	– 1
3	– 1	+ 1	+ 1	– 1	+ 1	– 1	– 1	– 1	+ 1	+ 1	+ 1
4	+ 1	– 1	+ 1	+ 1	– 1	+ 1	– 1	– 1	– 1	+ 1	+ 1
5	+ 1	+ 1	– 1	+ 1	+ 1	– 1	+ 1	– 1	– 1	– 1	+ 1
6	+ 1	+ 1	+ 1	– 1	+ 1	+ 1	– 1	+ 1	– 1	– 1	– 1
7	– 1	+ 1	+ 1	+ 1	– 1	+ 1	+ 1	– 1	+ 1	– 1	– 1
8	– 1	– 1	+ 1	+ 1	+ 1	– 1	+ 1	+ 1	– 1	+ 1	– 1
9	– 1	– 1	– 1	+ 1	+ 1	+ 1	– 1	+ 1	+ 1	– 1	+ 1
10	+ 1	– 1	– 1	– 1	+ 1	+ 1	+ 1	– 1	+ 1	+ 1	– 1
11	– 1	+ 1	– 1	– 1	– 1	+ 1	+ 1	+ 1	– 1	+ 1	+ 1
12	– 1	– 1	– 1	– 1	– 1	– 1	– 1	– 1	– 1	– 1	– 1

Source: Plackett and Burman (1946).

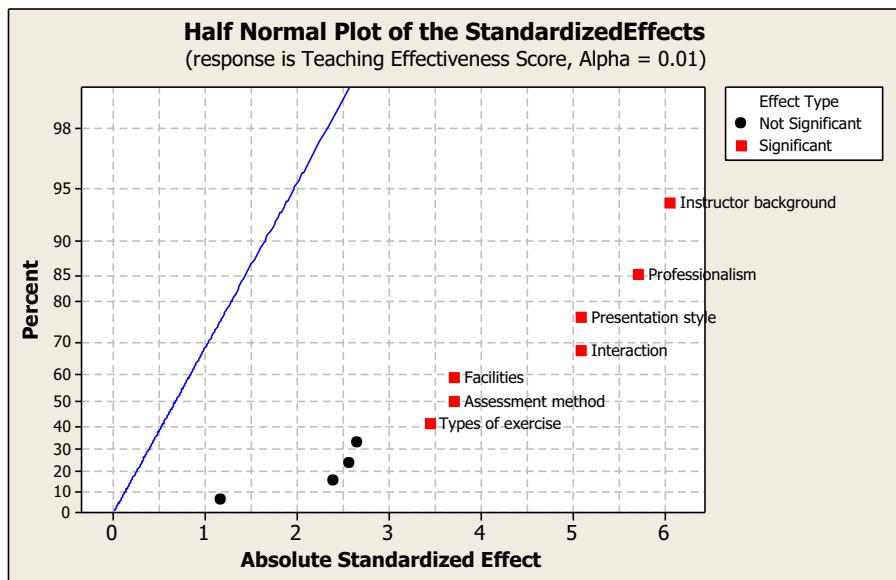
**Table 9.46** Plackett-Burmann layout with experimental results.

Runs	A	B	C	D	E	F	G	H	I	J	K	Teaching effectiveness
1	+ 1	- 1	+ 1	- 1	- 1	- 1	+ 1	+ 1	+ 1	- 1	+ 1	6.0, 5.2
2	+ 1	+ 1	- 1	+ 1	- 1	- 1	- 1	+ 1	+ 1	+ 1	- 1	4.7, 6.3
3	- 1	+ 1	+ 1	- 1	+ 1	- 1	- 1	- 1	+ 1	+ 1	+ 1	5.8, 6.5
4	+ 1	- 1	+ 1	+ 1	- 1	+ 1	- 1	- 1	- 1	+ 1	+ 1	4.3, 3.5
5	+ 1	+ 1	- 1	+ 1	+ 1	- 1	+ 1	- 1	- 1	- 1	+ 1	5.7, 6.1
6	+ 1	+ 1	+ 1	- 1	+ 1	+ 1	- 1	+ 1	- 1	- 1	- 1	5.5, 5.1
7	- 1	+ 1	+ 1	+ 1	- 1	+ 1	+ 1	- 1	+ 1	- 1	- 1	5.3, 5.1
8	- 1	- 1	+ 1	+ 1	+ 1	- 1	+ 1	+ 1	- 1	+ 1	- 1	6.7, 6.5
9	- 1	- 1	- 1	+ 1	+ 1	+ 1	- 1	+ 1	+ 1	- 1	+ 1	4.3, 4.2
10	+ 1	- 1	- 1	- 1	+ 1	+ 1	+ 1	- 1	+ 1	+ 1	- 1	5.3, 4.9
11	- 1	+ 1	- 1	- 1	- 1	+ 1	+ 1	+ 1	- 1	+ 1	+ 1	5.0, 4.4
12	- 1	- 1	- 1	- 1	- 1	- 1	- 1	- 1	- 1	- 1	- 1	1.5, 1.4

#### 9.2.14.4 Phase 4: Analysing the experiment

The purpose of this phase is to analyse the data in the experimental layout and interpret the results so that valid and sound conclusions can be derived. As the authors of the article would like to adopt “Keep it Statistically Simple” approach for the analysis, we have decided to introduce simple but powerful graphical tools instead of heavy statistical methods for the analysis. Minitab software system version 17 has been used for the analysis of data. The authors have used a number of graphical tools to validate the results from the experiment. The first task in the analysis was to identify the most important factors which have an impact on average teaching effectiveness scores. Quite often, people pay too much attention to the most important factors from an experiment. In fact, it is equally important for experimenters to understand the least important factors which influence the quality characteristics of a product or service. The idea is to set such least important factors at their most economical levels for cost savings. Figs. 9.50 and 9.51 show the Pareto plot and half normal plot of main effects of all the factors which influence the average teaching effectiveness.

The Pareto plot displays the absolute values of the effects and draws a reference line on the chart. Any effect that extends past the reference line is statistically significant at 5% significance level (Antony, 2014). Here, the significance level is the risk of saying that a factor is significant when in fact it is not. In other words, it is the probability of the observed significant effect due to pure chance. It is always a good practice to check the findings from a Pareto plot with half normal probability plot (HNPP) of the estimates of the effects. An HNPP plots the absolute value of the effects of factors. Unimportant (i.e. near-zero) effects manifest themselves as being near zero and on a line while important (i.e. large) effects manifest themselves by being off the line and well-displaced from zero. A line through the insignificant factors helps to graphically delineate the difference between significant and insignificant factors.

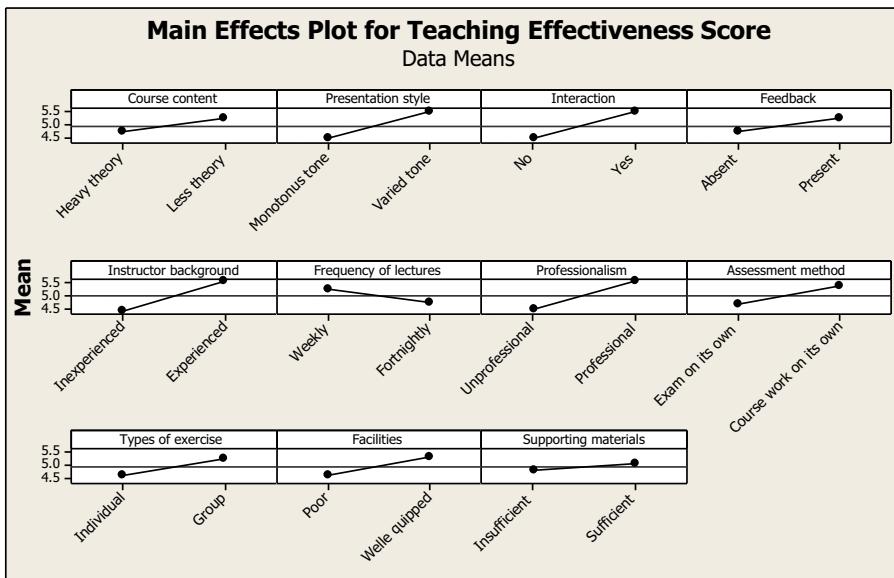


**Figure 9.51** Half normal probability plot of the effects for the screening experiment.

Figs. 9.50 and 9.51 suggest that the most important factors (arranged in the order of importance) from the screening experiment are:

1. *Instructor background*
2. *Professionalism of the instructor*
3. *Presentation style of the instructor*
4. *Interaction between the students and instructor in the classroom*
5. *Facilities*
6. *Method of course assessment*
7. *Types of exercise set by the instructor*

The unimportant factors were *feedback provided to the students, course content, frequency of lectures and supporting materials provided in the virtual learning environment (e.g. case studies)*. The last part of the analysis phase was to understand the optimal settings of the factors to maximise average teaching effectiveness score. In order to accomplish this objective, the authors have decided to utilise a main effects plot. A main effects plot is a plot of the mean response values of each level of a factor. One can use this tool to compare the relative strength of the effects of various factors in an experiment. The sign of a main effect tells us of the direction of the effect, whether the average teaching effectiveness scores increases or decreases. The magnitude tells us the strength of the effect. If the effect of a factor is positive, it implies that the average teaching effectiveness score is higher at a high level than at a low level of that specific factor. Fig. 9.52 illustrates the main effects plot of all factors influencing the average teaching effectiveness.



**Figure 9.52** Main effects plot for the screening experiment.

The optimal settings for maximising the teaching effectiveness score are as follows:

*Instructor background – experienced tutor on the subject matter*

*Professionalism of the instructor – professional tutor with familiarity of materials*

*Presentation style of the instructor – varied tone during the duration of the lecture*

*Interaction between the students and instructor in the classroom – good interaction with students by asking questions and engaging with them via exercises*

*Facilities – well-equipped room with all the facilities for the delivery of lecture*

*Method of course assessment*

*Types of exercise set by the instructor – group exercises (optimal size of 7–8)*

*Feedback – effective feedback to course work*

*Course content – less theory with more practical examples and real case studies*

*Frequency of lectures – weekly lectures (3 h)*

*Supporting materials provided – good case studies on different topics and other supporting materials such as white papers and practitioner-based viewpoint articles.*

## 9.3 Discussion and limitations of the study

This case study has demonstrated the power of ED methods in understanding and scientifically evaluating the most influential factors which affect the teaching effectiveness in the delivery of a postgraduate course within the higher education sector. The students were asked to identify the top five factors before the experiment was executed. The students have used brainstorming and multi-voting methods to come up with the top five factors they have thought which are important to teaching effectiveness. The results

**Table 9.47** Comparison of students' perceptions with scientific experiment.

<b>Top 5 factors from students' perspective (use of brainstorming and multi-voting methods)</b>	<b>Top 5 factors from the screening experiment</b>
<i>Course content</i>	<i>Background of the instructor</i>
<i>Presentation style of the instructor</i>	<i>Professionalism of the instructor</i>
<i>Interaction in the classroom</i>	<i>Presentation style of the instructor</i>
<i>Professionalism</i>	<i>Interaction in the classroom</i>
<i>Method of assessment</i>	<i>Facilities for the delivery of lecture</i>

from students' perceptions were compared with the results from the screening experiment conducted with the inputs of over 100 students as shown in **Table 9.47**.

It was very surprising to the author that the most important factor identified by the students is not turned out to be statistically significant from the screening experiment. Moreover, method of assessment was important to students' perception, but it was not appeared to be in the top five based on the analysis of data obtained from the experiment. The students did not rate background of the instructor and facilities in the top five, but they have turned out to be statistically significant and listed among the top five factors from the screening experiment. One of the major challenges of the study was that the experiment has taken more than 3 h to plan, design, conduct and analyse the data collated from the experiment. The authors have also noticed that there has been some variation in the teaching effectiveness scores between the groups and this is primarily due to students from varied cultural backgrounds. One of the limitations of the study is that the experiment is conducted for a popular postgraduate course and it would be really beneficial to understand the results of the experiment for less popular postgraduate courses in the university. Moreover, the author has not had a chance to run the experiment for undergraduate courses with a high proportion of home students. It would be really interesting to see if there are any differences in the ranking of factors between postgraduate and undergraduate courses. Finally, the author would like to capture the perceptions of teaching effectiveness with a number of key academics through semi-structured interviews and the purpose of this investigation to understand their perceptions on teaching effectiveness.

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# **Design of experiments and its applications in the service industry**

**10**

## **10.1 Introduction to the service industry**

In many countries, service industries dominate the economy. In the context of the service industry, we have to make sure that the product or service not only meets the functional requirements of the customer but also – equally important – meets the intangible characteristics associated with the delivery of service, such as friendliness, courtesy, willingness to help, etc. In other words, the total service concept is a combination of both tangibles and intangibles and the latter are more difficult to quantify, measure and control. When something goes wrong in the eyes of the customer, it is very difficult to identify the failure points in this context due to the human behavioural aspects associated with the service. The service industry today is beginning to recognise the importance of quality as studies show that companies can boost their profits by almost 100% by retaining just 5% more of their customers than their competitors retain. The definition of quality that applies to manufactured products can be equally applied to service products. The very nature of service implies that it must respond to the needs of the customer. This means that service must meet or exceed customer expectations.

Although DOE has been around for decades, few business leaders in service organisations have a good grasp of its power in tackling problems associated with service process efficiency and effectiveness (Johnson and Bell, 2009). This field remains fertile ground for greater education, experience and application. Service-oriented industries such as financial services, transportation services, hotel and restaurant services, the health care industry, utility services, IT services, the airline industry, etc. are the fastest growing sectors around the world (Kapadia and Krishnamoorthy, 1999). Customers are becoming more critical of the service they receive today and therefore most modern organisations are paying more attention to their transactional service processes.

## **10.2 Fundamental differences between the manufacturing and service organisations**

Services are characterised as being different from products along a number of dimensions that have implications for the quality of service provided to customers. Manufacturing companies make products that are tangible, whereas services have

an associated intangible component. There is little or intangible evidence to show once a service has been performed (e.g., consultation with a doctor). If a service is not provided within a given time frame, it cannot be used at a later time. Services are produced and consumed simultaneously, whereas manufactured goods are produced prior to consumption. Services cannot be stored, inventoried or inspected prior to delivery as manufactured goods are. Therefore, greater attention must be paid to building quality into the service process in order to ensure that customers receive a world-class experience from that service. In a manufacturing set-up, customers have a direct impact on creating formal product specifications; however, in a service context, the customer does not provide direct input on the quality characteristics. Variability often exists in services as a function of labour inputs and non-standardisation of delivery. In such cases, the use of quality standards in the conventional sense becomes more difficult. The production of services requires a higher degree of customisation than does manufacturing. For instance, doctors, lawyers, insurance salespeople etc. must tailor their services to individual customers. Customers often are involved in the service process and are present while it is being performed, whereas in manufacturing settings, customers are not normally present when the product is produced. The quality of human interaction is a more crucial factor in the service settings than in manufacturing. For example, in a hospital setting, a patient has a number of interactions with the nurses, doctors and other medical staff. In manufacturing companies, the degree to which a product is accepted can be easily quantified whereas in a service context, the degree of customer satisfaction is not as easily quantified because of the human factors involved with delivery of a service.

### **10.3 DOE in the service industry: fundamental challenges**

A product realisation process initiated by the manufacturer usually begins with product design and development, a set of product specifications and process development, followed by production and testing, and concludes with delivery to the customer. If at any point in the process products do not meet specifications, they can either be scrapped or reworked. Service processes, on the other hand, generate value as the customer interacts with the process and ultimately, it is the customer's experience with the process that is most important. The distinction among the process, the delivery of the process and the customer's responses is often difficult to define. The exact sequence of activities in a service process is often difficult to predict in advance.

There are a number of reasons why DOE has not been commonly employed in service settings. Following are some of the most fundamental barriers and challenges in applying DOE in a service environment. For more discussion, see [Roes and Dorr \(1997\)](#), [Raajpoot et al. \(2008\)](#), [Holcomb \(1994\)](#), [Kumar et al. \(1996\)](#), [Johnson and Bell \(2009\)](#) and [Blosch and Antony \(1999\)](#).

- Lack of awareness and knowledge and misconceptions discourage experimentation in many service organisations.

- The performance of a service process is very difficult to measure accurately.
- Service process performance depends a great deal on the behaviour of the human beings involved in delivering it.
- Service processes have more ‘noise’ factors associated with them (queuing, friendliness, location, politeness, etc.)
- As service is often simultaneously created and consumed and intangible dimensions are important indicators of quality in the service context, experimental control of inputs and measurement of output require careful consideration.
- In any service process, a clear description and distinction of service processes is needed for quality control and improvement. A good understanding of front office, back office and customer processes is required for quality and process improvements.
- DOE is a ‘techy’ tool; managers in the service sector may be less likely to have a mathematical background and be perhaps more likely (than in engineering, say) to be driven by ‘experience’ and gut feel – wanting to be seen to be incisive and intuitive.
- The biggest challenge in services is in determining what to measure and in finding operational control factors to conduct the DOE. It is also effective if a service process can be computer simulated so that the DOE may be done as a simulation.
- The fundamental challenges are, first, that it is not easy to obtain necessary observed data in the service sector, and second, that it is not easy to provide the same experimental conditions for repeated measurement in the service sector.
- The lack of standardised work processes in a service sector makes the application of DOE a very challenging task.
- Lack of an improvement mindset.
- Careful selection of factor levels is required due to the involvement of people and the interaction between customer and service provider.
- Persuade people to follow a systematic methodology for process improvement and to convince them to rely on the power of data to drive the decision-making process.

## 10.4 Benefits of DOE in service/non-manufacturing industry

The purpose of this section is to illustrate the benefits of DOE in various service or non-manufacturing settings. [Holland and Cravens \(1973\)](#) presented the essential features of fractional factorial design and illustrated a very interesting example looking into the effect of advertising and other critical factors on the sales of candy bars. A large US-based company reduced their accounts receivable from 200 days to only 44 days, generating a significant cash flow in the process ([Frigon, 1997](#)). They studied four factors at 2-levels and a half-fractional factorial design was utilised. A US-based hospital performed a DOE with seven factors to better educate patients on how to safely use an anti-blood-clotting drug that can be fatal if used improperly. They achieved a 68% improvement in patient understanding by using a standardised instruction sheet and having a pharmacist discuss the drug. [Curhan \(1974\)](#) used a 2-level fractional factorial design to test the effects of price, newspaper advertising, display space and display location on sales of fresh fruits and vegetables in supermarkets. In particular, he found that,

for the four items tested, doubling display space increased sales from 28% to 49%. In a closely related study, Wilkinson et al. (1982) described a factorial experiment for assessing the impact of price, newspaper advertising, and display on the sales of four products (bar soap, pie shells, apple juice and rice) at a Piggly Wiggly grocery store. Their experiment considered three display levels (normal shelf space, expanded shelf space and special display), and three price points (regular price, price cut and deeper cut). Overall, the authors found large effects for expanded shelf space, very large effects for special display at the reduced price levels and a large effect for special display even at the regular price (a sales increase of about 70%).

Ledolter and Swersey (2006) described the power of a fractional factorial experiment to increase the subscription response rate of *Mother Jones* magazine. It was shown that direct mail response at *Mother Jones* has been improved by using a 16-run 2-level fractional factorial design that tests seven factors simultaneously. Kumar et al. (1996) used a Taguchi RPD methodology in order to improve the response-time performance of an information group operation which was responsible for addressing customer complaints concerning a small software export company. The limitation of this approach relates to process data availability and quality. Current databases were not designed for process improvement, resulting in potential difficulties for the Taguchi experimentation, where available data does not explain all the variability in process outcomes. Holcomb (1994) illustrated the use of Taguchi parameter design methodology to determine the optimal settings of customer service delivery attributes that reduce cost without affecting quality.

The Royal Navy's manpower planning system represents a highly complex queue which aims to provide sufficient manpower to meet both operational and structural commitments. This queue is affected by many variables and therefore it is essential to understand the influence of these variables and also the interactions (if any) among the variables. As real experimentation was impractical and infeasible, a computer-based simulation was developed to model the system to be studied. This paper illustrates how computer simulation and ED was applied to identify the key risk variables within the manpower planning system for the UK's Royal Navy (Blosch and Antony, 1999).

Starkey (1997) used a Plackett–Burman design in designing an effective direct response TV advertisement. Raajpoot et al. (2008) presented the application of the Taguchi approach of DOE to retail service. The study was performed by undergraduate students at a mid-size university in the US to determine the key attributes of a shopping experience in a superstore setting such as Walmart or Target. The potential applications of DOE in the service environment include the following:

- identifying the key service process or system variables which influence the process or system performance
- identifying the service design parameters which influence the service quality characteristics or CTQs in the eyes of customers
- minimising the time to respond to customer complaints
- minimising errors on service orders
- reducing the service delivery time to customers (e.g., banks, restaurants, etc.)

- providing a better understanding of cause–effect relationships between what we do and what we want to achieve, so that we can more efficiently optimise performance of the system we are working in
- reducing cost of quality due to rework and misinformation that lead to bad decision-making
- creating a clear competitive advantage over our competitors as very few are aware of this powerful technique
- reducing the turn-around time in producing reports and so on.

## 10.5 DOE: case examples from the service industry

### 10.5.1 Data entry errors

The Prescription Pricing Authority (PPA) is responsible for processing all prescriptions issued by medical doctors and dispensed by pharmacies throughout England. About 500 million prescriptions per annum are processed by nearly 1000 staff. With a general rise in competition to supply such a service, there is a constant need to update and improve efficiency (Antony et al., 2011). There are two main aims of the working process: to input data accurately and to input it quickly. It has long been thought that asking staff to work as quickly as possible compromises accuracy levels, i.e. that as input speeds become more rapid less care is taken and fewer self-checks are performed.

It was decided to run an experiment with two 3-level factors:

1. Staff factor: experienced, semi-experienced and novice
2. Instructions factor: ‘go as fast as you can,’ ‘be as accurate as possible’ and ‘go as fast as you can *and* be as accurate as possible’.

Thus, it would be discovered if particular instructions produced different effects in relation to different experience levels (Stewardson et al., 2002). The trials proved to be a resounding success, with good cooperation from all staff. The experiment established that the speed of input was the critical item that needed to be included in working instructions. Accuracy is affected by the experience level. If a person is asked to ‘go fast’, it will not tend to affect their accuracy level; however, if they are asked to be accurate, speed will be reduced without any noticeable effect on accuracy. It is thus favourable to insist on faster speeds: accuracy levels will, apparently, hold their ‘natural’ level. This is just one example of the use of a designed experiment involving human performance.

The key benefits of this designed experiment were that it showed the effect of issuing different types of commands on the speed and accuracy of data entry as well as evaluating the differences in performance between different types of staff. It also led to the establishment of a minimum expected performance standard for novices which helped determine recruitment and training needs. The experiment also allowed an assessment of the level of variation in data entry speed and accuracy among individuals.

Managerial implications were that a scientific approach could be applied to the assessment of performance. SPC using CUSUM (Cumulative Sum Control Charts) charts was also implemented for the data entry process and proved to be a workable methodology for deciding when bonuses should be given and when retraining was needed.

Lessons learnt included that a range of statistical techniques could be used in the context of the PPA, which is effectively an enormous data processing plant. Many quality improvement initiatives were also carried out and random sampling and statistical modelling were widely employed in a cross-departmental acceptance of the importance of the quantitative approach. More recently, extensive data mining has been undertaken to examine changes in the pattern of prescriptions over time as regards their value, content, source and mix with the aim of providing a foundation for process improvement.

### **10.5.2 Debt collection**

Slow payment of invoices is a big problem and is particularly difficult for smaller companies. A continuous improvement project at a local SME looked at the performance of the whole flow of the company from receipt of orders to receipt of payment ([Coleman et al., 2001](#)).

In common with many companies, the manufacturing plant had been intensely modernised and was working very efficiently. Payment of invoices, however, was very slow and variable between customers. To help improve this situation, data were collected and analysed. It was found that the Pareto principle applied with most customers paying within reasonable time and some delaying unacceptably.

The ideas of ED were discussed at a problem-solving team meeting. It was decided to see which factors would help speed up the payment of bills. It was noted from experience that it was better to phone after 2 p.m. and to avoid phoning on Fridays. The aim was to try to find the optimum strategy and improve the time to payment of bills.

Three 2-level factors were chosen for the designed experiment:

1. Written contact: send or do not send a letter
2. Phone contact: phone or do not phone
3. Timing of contact: 10 days after sending invoice or 30 days.

Eight trials were planned. The debtor companies were randomly assigned to one of the eight trials. They were dealt with according to the ED and the time before payment was recorded. The outcome variable was the time to payment. It was found that sending a letter and telephoning 10 days after sending the invoice was by far the best strategy. Applying this new strategy over the next few months, the time to wait for payment of bills was significantly reduced. Overall, the time from enquiry to payment was reduced from a mean of 110 days to a mean of 85 days. This reduction of 25 days is a significant improvement and could make the difference between staying in business and going out of business.

The key benefits of this exercise were introducing staff to the concept of logical problem solving. There were also major benefits from the team activity of setting up the experiment which involved identifying late payment as a problem, gathering information to quantify the problem, encouraging input from all the staff team, taking some action and showing a useful result. Even if the results are not particularly surprising, the designed experiment has the advantage of making it possible to quantify the effect of the new strategy so that the cost of writing and phoning can be justified. There are several shortcomings in this ED, such as the skewed distribution of the measurable outcome, but, nevertheless it shows that experiments can be useful in a service context. In this case study, designed experiments were used in the manufacturing plant and it was good for staff from all departments to share the methodology.

Managerial implications are that all staff can contribute to process improvement through quantitative analysis. The designed experiment provided more than just the measured outcome; an added bonus was that information was obtained as a result of the intervention and managers found out that many invoices were paid late because they were incorrect or had been lost in the post or had not been received for other reasons. The early intervention identified these problems so that they could be rectified. Lessons learned are that it is possible to improve the payment of invoices. Recent contact with the company revealed that currently less than 1% of invoices are being paid late, which is a marked improvement.

### **10.5.3 Emergency department performance**

Kolker (2008) describes a discrete-event simulation model of the patient flow in a hospital Emergency Department. Three metrics – per cent ambulance diversion, number of patients in the waiting room and upper limit length of stay (LOS) – were used to characterise the performance of the studied Emergency Department. A baseline simulation model, which represented the historical performance of the ED, was validated through the three performance metrics.

This case study had two main phases. The goal in the first phase was to utilise simulation and ED to create a response model that could be used to predict the metrics, such as percentage of ambulance diversion, as a function of the LOS for patients admitted as inpatients and LOS for patients admitted as outpatients (home patients). The goal in the second phase of the study was to determine an optimal ED closure criterion. ED closure would allow the ED to temporarily divert ED ambulance drivers to other hospitals in order to reduce the size of the queue in the waiting room. A factorial design was used to carry out the study in phase one.

Results of the experimentation performed on the simulation provided quantitative measures of the performance characteristics of the ED. Response Surface (RS) modelling illustrated that the per cent of ambulance diversions was negligible when LOS was less than 6 and 5 h for inpatient and home patient visits respectively. The ED closure criterion was when the number of patients in the queue was 11. Through the modelling of the ED department and use of historical data to drive the inputs, Kolker demonstrated how ED was beneficial in the context of analysis of the current system and how to use findings of the study to influence management decisions.

## 10.6 Role of computer simulation models within DOE

One of the difficulties in applying DOE in service and transactional businesses is that it is often difficult or impossible to physically experiment with the system under study. For example, suppose that we want to improve service operations in a hospital emergency department, the response variable may be patient waiting time, and there may be several factors that could be considered as factors in a designed experiment, including the number of personnel on duty, the mix of skills in the on-duty personnel, the number of treatment rooms, the types of treatment and diagnostic equipment available, the physical layout of the ED and the sequencing procedure that determines the order in which arriving patients are processed. Clearly some of these factors should have an effect on patient throughput and hence on waiting times. However, varying these factors in a designed experiment would be impractical and, in most instances, impossible. This situation is encountered in many improvement projects involving service and transactional operations. The Winter Simulation Conference held in December each year has a health care track that includes many simulation models of hospitals and health care systems. For examples of ED simulations that involve ED, see [Garcia et al. \(1995\)](#), [Miller et al. \(2003\)](#) and [Simon and Armel \(2003\)](#). Later in the paper, a case study is presented. The remainder of this section details the approach of experiments on computer simulation and some unique ED challenges.

The usual approach in these situations is to build a computer model of the process and then apply designed experiments to the model. If the model is built properly and validated, then results from the experiment conducted on the model can be transferred to the actual process. Broadly speaking, there are two types of computer models used in improvement activities: discrete-event simulation models and deterministic models. Discrete-event simulation models are usually transaction-based and driven by random components that are modelled by probability distributions. For example, in the hospital emergency department application, the number of patients (or transactions) that arrive per hour may be modelled by a Poisson distribution whose mean is time dependent; the type of complaint that the patient presents may be selected at random from a distribution that reflects the actual historical experience with patients; and the service time for each procedure that the patient undergoes could be modelled by an exponential or a gamma distribution (for example). Random numbers generated from these distributions move transactions through the system until they are either discharged or admitted to the hospital's general population. For an introduction to discrete-event simulation methods, see [Banks et al. \(2005\)](#).

Because discrete-event simulations are driven internally by random forces, they produce an output response that is a random variable. Consequently, the full range of standard ED methods, including factorial and fractional factorial designs and RS designs, can be applied to these models. [Hunter and Naylor \(1970\)](#) illustrate the uses of factorial, fractional factorial and RS designs in the context of two computer simulation models and provide a brief discussion about the pitfalls associated with computer simulation experiments.

Some practical problems that arise when experimenting on computer simulations include sample size determination, the issue of multiple responses and the problem of nonlinearity. Additional issues that are unique to computer simulation models include how to choose the simulation run length and the duration of the warm-up period (if any is required). See [Law \(2007\)](#) for a discussion of these and other related issues. Also, if replication is used, it is usually a standard practice to use a different stream of random numbers (or a different random number generator speed) for each replicate, so that replicates can be taken as blocks to reduce some of the variability in the model output.

Many discrete-event simulations have a large number of input variables. Depending on the simulation run length in real time, there can be situations where the number of factors renders the use of conventional fractional factorial designs problematic. Supersaturated designs, which have fewer runs than the number of factors, can prove useful in these situations. [Lin \(2000\)](#) is a useful reference on construction of supersaturated designs. Forward stepwise regression can be used to analyse the data from a supersaturated design. See [Holcomb et al. \(2003\)](#) for a discussion of other design construction and analysis methods. In some simulations there can be input variables that can be treated as noise variables. For example, in the hospital emergency department, the analyst may want to treat the patient arrival rate as a noise factor because it cannot be controlled in practice by the management of the emergency department, and it may be desirable to try to find settings of the factors that can be controlled that work well across a wide range of arrival patterns. Designs that incorporate noise factors and methods for analysing these designs to minimise the variability transmitted from the noise factors are discussed in [Myers et al. \(2010\)](#). Simulation models can present other challenges for the experimental designer. Often the output response cannot be summarised by a single summary statistic or group of summary statistics. Common situations are time series output or functional output in which one response is related to one or more other responses through a functional relationship. In many cases, the output response may be poorly modelled by a normal distribution. For example, in the hospital emergency room simulation, the patient waiting times may follow a gamma distribution. Since the gamma distribution is a member of the exponential family, generalised linear models may be useful in the analysis of these types of responses. For examples of using generalised linear models to analyse data from designed experiments, see [Lewis et al. \(2001\)](#) and [Myers et al. \(2010\)](#). If the experimenter knows or suspects in advance that the response is an exponential family member, it is possible to design an experiment based on the D-optimality criterion that is more appropriate than classical designs. This is discussed in [Johnson and Montgomery \(2009\)](#) and [Myers et al. \(2010\)](#).

## Exercises

1. What are the fundamental differences between manufacturing and service industries?
2. What are the challenges in the use of DOE in a service environment?

3. What are the benefits of DOE in a service sector?
4. What is the role of computer simulation models in the use of DOE within a service context?

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# Design of experiments and its role within Six Sigma

11

## 11.1 What is Six Sigma?

Sigma ( $\sigma$ ) is a letter of the Greek alphabet that has become the metric of process variation. The sigma scale of measure is correlated to other metrics of Six Sigma such as defects per million opportunities (DPMO), throughput yield, process capability indices ( $C_p$  and  $C_{pk}$ ), etc. Six is the number of sigma measured in a process, when the variation around the target is such that less than four outputs out of one million are defects under the assumption that the process average may drift over the long term by as much as 1.5 SDs.

Six Sigma was launched in the mid- to late 1980s by Motorola. It was the result of a series of changes in the quality area starting in the late 1970s, with ambitious tenfold improvement drives. The senior management along with CEO Robert Galvin formulated the goal of achieving Six Sigma capability by 1992 in a memo to all Motorola employees. In the wake of successes at Motorola, other leading electronic manufacturing companies such as IBM, DEC, Texas Instruments, etc. launched Six Sigma initiatives in the early 1990s. However, it was not until 1995, when GE and Honeywell (previously Allied Signal) launched Six Sigma as strategic initiatives, that a rapid dissemination took place in non-electronic industries all over the world (Hendricks and Kelbaugh, 1998).

The term Six Sigma may be defined in several ways. Some of the most prominent definitions of Six Sigma include the following:

- Six Sigma is a highly disciplined and statistically based approach for reducing/eliminating defects from processes, products and transactions, involving everyone in the corporation (Hahn, 1999).
- Harry and Schroeder (2000) defined Six Sigma as a business strategy and philosophy built around the concept that companies can gain a competitive edge by reducing defects in their industrial and commercial processes.
- Pande (2000) commented that Six Sigma is a comprehensive and flexible system for achieving, sustaining and maximising business success. It is driven by close understanding of customer needs and disciplined use of facts, data and statistical analysis.
- Pearson (2001) described Six Sigma as a programme that combines the most effective statistical and non-statistical methods to make overall business improvements.
- Treichler (2002) commented that Six Sigma is a highly disciplined process that helps organisations to focus on developing and delivering near-perfect products and services.
- Six Sigma is a business strategy that employs statistical, non-statistical, change management, project management and teamwork tools and skills to maximise an organisation's ROI through the elimination of defects in processes (Antony et al., 2006).

## 11.2 How Six Sigma is different from other quality improvement initiatives of the past

In the author's opinion, the following aspects of the Six Sigma business strategy are not accentuated in other quality improvement or continuous improvement initiatives of the past.

- Six Sigma provides a scientific and statistical basis for quality assessment for all processes through measurement of quality levels.
- Six Sigma places an unprecedented importance on strong and visionary leadership and the support required for its successful deployment.
- Six Sigma strategy places a clear focus on achieving measurable and quantifiable financial savings to improve the bottom line of an organisation.
- Six Sigma methodology integrates the most powerful and well-established quality and problem-solving tools and techniques in a disciplined and systematic manner.
- Six Sigma provides an organisational infrastructure showing clear roles and responsibilities for the people who are executing projects and delivering quantifiable results to the bottom line.
- In the author's opinion, DOE is a topic that is not taught properly to engineering and business school students across many universities. Six Sigma has been now proven to be a catalyst for teaching DOE to both engineers and managers in organisations today.
- Six Sigma focuses on the application of DMAIC (Define—Measure—Analyse—Improve—Control) (<http://www.isixsigma.com/methodology/dmaic-methodology/what-dmaic/>) methodology in the form of continuous or even breakthrough improvement projects compared to many other initiatives we have witnessed in the past.

## 11.3 Who makes Six Sigma work?

In any Six Sigma programme, a comprehensive knowledge of process performance, improvement methodology, statistical tools, processes of project team activities, deployment of customer requirements, etc. is needed. This knowledge can be cascaded throughout the organisation and become the shared knowledge of all employees only through a proper training scheme. Many companies who have introduced Six Sigma have adopted the following belt rank system from martial arts. These are the people within the organisation who can make Six Sigma work.

*Yellow Belts:* This is the lowest level of the belt system and gives a basic introduction to Six Sigma. The 2-day training programme covers fundamentals of Six Sigma, Six Sigma metrics, DMAIC methodology, some of the basic tools, the project selection process and critical success factors for Six Sigma deployment and is usually offered to people on the shop floor or to front-line staff members in a service organisation. Yellow Belts are expected to complete a continuous improvement project and demonstrate savings of at least £2500 to the bottom line of the business. The project should involve the application of at least two basic tools of Six Sigma taught in the training course.

*Green Belts:* Green Belts fulfil the roles of Process Improvement or Quality Improvement team members on full-time Black Belt projects. A Green Belt team member can come from any level within an organisation and provide subject matter expertise for a project. It is usually a 1- to 2-week course and is generally offered to middle management in an organisation. Six Sigma Green Belts are groomed in the Six Sigma DMAIC methodology which helps them to cascade Six Sigma tools and techniques throughout an organisation. Six Sigma Green Belts are required to complete a continuous improvement project based on Six Sigma tools and techniques demonstrating a benefit of approximately £30 k to the case study organisation.

*Black Belts:* Six Sigma Black Belts are team leaders responsible for implementing process improvement projects within an organisation to increase customer satisfaction levels and business productivity. Black Belts have typically completed 4 weeks of training and have demonstrated mastery of the subject matter through the completion of projects. They are required to complete one or two projects based on Six Sigma tools and techniques and should follow the DMAIC methodology, demonstrating a benefit of approximately £90 k to the bottom line of the business. The Black Belt course is advanced and comprehensive and aims to create full-time process improvement leaders in the business. A Black Belt should demonstrate team leadership, understand team dynamics and assign team member roles and responsibilities. Black Belt candidates are selected from the very best young leaders in any organisation.

*Master Black Belts:* Six Sigma Master Black Belts (MBBs) are change agents who lead Lean Six Sigma projects at an enterprise level. Their efforts include deployment, training, coaching, mentoring and providing technical support to Green Belts and Black Belts. An MBB has Black Belt qualifications and is selected from Black Belts who have a great deal of experience with project activities. Six Sigma MBBs should have good presentation and leadership skills. They constantly monitor the Six Sigma performance in their organisation and ensure that its practices are consistently followed by all the underlying departments in their true sense. In some organisations, MBBs also hold the role of champions. In others, they are more inclined towards coaching roles and assist champions in the company who represent its top-level hierarchy.

### **11.3.1 Six Sigma deployment champions**

Six Sigma Deployment Champions focus on providing an organisation with the managerial and technical knowledge to facilitate the leadership and deployment of the Six Sigma strategy. Champions are upper-level managers who lead the execution of the Six Sigma deployment plans for the company. Guided by the direction set forth by the executive team, champions select the projects, determine who is trained as a Black Belt or a Green Belt, review progress and mentor the Black Belts and Green Belts in order for the deployment to be effective. One of the Champion's primary roles is to assure that operational-level projects are aligned with the strategic-level business objectives. Project reviews should be conducted by Six Sigma Champions not as a tool to manage Black Belts but to ensure that the project

is progressing as planned and that the result will produce a result that resembles (and aligns with) the needs of the organisation. A Six Sigma Deployment Champion course is usually 2 or 3 days, and it concentrates on how to guide the overall Six Sigma programme, how to select good improvement projects and how to evaluate the results of improvement efforts.

## 11.4 Six Sigma methodology (DMAIC methodology)

The DMAIC methodology is the driving force behind Six Sigma process improvement projects. This methodology is used only for improving existing processes. If the existing processes cannot be improved further, then one has to think about redesigning them using the so-called DFSS methodology. The explanation of DFSS methodology is beyond the scope of this book. DMAIC methodology works equally well for tackling undesirable variation in processes, longer cycle times of processes, poor throughput yields, high costs of poor quality, etc. The following section describes the five stages of the methodology in detail.

### 11.4.1 Define phase

In the Define Phase, we need to identify the process where the problem lies; this is followed by a proper definition of the problem. In this phase, it is important to justify the use of Six Sigma methodology. If the solution to the problem is unknown to the team and its members, then it is a good candidate for Six Sigma. In the Define Phase, one may have to develop the project charter, which is a living document throughout the life of the project. The project charter may be revised from time to time, especially when the team collects data, in order to provide a good understanding of the problem. The project charter should include the following elements:

- The Problem Statement – The purpose of the problem statement is to clearly describe the problem at hand and to provide important details of the problem's impact on the organisation.
- The Goal Statement – This element defines the results expected from the project. This should include the targets to be achieved, savings expected from the project, how CTQs will be impacted, etc.
- Project Scope – Every project should have some boundaries and these must be clearly understood at the outset of the project.
- Cost of Poor Quality – This indicates how much the problem has cost the organisation over a period of 1 year and assists the team to understand the impact of the problem in financial terms.
- Risk Assessment – There is always a risk associated with the execution of any project and hence it is absolutely critical to evaluate the potential for these and to develop strategies to mitigate such risks.

### **11.4.2 Measure phase**

In this phase, it is important to baseline key performance measures associated with the problem. The objective of this phase is to garner as much information as possible from the current process. The improvement team needs to know exactly how the process operates and is not concerned with how to improve the process at this time. The important tasks in the Measure Phase are the creation of a detailed process map, collection of baseline data and summarising the collected data. In most projects, the process map will be completed first. The process map provides a visual representation of the process under investigation. It can also provide additional awareness of process inefficiencies such as cycle times and bottlenecks or identify non-value-added process requirements. The process map may also show where data can be collected.

One of the things which is not heavily emphasised in this phase is the quality of data one may collect to baseline the process performance. The author strongly recommends the use of Measurement System Analysis (MSA) to verify the measurement system so that reliable data can be collected for analysis in the next phase.

### **11.4.3 Analyse phase**

In this phase, the team sets out to identify the root cause or causes of the problem being studied. But unlike other simpler problem-solving strategies, DMAIC requires that the root cause be validated by data. One can use tools such as Brainstorming, 5 Whys, and the Fishbone Diagram, also known as a Cause and Effect Diagram or an Ishikawa Diagram, to understand the potential causes of the problem. In the Analyse Phase, one has to validate the root causes of the problem; here it is advised to use statistical tools such as hypothesis testing, correlation analysis, regression analysis, ANOVA, etc. The Analyse Phase of the Six Sigma methodology focuses on why errors, defects or excessive variation occur, which often result from one or more of the following:

- failure to understand the capability of a process to meet specifications
- poor instrument calibration and testing
- inadequate control on environmental factors such as temperature, noise, humidity, pressure, etc.
- lack of control of materials and equipment used in a process
- lack of training
- lack of knowledge about how a process works, etc.

### **11.4.4 Improve phase**

Once the root causes of a problem are understood, the team needs to generate ideas for removing or resolving the problem and improve the performance measures and CTQs. Brainstorming is commonly used to generate an abundance of potential solutions. It is a great idea to include people who perform the process regularly.

Their input to solution creation can be invaluable; they may also provide the best potential solution ideas because of their process knowledge. In fact, it is an excellent idea to communicate to those involved in the process on a regular basis throughout the improvement project.

At times, we come up with a number of ideas from brainstorming and we need to evaluate them and select the most promising. This process includes confirming that the proposed solution will positively impact the key process variables and the CTQs. In order to understand the relationship between the set of key process variables and the CTQs, one can utilise DOE: it is one of the most powerful techniques that can be employed in the Improve Phase of Six Sigma methodology.

#### **11.4.5 Control phase**

The purpose of the Control Phase is to sustain the gains that were achieved as a result of the Improve Phase. This phase is initiated by ensuring that the new process conditions are documented and monitored via SPC methods. One may have to establish the new procedures, train the workforce on the new procedures or methods adopted, institute controls to make sure that improvements can be maintained over time, document the control plans etc. Moreover, one may have to develop new metrics to verify the effectiveness of new processes and determine if the lessons learned can be transferred to other processes in the business.

### **11.5 DOE and its role within Six Sigma**

We have already seen from the above section that DOE has a clear role in the Improve Phase of the Six Sigma methodology. However, the author of the book has observed that the applications of DOE have increased significantly since the ‘post-Six Sigma’ years. Some pioneering work on this topic was carried out by Professor Goh ([Goh, 2002](#)) on this topic. Developments in the deployment of DOE for quality purposes may be viewed in terms of ‘labelled’ methodologies that quality practitioners and managers have faced over the last few decades. [Table 11.1](#) gives an approximate timeline for the appearance of these methodologies where the year given refers to the time around which there was clear evidence of acceptance and popularity of the named methodology.

In a Six Sigma programme, DOE is very useful in terms of verifying the cause-and-effect relationships between the CTQ(s) and the critical few factors that drive the process under study. Multi-vari studies are also used in Six Sigma to identify sources of variation due to process variables whose effects are to be verified through the application of DOE. Six Sigma makes use of statistical thinking to integrate established management and statistical tools into the DMAIC approach to customer-oriented quality improvement. DOE is primarily used in the Improve Phase of DMAIC for evaluating the impact of key process parameters that influence the CTQs. DOE also plays a crucial role in the design of Six Sigma methodology. DFSS utilises a different methodology

**Table 11.1** Approximate chronology of applied DOE.

<b>When (circa)</b>	<b>How (label)</b>	<b>Why (focus)</b>	<b>Who (users)</b>	<b>Where (environment)</b>
Traditional 1975	One Factor at a Time Shainin methodology of experimental design	Study known factors Search for unknown factors and classify them as Red X, Pink X and Pale Pink X	Scientists Technicians	Laboratories Shop floor
1980	BH <sup>2</sup> methodology (Box, Hunter and Hunter)	Improve process performance through optimisation strategies	Statisticians	Production
1985	Taguchi methods	Reduce variation in the functional performance of products/processes	Engineers	Operation
1990	Robust design	Minimise cost	Managers	New product development process
1995	Six Sigma	Maximise business profitability	CEOs and business leaders in organisations	Company-wide

*Source:* From, Goh, T.N., 2002. The role of statistical design of experiments in Six Sigma: perspectives of a practitioner. Qual. Eng. 14 (4), 659–671.

such as Define—Measure—Analyse—Design—Optimise—Verify. DOE can be very useful in the Define and Optimise Phases of the above methodology in terms of understanding the critical design parameters which affect the design performance of products/services. Moreover, one has to reduce the number of design parameters to a manageable number and tolerances must be set on those ones which are verified to be critical to customers. Because of Six Sigma initiatives in many organisations, the author has observed that DOE is now enforced by top management and executed by engineers with Black Belt training. Moreover, recently DOE has gained the attention of many senior managers in service organisations in terms of better understanding of their core business processes and how to optimise them for fewer customer problems and improved customer experience.

Although DOE was viewed by many practitioners as a stand-alone technique in the past, it will no longer be treated as one because of the Six Sigma and DFSS methodologies adopted by a large number of world-class companies today. The contrast between the way DOE was used in the past and the way it can be expected to be deployed in the future as part of the Six Sigma or DFSS initiative is outlined in [Table 11.2](#). While the theoretical basis of DOE remains the same, the applications of DOE within the Six Sigma context will continue to grow exponentially and may even make use of Six Sigma methodologies even more widespread than before.

It is evident that the DOE technique demands generation of data for analysis and that data mining can play a major role in achieving this. Indeed, the data mining approach is already apparent in multi-vari studies in the Analyse Phase of Six Sigma, where searches are conducted through available data for significant noise or uncontrolled variables. [Table 11.2](#) clearly demonstrates that DOE will continue to be a primary driver for the success of many process optimisation and understanding problems in the twenty-first century. The author foresees its wider and broader applications in the context of Six Sigma for many more years to come.

**Table 11.2** Deployment of DOE (pre- versus post-Six Sigma).

Feature	Past (pre-Six Sigma)	Future (post-Six Sigma)
Source of impetus	Operations level	Senior management/executives
Training effort	Stand-alone courses	Structured programs
Motivation for study	To improve process performance	To improve customer experience
Guiding principles	Analytical requirements	Statistical thinking
Application mode	Localised	Organisation-wide
Project selection	Single function problems	Cross-functional concerns
Areas of investigation	Primarily manufacturing problems	Manufacturing/service/transactional problems
Deployment leadership	Led by industry statisticians	Led by Black Belts or MBBs
Performance indicators	Statistical parameters (SD, mean, capability, etc.)	Financial impact
Success criterion	Engineering objectives	Business bottom line

*Source:* From, Goh, T.N., 2002. The role of statistical design of experiments in Six Sigma: perspectives of a practitioner. Qual. Eng. 14 (4), 659–671.

## Exercises

1. What is your understanding of the term Six Sigma?
2. What makes Six Sigma different from other quality improvement initiatives?
3. What is the role of Six Sigma Deployment Champions in an organisation?
4. What is the role of the Measure Phase in Six Sigma methodology?
5. What are the five fundamental differences in the deployment of DOE for pre- and post-Six Sigma initiatives within an organisation?

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# Design of Experiments in the service industry: a critical literature review and future research directions

12

## 12.1 Introduction

Design of Experiments (DoE) methodology refers to the use of practical and powerful statistical tools and techniques for the development of efficient, balanced and economical experimental designs that allow the experimenter to determine how controlled and uncontrolled factors are related to the process output(s) (Montgomery, 2017). The different designs created with this methodology allow inferences with high confidence levels, which make DoE a powerful tool for managing process inputs in order to optimise process outputs. In the 1980s DoE was integrated into Motorola's Six Sigma approach as a practical quality tool for reducing variation and improving performance (Kubiak and Benbow, 2009).

During the last six to seven decades, DoE has been extensively applied in the manufacturing industry. A bibliographical review of DoE applied in the field of engineering was carried out by Ilzarbe et al. (2008), which found 77 papers published between 2001 and 2005. Nowadays, the number of publications on DoE in the manufacturing industry continues to increase (Brito et al., 2016; Mia et al., 2018; Oliveira et al., 2019). Nevertheless, when it comes to the non-manufacturing industry or service industry, there is still a lack of experimental design applications (Antony et al., 2010). With the introduction of Six Sigma in the service industry, DoE has been used by black belts, master black belts and other professionals as a support tool in the improvement phase of the define, measure, analyse, improve and control approach (Arafeh et al., 2014). However, the use of DoE is still infrequent in the literature and even more so with respect to case studies focused exclusively on this methodology.

In this chapter, a critical review of the literature on applications of DoE in the service industry was conducted out in order to identify challenges and opportunities in the service industry. For practitioners such as senior managers or process managers, the practical application of experimental design in their field of business can serve as inspiration, and it enhances the dissemination of the methodology as reported in Bell et al. (2006). From the academic point of view, this study can serve to identify research gaps that will enable progress in applying the DoE methodology in the service industry.

The rest of the chapter is organised as follows. [Section 12.2](#) describes the method followed to carry out the critical literature review (CLR) in this study, including the type of search, inclusion criteria and research questions. [Section 12.3](#) presents the key findings from the state-of-the-art literature in both quantitative and qualitative terms, followed by the discussion and implications in [Section 12.4](#). Finally, the limitations and directions for further research are presented in [Section 12.5](#).

## 12.2 Methodology

A CLR was carried out which is a careful investigation of the main ideas and relationships of a topic and includes a critique of the existing literature ([Torrao, 2005](#)). A CLR is defined by [Fernandez \(2019\)](#) as “a detailed analysis and assessment of the strengths and weaknesses of the ideas and information in written text”. [Fernandez \(2019\)](#) points out the following aspects of a strong CLR: (1) it demonstrates that the authors are knowledgeable about the previous work on the topic(s); (2) it identifies research gaps; (3) it develops precise research questions for further research; (4) it positions empirical articles with respect to the prior literature and (5) it develops theory.

The present CLR was conducted based on the aforementioned concepts and included quantitative and qualitative analyses. The inclusion criteria were the following:

- Source and databases used for search: Google Scholar, Scopus, Web of Science, Emerald and Science Direct.
- Time period: 1994–2019.
- Document type: peer-reviewed journal articles.
- Language: English.
- *The papers must present a case study on DoE in a service industry.*

Several papers were identified in the Scopus, Web of Science and Google Scholar databases and many referred to randomised controlled trials (e.g., drug testing, psychological experiments and other studies from the medical field). These papers were not of interest to this particular review and, therefore, were excluded. This CLR instead focused on instances where classical DoE (such as factorial or fractional factorial designs), Taguchi or response surface methodology (RSM), which is an advanced DoE approach to process optimisation, were applied.

For the quantitative analyses, the following aspects were analysed: year of publication, country of author affiliation, journal type, service industry where DoE was applied, number of physical versus simulation-based experiments, number of replications carried out, DoE strategies, experimental designs, number of factors studied in given experiment, levels where factors were studied and quality characteristics of interest.

Regarding the qualitative analysis, three research questions were addressed, which included the following:

1. What are the critical success factors (CSFs) for DoE in the service context?

2. What essential skills should service quality or process improvement managers and experts/specialists in organisations need to have in order to use DoE?
3. What are the key lessons learned from using DoE in the service industry?

## 12.3 Key findings

At the end of the search phase, 26 articles from 23 different journals were selected for the CLR. The 26 selected papers presented 29 practical DoE applications in the service industry. One of the papers (Aslan, 2015) described four different DoE applications in healthcare, while each of the other papers presented only one application. Table 12.1 presents the author(s), year of publication, country of author affiliation, service industry studied, DoE strategy and design type used for each article. Fig. 12.1 shows that 18 articles were published in the last 10 years, three papers were published in the 1990s, and four studies were published between 2000 and 2010. As shown in Fig. 12.2, most of the papers were published by researchers in the United States (26.7%), followed India (10%), the United Kingdom (10%), Taiwan (6.7%) and Canada (6.7%). Each of the remaining countries represented 3.3% of the total. It is important to highlight that some papers were authored by researchers in different countries. It was also observed that there is a lack of publications on DoE in the service industries within three continents—Australia, South America and Africa. With regard to the different service industries, Fig. 12.3 shows that DoE was applied most in healthcare (27.6%), followed by retail (24.1%), logistics (17.2%), education (10.3%), marketing (10.3%), after sales (6.9%) and catering (3.4%).

### 12.3.1 *Experimentation environment and number of replications*

Discrete event simulation is usually applied when real experimentation is expensive or unfeasible to conduct (Banks et al., 2010; Baril et al., 2019; Law, 2015). Even though this situation is quite common in the service industry, about 62.1% of the studies used physical experimentation rather than simulation-based experiments, as presented in Fig. 12.4.

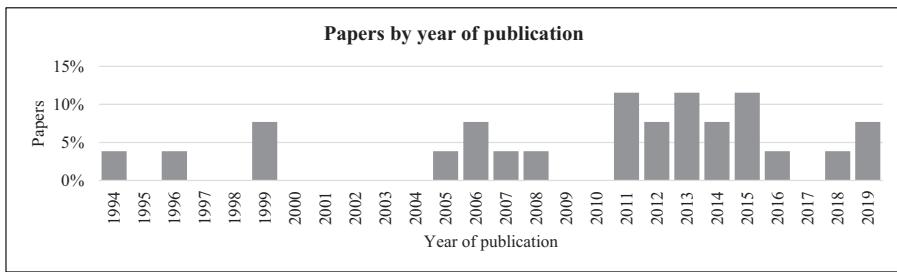
Many of the studies (34.5%) failed to provide information on the number of replications. In Fig. 12.5, the first column includes all of the papers that did not replicate the experiment (24.1%), which means that the experiment was executed only once. On the other hand, the column referred to 5000 or more replications is related to the work of Bell et al. (2006) on direct mail sales. It was also observed that the experiments with 50 (Chuang and Oliva, 2015) and 30 (Baril et al., 2019; Zhao et al., 2015) replications used simulation to carry out the experiments. Simulation provides the advantage of easily replicating experiments compared with physical experiments (Law, 2015).

**Table 12.1** Papers selected for the critical literature review and service industries.

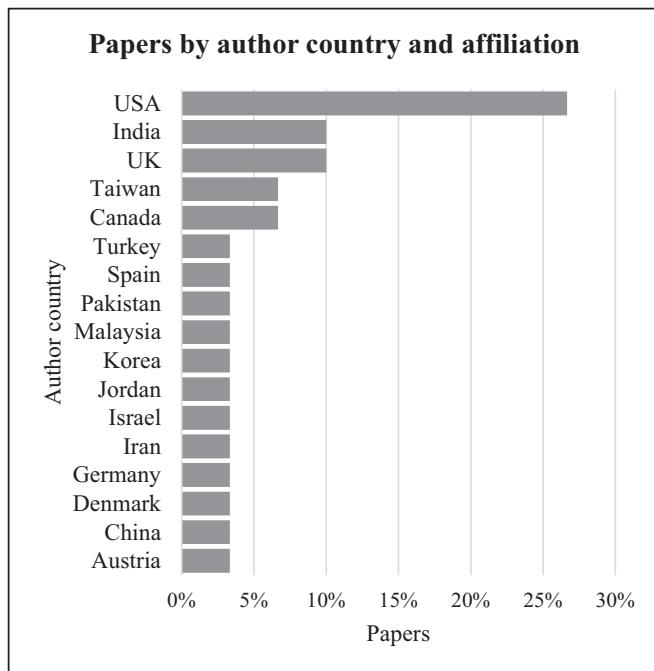
No.	Author(s) and year of publication	Author affiliation	Service industry(s)	DoE strategy	Design type
1	<a href="#">Holcomb (1994)</a>	United States	Logistics (customer service)	Taguchi	Orthogonal
2	<a href="#">Kumar et al. (1996)</a>	United States	After sales (complaint correction process)	Taguchi	Orthogonal
3	<a href="#">Krishnamoorthy and Kapadia (1999)</a>	India	Catering business (catering business)	Taguchi	Orthogonal
4	<a href="#">Blosch and Antony (1999)</a>	United Kingdom	Logistics (military operations)	Taguchi	Orthogonal
5	<a href="#">Tsang and Tse (2005)</a>	China	Marketing (web interface promotion)	Classical DoE	Full factorial
6	<a href="#">Bell et al. (2006)</a>	United States and Austria	Marketing (direct mail sales)	Screening and Classical DoE	Plackett–Burman and Full factorial
7	<a href="#">Ledolter and Swersey (2006)</a>	United States	Marketing (direct mail response)	Classical DoE	Fractional factorial
8	<a href="#">Kukar-Kinney and Grewal (2007)</a>	United States	Retail (product choice)	Classical DoE	Full factorial
9	<a href="#">Raajpoot et al. (2008)</a>	United States and Pakistan	Retail (customer choice)	Taguchi	Orthogonal
10	<a href="#">Dehlendorff et al. (2011)</a>	Denmark	Healthcare (surgical unit)	New strategy (proposal)	Split-plot
11	<a href="#">Kaner et al. (2011)</a>	Israel	Logistics (customer order handling process)	Classical DoE	Full factorial
12	<a href="#">Chen and Ou (2011)</a>	Taiwan	Retail (sales forecasting)	Taguchi	Orthogonal

13	<a href="#">Shahin et al. (2012)</a>	Iran	Logistics (airport services)	Taguchi	Orthogonal
14	<a href="#">Sharma and Garg (2013)</a>	India	After sales (automobile service centre)	Taguchi	Orthogonal
15	<a href="#">Chackelson et al. (2013)</a>	Spain	Retail (distributor)	Classical DoE	Full factorial
16	<a href="#">El-Banna (2013)</a>	Jordan	Healthcare (patient discharge process)	Classical DoE and Response Surface Method	Full factorial and Central Composite Design (CCD)
17	<a href="#">Mishra and Gangele (2013)</a>	India	Retail (outlets)	Taguchi	Orthogonal
18	<a href="#">Ree et al. (2014)</a>	Korea	Education (lecture quality)	Taguchi	Orthogonal
19	<a href="#">Antony et al. (2014)</a>	United Kingdom	Education (student satisfaction)	Classical DoE	Full factorial
20	<a href="#">Aslan (2015)</a>	Turkey	Healthcare (emergency ulcer, body films and breast cancer)	Classical DoE	Full factorial
21	<a href="#">Chuang and Oliva (2015)</a>	Taiwan and United States	Retail (inventory record)	Classical DoE	Full factorial
22	<a href="#">Zhao et al. (2015)</a>	Canada	Healthcare (emergency department)	Classical DoE	Full factorial
23	<a href="#">Galankashi et al. (2016)</a>	Malaysia	Logistics (petrol station queueing system)	Classical DoE	Full factorial
24	<a href="#">Bleier et al. (2019)</a>	Germany and United States	Retail (web page design)	Taguchi	Orthogonal
25	<a href="#">Antony et al. (2019)</a>	United Kingdom	Education (teaching effectiveness)	Screening	Plackett–Burman
26	<a href="#">Baril et al. (2019)</a>	Canada	Healthcare (ambulatory)	Classical DoE	Full factorial

DoE, Design of Experiments.



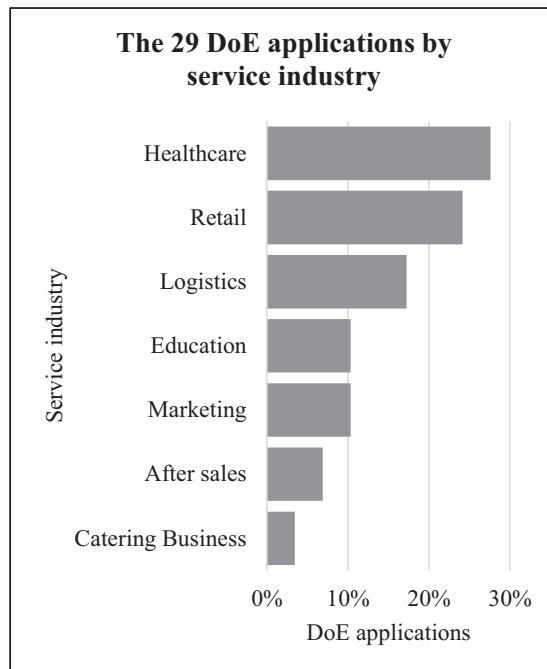
**Figure 12.1** Papers by year of publication.



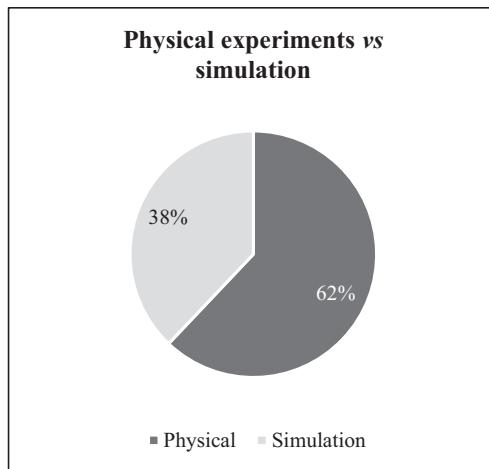
**Figure 12.2** Papers by author country of affiliation.

### 12.3.2 Design of Experiments strategies and designs

According to [Tanco et al. \(2008\)](#), DoE strategies can be classified into three main approaches: the classical approach, Taguchi approach and Shainin approach. The classical approach, in particular, includes the general strategy, screening strategy and RSM. In this article, the term “classical DoE” refers to the general strategy that is usually applied to determine the most significant factors that affect the responses of interest. The screening strategy is similar to

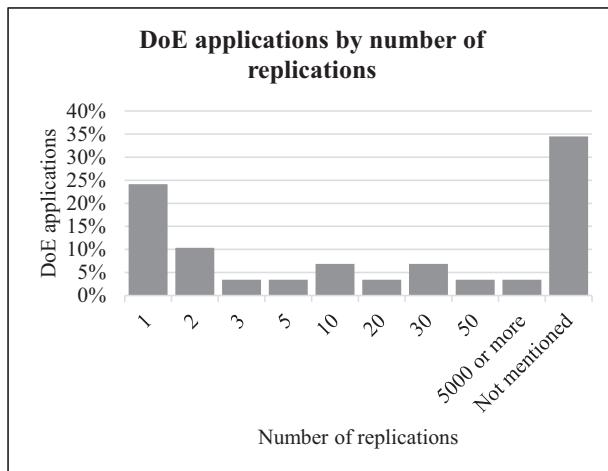


**Figure 12.3** The 29 DoE applications by service industry. *DoE*, Design of Experiments.

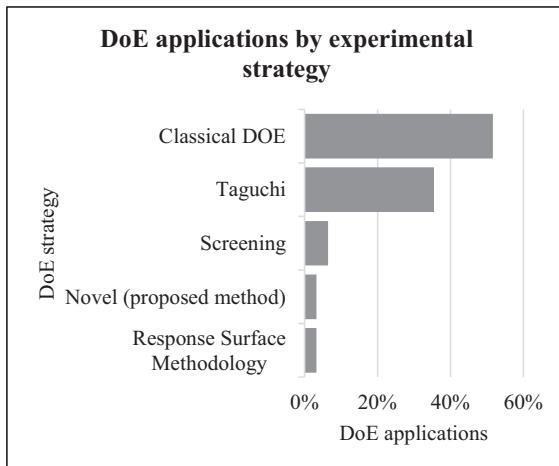


**Figure 12.4** Physical experiments versus simulation.

the classical strategy, but it has the additional aim of reducing the number of factors. Therefore the screening strategy and RSM were separated from the classical approach in order to quantify the strategies employed by the analysed



**Figure 12.5** Papers by number of replications.



**Figure 12.6** Papers by DoE strategies. *DoE*, Design of Experiments.

papers and provide more specific information. Fig. 12.6 shows that the most used strategy was the classical DoE (51.6%), followed by the Taguchi method (35.5%), screening method (6.5%), RSM (3.2%) and a new method proposed by Dehlendorff et al. (2011) (3.2%), which is based on split-plot designs. Fig. 12.7 indicates that the number of experimental designs matches the DoE strategies used in the papers. There is a clear preference for full factorial designs when using the classical DoE strategy.

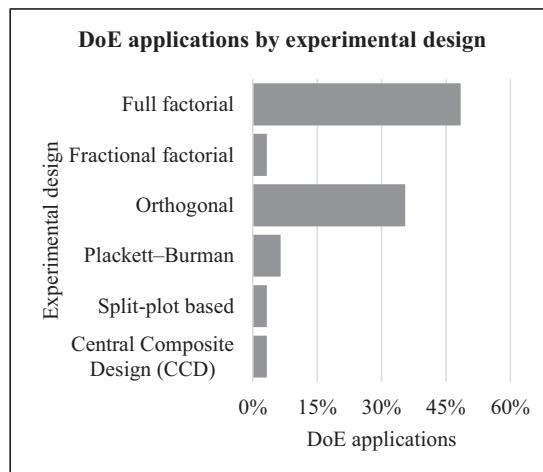


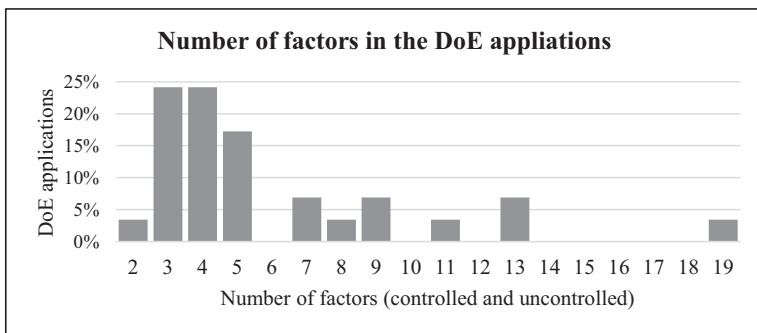
Figure 12.7 Papers by experimental designs.

### 12.3.3 Number of factors, levels and quality characteristics

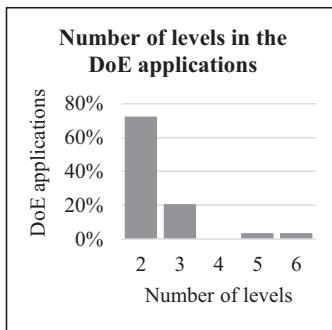
In 66.7% of the case studies, the number of factors were less than or equal to five, as shown in Fig. 12.8. The studies that included more than 10 factors used either the screening strategy (Antony et al., 2019; Bell et al., 2006) or the Taguchi method (Bleier et al., 2019; Shahin et al., 2012) to identify the most significant factors. Some experimenters utilised Plackett–Burman designs to separate out the vital few factors from the trivial many. It is important to note that the purpose of screening is not only to identify the most important factors but also to understand which factors are unimportant so that they can be removed from the subsequent rounds of experimentation. This aspect has a significant impact on cost savings, as managers can keep the unimportant factors at their most economic levels. Another observation was that 72.4% of the DoE applications used two levels and 20.7% used three levels (Fig. 12.9), which required a reduced number of experiments. Only two studies used more than three factors. In Chen and Ou (2011), there was a factor with six levels, and in El-Banna (2013), five levels were used in a central composite design (CCD). From a qualitative point of view, although both benefits and practical findings are very specific to each application, it was possible to address the research questions regarding the success factors, essential skills and key lessons learned from the DoE applications in the service industry. Such information is presented in the following sections.

### 12.3.4 Critical success factors

Although the aforementioned CSFs are strongly recommended for industrial designed experiments carried out in the service industry, only a few of these factors were



**Figure 12.8** Number of factors in the studies.



**Figure 12.9** Number of levels.

reported in the papers selected for this critical review. Many authors mentioned that one of the most critical factors for successfully applying DoE techniques is the correct identification of which characteristics must be measured and how to measure them with accuracy, precision and less bias (Antony et al., 2014; Holcomb, 1994; Kaner et al., 2011; Krishnamoorthy and Kapadia, 1999; Kumar et al., 1996).

Choosing an appropriate experimentation strategy is also considered critical by many authors. It is especially important when testing many factors at the same time. Many of the studies chose to use screening designs (e.g. Plackett–Burman design), fractional factorial, or Taguchi orthogonal array (OA) to identify the most important factors (Antony et al., 2019; Bell et al., 2006; Bleier et al., 2019; Krishnamoorthy and Kapadia, 1999; Kumar et al., 1996; Ledolter and Swersey, 2006; Raajpoot et al., 2008; Shahin et al., 2012). For Sharma and Garg (2013), the use of Taguchi's OA designs also saved computational time in the simulation, which reinforces the importance of choosing the correct experimental design. Finally, conducting confirmatory experiments (Chen and Ou, 2011; Krishnamoorthy and Kapadia, 1999; Ree et al., 2014; Sharma and Garg, 2013) is also reported to be a very important CSF for industrial experiments.

### 12.3.5 Essential skills required for professionals

Some of the essential skills required for service quality or process improvement managers are *planning skills, statistical skills, teamwork skills and technical skills* ([Antony et al., 2014](#)).

- *Planning skills*: These are important for recognising the significance of experimentation for a specific problem, for estimating the time, budget and number of people necessary to carry out the tests and to establish the responsibilities of each team member.
- *Statistical skills*: They are essential in order to correctly analyse the results of the experiment. Concepts such as the importance of replication, blocking and randomisation, statistical significance, along the correct interpretation of statistical results are indispensable.
- *Teamwork skills*: Such skills are related to the company-wide comprehension about the benefits of DoE methods and the cooperation and support from all of the team members.
- *Technical skills*: They consist of having the necessary knowledge about the specific service under analysis. Such knowledge is key to define the controlled and uncontrolled factors the need to be analysed, their levels, the range that they can be varied and the most appropriate quality characteristics to be measured, among others. However, none of the analysed papers in the literature provided information on the essential skills required for service quality professionals to be able to apply DoE in the service industry. This is a major gap in the existing literature which needs to be addressed in the future research. In addition to the skill set required for service quality professionals, it is also important to understand the competencies required for both quality and continuous improvement professionals who are keen to implement this powerful technique in any service domain.

### 12.3.6 Key lessons learned from designed experiments

The lessons learned by most authors were related to the case study in particular, but not to the issues faced while conducting the experimental design project. Nor was any information found about organisational learning from experimental activities. [Antony et al. \(2014\)](#) reported that one of the limitations of their study in higher education was that the experiment was confined to one 24-hour module and the number of students who participated in the experimentation was relatively small. For this reason, the authors planned to extend the study to more modules. In the marketing sector, [Bell et al. \(2006\)](#) stated that, after the screening and the full factorial designs, the marketing team learned more than they had previously when using the one variable at a time experimentation strategy. It showed the power of analysing not only the main effects but also investigating the interactions among the factors.

## 12.4 Discussion and implications

This section discusses the articles reviewed from two points of view. First, the results from a methodological point of view (e.g. planning, sequencing, metric and experimental design selection and results obtained) are presented. It allows us to

highlight two research topics: first, if there are common methodological aspects that characterise the applications of DoE in the service industry and to find methodological difficulties or knowledge gaps, if they exist. Second, the results are discussed from a more practical point of view such as capacities needed to carry out the experiments, resources involved and results obtained in terms of individual and organisational learning. In this case, this analysis can help to assess the suitability and interest of organisations in applying DoE methodology as a tool for learning and improving service processes.

Much of the success when applying DoE has its origin in the proper planning of the experiments. The planning phase is a very important stage and must begin in the initial stage of any experiment. This stage includes the way in which the problem is approached in terms of previous knowledge of the problem, available resources, time available to carry out the experiment, equipment for the experiment, knowledge of the team and existing limitations, among other aspects. In the articles reviewed, this type of information is generally lacking. Focusing only on the numerical results of the experiments makes it difficult to understand the importance of having an adequate strategy when solving complex problems through experimentation. Likewise, this lack of information prevents both the importance of the findings and their sustainability over time from being evaluated.

The sequencing of experiments is usually part of the strategy followed in order to achieve the proposed objectives related to the problem under study. Trying to solve a complex problem through the application of a single experiment is rarely successful no matter how well the experimental design has been chosen. Only a few of the articles analysed presented sequencing in the experimentation process. However, it is important to have case studies that cover the whole experimentation process and show which tactics were used to achieve the proposed objective in each case. From the perspective of knowledge contribution, in case studies it is more interesting to delve into the strategy and tactics used to tackle a problem rather than only the resolution, particularly when the resolution does not present novel mathematical difficulties.

Regarding the selection of the most suitable metrics and designs for experimentation, [Section 12.3.2](#) detailed the most frequently chosen designs. The articles analysed described the use of metrics that are more subjective than objective as challenges. Sometimes these types of metrics make it difficult to reach to an acceptable conclusion. From author's point of view, it could be convenient in scenarios like this for researchers to perform an attribute agreement analysis and use Kappa statistics to assess the degree of assessment of the nominal or ordinal ratings made by multiple appraisers when the appraisers evaluate the same samples. This consideration, which is not specific to the service industry but is more characteristic of it, is an interesting research challenge from an academic point of view. Moreover, the fact that there are statisticians that go deeper into the knowledge of a specific area can help to resolve some of the uncertainties linked to the analysis and treatment of the subjectivity and variability of the responses.

As far as the validation of experimental results are concerned, only five articles reported the validation of the results with new experiments, three of which did so

by presenting simulation-based experiments. Chen and Ou (2011) simulated five confirmation experiments and proved that the factor levels selected were significant and suitable. Galankashi et al. (2016) also simulated five confirmation tests, where all the values for the runs were within a 95% prediction interval built from the previous runs. Sharma and Garg (2013) used the optimal level of the design parameters to predict and verify the improvement of the quality characteristic and observed that the performance increased using the optimal levels. In the food industry study by Krishnamoorthy and Kapadia (1999), the optimised recipe was used two times for confirmation, and the results closely matched the prediction from the model. Lastly, in the higher education context, Ree et al. (2014) gave six new lectures to verify the results of the previous experiments, which confirmed their results and resulted in higher teaching satisfaction.

Concerning the type of design chosen for experimentation, most authors were very clear in explaining their reasons for selecting one experimental design or another. The authors that opted for full factorial designs usually mentioned the importance of this type of design for studying all the possible combinations of controlled factors and their respective interactions (Antony et al., 2014; Chuang and Oliva, 2015; Galankashi et al., 2016). On the other hand, Taguchi designs were mostly chosen when the authors needed to test controlled and uncontrolled factors (Dehlendorff et al., 2011; Holcomb, 1994; Raajpoot et al., 2008; Ree et al., 2014; Shahin et al., 2012). Taguchi designs were also used to reduce the number of experiments required to test too many factors (Bleier et al., 2019; Krishnamoorthy and Kapadia, 1999; Sharma and Garg, 2013). Plackett–Burman design was chosen by Bell et al. (2006) and Antony et al. (2019) because it allowed the study of many factors' effects in just a few runs. El-Banna (2013) used a CCD in order to obtain the response model and optimise it. Additionally, when it comes to the RSM, the results are significantly different from the manufacturing industry, where the RSM is widely used (Oliveira et al., 2019). One of the reasons may be that many of input factors are continuous in the manufacturing industry, which suits the possibility of developing regression models linking continuous output(s) with controllable variables which are quantitative in nature (Myers et al., 2016).

One of the main objectives of organisational learning is for organisations to improve the effectiveness of their collective action enabling the organisation to remain competitive in a changing economic and industrial context. From a practical point of view, the articles analysed present little information in general on teamwork, essential skills and learning. Experimentation as a method for learning from processes could be considered a key aspect of organisational learning. As such, it should be properly documented and recorded in order to improve the individual competence of workers and structures, routines and methods of coordination of work teams in future experimentation processes.

The papers analysed from the existing literature did not clarify some of the key questions that practitioners need answers in order to conduct designed experiments in their service processes or systems. The first question usually asked by managers is about the cost and time needed for a project, yet almost none of the papers provided such information. In other words, the cost-benefit analysis has been missing in almost all case studies. In addition to that, most case studies did not report the financial savings generated from

the execution of designed experiments except for the study by [Krishnamoorthy and Kapadia \(1999\)](#), where the authors reported a 58.4% reduction in cost (from US\$ 192.50 to US\$ 80.00 per week). [Antony et al. \(2019\)](#) reported that their experiment took considerable time to plan, design, conduct and analyse, but most experimenters failed to present the time scale for each phase in the execution of the project from start to finish. In addition to this, none of the case studies executed any sort of risk analysis associated with DoE projects in the current literature on service industry.

The implications of this study have two parts. The first part will be looking into the usefulness of the findings for service quality management as well as operational excellence (OPEX) professionals in the service sector. The results of this study can be invaluable for many service quality professionals who are engaged in continuous improvement projects in terms of understanding the skills required, CSFs for implementation of DoE in the service sector, benefits that can be gained from the use of DoE in the service industry and so on. Moreover, senior managers need to understand their roles and responsibilities before they invest on DoE. The fundamental problem is that many senior managers in the service industry perceive that DoE is only meant for manufacturing settings and cannot be applied to service industry where human beings are involved and human errors are more prevalent which leads to many issues in the business. The second part will be looking into the role of key academics and researchers who have a vested interest on the topic of DoE. Clearly, more applications of DoE must be introduced into the service sector through effective collaboration between the university sector and service industry in various countries. In addition, the use of computer simulation should be explored further and academics certainly can help many service companies to integrate these two: DoE and computer simulation for greater understanding of service processes in terms of critical service parameters and their impact on service performance.

## 12.5 Limitations and future directions of research

The main limitation of this study is the fact that the CLR was not conducted in a systematic way. Therefore the results obtained in this research could not easily be replicated by other scholars, as these results refer to the specific sample of the articles analysed in the study. The articles used in the analysis were from peer-reviewed journals and a number of conference and professional magazine related papers were ignored in the study. The author would like to emphasise the point that all senior managers in the service industry should be introduced to DoE as a powerful tool to improve the service performance, reduce the number of customer complaints, increase service efficiency, improve service reliability and increase sales revenue. Finally, the author would like to conclude that future research should uncover the main challenges and difficulties that professionals face when they apply the DoE methodology and address how organisations could strengthen the learning of experimental process in the service industry. The next chapter presents some of the key findings from a global survey addressing some of the key things discussed in this chapter.

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# Design of Experiments in the service industry: results from a global survey and directions for further research

13

## 13.1 Introduction

Design of Experiments (DoE) is a statistical technique that helps to carry out experimentation in a systematic and controlled manner. DoE guides the experimenter to introduce deliberate changes in the variables of a process with the objective of being able to identify the causes of the changes that are observed in a chosen response variable. DoE is a fundamental and crucial methodology to increase the understanding of a process (e.g. manufacturing or service) and provides a means to achieve breakthrough improvements in product, service quality and process efficiency. The growth of DoE in the service industry has not occurred in the same way as in the manufacturing sector for several decades (Bisgaard, Hoerl, and Snee, 2002; Antony et al., 2010). A recent study (Antony et al., 2020) indicates that the number of scientific articles on the application of DoE techniques in the service industry is scarce.

The purpose of this chapter is to report the findings from a global survey on DoE in the service industry. The survey protocol was developed from a systematic review performed (refer to the previous chapter) that showed explicitly the current gaps on the topic and, thereby, justifies the need for this research (Antony et al., 2020). The target population of the study included six sigma black belt (SSBB), six sigma master black belt (SSMBB), quality or process improvement managers and experts/specialists of DoE techniques in service organisations or manufacturing organisations where they have performed designed experiments on non-manufacturing-related processes (e.g. invoicing, finance, health processes and education).

Although a few articles are published on challenges in the use of DoE within the service sector, some other important aspects such as what skills are needed to successfully conduct DoE or what factors must be considered are underestimated in the literature with respect to the service industry. Also, only a handful of case studies are reported in the extant literature related to DoE in the service sector (Antony et al., 2020). Moreover, although there are a handful of empirical studies widely reported on DoE applications in the manufacturing sector (Tanco et al., 2007, 2009), there is no evidence of similar empirical studies in the service industry.

Consequently, the focus of this global study was to fill the current gaps identified in the literature review through the development of an empirical study with the aim of answering the following four key research questions:

1. *What are the main challenges and difficulties faced by service industry process improvement professionals when applying DoE methods to service processes?*
2. *What are the typical benefits that can be gained from the application of DoE in the service industry?*
3. *What are the top five critical success factors (CSFs) for the effective implementation of DoE in service settings?*
4. *What are the essential skills that should be acquired by process improvement professionals for the successful application of DoE?*

### **13.1.1 Research methodology**

The research methodology adopted in our study has two different phases. This includes the development of survey questionnaire and pilot testing as phase 1 and sampling strategy and data collection as phase 2. These phases are explained in detail next.

#### **13.1.1.1 Development of survey instrument and piloting the instrument**

The survey instrument was developed based on the existing literature on the topic and most of the themes chosen for the survey are based on the current research gaps. An online survey developed in Google Forms was utilised, which targeted a number of professionals, including SSMBB, SSBB and process improvement professionals, among others, which work in various non-manufacturing settings and the service industry. This survey method is one of the most appropriate methods for this type of study as it enables the collection of a large amount of information from respondents in a short period of time. The questionnaire consisted of five parts, with each part designed with a specific purpose. Some parts of the questionnaire were developed using a five-point Likert scale, which is used extensively in research surveys of this nature (Flynn et al., 1990; Forza, 2002).

A pilot study was conducted during the scale development process. The online survey protocol was first piloted with five to seven experts who have hands-on experience with DoE or a combination of research experience through publications and involvement with experiments in their academic career. The purpose of piloting the survey questionnaire was to validate it and ensure that the questions are aligned with the four research questions (Couper and Miller, 2008). The comments and feedback from the pilot study were subsequently used to revise the survey questions and make the questions more readable and relevant to the research. The comments were positive; hence, the survey questionnaire was deemed suitable for research.

### 13.1.1.2 Sampling strategy and data collection

The revised online survey link was sent out to 500 process improvement professionals, leading academics with experience in DoE, consultants with experience in the use of DoE in the service industry and middle and senior managers with a good understanding of the topic. The contacts were obtained through LinkedIn and each of the respondents was contacted through email. This purposive sampling strategy was deliberately chosen to minimise the chance for selection error and assured experienced and knowledgeable respondents (Eisenhardt, 1989; Shokri et al., 2016). This yielded a total sample of 109 respondents (approximately 22%) representing five continents and 34 service sectors, which is satisfactory according to similar publications in the literature (Laureani and Antony, 2012; Ribeiro de Jesus et al., 2016).

## 13.1.2 Key findings

### 13.1.2.1 Demographical information

The sample was constructed by tapping into the researchers' networks, with an aim of equal responses from different geographical areas. Unfortunately, not all regions are equally represented in the final sample. Finally, a total of 109 responses were collected, including professionals from five different continents representing 34 service sectors in various different levels of corporate positions. Almost 90% of the respondents were either from Europe, Latin America or North America as presented in Fig. 13.1. The most representative service sectors among the respondents, with a cumulative percentage of almost 80%, were training and consultancy, transactional (i.e. services within the manufacturing industry, such as logistics, maintenance and marketing) and healthcare as illustrated in

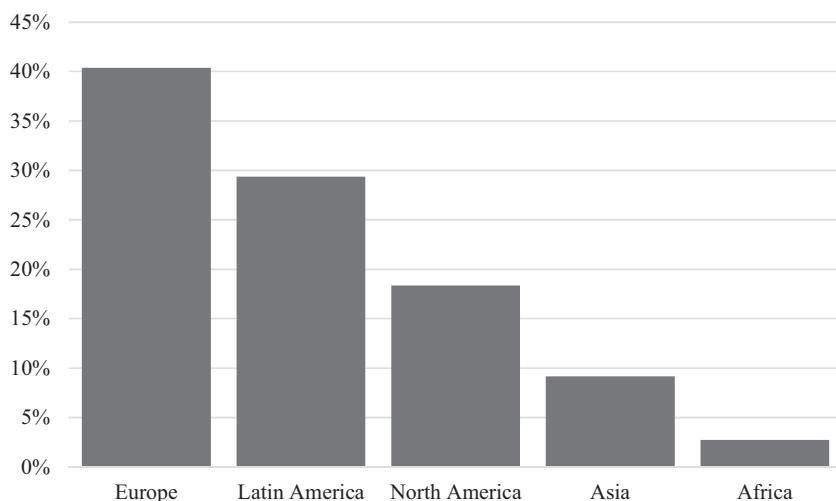
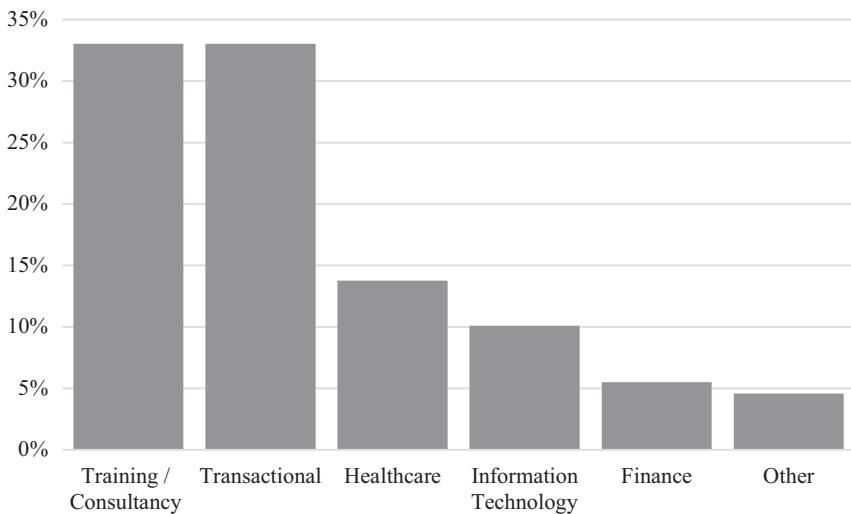
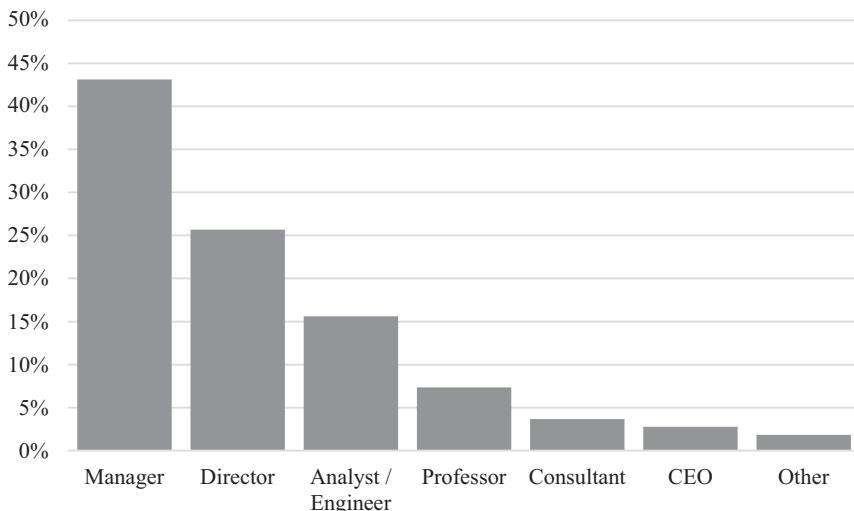


Figure 13.1 Respondents by continent.



**Figure 13.2** Respondents by service sector.



**Figure 13.3** Respondents by job title.

**Fig. 13.2.** The sample of professionals consulted in this survey was managers, directors and analysts, representing 84.4% of the all respondents (see Fig. 13.3).

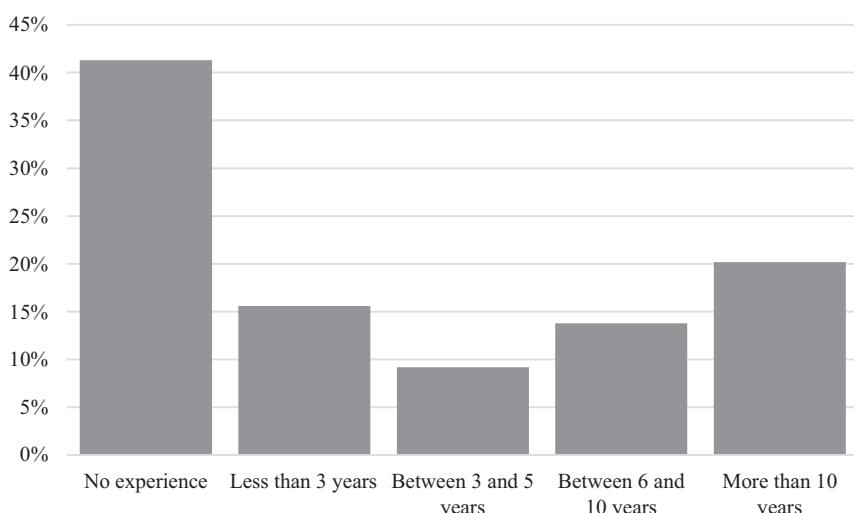
Some interesting findings include (1) 53.2% of the respondents have less than 5 years of experience in their current positions and (2) nearly 35% of the companies where the respondents work have more than 1000 employees, and 34% were small companies with 50 employees or less.

### 13.1.2.2 Education, training and experience in Design of Experiments

Overall, the respondents presented a relatively high level of education, as 24% are PhDs or DBAs and 43% have a master's degree. Out of the 109 respondents, only one of them has not been trained in Lean Six Sigma, 56.5% are SSMBB and 38.9% are SSBB. However, only 50% of the respondents had taken a course on DoE at a university. Out of these, only 44% studied DoE applications in the service industry during their academic courses. This finding indicates that DoE applied in the service industry is still a topic underexplored in the higher education sector. Nevertheless, more than 85% of the respondents were trained in DoE outside a university, nearly 60% of which has been exposed to examples of DoE applications in the service industry during the training. When it comes to the experience levels of the respondents, it was found that over 40% of the respondents do not have any experience in applying DoE methods in the service industry, as shown in Fig. 13.4.

The phase of the experimentation in which the respondents experience most difficulties is the definition of the input factors (20.1%), followed by data collection (19.4%) and selection of the experimental design (15.1%). It was observed that none of the respondents found difficulties in the interpretation of the results. The top five benefits stated by the respondents were (1) identifying the key variables of processes (21.5%); (2) reducing variability in service processes (15.0%); (3) improving process productivity (14.6%); (4) minimising errors in the processes (13.0%) and (5) improving the throughput of processes (12.2%).

The respondents who did have some experience in applying DoE in the service industry were asked about the experimental designs they used in their experiments.



**Figure 13.4** Levels of experience in applying DoE in the service industry. DoE, Design of Experiments.

It was found that the most used designs are fractional factorial designs (32.5%) and full factorial designs (28.7%), as shown in [Fig. 13.5](#).

### 13.1.2.3 Challenges in applying Design of Experiments in the service industry

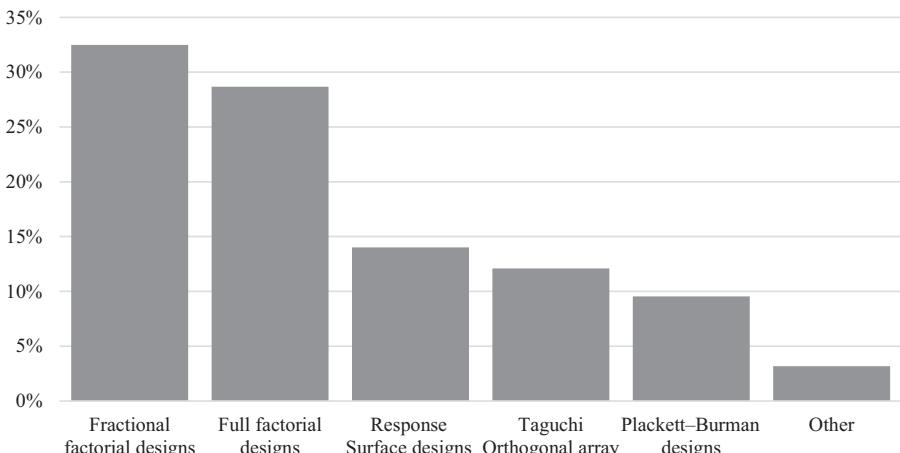
The respondents who have experience in applying DoE in the service industry evaluated each of the 16 statements following a Likert scale from 1 (I strongly disagree with the statement) to 5 (I strongly agree with the statement).

[Fig. 13.6](#) shows the responses by scores and statements, which are presented in [Appendix A](#). By calculating the average scores of the responses, it is possible to rank the top three challenges as follows:

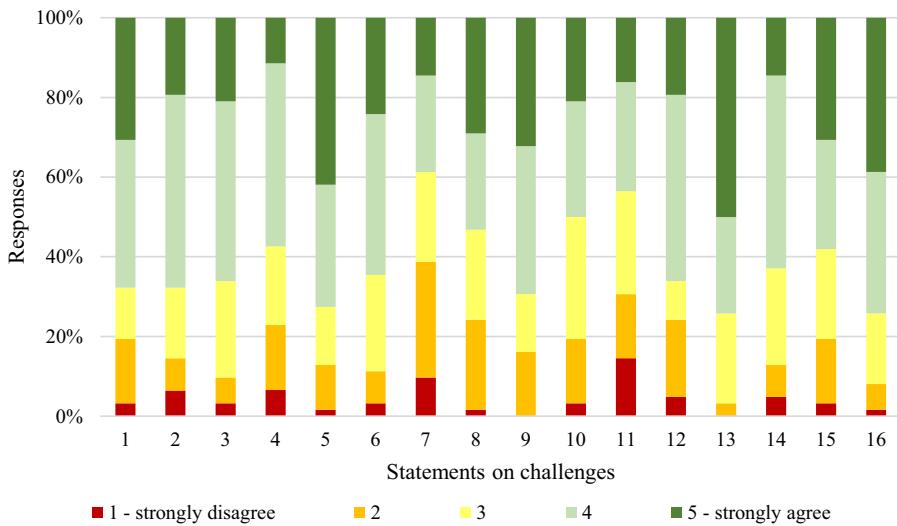
1. *Lack of awareness and knowledge and misconceptions among senior managers discourage experimentation in many service organisations.*
2. *There is a lack of adequate planning for DoE experiments (e.g. team selection, good problem definition, adequate variables selection and adequate metrics selection).*
3. *Most professionals in the service sector do not have a mathematical background and, thus, are not likely to apply data-based decision-making.*

Additional challenges in applying DoE in the service industry pointed out by the respondents include the following:

- “*Gaining support for additional experimentation once success has been achieved through screening experimentation*”.
- “*Achieving compliance with the experimental design*”.
- “*Appropriately controlling for external, uncontrollable variables that can have a large impact on the service output quality characteristics*”.
- “*Ensuring the factors in the experiment do not disrupt normal operations to an unacceptable extent*”.



**Figure 13.5** Most used experimental designs in the service sector.



**Figure 13.6** Responses to the statements about the challenges in applying DoE in the service industry. Please check the online version to view the colour image of the figure. *DoE*, Design of Experiments.

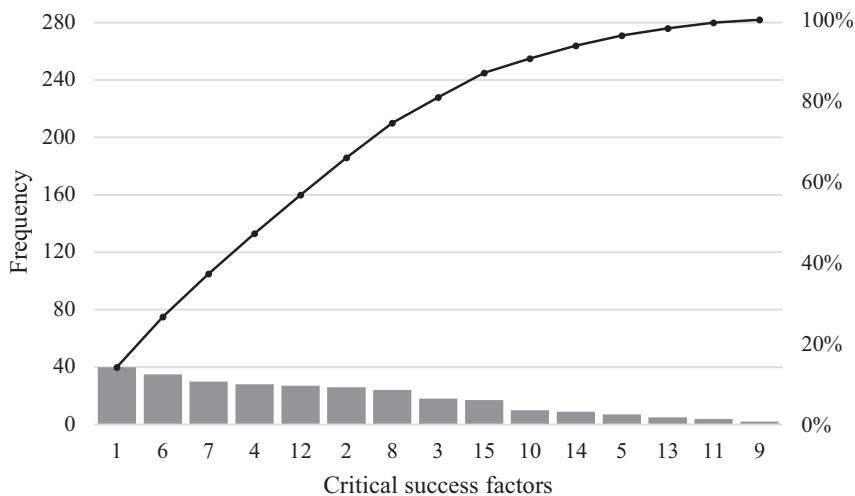
- “*Replication is tricky, also in service processes the customer may be involved in the delivery - this means some settings of the factors may result in unhappy customers - in manufacturing you can at least stop customer involvement*”.
- “*Senior leadership missing a culture of process improvements*”.
- “*Convincing people in the service sector of the value and payback for performing DOEs*”.

When asked about the possible contributions of academic institutions to the dissemination of DoE in the service industry, the top two choices of the respondents were (1) conducting more practical training in DoE with real problem-solving in the service industry (42.0%) and (2) publication of good practical cases for increased awareness and demonstrating the true power of DoE (34.4%).

### 13.1.2.4 Critical success factors for applying Design of Experiments in the service industry

In this part of the global survey, the respondents were asked to select the top 5 CSFs from a list of 15 identified from the literature. Fig. 13.7 summarises the results for the top CSFs according to the respondents.

Therefore, the top five CSFs pointed out by the respondents were the following: (1) *allocating adequate resources (e.g. time, budget and people) for the experiments* (14.2%); (2) *getting a clear understanding of the problem* (12.4%); (3) *having the adequate measurement system in place* (10.6%); (4) *choosing the appropriate input factors or service process parameters* (9.9%) and (5) *providing the appropriate training and education* (9.6%).



**Figure 13.7** Pareto chart of the critical success factors for successful application of DoE in the service industry. *DoE*, Design of Experiments.

Other CSFs suggested by the respondents included (1) identifying a need with potential application of DoE; (2) corporating expectation that data will be used to drive decision-making, followed by sound data collection methods; (3) getting the buy-in from any personnel impacted by the experimentation and (4) communicating the business value of the designed experiments in the service industry.

### 13.1.2.5 Essential skills for successful application of Design of Experiments in the service industry

Planning skills, statistical skills, teamwork skills and technical skills are the four types of skills considered important for applying DoE in the service sector (Antony et al., 2020). The respondents were asked to rate these four essential skills using a Likert scale from 1 (strongly disagree) to 5 (strongly agree). All of the aforementioned skills were highly rated by the respondents as important ones. In addition, communication skills were also pointed out by many respondents as another important set of skills.

### 13.1.3 Discussion and implications

The survey respondents overwhelmingly agree that the use of DoE methods has reported benefits to their organisations, specifically with respect to identifying the key variables of the service processes and reducing variability of those processes, as well as reducing in the number of errors they produce. However, as also indicated by the results of this global survey, there is significant room to expand the use of DoE in the service industry.

With regard to which are the skills required to successfully carry out experiments and apply DoE methods, it should be noted that the survey respondents prioritise skills that favour the strategy of the experiments (i.e. planning and statistical skills) and personal and group learning (i.e. teamwork skills), as opposed to more technical skills. The great diversity of software supporting the mathematical aspects of these methods explains this result.

As noted by one survey respondent, "It (DoE) is applicable anywhere". Many organisations lack management support, which is necessary for the successful and continued implementation of DoE into their continuous improvement activities. As highlighted by another respondent: "If there is little management support and commitment, DoE will die". Further, if management does not understand the value of DoE in the service industry, they will not provide the necessary training and resources. In a comment from a respondent, "Training and applying DoE alone is ineffective. When using DoE, the staff and senior management need to have the training and also the mentoring and guidance (end to end) for it to be effective". It is through multiple DoEs that the organisation begins to understand the true value of this methodology, as noted in the following comment from a respondent, "Once the organisations start to see some real benefits from the application of DoE, they start to support such experiments". Furthermore, the experience gained from running a DoE enables team members to properly analyse the data and develop suggestions for improvements. Another respondent commented, "Results are seldom conclusive, but do throw light into the problem. Many times, we have had to repeat runs or the whole experiment because procedures were not properly followed, and the experiment was not properly controlled". However, the repetition of running DoE experiments enables team members to overcome the obstacles required to build effective models as noted by a respondent, "You need to verify the optimised model to build confidence in the final results" and effectively communicate such findings.

The results of this global study and subsequent analysis will enable managers and continuous improvement teams to address the challenges and CSFs prior to implementing DoE in the service industry. A key finding of the analysis is that over 40% of the respondents had no hands-on experience with applying DoE. The literature indicates that DoE can be successfully applied in the service industry, therefore there is a significant opportunity to further enhance continuous improvement activities through the use of DoE. The identification of CSFs through the global study can assist many service improvement professionals and continuous improvement managers or operational excellence managers in service organisations in their endeavours for the implementation of DoE. Management can ensure that the challenges are addressed through the preliminary and continued communication on DoE and during the development and delivery of appropriate training. The results will also enable managers to encourage quality, continuous improvement and process improvement professionals in the service sector to utilise DoE in their problem-solving efforts.

### **13.1.4 Limitations and directions for future research**

As with any study, there are inherent limitations. First, the data was collected at an individual level. Therefore inter-reliability could not be captured to measure the consistency of responses for each survey question. Further, the response rate was low for some continents. Subsequently, an inter-continental comparative study could not be performed to identify trends of DoE applications across various continents. In addition, every survey has some major limitations in the sense that it does not provide deeper insights into the issues. For instance, one cannot determine from the survey why a particular box was ticked off by the respondent. Moreover, the response to each question depends upon the situational influences and mood of the individual at the time of completion of the survey instrument. This might have a bias on the findings of the study and therefore the author recommends semi-structured interviews with key professionals with experience on the subject matter to obtain their valuable opinions or recommendations. One of the key findings of the global study was that more than 40% of the respondents did not have any experience in the application of DoE in the service industry. This further highlights the need and importance of contributing to a widespread of statistical techniques such as DoE for the establishment of a data-based decision-making culture in the service sector.

## **Appendix A Statements related to the challenges in applying Design of Experiments (DoE) in the service industry**

No.	Statements related to the challenges in applying DoE in the service industry
1	Getting the cooperation of the employees was a big challenge in applying DoE in the service sector.
2	Having a high number of possible factors to include in the experiment was a big challenge in applying DoE in the service sector.
3	The challenge to measure the responses (which are often quite subjective) with satisfactory accuracy was a big challenge in applying DoE in the service sector.
4	The length of time researchers may take for data collection was a big challenge in applying DoE in the service sector.
5	Most professionals in the service sector do not have a mathematical background and, thus, are not likely to apply data-based decision-making.
6	The intangible component with the delivery of service is a challenge in applying DoE in the service sector.
7	It is not easy to obtain an appropriate sample size in the service sector.
8	It is not easy to provide the same experimental conditions for repeated measurement in the service sector.
9	There is rarely a culture of using the scientific method or applying continuous improvement in the service sector.
10	The difficulty in recognising which are the factors of the system or process under investigation is a challenge in applying DoE in the service sector.

(Continued)

(Continued)

No.	Statements related to the challenges in applying DoE in the service industry
11	The difficulty in classifying the factors into controlled and uncontrolled is a big challenge in applying DoE in the service sector.
12	The lack of standardized work processes is a challenge in applying DoE in the service sector.
13	Lack of awareness and knowledge and misconceptions among senior managers discourage experimentation in many service organisations.
14	Service processes have more ‘noise’ factors associated with them and therefore service performance is difficult to measure accurately.
15	There is a lack of continuous improvement mindset among employees in many service organisations.
16	There is a lack of adequate planning for DoE experiments (team selection, good problem definition, adequate variables selection, adequate metrics selection etc.).

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