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Fatigue

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Fatigue

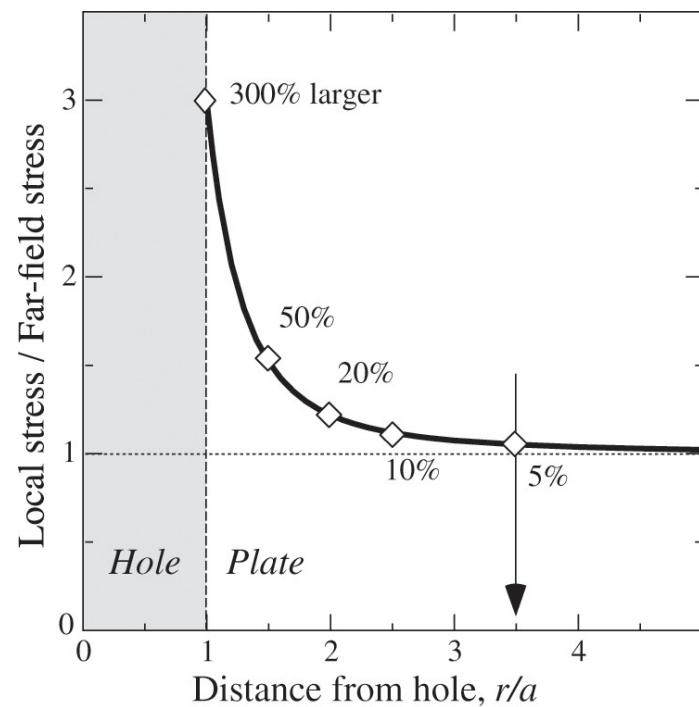
Part-2: Mechanism of fatigue

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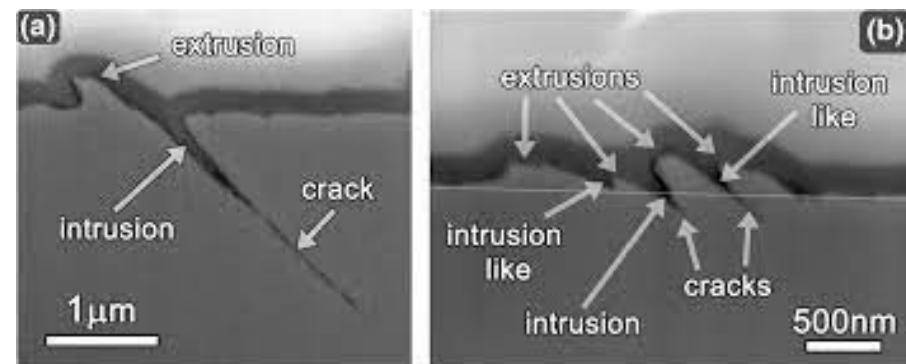
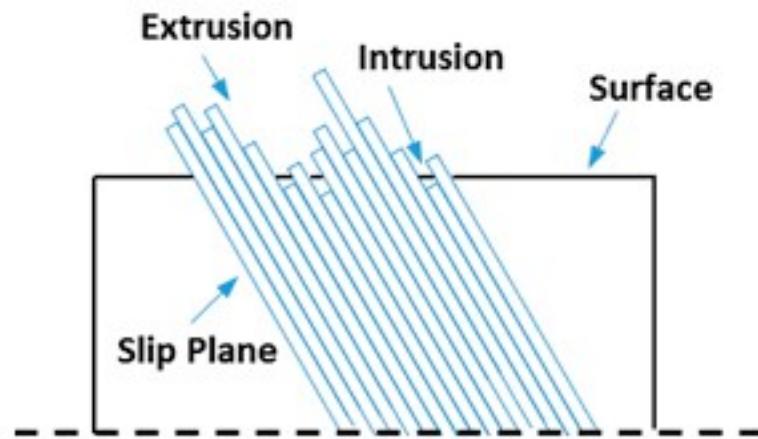
Stages of fatigue

- Fatigue failure stress << static strength
 - Fracture initiating at surface
 - Stress concentrations due to stress raisers
 - $K_t = S_{\max} / S_{\text{avg}}$ (K_t is fn. of crack length & root radius)
 - $S_{\text{local}} > Y.S$
 - Local plastic deformation (through slip)
- Damage accumulation stages
 - Stage-1: Crack initiation (Fatigue analysis: >75% of life)
 - Safe Life design of safety critical (e.g. undercarriage) or less inspectable (wing spar) structures – crack free life assuming no initial macro crack
 - Stage-2: Slow propagation of crack (Fracture analysis)
 - Fail Safe design of easily inspectable structures (e.g. fuselage skin, empennage) – assuming initial macro crack
 - Stage-3: Fast propagation of crack



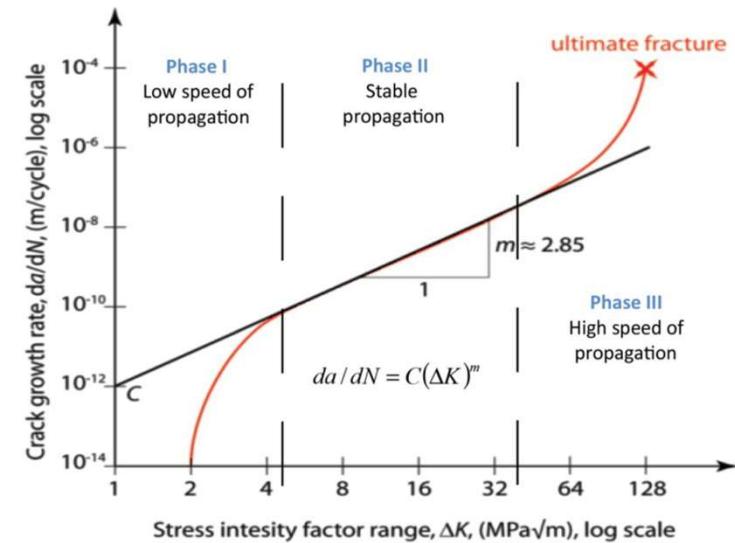
Stage-1: Crack initiation

- Stress raisers
- S_{\max} or $S_{\text{local}} > YS$
- Local plastic deformation
- Shear based slip (in slip planes along slip directions)
- Reversal of cycle
- Change in direction of slip planes
- Formation of extrusions & intrusions
- Intrusions act as small cracks
- Intrusion crack grows, cuts through grain boundaries to slip planes of adjacent grains
- Macroscopic surface crack



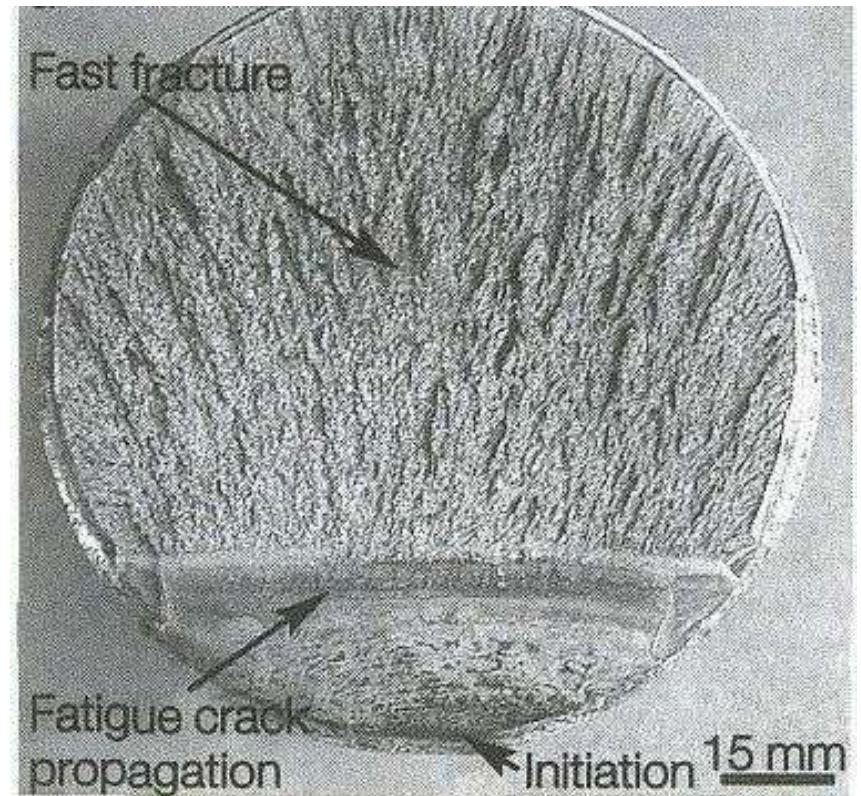
Stage-2: Slow propagation of crack

- Tensile cycle
 - Opening of the crack
 - Advancement of the crack
- Cycle reversal
 - Closure of the crack
 - Sharpening of the crack
- Net advancement in each cycle = crack advancement in tensile cycle – crack closure in compression cycle
 - If net advancement = 0: Infinite fatigue life
 - Else, crack growth rate (da/dN) as per Paris Law / Paris Erdogan equation
 - ΔK = Range of stress intensity factor = $K_{\max} - K_{\min}$ in a load cycle
 - $K = \sigma \times (\pi \cdot a)^{1/2} \times f$ (geometry)
 - C & m are material constants, m is typically 2-4, but can be as high as 10 for low fracture toughness materials

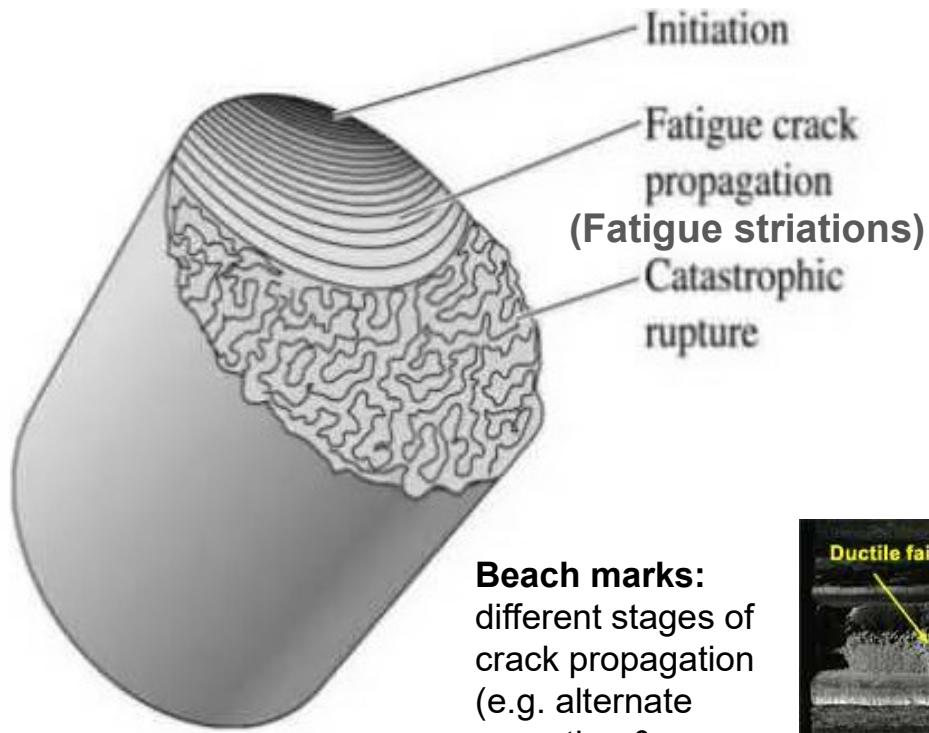


Stage-3: Fast propagation of crack

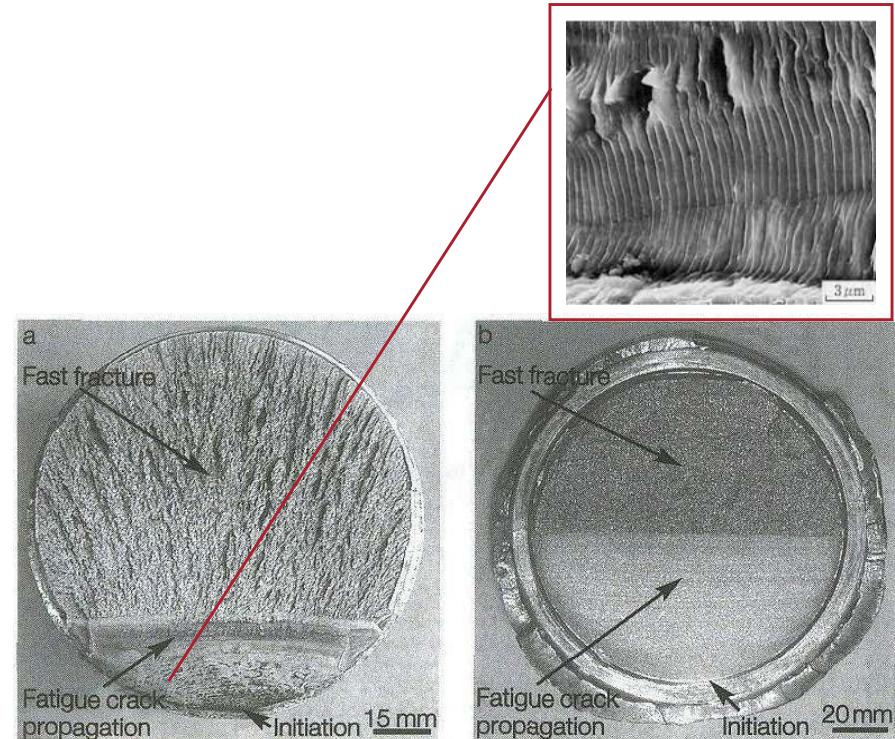
- Progress of crack
- Lowering of load bearing area
- $S_{\text{local}} > \text{UTS}$
- Fracture of material



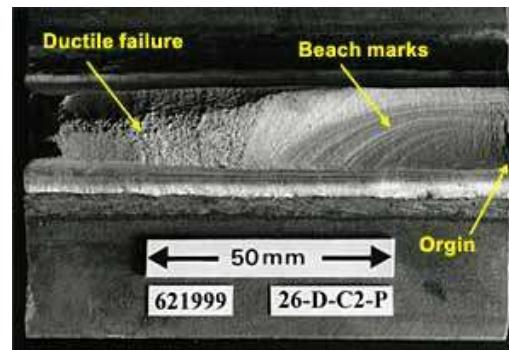
Fatigue fractography



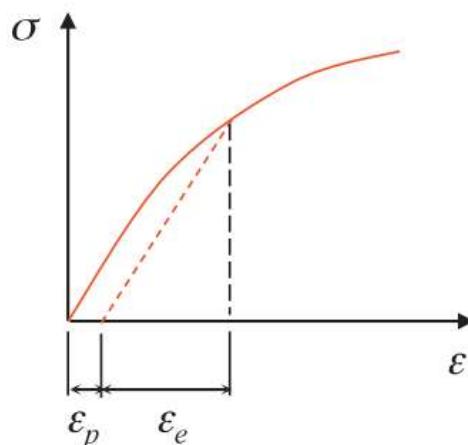
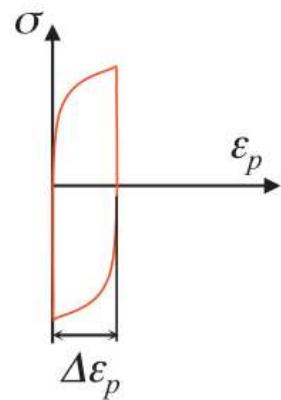
Beach marks:
different stages of
crack propagation
(e.g. alternate
operating &
stopping of a
machine)



Fatigue fracture surface: (a) high applied load; (b) low applied load.



Energy considerations in fatigue



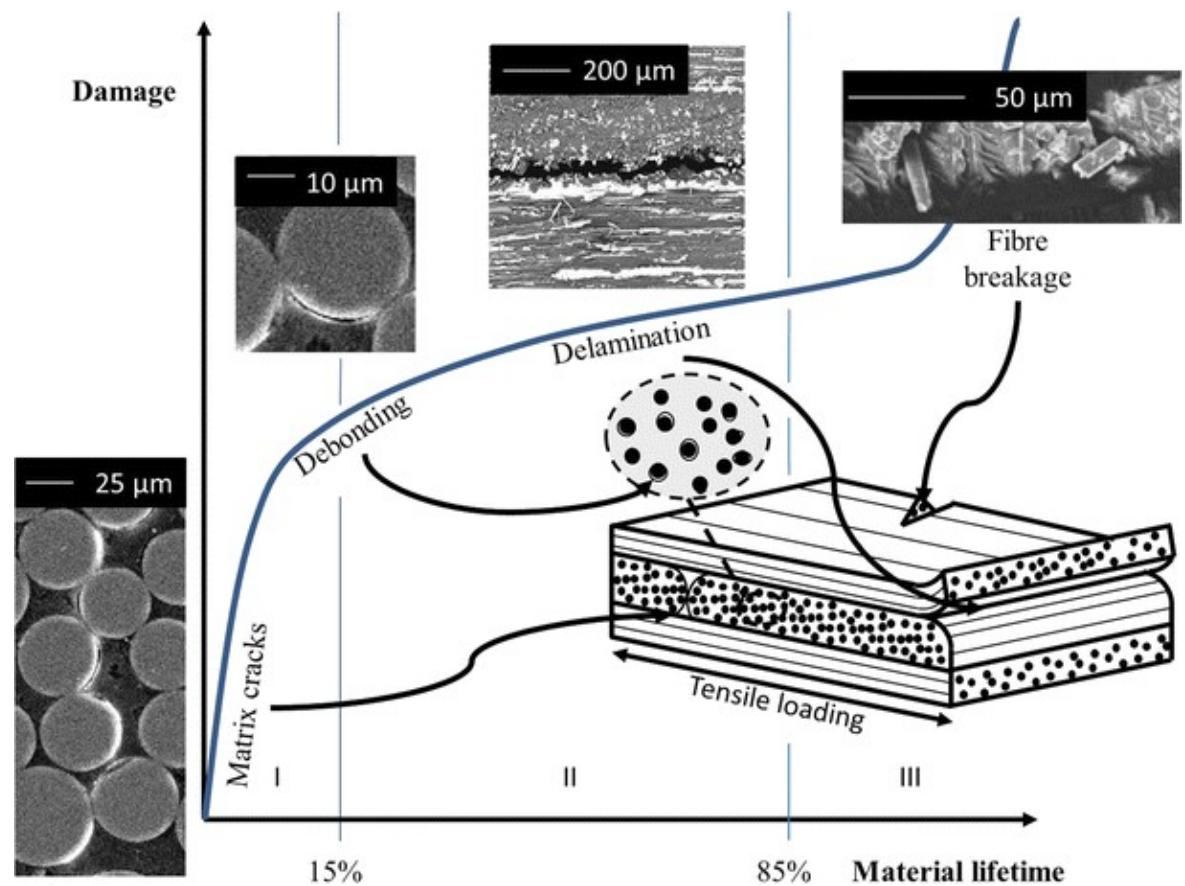
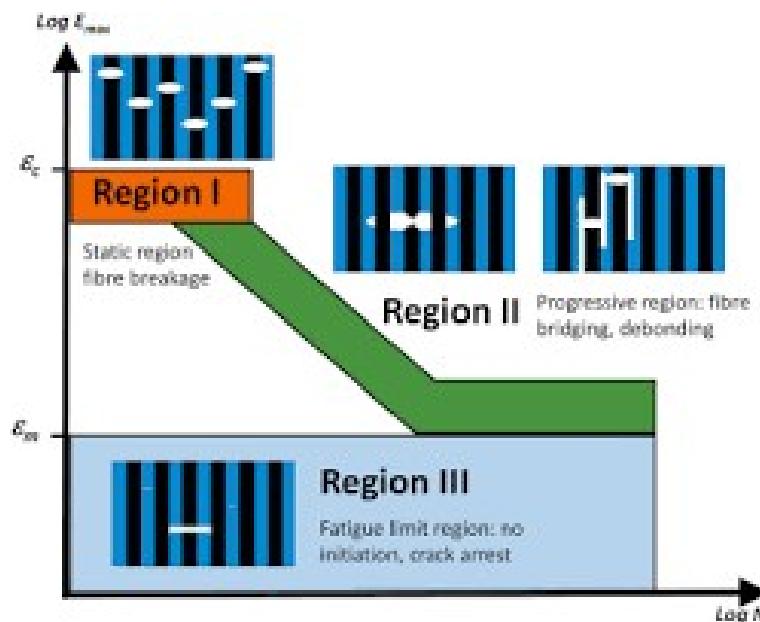
$$W_p \text{ (HCF)} \sim 100 \times W_p \text{ (static)}$$

Total plastic strain energy: $W_p = \Delta W.N_f$ "Fatigue toughness"

Note:

- Plastic strain energy : is responsible for crack initiation
- Elastic strain energy : is responsible for crack propagation

Fatigue in composites



End of Part-2

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Thank you

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