Lab 3 - Reducing Crime

Clayton G. Leach, Karl I. Siil, Timothy S. Slade July 23, 2018

Introduction

Our client is running for office in the state of North Carolina (NC). Her campaign commissioned us to research the determinants of crime in NC to help her develop her platform regarding crime-related policy initiatives at the level of local government. This report explores a subset of the county-level data from Cornwell & Trumball's Estimating the Economic Model of Crime with Panel Data (1994) that provides various economic, demographic, and crime indicators for 1987. Our analysis describes the dataset, presents initial summary statistics, develops several linear regression models, and proposes additional research to inform policy recommendations.

Initial Exploratory Data Analysis (EDA)

We begin by exploring our dataset. We see that it has 97 records and 25 variables.

```
dim(crime_raw)
## [1] 97 25
names(crime_raw)
                                            "prbarr"
                                                        "prbconv"
    [1] "county"
                    "year"
                                 "crmrte"
                                                                     "prbpris"
##
    [7] "avgsen"
                    "polpc"
                                "density"
                                            "taxpc"
                                                        "west"
                                                                     "central"
## [13] "urban"
                    "pctmin80"
                                "wcon"
                                            "wtuc"
                                                                     "wfir"
                                                         "wtrd"
## [19] "wser"
                    "wmfg"
                                                                     "mix"
                                 "wfed"
                                            "wsta"
                                                         "wloc"
## [25] "pctymle"
```

The notes we receive provide the following insight into the variables:

Table 1: Available Variables from Cornwell & Trumball (1994)

#	Variable Name	Type	Description	
1	county	integer	Source county of data	
2	year	integer	Source year of data	
3	crmrte	numeric	crime rate	
4	prbarr	numeric	'probability' of arrest	
5	prbconv	numeric	'probability' of conviction	
6	prbpris	numeric	'probability' of prison sentence	
7	avgsen	numeric	average sentence, in days	
8	polpc	numeric	police per capita	
9	density	numeric	people per sq. mile	
10	taxpc	numeric	tax revenue per capita	
11	west	dummy	source county of data is in Western NC	
12	central	dummy	source county of data is in Central NC	
13	urban	dummy	source county of data is urban	
14	pctmin80	numeric	percent minority in 1980	
15	wcon	numeric	wages in the construction industry	
16	wtuc	numeric	wages in the transportation, utilities, and communication industries	
17	wtrd	numeric	wages in the construction industry	
18	wfir	numeric	wages in the finance, insurance, real estate industries	
19	wser	$\operatorname{numeric}$	wages in the service industry	
20	wmfg	$\operatorname{numeric}$	wages in the manufacturing industry	
21	wfed	$\operatorname{numeric}$	wages among federal employees	
22	wsta	numeric	wages among state employees	
23	wloc	numeric	wages among local government employees	
24	mix	$\operatorname{numeric}$	$mix\ of\ offenses;\ face-to-face\ v\ others$	
25	pctymle	numeric	percent young male	

We see some variables which a priori seem useful: the 'probability' variables, police per capita, tax revenue, wages, and youth and minority composition of a county. Before exploring them further, however, we search the entire dataset for missing values that may affect our analyses.

Missing Values

We find 6 rows that are missing data; further scrutiny shows 5 are entirely blank and 1 contains only a backtick. We eliminate those to generate our working dataset.

```
crime_na <- crime_raw %>% filter_all(any_vars(!is.na(.))) # Rows with no data
crime_na %>% filter_all(any_vars(is.na(.))) %>% select(which(!is.na(.))) # Formerly row with one back
## # A tibble: 0 x 0
crime_na <- crime_na %>% filter_all(all_vars(!is.na(.))) # Verification
```

Erroneously Duplicated Records

Continuing our QC, we note that 1 of the counties' records has been duplicated exactly. We therefore drop the duplicate record from our dataset.

```
crime_na %>% count(county) %>% filter(n > 1) # county 193 is an exact duplicate

## # A tibble: 1 x 2

## county n

## <int> <int>
## 1 193 2
```

```
crime_na <- crime_na %>% filter(!duplicated(.)) # removed
```

Plausibility Checks for Variables

We see from the notes that three of our key variables of interest (prbarr, prbconv, and prbpris) represent probabilities and should therefore theoretically be in the range of 0:1.

Examining the data,¹ we find 10 counties have values for the "probability" variables that are outside of the expected range. In each case, it is either prbconv (10 records) or prbarr (1 record) that fall outside the range.

Per the notes accompanying our data, the probability of conviction is proxied by the ratio of convictions to arrests... Given that definition, if not all suspects arrested are convicted, prbconv will be below 1. However, it may also exceed 1 if the number of exonerated suspects is exceeded by the number of suspects convicted of multiple charges. (See here for examples of multiple charges stemming from a single arrest.)

The notes on prbarr indicate the probability of arrest is proxied by the ratio of arrests to offenses.... If multiple suspects are arrested for a single offense, and this happens more frequently than offenses which do not lead to arrests, prbarr would indeed exceed 1.

In both cases, there are plausible explanations for a probability value in excess of 1. However, one of the observations appears to be an outlier. The county labeled 115 has the lowest crime rate by far (~50% lower than that of any other county), the highest 'probability' of arrest (>1 arrest per offense, nearly 58% greater than the county with the second-highest probability), the longest average sentence (20.7 days, ~15% higher than the second-longest), and the largest number of police per capita (9 officers per 1,000 residents, more than twice as many as the second-highest county). While those numbers appear unusual, they are also internally consistent: one would expect a very low crime rate from a county that has a very strong police presence, arrests a large proportion of suspects, and punishes convicted criminals severely.²

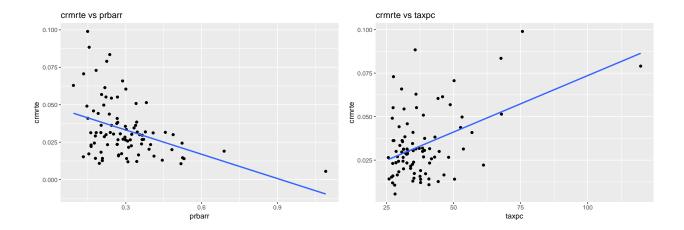
Overview of Scatterplots

We generate a series of scatterplots that we use to examine the relationships between our variable of interest, crmrte, and the other variables in the dataset. We present the code and a pair of example plots below, but full results are omitted for parsimony.³

¹See Appendix for the non_prob table

²Discussion with peers and further research reveals that the county labels are, in fact, FIPS (Federal Information Processing Standard) codes. A deep dive into additional county-level contextual factors that could inform our analyses is beyond the scope of this report; we leave it as an exercise for the reader.

³See Appendix for the remainder of the graphs.



Check for Truncated Variables and Outliers

Examining the remainder of our data, we found no substantial evidence of top-coded or bottom-coded (i.e., truncated) variables which might bias our regression models.

We see a handful of outliers. In wser, the variable indicating the county's weekly wage in the service industry, we find that county 185 is an extreme outlier. To determine if this is valid we looked at the wage values in that county for other sectors of the economy.

```
outlier_wser <- filter(crime_na, crime_na$wser == max(crime_na$wser))
outlier_wser[, c(1, 15:ncol(outlier_wser))]
## # A tibble: 1 x 12
##
     county wcon wtuc wtrd wfir wser wmfg wfed wsta
                                                                      mix
      <int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
##
                                                 381.
                                           248.
## 1
            227. 332.
                         167.
                               264. 2177.
                                                        367.
                                                              300. 0.0497
## # ... with 1 more variable: pctymle <dbl>
mean_other_wage <- with(outlier_wser, mean(wcon, wtuc, wtrd, wmfg, wfed, wsta,
    wloc))
```

It is improbable, but not impossible, that individuals in the service industry are making 9.6X more than the average wage of all other workers in the county. It seems more likely that a keystroke error was made in the recording of this variable (e.g., $2177.07 \rightarrow 217.71$). As we get into model-building we will check whether this particular value exerts undue influence on our results.

The other "outliers" we see are the values associated with county 115 discussed above, but those are neither as extreme nor inconsistent with theory.

Transformation Analysis

If the relationship between two variables is not linear, adding them to a linear regression model as-is (without a transformation) will generate inaccurate results and possibly result in an invalidation of our heteroskedasticity assumption. It is therefore important to explore whether the relationship between two variables shares some non-linear relationship and thus whether a transformation is required. As part of our EDA we explored this question for all of the variables in the dataset.

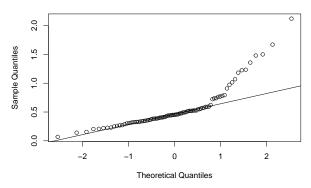
Our first step was to evaluate if any variables had significant skew in their distributions by checking whether they generally conformed to a normal distribution using R's qqplot. While this is not necessarily a reason to transform a variable, it can help us identify variables of interest. Below we present the code we used to generate the series of graphs as well as two sample graphs for illustrative purposes. 4

TS: Karl, I'm really struggling with this. Please rescue me!

```
for (i in 1:length(colnames(crime_na))) {
    column_interest <- paste("crime_na$", colnames(crime_na)[i], sep = "")
    qqnorm(eval(parse(text = column_interest)), main = colnames(crime_na)[i])
}

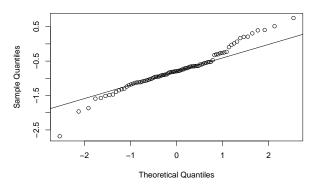
qqnorm(crime_na$prbconv, main = "Normality of prbconv")
qqline(crime_na$prbconv)</pre>
```

Normality of prbconv



```
qqnorm(log(crime_na$prbconv), main = "Normality of log(prbconv)")
qqline(log(crime_na$prbconv))
```

Normality of log(prbconv)



From our graphs we saw that probability of conviction (prbconv), police per capita (polpc), probability of arrest (prbarr), tax revenue per capita (taxpc), population density (density), proportion of young males in the population (pctymle), and the mix of face-to-face vs. impersonal crimes (mix) all deviated from normality. We will consider this in addition to other factors when deciding if a transformation would be beneficial.

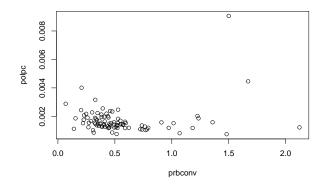
⁴See Appendix for the remainder of the graphs.

Checking for Linearity Between Predictor and Response Variables

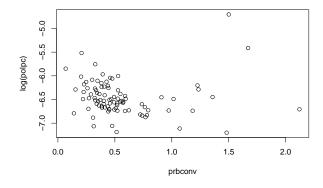
While it is not a perfect approach due to the possible interactions amongst variables, we also wanted to look at whether there is any obvious non-linearity when looking at crime rate and each variable independently. To do this we looked at a scatterplot of crime rate vs. each variable, and then applied various transformations to see whether those would improve the distribution. We present sample code and an illustrative graph here as an example.⁵

TS: Karl, I'm really struggling with this. Please rescue me!

```
for (i in 1:length(colnames(crime_na))) {
    column_interest <- paste("crime_na$", colnames(crime_na)[i], sep = "")
    plot(eval(parse(text = column_interest)), crime_na$crmrte, main = colnames(crime_na)[i],
        ylab = "Crime Rate", xlab = colnames(crime_na)[i])
}
with(crime_na, plot(prbconv, polpc), title = "Crime Rate v Police Per Capita")</pre>
```



```
with(crime_na, plot(prbconv, log(polpc)), title = "Crime Rate v log(Police per capita)")
```



Reviewing these graphs yields five (5) variables which appear to have a non-linear relationship with crime rate: prbarr, prbconv, polpc, density, and taxpc. While it is not particularly important that predictor variables be normally distributed, we do want them to display both *symmetry* and *high variance*; to the extent applying a transformation advances those goals, it is worth considering provided it does not inhibit interpretability or run strongly counter to theory.

⁵See Appendix for remaining graphs.

Four of the variables appear to benefit from a log transform, while the fifth (density) appears to be related to crime rate via the square root function. The pre- and post-transformation scatterplots and q-q plots for prbconv are presented here for illustrative purposes. TS: Karl, I'm really struggling with this. Please rescue me!

In addition to checking whether the relationship appeared to improve in linearity, we also checked whether this transformation helped with variable skew. In every case the distribution of our variable moved closer to normality. Given the improvement in linearity and normality we will use these transformations moving forward. <- TS: Given what we now know about not needing to transform dependent variables unless it helps with our need for symmetry and high variability, do we still want to do this?

Normality/Skew With and Without Transformation:

```
crime_na["log_prbarr"] = log(crime_na$prbarr)
crime_na["log_prbconv"] = log(crime_na$prbconv)
crime_na["log_polpc"] = log(crime_na$polpc)
crime_na["log_taxpc"] = log(crime_na$taxpc)
crime_na["sqrt_density"] = sqrt(crime_na$density)
```

Finally, we examined collinearity between various variables that we thought would comprise our models. For the sake of narrative flow, discussion of those findings is presented alongside the models in question.

Research Question and Model-Building

Our candidate seeks to develop a policy platform to address crime in NC. However, she knows that both the state's resources and her polical capital are limited, so she would like to know how to prioritize her efforts to achieve maximal impact. Our **research question** is thus the following: What is a small number of factors which are jointly highly predictive of the observable crime rate which our candidate should seek to address through legislation?

We face a key limitation: our data does not give us visibility into the crimes themselves or changes in crime, but rather provides only the official *crime rate*. The crime rate is a function not only of crimes committed but also of various additional factors, some of which may be unobservable. For instance, poor community-police relations may bias crime rates downward if an area's residents do not report all the crimes they observe or experience. Conversely, those poor relations may also bias crime rates upward if police officers engage in predatory policing practices and the community lacks the wherewithal to fight back. A full discussion of omitted variable bias will occur later in this analysis, but we preface our model-building section with this note to as a practical way to invite the reader to critically examine the models we propose.

In order to answer our research question we created several models which included variables related to key crime policy decisions. While there are 25 variables in our raw dataset, our model-building proceeded systematically. First, we grouped variables together *thematically*. Next, we built a model with the variables comprising the theme we believed a *priori* would be most likely to have high predictive value. After evaluating the model's performance, we added the variables for the next theme, and so forth.

Thematic grouping of variables

Theme 1: Crime and Punishment

Our first theme revolves around crime and the likelihood of punishment resulting from the act of committing a crime. We believe that the variables police per capita (polpc), probability of arrest (prbarr), probability of conviction (prbconv), probability of incarceration (prbpris), and average sentence length (avgsen) fit well

⁶See Appendix for the others.

together. Taken comprehensively, they help frame the observed crime rate in economic terms as a sort of "risk-reward" proposition for would-be criminals: is the presence of a well-functioning criminal justice system⁷—in which crimes consistently lead to arrests (of the actual perpetrators, and not innocent bystanders), and arrests consistently lead to (warranted) convictions, and convictions lead to prison sentences, and sentences are indeed punitive—predictively associated with the crime rate?

The variables in this theme are particularly valuable because they provide a solid foundation for policy development. If the size of the police force is associated with changes in the crime rate, it can be scaled up or scaled down appropriately. If the probability of arrest makes a difference, the county could invest in improving community-police relationships with the goal of improving the speed with which crimes are reported and the quality of the actionable intelligence witnesses provide. If the probability of conviction is important, funds could be invested in further training the police and District Attorneys on the collection and presentation of evidence. If the probability of incarceration and average sentence are important, legislators could advocate for changes to sentencing guidelines.

Theme 2: Demography and Economics

Our second theme focuses on issues of community composition, economic resources, and opportunity. Population density (density) may influence the crime rate in complex ways: from a sociological perspective, the social ecology approach to studying criminality considers population density to be one of several so-called criminogenic ("crime-causing") factors. From a psychological perspective, a larger population may weaken community bonds⁸ and thus the pressure to exhibit prosocial behavior. Where significant wealth or income disparities exist within close proximity, relative deprivation theory suggests population density may drive greater criminality. On the other hand, large, sparsely-populated swathes of land are difficult for police to monitor and may present opportunities for various non-violent crimes.⁹

Social control theory suggests that young people with weaker bonds to their communities may be more likely to commit crime. Indeed, economic and criminological research over the last several decades has argued young men are disproportionately involved in crime. There has also been widespread discussion of the role that race and ethnicity play in criminality. We thus include the variables pctymle and pctmin80 in this model.

The police force is funded by the local government, which in turn is funded by the local taxpayers. We might thus expect that the taxes paid per capita (taxpc) might have an influence on the size and/or effectiveness of the police force, either reinforcing or undermining any effect polpc might have on the crime rate.

The dataset contains nine variables related to wage: wfed, wsta, wloc, wmfg, wser, wcon, wfir, wtrd, wtuc. While much of their cumulative influence on a community may be captured in the taxpc variable - and thus we must beware excessive collinearity - different groupings of those wage variables may provide insight into well- or under-funded segments of the local economy. We discuss these alternative specifications below under Model 2.

While we believe these variables are sufficiently distinct to warrant their own model, we believe they may exhibit some colinearity with the predictors we included in **Model 1**. Specifically, we suspect taxpc and density may be colinear with polpc; pctymle and pctmin80 may be colinear with prbarr; and government wages (wfed, wsta, wloc) may be colinear with prbconv. We theorize that both prbpris and avgsen may be colinear with some underlying omitted variable (for instance, local sentencing guidelines), but lack an alternative variable that might serve as a reasonable proxy. We will conduct checks for colinearity when analyzing our models.

Theme 3: 'The Kitchen Sink, or, everything else'

 $^{^7\}mathrm{Using}$ an admittedly naı̈ve formulation in which socioeconomic status, racial bias, and predatory policing are assumed to be non-issues.

⁸Consider the various tiers of Dunbar's number

⁹Consider, for instance, the prevalence of marijuana cultivation in rural northern California or moonshine production in the rural South. Both are industries in which lots of land with very few people living on it is a desirable feature.

¹⁰The expected colinearity of government wages with prbconv is premised on a theorized relationship between prbconv as an outcome variable and the quality or effectiveness of police investigators, court-appointed advocates, judges, and other government officials as proxied loosely by wage.

Of the 25 variables in the dataset, we incorporated five into **Model 1** and 13 into **Model 2**. Of the remaining seven, year is meaningless (it is a constant, 87, for all observations in the dataset) and crmrte is our outcome of interest. That leaves five we can incorporate into a final model that attempts to capture everything that might plausibly predict crime rate: three dummy variables describing a county's location within NC (west, central) and its degree of urbanization (urban), one describing the ratio of face-to-face vs. 'other' crimes (mix), and the county identifier (county), which we know is a FIPS code. The unifying theme for these variables is essentially the absence of a unifying theme: these are the leftovers.

Building of Initial Models

In the section below, we build our models, assess them in light of the six assumptions of the classical linear model (**CLM**), examine their coefficients, and provide some basic interpretation. In addition to the models suggested by the three themes above, we will generate a fourth model which incorporates our insights from evaluating our models.

The CLM Assumptions

There are six assumptions of the CLM that we will try to uphold in our models.

- 1. Linear population model: The model is linear in the coefficients of the predictors, correctly specified, and has an additive error term.
- 2. Random Sampling: The data on which the model is based represent a random sample from the population
- 3. No perfect multicollinearity: None of the predictors in the models are perfect linear transformations of another predictor.
- 4. Zero-conditional mean / Exogeneity: There is no expected error in the regression function.
- 5. Homoskedasticity: Residuals display equal variance for all X_i .
- $6.\ Normality\ of\ Errors$: Residuals will be normally distributed.

We cannot empirically test **CLM2**, so we will omit it from our discussion of the models.

Model 1: Crime and Punishment

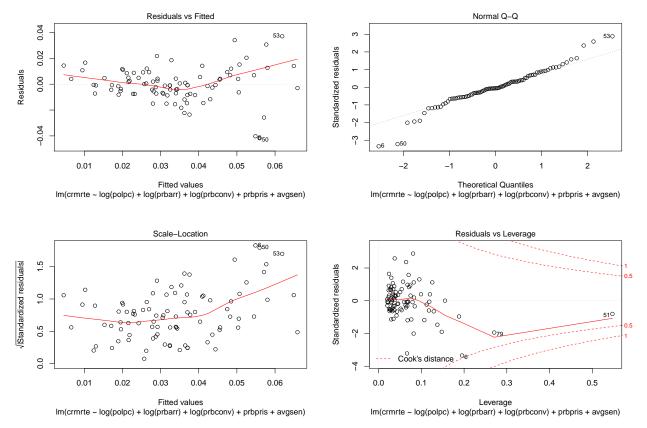
Drawing upon the transformations suggested by our exploratory data analysis and the discussion above, the first model we develop and examine is thus as follows:

```
\mathtt{crmrte} = \beta_0 + \beta_1 \log(\mathtt{polpc}) + \beta_2 \log(\mathtt{prbarr}) + \beta_3 \log(\mathtt{prbconv}) + \beta_4 \mathtt{prbpris} + \beta_5 \mathtt{avgsen} + u \tag{1}
```

```
# Model for Theme 1
mod1 <- with(crime_na, lm(crmrte ~ log(polpc) + log(prbarr) + log(prbconv) +
    prbpris + avgsen))
# Adding AIC to our model to help us compare models in the future.
mod1$AIC <- AIC(mod1)</pre>
```

Before we examine the coefficients of our model, we generate our diagnostic plots to see whether the model adheres to the six assumptions of the classical linear model.

```
# par(mfrow = c(3, 2))
plot(mod1)
```



While the mean of the residuals appears to be centered on 0 as we would expect (supporting **CLM4**), the curvature in our loess smoother suggests that our model may not be correctly specified (violating **CLM1**). Our residuals appear to be quite normal (supporting **CLM6**), except at the extremes of our model where few data points are available. We can check for multicollinearity in our model by examining the variance inflation factors (VIF) for each of the predictors we include; a VIF above 5 for any of them would represent cause for concern.

```
vif(mod1) # All clear

## log(polpc) log(prbarr) log(prbconv) prbpris avgsen
## 1.284926 1.047115 1.084671 1.012953 1.280973
```

We appear to see some evidence of heteroskedasticity (violating **CLM5**), indicating a need to apply heteroskedasticity-consistent ("robust") standard errors.

```
bptest(mod1) # Breusch-Pagan: heteroskedasticity confirmed
```

```
##
## studentized Breusch-Pagan test
##
## data: mod1
## BP = 22.112, df = 5, p-value = 0.0004984
ncvTest(mod1) # Non-constant variance: heteroskedasticity confirmed
## Non-constant Variance Score Test
## Variance formula: ~ fitted.values
## Chisquare = 32.97464 Df = 1 p = 9.336874e-09
```

Having confirmed the heterosked asticity in our model, we will need to replace the standard errors and the F-statistic with robust versions of themselves. We demonstrate the code here, but will omit it from our discussion of future models.¹¹

Table 2: Model 1: Crime and Punishment

	$Dependent\ variable:$
	crmrte
log(polpc)	$0.020^{***} (0.005)$
log(prbarr)	-0.024***(0.004)
log(prbconv)	$-0.014^{***} (0.004)$
prbpris	$0.009 \ (0.021)$
avgsen	-0.001(0.001)
Constant	$0.126^{***}(0.036)$
F Statistic	11.09
$\Pr(>F)$	3.22 e-08
Observations	90
\mathbb{R}^2	0.524
Adjusted R^2	0.495
Akaike Inf. Crit.	-512.807
Residual Std. Error	0.013 (df = 84)
Note:	*p<0.05; **p<0.01; ***p<0.001

p-values based on Wald test; robust standard errors in parentheses

Comments on Model 1: Crime and Punishment

The p-value associated with our heteroskedasticity-robust F-test is highly significant, indicating that our model is more predictive than a simple horizontal line at a y-intercept would be. The adjusted R^2 of our model is 0.495, which is pretty good.

We highlight four main observations:

1) The log of police per capita, the log of the probability of arrest, and the log of probability of conviction are all highly statistically-significant. Because these predictors are all log transformed while the outcome variable is not, the interpretation is that the coefficient represents the change in the predicted value of the outcome variable associated with a 1% change in the predictor. In other words,

¹¹See Appendix for detailed code

```
\Delta y = \Delta x_i / 100.
```

- 2) Our coefficient for $(\log(polpc))$ is positive, and suggests that a 1% increase in the # of police per capita would be associated with an *increase* of 2.05 crimes per 10,000 people. If we inaccurately assumed this model was causal the best mechanism to reduce crime rates would be to sunset the police force! However, a more plausible interpretation is that a higher number of police per capita is a response to higher levels of criminal activity, rather than a cause of it.
- 3) Both log probability of arrest $(\log(prbarr))$ and log probability of conviction $(\log(prbconv))$ have highly significant and negative coefficients. This fits with what we would expect: the more likely an individual is to be caught and convicted the less likely they are to commit crime. Our model suggests a 1% increase in the 'probability' of arrest and conviction would be associated with -2.44 and -1.37 fewer crimes per 10,000 people.
- 4) Neither the probability of incarceration of the average sentence length are statistically significant.

Model 2: Demography and Economics

Model 2 builds upon **Model 1** by including the additional covariates discussed earlier. As discussed above, we theorized that collapsing the nine wage variables into two or three that are logically grouped might be of use. The base (extended) version of **Model 2** would be as follows:

$$\begin{aligned} \mathsf{crmrte} &= \beta_0 + \beta_1 \log(\mathsf{polpc}) + \beta_2 \log(\mathsf{prbarr}) + \beta_3 \log(\mathsf{prbconv}) + \beta_4 \mathsf{prbpris} + \beta_5 \mathsf{avgsen} & \quad (\mathsf{Model} \ 1) \\ &+ \beta_6 \log(\mathsf{taxpc}) + \beta_7 \mathsf{sqrt_density} + \beta_8 \mathsf{pctymle} + \beta_9 \mathsf{pctmin80} \\ &+ \beta_{10} \mathsf{wcon} + \beta_{11} \mathsf{wtuc} + \beta_{12} \mathsf{wtrd} + \beta_{13} \mathsf{wfir} + \beta_{14} \mathsf{wser} \\ &+ \beta_{15} \mathsf{wmfg} + \beta_{16} \mathsf{wfed} + \beta_{17} \mathsf{wsta} + \beta_{18} \mathsf{wloc} + u \end{aligned}$$

Condensed Wage Metrics

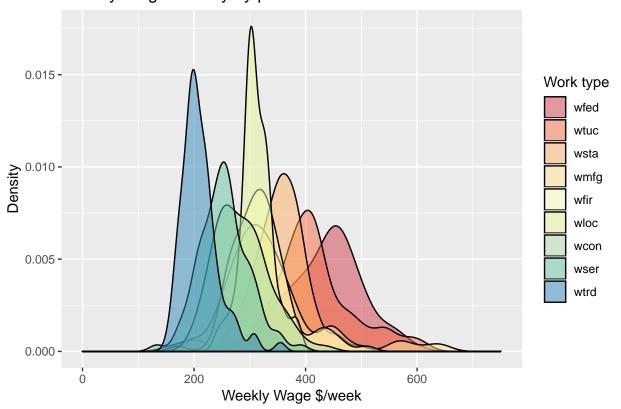
↓ TS: I am thinking we should consider cutting this out, or presenting it as a secondary (exploratory) model rather than our "main" model. The critique we got from the peer reviewers is spot-on: a straight average is an extremely naïve approach to combining the wage inputs, and likely doesn't make sense. A PCA or something might make more sense, but we've not the necessary data to do that on a per-county basis, which is the only unit for which it would fit and be relevant for our model.

Each of the nine wage variables represents a different sector or group of industries. We do not have a priori justification to believe a single industry might contribute disproportionately to crime, but we can assume that low wages in general might create an environment of economic scarcity in which crime incidence would increases. Including all nine variables when our dataset only contains 90 observations would be extremely limiting, but excluding them entirely prohibits us from understanding how microeconomic conditions may be contributing to observed crime rates. Researching the composition of each county's economy and weighting each variable accordingly might be a fruitful strategy, but it lies outside the scope of this report. The solution we propose iss to create three new composite variables:

- 1) Government Wage: Average of wfed (federal government wage), wsta (state government wage), and wloc (local government wage)
- 2) Blue-Collar Wage: Average of wmfg (manufacturing), wser (service), wcon (construction)
- 3) Professional Wage: Average of wfir (Finance/Investment/Real Estate), wtrd (Wholesale/Retail Trade), and wtuc (Transportation, Utilities, Communication)

```
crime_na %>% gather(wfed, wtuc, wsta, wmfg, wfir, wloc, wcon, wser, wtrd, key = "work_type",
    value = "weekly_wage") %>% select(county, work_type, weekly_wage, everything()) %>%
```

Weekly Wage Density by position



```
crime_na$govt_wg <- (crime_na$wfed + crime_na$wsta + crime_na$wloc)/3
crime_na$physical_wg <- (crime_na$wmfg + crime_na$wser + crime_na$wcon)/3
crime_na$industry_wg <- (crime_na$wfir + crime_na$wtrd + crime_na$wtuc)/3

# Model with our key explanatory variables, and what we suspect to be key
# covariates

mod2_b <- with(crime_na, lm(crmrte ~ log(polpc) + log(prbarr) + log(prbconv) +
    prbpris + avgsen + log(taxpc) + sqrt_density + pctymle + pctmin80 + wcon +
    wtuc + wtrd + wfir + wser + wmfg + wfed + wsta + wloc))

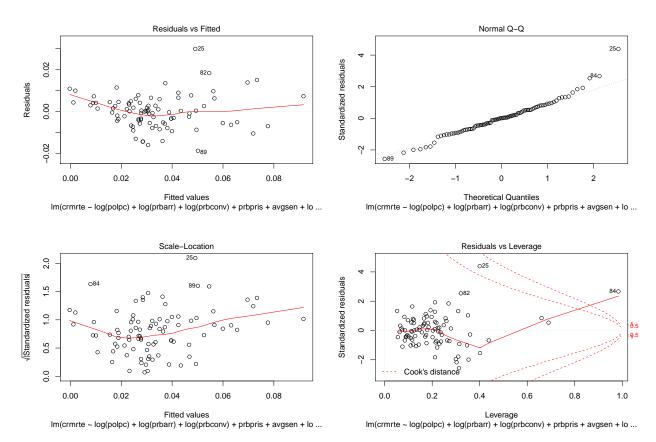
mod2_b_nomin <- with(crime_na, lm(crmrte ~ log(polpc) + log(prbarr) + log(prbconv) +
    prbpris + avgsen + log(taxpc) + sqrt_density + pctymle + wcon + wtuc + wtrd +
    wfir + wser + wmfg + wfed + wsta + wloc))

min_ars_diff <- summary(mod2_b)$adj.r.squared - summary(mod2_b_nomin)$adj.r.squared

# Adding AIC to our model to help us compare models in the future.
mod2_b$AIC <- AIC(mod2_b)</pre>
```

Before we examine the coefficients of our model, we generate our diagnostic plots to see whether the model adheres to the six assumptions of the classical linear model.

```
# par(mfrow = c(3, 2))
plot(mod2_b)
```



Overall, the most salient feature of these diagnostic plots is how similar they are to the plots for **Model 1**. The plot of residuals vs. fitted values continues to suggest that the model is improperly specified, although perhaps marginally less so than before. The only striking difference is that two observations - for counties 25 and 84 - are now both high-leverage and high-influence, with Cook's distances of > 0.5 and > 1.0 respectively.

```
vif(mod2_b) # All clear
```

avgsen	prbpris	log(prbconv)	log(prbarr)	log(polpc)	##
1.556323	1.154503	1.866910	1.730140	2.099671	##
wcon	pctmin80	pctymle	sqrt_density	log(taxpc)	##
2.135526	1.297078	1.466395	3.014007	1.745862	##
wmfg	wser	wfir	wtrd	wtuc	##
1.947060	1.239784	2.650859	3.143922	1.720211	##
		wloc	wsta	wfed	##
		2.235522	1.510677	3.076304	##

Our analysis of the VIFs indicates that multicollinearity has increased slightly, but not yet to the point where our rule of thumb (excluding covariates with VIF > 5) would come into play.

```
bptest(mod2_b) # Breusch-Pagan: heteroskedasticity confirmed
```

```
##
## studentized Breusch-Pagan test
##
## data: mod2_b
```

```
## BP = 43.242, df = 18, p-value = 0.0007396
ncvTest(mod2_b) # Non-constant variance: heteroskedasticity confirmed

## Non-constant Variance Score Test
## Variance formula: ~ fitted.values
## Chisquare = 9.32617 Df = 1 p = 0.00225904
```

As with **Model 1**, graphical indications of heteroskedasticity (violating **CLM5**) are confirmed by Breusch-Pagan and non-constant variance diagnostic tests, indicating a need to apply heteroskedasticity-consistent ("robust") standard errors.¹²

```
# Output model results in nice format using tidy and kable kable(tidy(mod1))
# # <- TS: Superfluous b/c need RSE, so stargazer
stargazer(mod2_b, header = FALSE, type = "latex", se = mod2_b_robse, p = mod2_b_pvals,
    report = "vc*s", star.cutoffs = c(0.05, 0.01, 0.001), title = "Model 2: Demography and Economics",
    single.row = TRUE, omit.stat = "f", add.lines = list(c("F Statistic", mod2_b_wF),
        c("Pr(>F)", mod2_b_wp)), notes = "p-values based on Wald test; robust standard errors in parent.
```

Table 3: Model 2: Demography and Economics

	Dependent variable:	
	crmrte	
log(polpc)	$0.014^{**} (0.005)$	
log(prbarr)	-0.016^{***} (0.004)	
log(prbconv)	-0.008*(0.003)	
prbpris	$-0.010 \; (0.011)$	
avgsen	-0.001 (0.0004)	
$\log(\text{taxpc})$	$0.006 \ (0.007)$	
sqrt_density	0.018*** (0.004)	
pctymle	0.064 (0.033)	
pctmin80	$0.0004^{***} (0.0001)$	
wcon	0.00002 (0.00002)	
wtuc	0.00001 (0.00002)	
wtrd	0.00004 (0.0001)	
wfir	-0.00005 (0.00002)	
wser	-0.00001***(0.00000)	
wmfg	$-0.00000 \ (0.00001)$	
wfed	$0.00000 \ (0.00003)$	
wsta	$-0.00001 \ (0.00003)$	
wloc	$0.00003 \ (0.0001)$	
Constant	$0.047 \ (0.048)$	
F Statistic	19.27	
$\Pr(>F)$	1.79e-20	
Observations	90	
\mathbb{R}^2	0.827	
Adjusted R^2	0.783	
Akaike Inf. Crit.	-577.971	
Residual Std. Error	0.009 (df = 71)	

Note: *p<0.05; **p<0.01; ***p<0.001 p-values based on Wald test; robust standard errors in parentheses

 $^{^{12}\}mathrm{See}$ Appendix for the detailed code showing the calculation of those SEs

Comments on Model 2:

- 1) One item of interest was the extreme degree of significance we see associated with our percent minority variable (pctmin80). Interestingly, when using only this variable to predict crime rates our R^2 is very low; after controlling for other factors, however, this variable becomes extremely important. One way to measure this importance is by calculating the difference between the adjusted R^2 values for a model that includes the variable and one that excludes it. When including the minority variable in our model, the adjusted R^2 is 0.783. When excluding it, the adjusted R^2 is 0.661, a difference of 12.3 percentage points.
- 2) The square root of the population density is also highly significant. Given the transformation the correct interpretation is that crime activity increases quickly when moving from very small to medium sized population densities, but requires increasingly large levels of population increase to have an effect on crime rate.

Model 3

Model 2 yielded greater predictive value than Model 1 by including a few extra covariates. Model 3 throws in essentially every variable in the dataset.

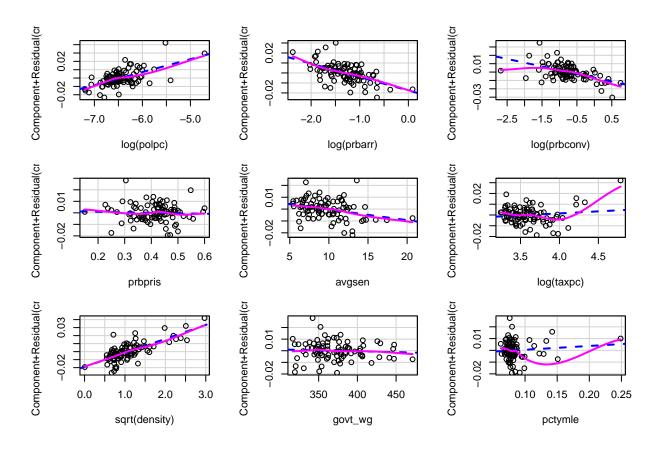
$$\begin{split} \mathsf{crmrte} &= \beta_0 + \beta_1 \log(\mathsf{polpc}) + \beta_2 \log(\mathsf{prbarr}) + \beta_3 \mathsf{prbconv} + \beta_4 \mathsf{prbpris} + \beta_5 \mathsf{avgsen} \\ &+ \beta_6 \log(\mathsf{taxpc}) + \beta_7 \mathsf{sqrt_density} + \beta_8 \mathsf{pctymle} + \beta_9 \mathsf{pctmin80} \\ &+ \beta_{10} \mathsf{wcon} + \beta_{11} \mathsf{wtuc} + \beta_{12} \mathsf{wtrd} + \beta_{13} \mathsf{wfir} + \beta_{14} \mathsf{wser} \\ &+ \beta_{15} \mathsf{wmfg} + \beta_{16} \mathsf{wfed} + \beta_{17} \mathsf{wsta} + \beta_{18} \mathsf{wloc} \\ &+ \beta_{19} \mathsf{mix} + \beta_{20} \mathsf{central} + \beta_{21} \mathsf{west} + \beta_{22} \mathsf{urban} + \beta_{23} \mathsf{county} + u \end{split} \tag{Model 2}$$

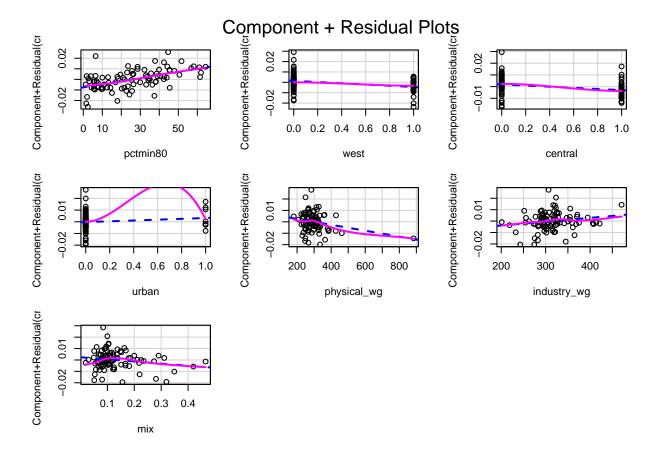
Given the countless ways behavioral issues are interconnected, we wondered whether every variable we had data on might be correlated with either the crime rate or an already included variable in some fashion. Our focus was to determine if including all our variables substantially changed the significance or corefficient of any of our previously included variables. Additionally, we wanted to understand if any of the variables we had previously left out were in fact predictive overall.

term	estimate	std.error	statistic	p.value
(Intercept)	0.0855755	0.0457433	1.8707776	0.0653840
$\log(\text{polpc})$	0.0155349	0.0035528	4.3725722	0.0000401
$\log(\text{prbarr})$	-0.0134649	0.0030555	-4.4067304	0.0000354
$\log(\text{prbconv})$	-0.0089994	0.0021761	-4.1355031	0.0000936
prbpris	-0.0043629	0.0121923	-0.3578438	0.7214928
avgsen	-0.0009032	0.0004166	-2.1679559	0.0334227
$\log(\text{taxpc})$	0.0037515	0.0049573	0.7567610	0.4516286

term	estimate	std.error	statistic	p.value
sqrt(density)	0.0174525	0.0040678	4.2904401	0.0000539
$govt_wg$	-0.0000155	0.0000445	-0.3485367	0.7284403
pctymle	0.0320931	0.0471316	0.6809257	0.4980728
pctmin80	0.0002928	0.0000948	3.0872972	0.0028548
west	-0.0059240	0.0039528	-1.4986898	0.1382663
central	-0.0048302	0.0028514	-1.6939831	0.0945314
urban	0.0035046	0.0057624	0.6081836	0.5449534
physical_wg	-0.0000259	0.0000157	-1.6443824	0.1043973
$industry_wg$	0.0000335	0.0000317	1.0581013	0.2934980
mix	-0.0185578	0.0155657	-1.1922224	0.2370353

crPlots(mod3)





Model 3 Notes:

Similarly to model 2, we find that log police per capita, log probability of arrest, log probability of conviction, square root of density, and percent minority are significant. While model 3 coefficients do change relative to model 2, there are not any drastic changes, or sign (+/-) changes indicating a reversal of effect.

Our adjusted R squared value for this model is 0.785 which represents a negligible improvement over our previous model.

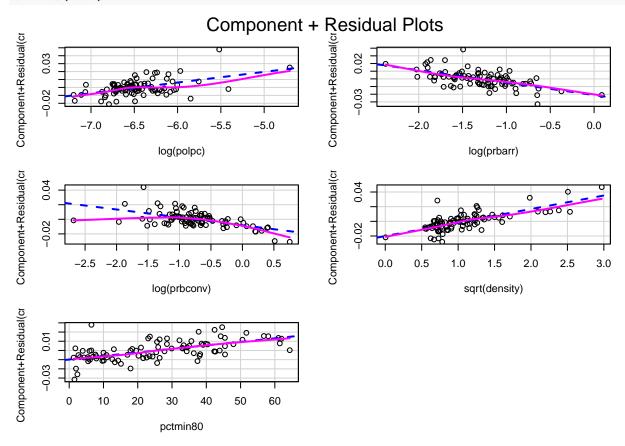
Model 4

One item we wished to investigate is whether we could build a more parsimonious model by selectively removing variables from our second model which did not appear to be significant.

term	estimate	$\operatorname{std.error}$	statistic	p.value
(Intercept)	0.0611285	0.0181177	3.373970	0.0011230

term	estimate	std.error	statistic	p.value
log(polpc)	0.0134516	0.0027352	4.918024	0.0000043
$\log(\text{prbarr})$	-0.0162011	0.0027616	-5.866582	0.0000001
$\log(\text{prbconv})$	-0.0108138	0.0018482	-5.850964	0.0000001
sqrt(density)	0.0184354	0.0023000	8.015235	0.0000000
pctmin80	0.0003842	0.0000572	6.719658	0.0000000





Model Comparison

Below is a comparison table for our three initial models, as well as the fourth model that excluded all non-significant predictors. The table reports key statistics related to each model, including the coefficients for each predictor, the R^2 and adjusted R^2 , and the Akaike information criterion, or AIC.

Our findings match with what we would hope to see from a model building perspective: Our AIC and adjusted R^2 numbers suggest that of our three original models, $Model\ 2$ (which includes both our key explanatory variables and plausible covariates) performs the best. Our model which excludes key covariates has significantly less predictive power (as measured by adjusted R^2), and our model which includes everything—despite having the highest R^2 values—performs slightly less well on the AIC (a measure of explanatory power and parsimony).

Table 6: Linear Models Predicting Crime Rate

	Dependent variable:					
	crmrte					
	(1)	(2)	(3)	(4)		
$\log(\text{polpc})$	$0.020^{***} (0.004)$	$0.014^{***} (0.004)$	$0.016^{***} (0.004)$	0.013*** (0.003)		
log(prbarr)	-0.024***(0.004)	-0.016***(0.003)	-0.013***(0.003)	-0.016***(0.003)		
log(prbconv)	$-0.014^{***}(0.003)$	-0.008***(0.002)	-0.009***(0.002)	-0.011***(0.002)		
prbpris	0.009 (0.018)	$-0.010 \ (0.012)$	$-0.004 \ (0.012)$, ,		
avgsen	-0.001(0.001)	$-0.001\ (0.0004)$	-0.001**(0.0004)			
log(taxpc)	,	0.006(0.005)	$0.004 \ (0.005)$			
sqrt_density		0.018***(0.003)	,			
sqrt(density)		,	$0.017^{***} (0.004)$	0.018*** (0.002)		
govt_wg			-0.00002 (0.00004)	,		
pctymle		$0.064\ (0.048)$	$0.032 \ (0.047)$			
pctmin80		0.0004***(0.0001)	0.0003***(0.0001)	0.0004*** (0.0001)		
wcon		$0.00002 \ (0.00003)$,	,		
wtuc		0.00001 (0.00002)				
wtrd		0.00004 (0.00005)				
wfir		-0.00005(0.00003)				
wser		-0.00001**(0.00001)				
wmfg		$-0.00000 \ (0.00001)$				
wfed		$0.00000 \ (0.00003)$				
wsta		-0.00001(0.00003)				
wloc		$0.00003 \ (0.00005)$				
west		,	-0.006 (0.004)			
central			-0.005*(0.003)			
urban			$0.004\ (0.006)$			
physical_wg			-0.00003(0.00002)			
industry_wg			$0.00003 \ (0.00003)$			
mix			-0.019(0.016)			
Constant	$0.126^{***} (0.033)$	$0.047 \ (0.042)$	0.086* (0.046)	$0.061^{***} (0.018)$		
Observations	90	90	90	90		
\mathbb{R}^2	0.524	0.827	0.824	0.787		
Adjusted R ²	0.495	0.783	0.785	0.775		
Akaike Inf. Crit.	-512.807	-577.971	-580.222	-585.459		

Omitted Variables

Despite the promising results from our three models it is difficult to ascribe causality to the variables of interest. One issue with causal inference in general is ommitted variable bias, which can invalidate our ability to assume each explanatory variable is uncorrelated with the error term. While there are infinite variables which exist, there are several which deserve commentary:

- 1) Political Party in Control: Traditionally the issue of crime policy is a highly partisan issue, with each party having very different approaches to crime reduction. All else being equal, we might expect police levels and average sentence lengths to be correlated with the party that is crafting legislation. Assuming we construct our variable as a boolean indicator ("is_republican"), we might expect the coefficient for police per capita to diminish as we assume a priori that higher police levels are correlated with conservative crime policies. We could include this data by appending public records to our dataset which would be more appropriate than trying to find some other variable to proxy.
- 2) Unemployment Rate: While we have data on weekly wages, this does nothing to tell us what percentage of the population was actually earning those wages. It is likely that a higher unemployment rate would be correlated with higher rates of crime as people who may not normally commit criminal activity are pushed to their limits. We might also wish to be more granular, and include both minority and majority unemployment rates to help control for racial inequality. We realistically could obtain this data from the Bearue of Labor Statistics and append it to our dataset; we leave this next step to future researchers.
- 3) Concentrated/Siloed Urban Blight: Our data is at the county level and therefore may obscure differences within the county. We would expect there to be a difference in crime rates between a county which is relatively homogenous with respect to the variables, and one which has drastic differences (e.g. a very poor area and a very nice area). One way to proxy this might be to calculate a normalized standard deviation of housing prices which could help capture if this phenomenom exists.
- 4) Policing Methodology: In recent years there has been a growing focus on "warrior" versus "guardian" mindsets in policing. Depending on the type of methodology we might see very different rates of arrest and conviction.
- 5) Police Representation: A community's relationship with the police can vary drastically from place to place. In recent years certain cities have had significant unrest, with a key element being a majority white police force existing in a largely minority community. Similar to police methodology, we might expect very different rates of arrest and conviction depending on whether the community feels the police represent them and their interests.
- 6) Criminals' Perception of Risk-Reward Ratios: Of particular relevance to the Model 1 ("Crime and Punishment") analysis is the issue of criminals' perception of the "effectiveness' of the justice system. The model makes two critical assumptions: first, that criminality is driven by rational behavior; second, that criminals have sufficient insight into the outcomes of criminal justice proceedings for their decisions (which we are assuming to be rational) to be informed by them. Obviously if criminals are not of the genus *Homo economicus*, a major theoretical underpinning of the model is removed. However, even if criminals are rational actors, they may be operating with imperfect information: they may make the "incorrect" risk-reward calculation if they are unaware of how risky their criminality truly is. For instance, a thief who does not know the District Attorney always 'gets her man' may not be deterred by a high prbconv as our model might assume. Similarly, the salience of the potential punishment <- TS: Need to finish this thought...

7)

Conclusion: Findings and Policy Recommendations

Unfortunately, we only have a single cross section of data at our disposal and therefore it is nearly impossible to determine whether our variables are causes or effects. In reality it is most likely a combination of both, with

changes in crime rate driving changes in policy, which in turn impact crime rates, ad infinitum. Because our ability to conduct causal inference is restricted, it would be unwise to make specific policy reccomendations based on our model.

We can recommend to our candidate that she advocate for increased investment in research that will investigate the relationships between crime rates and the following factors:

- 1) The number of police per capita
- 2) The likelihood that crimes, once reported, result in arrests
- 3) The likelihood that arrests result in convictions
- 4) The population density in a given area
- 5) The demographic composition in a given area

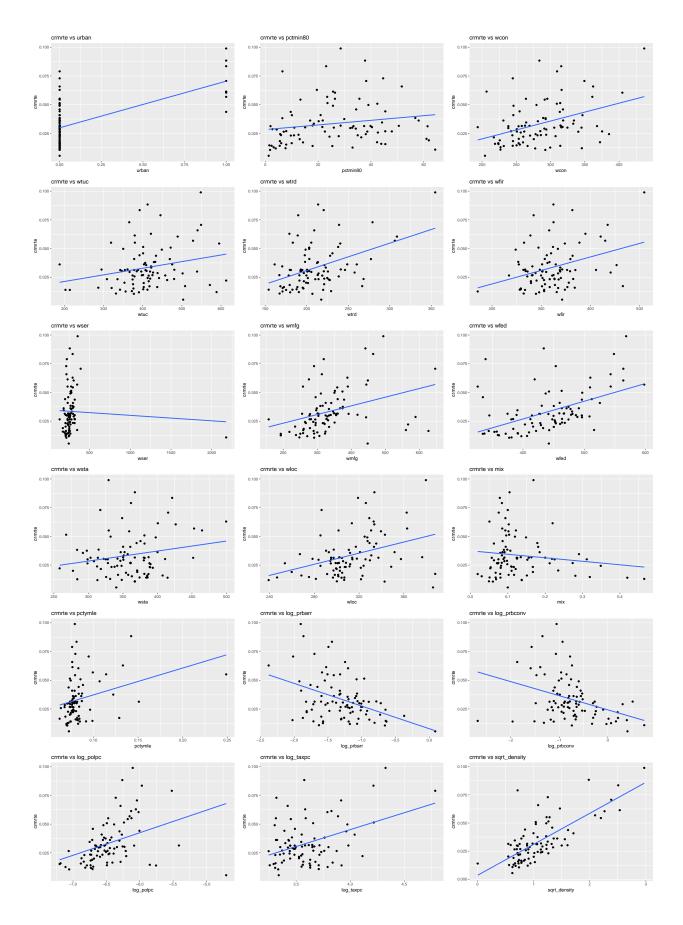
The relationships suggested by our models are intuitive: an increase in the number of police per capita and the population density in an area are associated with (predictive of, in our model) increases in the crime rate; increases in the probability of arrest and probability of conviction are associated with decreases in the crime rate. An increase in the percentage of minority residents is associated with an increase in the crime rate.

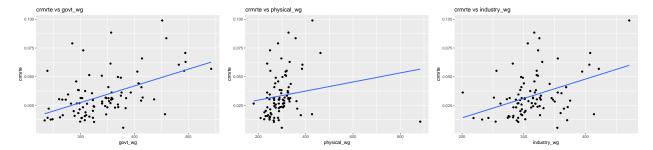
Four of them are simple to interpret: a 1% increase in the number of police is associated with an increase in the crime rate of 11.1 crimes per 100,000 people. Increasing by 1% the probability that a crime report leads to an arrest is associated with a decrease in the crime rate of 15.9 crimes per 100,000 people; a similar increase in the probability of conviction is associated with a decrease in the crime rate of 10.2 crimes per 100,000 people. A 1% increase in the minority share of the population is associated with an increase of 3.8 crimes per 100,000 people. The relationship with the population density is more complex, however, and bears further investigation

Appendix

Detail: scatterplots of variables generated during EDA.

```
make_scatters <- function(df, var_list, y, trans) {</pre>
    if (!missing(trans)) {
        var_list <- append(var_list, str_glue("{trans}({var_list})"))</pre>
    for (v in var_list) {
        print(ggplot(df, aes_string(x = v, y = y)) + geom_point() + geom_smooth(method = "lm",
            se = FALSE) + xlab(v) + ylab(substitute(y)) + ggtitle(str_glue("{y} vs {v}")))
}
make_scatters(crime_na, var_list = names(crime_na), "crmrte")
```





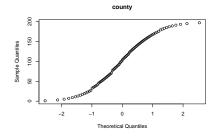
Detail: observations in which the 'probability' variables did not behave as probabilities insofar as they fell outside the range of 0:1.

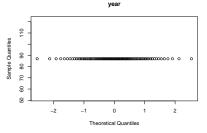
non_prob

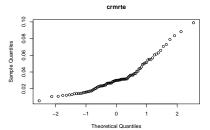
```
## # A tibble: 10 x 25
##
                    crmrte prbarr prbconv prbpris avgsen
                                                               polpc density
      county year
                             <dbl>
                                              <dbl>
                                                      <dbl>
                                                               <dbl>
                                                                        <dbl>
##
       <int> <int>
                      <dbl>
                                      <dbl>
##
    1
           3
                 87 0.0153
                             0.132
                                       1.48
                                              0.450
                                                      6.35 0.000746
                                                                        1.05
##
    2
                87 0.0222
                             0.163
                                              0.333
                                                            0.00202
          19
                                       1.23
                                                     10.3
                                                                       0.577
##
    3
          99
                87 0.0172
                             0.154
                                       1.23
                                              0.557
                                                     14.8
                                                            0.00186
                                                                       0.548
                87 0.00553
                                                      20.7
                                                            0.00905
                                                                       0.386
##
    4
         115
                             1.09
                                       1.5
                                              0.5
                87 0.0291
                                              0.336
                                                            0.00158
##
    5
         127
                             0.180
                                       1.36
                                                     16.0
                                                                       1.34
##
    6
         137
                87 0.0127
                             0.207
                                       1.07
                                              0.323
                                                      6.18 0.000814
                                                                       0.317
##
    7
         149
                87 0.0165
                             0.272
                                       1.02
                                              0.227
                                                     14.6
                                                            0.00152
                                                                       0.609
##
         185
                87 0.0109
                             0.195
                                       2.12
                                              0.443
                                                      5.38 0.00122
                                                                       0.389
    8
         195
                 87 0.0314
                             0.201
                                       1.67
                                              0.471
                                                     13.0
                                                                       1.75
##
    9
                                                            0.00446
## 10
         197
                 87 0.0142
                             0.208
                                       1.18
                                              0.361
                                                     12.2 0.00119
                                                                       0.890
     ... with 16 more variables: taxpc <dbl>, west <int>, central <int>,
       urban <int>, pctmin80 <dbl>, wcon <dbl>, wtuc <dbl>, wtrd <dbl>,
## #
## #
       wfir <dbl>, wser <dbl>, wmfg <dbl>, wfed <dbl>, wsta <dbl>,
## #
       wloc <dbl>, mix <dbl>, pctymle <dbl>
```

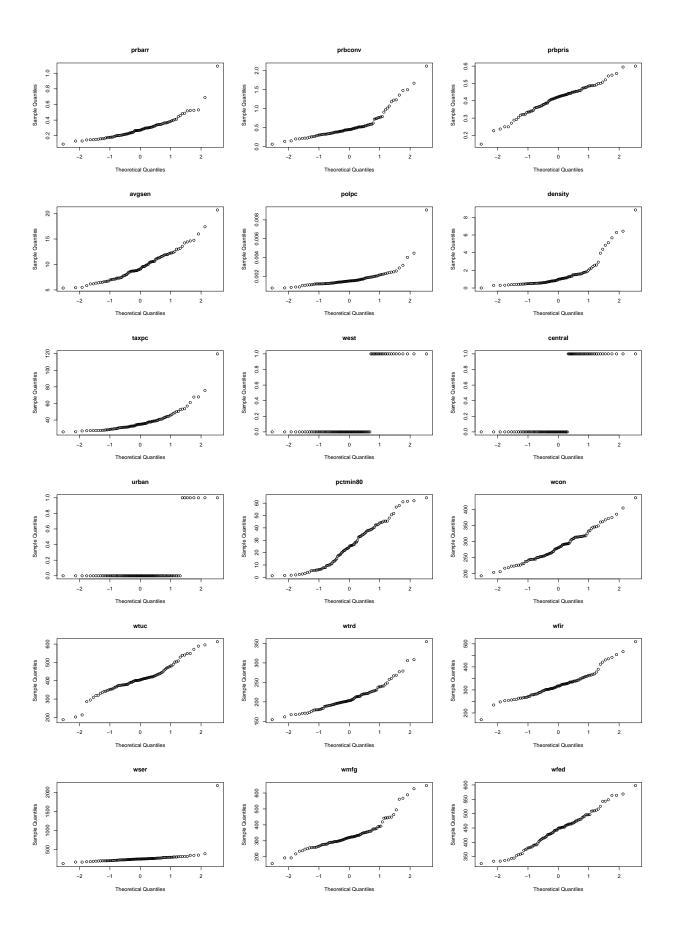
Detail: code to generate qqplots for evaluation of normality in EDA step

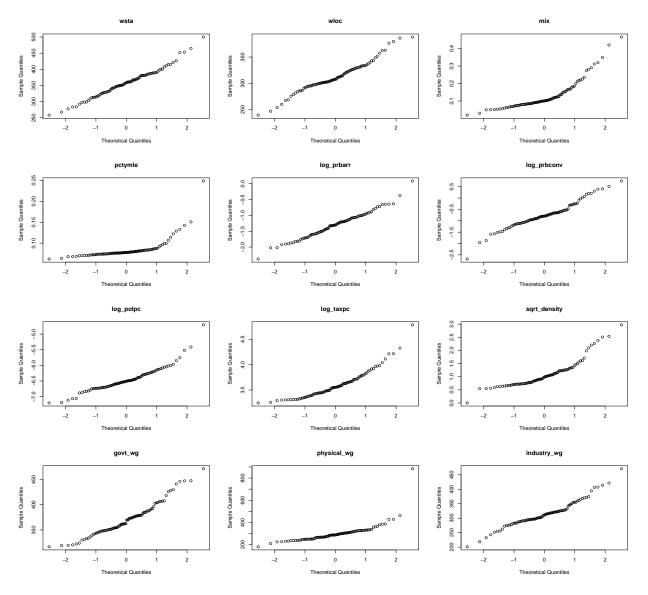
```
for (i in 1:length(colnames(crime_na))) {
    column_interest <- paste("crime_na$", colnames(crime_na)[i], sep = "")
    qqnorm(eval(parse(text = column_interest)), main = colnames(crime_na)[i])
}</pre>
```





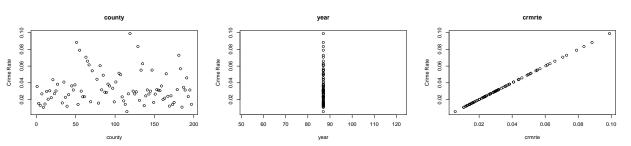


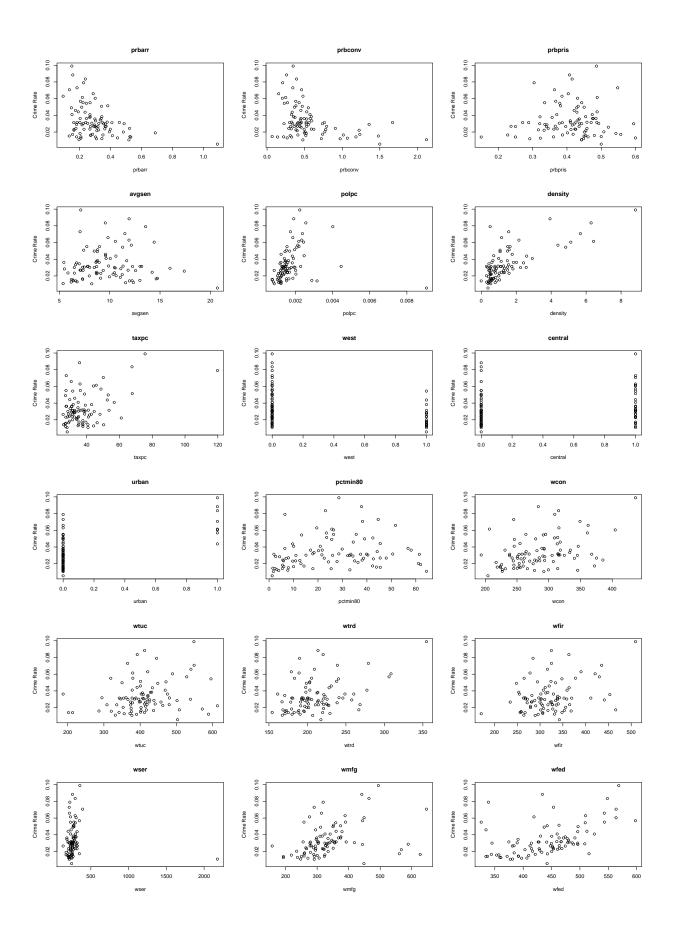


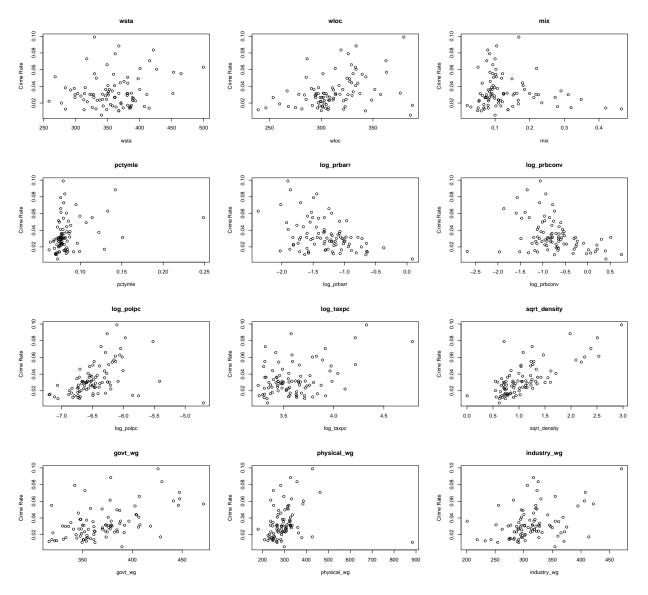


Detail: code to explore 'crime rate' vs. specific variables of interest

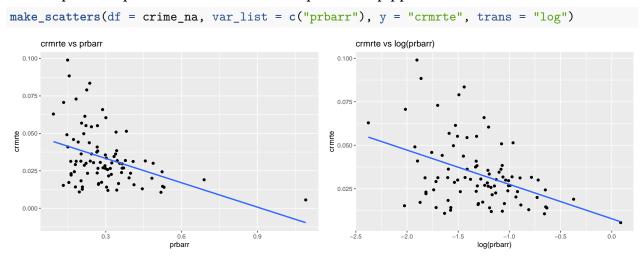
```
for (i in 1:length(colnames(crime_na))) {
    column_interest <- paste("crime_na$", colnames(crime_na)[i], sep = "")
    plot(eval(parse(text = column_interest)), crime_na$crmrte, main = colnames(crime_na)[i],
        ylab = "Crime Rate", xlab = colnames(crime_na)[i])
}</pre>
```



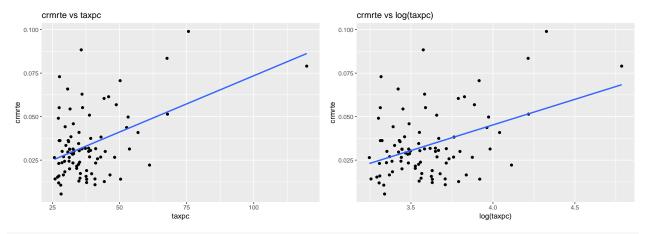




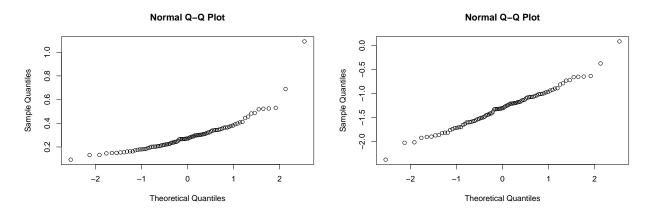
Detail: pre- and post-transformation scatterplots and q-q plots



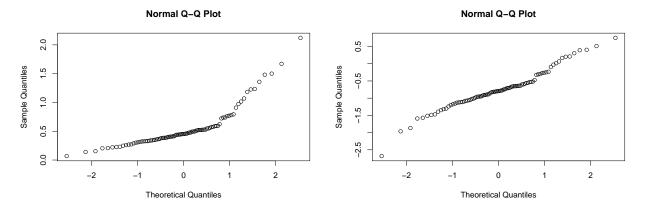
```
make_scatters(df = crime_na, var_list = c("prbconv"), y = "crmrte", trans = "log")
                                                                   crmrte vs log(prbconv)
      crmrte vs prbconv
  0.100 -
                                                               0.100 -
  0.075
                                                               0.075
                                                              0.050
  0.025
  0.000
                                                                                          log(prbconv)
make_scatters(df = crime_na, var_list = c("polpc"), y = "crmrte", trans = "log")
      crmrte vs polpc
                                                                   crmrte vs log(polpc)
  0.100 -
                                                               0.100 -
  0.075
                                                               0.075
                                                              0.050
  0.025
                                                               0.025
                               0.0050
polpc
                                              0.0075
                 0.0025
                                                                                           -6.0
log(polpc)
make_scatters(df = crime_na, var_list = c("density"), y = "crmrte", trans = "sqrt")
      crmrte vs density
                                                                   crmrte vs sqrt(density)
                                                               0.100 -
  0.100 -
                                                               0.075
  0.075
cmre 0.050
                                                              o.050
  0.025
                              5.0
density
                                                                                          sqrt(density)
make_scatters(df = crime_na, var_list = c("taxpc"), y = "crmrte", trans = "log")
```



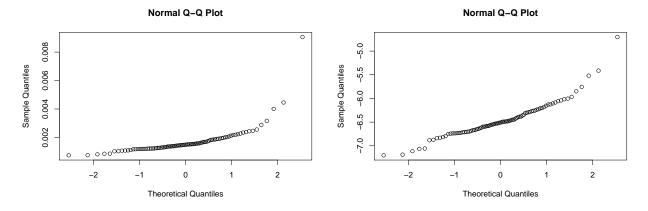
Normality/skew with and without transformations
print(c(qqnorm(crime_na*prbarr), qqnorm(log(crime_na*prbarr))))



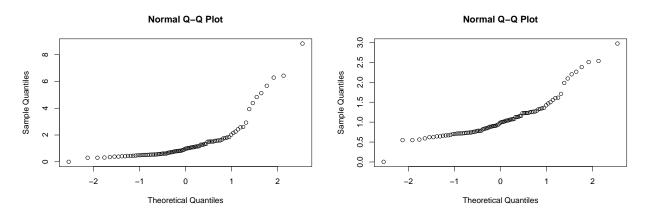
print(c(qqnorm(crime_na\$prbconv), qqnorm(log(crime_na\$prbconv))))



print(c(qqnorm(crime_na\$polpc), qqnorm(log(crime_na\$polpc))))



print(c(qqnorm(crime_na\$density), qqnorm(sqrt(crime_na\$density))))



print(c(qqnorm(crime_na\$taxpc), qqnorm(log(crime_na\$taxpc))))

