

Exercise 1 chart for recursive Graph-Exploration

(Take **s** as starting vertex and scan adjacency list from left to right)

Vertex	Adj. Vertices	seen	p (predecessor)
s	a m		
a	m c d		
m	b d		
b	d		
c	t		
d	t		
t			

Exercise 2 chart for recursive Graph-Exploration

(Take **d** as starting vertex and scan adjacency list from left to right)

Vertex	Adj. Vertices	seen	p (predecessor)
s	a m		
a	m c d		
m	b d		
b	d c s		
c	t s m		
d	a c t		
t	b		

stack-based

Vertex	Adj. Vertices	seen	p (predecessor)
s	a m		
a	m c z		
m	b z		
b	z		
c	t		
z	t		
t			

destination “z”

Tick mark “s” as seen, push it onto a stack

```
while stack is not empty
```

 $\{$

cc = value popped from stack

if **cc** is destination

$$\{$$

job done: path is found

display it using predecessor data

}

else

 $\{$

for each of **its** (**cc**) unseen Adj. Vertices

Tick mark **it** (Adj. Vertex) as seen,

$p = \mathbf{cc}$ // Assign \mathbf{cc} to \mathbf{its} (Adj. Vertex) p (predecessor)

push **it** (Adj. Vertex) onto the stack

}

}

If Stack is empty: Path not found → display path not found message

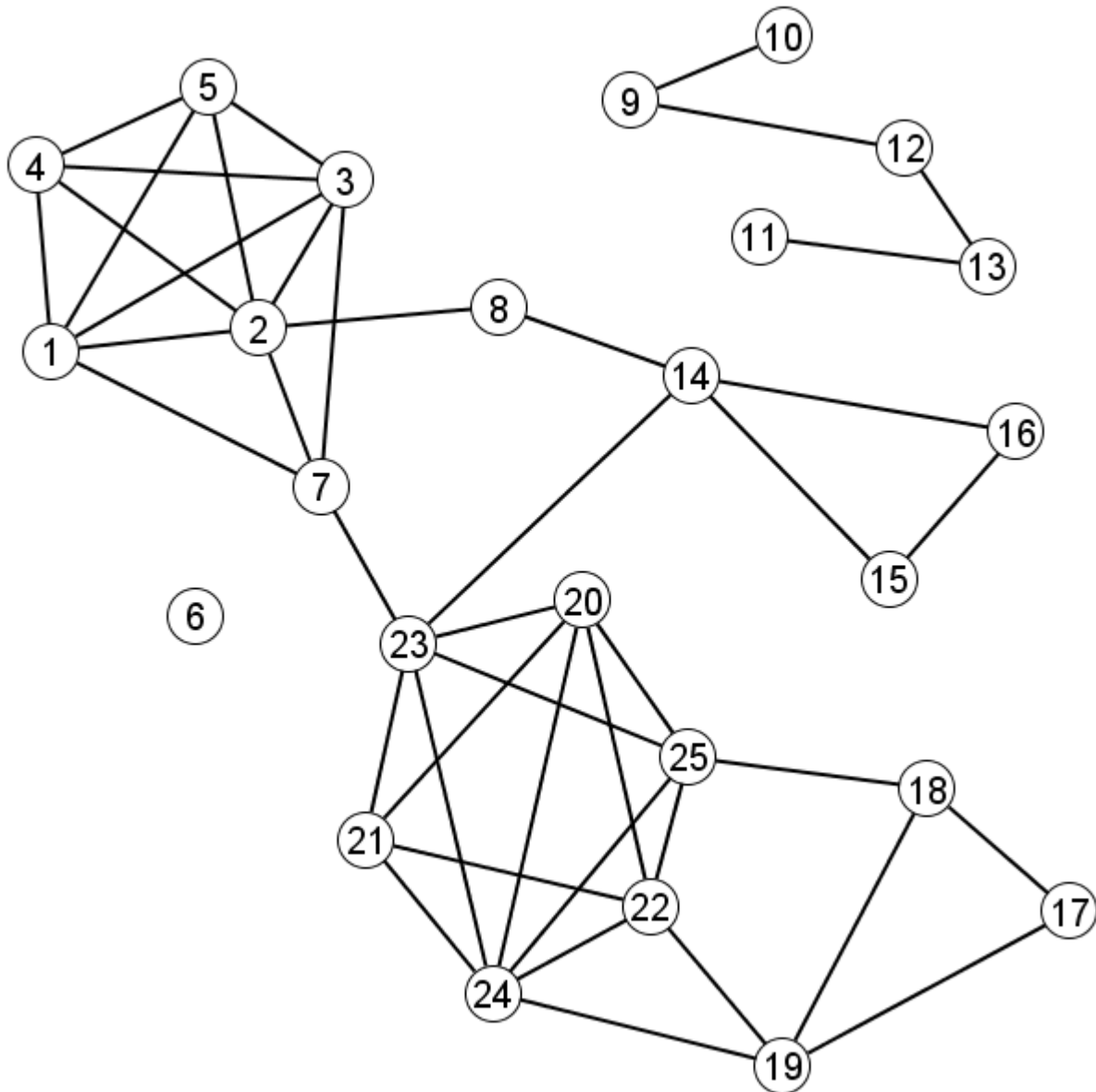
[illegible]

Run BFS (start from 20) and DFS on it

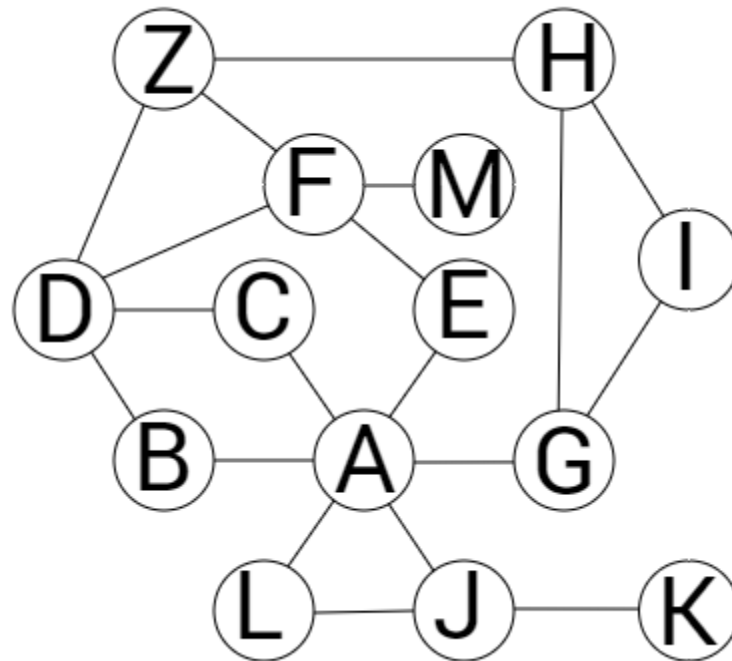
1. to compute d, p for BFS and d, f and p

2. Can you make its adjacency list and show working on it

3. Put random arrows and run DFS again

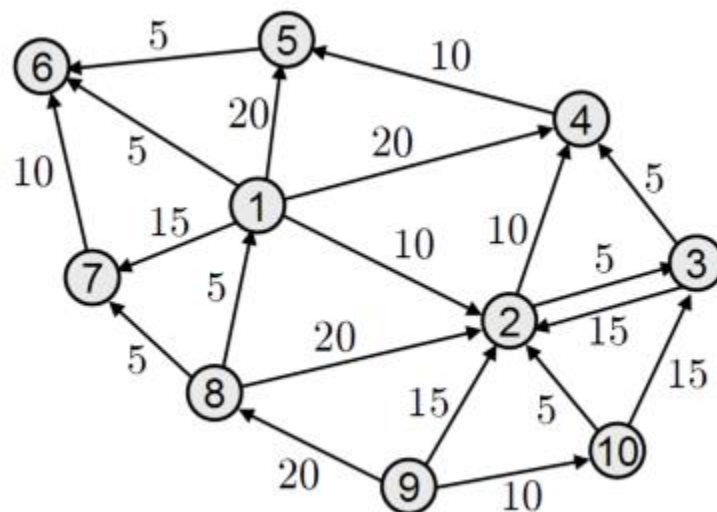


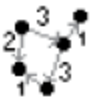



Make its adjacency matrix and run BFS (start M) on it to compute P only



Run Dijkstra algo on the following graph twice

1. Take 9 as source vertex
2. Take 3 as source vertex

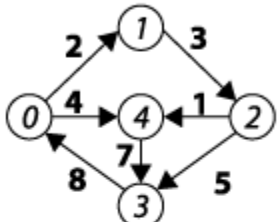


DIJKSTRA'S ALGORITHM PQ			 Weighted Directed Graph  Priority queue  Array  Overflow
Best	Average	Worst	
$O((V + E) \cdot \log V)$	same	same	

singleSourceShortest (G, s)

- PQ = new Priority Queue
- foreach** $v \in V$ **do**
- $\text{dist}[v] = \infty$
- $\text{pred}[v] = -1$
- $\text{dist}[s] = 0$
- foreach** $v \in V$ **do**
- insert ($v, \text{dist}[v]$) into PQ
- while** (PQ is not empty) **do**
- $u = \text{getMin}(\text{PQ})$
- foreach** neighbor v of u **do**
- $w = \text{weight of edge } (u,v)$
- $\text{newLen} = \text{dist}[u] + w$
- if** ($\text{newLen} < \text{dist}[v]$) **then**
- decreaseKey (PQ, v, newLen)
- $\text{dist}[v] = \text{newLen}$
- $\text{pred}[v] = u$
- end**

Create PQ from neighbors v of vertex $s = 0$ based on $\text{dist}[v]$



	0	1	2	3	4
$\text{dist}[v]$	0	∞	∞	∞	∞

1st iteration: remove 0 and adjust

	0	1	2	3	4
$\text{dist}[v]$	0	2	∞	∞	4

(0,0) + (0,1) < (0,1)
(0,0) + (0,4) < (0,4)

2nd iteration: remove 1 and adjust

	0	1	2	3	4
$\text{dist}[v]$	0	2	5	∞	4

(0,1) + (1,2) < (0,2)

3rd iteration: remove 4 and adjust

	0	1	2	3	4
$\text{dist}[v]$	0	2	5	11	4

(0,4) + (4,3) < (0,3)

4th iteration: remove 2 and adjust

	0	1	2	3	4
$\text{dist}[v]$	0	2	5	10	4

(0,2) + (2,3) < (0,3)

5th iteration: remove 3 and done

	0	1	2	3	4
$\text{dist}[v]$	0	2	5	10	4