

On the Role of Chain of Thought in Long Test-Time In-Context Learning

Anonymous ACL submission

Abstract

In-Context Learning (ICL) has emerged as a powerful paradigm for adapting Large Language Models (LLMs) to new tasks without gradient updates. While advances in long-context models have enabled a shift from few-shot to many-shot ICL, research has largely focused on non-reasoning tasks. Therefore, we target to address the underexplored behavior of Chain-of-Thought (CoT) prompting in many-shot scenarios, explaining the shift from studies in how to select appropriate ICL examples to how to enable LLMs to evolve their understanding at test-time. We present a comprehensive analysis of many-shot in-context CoT learning, uncovering behavioral differences between reasoning-oriented and non-reasoning oriented LLMs. Our findings show that with both types of models, there is a fundamental difference from earlier studies in the ICL setting. Crucially, we find that demonstration selection and ordering remain critically important, while semantic similarity, which is a strong heuristic for few-shot ICL and RAG, becomes ineffective. We propose that effective manyshot CoT-ICL functions as a parameter-free, test-time learning process. Supporting this, we show that (1) self-generated demonstrations (where the model creates its own training curriculum) outperform ground-truth or stronger-model demonstrations, particularly for weaker models, and (2) smoothly ordered demonstrations (measured via embedding space curvature) significantly enhance performance, mirroring principles of curriculum learning. Our findings bridge manyshot ICL with test-time scaling paradigms, reframing the context window not as a static retrieval database, but as a dynamic, structured learning environment that triggers latent model capabilities.

1 Introduction

In-context learning (ICL) enables large language models (LLMs) to perform tasks by conditioning

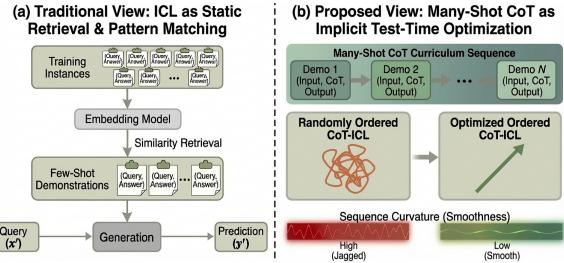


Figure 1: Reframing of CoT-ICL as test-time learning.

on a sequence of input-output demonstrations without updating their parameters (Min et al., 2022; von Oswald et al., 2023). Research has focused on improving ICL through strategies like selecting effective demonstrations (Sorensen et al., 2022; ?). Recently, with the expansion of context windows, many-shot ICL has emerged, where dozens to hundreds of demonstrations can be provided, achieving performance competitive with fine-tuning (Agarwal et al., 2024; Bertsch et al., 2025). A consistent finding in this setting is that for non-reasoning tasks (e.g., classification), the impact of demonstration order diminishes with scale (Bertsch et al., 2025; Baek et al., 2025).

Meanwhile, chain-of-thought (CoT) prompting has become essential for complex reasoning tasks (e.g., arithmetic, narrative), where models generate intermediate reasoning steps before producing an answer (Wei et al., 2022; Kojima et al., 2022). Concurrently, the paradigm of test-time scaling investigates how to improve LLMs during inference without weight updates, through methods like sequential revision and parallel sampling (Snell et al., 2025; Lin et al., 2024). These threads connect naturally: many-shot ICL with CoT represents a fundamental form of test-time computation, where demonstrations guide the model’s behavior and understanding.

However, a critical gap exists. Our understanding of many-shot dynamics derives almost entirely

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from studies of non-reasoning tasks. It remains unknown whether the established principles (e.g., that order matters less and similarity-based selection works) extend to many-shot CoT-ICL for reasoning. Does providing more reasoning demonstrations lead to reliable improvement, or does it introduce new instabilities? This question is practically important for deploying reasoning-capable LLMs and theoretically fundamental: it probes whether ICL for reasoning is merely large-scale pattern matching or a form of genuine in-context learning that follows pedagogical principles.

In this work, we demonstrate that the established rules of many-shot ICL break down for reasoning tasks. Through systematic experiments across model types (non-reasoning vs. reasoning-oriented) and tasks (non-reasoning vs. reasoning), our experiment uncover: (1) non-reasoning LLMs show negligible or negative gains from increasing CoT demonstrations; (2) Performance becomes more unstable with more demonstrations, indicating increased sensitivity to their order; and (3) Standard similarity-based retrieval consistently underperforms.

We explain these results by reframing effective many-shot CoT as in-context learning rather than pattern matching. We propose that successful demonstrations must be both understandable to the model and smoothly sequenced. We formalize this through two principles: (1) The Ease of Understanding: demonstrations should align with the model’s current knowledge (explaining why self-generated demonstrations work best for weaker models); and (2) The Smoothness of Knowledge Progression: the conceptual transition between consecutive demonstrations should be gradual (quantifiable via the curvature of their embedding trajectory).

Building on these principles, we introduce Curvilinear Demonstration Selection (CDS), a practical method that orders demonstrations to minimize total conceptual curvature. This approach yields an average of 3.45% performance gains across both math and narrative reasoning tasks.

Our contributions are threefold: (1) We explore the dynamic with CoT-ICL; (2) We reframe effective many-shot CoT through the lens of comprehensibility and curricular smoothness, bridging ICL with insights from test-time learning; (3) We introduce and validate a practical, principle-driven method for demonstration ordering that advances many-shot reasoning as illustrated in Figure 1.

2 Related Works

2.1 Many-shot ICL

The extension of LLM context windows (Peng et al., 2024; Han et al., 2024) has enabled many-shot ICL, where models process significantly more demonstrations (Agarwal et al., 2024). Initial findings revealed that with sufficient demonstrations, model sensitivity to their ordering diminishes for standard classification tasks (Baek et al., 2025; Bertsch et al., 2025), suggesting a form of robustness with scaling. This led to a narrative that in many-shot settings, careful demonstration engineering may be unnecessary. However, these studies focused overwhelmingly on non-reasoning tasks (e.g., classification, simple QA) (Baek et al., 2025; Bertsch et al., 2025). Concurrent work on test-time scaling leveraging extended computation for self-improvement without parameter updates (Snell et al., 2024; Li et al., 2025), suggests that effective in-context learning can be viewed as a form of real-time optimization. Our work connects many-shot CoT-ICL to test-time learning, guided by two key principles that explain how learning occurs inside.

2.2 Chain-of-Thought

CoT prompting (Wei et al., 2022) decomposes reasoning into intermediate steps, substantially improving LLM performance on complex tasks. Subsequent studies like Tree-of-Thoughts (Yao et al., 2023) and Program-of-Thoughts (Chen et al., 2023) explore structured reasoning paths, while methods like rStar-Math (Guan et al., 2025) employ search algorithms for trajectory optimization. These approaches primarily focus on enhancing the reasoning process for a single query. In the ICL setting, Dr.ICL (Luo et al., 2023) demonstrates that retrieving relevant CoT demonstrations boosts few-shot performance. However, a critical gap remains with all existing CoT-ICL work operates in the few-shot settings. The fundamental question of how CoT demonstrations scale with context length and whether the principles of effective demonstration design change from few-shot to many-shot is largely unexplored. Our work positions many-shot CoT not merely as "more examples", but as a potential in-context curriculum that requires principled sequencing.

2.3 Demonstration Selection

Demonstration selection has long been studied for effective few-shot ICL. The dominant paradigm is

similarity-based retrieval, where demonstrations semantically closest to the test query are selected (Liu et al., 2022; Wu et al., 2023; Kapuriya et al., 2025). This approach implicitly frames ICL as a form of nearest-neighbor pattern matching. Interestingly, this paradigm finds a direct analogy in Retrieval-Augmented Generation (RAG), where relevant context chunks are retrieved via embedding similarity (Lewis et al., 2020). Our work challenges whether this conclusion extends to reasoning tasks. We hypothesize that for CoT-ICL, effective demonstration selection is less about retrieving semantically similar examples and more about constructing a smooth learning sequence that facilitates conceptual understanding, acting as a shift from "retrieval for matching" to "retrieval for learning".

3 Experimental Setup

We establish a comprehensive experimental framework to study the factors influencing many-shot Chain-of-Thought In-Context Learning (CoT-ICL). Our framework focuses on three core dimensions: **Tasks Type** (non-reasoning vs. reasoning), **LLMs Type** (non-reasoning vs. reasoning LLMs), and **ICL Configuration** (format and scale).

3.1 Tasks Studied

Previous studies in many-shot (Li et al., 2024; Bertsch et al., 2025) have focused primarily on non-reasoning tasks. We bridge this gap by evaluating a diverse set of benchmarks spanning both classification and reasoning domains. All tasks are formulated as open-ended text generation. The model's raw output is matched against the reference answer or label with extra match.

Non-Reasoning Tasks. These tasks require minimal intermediate reasoning. We include tasks with varying label-space complexity, including SuperGLUE (Wang et al., 2019) (narrow label space), NLU (nlu, 2021), TREC (Hovy et al., 2001), and BANKING77 (Casanueva et al., 2020) (large label space).

Reasoning Tasks. These tasks require logical deduction and math derivation. We focus on mathematical reasoning with GSM8K (Cobbe et al., 2021) and MATH (Hendrycks et al., 2021). Additionally, we include DetectiveQA (Xu et al., 2025) for narrative reasoning over long contexts. All datasets provide ground-truth reasoning chains (C_i) for deriving the answer (y_i), enabling CoT-ICL.

3.2 LLMs Studied

We compare performance of varies LLMs in long context settings, categorized by their inherent reasoning design.

Non-Reasoning LLMs. These models lack a dedicated internal reasoning mechanism and are typically instructed-tuned for direct response, including LLaMA 3.1 (Llama-3.1-8B-Instruct), LLaMA 3.3 (Llama-3.3-70B-Instruct) (MetaAI, 2024), Qwen 2.5 (7B) (Qwen2.5-7B-Instruct) and Qwen 2.5 (14B) (Qwen2.5-14B-Instruct).

Reasoning LLMs. These models are explicitly trained with a reasoning token (e.g., <think>), including Qwen 3 (8B) (Qwen3-8B), Qwen 3 (14B) (Qwen3-14B) (Yang et al., 2025) QwQ (32B) (QwQ-32B) (Qwen et al., 2025) and R1 (685B) (DeepSeek-R1) (DeepSeek-AI et al., 2025). For these models, we enable thinking token generation during inference.

To support the extended context required for many-shot evaluations (up to 131K tokens for Qwen family models), we applied official RoPE scaling configuration modifications.

3.3 ICL Configuration

We study performance from few-shot to many-shot under two prompting paradigms.

Traditional ICL. LLMs receives input-output pairs (x_i, y_i) . Given an input x' , it generates an answer $y' = \text{LLM}(x' | \{(x_i, y_i)\}_{i=1}^k)$.

CoT-ICL. LLMs receives triplets of input, reasoning chain, and output, i.e., (x_i, C_i, y_i) . Given an input x' , it generates both a reasoning chain C' and final answer $y' = \text{LLM}(x' | \{(x_i, C_i, y_i)\}_{i=1}^k)$.

Context Scaling. The token length of CoT-ICL is substantially larger than that of traditional ICL (e.g., geometry problems are about 30 times longer than BANKING77 examples). Therefore, while models can process hundreds to thousands of traditional ICL demos, the context window typically limits CoT-ICL to hundreds demonstrations. Our analysis focuses on this scaling range (up to 128 demonstrations), where we observe the most informative dynamics between model capability, task type, and demonstration count.

267 4 Properties of CoT-ICL

268 4.1 Scaling with Non-Reasoning LLMs

269 While recent work demonstrates that many-shot
 270 ICL yields consistent gains for non-reasoning
 271 tasks (Bertsch et al., 2025; Baek et al., 2025), we
 272 find this scaling behavior does not generalize to
 273 reasoning tasks with CoT prompts. Figure 2 reveals
 274 that non-reasoning tasks exhibit steady improve-
 275 ment with more demonstrations, whereas math rea-
 276 soning performance fluctuates or declines with
 277 non-reasoning LLMs for most of the tasks (especial-
 278 ly for math reasoning tasks).

279 This failure to scale is not simply a limitation of
 280 model size. As shown in the left subplot of Figure 3,
 281 even the 70B-parameter Llama 3.3 shows negative
 282 gains. This contrasts with the effect of scaling
 283 observed in previous many-shot ICL, suggesting a
 284 qualitative difference in how LLMs process long
 285 CoT-ICL.

286 4.2 Scaling with Reasoning LLMs

287 In contrast to non-reasoning LLMs, models with
 288 explicit reasoning capabilities exhibit a fundamen-
 289 tally different scaling pattern. As shown in right
 290 subplot of Figure 3, QwQ (32B) demonstrates clear
 291 positive scaling with additional demonstrations.
 292 This pattern holds for smaller reasoning-optimized
 293 models as well: the Qwen3 family (Figure 4) shows
 294 consistent performance gains as the number of
 295 demonstrations increases. LLMs with reasoning
 296 capabilities (enabled via thinking tokens or spe-
 297 cialized training) successfully leverage additional
 298 CoT demonstrations to improve performance on
 299 reasoning tasks. The divergence in scaling behavior
 300 between model types highlights that the ability to
 301 benefit from many-shot CoT is not merely a func-
 302 tion of pattern matching, but is intrinsically linked
 303 to a model’s capacity for in-context reasoning.

304 4.3 Instability of Many-shot CoT-ICL

305 The divergent scaling patterns suggest that the se-
 306 quence of demonstrations may be critical for CoT-
 307 ICL. To test this, we measure performance vari-
 308 ance across five random orderings of the same
 309 demonstration set. Prior work finds that vari-
 310 ance decreases with more demonstrations for non-
 311 reasoning tasks (Baek et al., 2025), indicating that
 312 order becomes less important. We observe the same
 313 for classification tasks in the left subplot in Fig-
 314 ure 5.

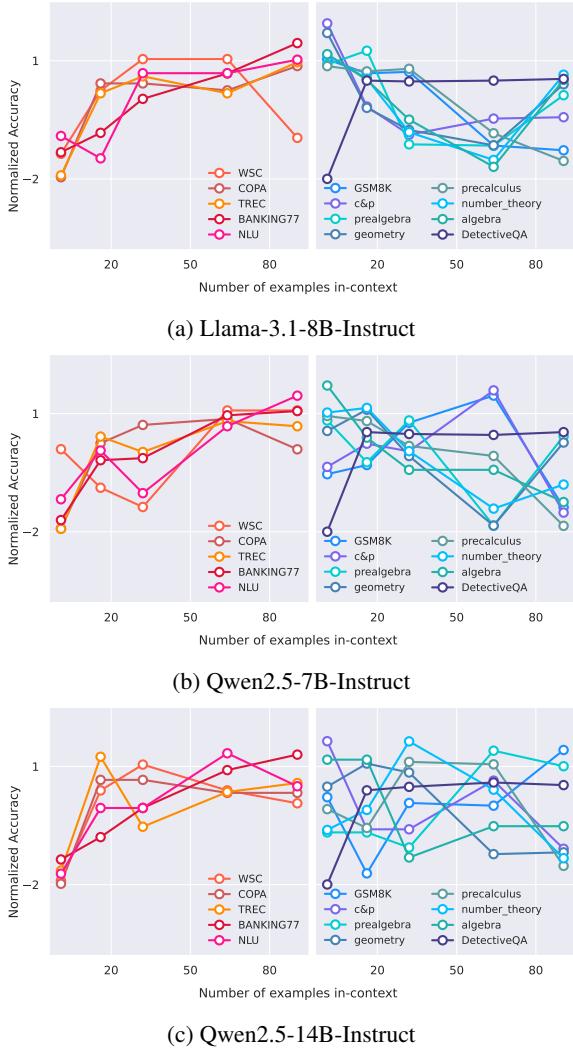


Figure 2: Scaling disparity between task types. Performance (normalized accuracy) of non-reasoning LLMs on classification tasks (**warm colors**) versus reasoning tasks (**cool colors**). The x-axis represents normalized accuracy (i.e., $\frac{x-\bar{x}}{\sigma_x}$ for accuracy x), while the y-axis indicates the number of in-context demonstrations.

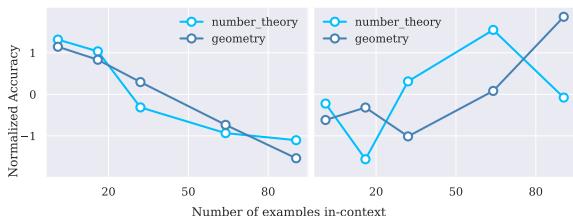


Figure 3: Scaling disparity between model types on math reasoning tasks. **Left:** Llama 3.3 (non-reasoning LLM) shows negative gains. **Right:** QwQ (32B) (reasoning LLM) shows clear positive scaling.

315 However, for reasoning tasks with CoT, we find
 316 the opposite trend. Variance increases with more
 317 demonstrations as shown in the right subplot in

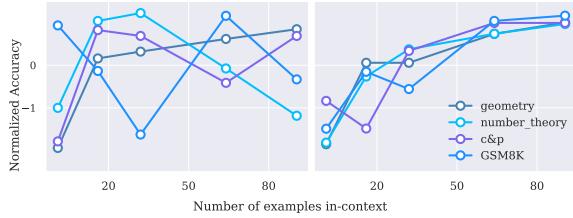


Figure 4: Positive scaling of reasoning LLMs. The Qwen3 family (reasoning LLMs) demonstrates consistent performance improvements with more demonstrations on math reasoning tasks. **Left:** Qwen3 (8B) **Right:** Qwen3 (14B)

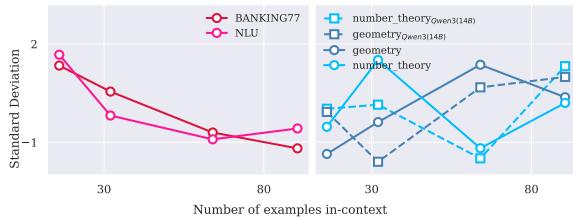


Figure 5: Standard deviation of performance across five random demonstration orders on classification tasks (warm colors) versus reasoning tasks (cool colors). Results shown for Qwen2.5 (14B) (**Left**, non-reasoning) and Qwen3 (14B) (**Right**, reasoning).

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Figure 5. This holds for both non-reasoning and reasoning LLMs, revealing a key instability finding: Many-shot CoT exhibits increasing sensitivity to demonstration order as context length grows, unlike non-reasoning ICL where order becomes less important.

This increasing instability indicates that simply adding more CoT examples can introduce confusing signal. The model’s performance becomes highly path-dependent, suggesting that the progression of reasoning steps across demonstrations is a critical, previously overlooked factor in CoT-ICL.

330 4.4 Rethinking the role of similarity

331 Given the importance of order, we investigate
332 whether standard retrieval heuristics can identify
333 helpful demonstrations. In few-shot ICL and
334 retrieved-augmented generation (RAG), retrieving
335 demonstrations semantically similar to the query is
336 highly effective (Liu et al., 2022; Wu et al., 2023).
337 We test this in the many-shot CoT setting using
338 Qwen3-Embedding-4B (Zhang et al., 2025) to con-
339 struct “most similar” and “most dissimilar” demon-
340 stration sets. Specifically, we construct two unified
341 sets of in-context examples: one comprising the
342 most semantically similar examples and the other

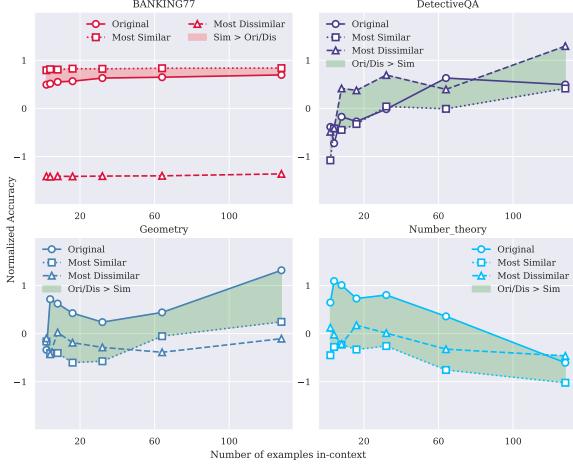


Figure 6: Performance with original(ori), similarity(sim) and dissimilar(dis) sets averaged across five LLMs. The area between the two sets is filled with colors, indicating the relative performance at each point. The normalization is performed with the mean and standard deviation computed over the concatenated sets of ori, sim and dis.

comprising the most dissimilar examples to the test set. Similarity is measured by computing the cosine similarity between question embeddings, averaged across the entire test set. The training set instances form the candidate pool for constructing the similar and dissimilar example sets. Experiments are conducted and averaged over five LLMs, including Llama 3.1, Qwen 2.5 family (7B and 14B) and Qwen 3 family (8B and 14B).

The results in Figure 6 reveal an opposite pattern. For the BANKING77 classification task, similar examples outperform dissimilar ones, aligning to prior findings. For all three reasoning tasks (geometry, number_theory, DetectiveQA), the dissimilar set or the original set consistently outperform the similar set as the number of demonstrations increases. Performance for separated evaluated on reasoning and non-reasoning LLMs is in Appendix B and same conclusion is drawn when looking separately on different types of LLMs.

This failure suggests that reasoning tasks require a deeper, structural understanding of the problem space rather than surface-level pattern matching. Similar questions may cluster in solution strategy, providing redundant learning signal, while diverse (dissimilar) examples might better scaffold the model’s understanding of the reasoning process itself.

371 **5 Rethinking ICL: From Pattern**
372 **Matching to Test-Time Learning**

373 Our empirical findings in Section 4.3 and 4.4
374 present a puzzling contradiction, while CoT-ICL
375 shows a promising trend with manyshot, it ex-
376hibits increasing sensitivity to demonstration or-
377 der and fails to benefit from established heuristics
378 like similarity-based selection. We propose a con-
379 ceptual shift to explain these observations: rather
380 than viewing ICL as mere pattern matching in an
381 extended context, we should conceptualize it as
382 test-time learning—a form of gradient-free opti-
383 mization occurring within the forward pass. This
384 reframing provides a principled basis for under-
385 standing what makes demonstrations effective and
386 leads us to formulate two complementary prin-
387 ciples for demonstration design.

388 **5.1 Test-Time Learning**

389 The success of simple heuristics like retrieving
390 demonstrations similar to the query in such settings
391 supports this pattern-matching view. However, our
392 findings in Section 4.3, particularly the increasing
393 variance with more demonstrations in reasoning
394 tasks and the failure of similarity-based selection,
395 directly contradict this interpretation for the many-
396 shot CoT setting.

397 We posit that when provided with many demon-
398 strations, especially those involving complex rea-
399 soning chains, the LLM engages in a more pro-
400 found form of in-context learning: it is not merely
401 recognizing a pattern, but actively constructing
402 or refining an internal "algorithm" or reasoning
403 schema based on the provided examples. This also
404 aligns with the emergent perspective of test-time
405 scaling and its effectiveness (Snell et al., 2024).

406 This learning analogy helps explain our key ob-
407 servations,

- **The importance of order:** Effective learning typically follows a curriculum—from simple to complex, or following logical progression. Random ordering disrupts this progression, leading to unstable "learning" outcomes.
- **The failure of similarity:** When learning a new concept, the most similar examples are often redundant and do not expand the model's understanding. Conversely, diverse examples that cover different facets of a problem can provide richer learning signals.

Effective demonstration selection for ICL re-
quires retrieving pedagogically useful examples,
those that facilitate learning the task itself rather
than just providing answers. Similarly, test-time
scaling methods like self-critique use multiple for-
ward passes to iteratively refine outputs; many-shot
ICL can be seen as a parallel, one-pass version
of this refinement, where multiple demonstrations
collectively shape the model's reasoning trajectory.

428 **5.2 The Ease of Understanding**

If ICL functions as test-time learning, then demon-
strations must be comprehensible to the model
within its current capabilities. Drawing from ed-
ucational psychology, effective instruction oper-
ates within a learner's "zone of proximal develop-
ment" (Benson, 2020), the space between what
they can do independently and what they can
achieve with guidance. We hypothesize that effec-
tive demonstrations must reside within the model's
"zone of understandable reasoning."

Settings. To test this principle, we investigate
whether demonstration efficacy depends more on
reasoning quality or alignment with the model's
own generative patterns. We generate CoT demon-
strations by prompting each LLM on training in-
stances and categorize them into three sets:

- **Correct Set (cr):** Model-generated CoT with correct final answers
- **Incorrect Set (wr):** Model-generated CoT with incorrect final answers
- **First Set (first):** The first generation for each instance, regardless of accuracy

These are compared against the dataset's
groundtruth CoT (i.e., origin). Each LLM is
prompted 10 times per training instance with tem-
perature=1.0 to ensure diversity. Due to high accu-
racy on GSM8K, the wr set is constructed only for
number_theory and geometry tasks. Additionally,
we evaluate whether "better" CoT from stronger
models (i.e., Qwen 2.5 (14B)) improves weaker
model performance.

Results. Figure 7 reveals that the wr set (in-
correct reasoning) consistently outperforms the orig-
inal CoT and performs comparably to the cr set
across both LLMs and tasks. This demonstrates
that distributional alignment with the model's own
reasoning style, even when flawed, contributes

more to stable CoT prompting than the presence of correct answers.

Furthermore, self-generated CoT (any of cr, wr, or first sets) significantly mitigates the instability issues observed with origin CoT. The first set, the model’s natural first attempt at each problem, also outperforms origin CoT (Figure 8), reinforcing that distributional alignment is paramount.

When using CoT from stronger models, we observe a mixed pattern: while occasional performance gains occur, instability persists (olive lines in Figures 7 and 8). This suggests that reasoning patterns too advanced for the target model can disrupt rather than enhance learning, similar to teaching advanced concepts before fundamentals.

Interpretation. These findings support that the effective demonstrations for in-context learning are those that the model can naturally comprehend and relate to its existing knowledge structures. Self-generated CoT, even when incorrect, provides such "understandable examples" by matching the model’s own reasoning distribution, facilitating more stable test-time learning. It is also related to the LLM’s internal ability to comprehend demonstration context. For demonstrations that are not understandable by LLMs (i.e., Qwen2.5 family and Qwen 3 (7B)), the benefit brings by self-generated CoT over groundtruth CoT is significant. But with a stronger LLM (i.e., Qwen 3 (14B)) that can understand well on the groundtruth CoT, this benefits shrink, as illustrated in Figure 8).

5.3 The Smoothness of Information Flow

Effective learning requires not just comprehensible individual examples, but a coherent progression between them. We hypothesize that smooth transitions between demonstrations facilitate the model’s construction of a coherent reasoning schema, while abrupt conceptual jumps disrupt this process.

Quantifying Transition Smoothness To operationalize this principle, we conceptualize the sequence of demonstration embeddings as a trajectory through semantic space. We define the curvature between consecutive demonstrations as the angle between the vectors connecting them:

$$\theta_i = \arccos \left(\frac{(\mathbf{e}_i - \mathbf{e}_{i-1}) \cdot (\mathbf{e}_{i+1} - \mathbf{e}_i)}{\|\mathbf{e}_i - \mathbf{e}_{i-1}\| \|\mathbf{e}_{i+1} - \mathbf{e}_i\|} \right) \quad (1)$$

For an ordered sequence $O = [\mathbf{d}_1, \mathbf{d}_2, \dots, \mathbf{d}_n]$ and their corresponding embedding $E =$

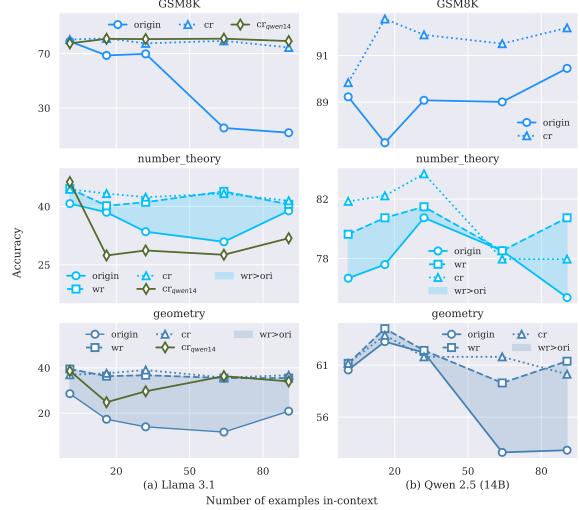


Figure 7: Performance of two sets of self-generated in-context CoT, including the set filtered with only correct answer(cr) and the set filtered with only wrong answer(wr). cr_{qwen14} is prompting the LLaMA model with the in-context CoT generated by Qwen 2.5 (14B). **Left:** Llama 3.1 **Right:** Qwen 2.5 (14B)

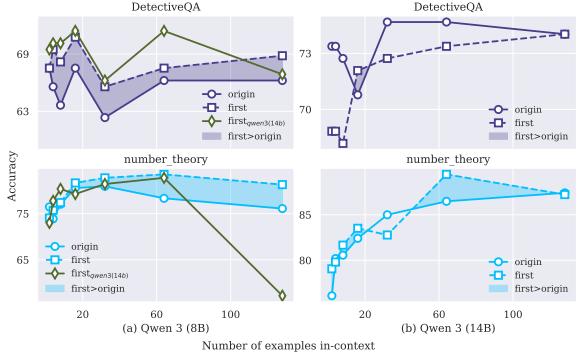


Figure 8: Performance of the first set of self-generated in-context CoT. cr_{qwen3(14b)} is prompting the Qwen 3 (8B) model with the in-context CoT generated by Qwen 3 (14B). **Left:** Qwen 3 (8B) **Right:** Qwen 3 (14B)

$\{\mathbf{e}_1, \mathbf{e}_2, \dots, \mathbf{e}_n\} \subset \mathbb{R}^d$, the total curvature $\Theta(E) = \sum_{i=2}^{n-1} \theta_i$, with lower values indicating smoother transitions between demonstrations. The detail algorithm is on Appendix A.

Dimensionality reduction for efficiency. To facilitate efficient computation of smoothness and to capture both global and local structures, as well as linear and non-linear patterns, we project the embeddings into a lower-dimensional space using PCA (Maćkiewicz and Ratajczak, 1993) and UMAP (McInnes et al., 2018). Correlation is computed with 128 number of demonstration and we set the number of component $d' = 50$.

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527 **Projection Method:** We compute a combined
projection $P(E) \in \mathbb{R}^{n \times d'}$ as:

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$$P(E) = \text{PCA}(E, d') + \text{UMAP}(E, d') \quad (2)$$

529 The PCA component $\text{PCA}(E, d')$ captures
530 global linear structure, while the UMAP com-
531 ponent $\text{UMAP}(E, d')$ preserves local nonlinear
532 relationships crucial for reasoning tasks. The PCA
533 projection is weighted by explained variance:

534
$$\text{PCA}(E, d') = E_{\text{pca}} \cdot \text{diag}(\sqrt{\lambda}) \quad (3)$$

535 where $\lambda = [\lambda_1, \dots, \lambda_{d'}]$ are the explained
536 variance ratios.

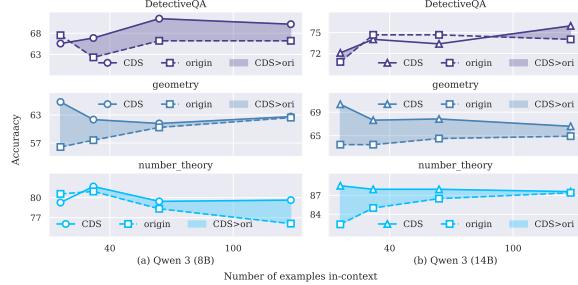
537 **Result.** Our analysis reveals a negative corre-
538 lation ($r=-0.602$) between ordering smoothness and
539 performance across three math reasoning tasks.
540 With the correlation of -0.654, -0.511 and -0.642
541 corresponding to geometry, number_theory and
542 counting_and_probability tasks, it supports that
543 smooth information flow facilitates effective in-
544 context learning. Additionally, the finding that
545 variance increases with more demonstrations in
546 reasoning tasks in Section 4.3 can be reinterpreted
547 as follow, With more demonstrations, the proba-
548 bility of encountering disruptive conceptual jumps
549 increases, leading to greater outcome variability.

550 **Pedagogical Analogy** This principle mirrors ef-
551 fective textbook design: concepts are introduced
552 progressively, with each chapter building smoothly
553 upon the previous. Abrupt topic changes or missing
554 prerequisites hinder learning. Similarly, in many-
555 shot CoT-ICL, demonstrations must be ordered to
556 create a "conceptual curriculum" that guides the
557 model from basic to advanced reasoning steps.

558 6 Curvilinear Demonstration Selection

559 Based on the strong correlation between curva-
560 ture and performance established in Section 5.3,
561 we now introduce Curvilinear Demonstration Se-
562 lection (CDS), a practical method for optimizing
563 demonstration ordering in many-shot CoT-ICL.
564 The core insight is that minimizing total curvature
565 along the demonstration sequence corresponds to
566 creating a smoother learning progression, analo-
567 gous to how textbooks organize chapters by gradu-
568 ally increasing conceptual difficulty.

569 **Method.** Finding the global minimizer of Θ can
570 computationally intractable for large n , but can
571 be effectively approximated by formulating it as a



572 Figure 9: Performance comparison between CDS or-
573 dered CoT-ICL and originally ordered CoT-ICL. **Left:**
574 Qwen 3 (8B) **Right:** Qwen 3 (14B)

572 Traveling Salesman Problem (TSP). We solve this
573 TSP using a nearest neighbor heuristic with 2-opt
574 optimization (Croes, 1958).

575 **Dimensionality reduction.** Since we cannot
576 adopt $d' = 50$ for all number of demonstrations, we
577 adopt the following strategy. For n demonstrations,
578 we set the number of components d' as:

$$579 d' = \left\lfloor \frac{n}{5} \right\rfloor \times 5 \quad (4)$$

580 This rounding to the nearest multiple of five en-
581 sures computational efficiency while maintaining
582 sufficient expressivity. For example, with $n = 128$,
583 we use $d' = 125$ components.

584 **Result.** We evaluate CDS on three challenging
585 reasoning tasks: geometry proof generation, num-
586 ber theory problem solving, and DetectiveQA log-
587 ical reasoning. Figure 9 shows the performance
588 comparison across different ordering strategies. Re-
589 sult shows that CDS outperform all baselines across
590 the evaluated tasks, with average improvements of
591 3.45%.

592 7 Conclusion

593 We have shown that many-shot chain-of-thought
594 in-context learning (CoT-ICL) does not follow the
595 same property as standard many-shot ICL. To ex-
596 plain this, we reframe the ICL from pattern match-
597 ing to in-context "learning", explained with two
598 principles. Based on these, we propose CDS,
599 a method that orders demonstrations to ensure
600 smooth conceptual transitions. Our work reframes
601 demonstration selection as a retrieval-for-learning
602 problem. By designing demonstrations that teach
603 rather than just match, we can build more robust
604 and capable reasoning systems.

605 Limitations

606 Due to the computational cost and performance
607 limitations of LLMs in long in-context CoT rea-
608 soning, our study is limited to approximately 100
609 examples. While LLMs like Qwen 2.5 and LLaMA
610 3.1 can handle up to 131K and 128K context to-
611 kens, respectively, their performance in in-context
612 CoT reasoning declines gradually beyond a cer-
613 tain threshold of context tokens, making exploring
614 beyond 100 shots in this setting insignificant. In
615 addition, the effectiveness of CDS depends on the
616 quality of the underlying embeddings. Though,
617 Qwen3-Embedding-4B shows a promising perfor-
618 mance on both narrative and math reasoning.

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A Algorithm for Curvature-Performance Correlation

To quantify the relationship between demonstration ordering smoothness and ICL performance, we develop Algorithm 1. The algorithm takes as input multiple orderings of demonstrations and their corresponding performance scores, and outputs a correlation coefficient between ordering smoothness and performance.

B Analysis of Similarity in Different LLM Types

Result in Figures 10 and 11 shows the performance comparison in different types of LLMs.

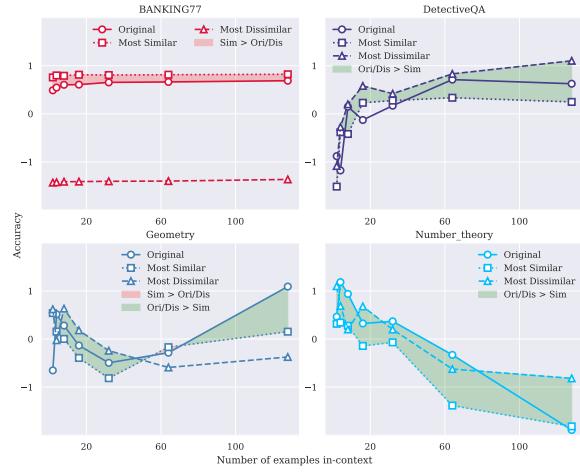


Figure 10: Performance with original (ori), similarity(sim) and dissimilar(dis) sets averaged across three non-reasoning LLMs. The area between the two sets is filled with colors, indicating the relative performance at each point.

C Prompt formatting and LLM performance for each task

C.1 SuperGlue

We evaluate the Winograd Schema Challenge (WSC) for coreference resolution, and the Choice of Plausible Alternatives (COPA) for open-domain commonsense causal reasoning. Both are formatted as a binary-label classification task. The prompt for inference is presented in Figure 12 and 13.

C.2 TREC

We evaluate the Text REtrieval Conference (TREC) Question Classification dataset with 50 fine class labels. The prompt for inference is presented in Figure 14.

Algorithm 1: Curvature-Performance Correlation Analysis

Input: For k different orderings:

- $E^{(1)}, E^{(2)}, \dots, E^{(k)}$: embedding matrices where $E^{(j)} = [e_1^{(j)}, e_2^{(j)}, \dots, e_N^{(j)}]^\top$ represents the j -th ordering of N demonstration embeddings

- $S = [S_1, S_2, \dots, S_k]$: performance scores for each ordering

Output: Correlation coefficient r between smoothness scores and performance scores

Initialize smoothness scores array

$$\mathbf{m} \leftarrow [0, 0, \dots, 0] \text{ of length } k$$

for each dimensionality reduction method

$$M \in \{PCA, UMAP\} \text{ do}$$

for $j = 1$ to k **do**

Step 1: Dimensionality reduction
 $\tilde{E}^{(j)} \leftarrow \text{ReduceDim}(E^{(j)}, M)$

Step 2: Compute curvature between consecutive demonstrations

$$\text{curvatures} \leftarrow []$$

for $i = 2$ to $N - 1$ **do**

$$\mathbf{v}_1 \leftarrow \tilde{\mathbf{e}}_i^{(j)} - \tilde{\mathbf{e}}_{i-1}^{(j)}$$

$$\mathbf{v}_2 \leftarrow \tilde{\mathbf{e}}_{i+1}^{(j)} - \tilde{\mathbf{e}}_i^{(j)}$$

if $\|\mathbf{v}_1\| > 0$ and $\|\mathbf{v}_2\| > 0$ **then**

$$\cos \theta_i \leftarrow \frac{\mathbf{v}_1 \cdot \mathbf{v}_2}{\|\mathbf{v}_1\| \|\mathbf{v}_2\|}$$

$$\theta_i \leftarrow \arccos(\cos \theta_i)$$

Append θ_i to curvatures

Step 3: Compute smoothness score

$$\bar{\theta}^{(j)} \leftarrow \text{mean}(\text{curvatures})$$

$$\text{score}_M^{(j)} \leftarrow \frac{1}{1 + \bar{\theta}^{(j)}}$$

Step 4: Weighted combination (equal weighting for PCA and UMAP)

$$\mathbf{m}[j] \leftarrow \mathbf{m}[j] + 0.5 \times \text{score}_M^{(j)}$$

Step 5: Compute correlation

$$r \leftarrow \text{PearsonCorrelation}(\mathbf{m}, S)$$

return r

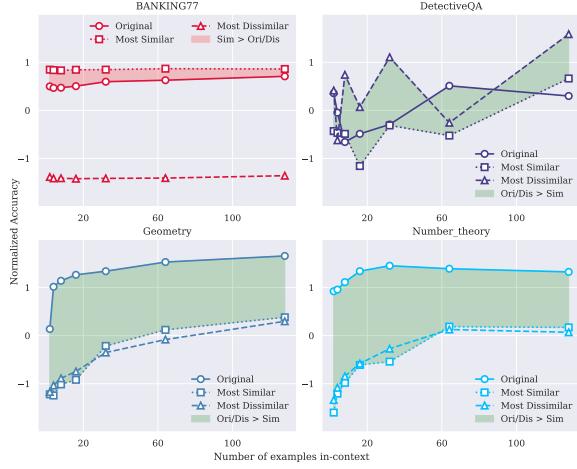


Figure 11: Performance with original (ori), similarity(sim) and dissimilar(dis) sets averaged across two reasoning LLMs. The area between the two sets is filled with colors, indicating the relative performance at each point.

C.3 BANKING77

We evaluate the BANKING77 dataset with 77 fine-grained intents in the banking domain. The prompt for inference is presented in Figure 15.

C.4 NLU

We evaluate the NLU dataset with 68 fine-grained intents in the conversational domain. The prompt for inference is presented in Figure 16.

C.5 GSM8K

We evaluate the GSM8K dataset for grade school math word problems. The prompt for inference is presented in Figure 17.

C.6 MATH

We evaluate the Mathematics Aptitude Test of Heuristics (MATH) dataset for mathematics competition problems, including the question types of counting_and_probability, prealgebra, geometry, precalculus, number_theory and algebra. The prompt for inference is presented in Figure 18.

Given a query, answer yes or no to the query.

The predicted answer must come from the demonstration examples with the exact format. The examples are as follows:

Question: In the sentence “{text₁ }”, does the pronoun ‘{span2_text₁}’ refer to {span1_text₁}?
Answer: {answer₁}

...

Question: In the sentence “{text_n }”, does the pronoun ‘{span2_text_n}’ refer to {span1_text_n}?
Answer: {answer_n}

Now predict the answer for the following query:

Question: In the sentence “{text_i }”, does the pronoun ‘{span2_text_i}’ refer to {span1_text_i}?

reply in the following format:
‘Answer: [yes | no]’

Figure 12: Prompt for WSC task

Answer in A or B.

The predicted answer must come from the demonstration examples with the exact format. The examples are as follows:

Premise: {premise₁}
Question: What is the {question₁} for this?
Options:
A. {choice1₁}
B. {choice2₁}
Answer: {answer₁}

...

Premise: {premise_n}
Question: What is the {question_n} for this?
Options:
A. {choice1_n}
B. {choice2_n}
Answer: {answer_n}

Now predict the answer for the following query:

Premise: {premise_i}
Question: What is the {question_i} for this?
Options:
A. {choice1_i}
B. {choice2_i}

reply in the following format:
‘Answer: [A | B]’

Figure 13: Prompt for COPA task

Given a question, predict the label of the question. You can only make predictions from the following categories:
{LIST_OF_CATEGORIES}
Please predict the label of the FINAL question with the provided demonstration example queries as follows:

question: {question₁}
label: {label₁}
...
question: {question_n}
label: {label_n}

Now predict the answer for the following query:

question: {question_i}

reply in the following format:
'label: [category_name]'

Figure 14: Prompt for TREC task

Given a question, predict the label of the question. You can only make predictions from the following categories:
{LIST_OF_CATEGORIES}
Please predict the intent category of the FINAL query with the provided demonstration example queries as follows:

service query: {question₁}
intent category: {label₁}
...
service query: {question_n}
intent category: {label_n}

Now predict the intent category for the following query:

service query: {question_i}

reply in the following format:
'intent category: [category_name]'

Figure 15: Prompt for BANKING77 task

Given a question, predict the label of the question. You can only make predictions from the following categories:
{LIST_OF_CATEGORIES}
Please predict the intent category of the FINAL utterance with the provided demonstration example queries as follows:

utterance: {question₁}
intent category: {label₁}
...
utterance: {question_n}
intent category: {label_n}

Now predict the intent category for the following utterance:

utterance: {question_i}

reply in the following format:
'intent category: [category_name]'

Figure 16: Prompt for NLU task

In the end of the response, add a summary ‘The answer is [answer].’

Q: {question₁}
A: {CoT₁} {answer₁}

...

Q: {question_n}
A: {CoT_n} {answer_n}

Q: {question_t}
A: Let’s think step by step.

Figure 17: Prompt for GSM8K task

Write a response that appropriately completes the request and wrap the final answer inside \boxed{ }.

Problem: {question₁}
Solution: {CoT_with_answer₁}

...

Problem: {question_n}
Solution: {CoT_with_answer_n}

Problem: {question_t}
Solution: Let’s think step by step.

Figure 18: Unified prompt for MATH task