

Lab 3

Analysis of d -ary heaps

A **d -ary heap** is like a binary heap, but (with one possible exception) non-leaf nodes have d children instead of 2 children.

- (1) How would you represent a d -ary heap in an array? (10%)
- (2) What is the height of a d -ary heap of n elements in terms of n and d ? (10%);
- (3) Given an efficient implementation of EXTRACT-MAX in a d -ary max-heap. Analyze its running time in terms of d and n . (20%);
- (4) Given an efficient implementation of INSERT in a d -ary max-heap. Analyze its running time in terms of d and n . (20%);
- (5) Give an efficient implementation of INCREASE-KEY(A, i, k), which first sets $A[i] \leftarrow \max(A[i], k)$ and then updates the d -ary max-heap structure appropriately. Analyze its running time in terms of d and n . (20%);
- (6) Document. (20%)