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Example 9 Consider the system and the fault point as given in Example 7 solved previously, [see Z_0, Z_1, Z_2 , and $V(0)$ from Example 7].

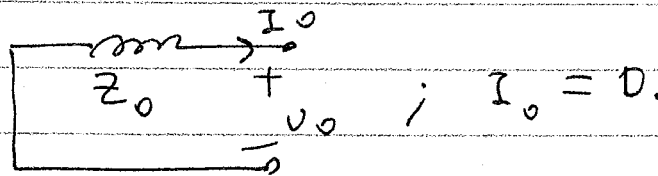
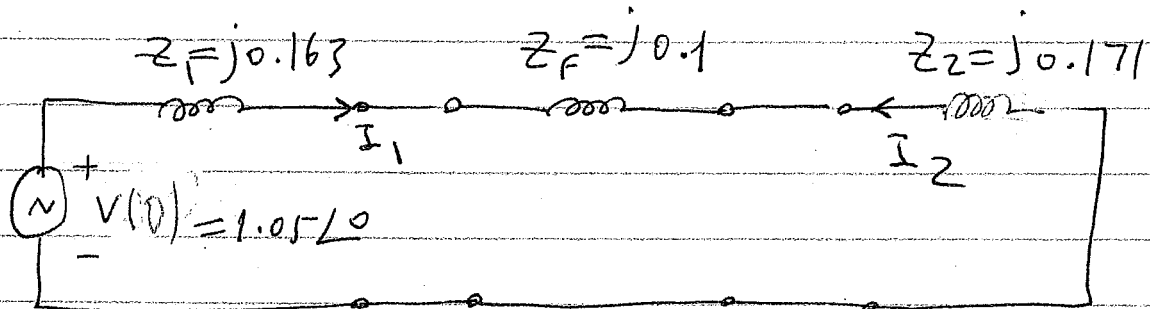
a) Consider a line-to-line fault with $Z_F = j0.1$ at the middle of the line.

Find the ^{Phase} voltages at the fault point during fault and the Phase current through the generator G and the motor M due to the fault

b) The same as Part (a) except, assume a line-to-line-to ground fault with $Z_F = j0.1$

Solution / Example 9

a) For Line-to-Line fault, we have the following sequence network connection:



$$I_1 = -I_2 = \frac{V(0)}{Z_1 + Z_f + Z_2} = \dots = -j2.423$$

$$V_2 = -Z_2 I_2 = \dots = +0.414$$

$$V_1 = (Z_f + Z_2) I_1 = \dots = 0.656$$

$$I_0 = 0 ; V_0 = 0$$

Now,

$$\begin{bmatrix} V_a \\ V_b \\ V_c \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & a^2 & a \\ 1 & a & a^2 \end{bmatrix} \begin{bmatrix} V_0 \\ V_1 \\ V_2 \end{bmatrix} = \dots$$

- Find $I_{abc, G}$ & $I_{abc, M}$. First we need to find the related seq values.

>> See Fig (3) of the previous example:

$$\begin{aligned} \Delta I_{0G} &= 0 \\ \Delta I_{0M} &= 0 \end{aligned} \quad \text{as seen from this Fig.}$$

>> See Fig (4).

$$\Delta I_{IG} = \frac{\left(\frac{X_{1L}}{2} + X_{T2} + X_{1M}\right) I_1}{\left(\frac{X_{1L}}{2} + X_{T1} + X_{1G}\right) + \left(\frac{X_{1L}}{2} + X_{T2} + X_{1M}\right)}$$

$$\Delta I_{1M} = I_1 - \Delta I_{IG} \quad ; \quad \text{we are using } \Delta\text{-values, thus sources are ignored.}$$

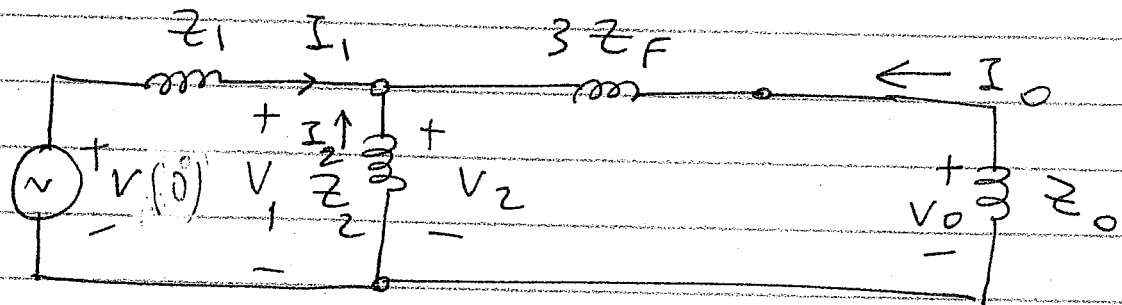
>> See Fig (5).

$$\begin{aligned} \rightarrow \Delta I_{2G} &= \frac{\left(\frac{X_{2L}}{2} + X_{T2} + X_{2M}\right) I_2}{\left(\frac{X_{2L}}{2} + X_{T2} + X_{2M}\right) + \left(\frac{X_{2L}}{2} + X_{T1} + X_{2G}\right)} \\ \rightarrow \Delta I_{2M} &= I_2 - \Delta I_{2G} \end{aligned}$$

Now, use transformation to find to find the phase values of these currents.

Note : Since pre-fault currents are zero due to flat voltage profile, the Δ -^{values of the} currents are the currents during fault.

b) For double line to ground fault we have:



$$V_F = 1.05 \angle 0^\circ; \quad Z_1 = j0.163, \quad Z_2 = j0.171$$

$$Z_0 = j0.129; \quad 3Z_F = j0.3$$

Now,

$$I_1 = \frac{V(0)}{Z_1 + Z_2 \parallel (Z_0 + 3Z_F)} = \dots$$

$$I_2 = \frac{(3Z_F + Z_0)(-I_1)}{(3Z_F + Z_0) + Z_2} = \dots$$

$$I_0 = -I_1 - I_2$$

$$V_0 = -Z_0 I_0$$

$$V_2 = -Z_2 I_2; \quad V_1 = V_2$$

Now,

$$\begin{bmatrix} V_a \\ V_b \\ V_c \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & a^2 & a \\ 1 & a & a^2 \end{bmatrix} \begin{bmatrix} V_0 \\ V_1 \\ V_2 \end{bmatrix}$$

For the rest of part (b) follow the procedure used in part (a).