

**Applications &  
Problem Settings**

**Scalability  
State of the Art**

**Accelerate the  
Multitude of Queries**

## Unleashing the Potential of Configuration Counting for Product Lines

PhD Defense | Chico Sundermann | 12.08.2025

# Introduction Product Lines



# Introduction Product Lines



## PC BUILDER

GET COMPATIBLE RECOMMENDATIONS

PICK YOUR IDEAL CORSAIR COMPONENTS

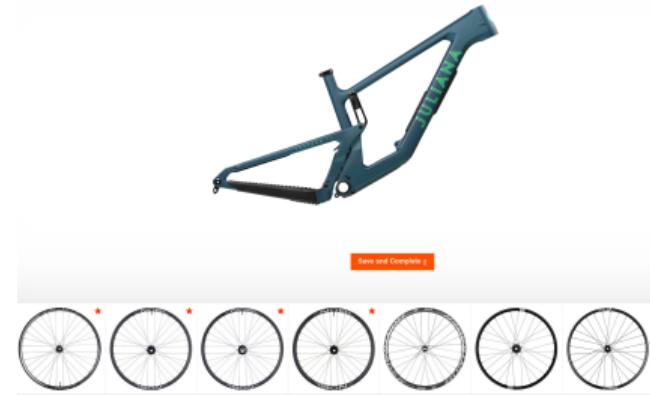


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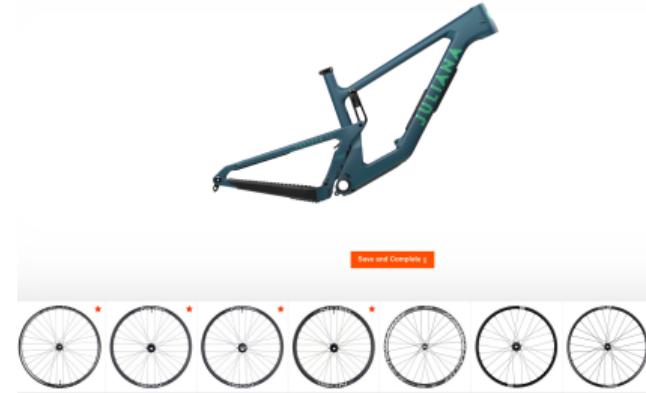


# Introduction Product Lines



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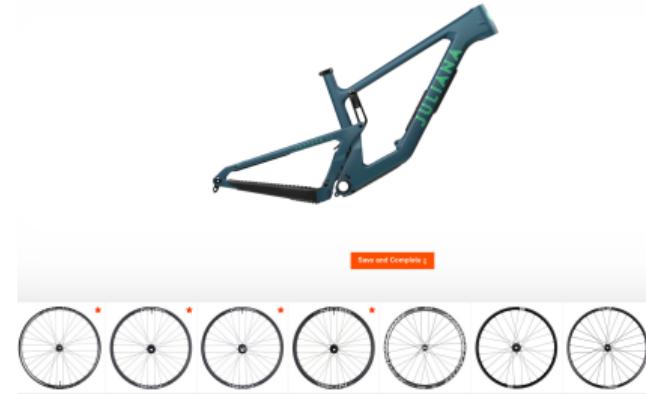
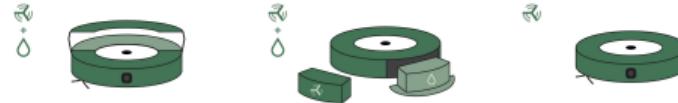


# Introduction Product Lines



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# Introduction Feature Dependencies



**Compatibility:** Warning! These parts have potential issues or incompatibilities. See [details](#) below.

# Introduction Feature Dependencies

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# Introduction Feature Dependencies

**Confirm your choice**

To add the accessory you need to confirm your choice

 +

Handlebar rear-view mirror.

Accessories to be added to the configuration:

 Pair of adapters for rear-view mirror...  
96881201AA  
 Anodized

Accessories to be removed from the configuration:

 Set for removing rear-view mirrors.  
97381241AA  
 Anodized

 **Compatibility:** Warning! These parts have potential issues or incompatibilities. See [details](#) below.

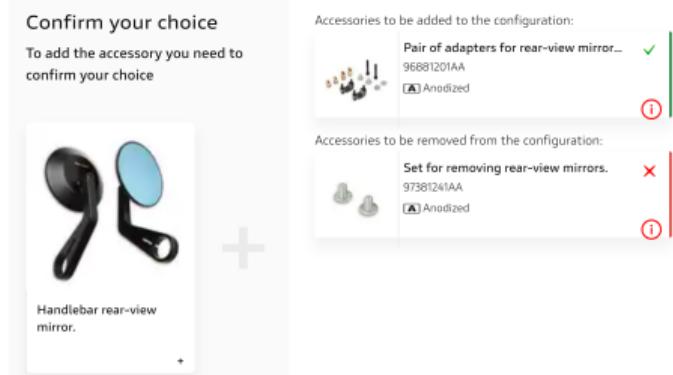
```
config SECURITY_INFINIBAND
    bool "Infiniband Security Hooks"
depends on SECURITY && INFINIBAND
```



# Introduction Feature Dependencies

Confirm your choice

To add the accessory you need to confirm your choice



The interface shows a handlebar rear-view mirror being added to a configuration. It includes a product image, a plus sign icon, and a confirmation message: "Handlebar rear-view mirror." Below the main area is a brown banner with a warning: "⚠ Compatibility Warning! CPU doesn't comes with stock cooler."

Accessories to be added to the configuration:

- Pair of adapters for rear-view mirror... ✓  
96881201AA  
Anodized

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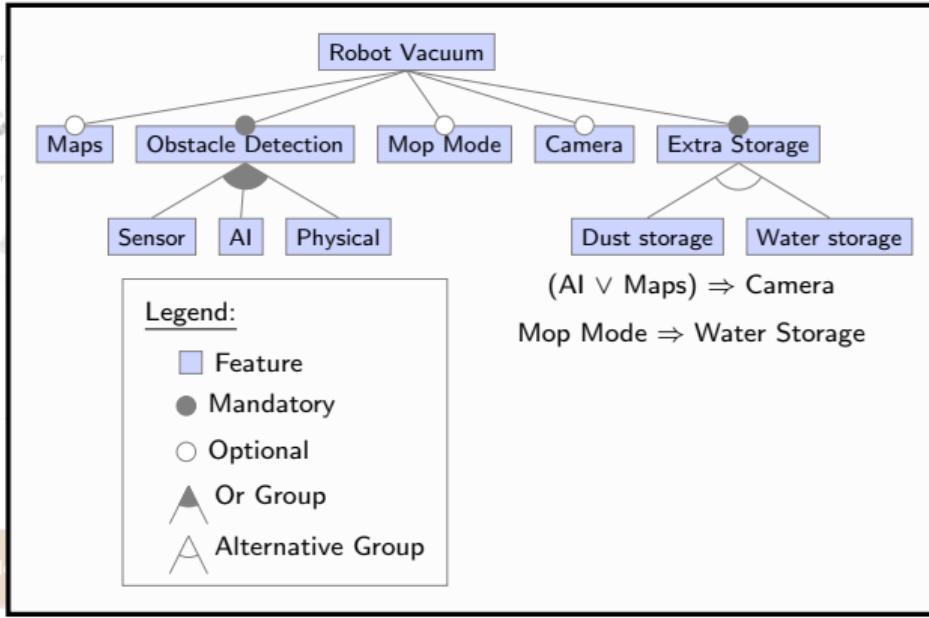


Handlebar rear-view mirror.

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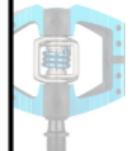
Accessories

Accessories

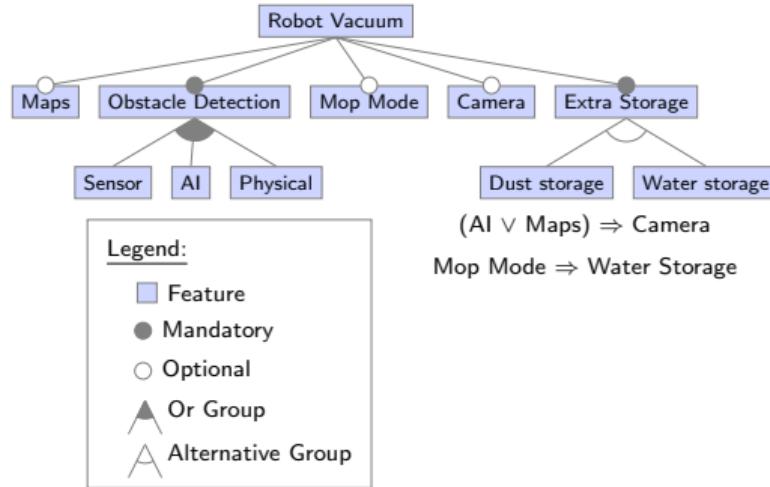


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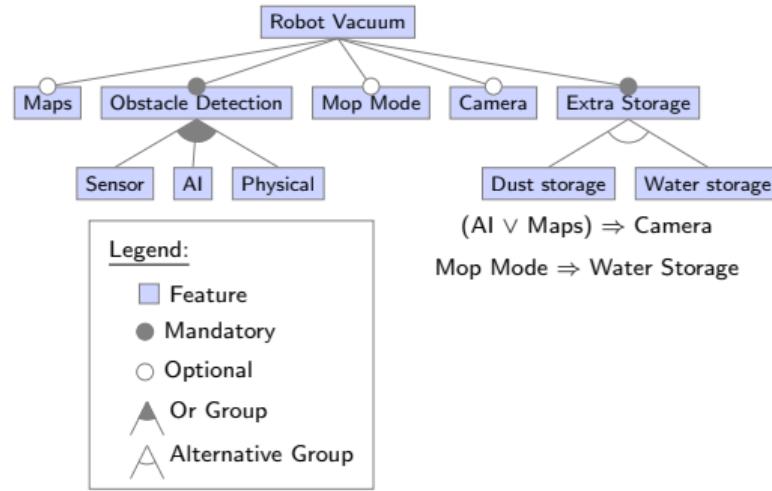
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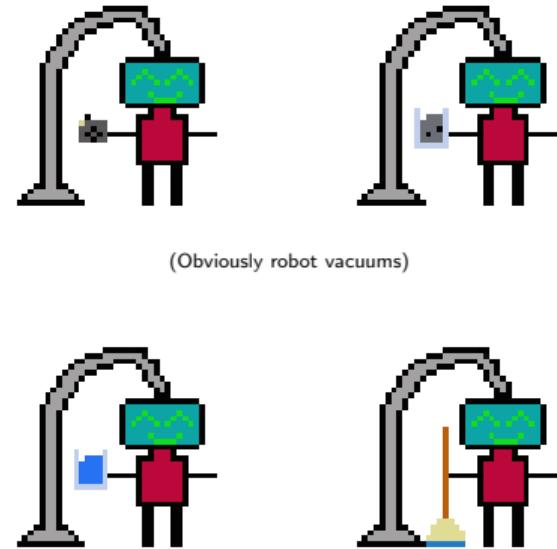
# Introduction Configuration Counting



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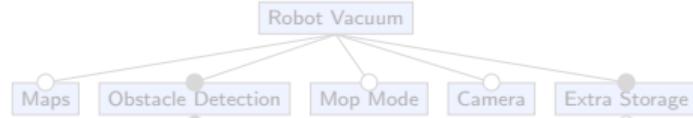


How many valid configurations?



# Introduction Configuration Counting

How many valid configurations?

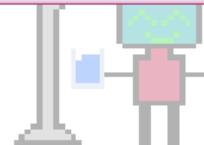


Thesis Main Objective

*How to improve the applicability of configuration counting?*

△ Or Group

▲ Alternative Group





## Applications & Problem Settings

*What applications are facilitated by which counting operations?*



## Scalability State of the Art

*How well does the state of the art scale for configuration counting?*



## Accelerate the Multitude of Queries

*How can we scale to the numerous different computations required for configuration counting?*



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# Applications Related Work

Related Work

Limitations

Contributions



Applications & Problem Settings



# Applications Related Work

## Related Work

- Occasional occurrences in related work
- Small collections (with specific scope)

## Limitations

## Contributions

### Inferring Information from Feature Diagrams to Product Line Economic Models

David Fernandez-Amoros\*, Ruben Heradio Gil† and Jose Cerrada Somolinos†  
*ETS de Ingenieria Informatica, Universidad Nacional de Educacion a Distancia, Madrid, Spain*  
\*david@isi.uned.es  
†(rheradio|jcerrada)@issi.uned.es

### A Literature Review on Feature Diagram Product Counting and Its Usage in Software Product Line Economic Models

Ruben Heradio\*†, David Fernandez-Amoros†‡, Jose Antonio Cerrada-Somolinos†‡, and Ismael Abad§†

### Automated Analysis of Feature Models 20 Years Later: A Literature Review<sup>△</sup>

David Benavides, Sergio Segura and Antonio Ruiz-Cortés  
*Dpto. de Lenguajes y Sistemas Informáticos, University of Seville  
Av. Reina Mercedes s/n, 41012, Seville - Spain*

### Model Counting in Product Configuration

Andreas J. Kübler      Christoph Zengler  
Wolfgang Küchlin



# Applications Related Work

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## Limitations

- Scattered
- Applications from practice missing
- Unclear how to compute

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†(rheradio|jcerrada)@issi.uned.es

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## Contributions

1. Collection (**VaMoS'21**)
2. Industry applications (**VaMoS'21**)
3. Computation (**VaMoS'21, AMAI'24**)

## Applications of #SAT Solvers on Feature Models

Chico Sundermann  
University of Ulm, Germany

Michael Nieke  
TU Braunschweig, Germany

Paul Maximilian Bittner  
University of Ulm, Germany

Tobias Heß  
University of Ulm, Germany

Thomas Thüm  
University of Ulm, Germany

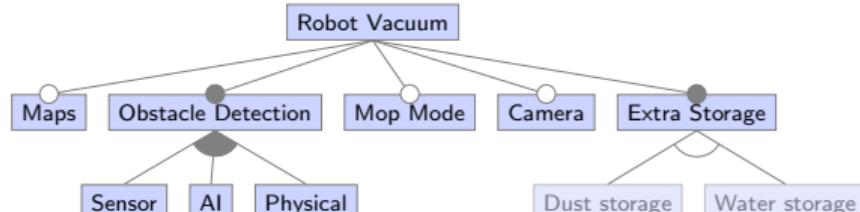
Ina Schaefer  
TU Braunschweig, Germany

VaMoS'21

AMAI'24

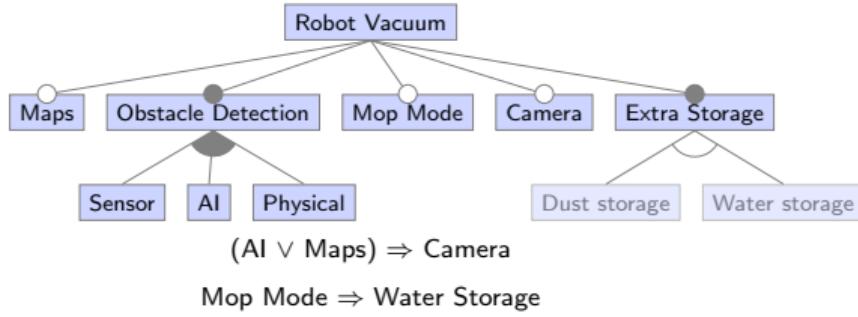
## On the benefits of knowledge compilation for feature-model analyses

Chico Sundermann<sup>1</sup> · Elias Kuitert<sup>2</sup> · Tobias Heß<sup>1</sup> · Heiko Raab<sup>1</sup> ·  
Sebastian Krieter<sup>1</sup> · Thomas Thüm<sup>1</sup>

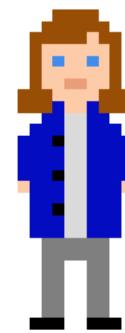


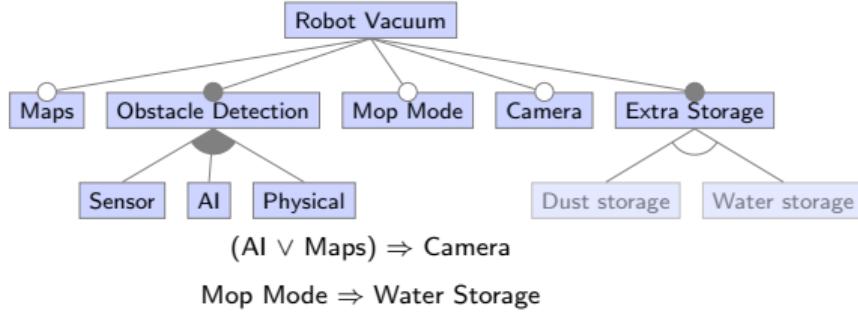
$(AI \vee Maps) \Rightarrow Camera$

$Mop\ Mode \Rightarrow Water\ Storage$



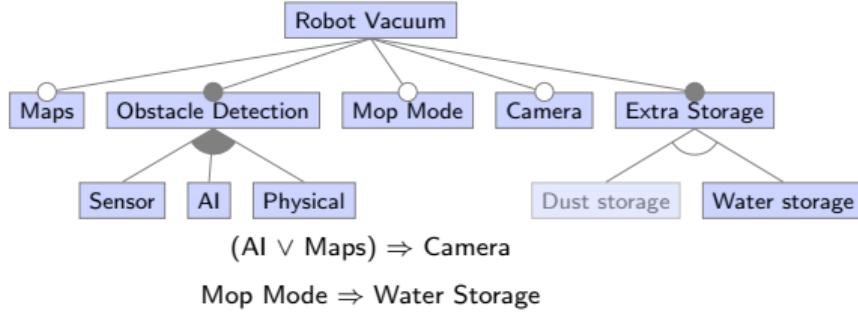
Extra dust or water?



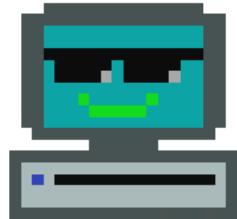


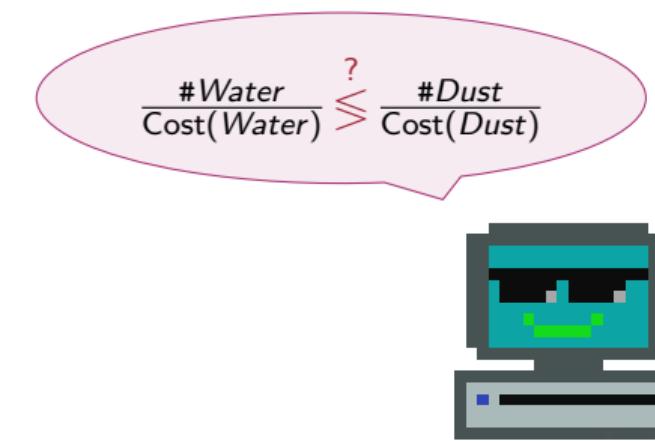
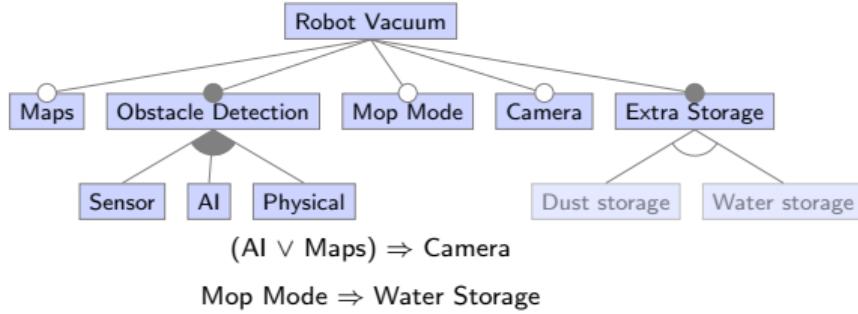
#Dust < #Water  
More robots with water!





#Dust < #Water  
More robots with water!







# Configuration Counting    Why Care?

Feature Prioritization

# Configuration Counting Why Care?

Variability Factor	Degree of Reuse	Uniform Random Sampling	Rating Errors
Degree of Orthogonality	Homogeneity	Atomic Sets <span style="background-color: yellow;">NEW</span>	Subset Variability <span style="background-color: yellow;">NEW</span>
Cost Savings	Feature Anomalies	Rate Interactions <span style="background-color: yellow;">NEW</span>	
Void Feature Model	Feature Payoff	Selection Impact <span style="background-color: yellow;">NEW</span>	
Maintainability Prediction	Optimize Configuring		
Variability Reduction <span style="background-color: yellow;">NEW</span>	Atomic Set Candidates <span style="background-color: yellow;">NEW</span>		
Configuration Relevance <span style="background-color: yellow;">NEW</span>	Feature Prioritization <span style="background-color: yellow;">NEW</span>		
	CTC Restrictiveness <span style="background-color: yellow;">NEW</span>		

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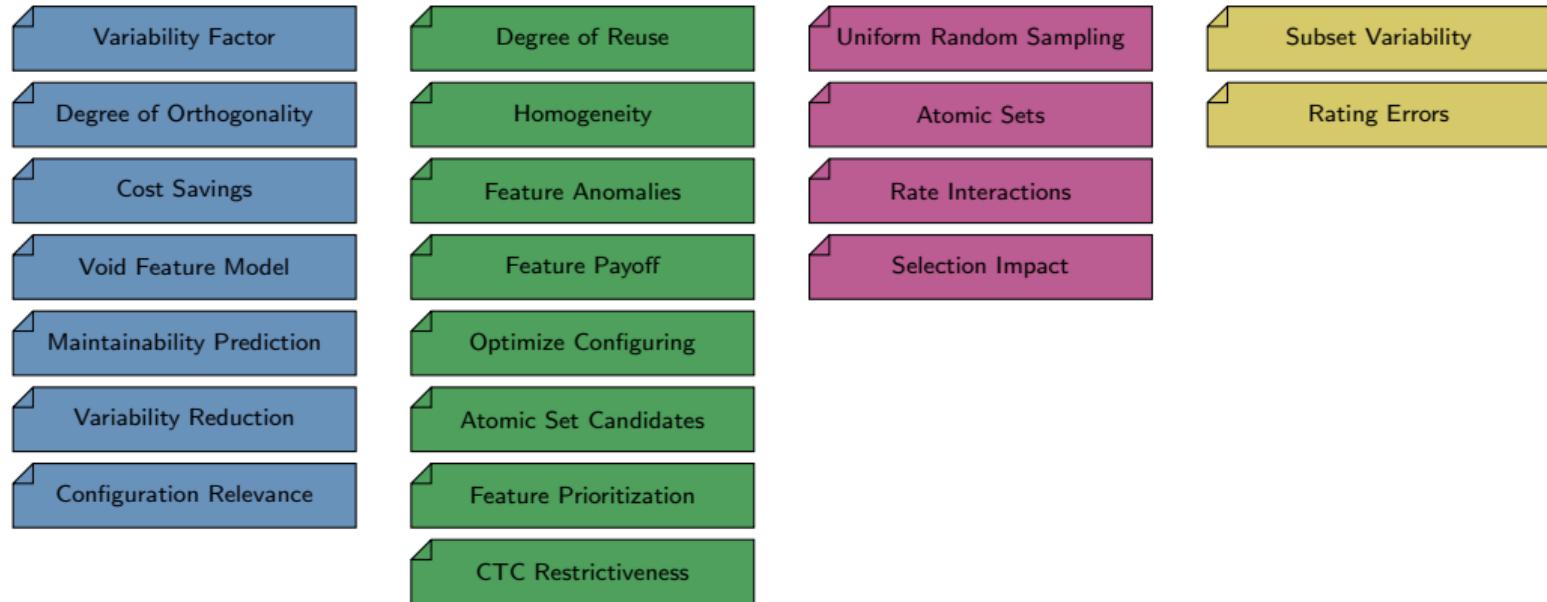
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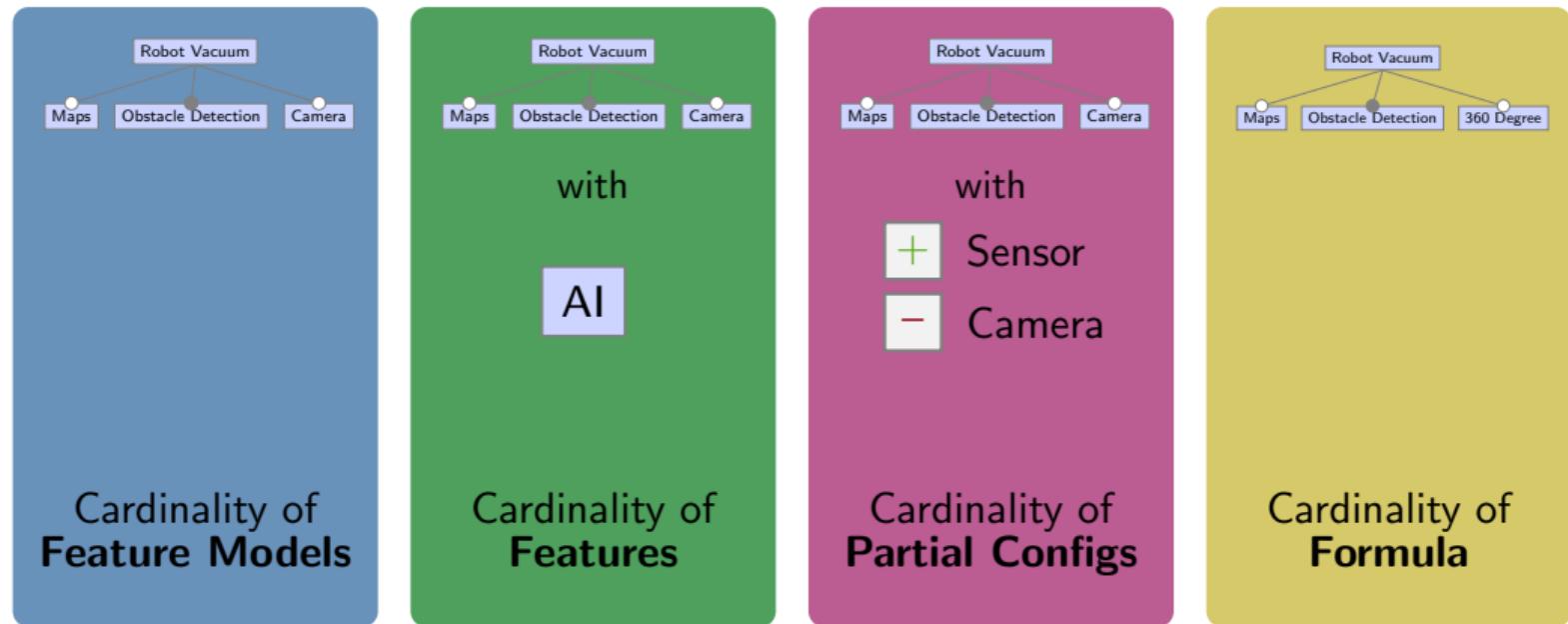
Key Result

Plenty applications rely on counting.

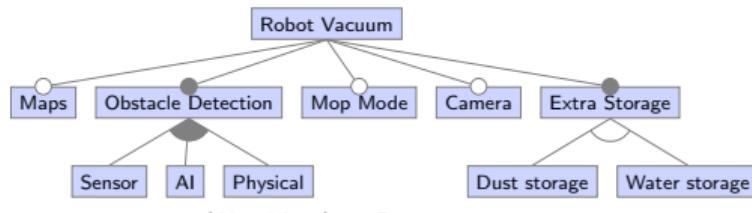
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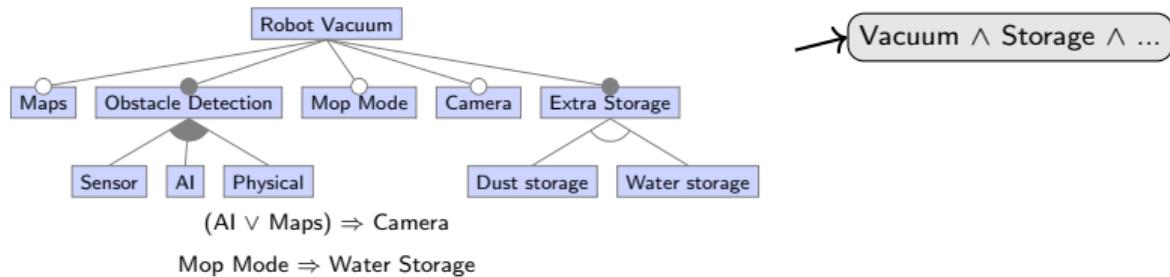
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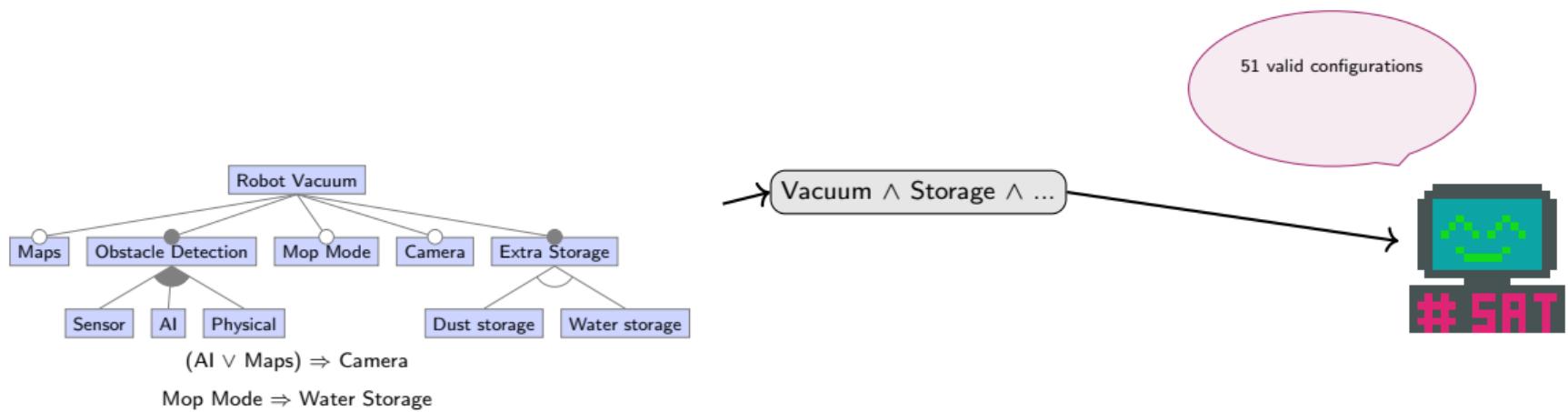
# How to?



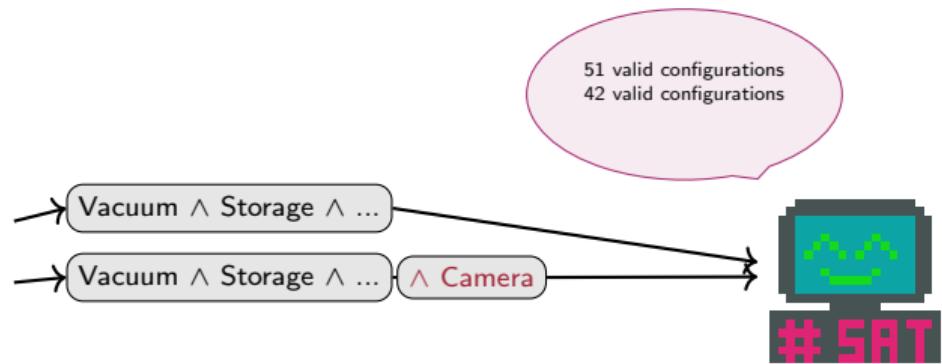
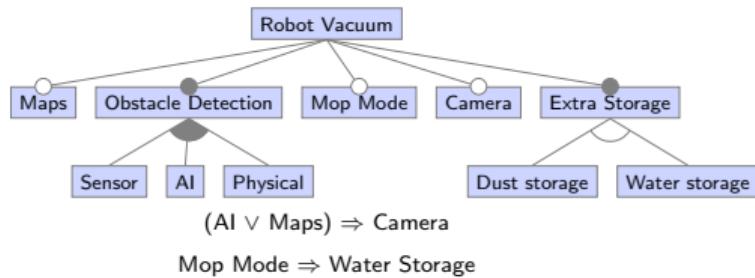
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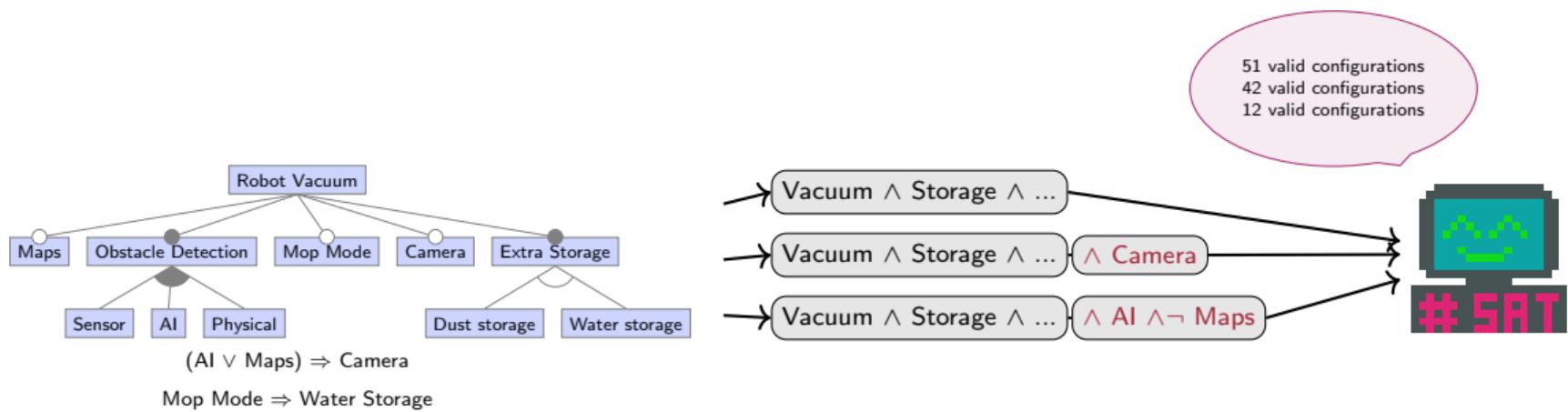
# How to? Reduce to #SAT



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# How to? Reduce to #SAT



# Applications Complexity of Applications

Type	Analysis	Number of Queries	Repeatability
Cardinality of Feature Models	Variability Factor [Benavides et al.(2005)]	1	Static
	Variability Reduction [Sundermann et al.(2021)]	1	Static
	Degree of Orthogonality [Czarnecki and Kim(2005)]	1	Static
	Maintainability Prediction [Bagheri et al.(2012)]	1	Static
	Configuration Relevance [Sundermann et al.(2021)]	1	Static
	Cost Savings of Product Line [Clements et al.(2005)]	1	Static
Cardinality of Features	Homogeneity [Fernández-Amorós et al.(2014)]	$O( F )$	Static
	Atomic Set Candidates [Sundermann et al.(2021)]	$O( F )$	Static
	Feature Prioritization [Sundermann et al.(2021)]	$O( F )$	Static
	CTC Restrictiveness [Sundermann et al.(2021)]	$O( F )$	Static
	Degree of Reuse [Cohen(2003)]	$O( F )$	Static
	Optimize Configuring [Chen and Erwig(2011), Mazo et al.(2014)]	$O( F )$	Static
	Payoff Threshold [Heradio et al.(2013)]	$O( F )$	Static
Cardinality of Partial Configuration	Interactive Configuration [Sundermann et al.(2021)]	$O( F ^2)$	Dynamic
	Uniform Random Sampling [Oh et al.(2019)]	$O( F )$	Dynamic
	Rating Feature Interactions [Sundermann et al.(2021)]	$O( F ^2)$	Dynamic
Cardinality of Formula	Rating Errors [Kübler et al.(2010)]	1	Dynamic
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**Key Result**

Multitude of complex operations required



## Applications & Problem Settings

*What applications are facilitated by which counting operations?*



## Scalability State of the Art

*How well does the state of the art scale for configuration counting?*



## Accelerate the Multitude of Queries

*How can we scale to the numerous different computations required for configuration counting?*



## Applications & Problem Settings

### Key Contributions

Collect applications  
Add industrial applications  
Computation instructions

VaMoS'21

AMAI'24

### Key Results

Plenty applications  
Multitude of queries



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# State of the Art    Related Work

Related Work



Limitations

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Scalability State of the Art



# State of the Art    Related Work

## Related Work

- Evaluations of several strategies
- Small-scale evaluations on #SAT solving

## Limitations

## Contributions

### SAT-based Analysis of Large Real-world Feature Models is Easy

Jia Hui Liang  
University of Waterloo,  
Canada

Vijay Ganesh  
University of Waterloo,  
Canada

Krzysztof Czarnecki  
University of Waterloo,  
Canada

Venkatesh Raman  
Institute of Mathematical  
Sciences, India

### Model Counting in Product Configuration

Andreas J. Kübler    Christoph Zengler  
Wolfgang Küchlin

### A Performance Comparison of Contemporary Algorithmic Approaches for Automated Analysis Operations on Feature Models

Richard Pohl, Kim Lauenroth, and Klaus Pohl  
Paluno – The Ruhr Institute for Software Technology  
University of Duisburg-Essen  
45127 Essen, Germany  
[{richard.pohl | kim.lauenroth | klaus.pohl}@paluno.uni-due.de](mailto:{richard.pohl | kim.lauenroth | klaus.pohl}@paluno.uni-due.de)

### A Scalable Approach to Exact Model and Commonality Counting for Extended Feature Models

David Fernandez-Amoros, Ruben Heradio, Jose A. Cerrada, and Carlos Cerrada



# State of the Art    Related Work

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- Restricted systems

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[{richard.pohl | kim.lauenroth | klaus.pohl}@paluno.uni-due.de](mailto:{richard.pohl | kim.lauenroth | klaus.pohl}@paluno.uni-due.de)

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## Contributions

1. Gathering solvers (**VaMoS'20, EMSE'23**)
2. Evaluate on industrial feature models (**VaMoS'20, EMSE'23**)
3. Evaluate on evolution (**VaMoS'20**)
4. Gather industrial feature models (**SPLC'24**)

### Evaluating #SAT Solvers on Industrial Feature Models

Chico Sundermann  
Technische Universität Braunschweig

Thomas Thüm  
University of Ulm

Ina Schaefer  
Technische Universität Braunschweig

Empirical Software Engineering (2023) 28:29  
<https://doi.org/10.1007/s10664-022-10265-9>

### Evaluating state-of-the-art #SAT solvers on industrial configuration spaces

Chico Sundermann<sup>1</sup> · Tobias Heß<sup>1</sup> · Michael Nieke<sup>2</sup> · Paul Maximilian Bittner<sup>1</sup> · Jeffrey M. Young<sup>3</sup> · Thomas Thüm<sup>1</sup> · Ina Schaefer<sup>2</sup>



### Collecting Feature Models from the Literature: A Comprehensive Dataset for Benchmarking

Chico Sundermann  
University of Ulm  
Germany

Sebastian Krieter  
Paderborn University  
Germany

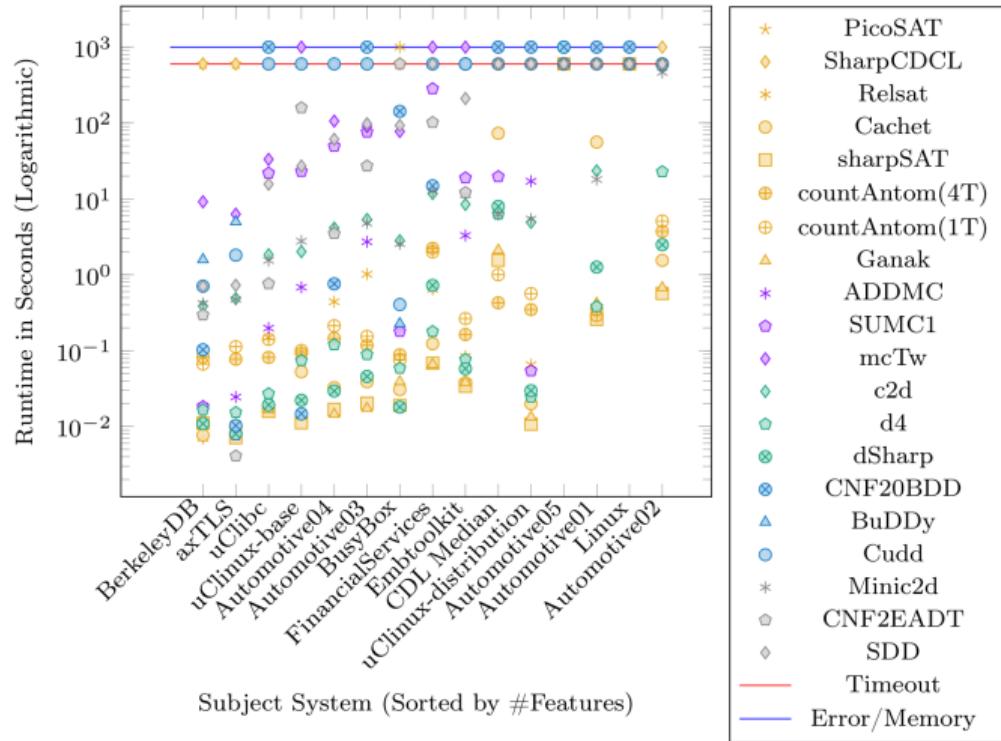
Vincenzo Francesco Brancaccio  
University of Ulm  
Germany

Tobias Heß  
University of Ulm  
Germany

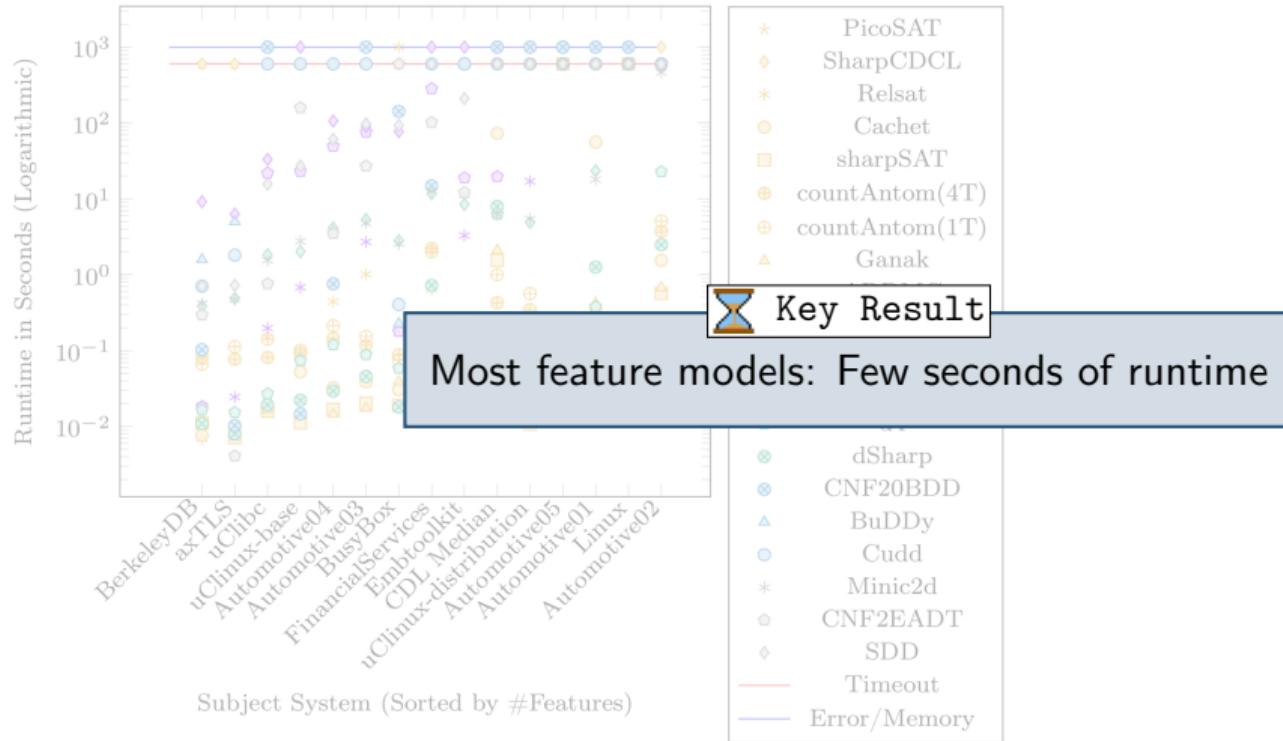
Elias Kuiter  
University of Magdeburg  
Germany

Thomas Thüm  
Paderborn University  
Germany

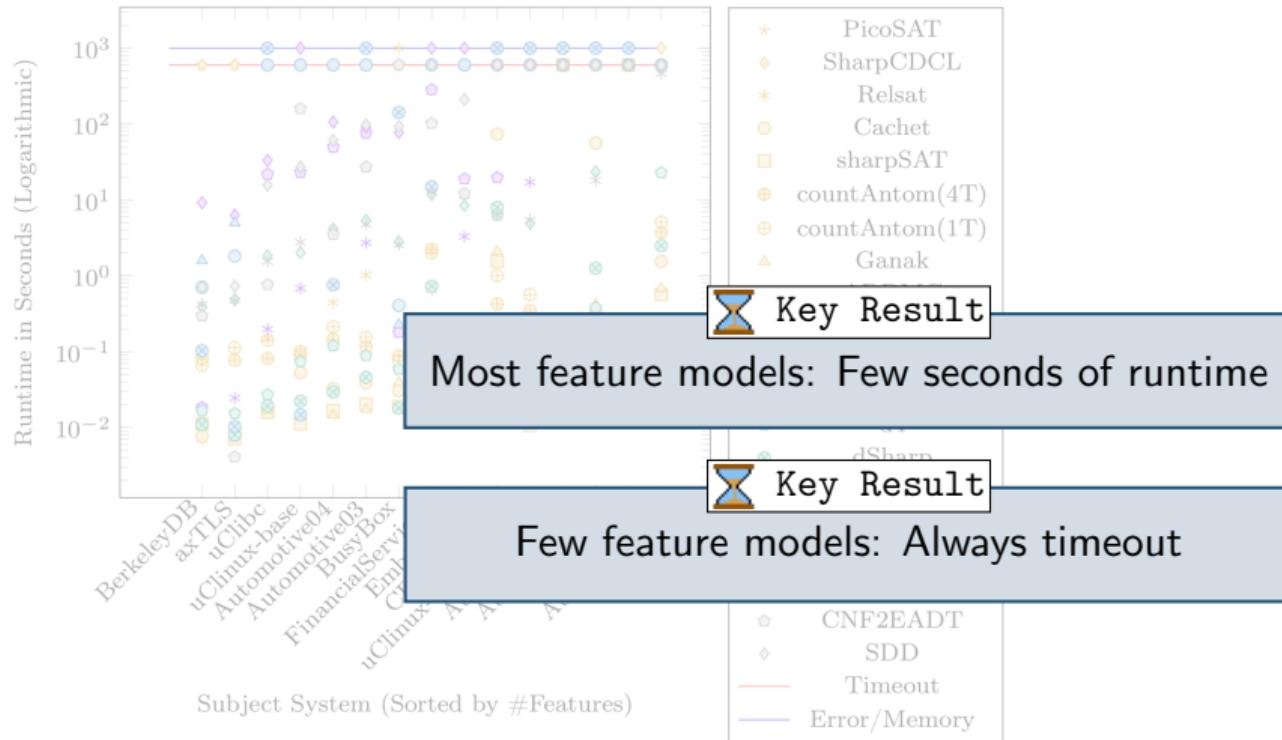
# State of the Art Runtimes #SAT on Feature Models



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## Applications & Problem Settings



### Key Contributions

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## Scalability State of the Art

### Key Contributions

Gather #SAT solvers  
Gather industrial models  
Performance study

VaMoS'20

EMSE'23

SPLC'24

### Key Results

Most systems in few seconds  
Few systems do not scale at all



## Accelerate the Multitude of Queries

*How can we scale to the numerous different computations required for configuration counting?*

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Gather industrial models  
Performance study

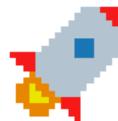
VaMoS'20

EMSE'23

SPLC'24

### Key Results

Most systems in few seconds  
Few systems do not scale at all



## Accelerate the Multitude of Queries

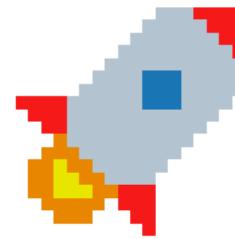
*How can we scale to the numerous different computations required for configuration counting?*

# Acceleration Related Work

Related Work

Limitations

Contributions



**Accelerate the Multitude of Queries**



# Acceleration Related Work

## Related Work

- State of the art: Black-box #SAT solving

## Limitations

## Contributions

### SAT-based Analysis of Large Real-world Feature Models is Easy

Jia Hui Liang  
University of Waterloo,  
Canada

Krzysztof Czarnecki  
University of Waterloo,  
Canada

Vijay Ganesh  
University of Waterloo,  
Canada

Venkatesh Raman  
Institute of Mathematical  
Sciences, India

### Model Counting in Product Configuration

Andreas J. Kübler      Christoph Zengler  
Wolfgang Küchlin

### A Literature Review on Feature Diagram Product Counting and Its Usage in Software Product Line Economic Models

Ruben Heradio<sup>\*1</sup>, David Fernandez-Amoros<sup>†1</sup>, Jose Antonio Cerrada-Somolinos<sup>‡1</sup>, and Ismael Abad<sup>§1</sup>



# Acceleration Related Work

## Related Work

- State of the art: Black-box #SAT solving

## Limitations

- Scalability for multi-query requirements
- Reuse between different queries

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# Acceleration Related Work

## Related Work

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## Limitations

- Scalability for multi-query requirements
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## Contributions

1. Address multitude of queries with knowledge compilation (**AMAI'24**)
2. Reusing d-DNNFs (**TOSEM'24**)
3. Projected d-DNNF Compilation (**ASE'24**)
4. Pseudo-Boolean d-DNNF Compilation (**TSE'25 Sub.**)

On the benefits of knowledge compilation for feature-model analyses

Chico Sundermann<sup>1</sup> · Elias Kuijter<sup>2</sup> · Tobias Heß<sup>1</sup> · Heiko Raab<sup>1</sup> · Sebastian Krieter<sup>1</sup> · Thomas Thüm<sup>1</sup>

AMAI'24

## Reusing d-DNNFs for Efficient Feature-Model Counting

CHICO SUNDERMANN, University of Ulm, Germany  
HEIKO RAAB, University of Ulm, Germany  
TOBIAS HESS, University of Ulm, Germany  
THOMAS THÜM, Paderborn University, Germany  
INA SCHAEFER, Karlsruhe Institute of Technology, Germany

TOSEM'24

## Efficient Slicing of Feature Models via Projected d-DNNF Compilation

Chico Sundermann  
University of Ulm  
Ulm, Germany

Jacob Loth  
University of Ulm  
Ulm, Germany

Thomas Thüm  
Paderborn University  
Paderborn, Germany

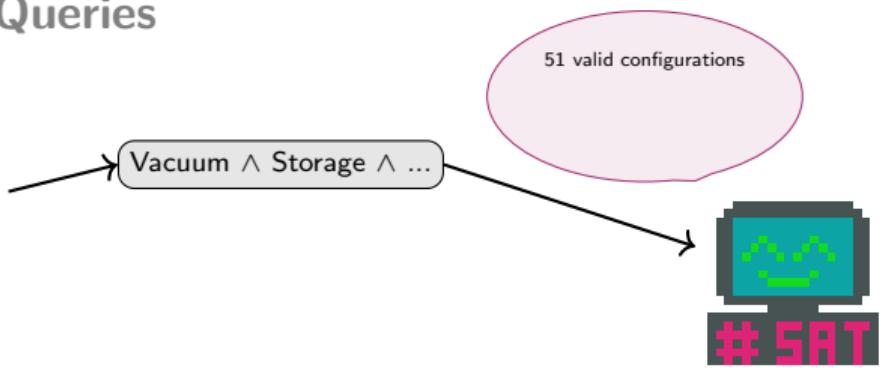
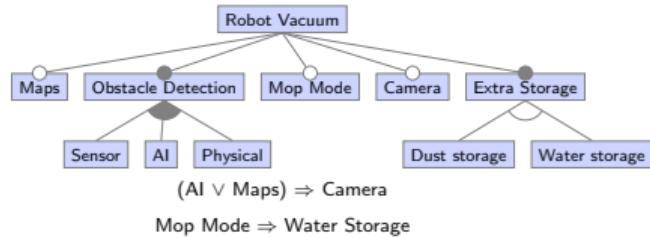
ASE'24

## Tackling Expressive Feature-Modeling Constructs with Pseudo-Boolean d-DNNF Compilation

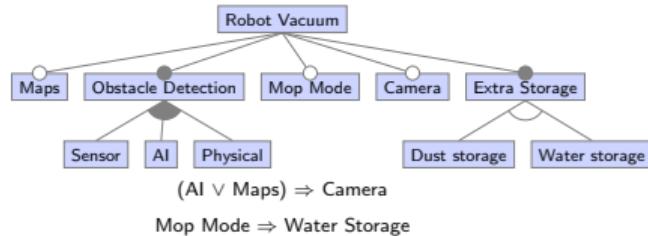
Chico Sundermann<sup>\*†</sup>, Stefan Vill<sup>\*</sup>, Elias Kuijter<sup>‡</sup>, Sebastian Krieter<sup>‡</sup>, Thomas Thüm<sup>†</sup>, and Matthias Tichy<sup>\*</sup>  
<sup>\*</sup> Ulm University, Germany <sup>†</sup> TU Braunschweig, Germany <sup>‡</sup> University of Magdeburg, Germany

TSE Sub.

# Scalability Issues      Multitude of Queries

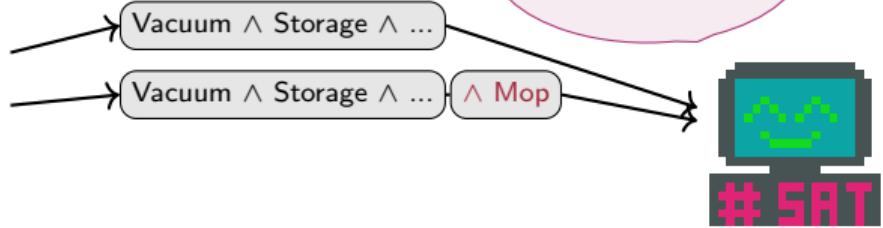
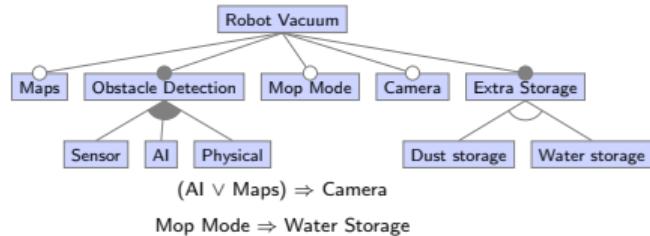


# Scalability Issues      Multitude of Queries



Most systems: Few seconds of runtime

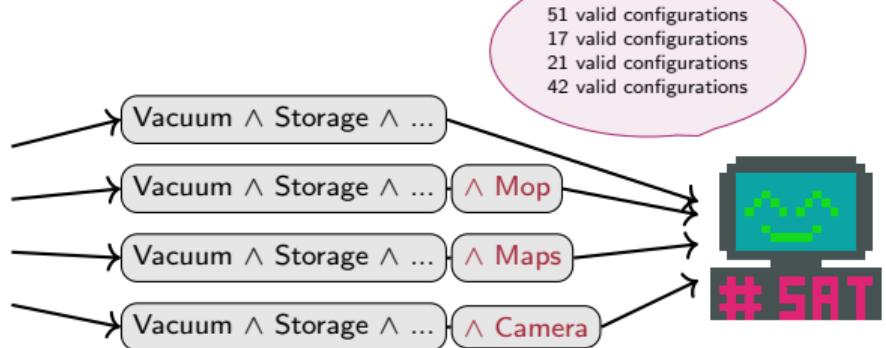
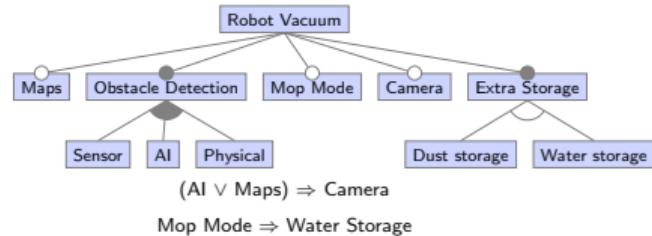
# Scalability Issues      Multitude of Queries



Most systems: Few seconds of runtime

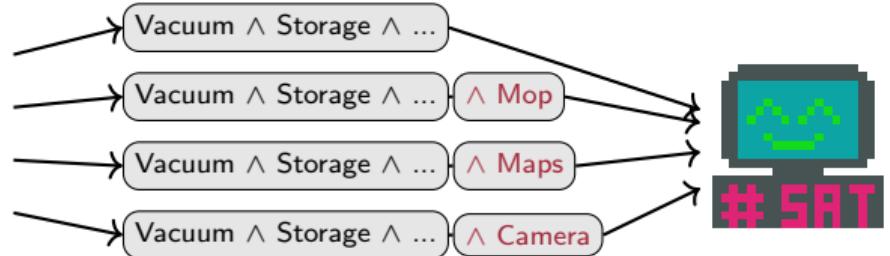
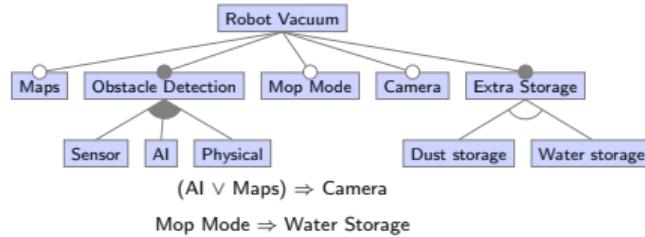


# Scalability Issues      Multitude of Queries



Most systems: Few seconds of runtime

# Scalability Issues      Multitude of Queries

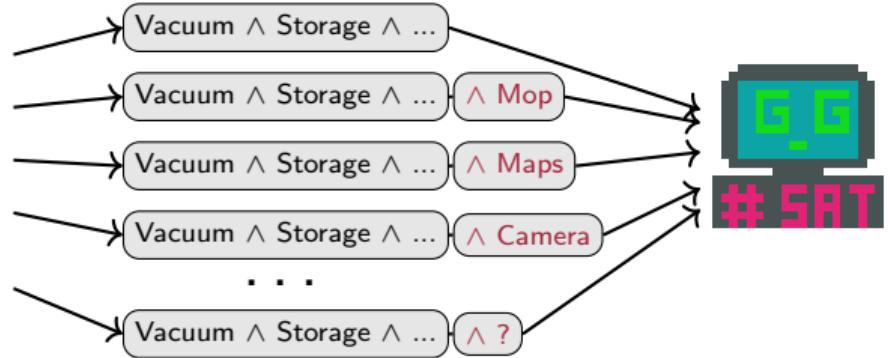
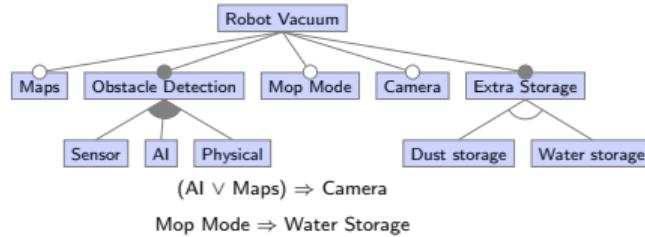


Most systems: Few seconds of runtime

Type	Number of Queries	Repeatability
Features	$O( F )$	Static
	$O( F )$	Static
Partial Configurations	$O( F ^2)$	Dynamic
	$O( F^2 )$	Dynamic
	$O( F )$	Dynamic
	$O( F^2 )$	Dynamic
Formula	1	Dynamic
	1	Dynamic



# Scalability Issues      Multitude of Queries



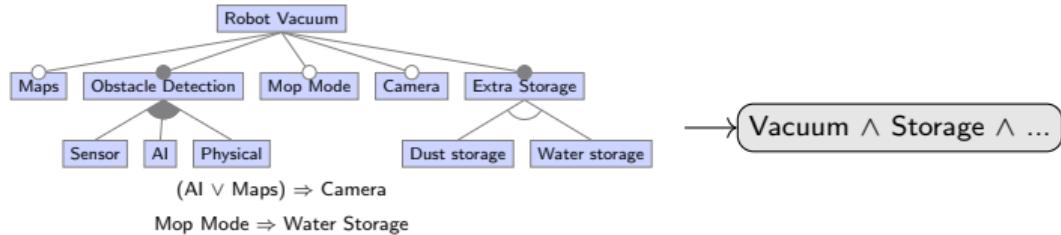
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Formula	1	Dynamic
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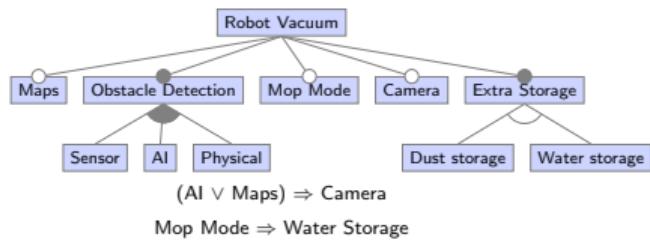


# Acceleration Knowledge Compilation

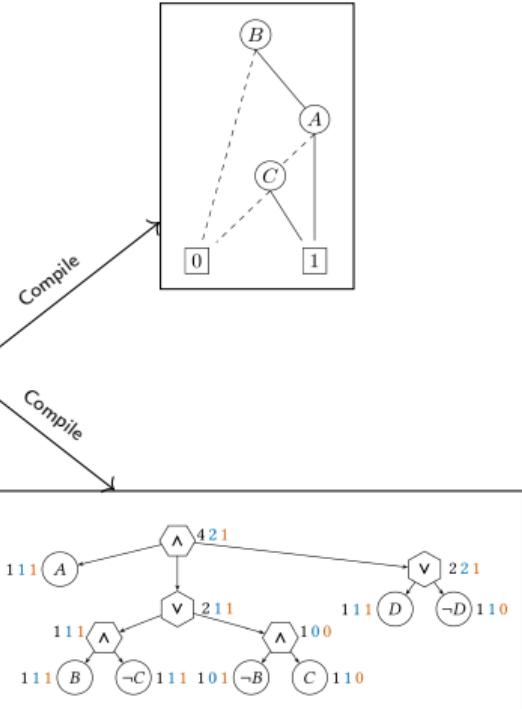


Darwiche and Marquis, A Knowledge Compilation Map, JAIR'02

# Acceleration Knowledge Compilation



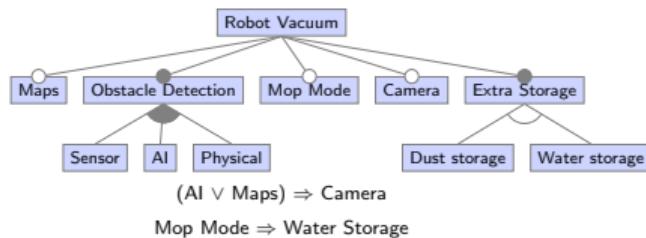
Vacuum  $\wedge$  Storage  $\wedge$  ...



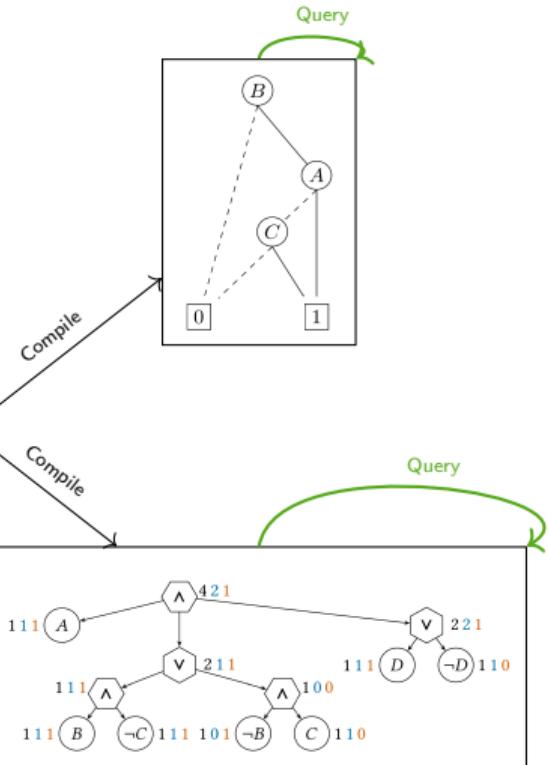
Darwiche and Marquis, A Knowledge Compilation Map, JAIR'02



# Acceleration Knowledge Compilation

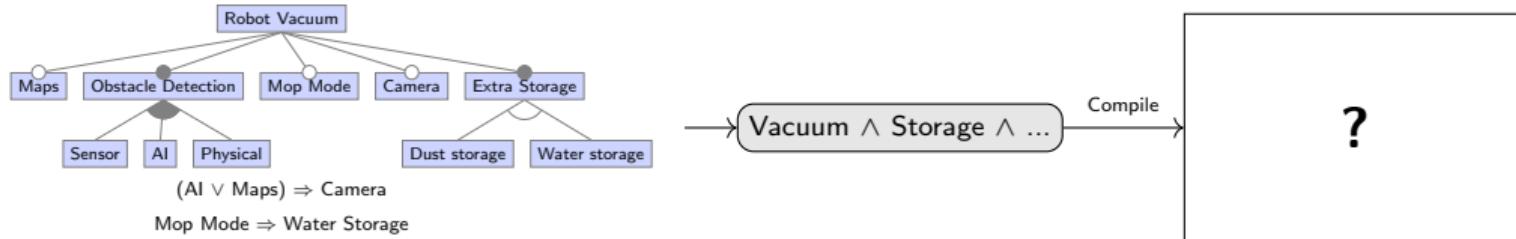


Vacuum  $\wedge$  Storage  $\wedge \dots$



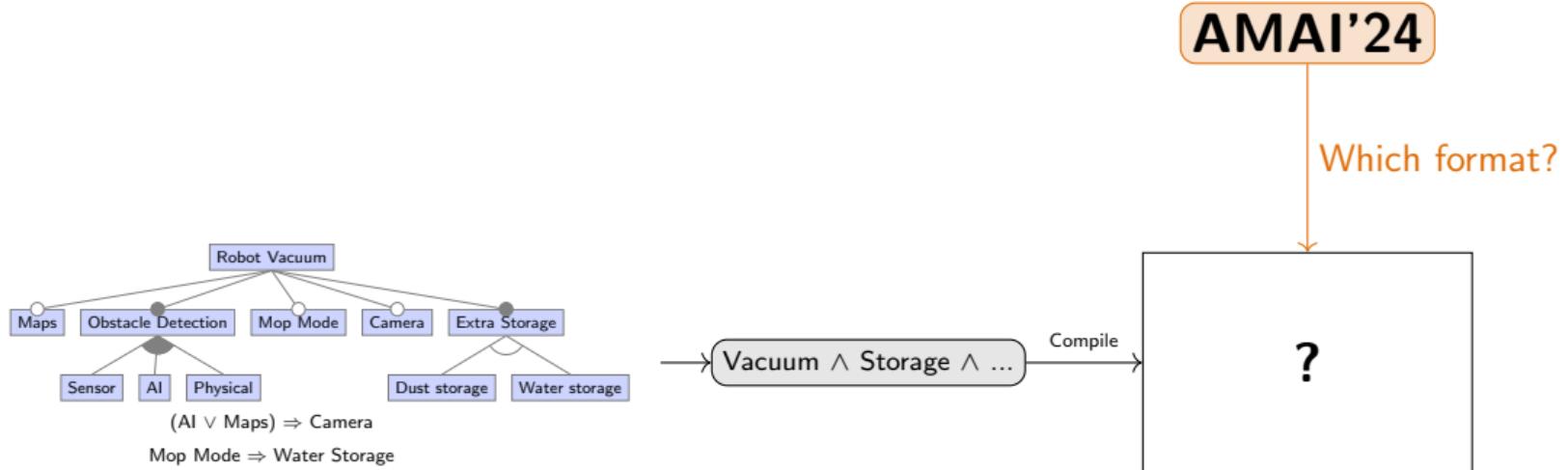
Darwiche and Marquis, A Knowledge Compilation Map, JAIR'02

# Acceleration Knowledge Compilation



Darwiche and Marquis, A Knowledge Compilation Map, JAIR'02

# Acceleration Knowledge Compilation



Darwiche and Marquis, A Knowledge Compilation Map, JAIR'02

# Acceleration Overview Contributions

1. Which problems need to be solved?

Survey over existing analyses surveys

Classify analyses by underlying problem

2. Which knowledge compilation formats exist?

SLR on knowledge compilation

3. What are the capabilities of the formats?

Mapping languages to tractable analyses

4. How do available compilers scale?

SLR & Github search for compilers

Empirical evaluation on feature models

# Acceleration Overview Contributions

1. Which problems need to be solved?

Survey over existing analyses surveys

Classify analyses by underlying problem

**Which knowledge compilation format to use in what scenario?**

2. What are the capabilities of the formats?

Mapping languages to tractable analyses

4. How do available compilers scale?

SLR & Github search for compilers

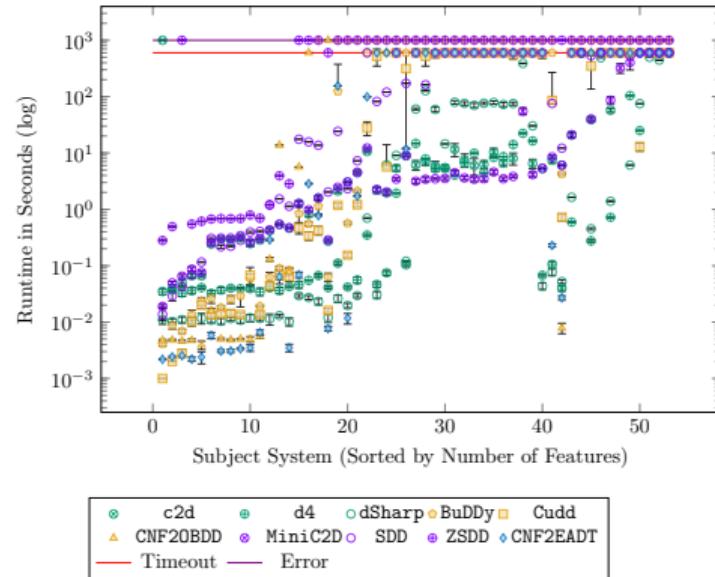
Empirical evaluation on feature models

# Acceleration Format Capabilities

	SAT-Based			#SAT-Based			AllSAT Enum.	Algebraic		
	$CO$	$CO_f$	$CO_c$	$\#FM$	$\#FM_f$	$\#FM_c$		$Comp$	$Diff.$	$Slice$
<b>CNF</b>										
Horn	✓	✓	✓							
EPCCL	✓	✓	✓							
DNF	✓	✓	✓				✓			✓
DNNF	✓	✓	✓				✓			✓
d-DNNF	✓	✓	✓	✓	✓	✓	✓			
EADT	✓	✓	✓	✓	✓	✓	✓			
SDD	✓	✓	✓	✓	✓	✓	✓			
PI	✓	✓	✓	✓	✓	✓	✓			✓
IP	✓	✓	✓	✓	✓	✓	✓			
ROBDD	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
MODS	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓

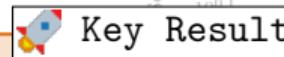
# Acceleration Scalability Compilers

	#SAT-Based		
	#FM	#FM <sub>f</sub>	#FM <sub>c</sub>
CNF			
Horn			
EPCCL			
DNF			
DNNF			
d-DNNF	✓	✓	✓
EADT	✓	✓	✓
SDD	✓	✓	✓
PI	✓	✓	✓
IP	✓	✓	✓
ROBDD	✓	✓	✓
MODS	✓	✓	✓

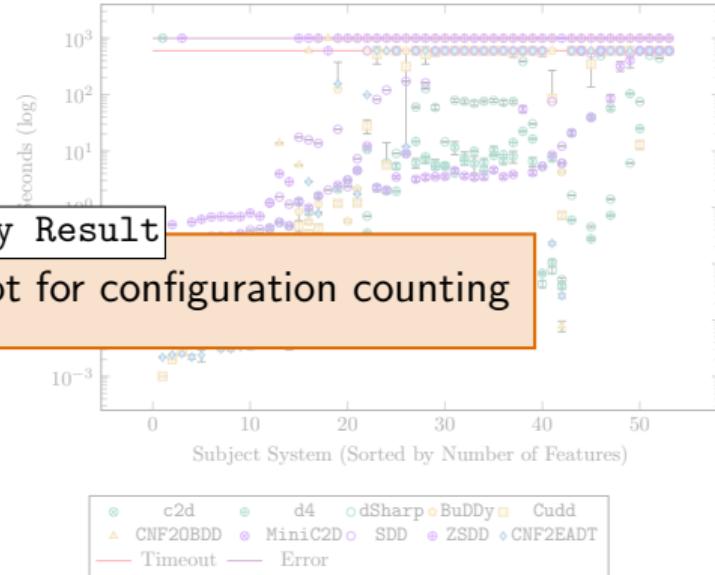


# Acceleration Scalability Compilers

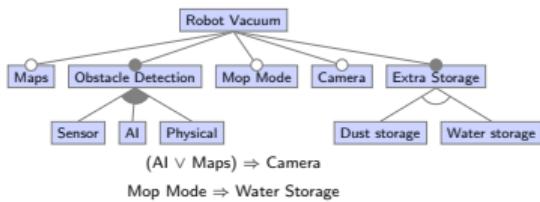
	#SAT-Based		
	#FM	#FM <sub>f</sub>	#FM <sub>c</sub>
CNF			
Horn			
EPCCL			
DNF			
DNNF			
d-DNNF	✓		
EADT	✓	✓	✓
SDD	✓	✓	✓
PI	✓	✓	✓
IP	✓	✓	✓
ROBDD	✓	✓	✓
MODS	✓	✓	✓



d-DNNFs are a sweet-spot for configuration counting

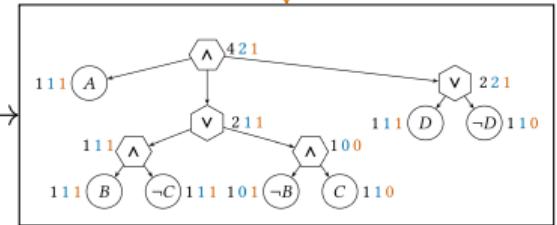


# Configuration Counting with Knowledge Compilation



Vacuum  $\wedge$  Storage  $\wedge$  ...

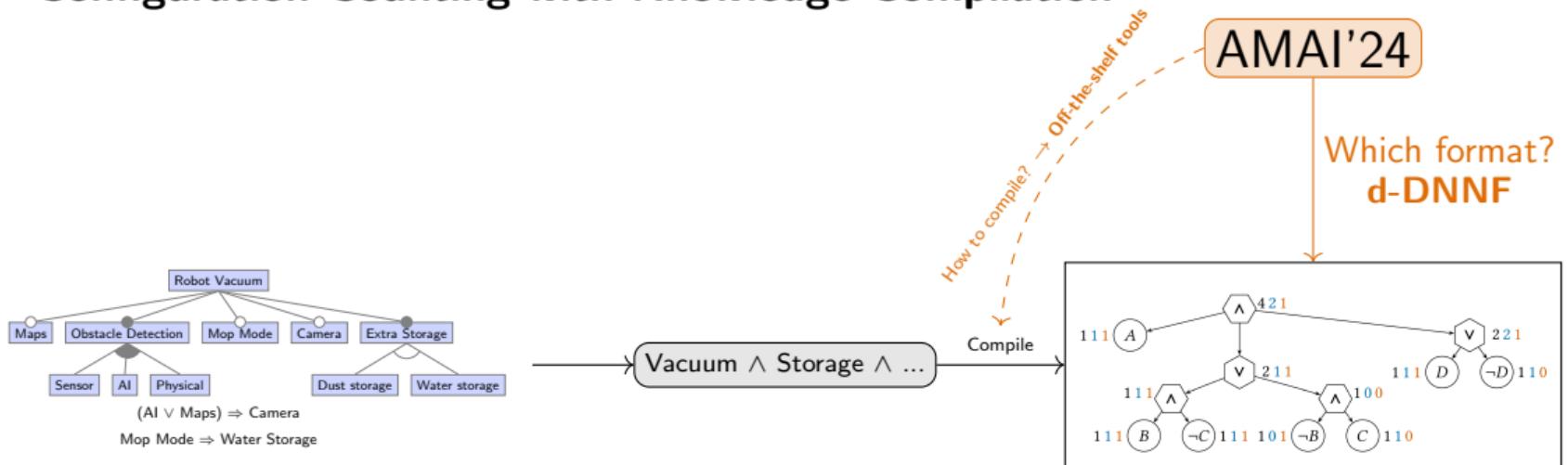
Compile



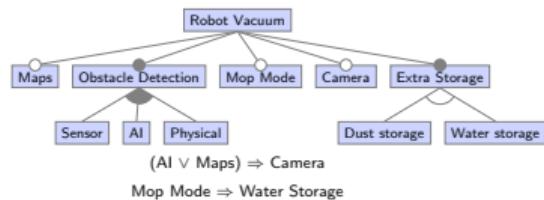
AMAI'24

Which format?  
d-DNNF

# Configuration Counting with Knowledge Compilation

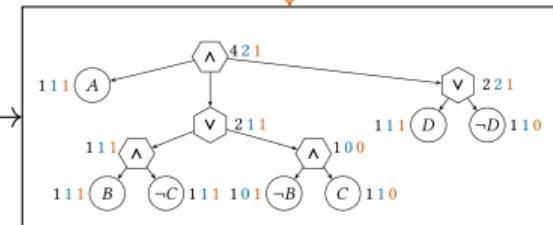


# Configuration Counting with Knowledge Compilation



$Vacuum \wedge Storage \wedge \dots$

Compile



AMAI'24

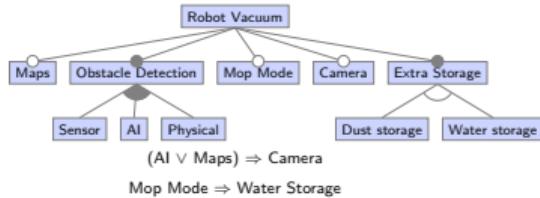
Which format?  
d-DNNF

TOSEM'24

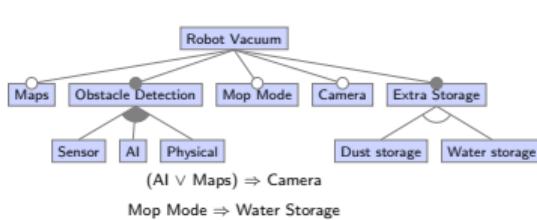
How to reuse?



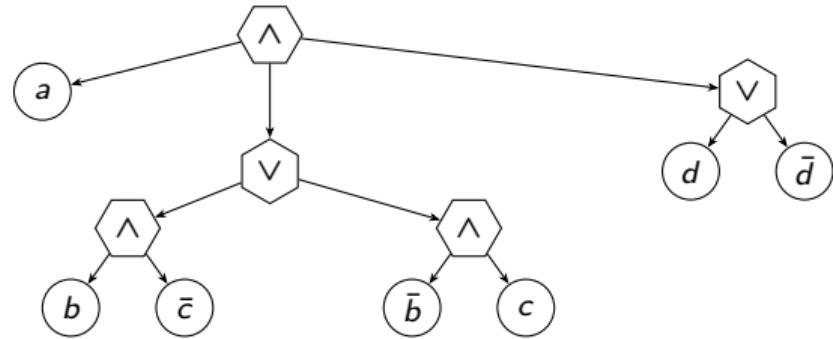
# Reusing d-DNNFs Approach



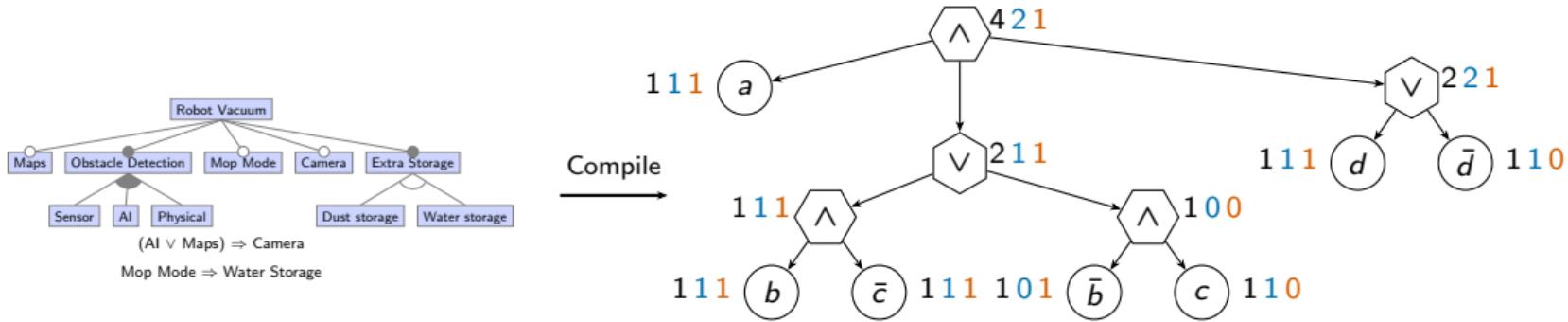
# Reusing d-DNNFs Approach



Compile  
→



# Reusing d-DNNFs Approach

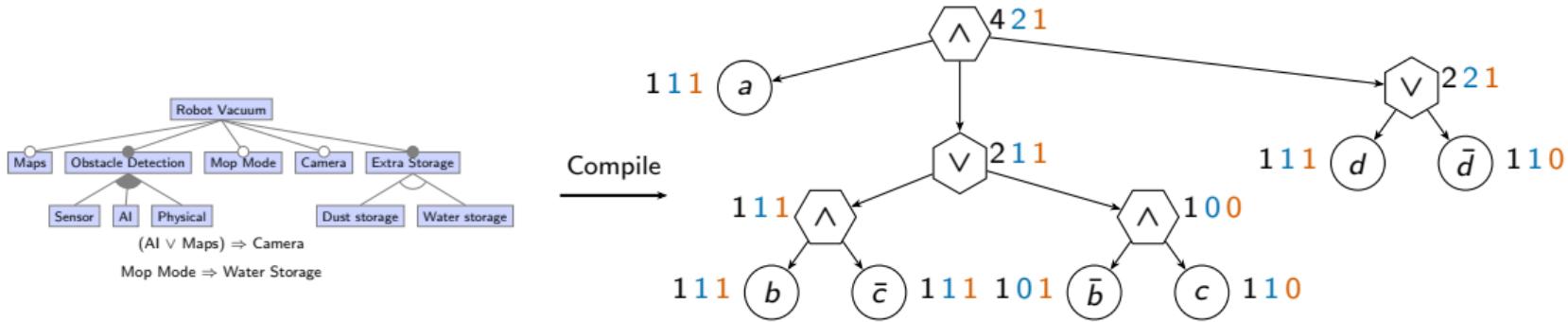


**ddnnife**

#FM (Feature Model):	.	$\wedge : \prod$
#f (Feature):	$b$	$\vee : \sum$
# $C_p$ (Partial Config.):	$\{\bar{c}, d\}$	$a$

<sup>a</sup>Basic algorithm adapted from: Darwiche, On the Tractable Counting of Theory Models and its Application to Belief Revision and Truth Maintenance, JANCL'01

# Reusing d-DNNFs Approach

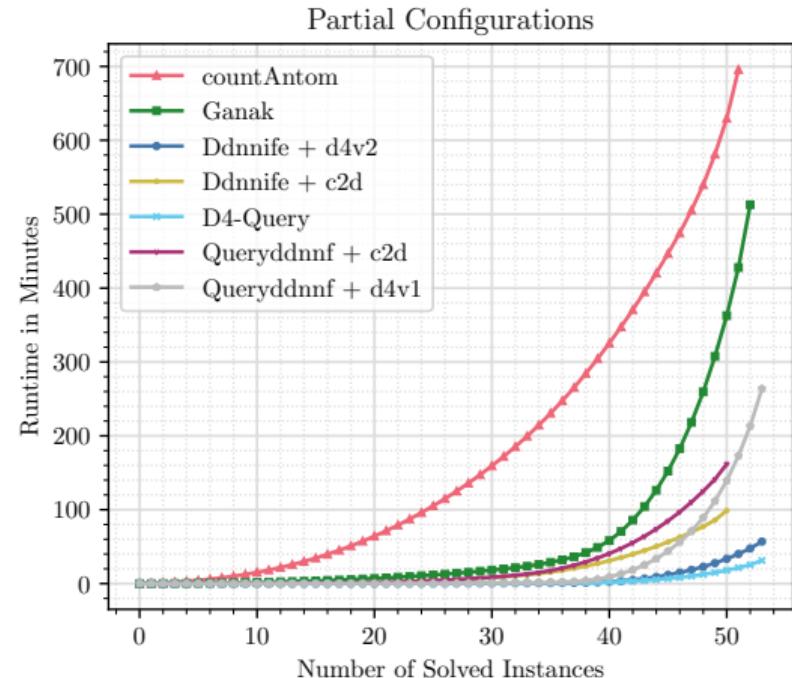
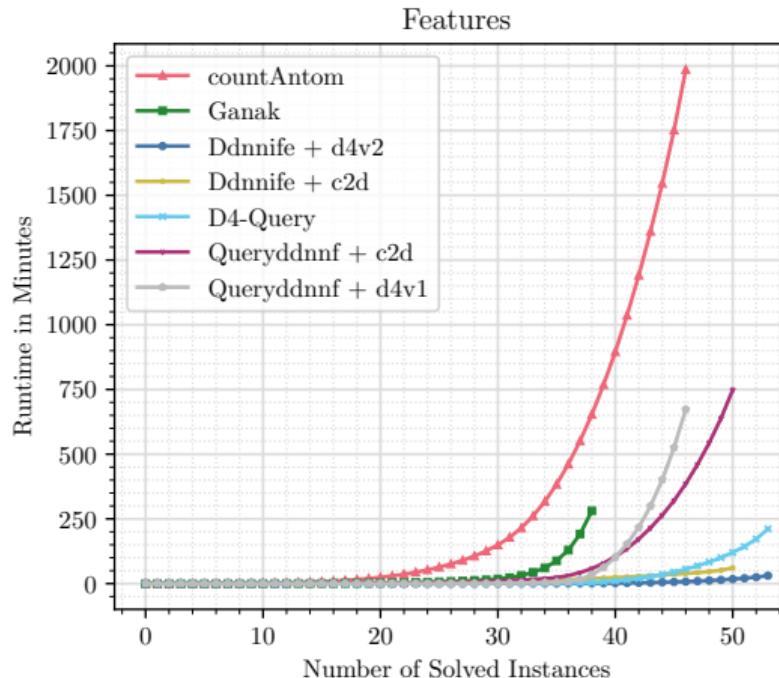


**ddnnife**

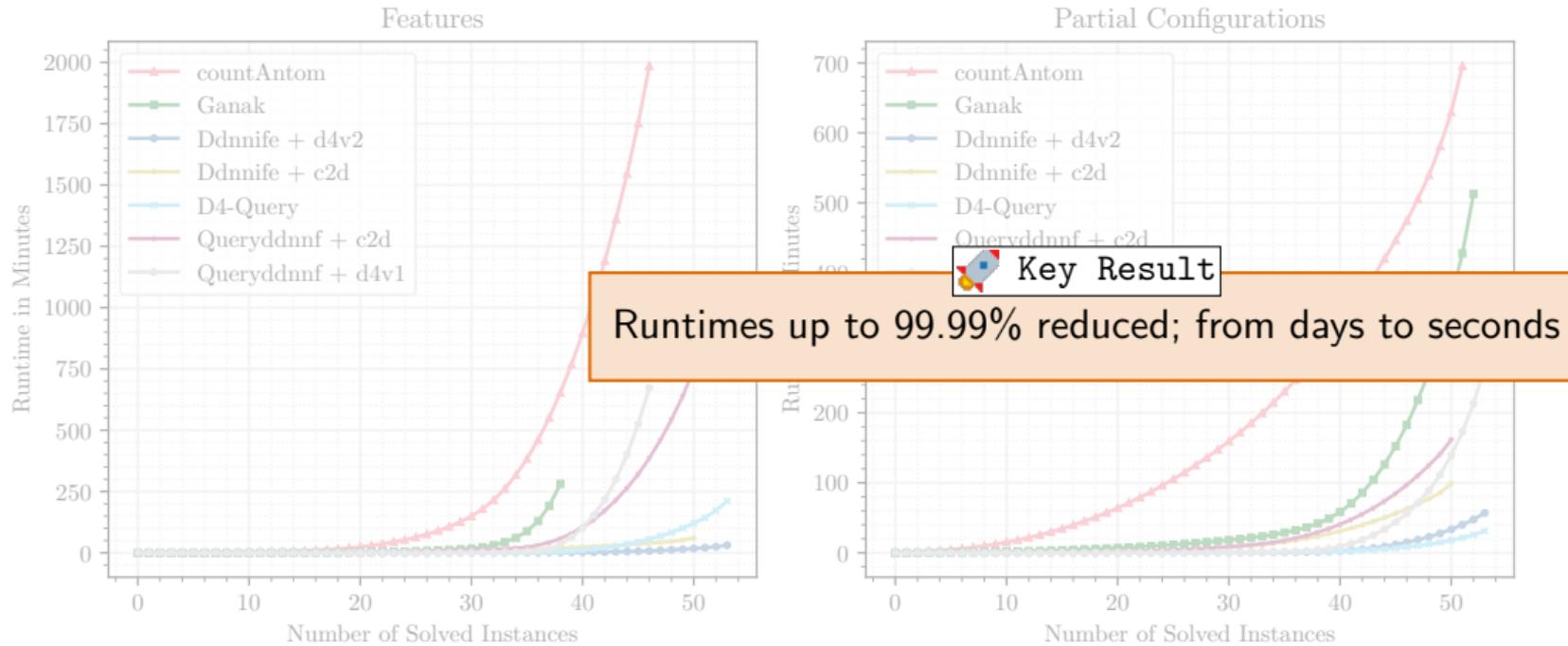
$$\begin{aligned} \#FM \text{ (Feature Model)}: & \quad \cdot \quad \wedge : \prod \\ \#f \text{ (Feature)}: & \quad b \quad \vee : \sum \\ \#C_p \text{ (Partial Config.)}: & \quad \{\bar{c}, d\} \end{aligned}$$

Partial Traversals   Partial Derivatives  
Reusing Subtrees   Core/Dead features  
...   ...

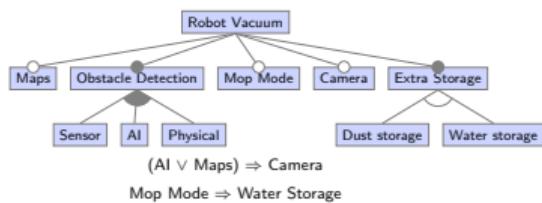
# Reusing d-DNNFs Performance



# Reusing d-DNNFs Performance

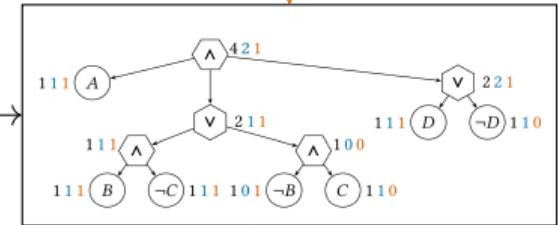


# Acceleration with Knowledge Compilation



Vacuum  $\wedge$  Storage  $\wedge$  ...

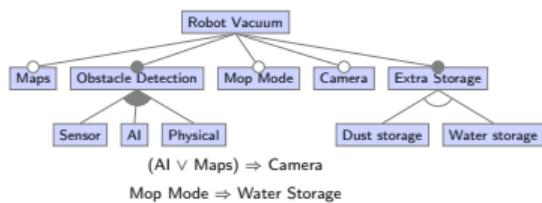
Compile



How to reuse?

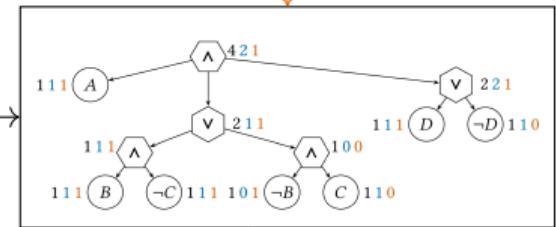
TOSEM'24

# Acceleration with Knowledge Compilation



Vacuum  $\wedge$  Storage  $\wedge$  ...

Compile



Query

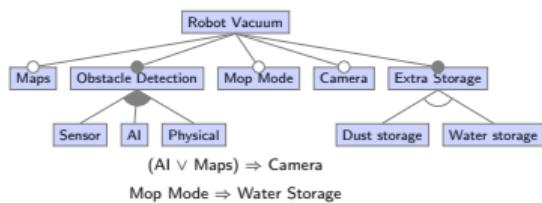
ASE'24

TOSEM'24

How to reuse?

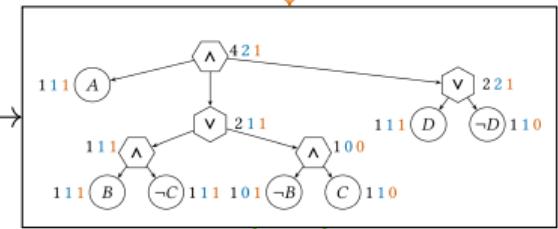
AMAI'24  
Which format?  
d-DNNF

# Acceleration with Knowledge Compilation



Vacuum  $\wedge$  Storage  $\wedge$  ...

Compile



How to compile subsets?

ASE'24

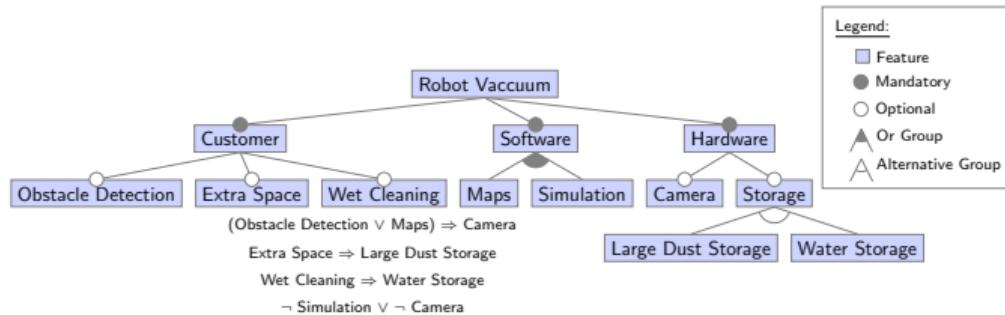
TOSEM'24

Which format?  
d-DNNF

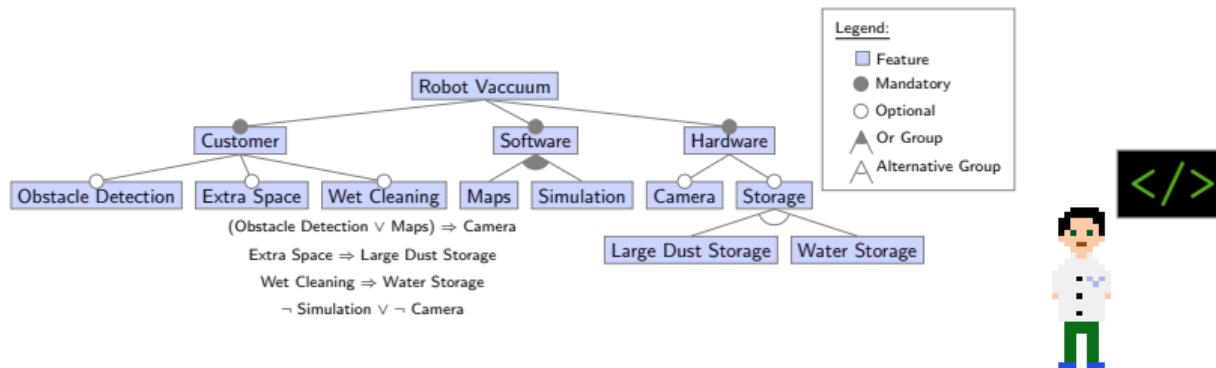
AMAI'24

How to reuse?

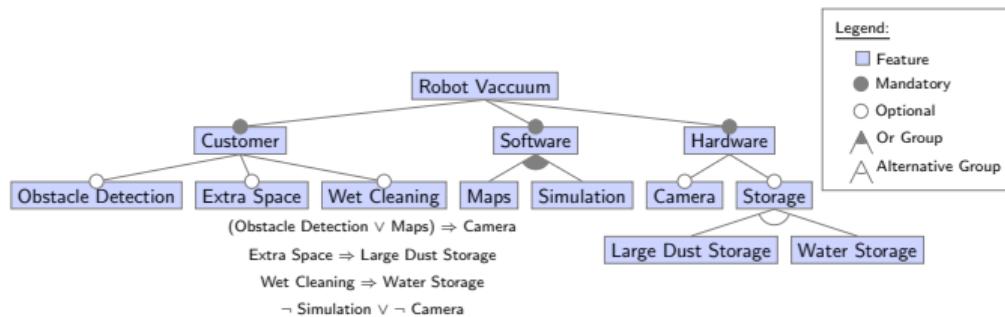
# Acceleration      Queries on Feature Subsets



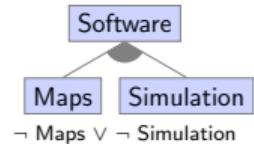
# Acceleration      Queries on Feature Subsets



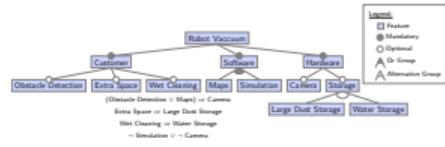
# Acceleration      Queries on Feature Subsets



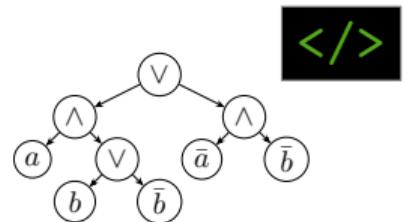
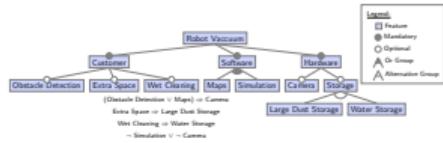
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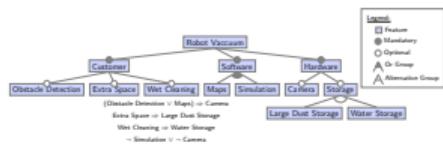
# Projected d-DNNF Compilation Approach



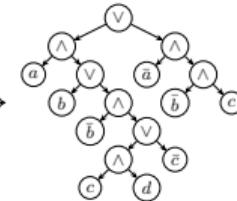
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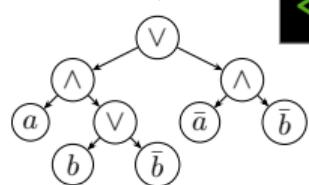
# Projected d-DNNF Compilation Approach



d-DNNF Compilation

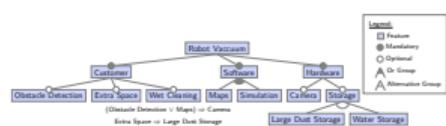


Forgetting

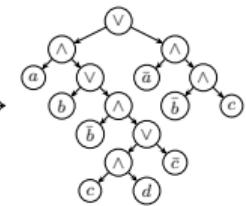


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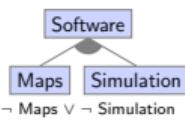
# Projected d-DNNF Compilation Approach



d-DNNF Compilation

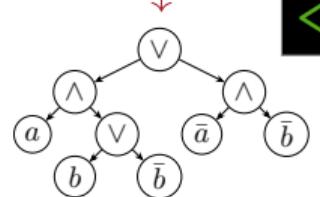


Feature-Model Slicing  
(Acher et al., Krieter et al.)



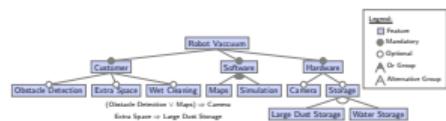
d-DNNF Compilation (Darwiche)

Forgetting

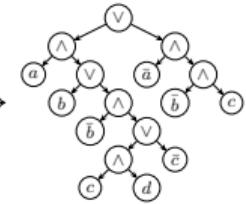


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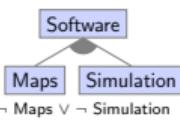
# Projected d-DNNF Compilation Approach



d-DNNF Compilation



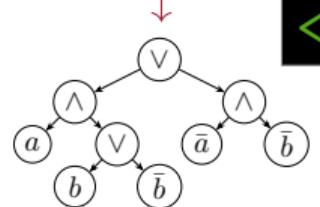
Feature-Model Slicing  
(Acher et al., Krieter et al.)



*Projected d-DNNF Compilation (pd4)*

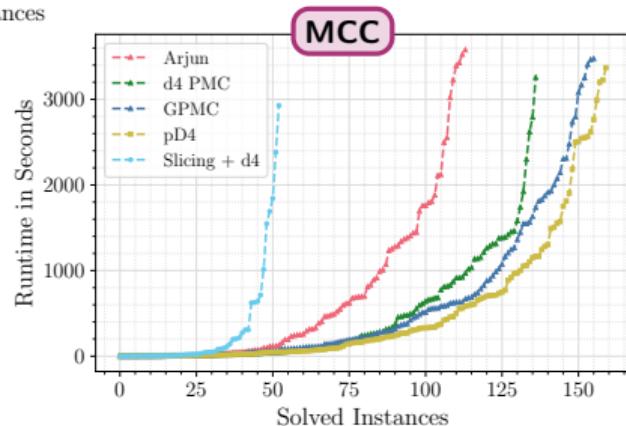
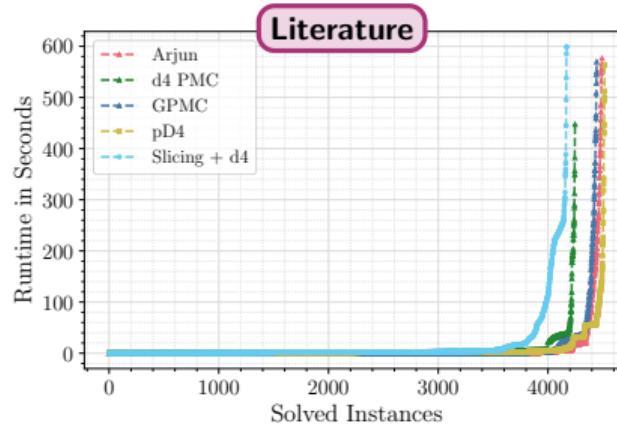
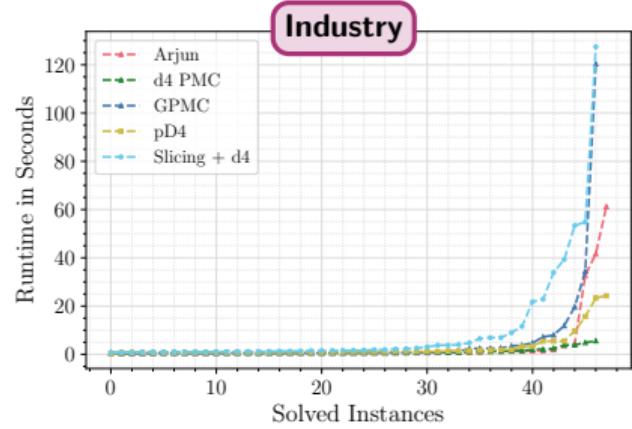
d-DNNF Compilation (Darwiche)

Forgetting

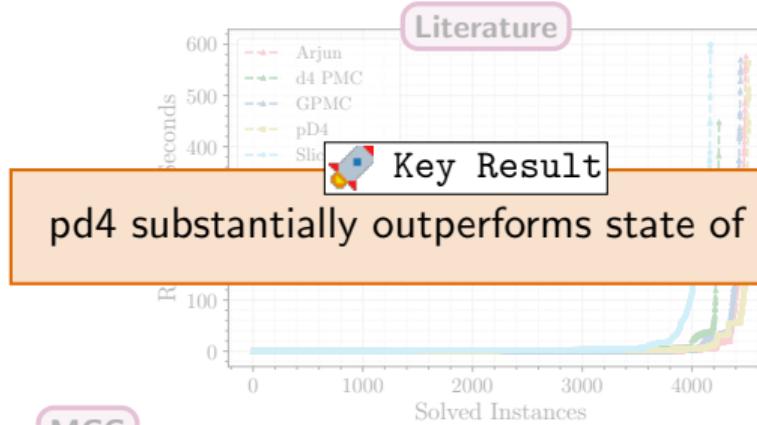
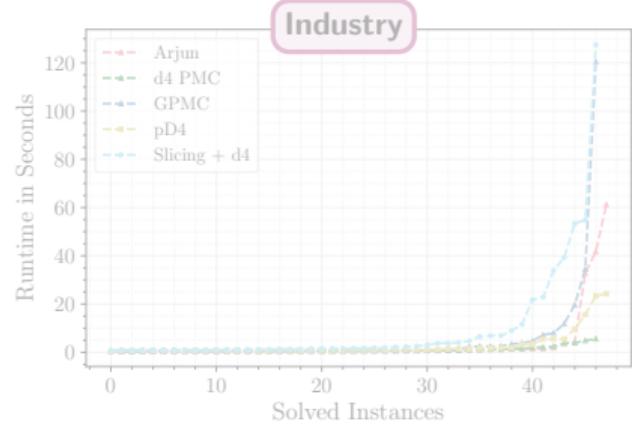


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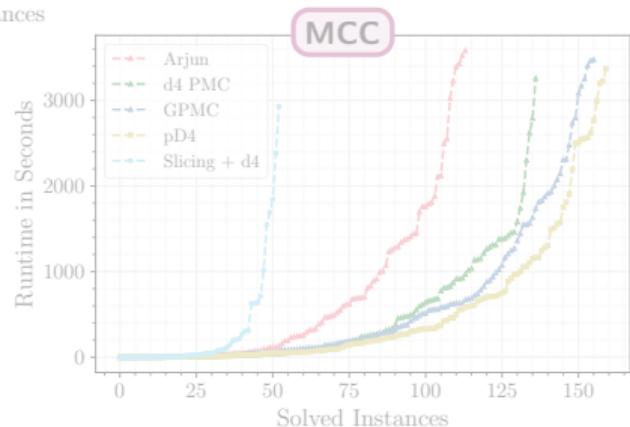
# Projected d-DNNF Compilation Performance



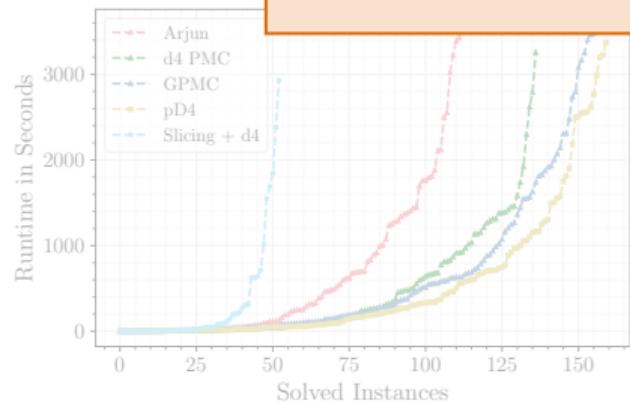
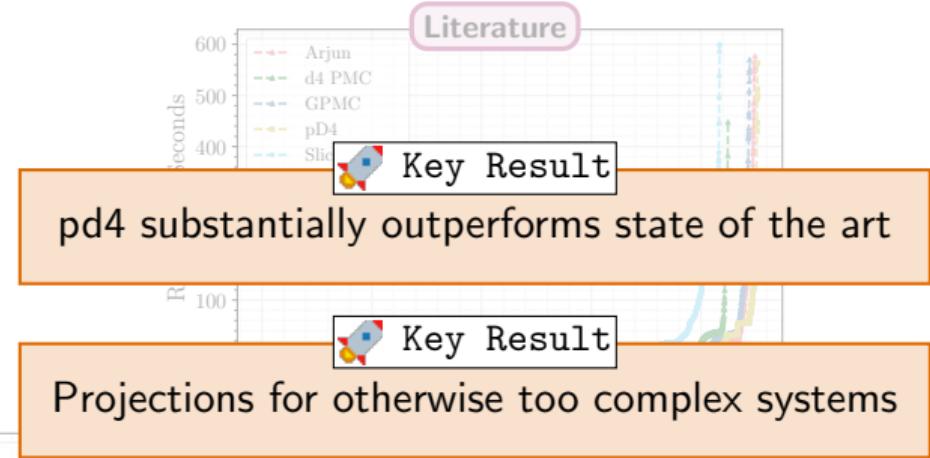
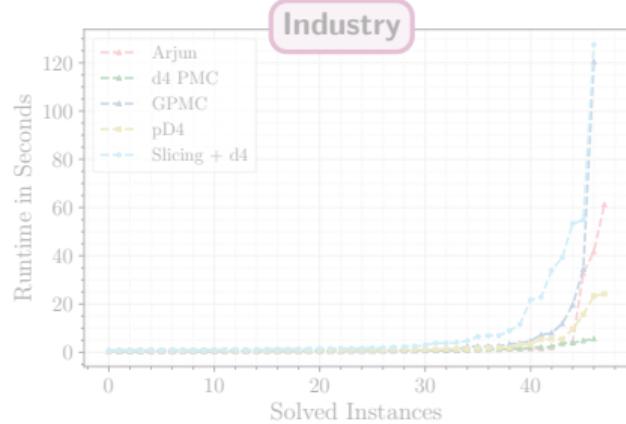
# Projected d-DNNF Compilation Performance



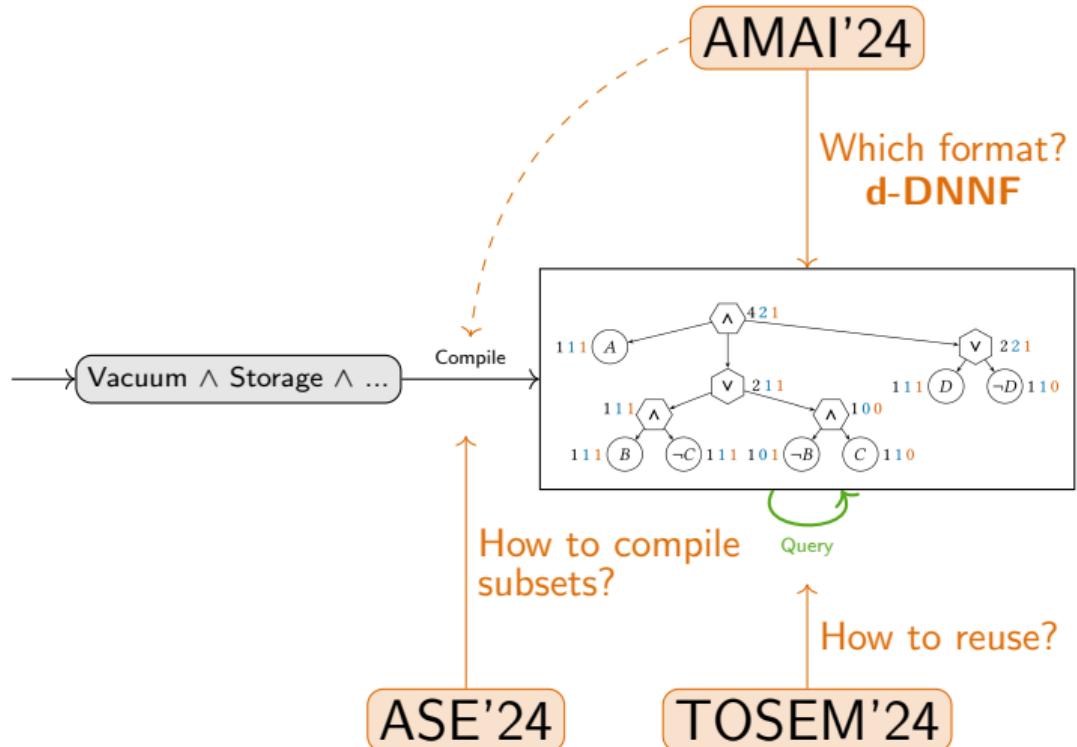
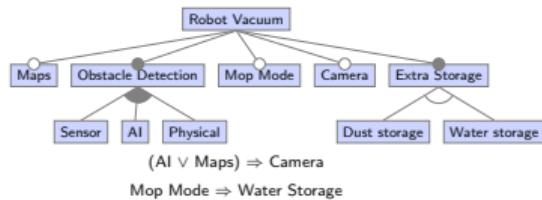
**Key Result**  
pd4 substantially outperforms state of the art



# Projected d-DNNF Compilation Performance

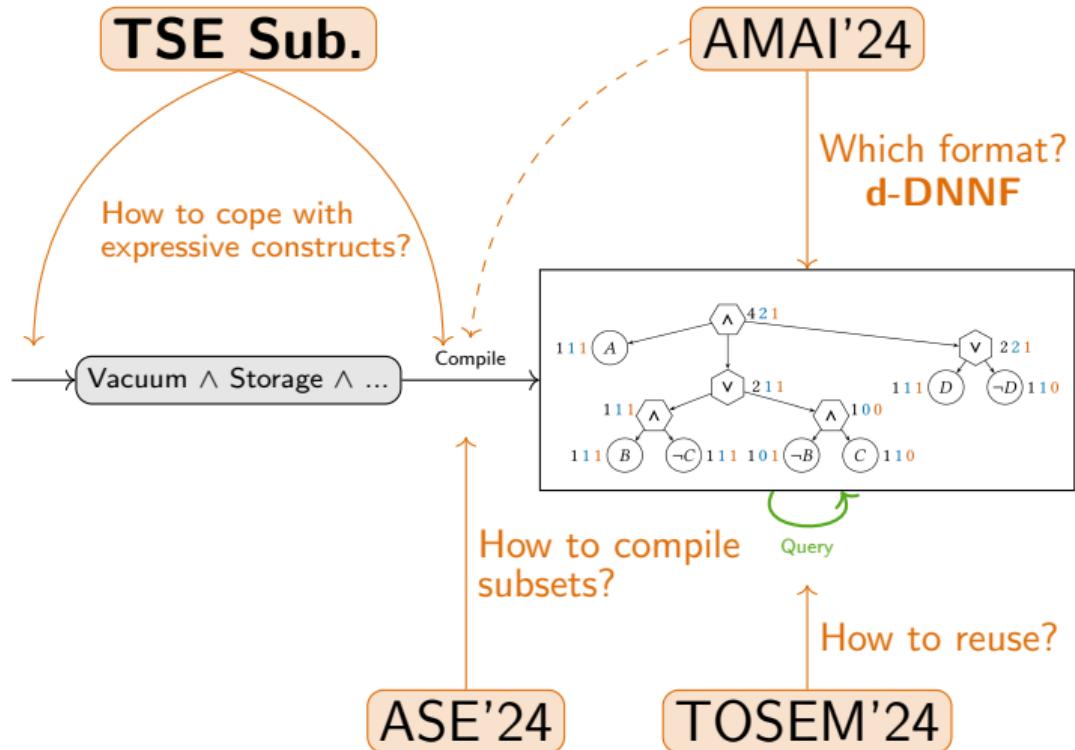
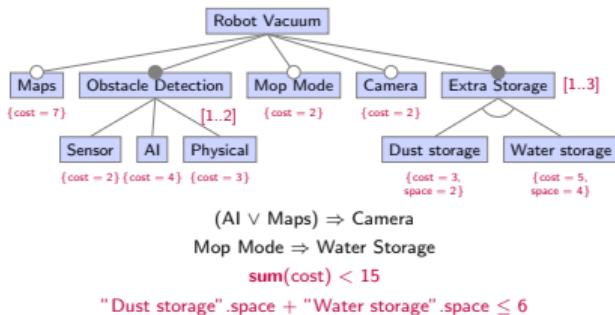


# Acceleration with Knowledge Compilation

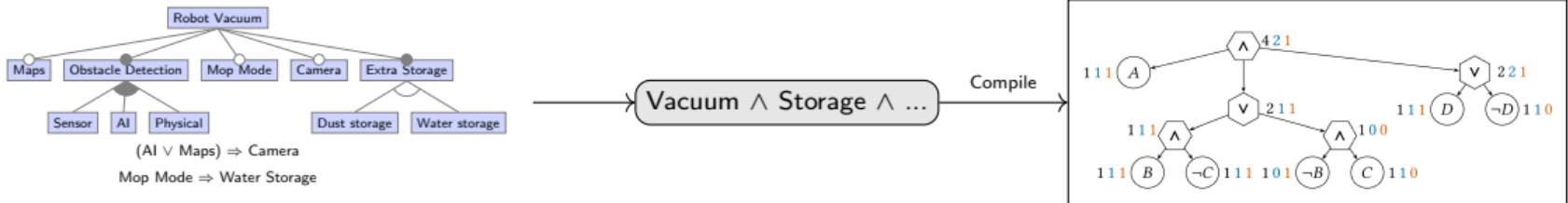




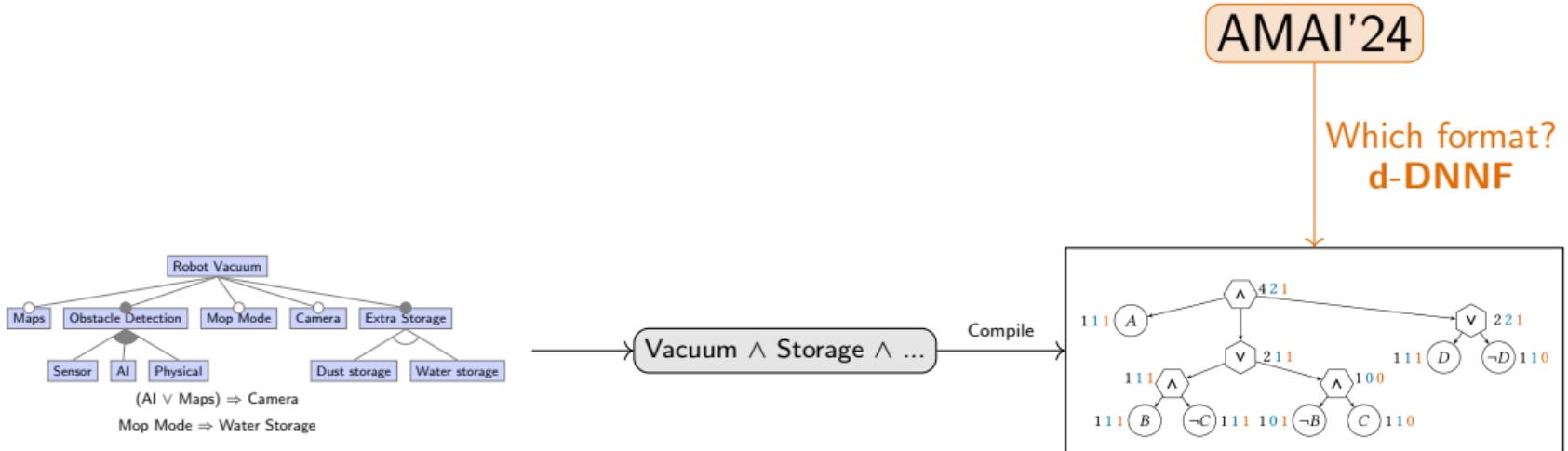
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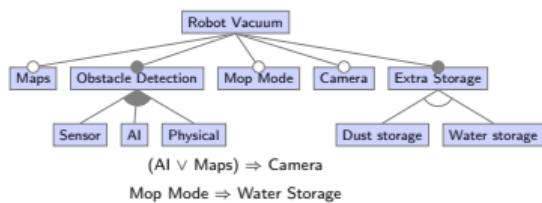
# Acceleration with Knowledge Compilation



# Acceleration with Knowledge Compilation

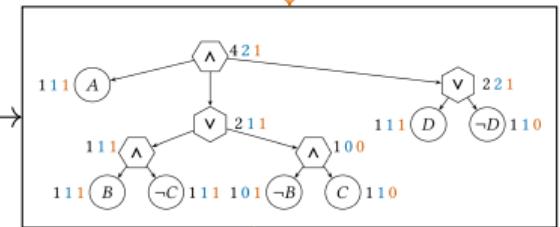


# Acceleration with Knowledge Compilation



Vacuum  $\wedge$  Storage  $\wedge$  ...

Compile



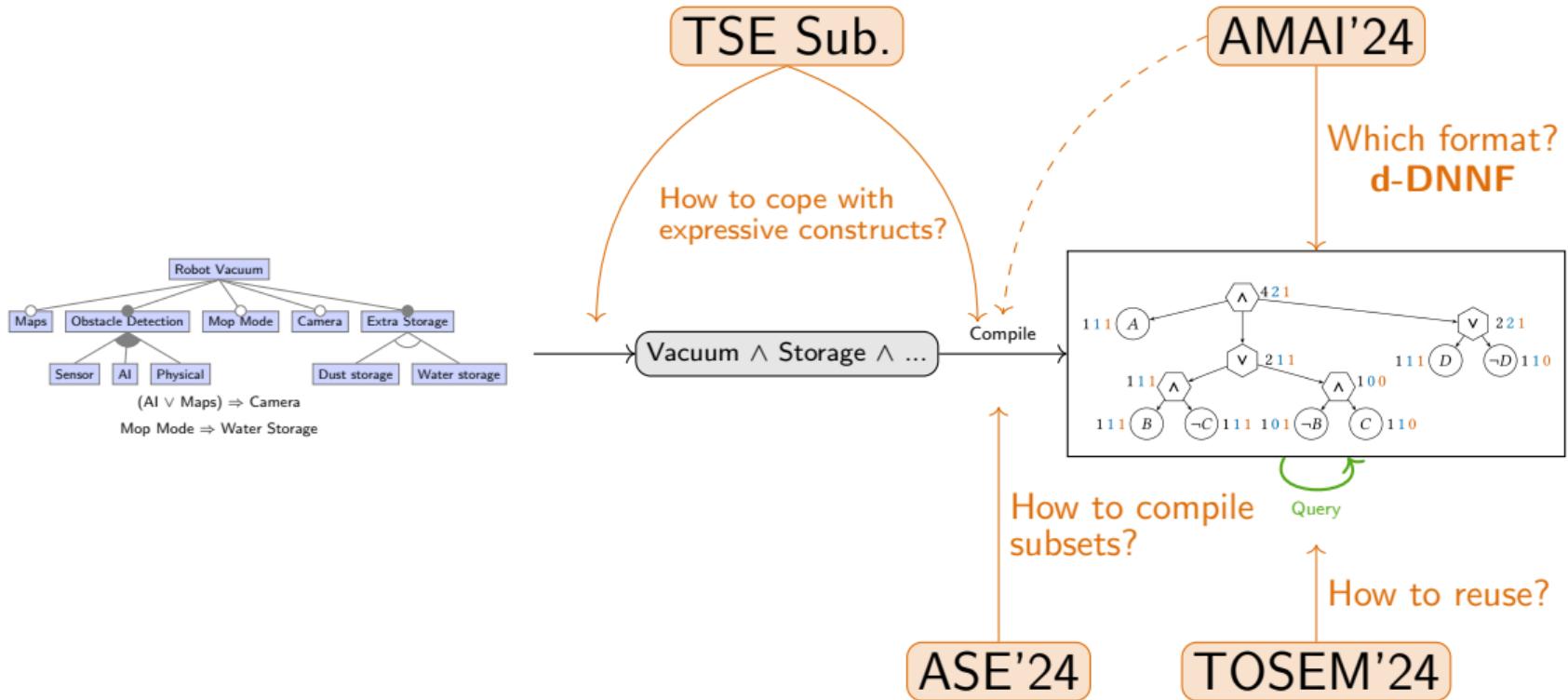
Query

TOSEM'24

How to reuse?

AMAI'24  
Which format?  
d-DNNF

# Acceleration with Knowledge Compilation





## Applications & Problem Settings

### Key Contributions

Collect applications  
Add industrial applications  
Computation instructions

VaMoS'21

AMAI'24

### Key Results

Plenty applications  
Multitude of queries



## Scalability State of the Art

### Key Contributions

Gather #SAT solvers  
Gather industrial models  
Performance study

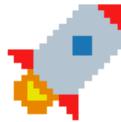
VaMoS'20

EMSE'23

SPLC'24

### Key Results

Most systems in few seconds  
Few systems do not scale at all



## Accelerate the Multitude of Queries

### Key Contributions

Knowledge-compilation ecosystem  
Efficient reuse of d-DNNFs  
Projection compilation  
Pseudo-Boolean compilation

AMAI'24

TOSEM'24

ASE'24

TSE Sub.

### Key Results

Runtimes reduced from days to seconds  
Compilation enabled for new scenarios  
Successfully applied in industry

## Applications & Problem Settings



### Key Contributions

- Collect applications
- Add industrial applications
- Computation instructions

VaMoS'21

AMAI'24

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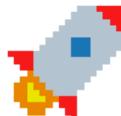
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## Accelerate the Multitude of Queries

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AMAI'24

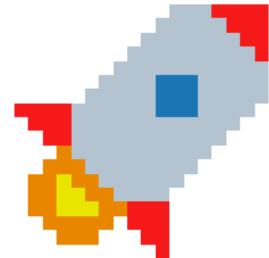
TOSEM'24

ASE'24

TSE Sub.

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**Applications &  
Problem Settings**

**Scalability  
State of the Art**

**Accelerate the  
Multitude of Queries**

## Unleashing the Potential of Configuration Counting for Product Lines

PhD Defense | Chico Sundermann | 12.08.2025

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<https://doi.org/10.1145/3442391.3442404>

# Unleashing the Potential of Configuration Counting for Product Lines

## 1. Introduction

Product Lines  
Feature Dependencies  
Configuration Counting

## 2. Contributions

Overview

## 3. Applications

Related Work

Example Application

## 4. State of the Art

Overview

Related Work

Runtimes #SAT on Feature Models

## 5. Acceleration

Related Work

AMAI'24

TOSEM'24

ASE'24

TSE Sub.

## 6. Conclusion

Content Overview