$$\begin{split} R[\mathbb{I}](x^{\mathbb{R}}) &:= \operatorname{let}\left(r,s\right) = \operatorname{Env}_{\mathcal{E}}[\{x^{\mathbb{R}}\} \cup \mathbb{I},\emptyset](\operatorname{Sc}(x^{\mathbb{R}}))\} \text{ in } \\ & \left\{ \bigcup_{i \neq r} \operatorname{Imp} \operatorname{Imp} \left\{ x^{\mathbb{D}} \middle| x^{\mathbb{D}} \in s \right\} = \emptyset \right. \\ & \left\{ x^{\mathbb{D}} \middle| x^{\mathbb{D}} \in s \right\} \end{split}$$

$$Env_{re}[\mathbb{I},\mathbb{S}](S) := \left\{ (\mathsf{T},\emptyset) & \text{if } S \in \mathbb{S} \text{ or } re = \varnothing \\ \operatorname{Env}_{re}^{\mathcal{L} \cup \{\mathbb{D}\}}[\mathbb{I},\mathbb{S}](S) \right. \\ & \left[\operatorname{Env}_{re}^{\mathbb{I}}[\mathbb{I},\mathbb{S}](S) := \left\{ (\operatorname{Env}_{re}^{\{l' \in L | l' < l\}}[\mathbb{I},\mathbb{S}](S) \triangleleft \operatorname{Env}_{re}^{l}[\mathbb{I},\mathbb{S}](S) \right. \right\} \\ & \left[\operatorname{Env}_{re}^{\mathbb{I}}[\mathbb{I},\mathbb{S}](S) := \left\{ (\mathsf{T},\emptyset) & \text{if } [\mathbb{I}] \notin re \\ (\mathsf{T},\mathcal{D}(S)) \right. \\ & \left. \operatorname{Env}_{re}^{l}[\mathbb{I},\mathbb{S}](S) := \left\{ (\mathsf{P},\emptyset) & \text{if } S_{l}^{\mathbb{D}} \text{ contains a variable or } \operatorname{IS}^{l}[\mathbb{I}](S) = \mathsf{U} \\ & \left. \operatorname{Env}_{re}[\mathbb{I},\mathbb{S}](S) := \left\{ (\operatorname{Imp}^{\mathbb{I}}(S) \cup \operatorname{Imp}^{\mathbb{D}}(S_{l}^{\mathbb{D}}) \cap \operatorname{Imp}^{\mathbb{D}}(S_{l}^{\mathbb{D}}) \right\} \right. \\ & \left. \operatorname{IS}^{l}[\mathbb{I}](S) := \left\{ \mathsf{U} & \text{if } \exists y^{\mathbb{R}} \in (S_{l}^{\mathbb{D}} \setminus \mathbb{I}) \text{ s.t. } \operatorname{R}[\mathbb{I}](y^{\mathbb{R}}) = \mathsf{U} \\ \left. \left\{ S' \mid y^{\mathbb{R}} \in (S_{l}^{\mathbb{D}} \setminus \mathbb{I}) \wedge y^{\mathbb{D}} \in \operatorname{R}[\mathbb{I}](y^{\mathbb{R}}) \wedge y^{\mathbb{D}} \longrightarrow S' \right\} \right. \end{aligned}$$