

# Lecture 10: Data-Flow Analysis

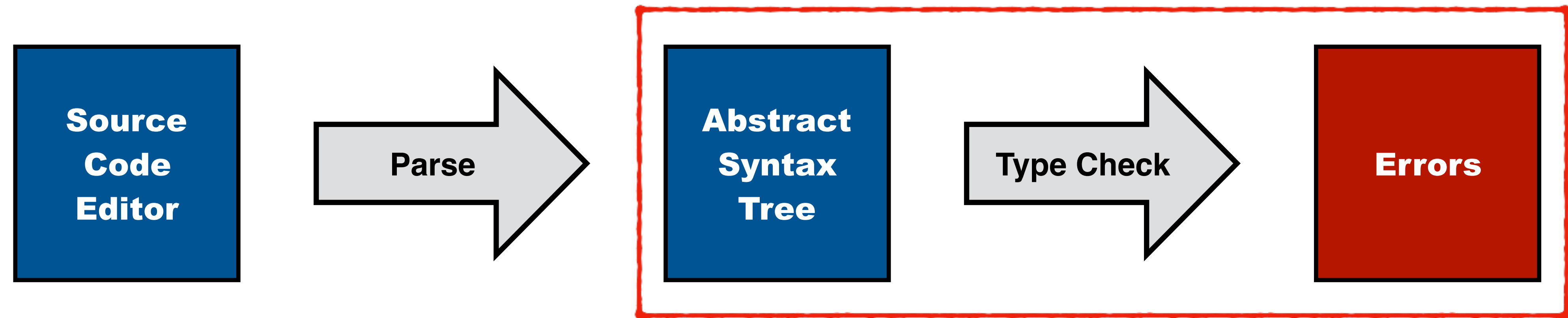
**Jeff Smits**

**CS4200 Compiler Construction**

**TU Delft**

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# Earlier Lecture



Check that names are used correctly and that expressions are well-typed

# Earlier Lecture

## Why Type Checking? Some Discussion Points

### Dynamically Typed vs Statically Typed

- Dynamic: type checking at run-time
- Static: type checking at compile-time (before run-time)

### What does it mean to type check?

- Type safety: guarantee absence of run-time type errors

### Why static type checking?

- Avoid overhead of run-time type checking
- Fail faster: find (type) errors at compile time
- Find all (type) errors: some errors may not be triggered by testing
- But: not all errors can be found statically (e.g. array bounds checking)

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## Why types?

### Why types?

- Statically prove the absence of certain (wrong) runtime behavior
  - ▶ “Well-typed programs cannot go wrong.” [Reynolds1985]
  - ▶ Also logical properties beyond runtime problems

### What are types?

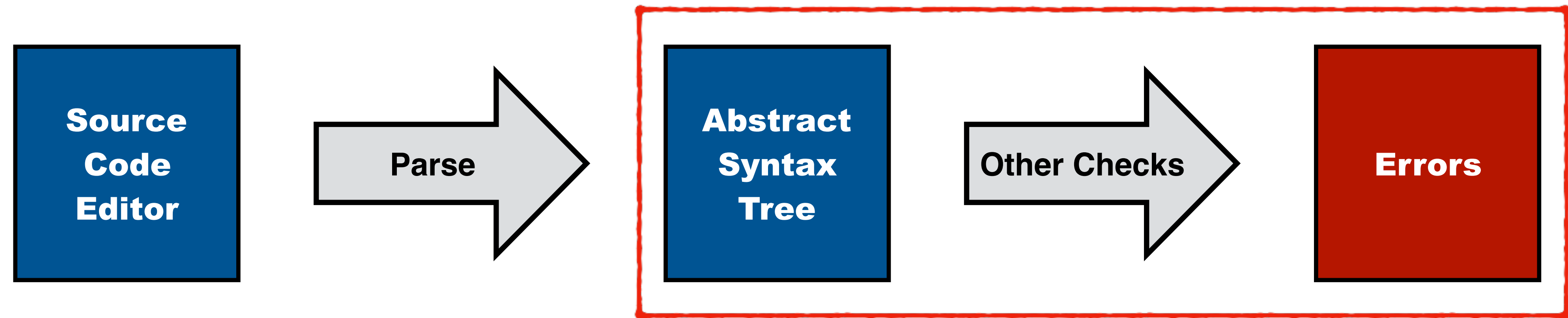
- Static classification of expressions by approximating the runtime values they may produce
- Richer types approximate runtime behavior better
- Richer types may encode correctness properties beyond runtime crashes

### What is the difference between typing and testing?

- Typing is an over-approximation of runtime behavior (proof of absence)
- Testing is an under-approximation of runtime behavior (proof of presence)

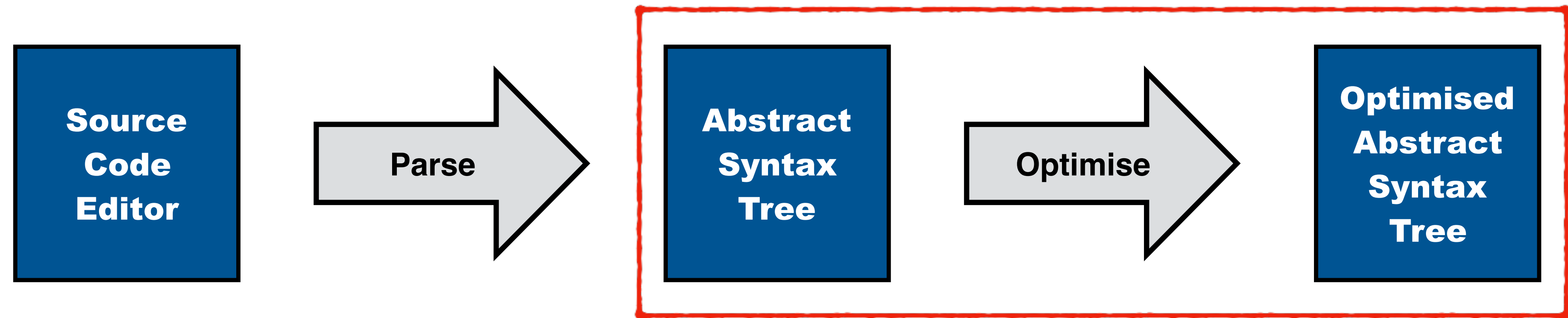
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# This Lecture



Check that variables are initialised, statements are reached, etc.

# This Lecture



Eliminate common subexpressions, reduce loop strength, etc.

# Reading Material

The following papers add background, conceptual exposition, and examples to the material from the slides. Some notation and technical details have been changed; check the documentation.



This paper introduces FlowSpec, the declarative data-flow analysis specification language in Spoofax. Although the design of the language described in this paper is still current, the syntax used is already dated, i.e. the current FlowSpec syntax in Spoofax is slightly different.

SLE 2017

<https://doi.org/10.1145/3136014.3136029>

# FlowSpec: Declarative Dataflow Analysis Specification

Jeff Smits  
TU Delft  
The Netherlands  
j.smits-1@tudelft.nl

Eelco Visser  
TU Delft  
The Netherlands  
e.visser@tudelft.nl

## Abstract

We present FlowSpec, a declarative specification language for the domain of dataflow analysis. FlowSpec has declarative support for the specification of control flow graphs of programming languages, and dataflow analyses on these control flow graphs. We define the formal semantics of FlowSpec, which is rooted in Monotone Frameworks. We also discuss implementation techniques for the language, partly used in the prototype implementation built in the Spoofax Language Workbench. Finally, we evaluate the expressiveness and conciseness of the language with two case studies. These case studies are analyses for Green-Marl, an industrial, domain-specific language for graph processing. The first case study is a classical dataflow analysis, scaled to this full language. The second case study is a domain-specific analysis of Green-Marl.

CCS Concepts • Software and its engineering → Domain specific languages;

Keywords control flow graph, dataflow analysis

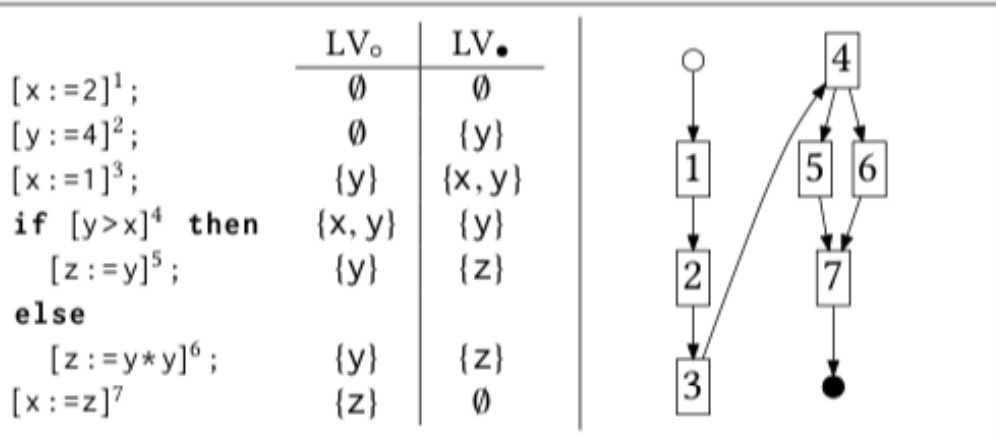
## ACM Reference Format:

Jeff Smits and Eelco Visser. 2017. FlowSpec: Declarative Dataflow Analysis Specification. In *Proceedings of 2017 ACM SIGPLAN International Conference on Software Language Engineering (SLE’17)*. ACM, New York, NY, USA, 11 pages. <https://doi.org/10.1145/3136014.3136029>

## 1 Introduction

Dataflow analysis is a static analysis that answers questions on what *may* or *must* happen before or after a certain point in a program’s execution. With dataflow analysis we can answer whether a value written to a variable *here* may be

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ACM ISBN 978-1-4503-5525-4/17/10...\$15.00  
<https://doi.org/10.1145/3136014.3136029>



**Figure 1.** Classical dataflow analysis Live Variables (LV). On the left is an example program in the WHILE language, with added brackets to number program fragments. On the right is the control flow graph (CFG) of the program. In the centre is the analysis result. The LV<sub>0</sub> and LV<sub>1</sub> are before and after the CFG node’s variables accesses respectively.

read *later*. Such dataflow analyses can be used to inform optimisations.

For example, consider Live Variables analysis, illustrated in Figure 1. This type of dataflow analysis can identify dead code, which can be removed as an optimisation. In the example this would be statement 1 since it writes x which is overwritten by statement 3 without being read in between. The Live Variables analysis provides a set of variables which are read before being written after each statement in LV<sub>1</sub>. The figure shows this in the LV<sub>1</sub> set of statement 1, which does not contain x.

Dataflow may also be part of a language’s static semantics. For example, in Java a final field in a class must be initialised by the end of construction of an object of that class. Since constructor code can have conditional control flow, a dataflow analysis is necessary to check that all possible execution paths through constructors actually assign a value to the final field [Gosling et al. 2005, sect. 16.9].

Dataflow analyses are often operationally encoded, whether in a general purpose language, an attribute grammar system or a logic programming language. This encoding is both an overhead for the engineer implementing it, as well as an overhead in decoding for anyone who wishes to understand the analysis.

In formal, mathematical descriptions of a dataflow analysis, the common patterns are often factored out. This shows commonalities between different analyses, allows the study of those commonalities and differences, as well as general



Documentation for FlowSpec  
at the [metaborg.org](http://metaborg.org) website.

<http://www.metaborg.org/en/latest/source/langdev/meta/lang/flowspec/index.html>

The screenshot shows the Spoofax website with a blue header. The header contains a home icon, the text "Spoofax", and "latest". Below the header is a white search bar with the text "Search docs". The main content area has a white background. It starts with a list of links: "The Spoofax Language Workbench", "Examples", and "Publications". This is followed by a blue section header "TUTORIALS". Under "TUTORIALS" are links for "Installing Spoofax", "Creating a Language Project", "Using the API", and "Getting Support". Next is another blue section header "REFERENCE MANUAL". Under "REFERENCE MANUAL" are links for "Language Definition with Spoofax", "Abstract Syntax with ATerms", "Syntax Definition with SDF3", and "Static Semantics with NaBL2". Below this is a blue section header "Data-Flow Analysis with FlowSpec". Under "Data-Flow Analysis with FlowSpec" is a numbered list: "1. Introduction", "2. Language Reference", "3. Stratego API", "4. Configuration", "5. Examples (under construction)", and "6. Bibliography". Below the numbered list are links for "Transformation with Stratego", "Dynamic Semantics with DynSem", "Editor Services with ESV", and "Language Testing with SPT". At the bottom of the screenshot, a white box contains the text "spec/index.html". To the right of this box, the text "Command-" is visible. At the very bottom of the screenshot, a green bar contains a document icon, the text "Read the Docs", and "v: latest" with a dropdown arrow.

[Docs](#) » Data Flow Analysis Definition with FlowSpec

[Edit on GitHub](#)

# Data Flow Analysis Definition with FlowSpec

Programs that are syntactically well-formed are not necessarily valid programs. Programming languages typically impose additional *context-sensitive* requirements on programs that cannot be captured in a syntax definition. Languages use data and control flow to check certain extra properties that fall outside of names and type systems. The FlowSpec ‘Flow Analysis Specification Language’ supports the specification of rules to define the static control flow of a language, and data flow analysis over that control flow. FlowSpec supports flow-sensitive intra-procedural data flow analysis.

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  - 3.4. Hover text
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  - 4.1. Prepare your project
  - 4.2. Inspecting analysis results



# Control-Flow

# Control-Flow

## What is Control-Flow?

- “Order of evaluation”

## Discuss a series of example programs

- What is the control flow?
- What constructs in the program determine that?

# What is Control-Flow?

```
function id(x) { return x; }  
id(4); id(true);
```

Function calls

- Calling a function passes control to that function
- A **return** passes control back to the caller

# What is Control-Flow?

```
if (c) { a = 5 } else { a = "four" }
```

Branching

- Control is passed to one of the two branches
- This is dependent on the value of the condition



# What is Control-Flow?

```
while (c) { a = 5 }
```

Looping

- Control is passed to the loop body depending on the condition
- After the body we start over

# What is Control-Flow?

```
function1(a);  
function2(b);
```

Sequence

- No conditions or anything complicated
- But still order of execution

# What is Control-Flow?

```
distance = distance + 1;
```

Reads and Writes

- The expression needs to be evaluated, before we can save its result

# What is Control-Flow?

```
int i = 2;  
int j = (i=3) * i;
```

Expressions & side-effects

- Order in sub-expressions is usually undefined
- Side-effects make sub-expression order relevant



# Kinds of Control-Flow

- Sequential statements
- Conditional if / switch / case
- Looping while / do while / for / foreach / loop
- Exceptions throw / try / catch / finally
- Continuations call/cc
- Async-await threading
- Coroutines / Generators yield
- Dispatch function calls / method calls
- Loop jumps break / continue
- ... many more ...

# Why Control-Flow?

## Shorter code

- No need to repeat the same statement 10 times

## Parametric code

- Extract reusable patterns
- Let user decide repetition amount

## Expressive power

- Playing with Turing Machines

## Reason about program execution

- What happens when?
- In what order?

# Control-Flow and Language Design

## Imperative programming

- Explicit control-flow constructs

## Declarative programming

- What, not how
- Less explicit control-flow
- More options for compilers to choose order
- Great if your compiler is often smarter than the programmer

# Separation of Concerns in Data-Flow Analysis

## Representation

- Represent control-flow of a program
- Conduct and represent results of data-flow analysis

## Declarative Rules

- To define control-flow of a language
- To define data-flow of a language

## Language-Independent Tooling

- Data-Flow Analysis
- Errors/Warnings
- Code completion
- Refactoring
- Optimisation
- ...



# Control-Flow Graphs

# What is a Control-Flow Graph?

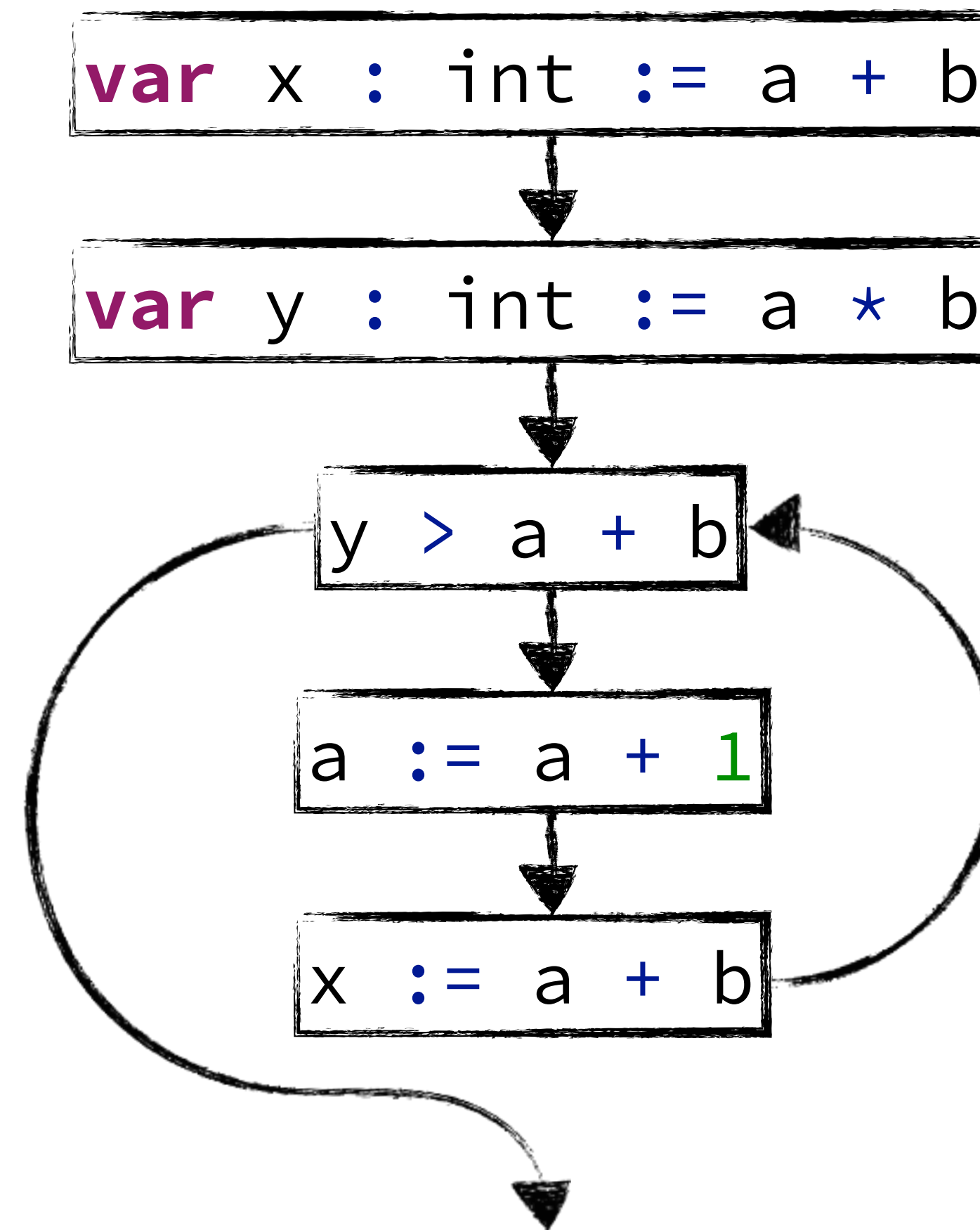
A **control flow graph (CFG)** in computer science is a representation, using graph notation, of all paths that might be traversed through a program during its execution.

[https://en.wikipedia.org/wiki/Control\\_flow\\_graph](https://en.wikipedia.org/wiki/Control_flow_graph)

# Control-Flow Graph Example

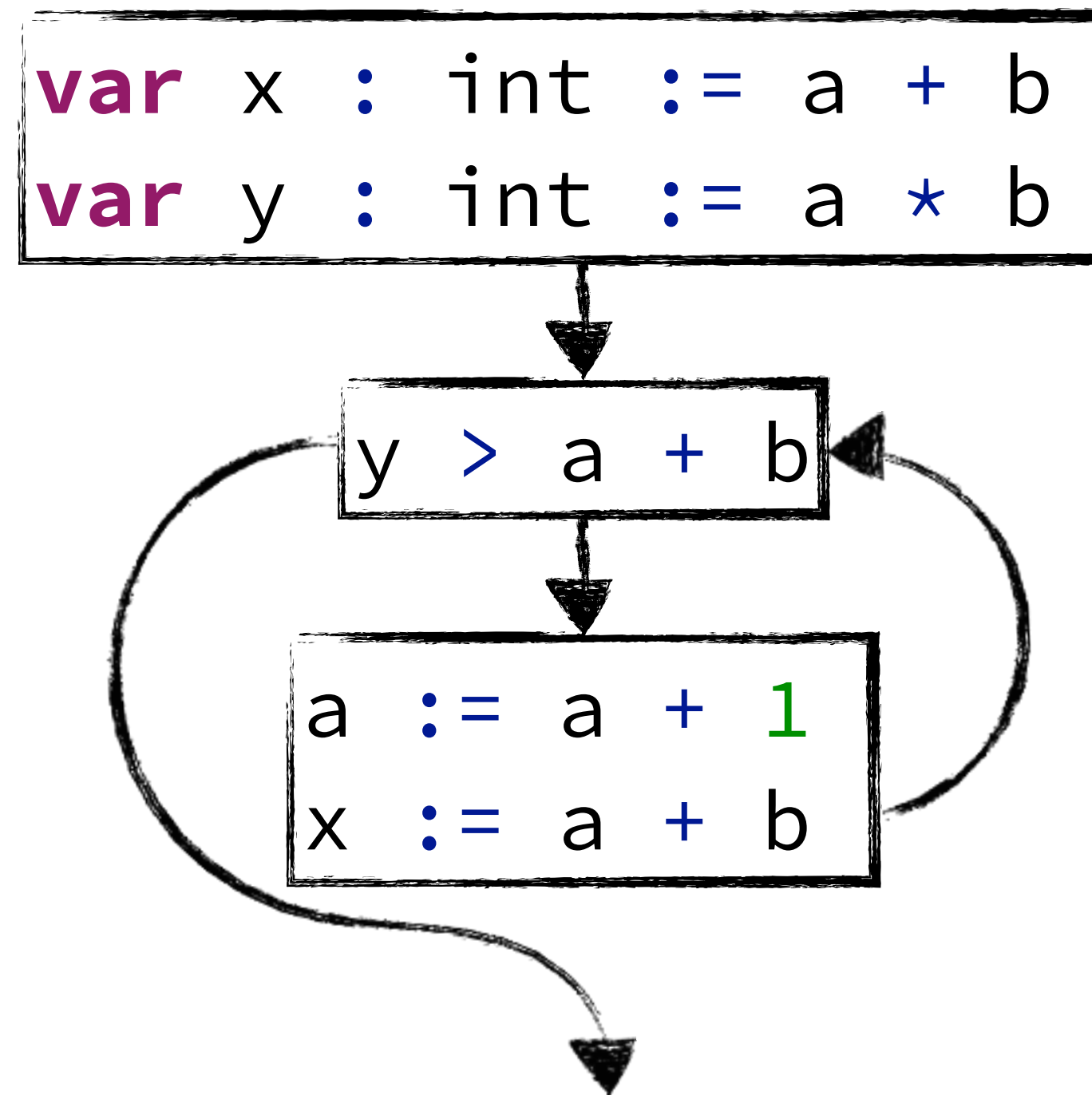
```
let
  var x : int := a + b
  var y : int := a * b
in
  while y > a + b do
    (
      a := a + 1;
      x := a + b
    )
end
```

# Control-Flow Graph Example





# Basic Blocks



# Control Flow Graphs

## Nodes

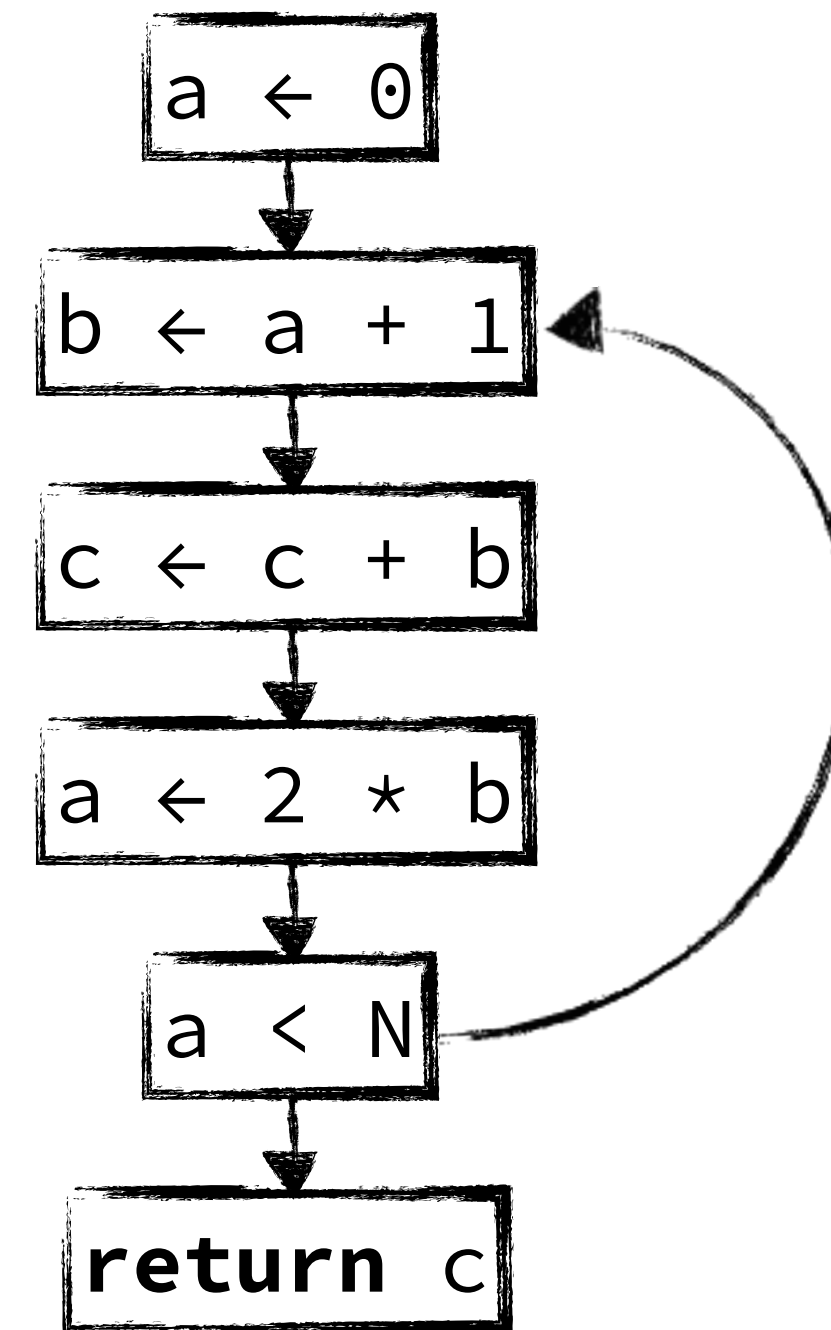
- Usually innermost statements and expressions
- Or blocks for consecutive statements (basic blocks)

## Edges

- Back edges: show loops
- Splits: conditionally split the control flow
- Merges: combine previously split control flow

# Equivalent to Unstructured Control-Flow

```
    a ← 0  
L1: b ← a + 1  
    c ← c + b  
    a ← 2 * b  
    if a < N goto L1  
    return c
```



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# Separation of Concerns in Data-Flow Analysis

## Representation

- **Control Flow Graphs (CFGs)**
- Conduct and represent results of data-flow analysis

## Declarative Rules

- To define control-flow of a language
- To define data-flow of a language

## Language-Independent Tooling

- Data-Flow Analysis
- Errors/Warnings
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- ...

# Data-Flow



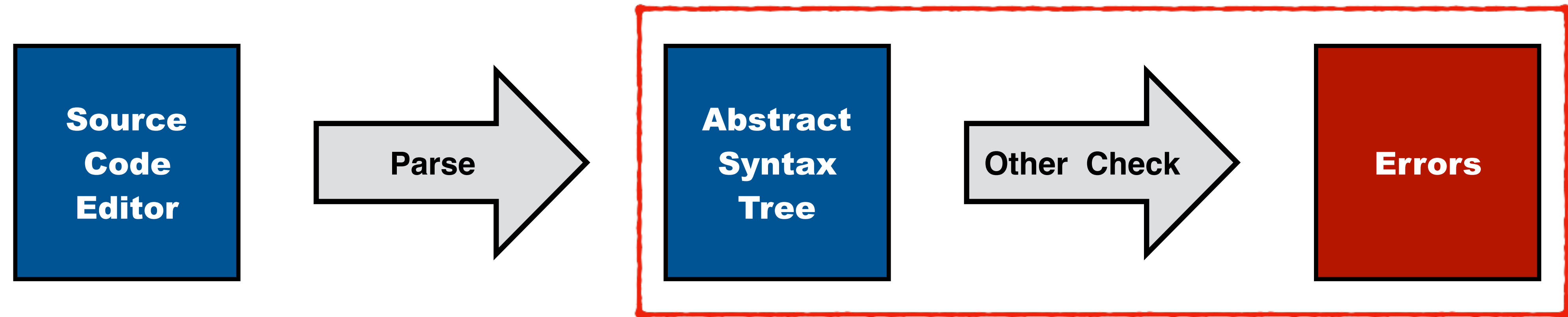
# Data-Flow

## What is Data-Flow?

- Possible values (data) that flow through the program
- Relations between those data (data dependence)

## Discuss a series of example programs

- What is wrong or can be optimised?
- What is the flow we can use for this?



Check that code is reachable or observable

# What is wrong here?

```
public int ComputeFac(int num) {  
    return num;  
    int num_aux;  
    if (num < 1)  
        num_aux = 1;  
    else  
        num_aux = num * this.ComputeFac(num-1);  
    return num_aux;  
}
```

Dead code (control-flow)

- Most of the code is never reached because of the early return
- This is usually considered an error by compilers

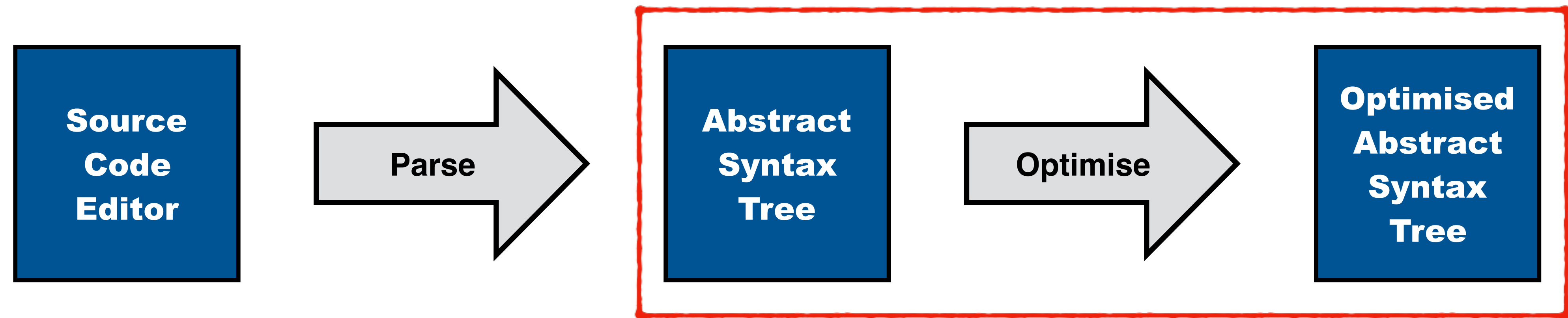
# What is “wrong” here?

```
x := 2;  
y := 4;  
x := 1;  
// x and y used later
```

Dead code (data-flow)

Live variable analysis

- The first value of x is never observed
- This is sometimes warned about by compilers



Eliminate common subexpressions, reduce loop strength, etc.

# What is suboptimal here?

```
let
  var x : int := a + b
  var y : int := a * b
in
  if y > a + b then
    (
      a := a + 1;
      x := a + b
    )
end
```

Common subexpression elimination

Available expression analysis

- a + b is already computed when you get to the condition
- There is no need to compute it again

# What is suboptimal here?

```
let
  var x : int := a + b
  var y : int := a * b
in
  while y > a + b do
    (
      a := a + 1;
      x := a + b
    )
  end
```

# What is suboptimal here?

```
for i := 1 to 100 do  
(  
  x[i] := y[i];  
  if w > 0 then  
    y[i] := 0  
)
```

Loop unswitching

Data-dependence analysis

- The if condition is not dependent on i, x or y
- Still it is checked in the loop, which is slowing the loop



# Separation of Concerns in Data-Flow Analysis

## Representation

- **Control Flow Graphs (CFGs)**
- Conduct and represent results of data-flow analysis

## Declarative Rules

- To define control-flow of a language
- To define data-flow of a language

## Language-Independent Tooling

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- ...

# Separation of Concerns in Data-Flow Analysis

## Representation

- Control Flow Graphs (CFGs)
- Data-flow information on CFG nodes

## Declarative Rules

- To define control-flow of a language
- To define data-flow of a language

## Language-Independent Tooling

- Data-Flow Analysis
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# Separation of Concerns in Data-Flow Analysis

## Representation

- Control Flow Graphs (CFGs)
- Data-flow information on CFG nodes

## Declarative Rules

- A domain-specific meta-language for Spoofax: FlowSpec

## Language-Independent Tooling

- Data-Flow Analysis
- Errors/Warnings
- Code completion
- Refactoring
- Optimisation
- ...

# Tiger in FlowSpec

# Control-Flow Rules

## Map abstract syntax to control-flow (sub)graphs

- Match an AST pattern
- List all CFG edges of that AST
- Mark subtrees as CFG nodes
- Or splice in their control-flow subgraph
- Use special “context” nodes to connect a subgraph to the outside graph

# Control-Flow Graphs in FlowSpec

*FlowSpec*

```
root Mod(s) =  
  start -> s -> end
```

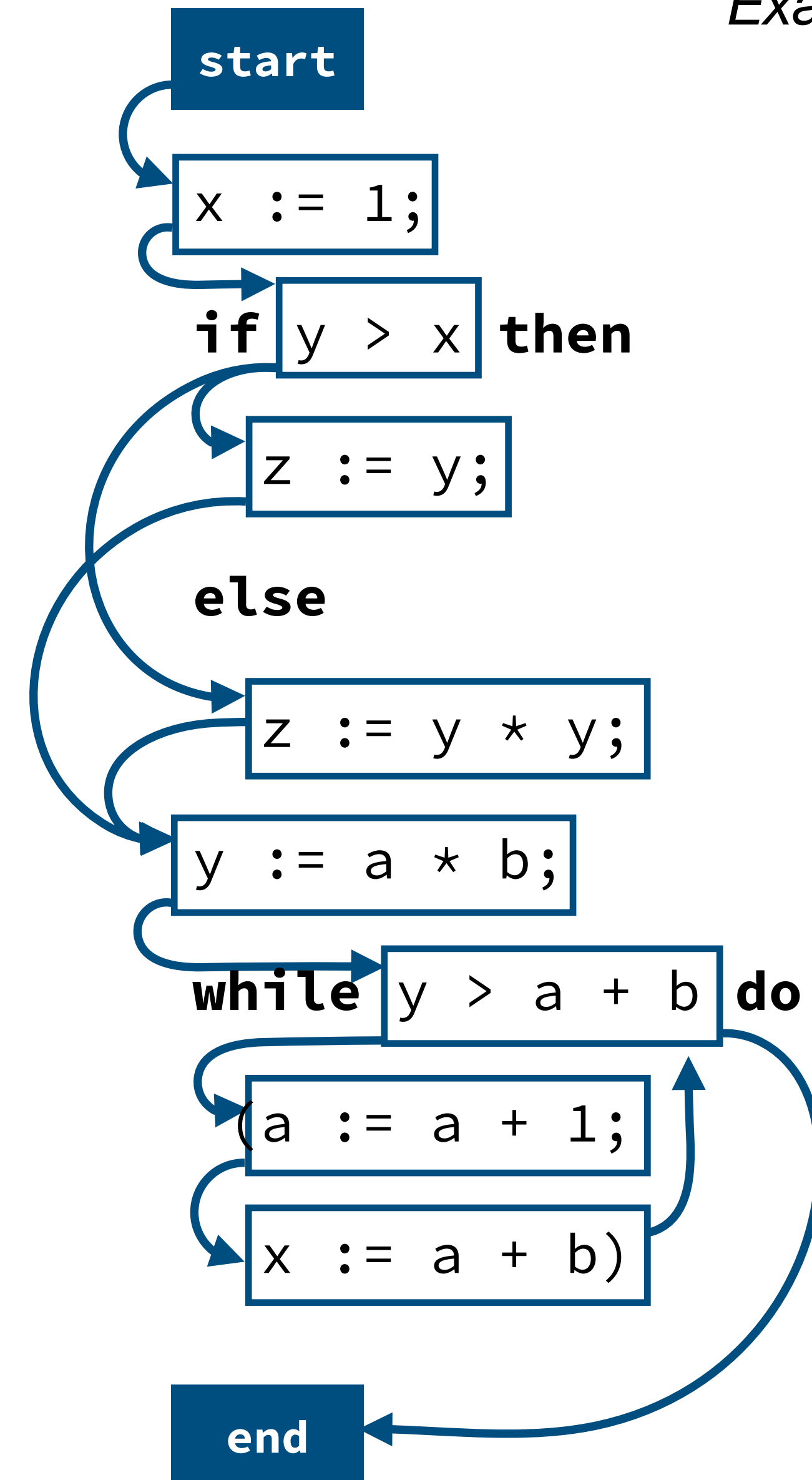
```
node Assign(_, _)
```

```
Seq(s1, s2) =  
  entry -> s1 -> s2 -> exit
```

```
IfThenElse(c, t, e) =  
  entry -> node c -> t -> exit,  
  node c -> e -> exit
```

```
While(c, b) =  
  entry -> node c -> b -> node c,  
  node c -> exit
```

*Example program*



# Data-Flow Rules

## Define effect of control-flow graph nodes

- Match an AST pattern on one side of a CFG edge
- Propagate the information from the other side of the edge
- Adapt that information as the effect of the matched CFG node

# Live Variables in FlowSpec

A variable is *live* if the current value of the variable *may* be read further along in the program

## properties

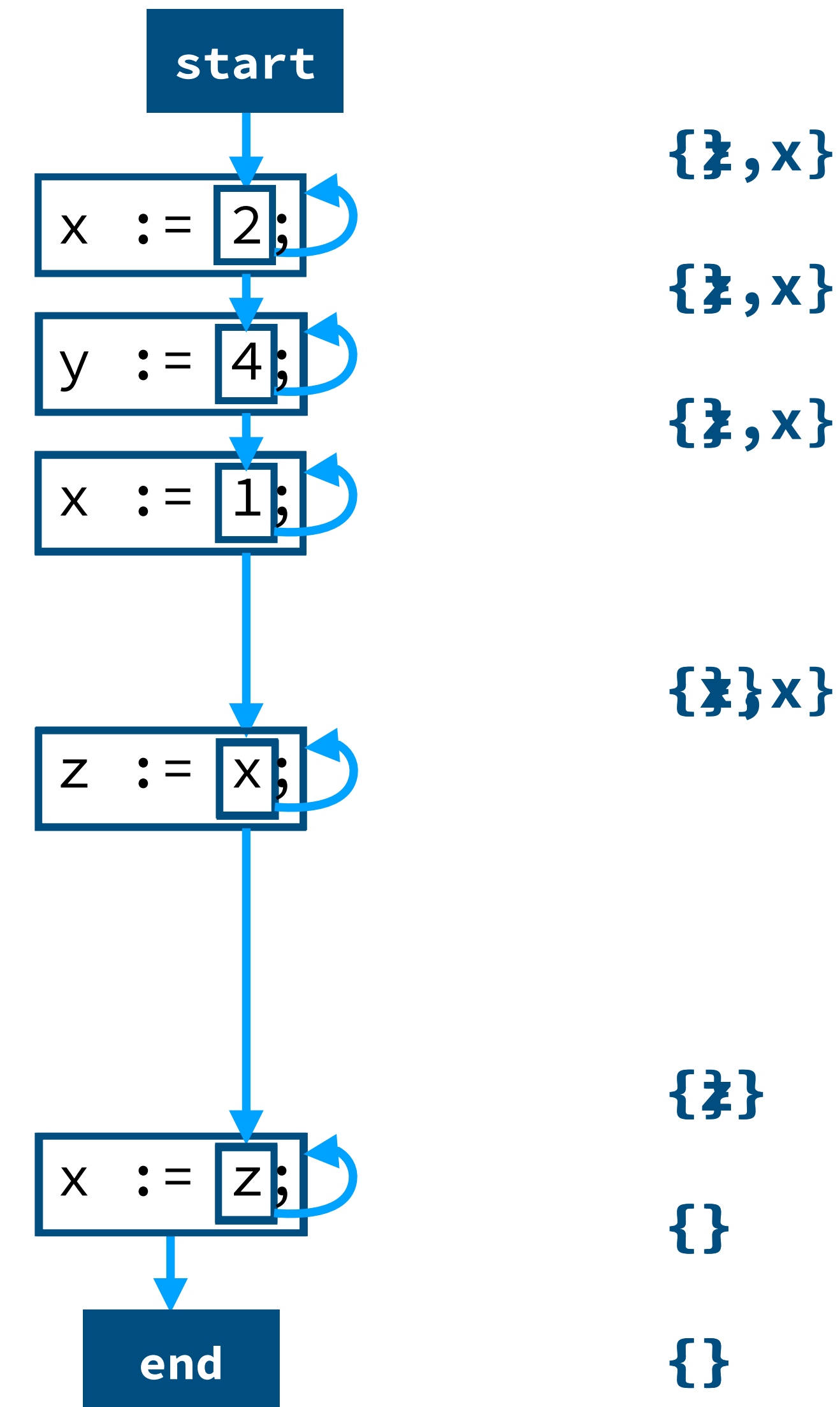
live: Set(name)

## property rules

live(Ref(n) -> next) =  
live(next) \ / { Var{n} }

live(Assign(n, \_) -> next) =  
{ m | m <- live(next), Var{n} != m }

live(\_.end) =  
{ }





# Live Variables in FlowSpec

A variable is *live* if the current value of the variable *may* be read further along in the program

## properties

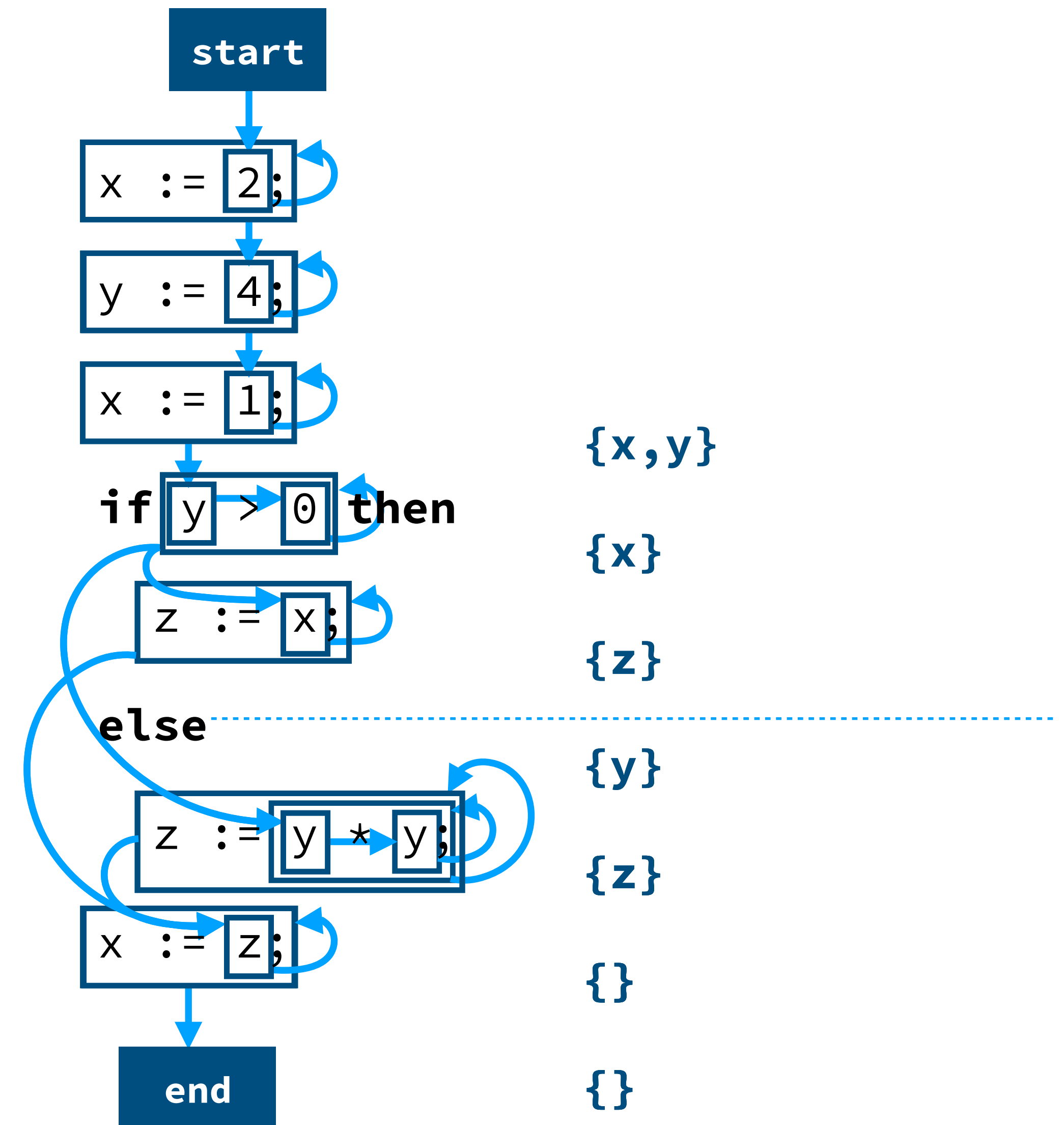
live: Set(name)

## property rules

live(Ref(n) -> next) =  
live(next) \ / {n}

live(Assign(n, \_) -> next) =  
{ m | m <- live(next), n != m }

live(\_.end) =  
{}



# Available Expressions in FlowSpec

An expression is *available* if it *must* have been evaluated previously and its variables not reassigned

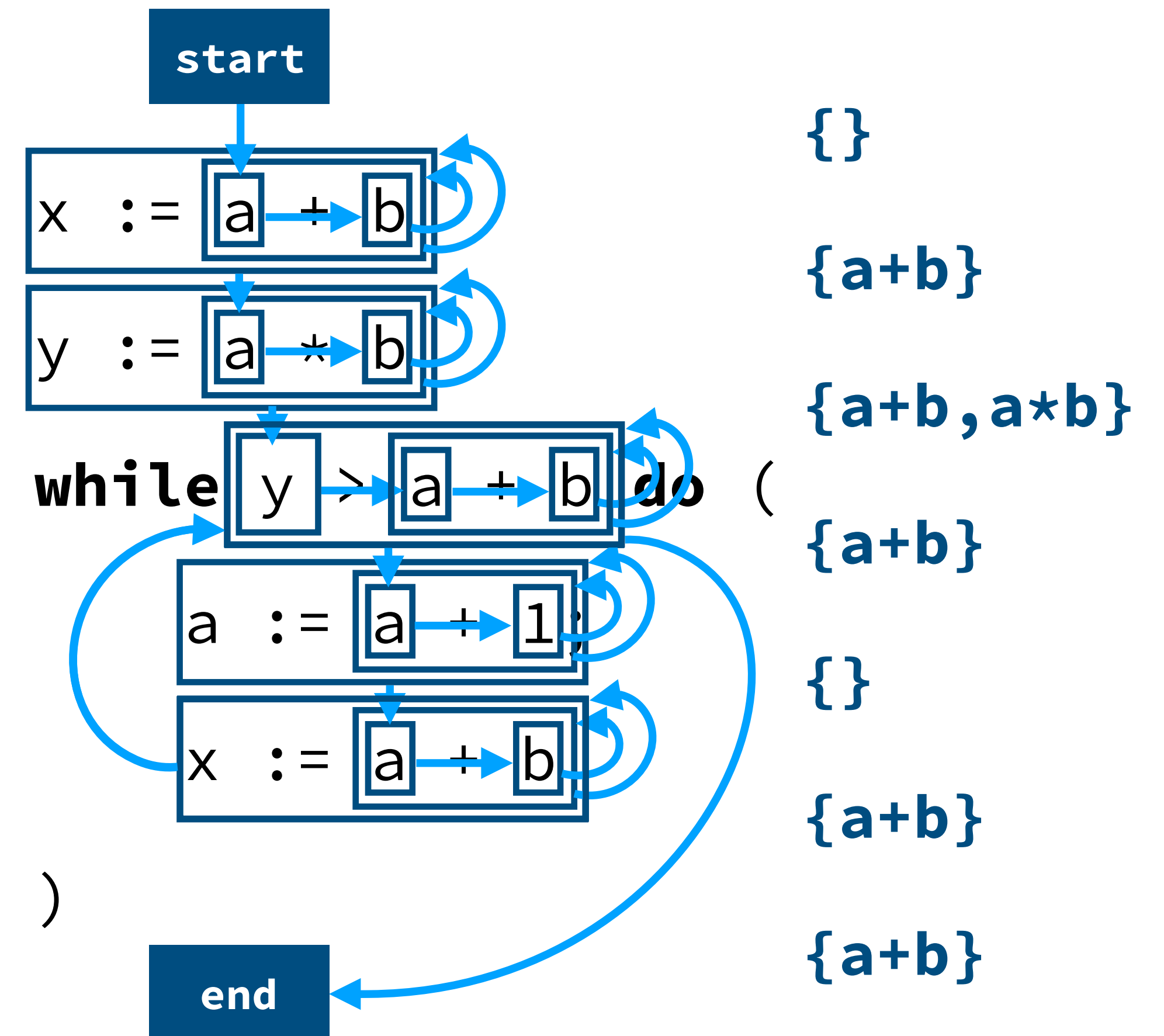
## properties

available: MustSet(**term**)

## property rules

```
available(prev -> Assign(n, e)) =  
  { expr |  
    expr <- available(prev) \ / {e},  
    !(n in reads(expr)) }
```

```
available(_.start) =  
  {}
```



# Conclusion

# Summary

## Control-Flow

- Order of execution
- Reasoning about what is reachable

## Data-Flow

- Flow of data through a program
- Reasoning about data, and dependencies between data

## FlowSpec

- Control-Flow rules to construct the graph
- Annotate with information from analysis by Data-Flow rules

# Next Week

## Monotone Frameworks

- The semantics behind FlowSpec
- A general framework for (intraprocedural, flow-sensitive) data-flow analysis

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