



# Register Allocation

Guido Wachsmuth, Eelco Visser

# Allocate Minimal Number of Registers

## exercise

```
live-in: k j
g := mem[j + 12]
h := k - 1
f := g * h
e := mem[j + 8]
m := mem[j + 16]
b := mem[f]
c := e + 8
d := c
k := m + 4
j := b
live out: d k j
```

# Overview

## today's lecture

### Interference graphs

- construction during liveness analysis

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### Graph Coloring

- assign registers to local variables and compiler temporaries
- store local variables and temporaries in memory

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## today's lecture

### Interference graphs

- construction during liveness analysis

### Graph Coloring

- assign registers to local variables and compiler temporaries
- store local variables and temporaries in memory

### Coalescing

- handle move instructions

# Overview

## today's lecture

### Interference graphs

- construction during liveness analysis

### Graph Coloring

- assign registers to local variables and compiler temporaries
- store local variables and temporaries in memory

### Coalescing

- handle move instructions

### Pre-colored nodes

# I

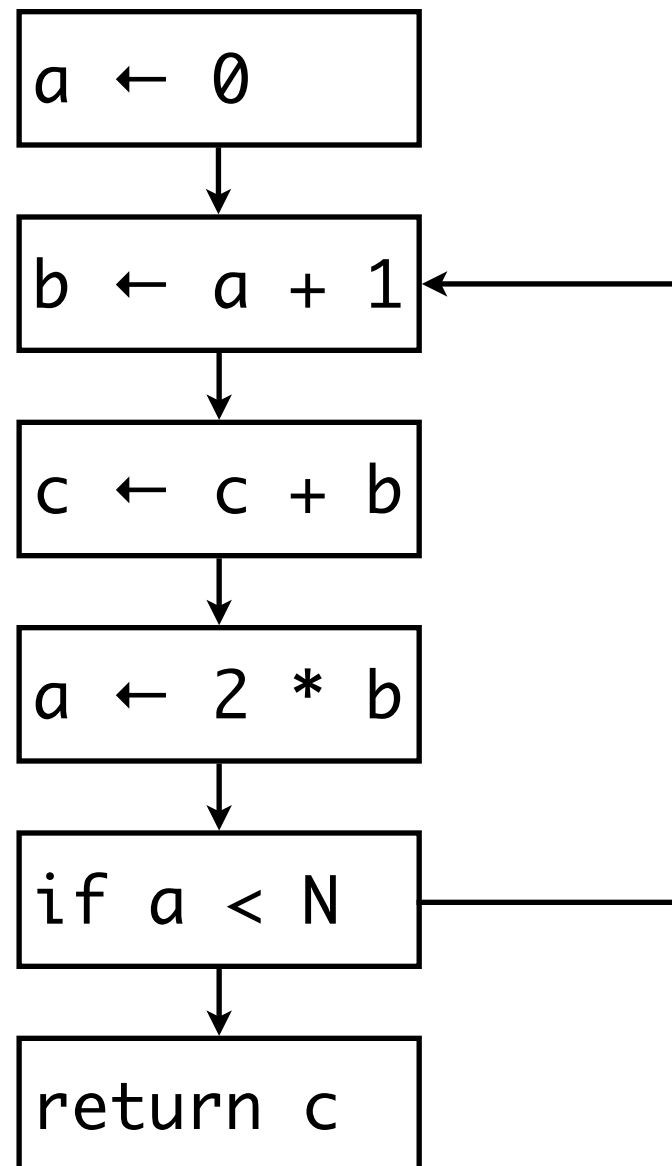
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## Interference Graphs

---

# Recap: Liveness Analysis

## terminology

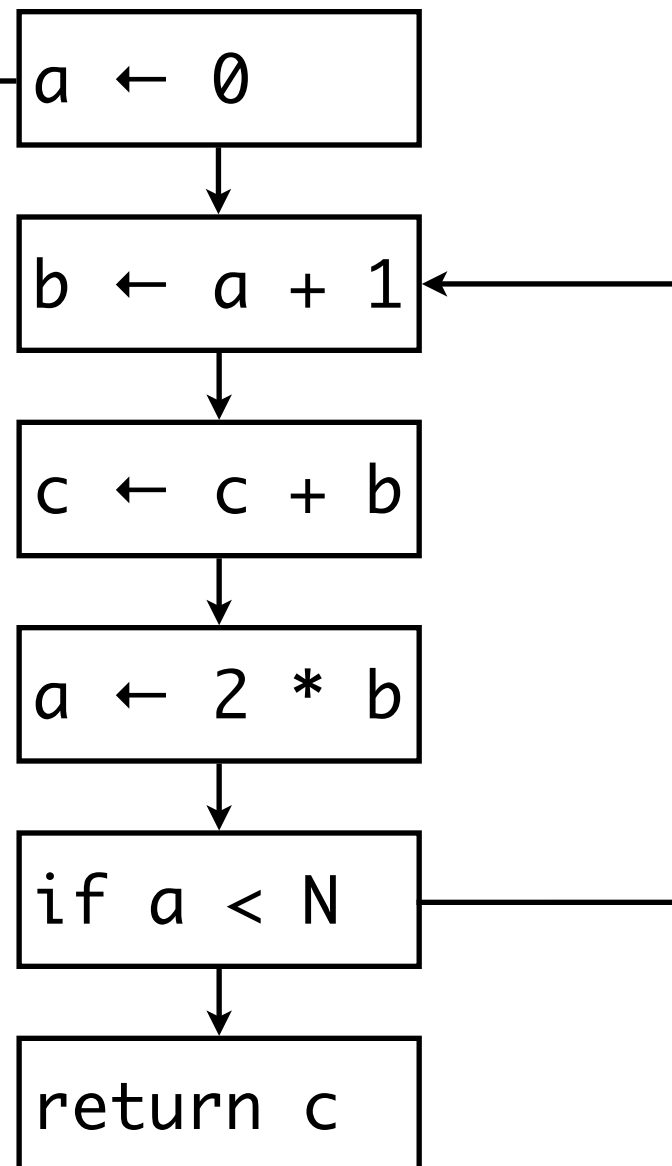




# Recap: Liveness Analysis

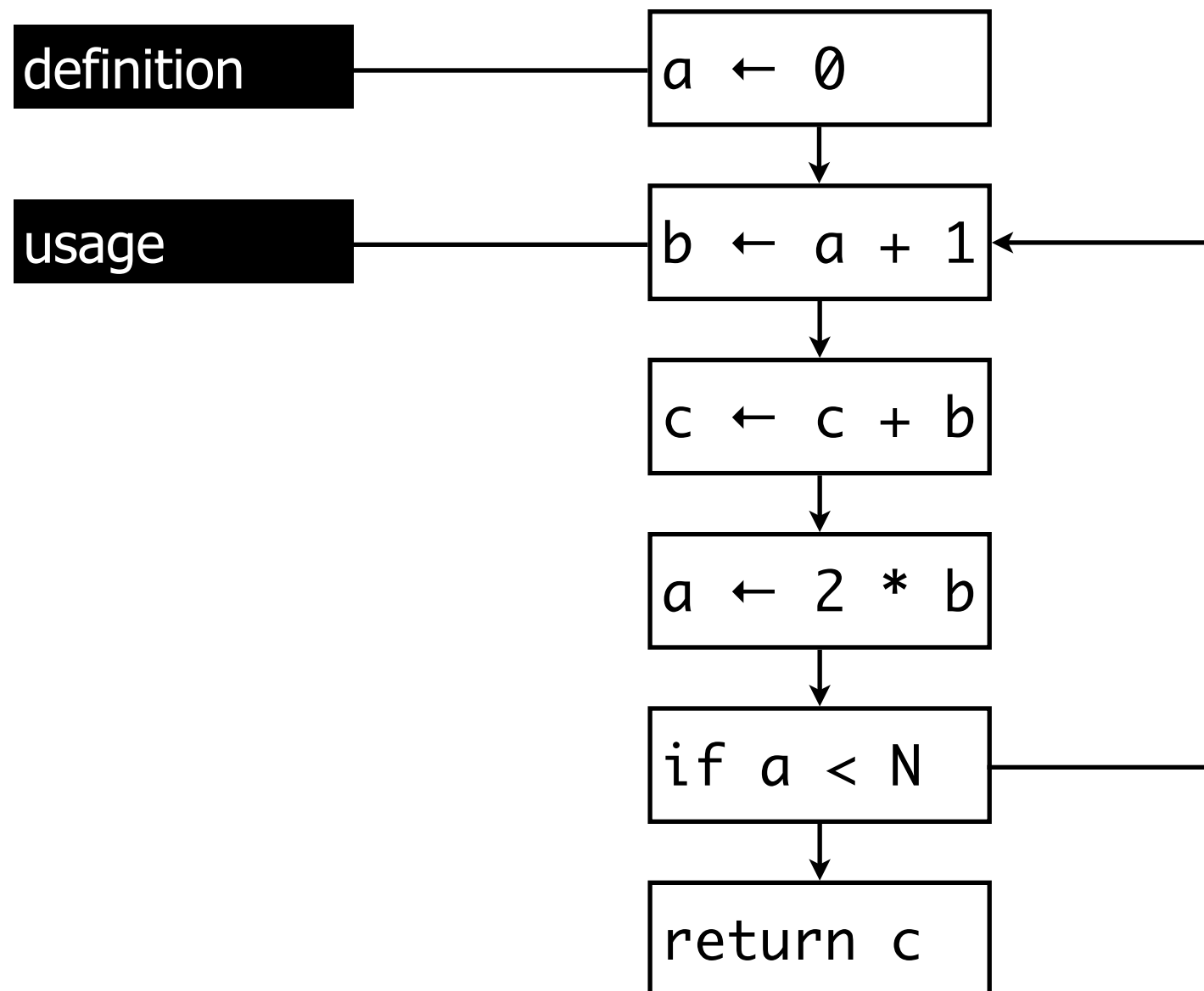
## terminology

definition



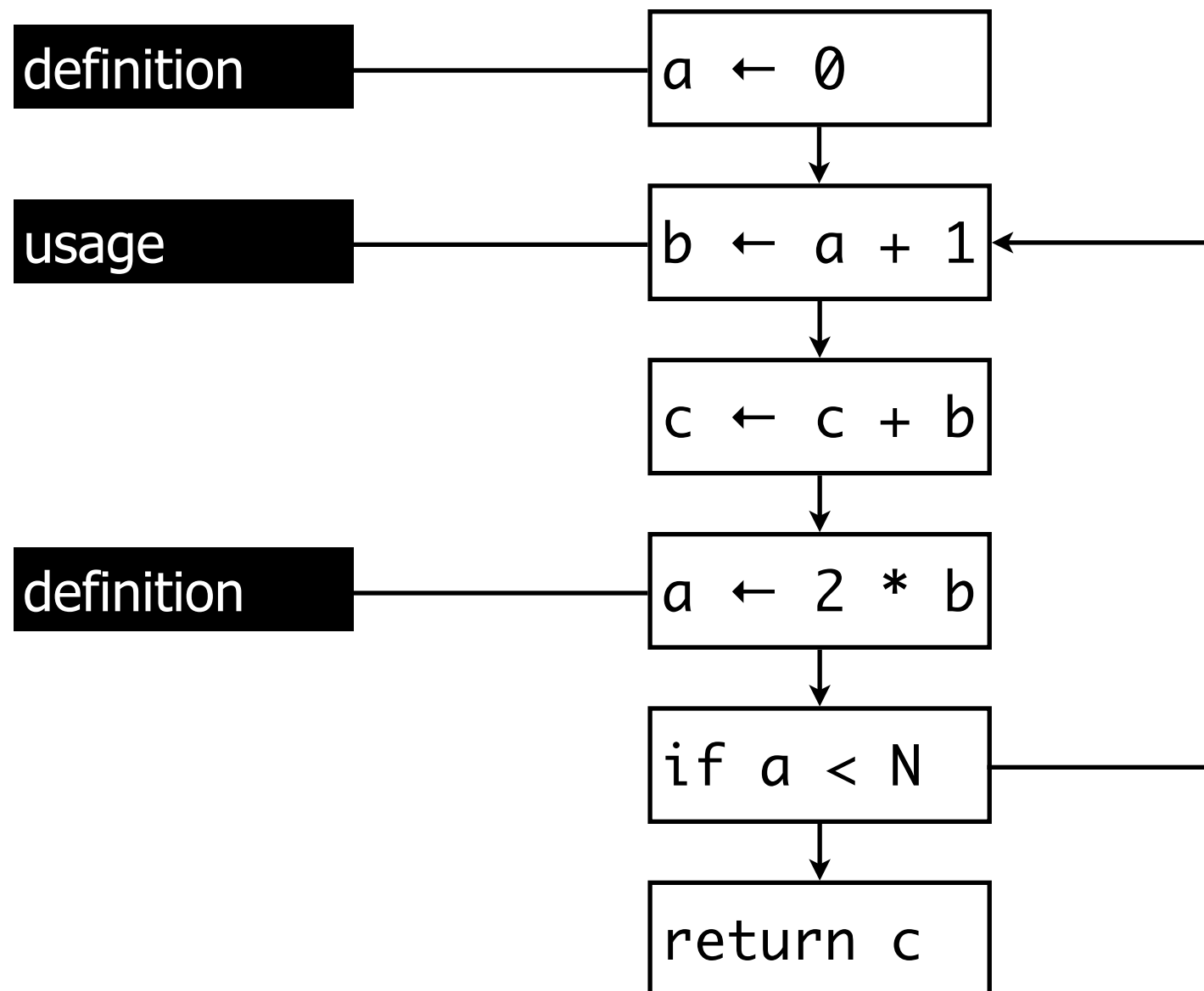
# Recap: Liveness Analysis

## terminology



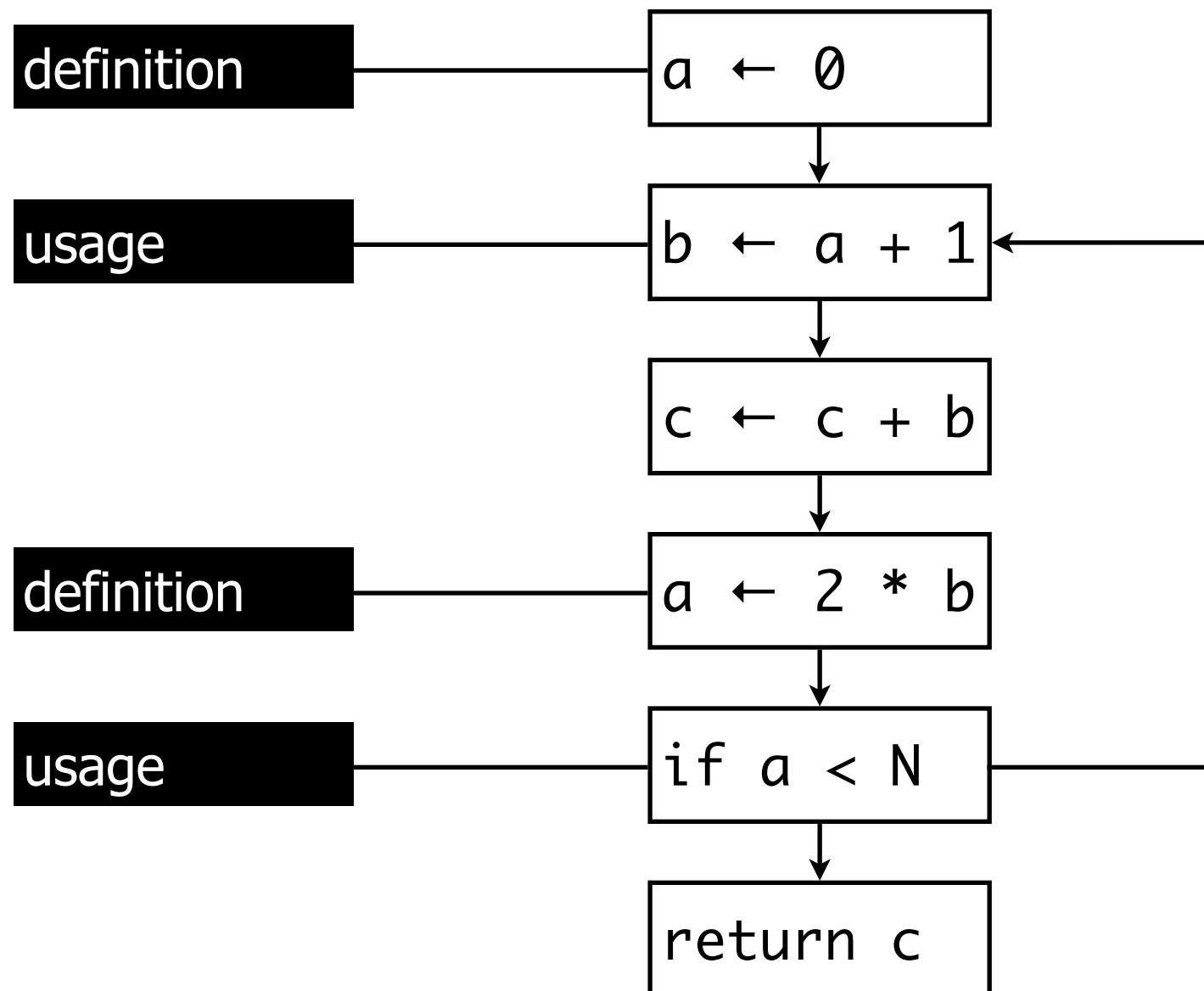
# Recap: Liveness Analysis

## terminology



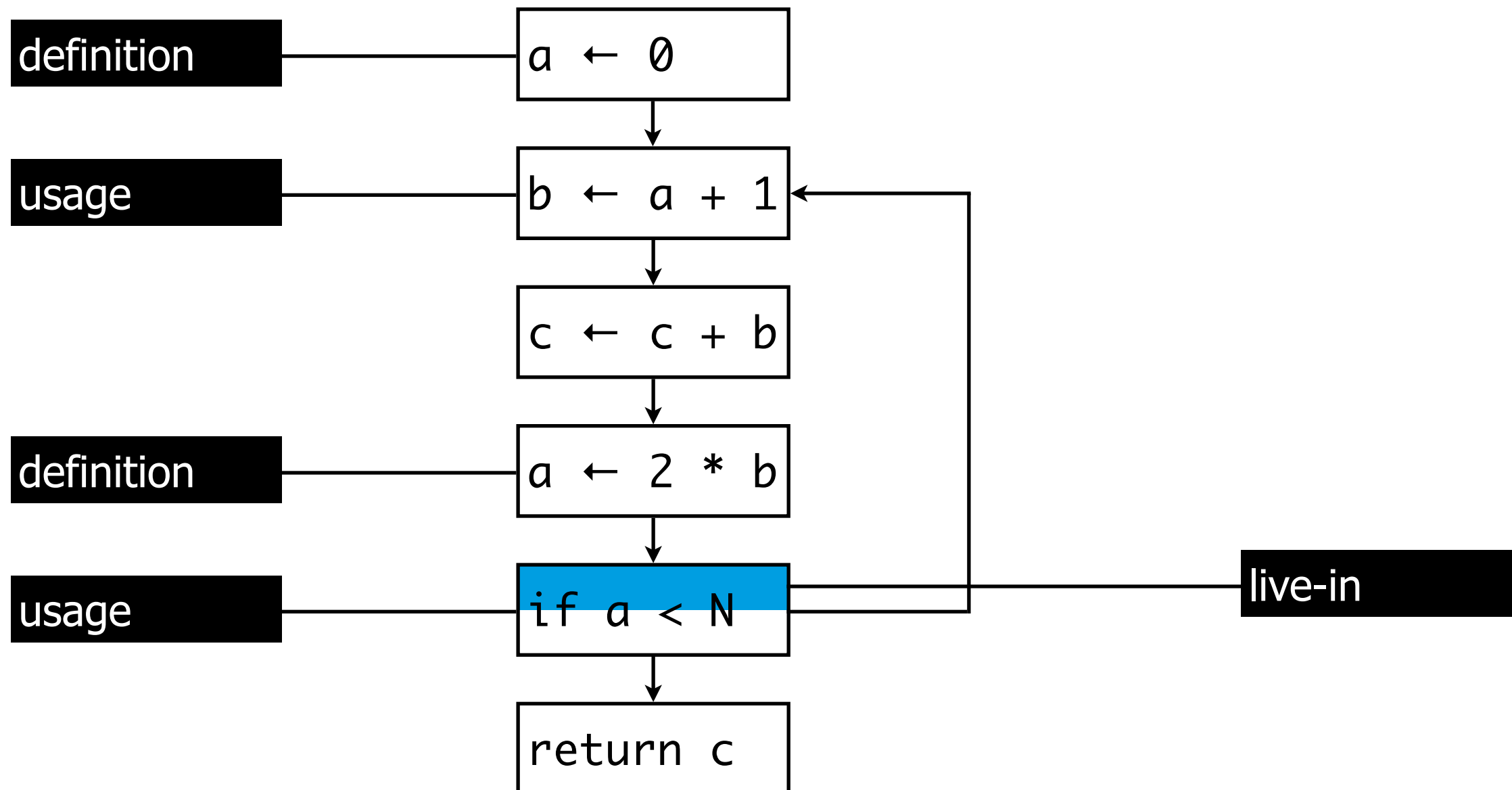
# Recap: Liveness Analysis

## terminology



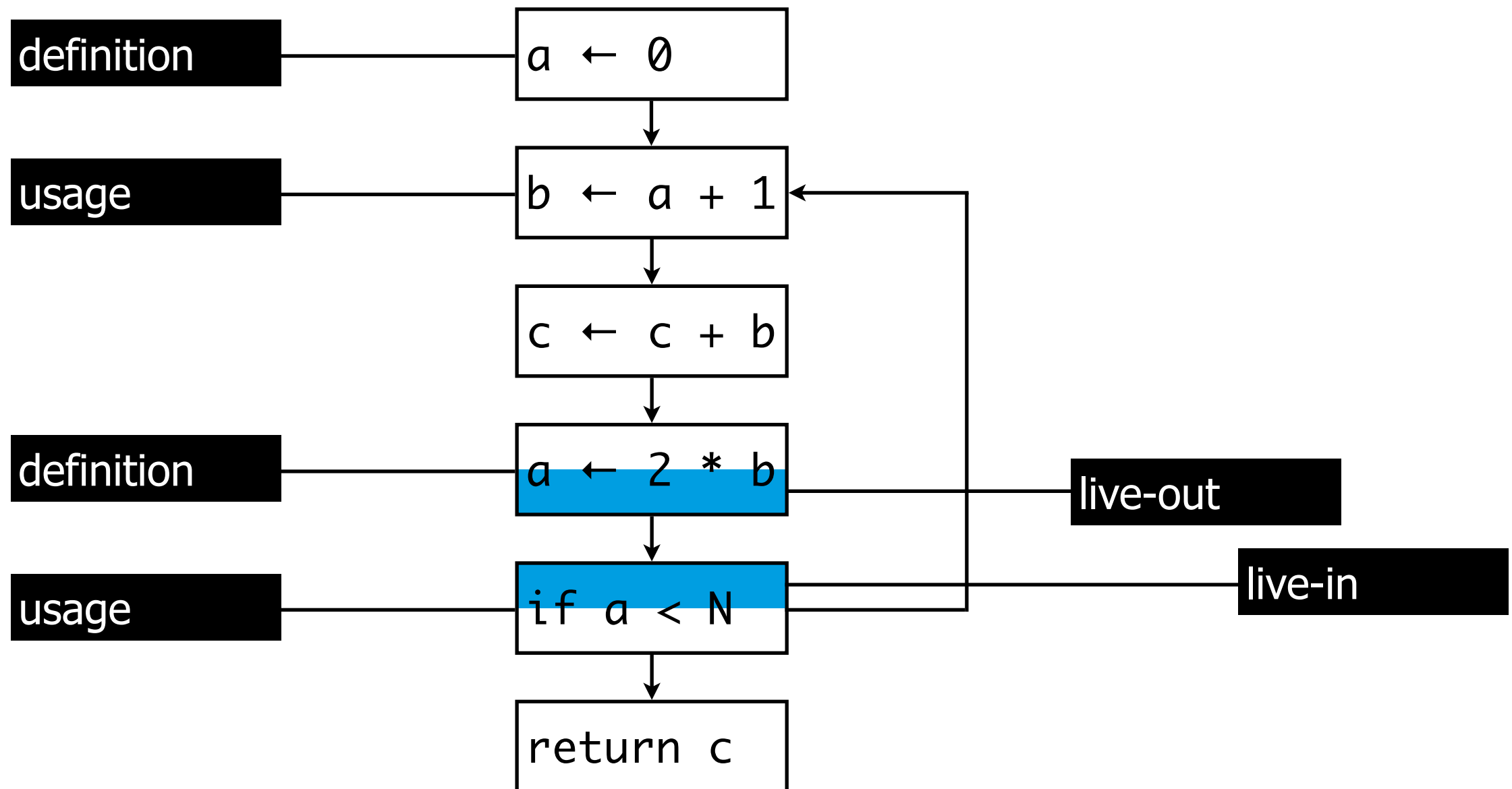
# Recap: Liveness Analysis

## terminology



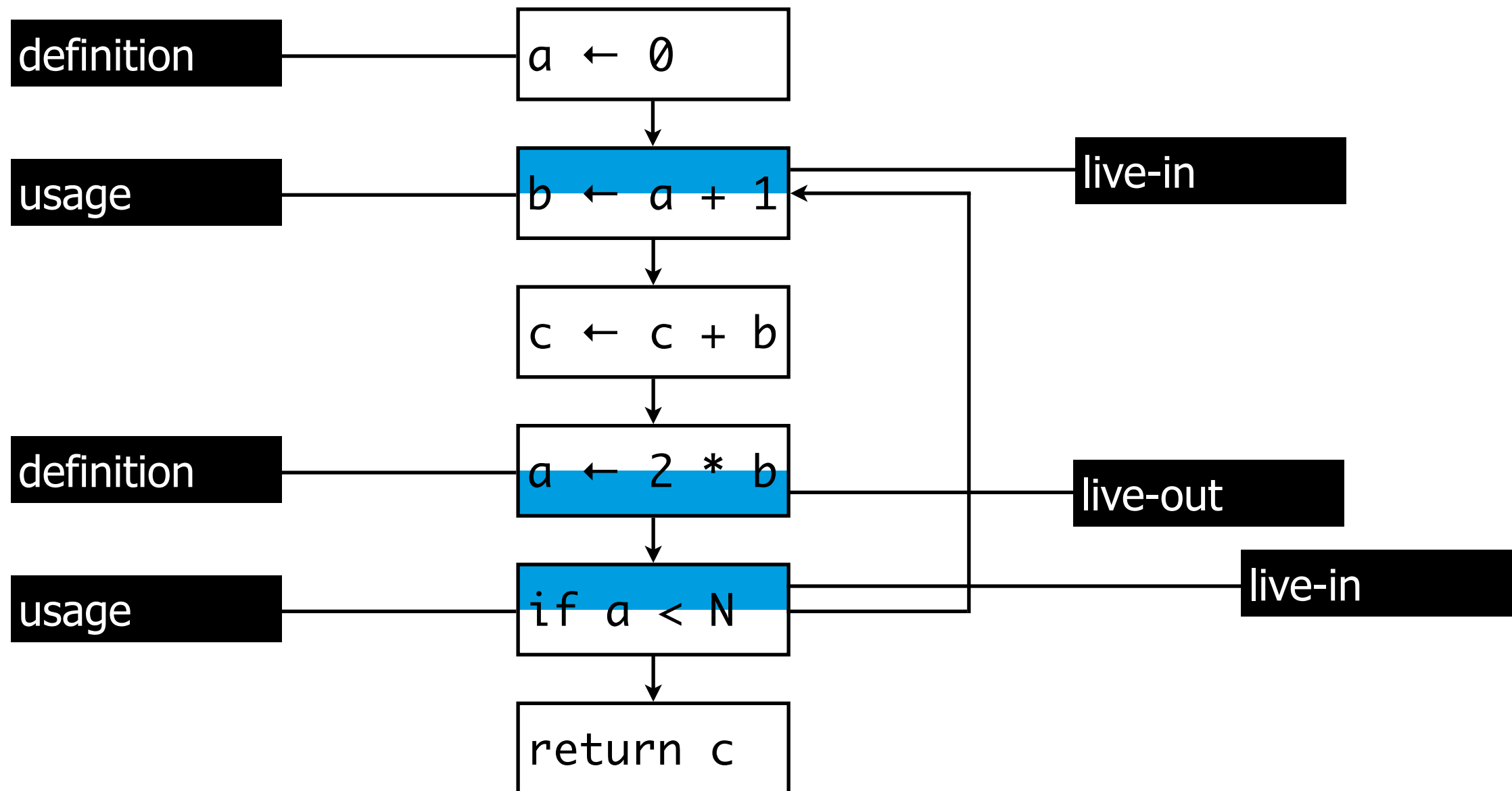
# Recap: Liveness Analysis

## terminology



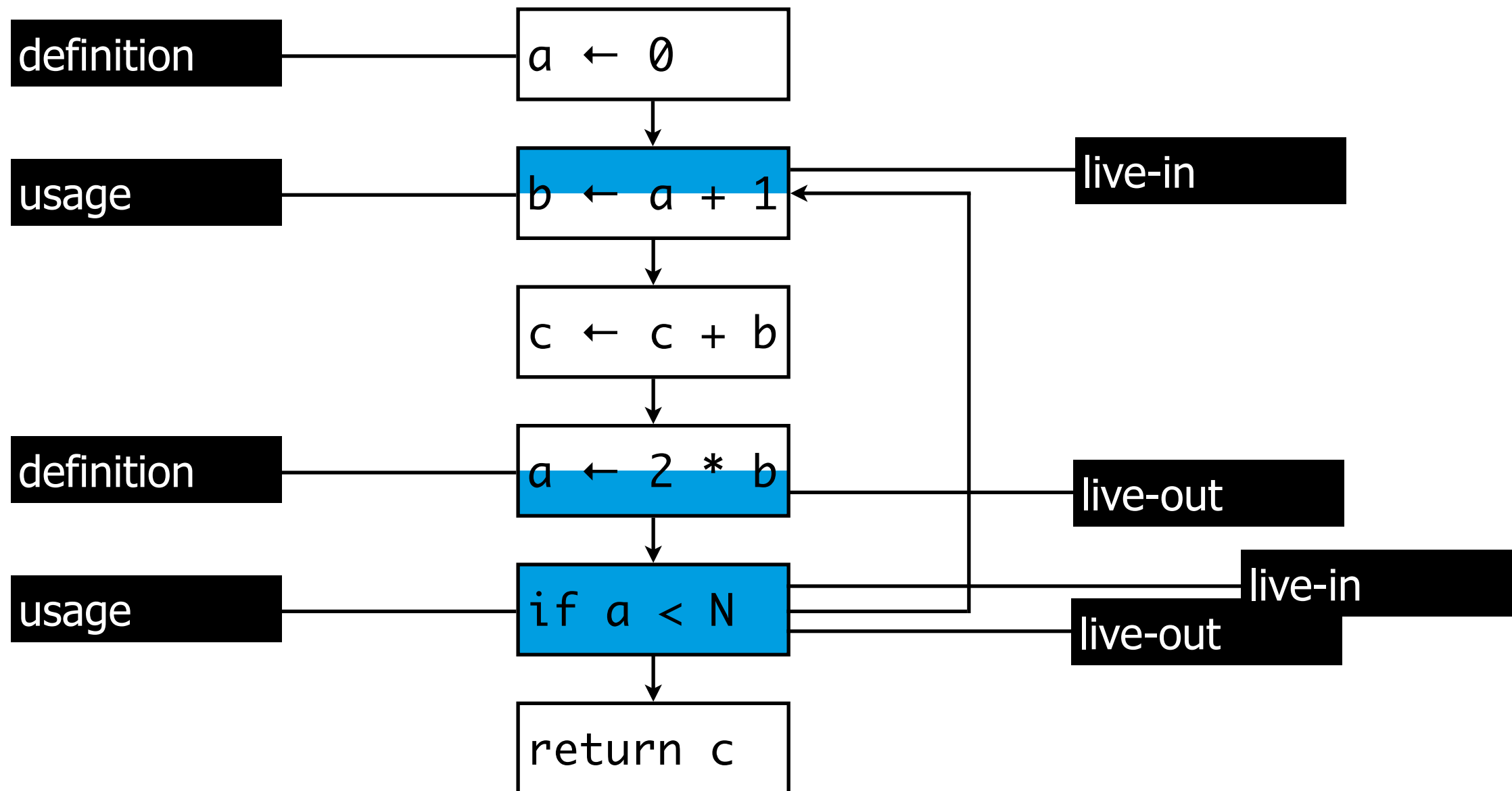
# Recap: Liveness Analysis

## terminology



# Recap: Liveness Analysis

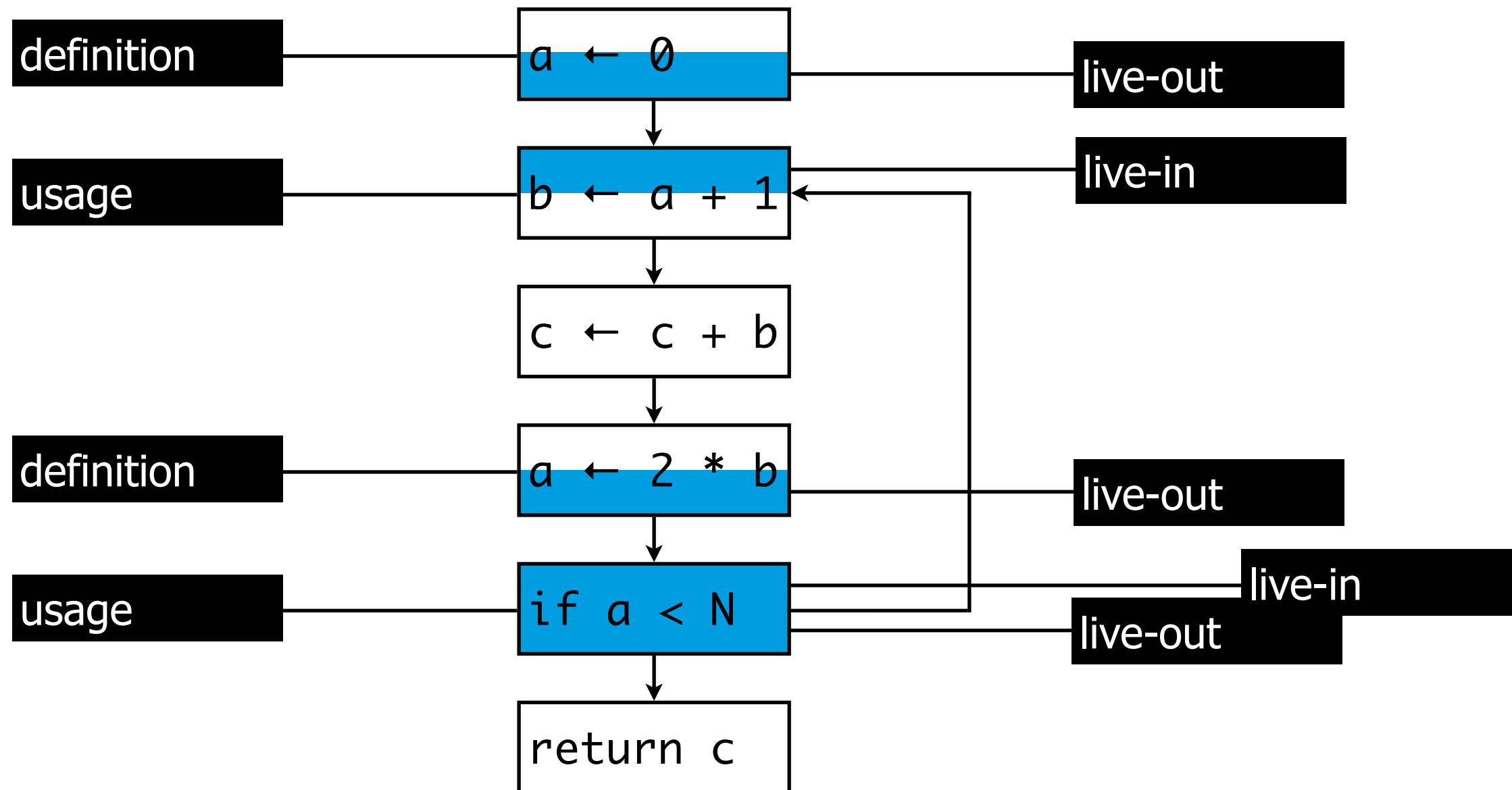
## terminology





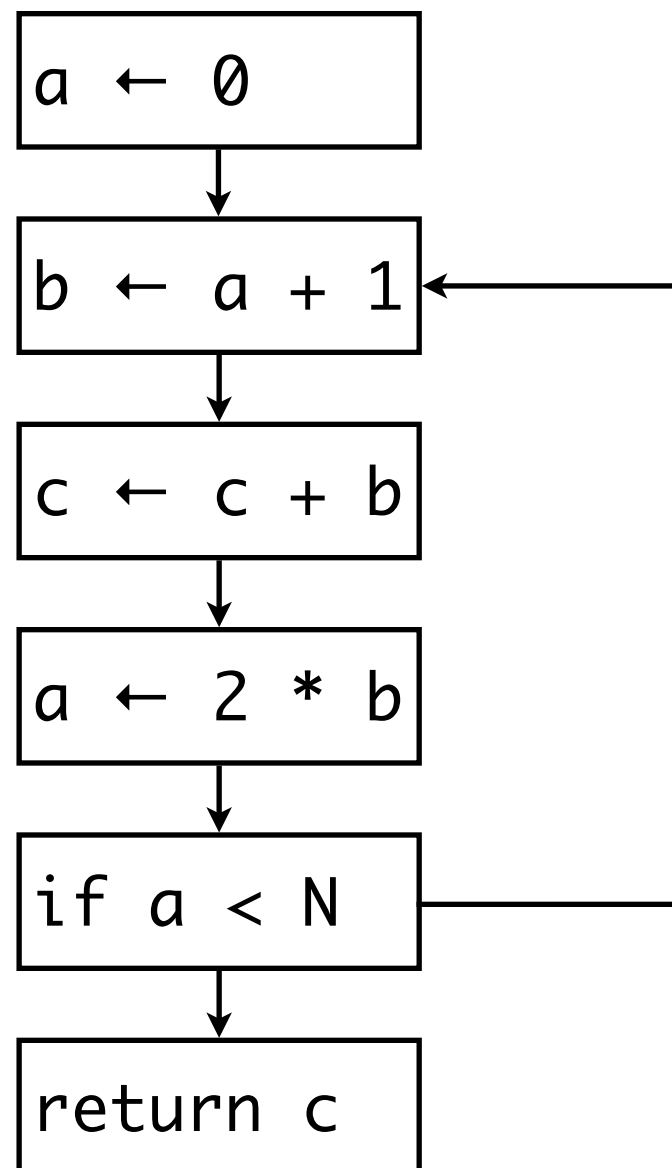
# Recap: Liveness Analysis

## terminology



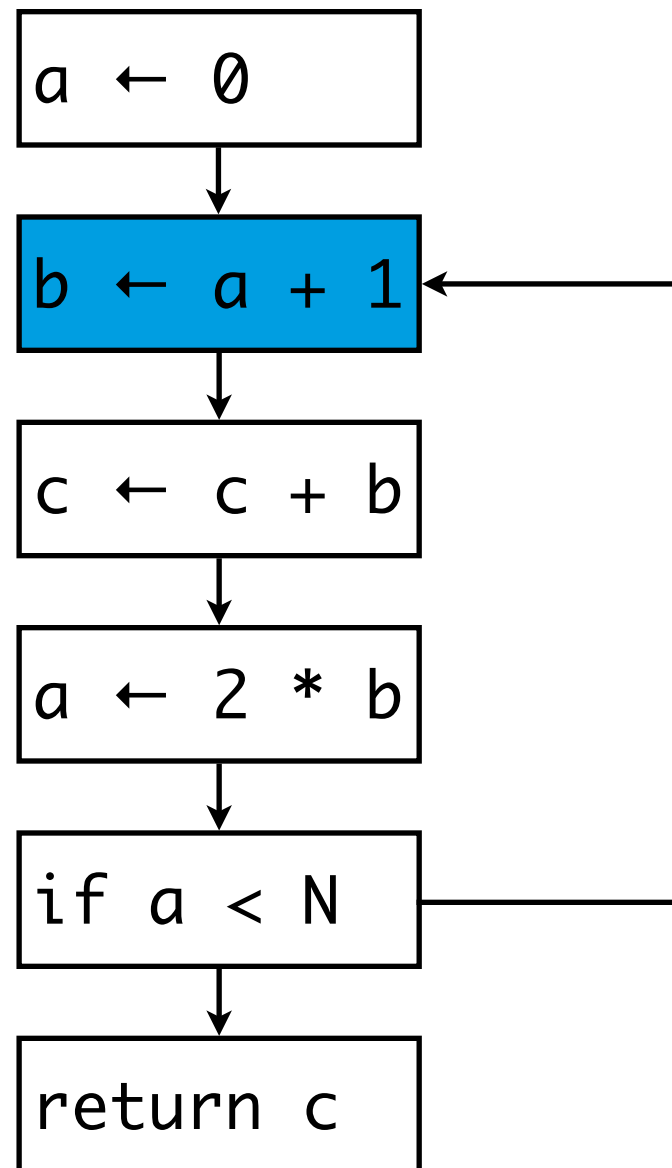
# Recap: Liveness Analysis

## example



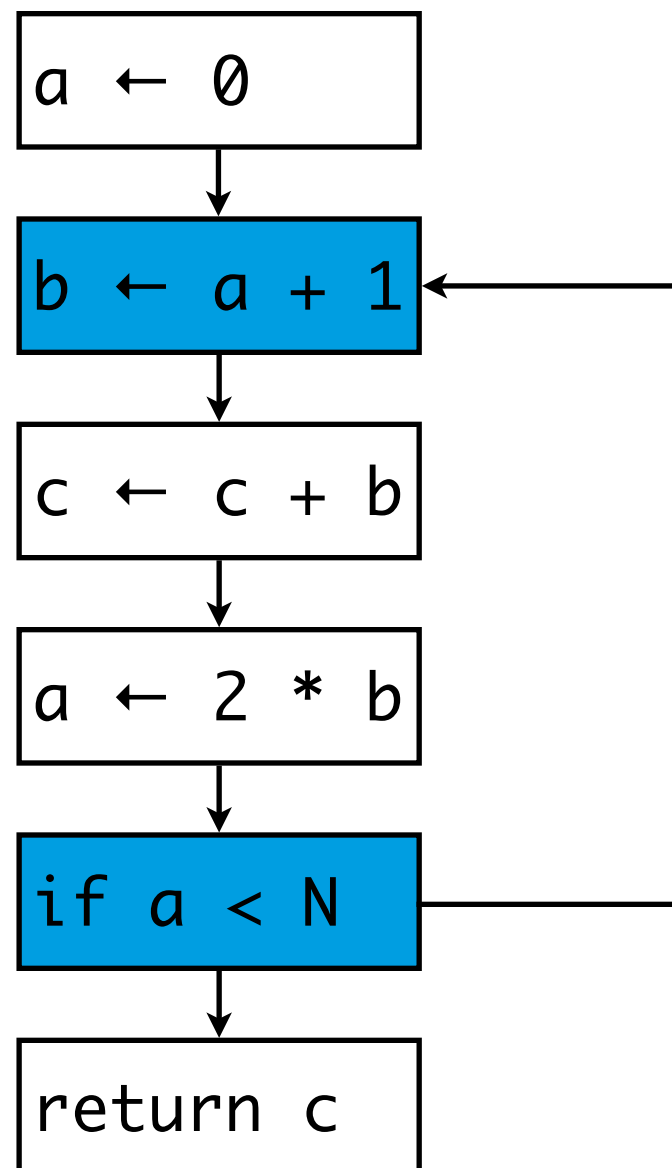
# Recap: Liveness Analysis

## example



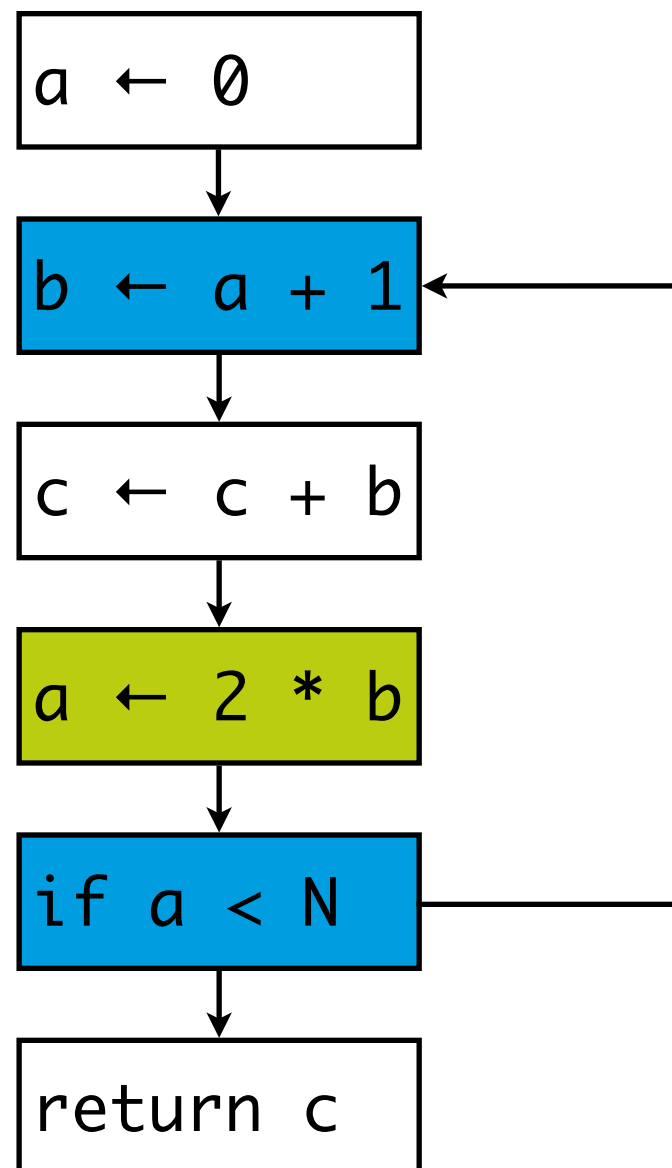
# Recap: Liveness Analysis

## example



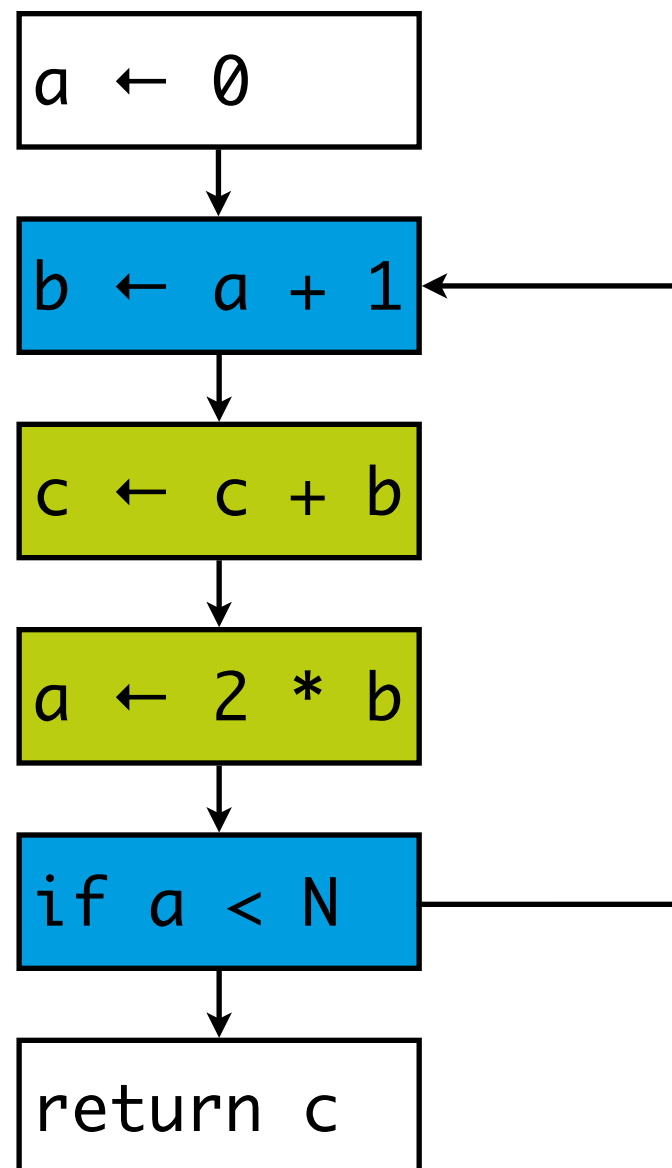
# Recap: Liveness Analysis

## example



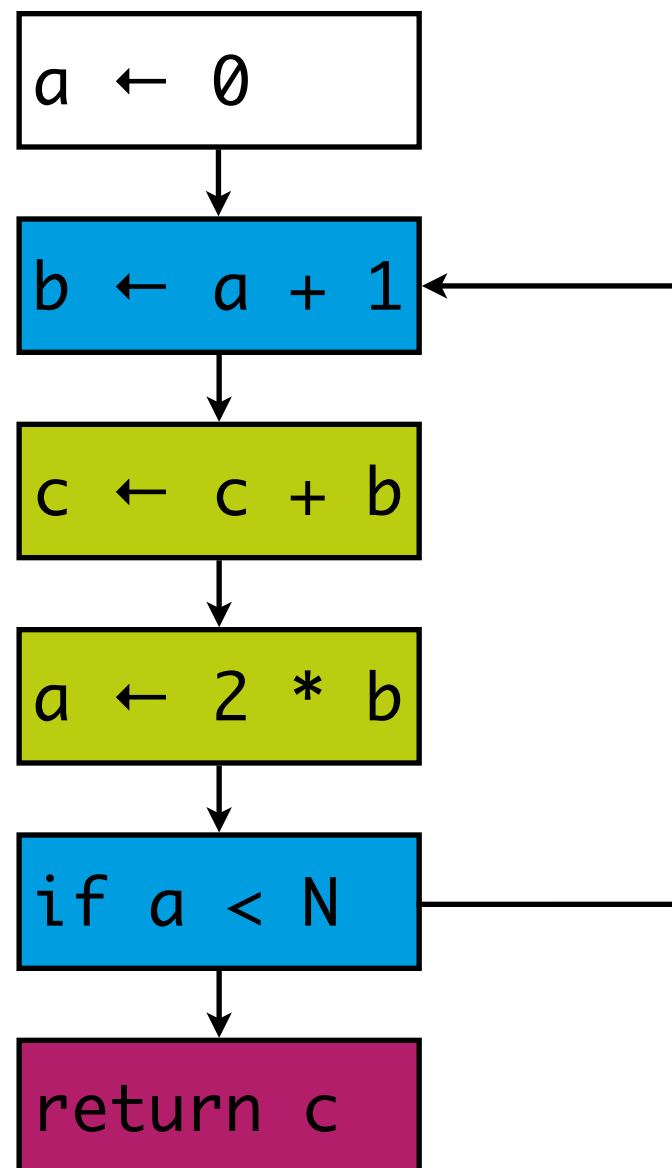
# Recap: Liveness Analysis

## example



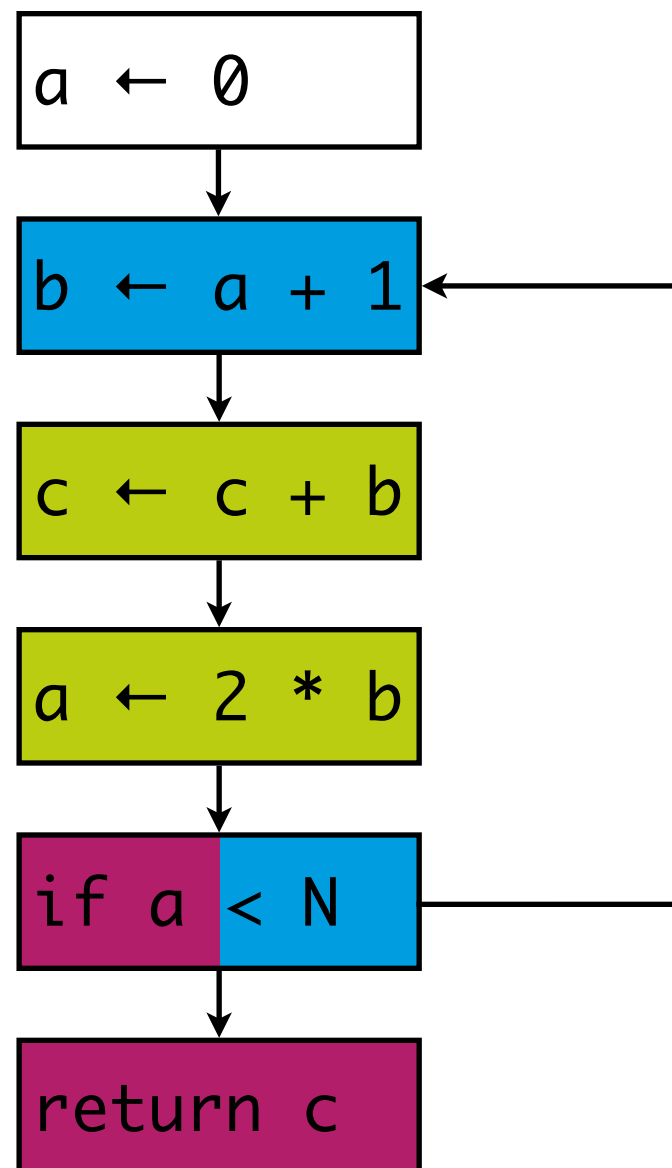
# Recap: Liveness Analysis

## example



# Recap: Liveness Analysis

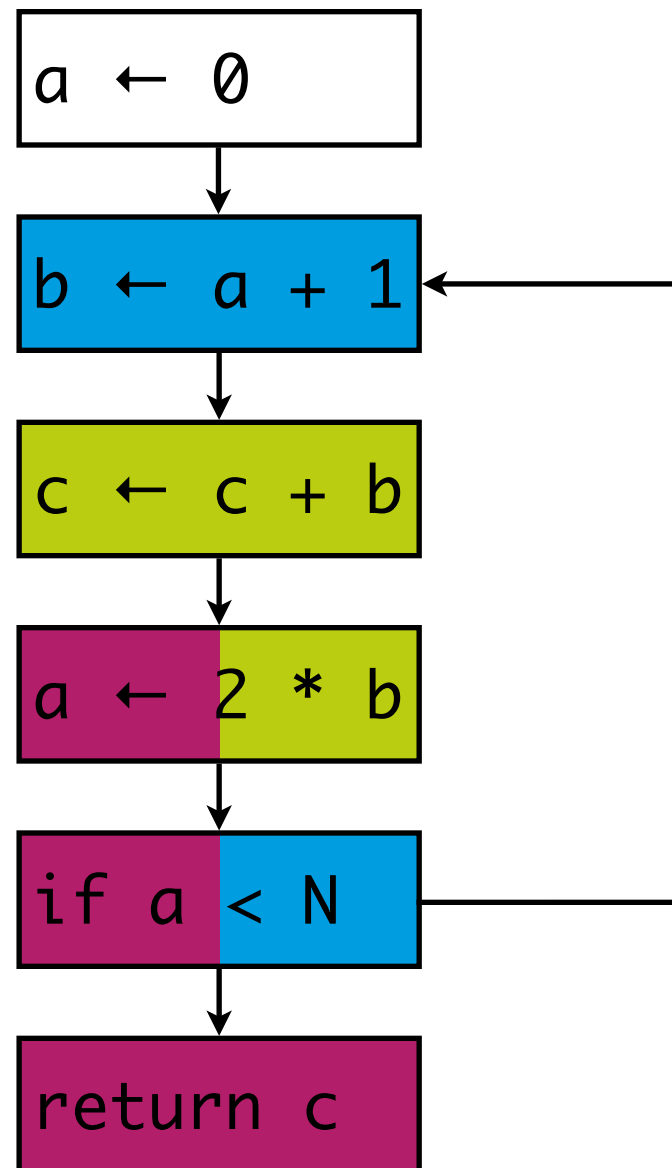
## example





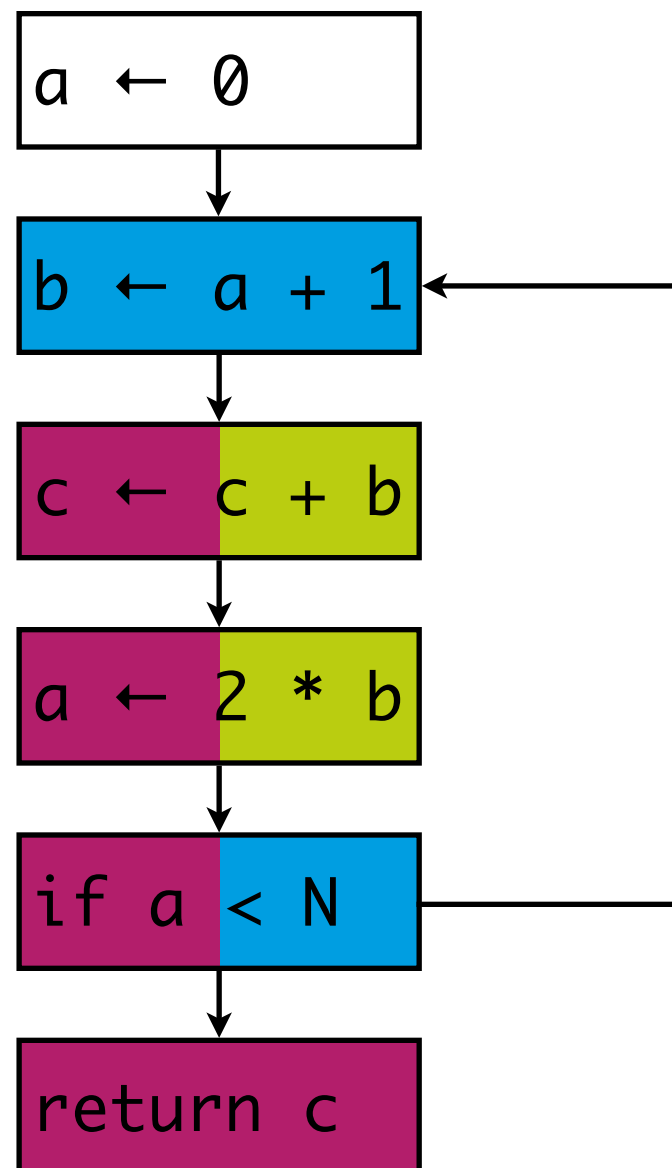
# Recap: Liveness Analysis

## example



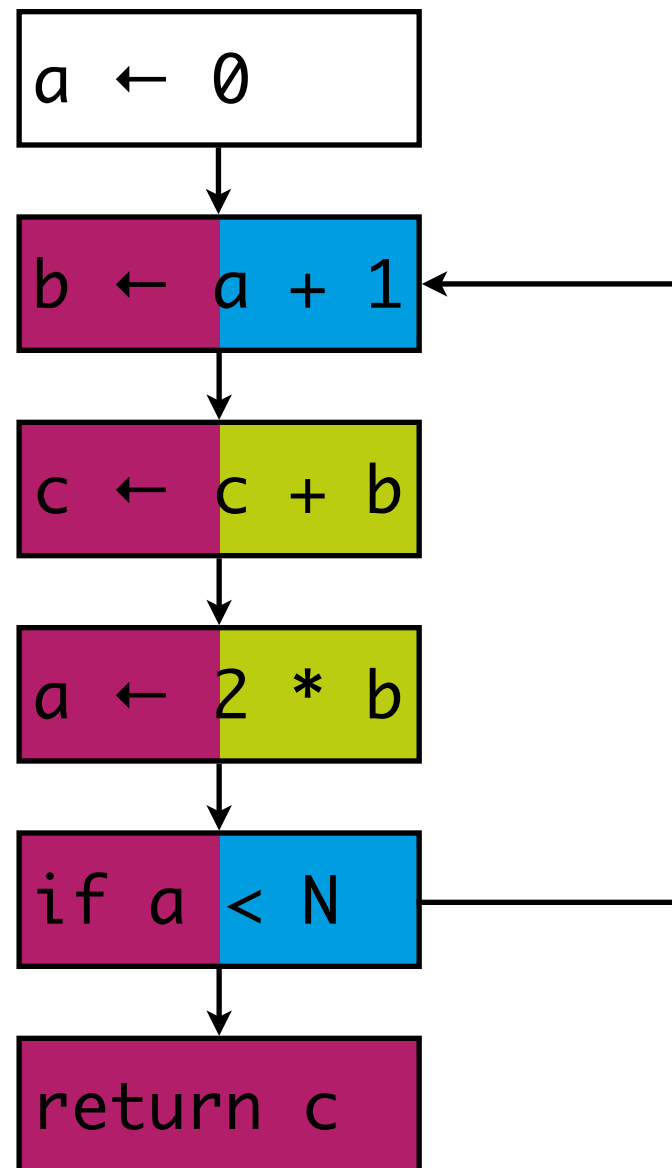
# Recap: Liveness Analysis

## example



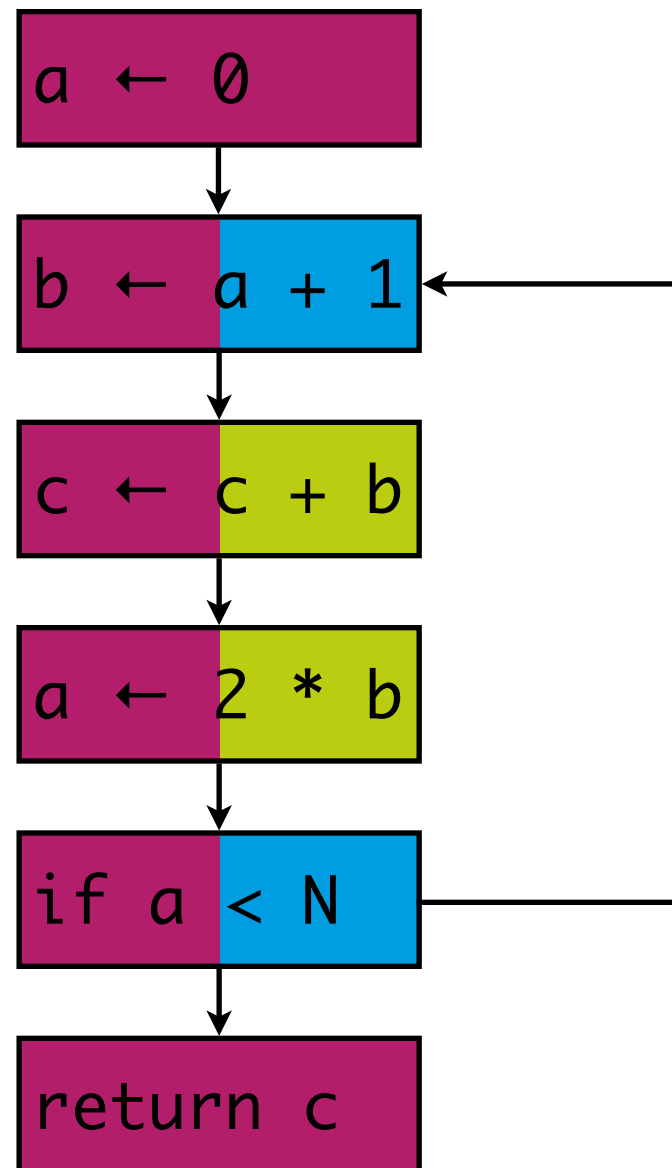
# Recap: Liveness Analysis

## example



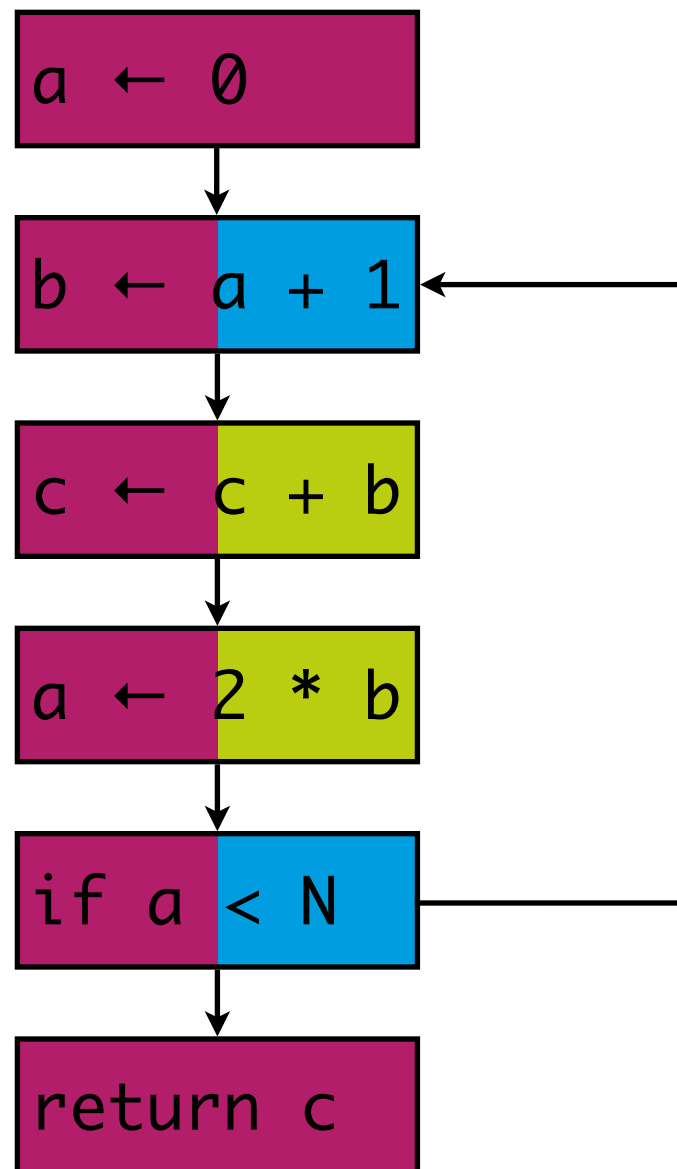
# Recap: Liveness Analysis

## example



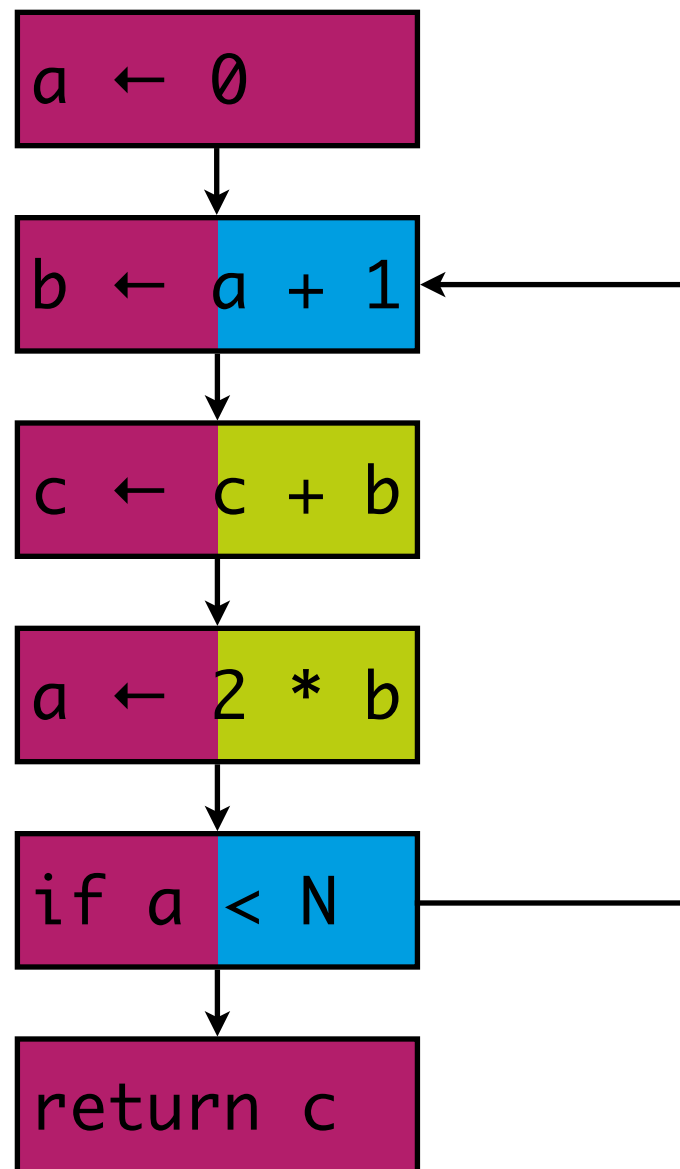
# Interference Graphs

## example



# Interference Graphs

## example



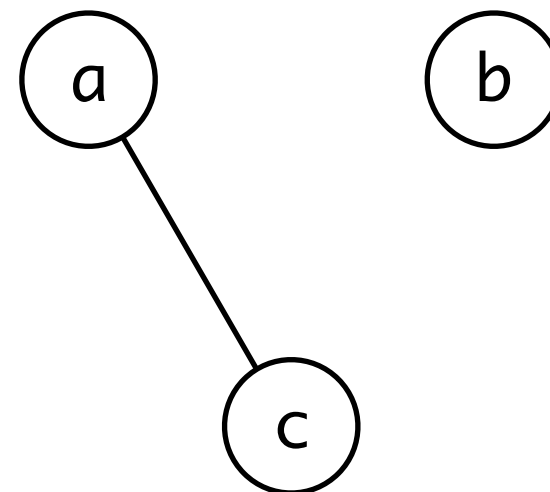
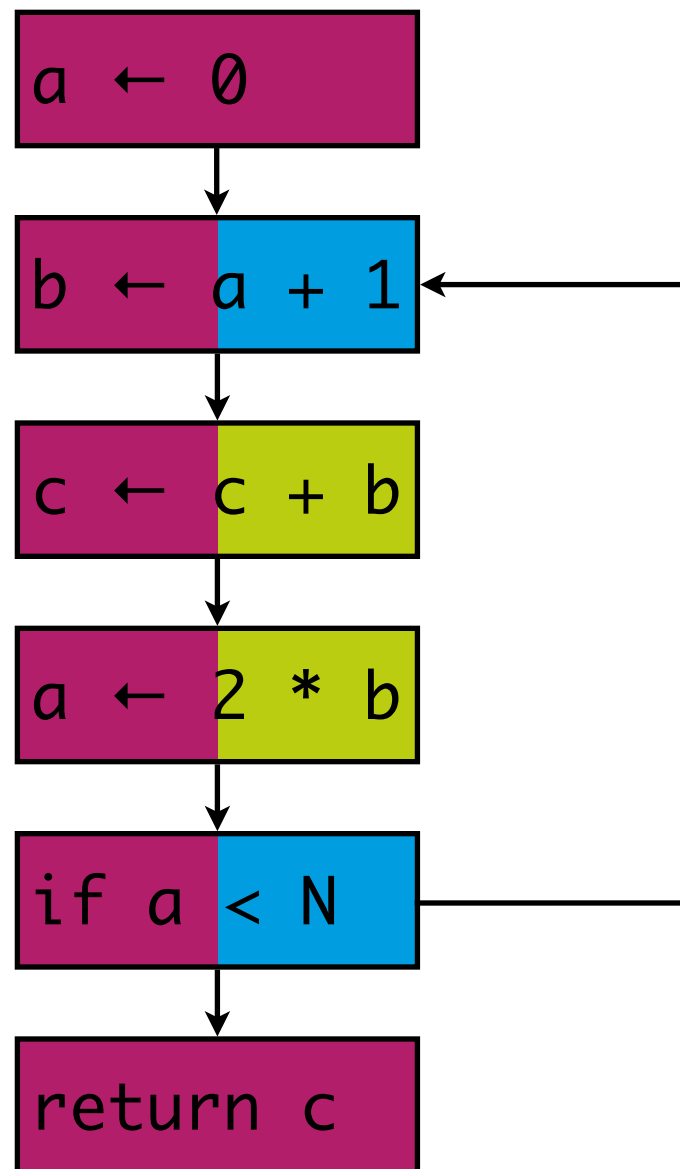
a

b

c

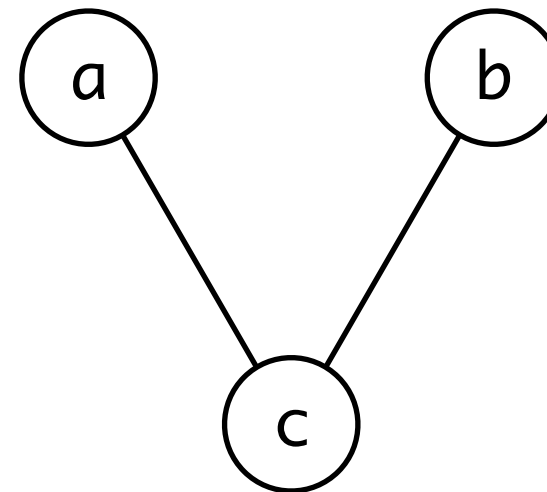
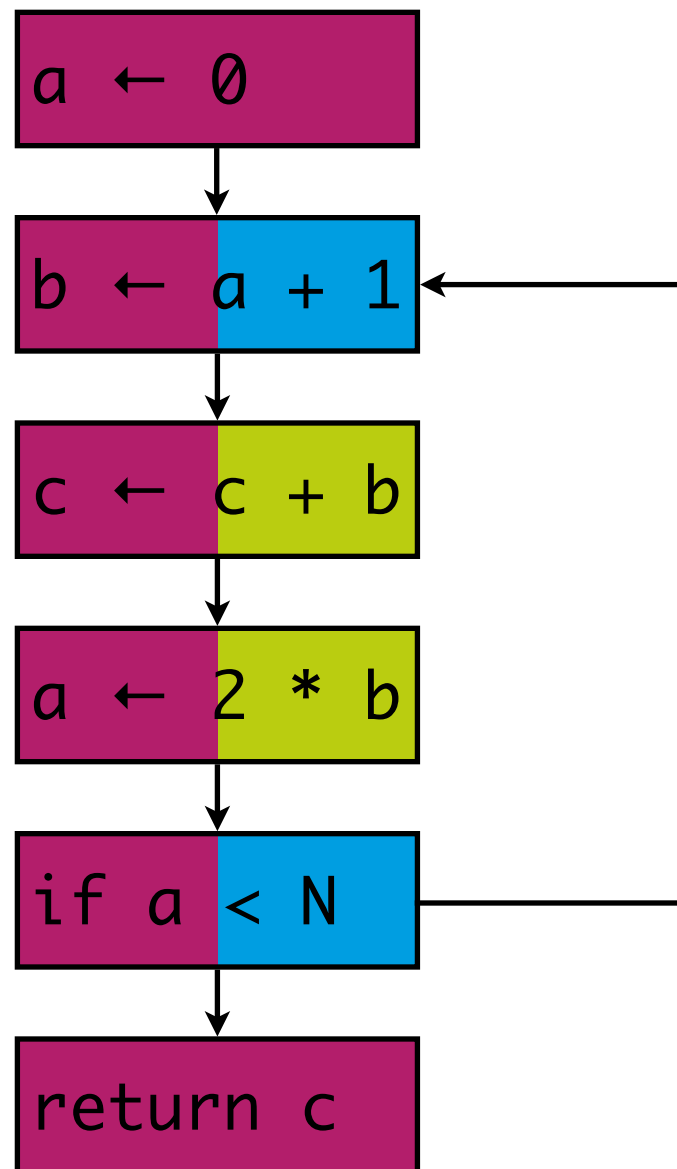
# Interference Graphs

## example



# Interference Graphs

## example





# II

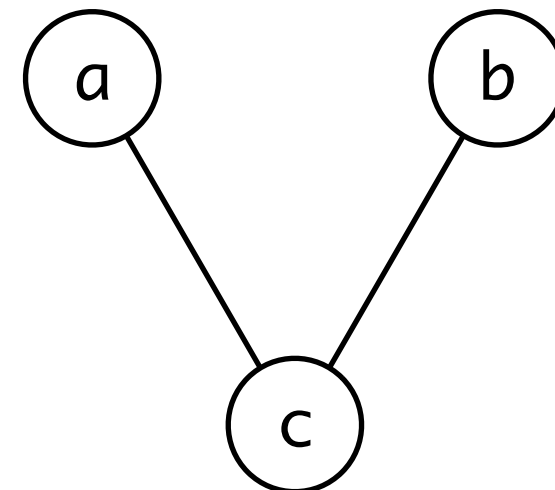
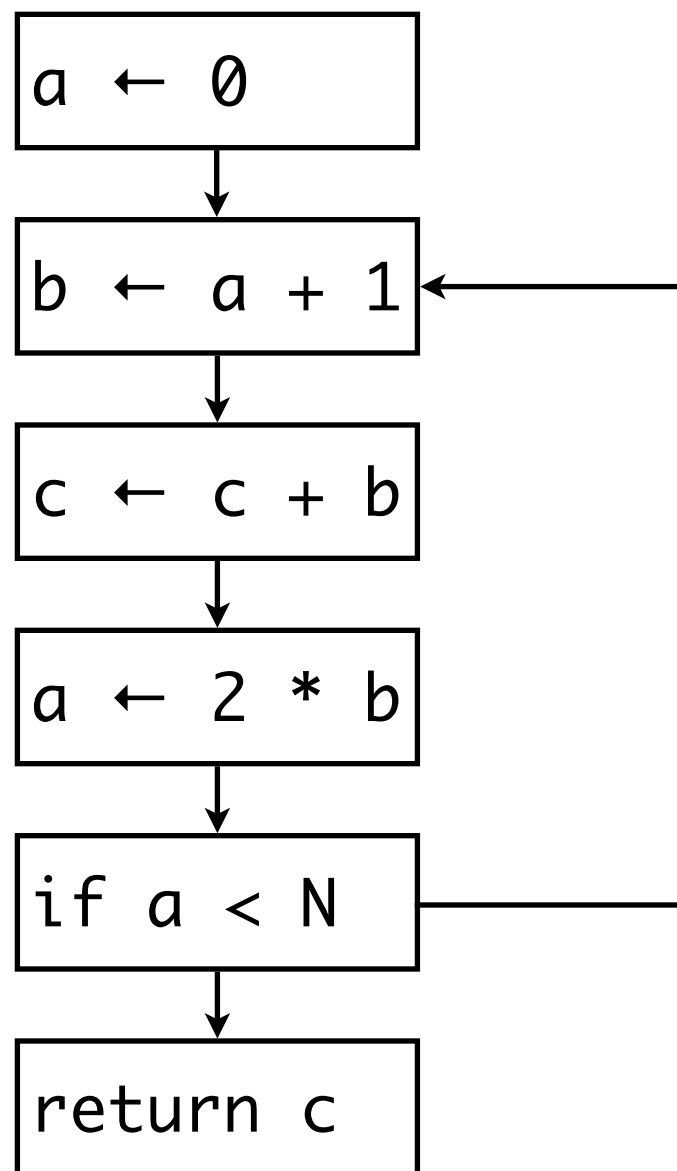
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## Graph Coloring

---

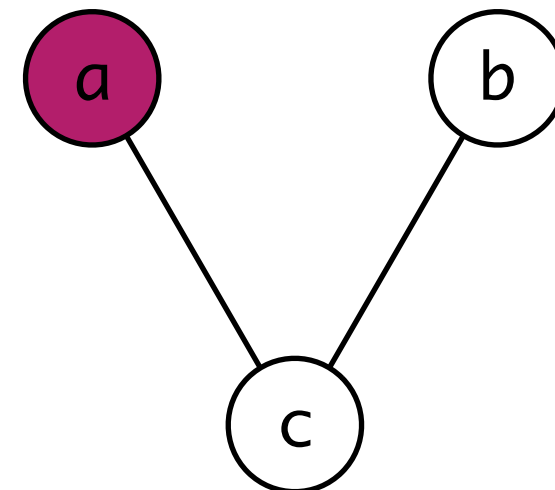
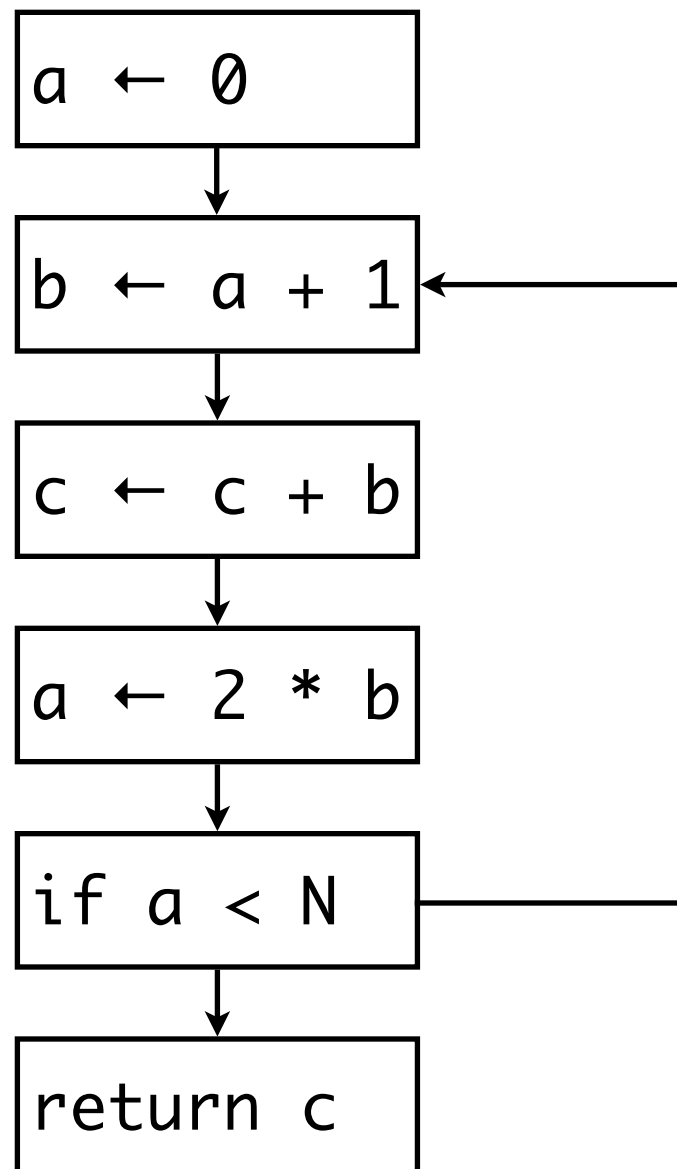
# Graph Coloring

## example



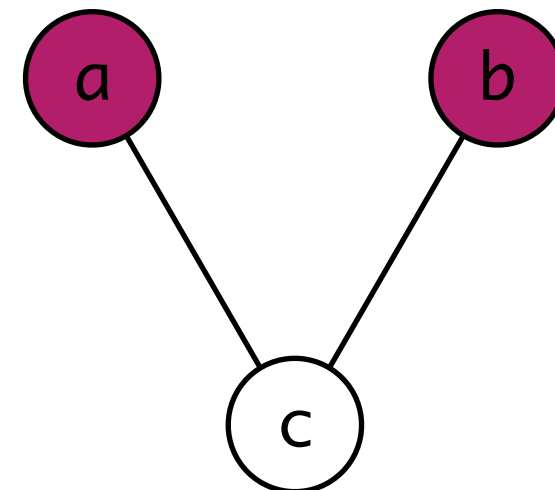
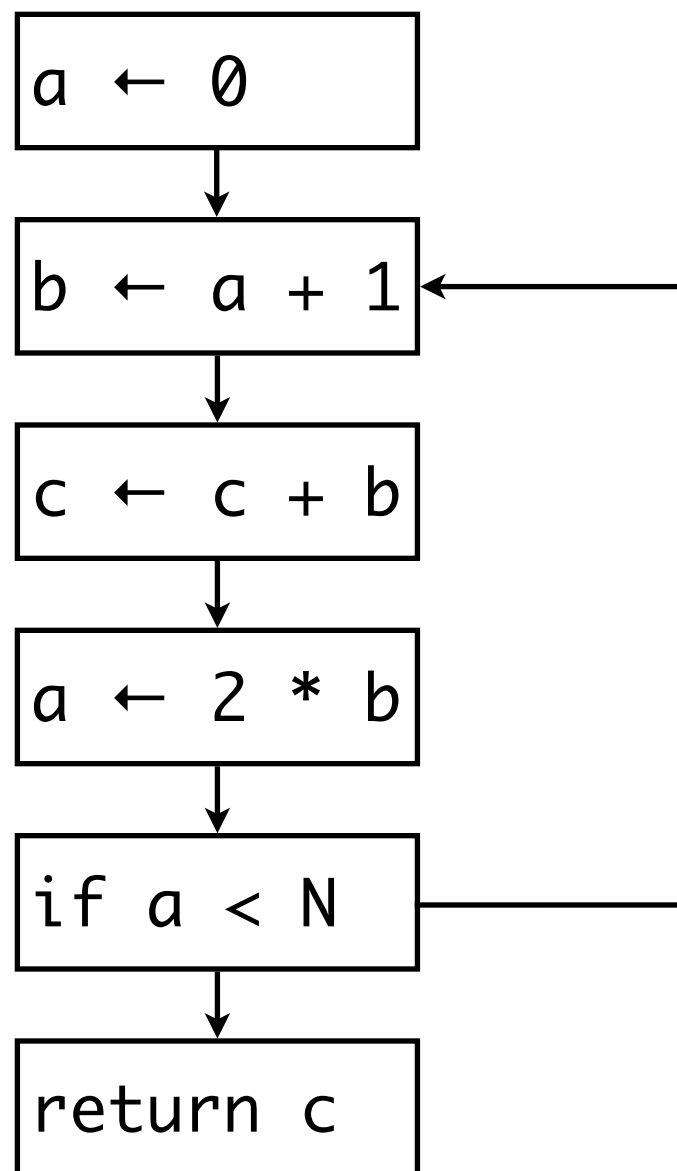
# Graph Coloring

## example



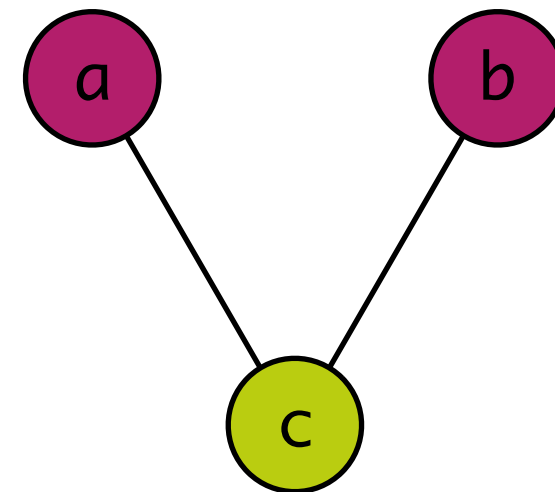
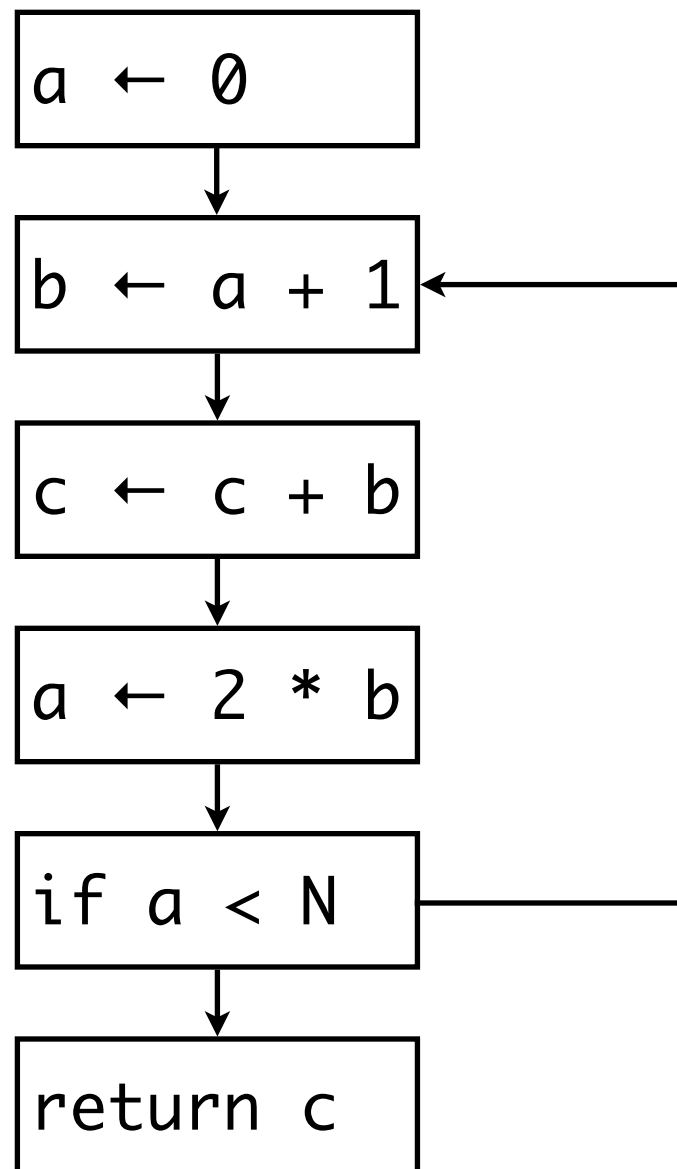
# Graph Coloring

## example



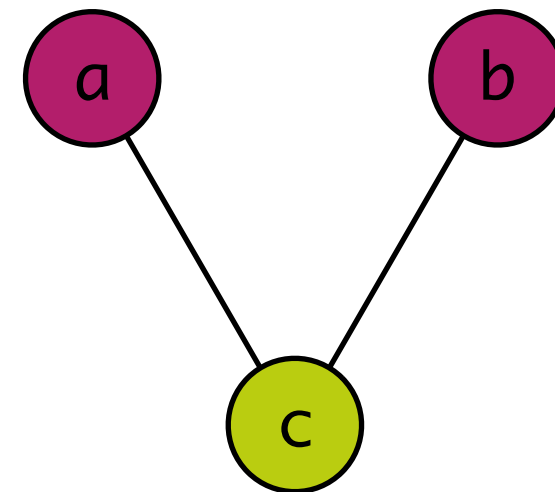
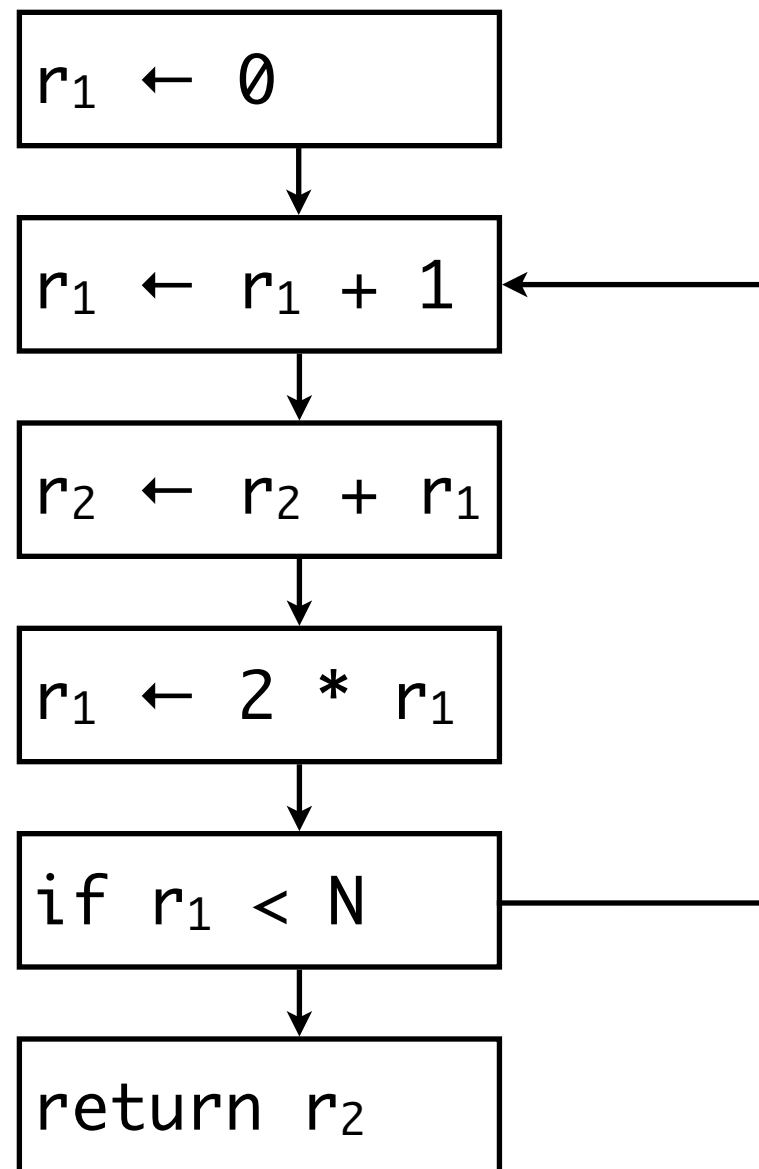
# Graph Coloring

## example



# Graph Coloring

## example



# Graph Coloring

## steps

### Simplify

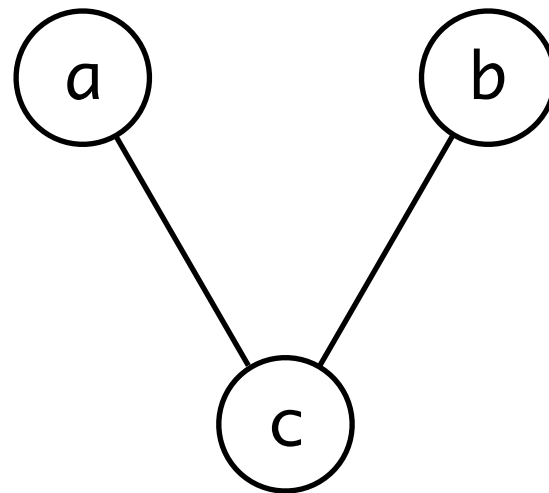
remove node of **insignificant** degree (fewer than **k** edges)

### Select

add node, select color

# Graph Coloring

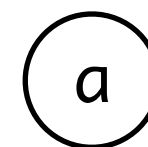
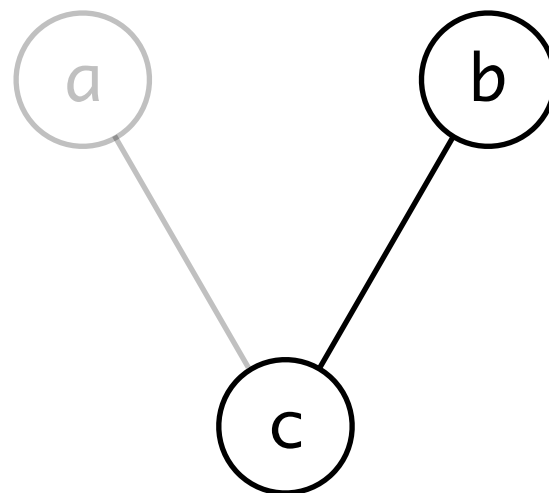
example with 2 colors





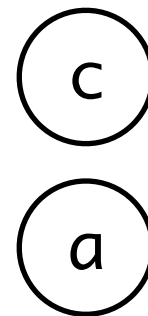
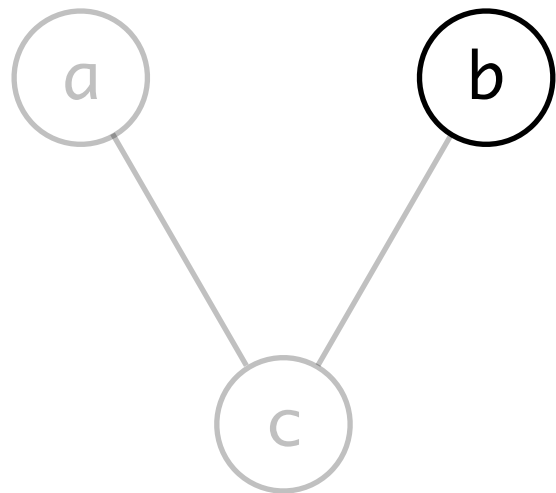
# Graph Coloring

example with 2 colors



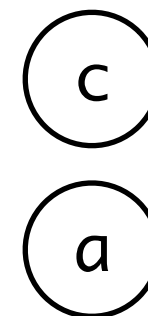
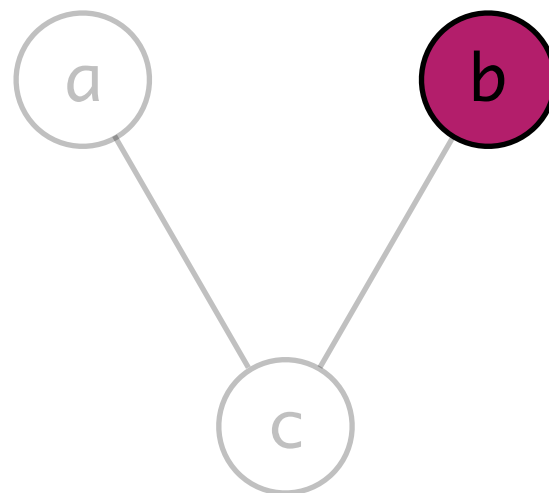
# Graph Coloring

example with 2 colors



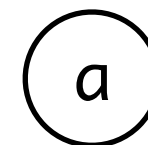
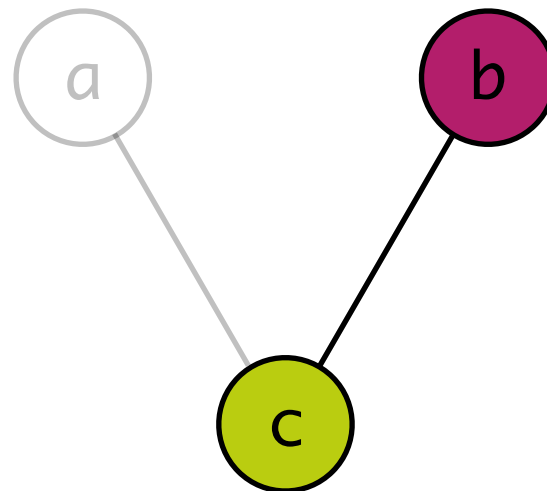
# Graph Coloring

example with 2 colors



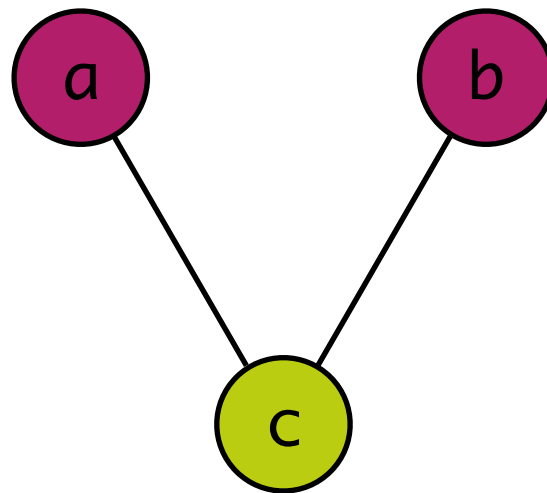
# Graph Coloring

example with 2 colors



# Graph Coloring

example with 2 colors



# Graph Coloring

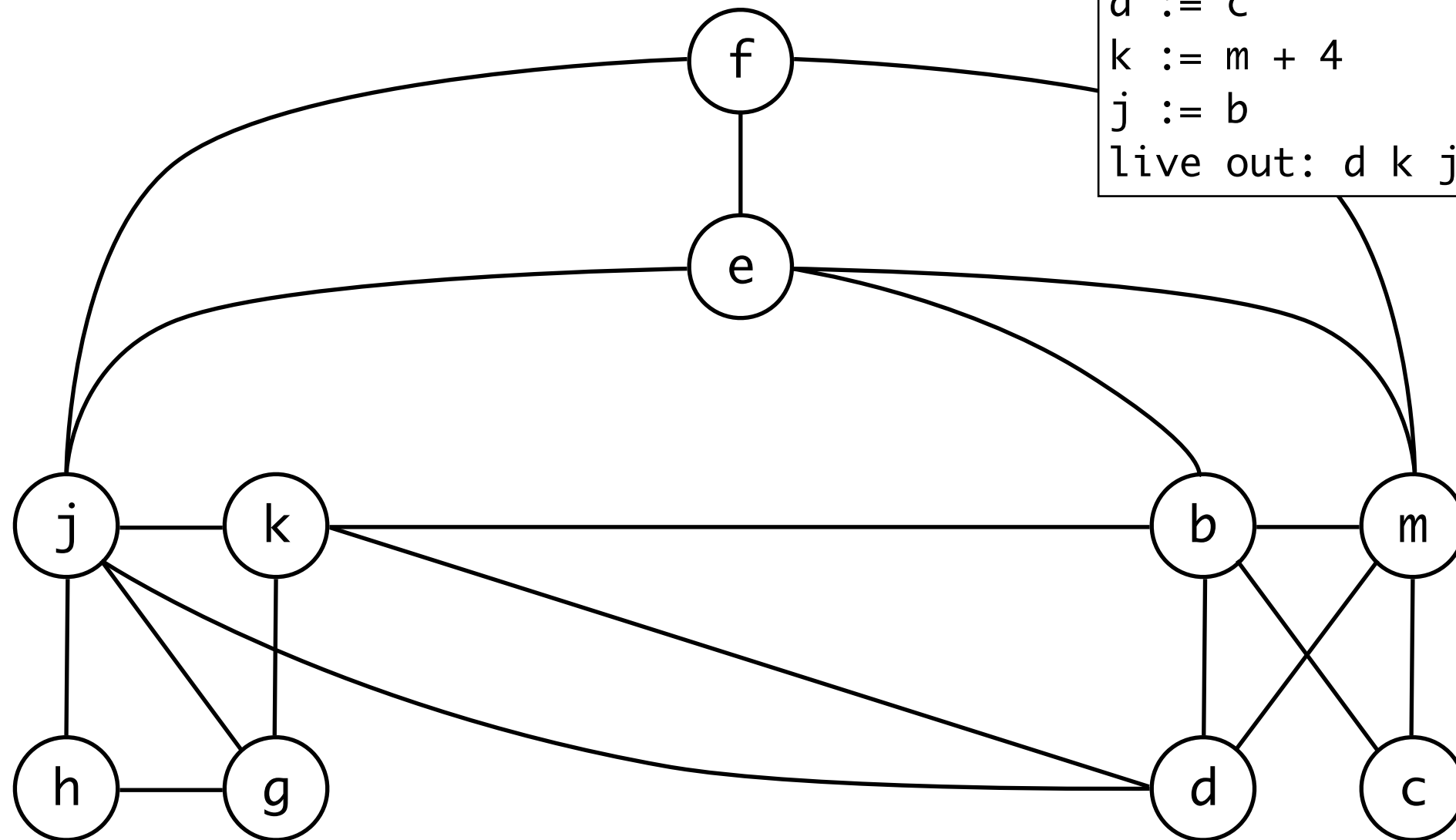
## example with 4 colors

```
live-in: k j
g := mem[j + 12]
h := k - 1
f := g * h
e := mem[j + 8]
m := mem[j + 16]
b := mem[f]
c := e + 8
d := c
k := m + 4
j := b
live out: d k j
```

# Graph Coloring

example with 4 colors

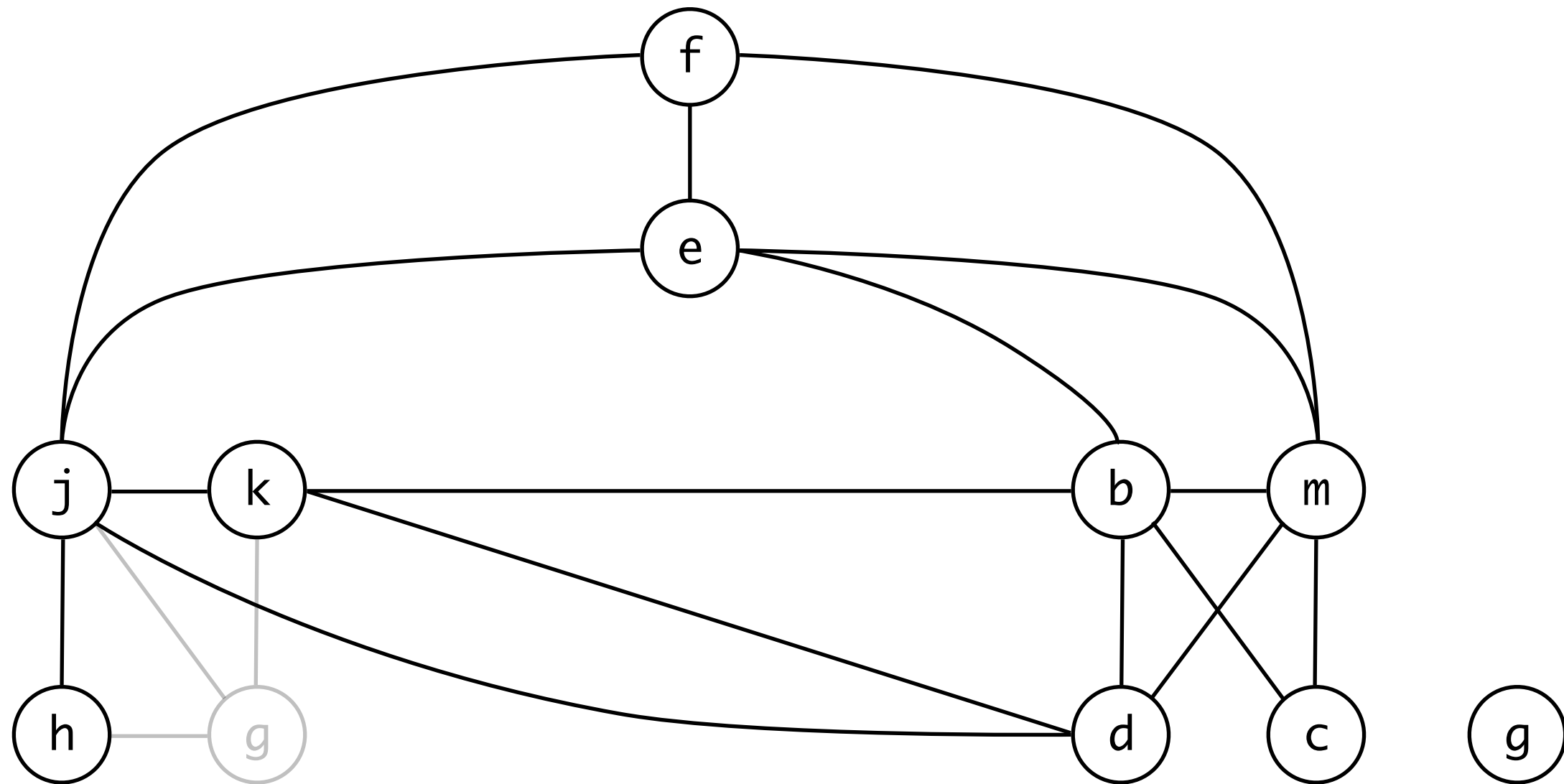
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b := mem[f]
c := e + 8
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j := b
live out: d k j
```



# Graph Coloring

example with 4 colors

$r_1$   
 $r_2$   
 $r_3$   
 $r_4$

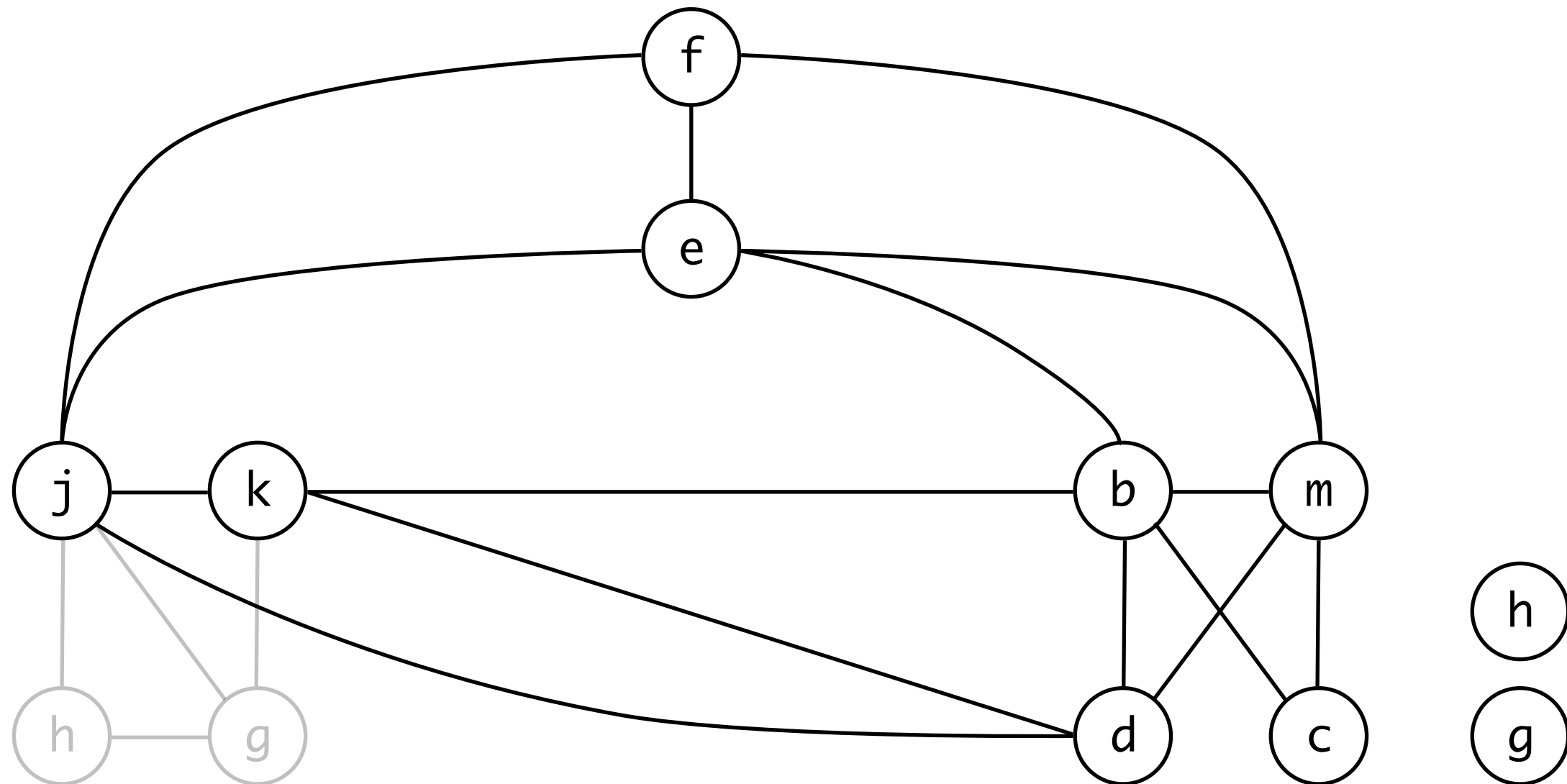




# Graph Coloring

example with 4 colors

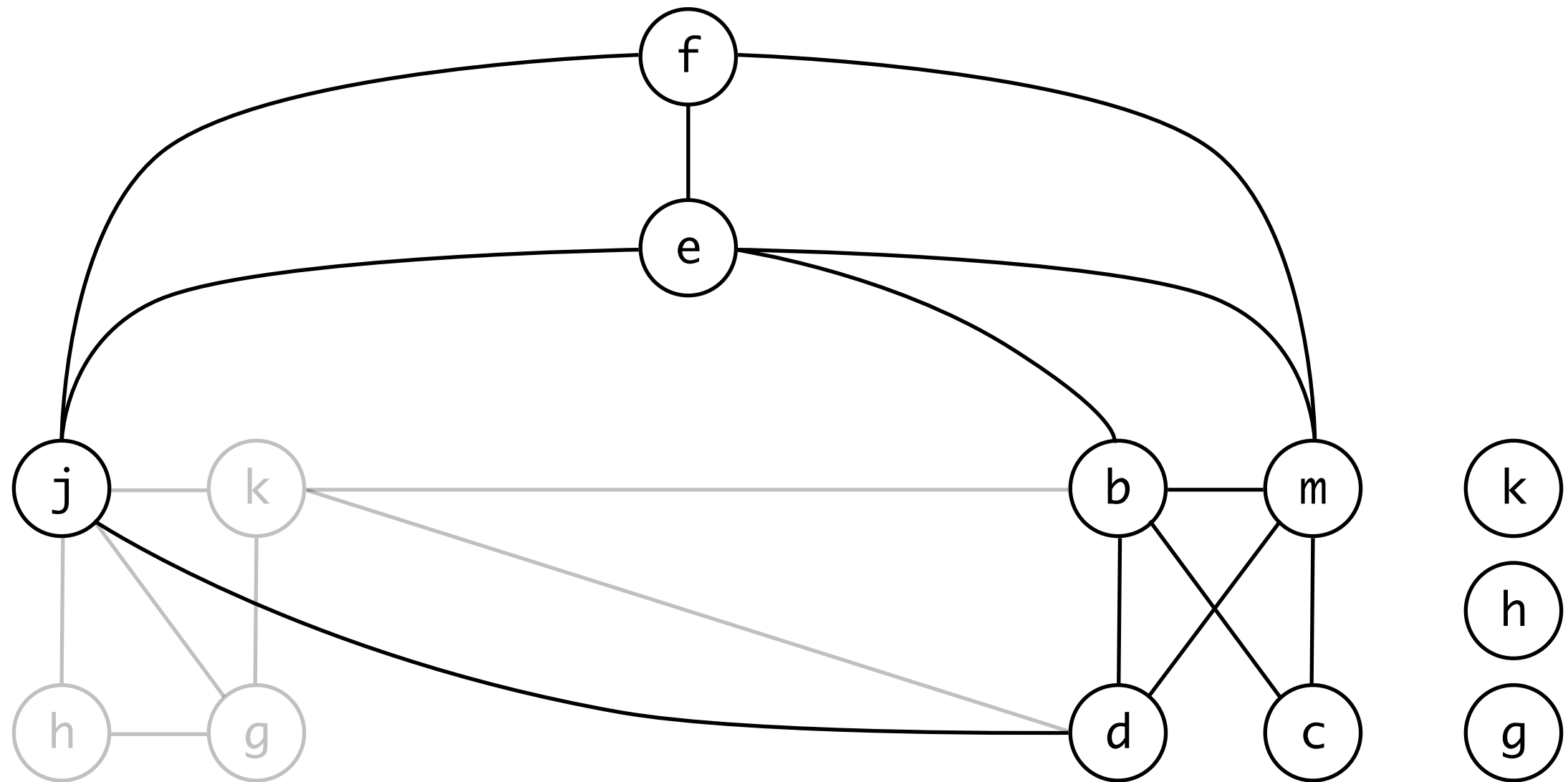
$r_1$   
 $r_2$   
 $r_3$   
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# Graph Coloring

example with 4 colors

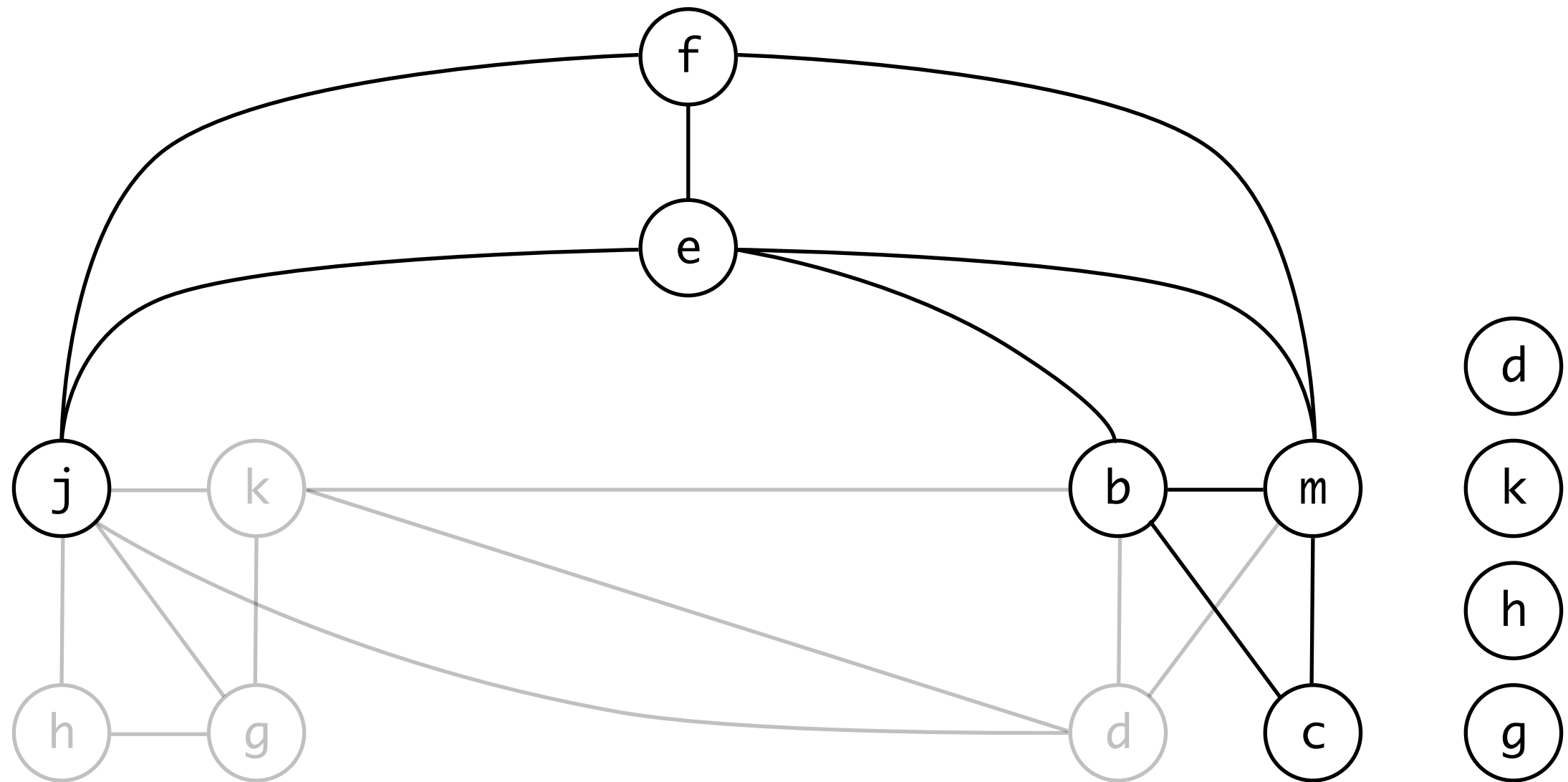
$r_1$   
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# Graph Coloring

example with 4 colors

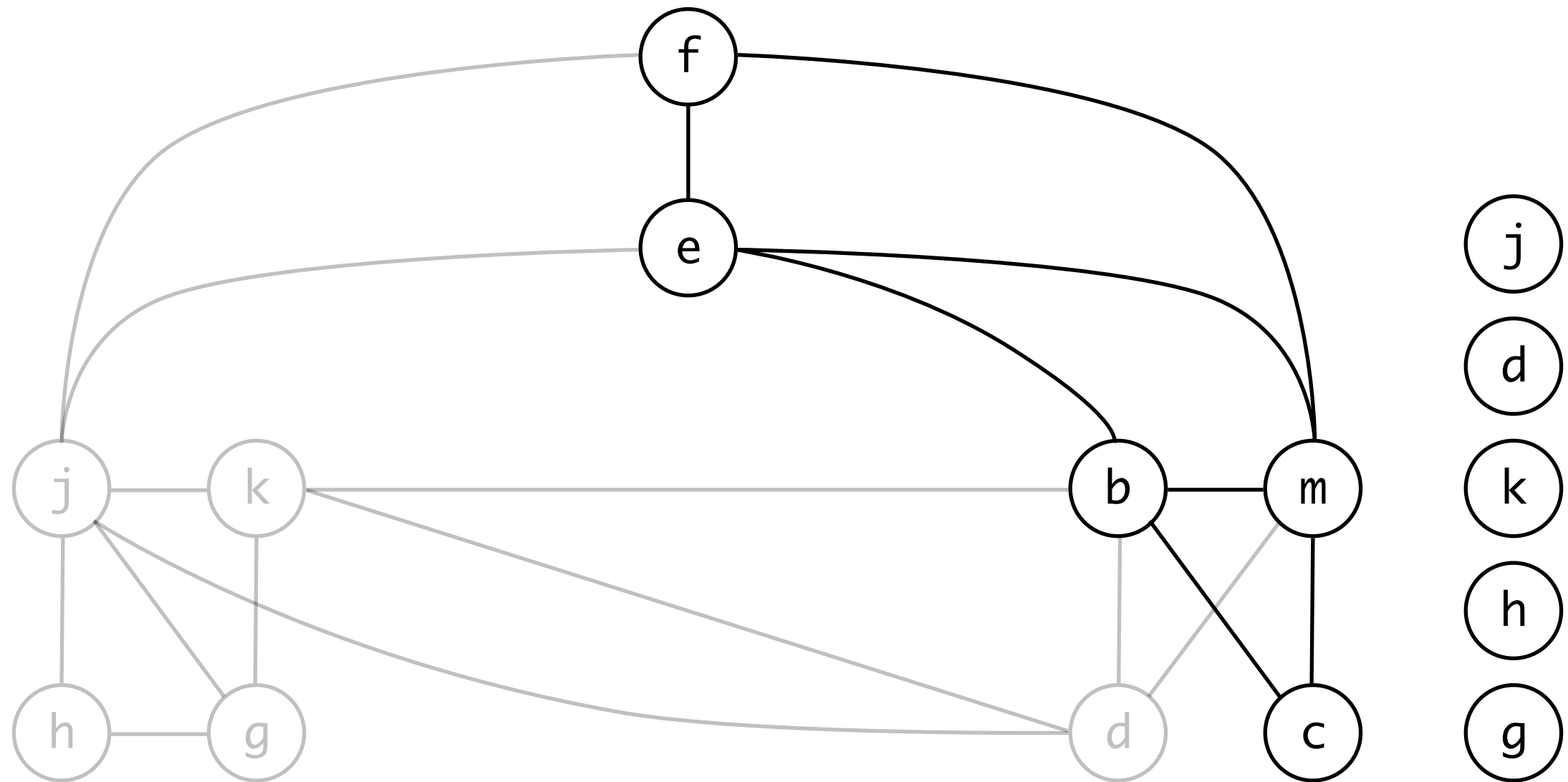
$r_1$   
 $r_2$   
 $r_3$   
 $r_4$



# Graph Coloring

example with 4 colors

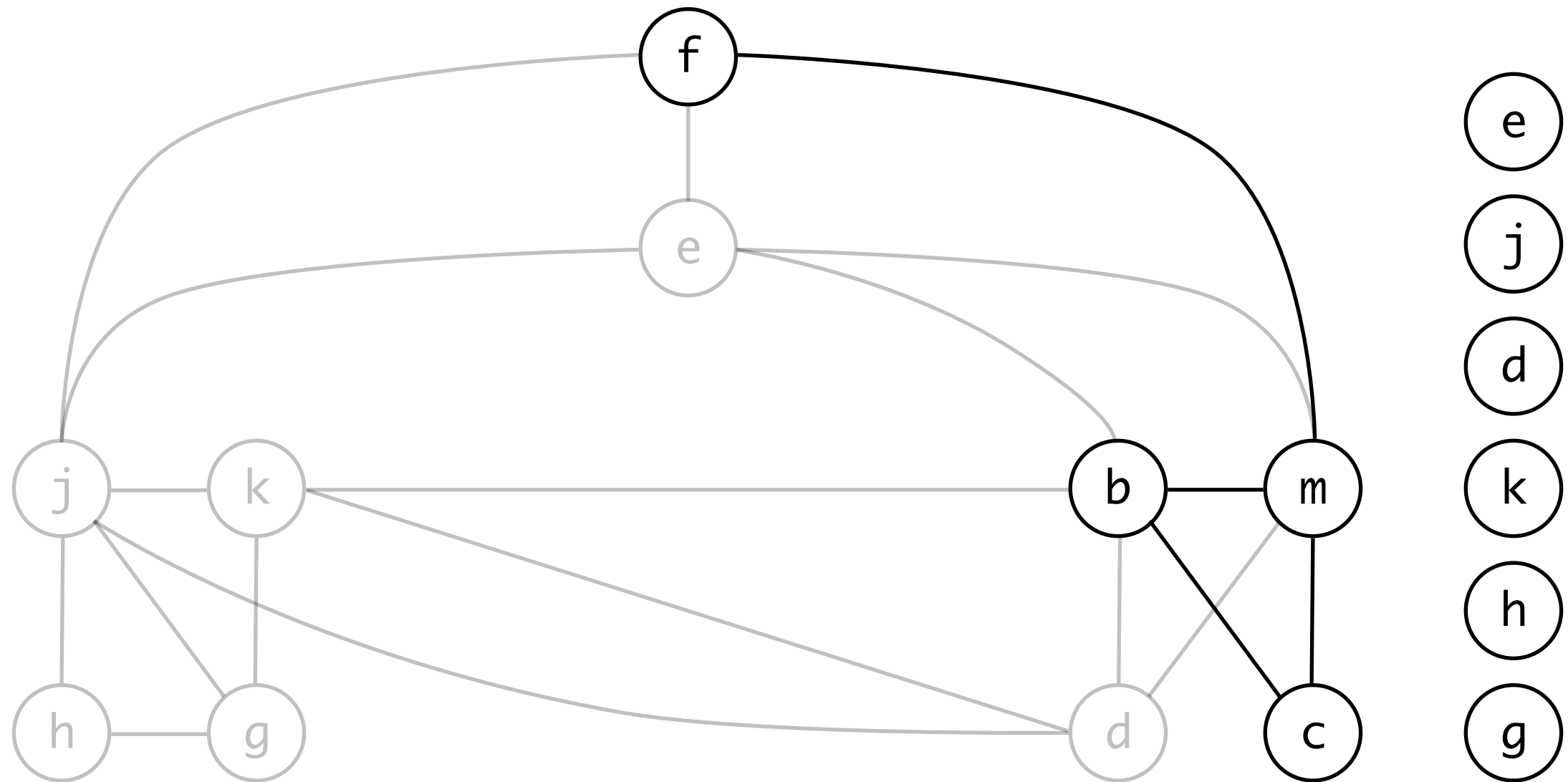
$r_1$   
 $r_2$   
 $r_3$   
 $r_4$



# Graph Coloring

example with 4 colors

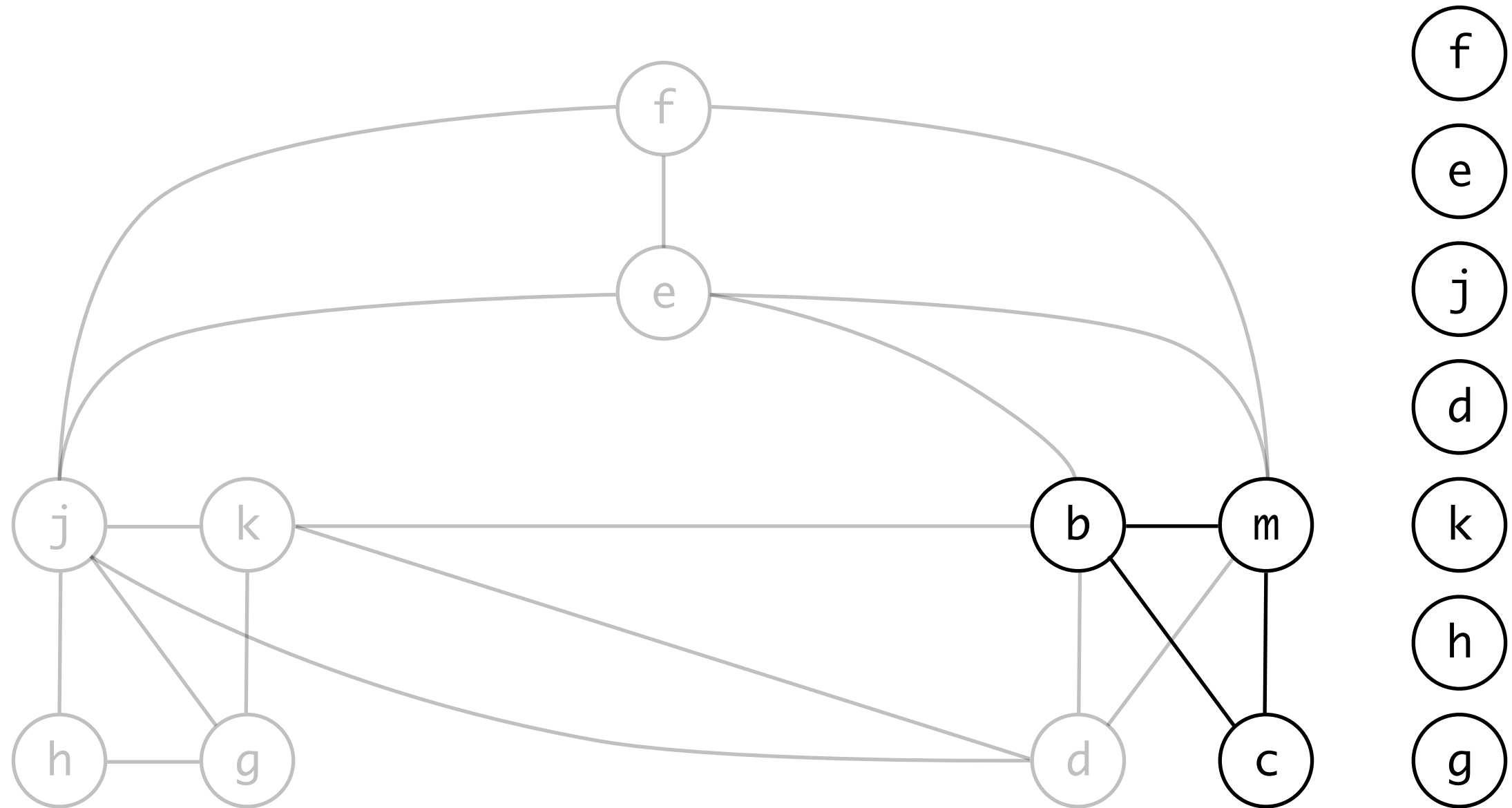
$r_1$   
 $r_2$   
 $r_3$   
 $r_4$



# Graph Coloring

example with 4 colors

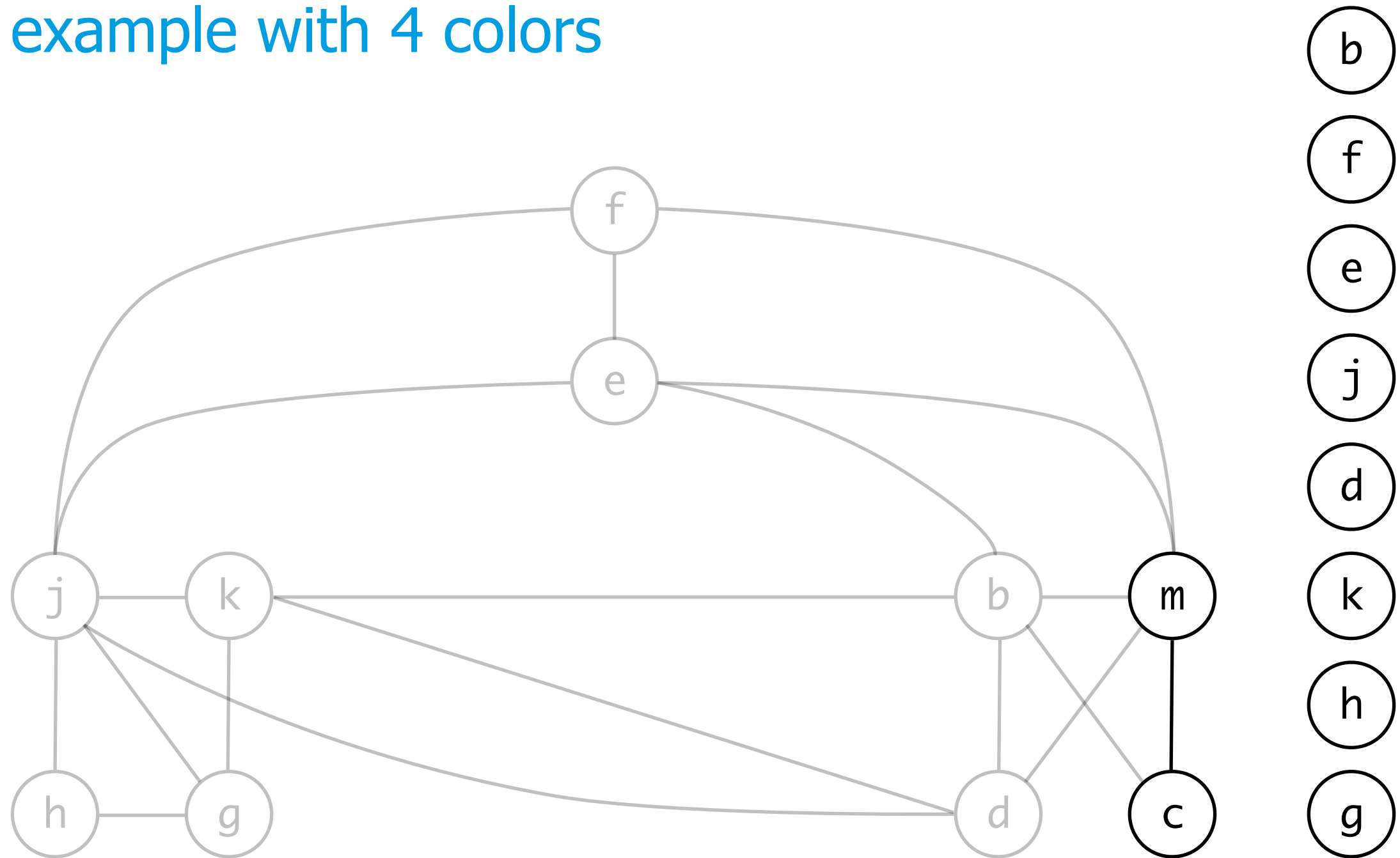
$r_1$   
 $r_2$   
 $r_3$   
 $r_4$



# Graph Coloring

example with 4 colors

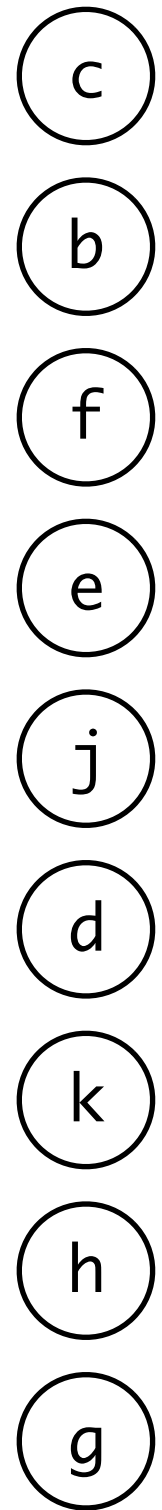
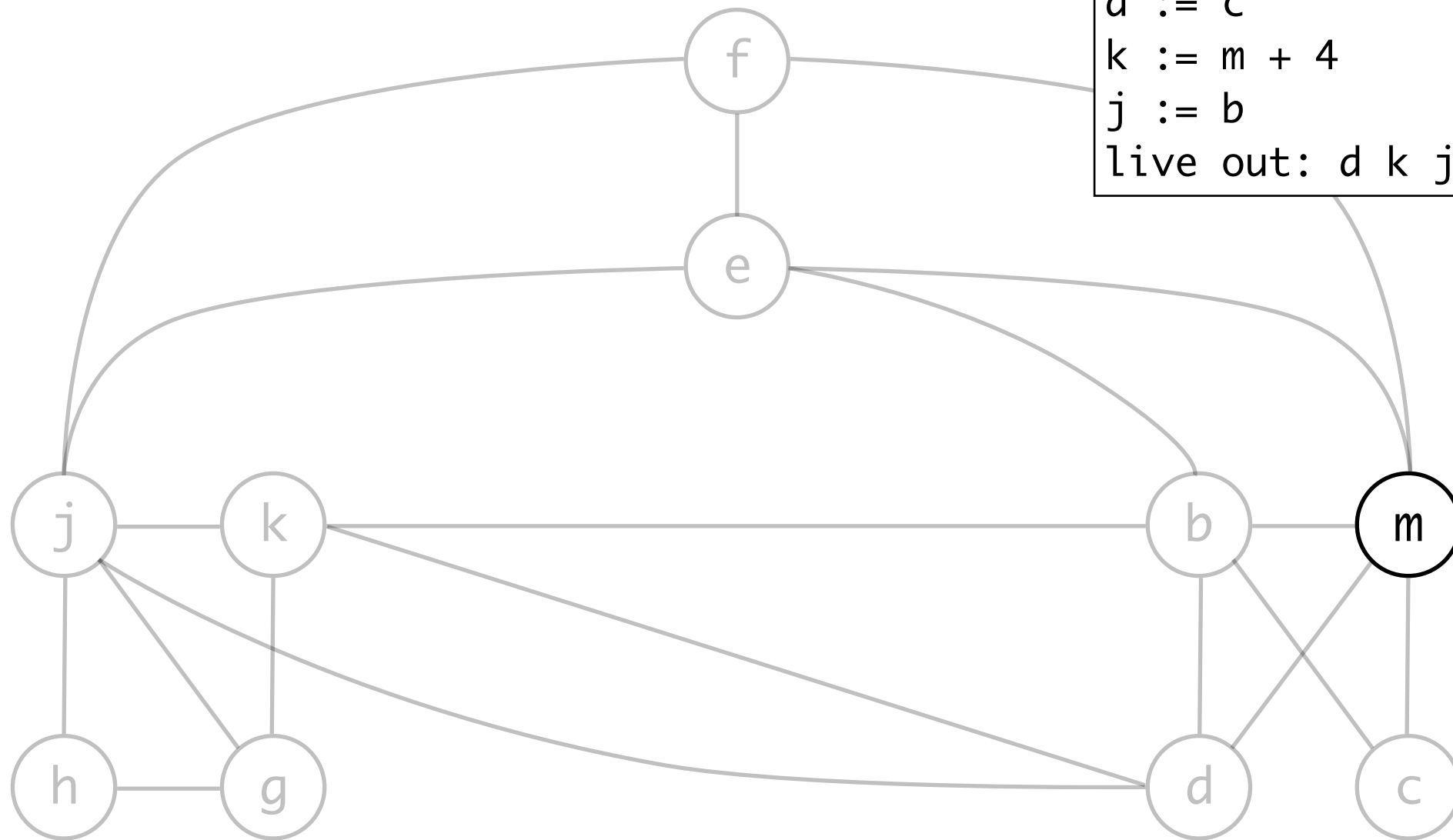
$r_1$   
 $r_2$   
 $r_3$   
 $r_4$



# Graph Coloring

example with 4 colors

```
live-in: k j
g := mem[j + 12]
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e := mem[j + 8]
m := mem[j + 16]
b := mem[f]
c := e + 8
d := c
k := m + 4
j := b
live out: d k j
```

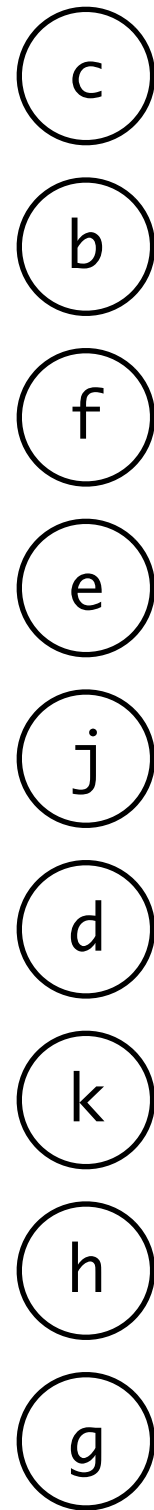
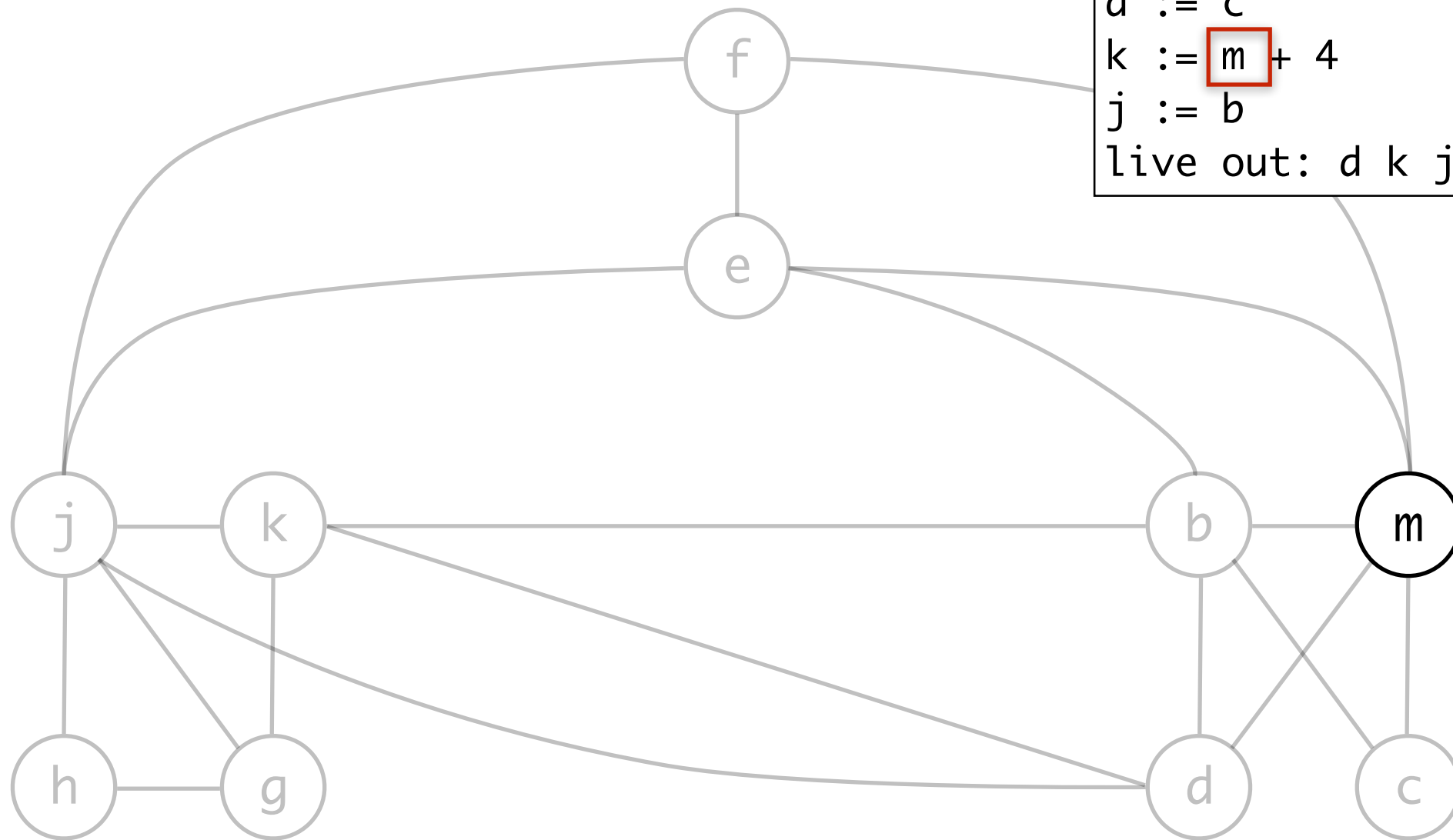




# Graph Coloring

example with 4 colors

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c := e + 8
d := c
k := m + 4
j := b
live out: d k j
```

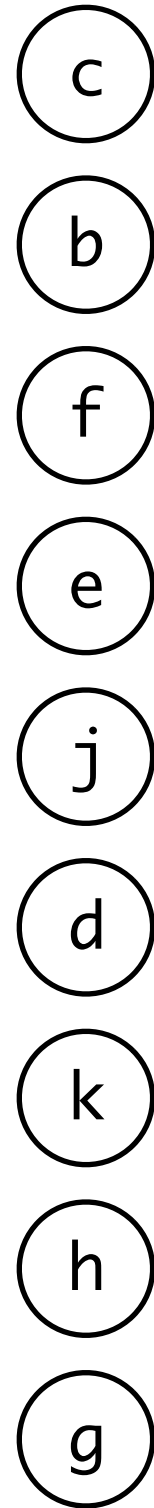
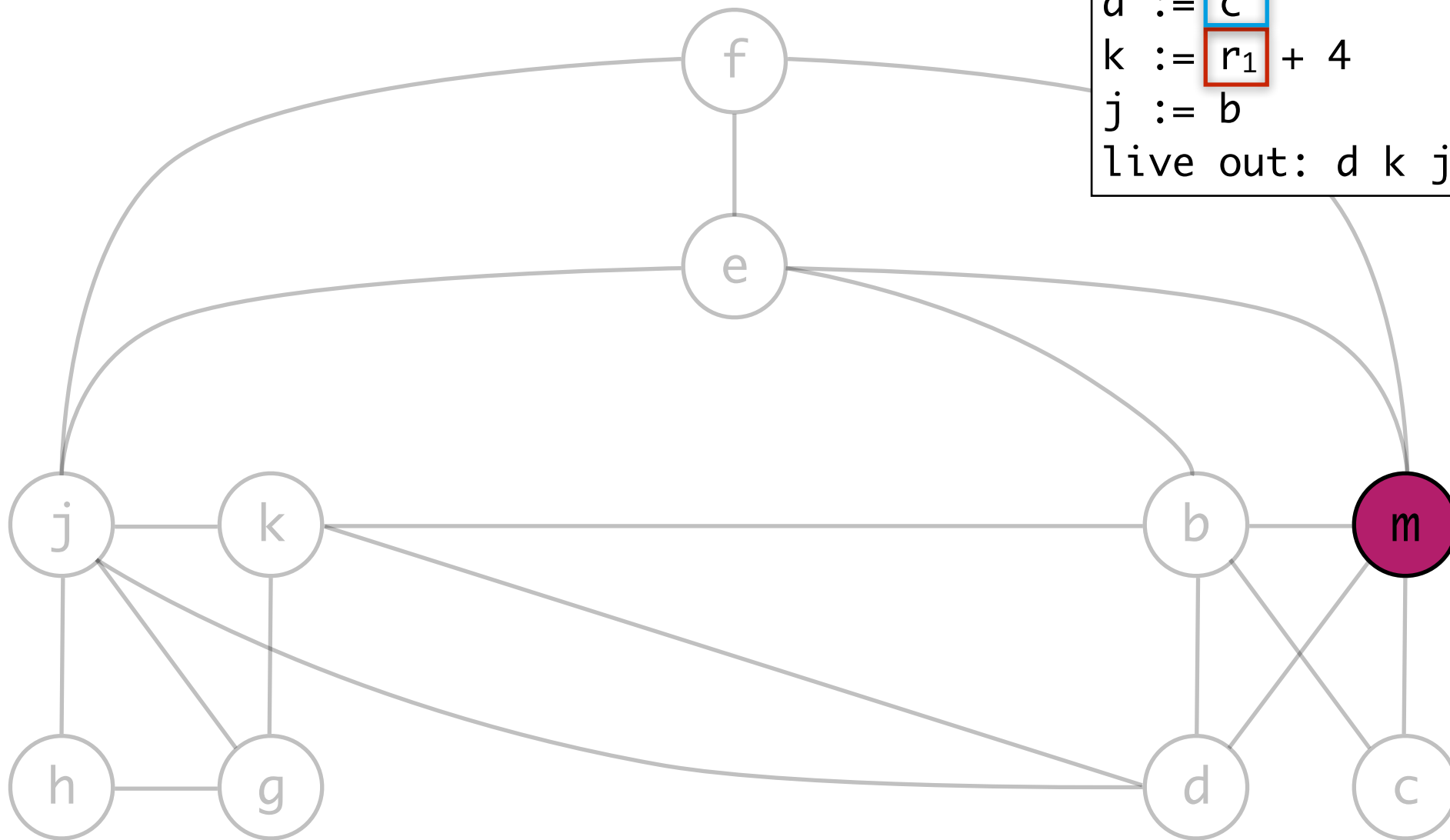


r<sub>1</sub>  
r<sub>2</sub>  
r<sub>3</sub>  
r<sub>4</sub>

# Graph Coloring

example with 4 colors

```
live-in: k j  
g := mem[j + 12]  
h := k - 1  
f := g * h  
e := mem[j + 8]  
r1 := mem[j + 16]  
b := mem[f]  
c := e + 8  
d := c  
k := r1 + 4  
j := b  
live out: d k j
```

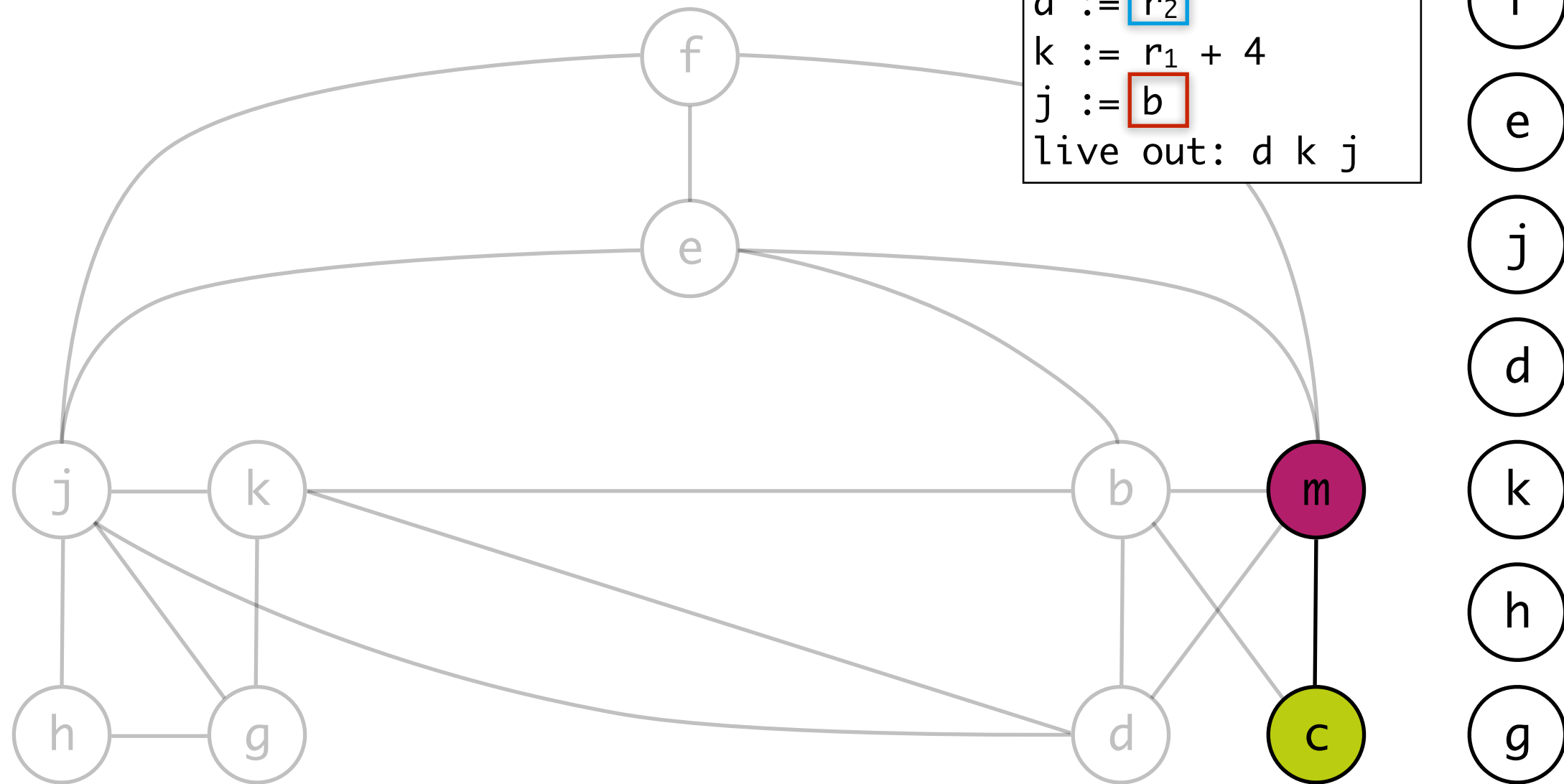


r<sub>1</sub>  
r<sub>2</sub>  
r<sub>3</sub>  
r<sub>4</sub>

# Graph Coloring

example with 4 colors

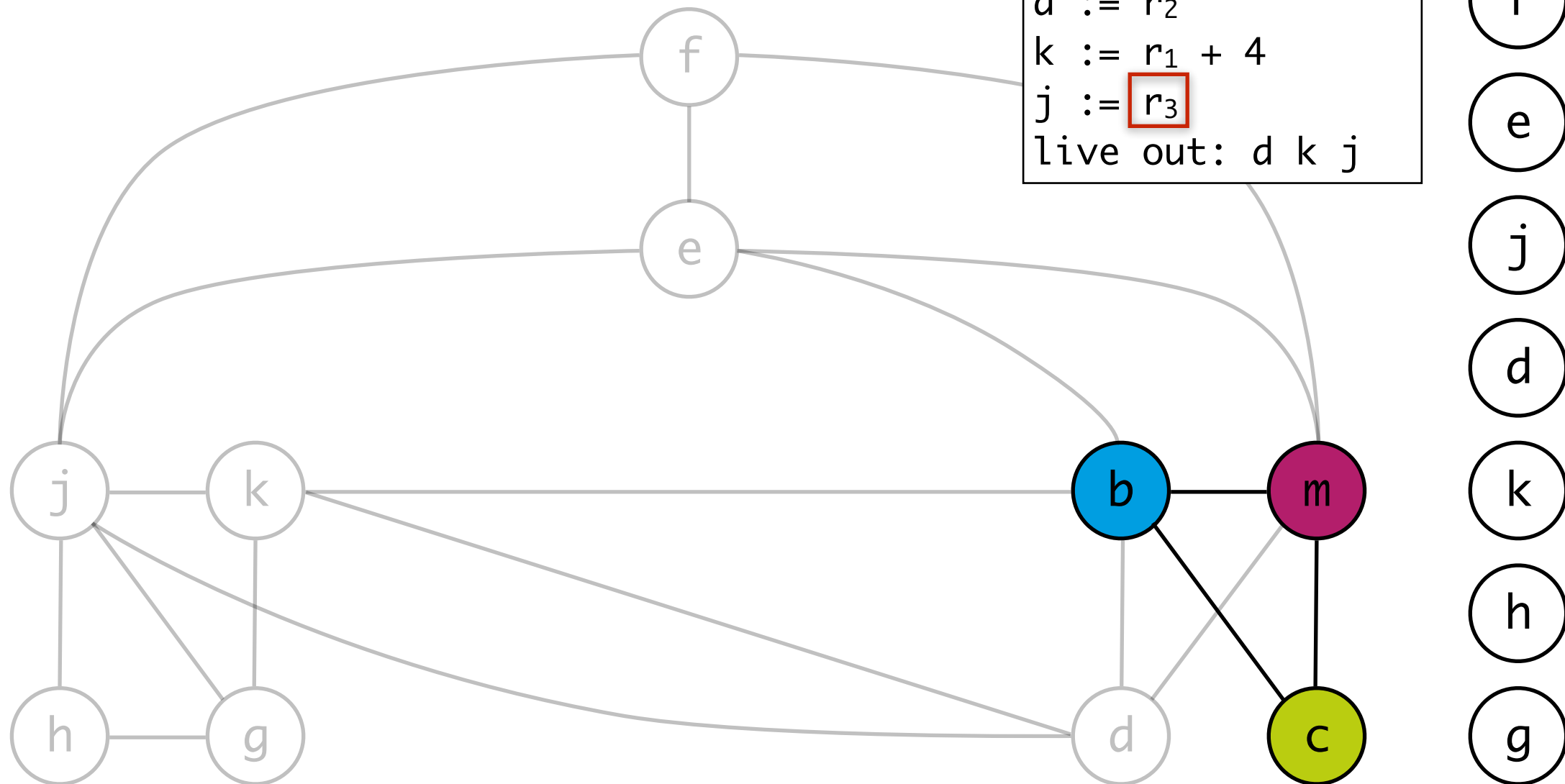
```
live-in: k j
g := mem[j + 12]
h := k - 1
f := g * h
e := mem[j + 8]
r1 := mem[j + 16]
b := mem[f]
r2 := e + 8
d := r2
k := r1 + 4
j := b
live out: d k j
```



# Graph Coloring

example with 4 colors

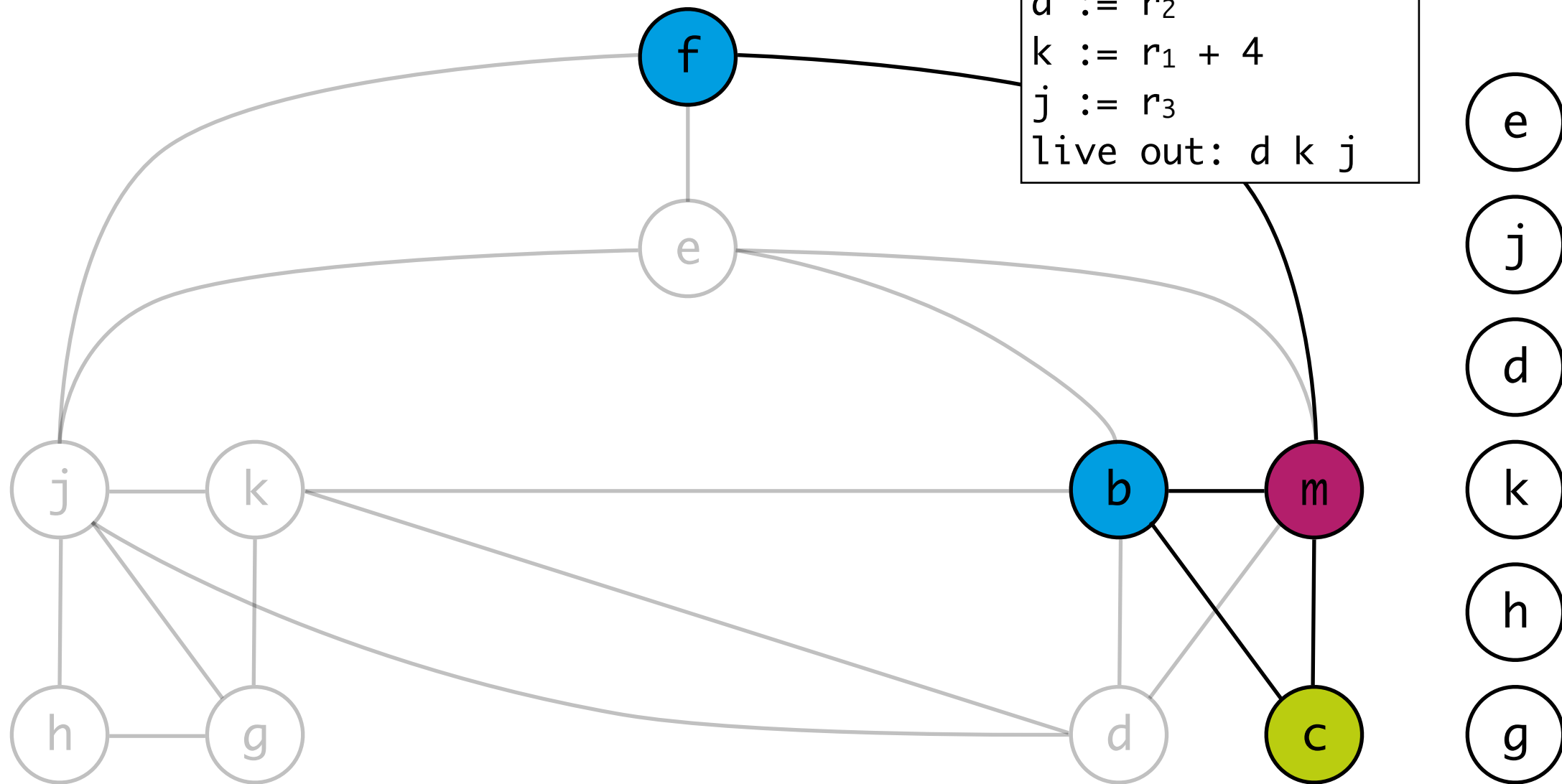
```
live-in: k j
g := mem[j + 12]
h := k - 1
f := g * h
e := mem[j + 8]
r1 := mem[j + 16]
r3 := mem[f]
r2 := e + 8
d := r2
k := r1 + 4
j := r3
live out: d k j
```



# Graph Coloring

example with 4 colors

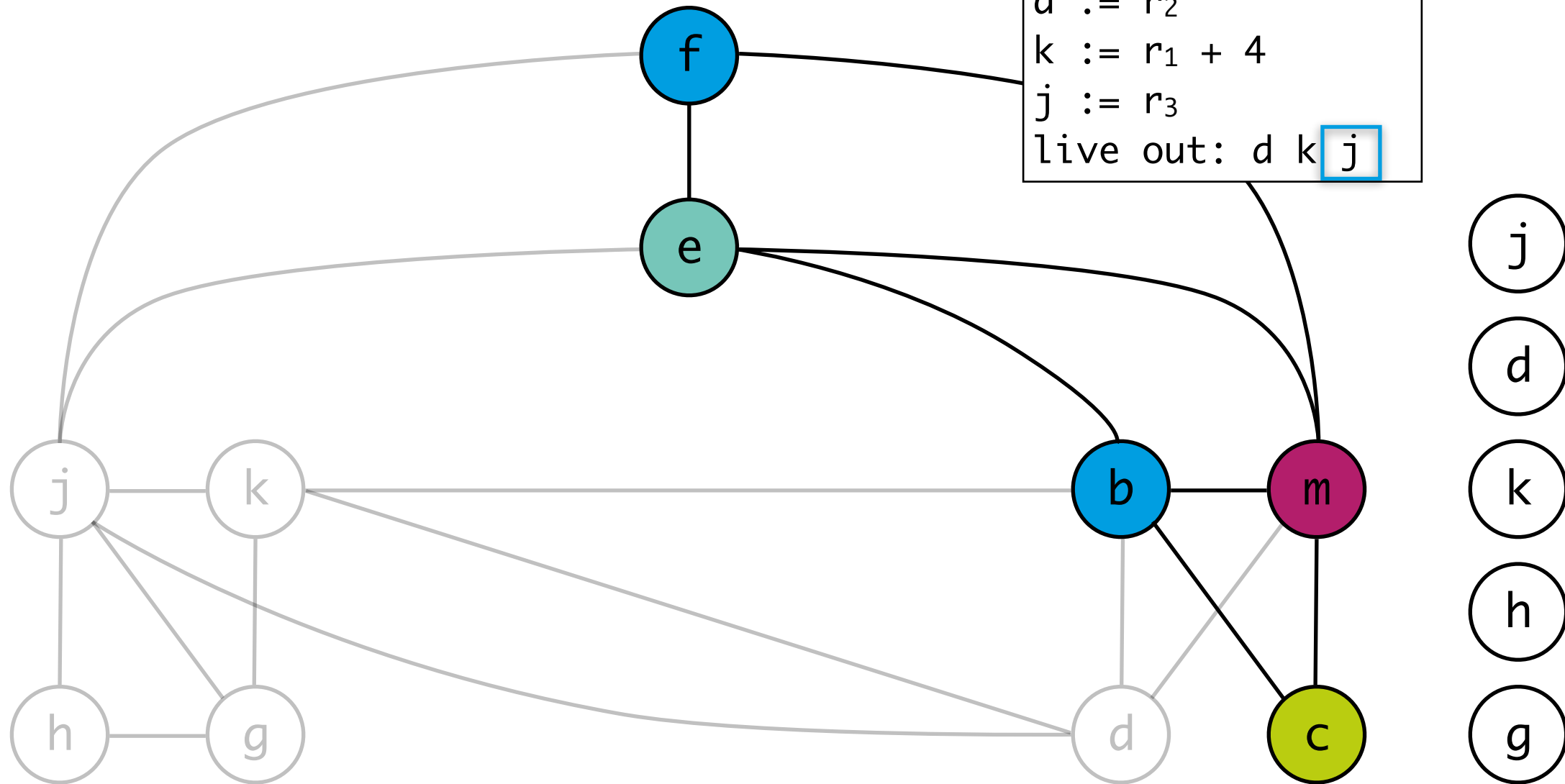
```
live-in: k j  
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e := mem[j + 8]  
r1 := mem[j + 16]  
r3 := mem[r3]  
r2 := e + 8  
d := r2  
k := r1 + 4  
j := r3  
live out: d k j
```



# Graph Coloring

example with 4 colors

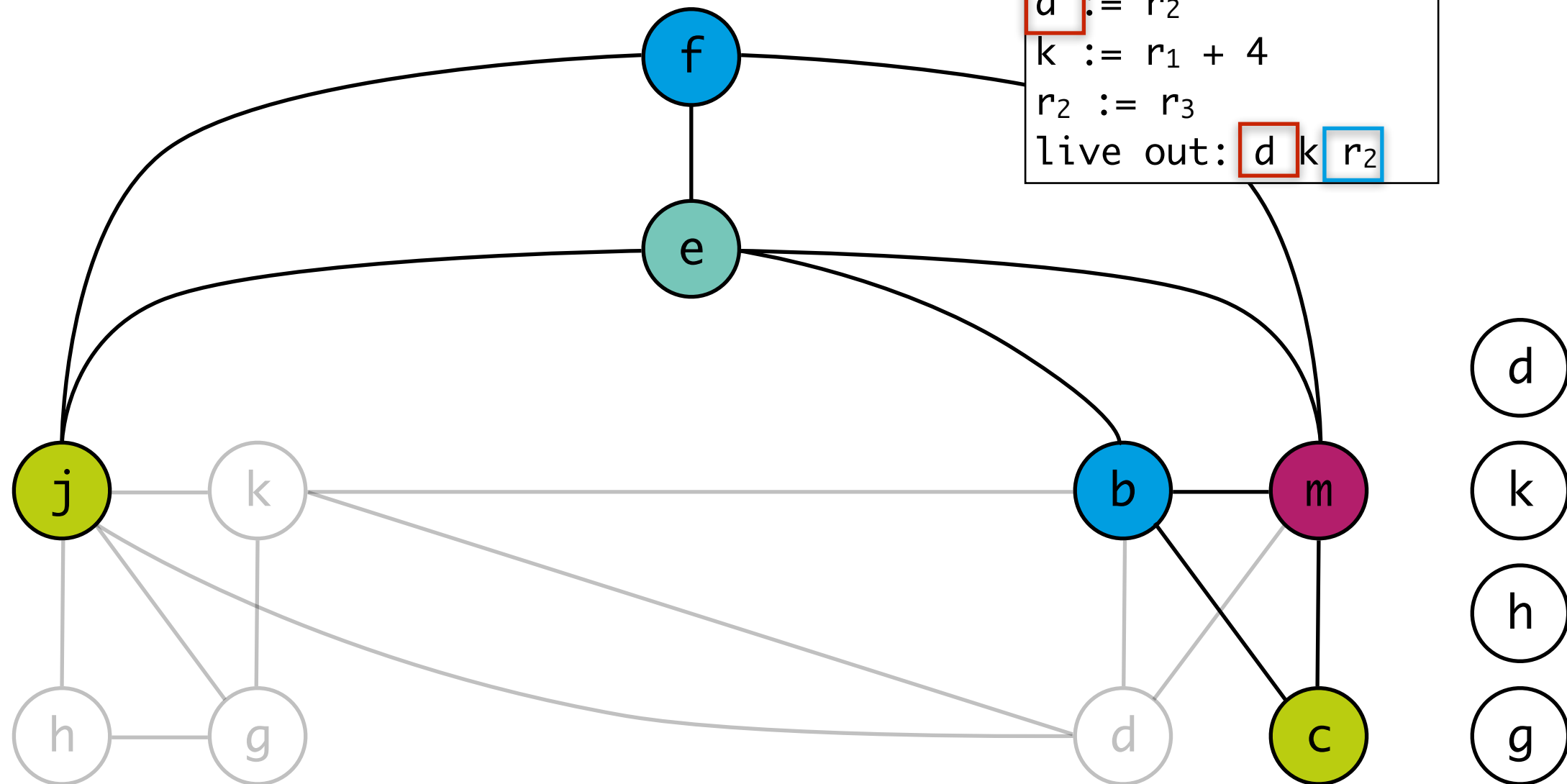
```
live-in: k j  
g := mem[j + 12]  
h := k - 1  
r3 := g * h  
r4 := mem[j + 8]  
r1 := mem[j + 16]  
r3 := mem[r3]  
r2 := r4 + 8  
d := r2  
k := r1 + 4  
j := r3  
live out: d k j
```



# Graph Coloring

example with 4 colors

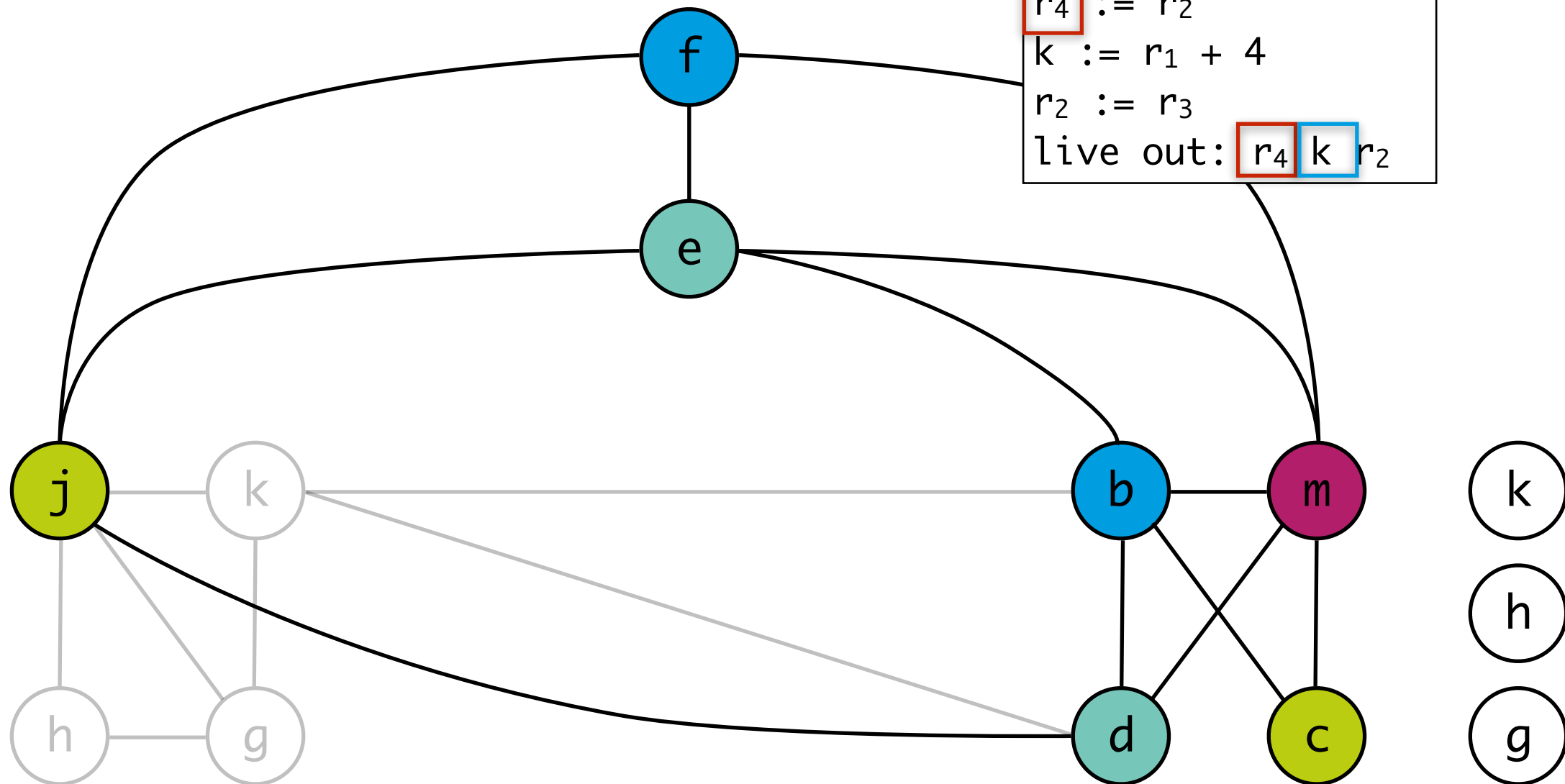
```
live-in: k r2
g := mem[r2 + 12]
h := k - 1
r3 := g * h
r4 := mem[r2 + 8]
r1 := mem[r2 + 16]
r3 := mem[r3]
r2 := r4 + 8
d := r2
k := r1 + 4
r2 := r3
live out: d k r2
```



# Graph Coloring

example with 4 colors

```
live-in: k r2  
g := mem[r2 + 12]  
h := k - 1  
r3 := g * h  
r4 := mem[r2 + 8]  
r1 := mem[r2 + 16]  
r3 := mem[r3]  
r2 := r4 + 8  
r4 := r2  
k := r1 + 4  
r2 := r3  
live out: r4 k r2
```

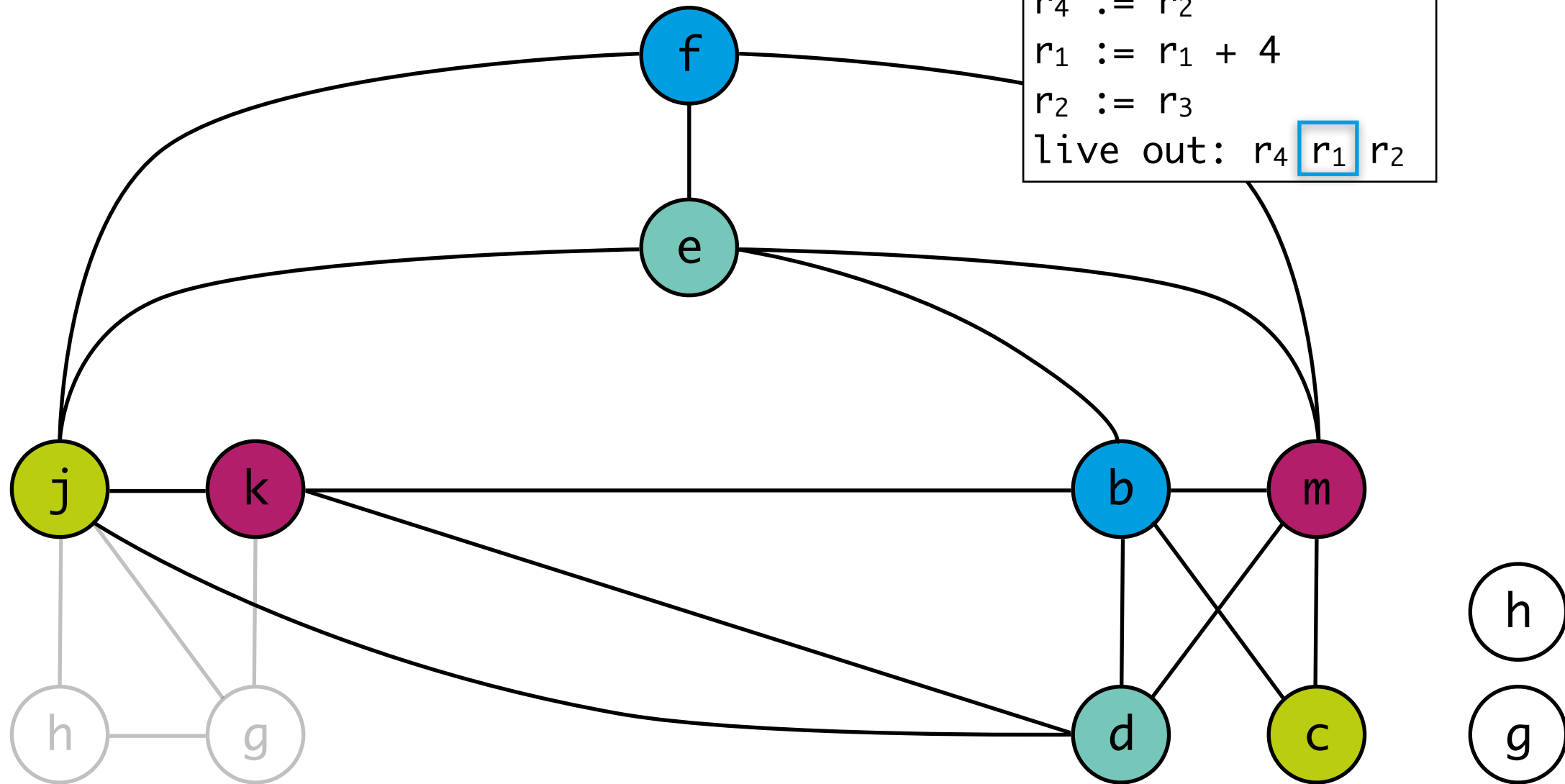




# Graph Coloring

example with 4 colors

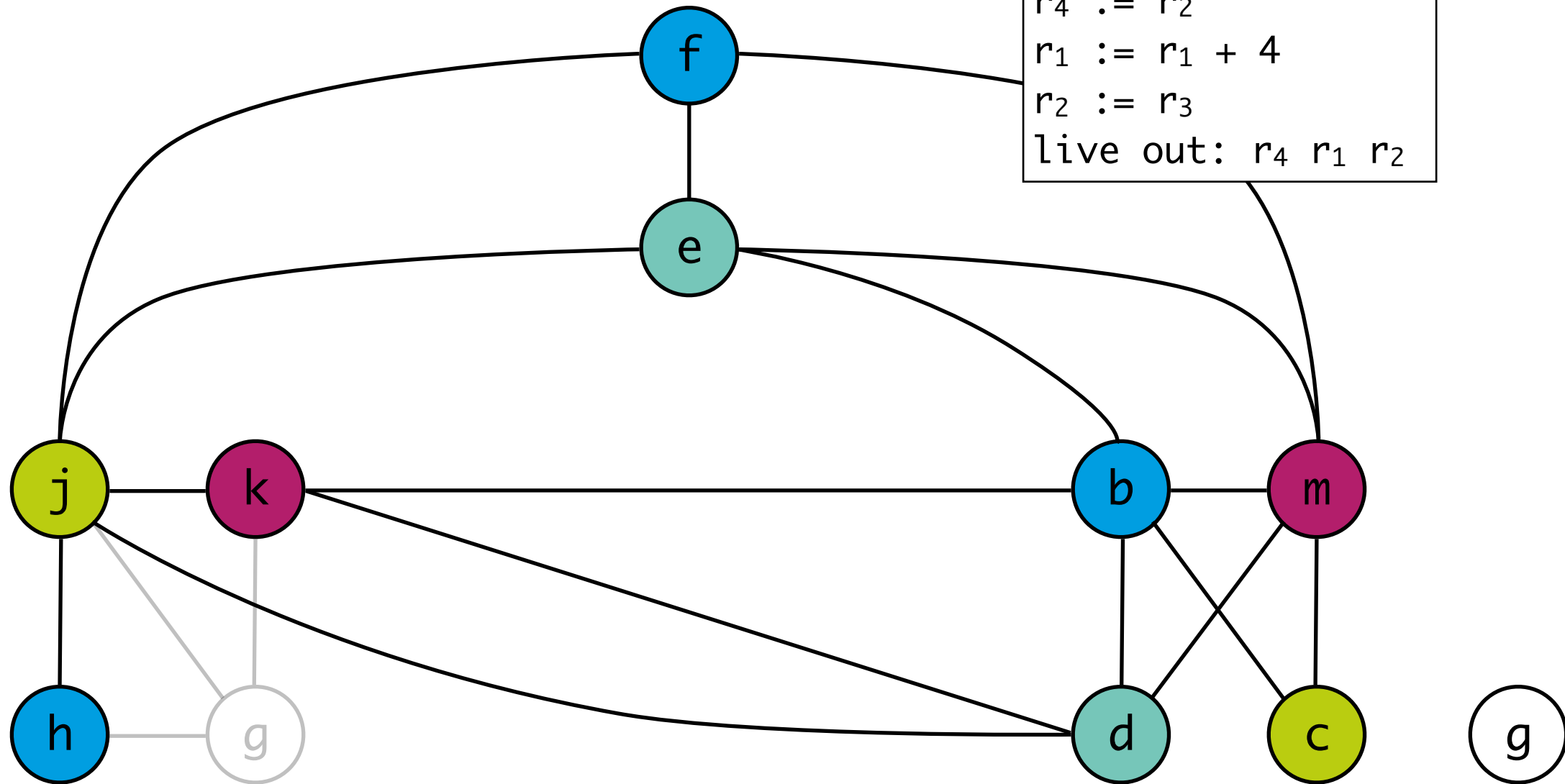
```
live-in: r1 r2
g := mem[r2 + 12]
h := r1 - 1
r3 := g * h
r4 := mem[r2 + 8]
r1 := mem[r2 + 16]
r3 := mem[r3]
r2 := r4 + 8
r4 := r2
r1 := r1 + 4
r2 := r3
live out: r4 r1 r2
```



# Graph Coloring

example with 4 colors

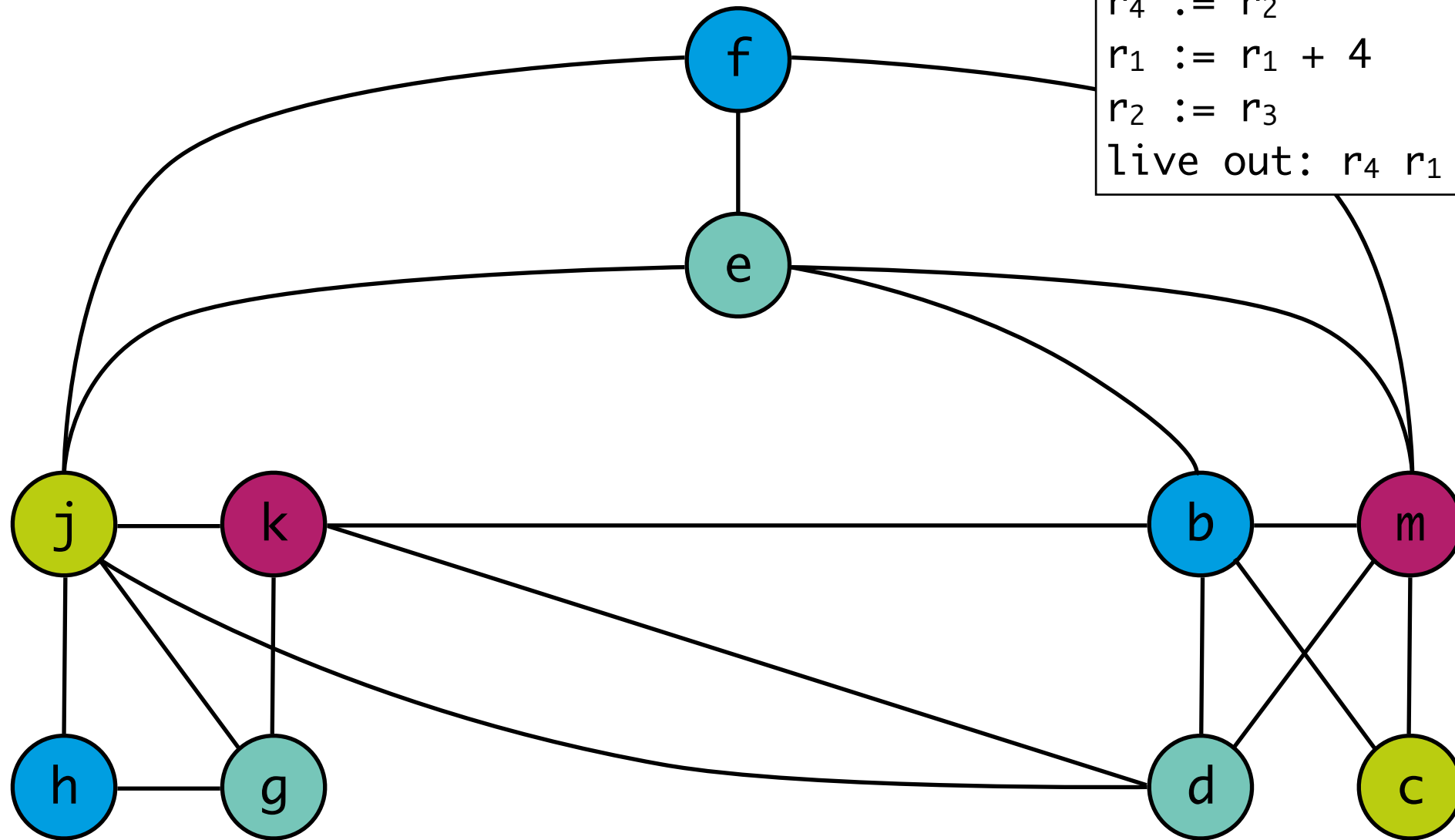
```
live-in: r1 r2  
g := mem[r2 + 12]  
r3 := r1 - 1  
r3 := g * r3  
r4 := mem[r2 + 8]  
r1 := mem[r2 + 16]  
r3 := mem[r3]  
r2 := r4 + 8  
r4 := r2  
r1 := r1 + 4  
r2 := r3  
live out: r4 r1 r2
```



# Graph Coloring

example with 4 colors

```
live-in: r1 r2  
r4 := mem[r2 + 12]  
r3 := r1 - 1  
r3 := r4 * r3  
r4 := mem[r2 + 8]  
r1 := mem[r2 + 16]  
r3 := mem[r3]  
r2 := r4 + 8  
r4 := r2  
r1 := r1 + 4  
r2 := r3  
live out: r4 r1 r2
```



# III

---

## Spilling

---

# Optimistic Coloring

## steps

### Simplify

remove node of **insignificant** degree (fewer than **k** edges)

### Spill

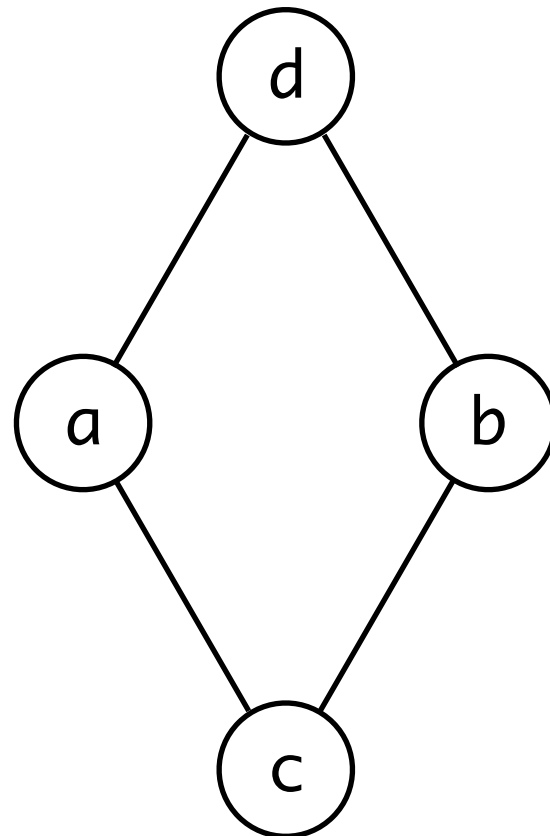
remove node of **significant** degree (**k** or more edges)

### Select

add node, select color

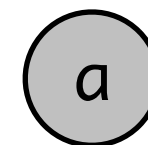
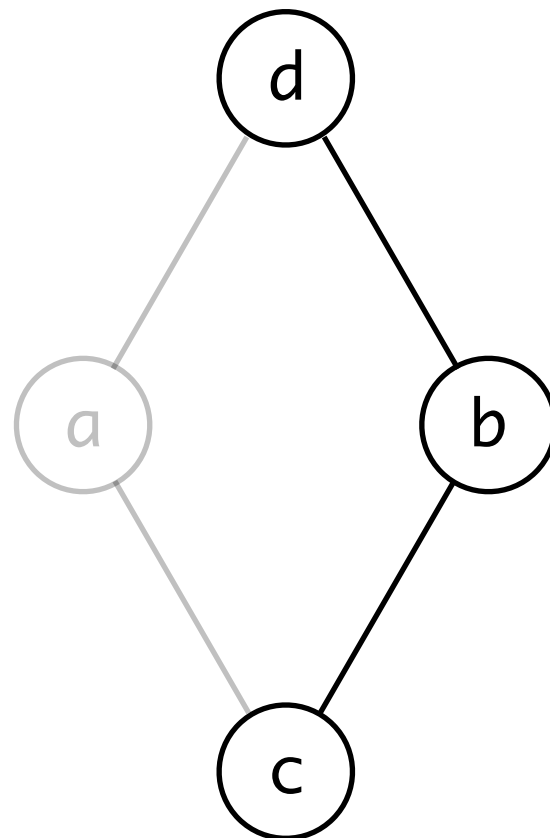
# Optimistic Coloring

example with 2 colors



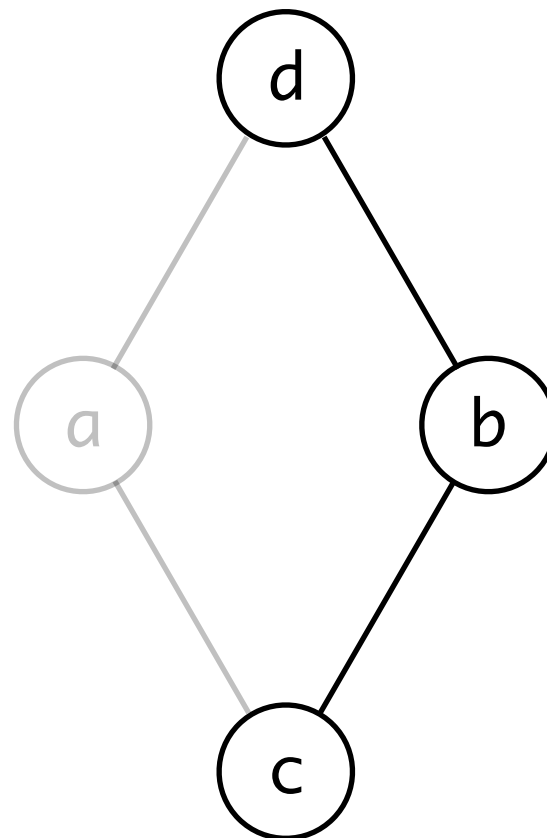
# Optimistic Coloring

example with 2 colors

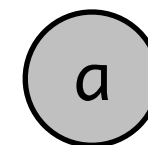


# Optimistic Coloring

example with 2 colors



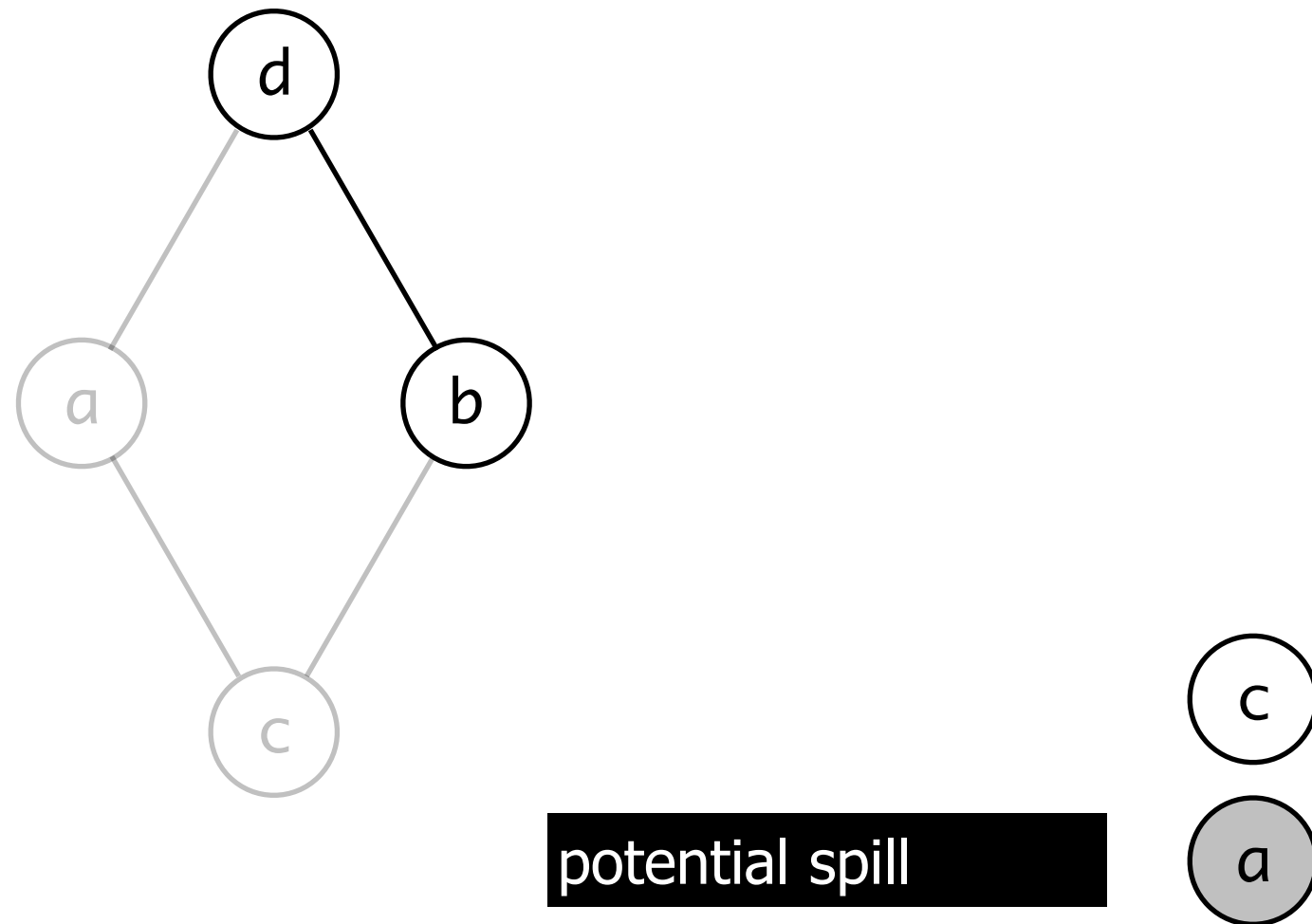
potential spill





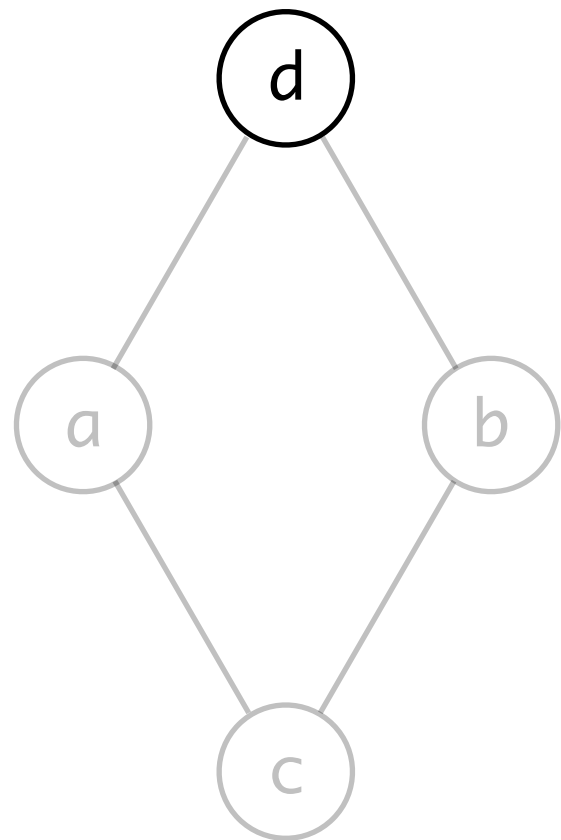
# Optimistic Coloring

example with 2 colors

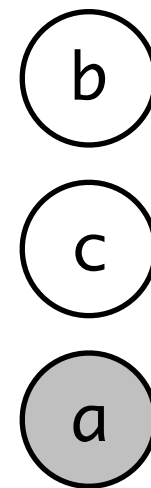


# Optimistic Coloring

example with 2 colors

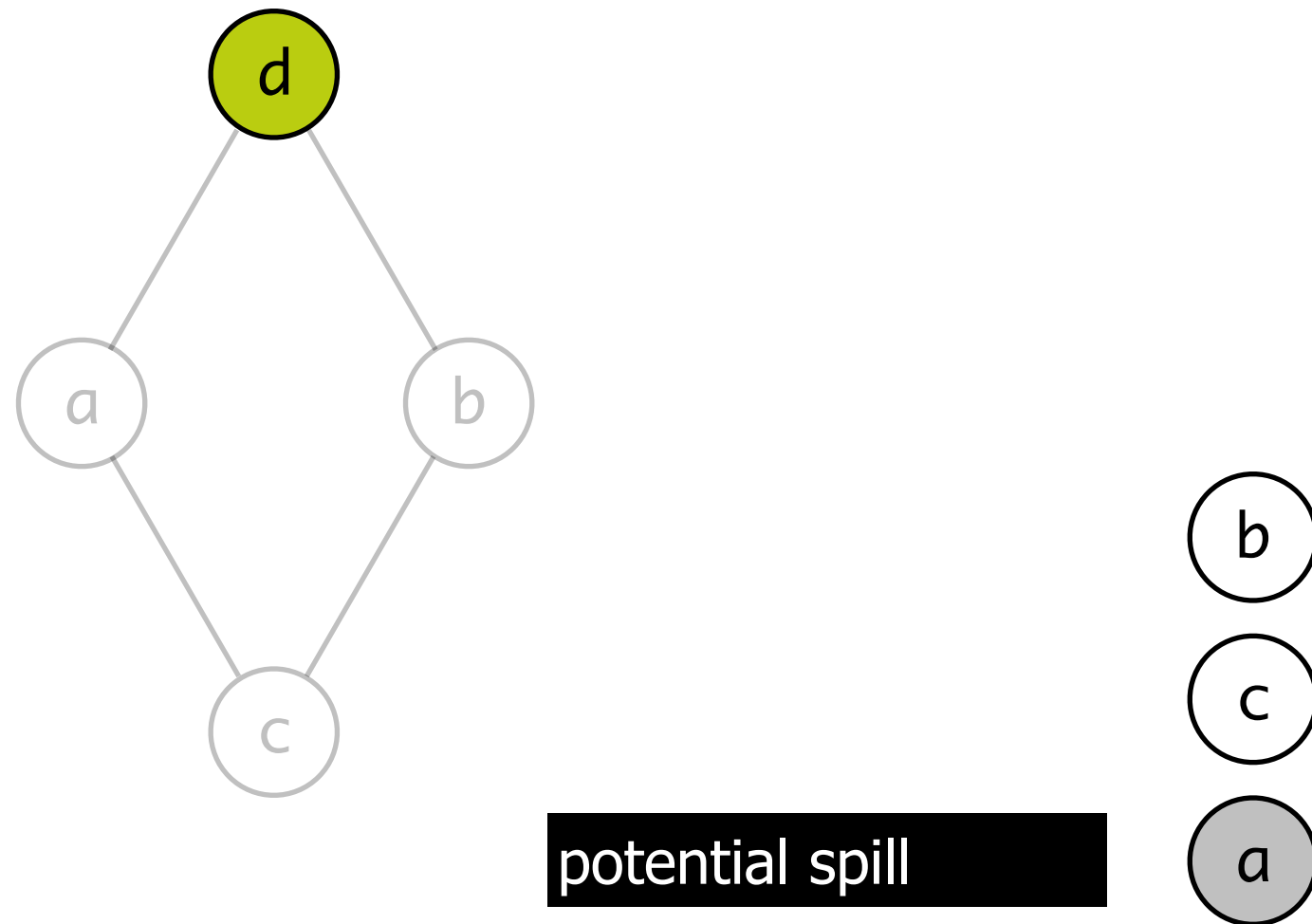


potential spill



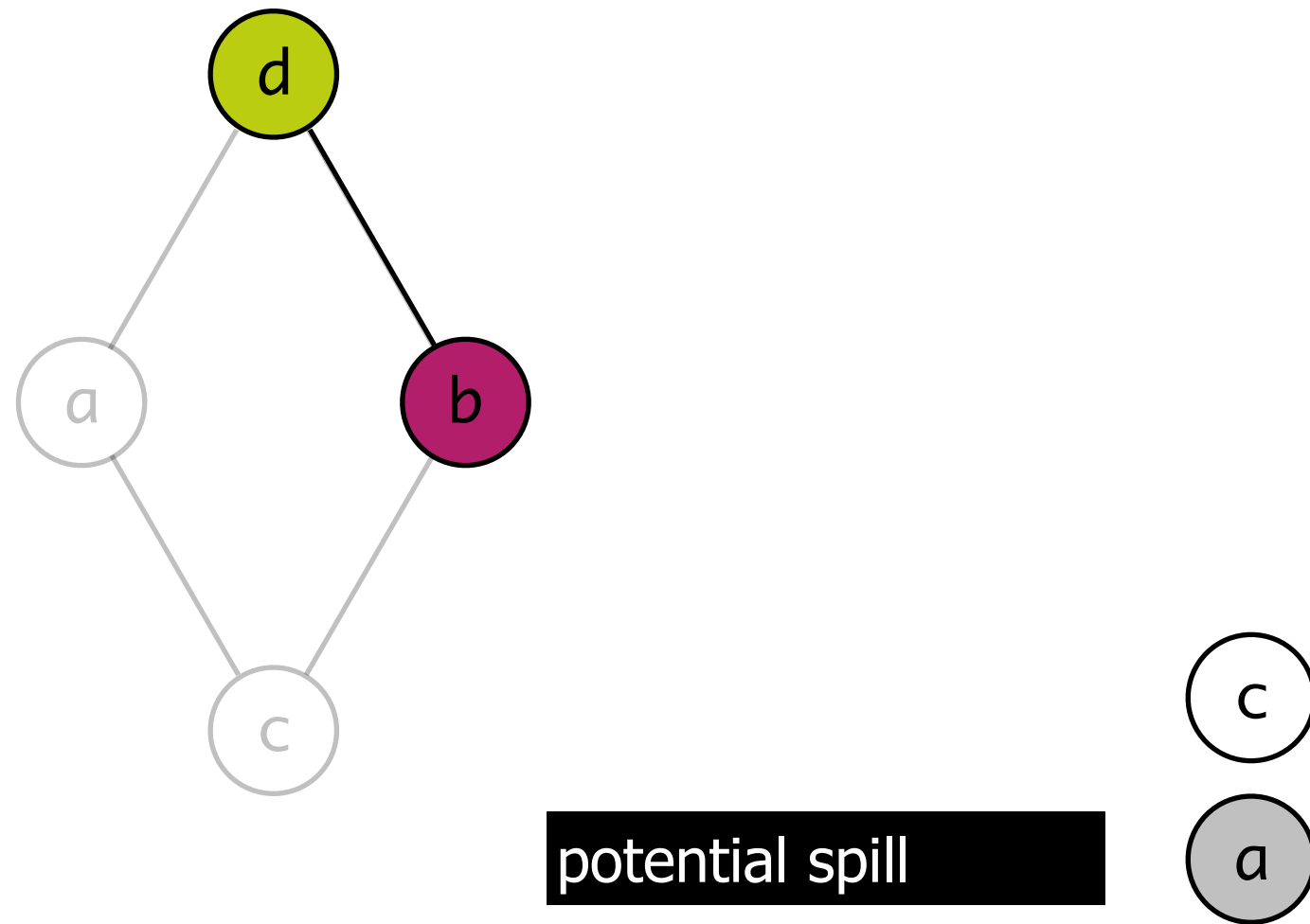
# Optimistic Coloring

example with 2 colors



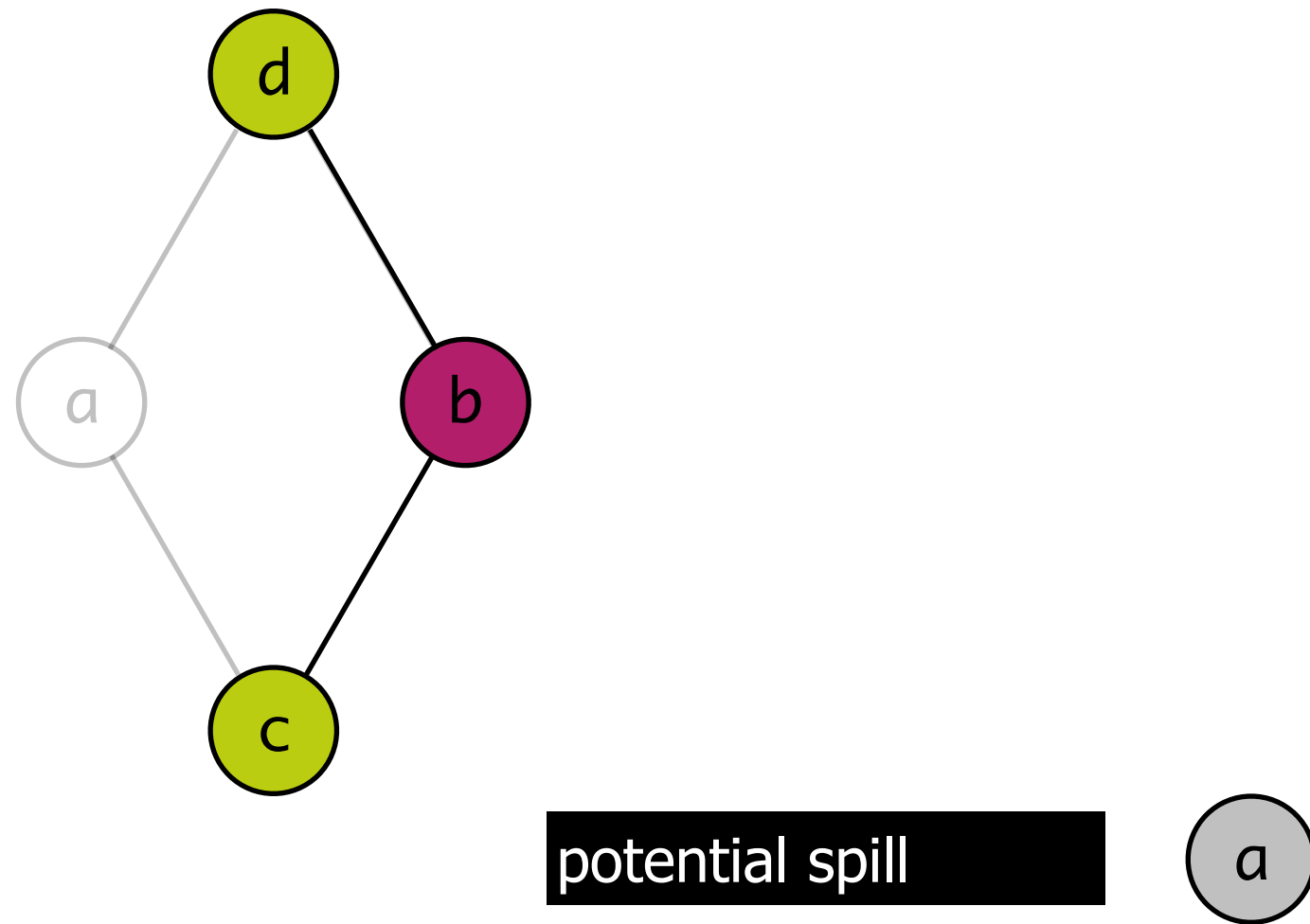
# Optimistic Coloring

example with 2 colors



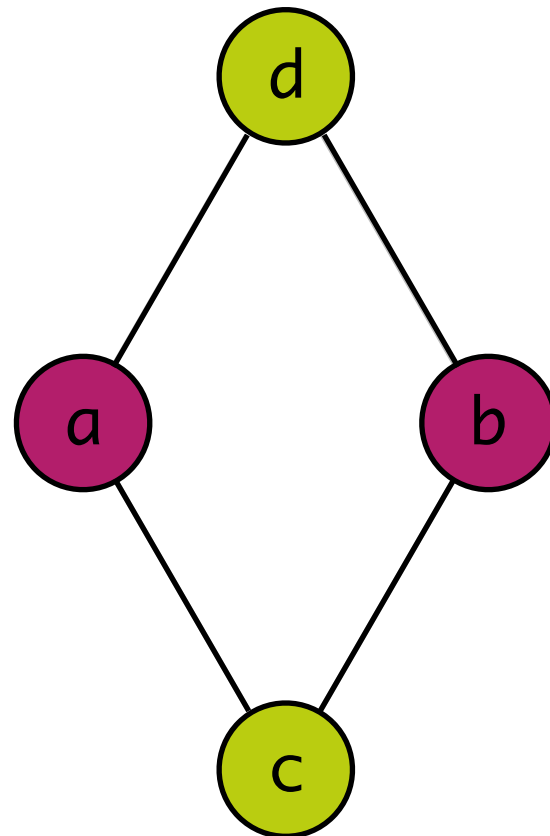
# Optimistic Coloring

example with 2 colors



# Optimistic Coloring

example with 2 colors



# Spilling

## steps

### Simplify

remove node of **insignificant** degree (less than **k** edges)

### Spill

remove node of **significant** degree (**k** or more edges)

### Select

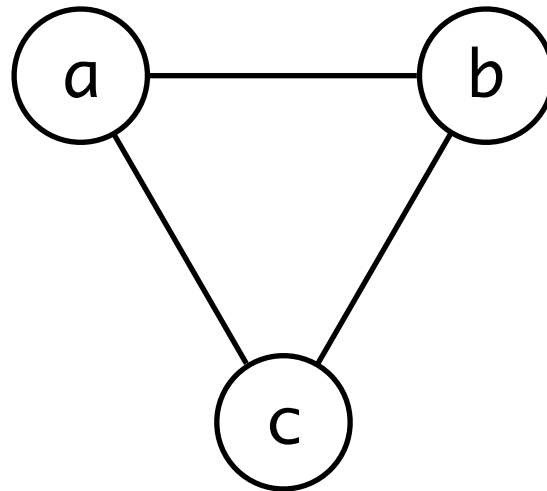
add node, select color

### Actual spill

### Start over

# Spilling

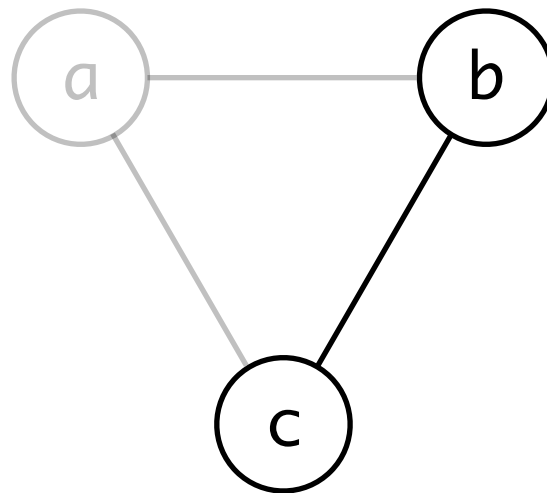
example with 2 colors



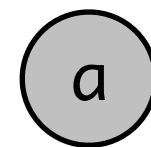


# Spilling

example with 2 colors

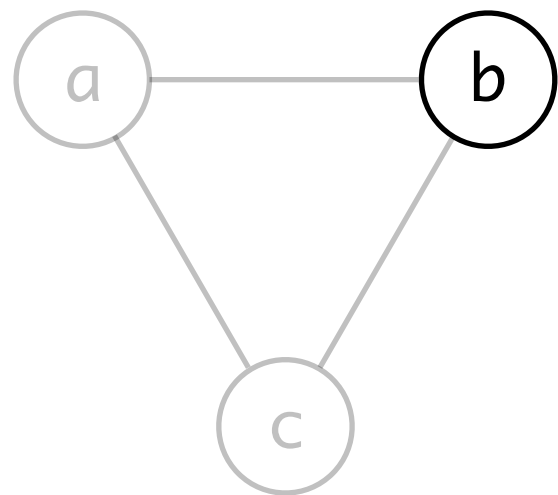


potential spill

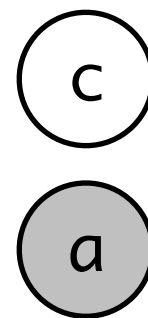


# Spilling

example with 2 colors

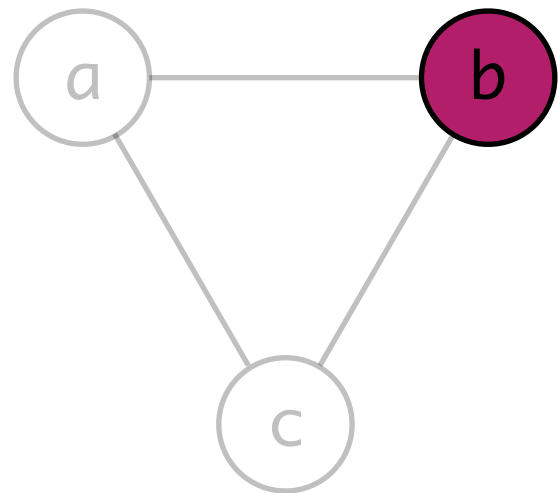


potential spill

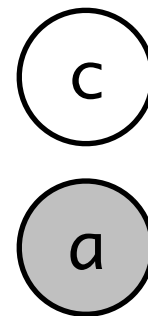


# Spilling

example with 2 colors

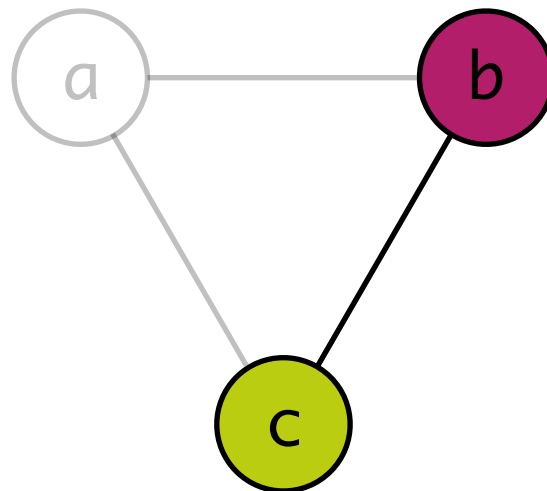


potential spill

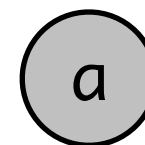


# Spilling

example with 2 colors

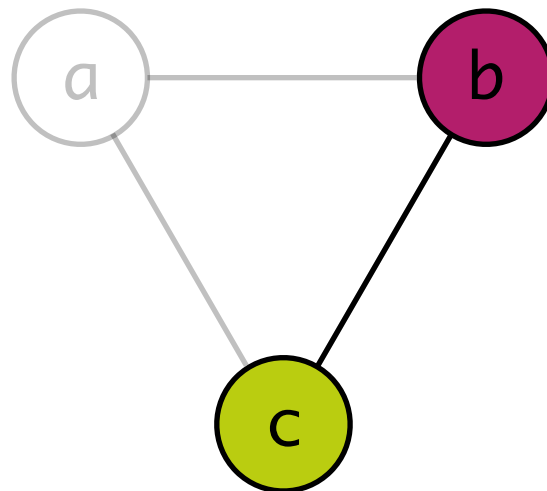


potential spill

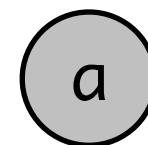


# Spilling

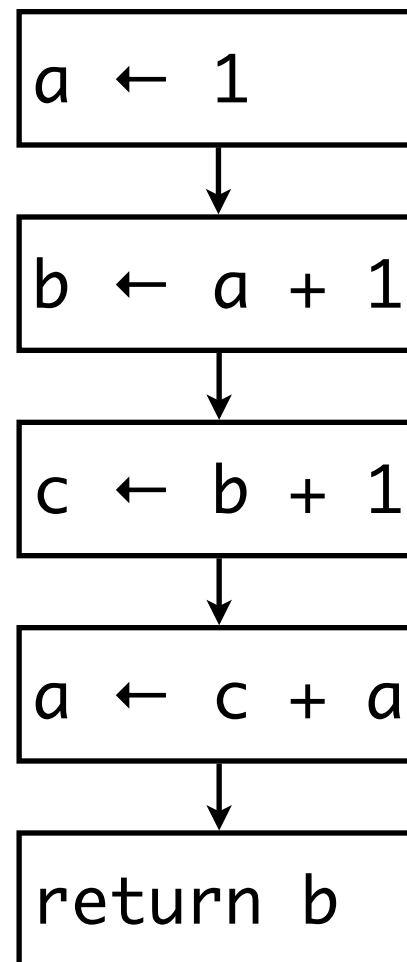
example with 2 colors



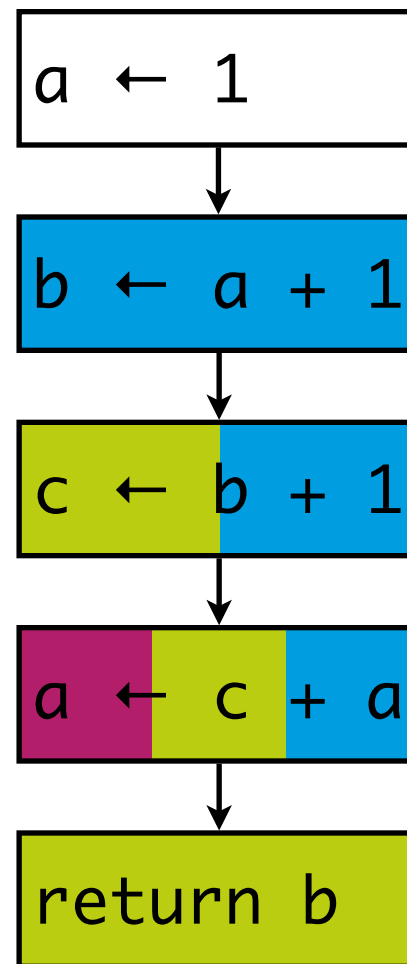
actual spill



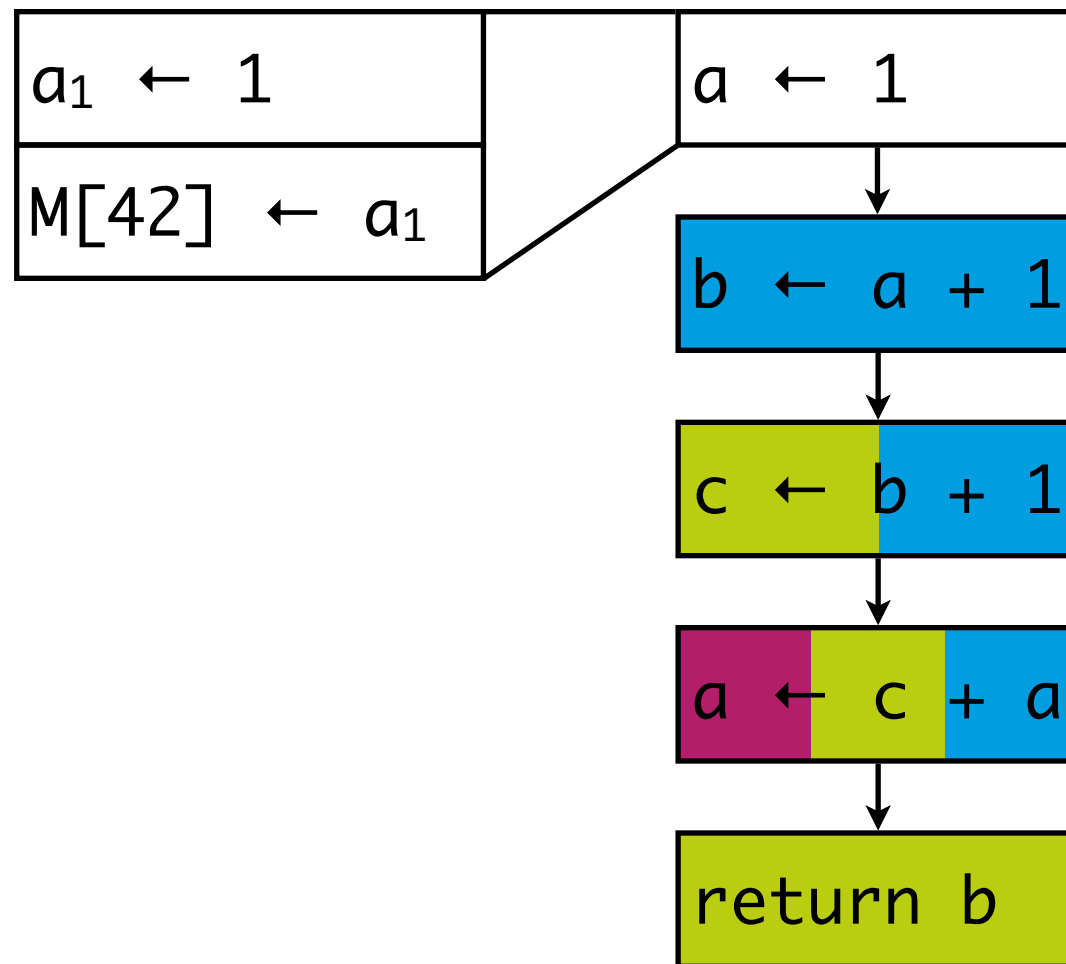
# Spilling example



# Spilling example

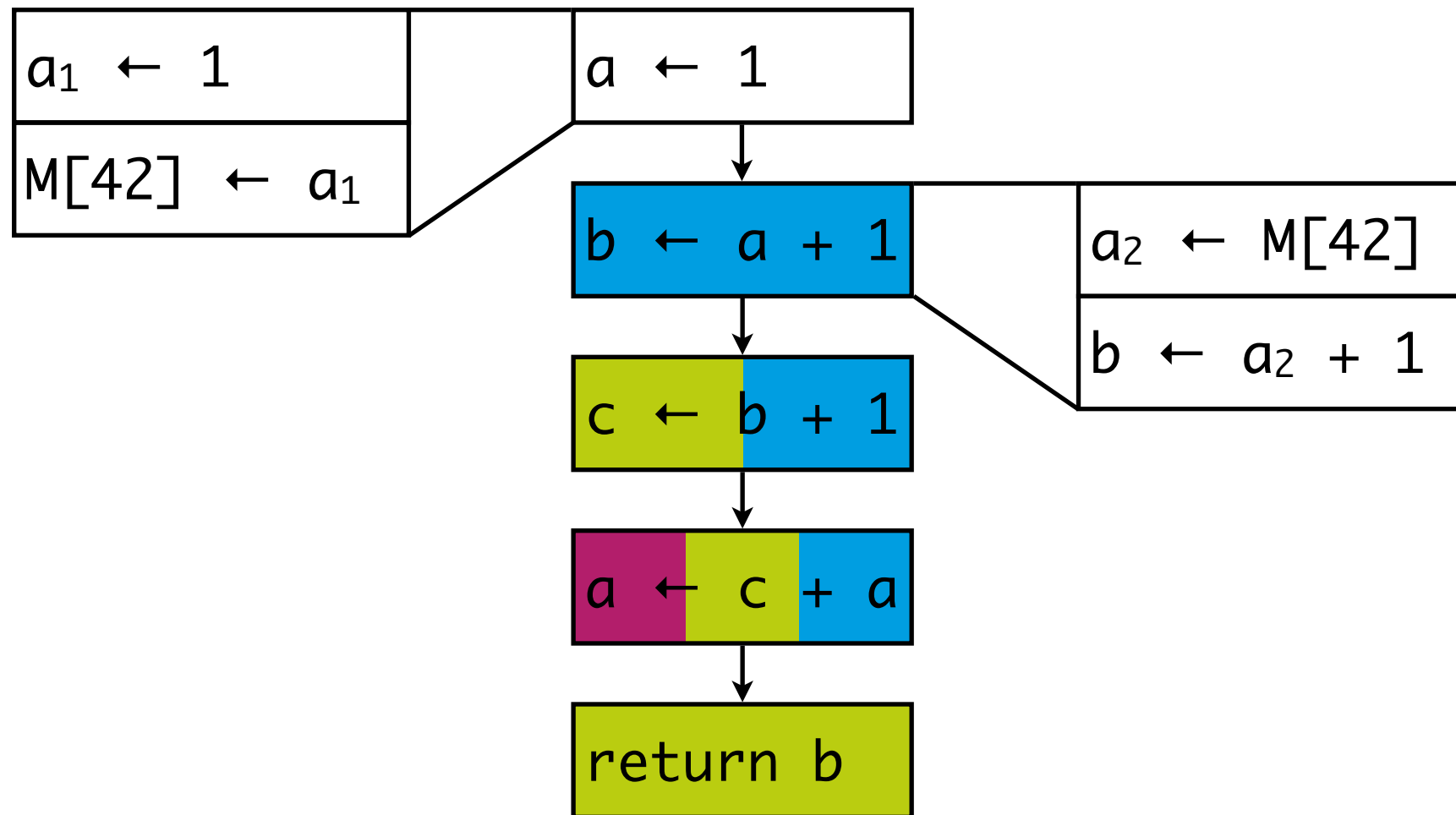


# Spilling example

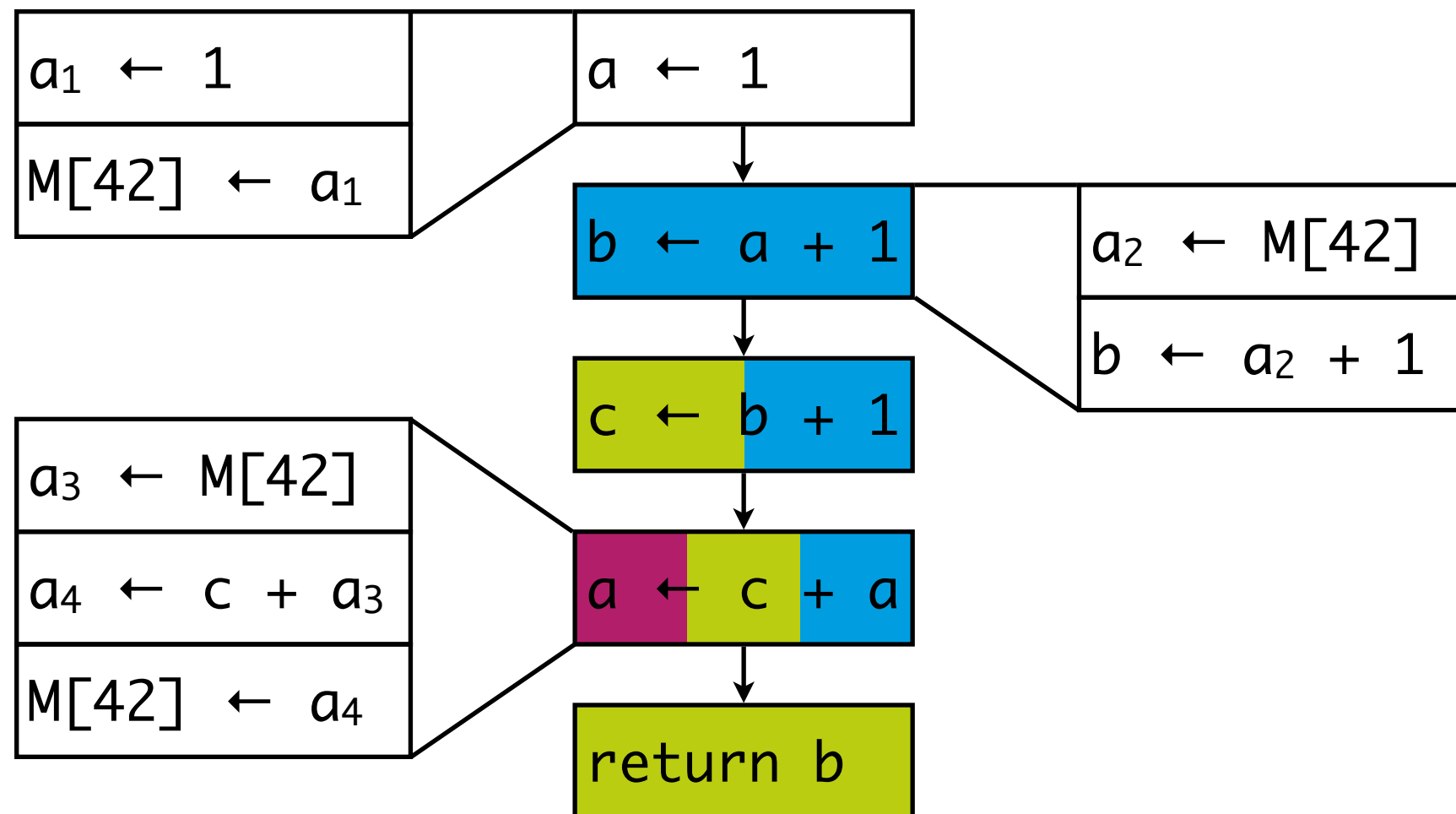




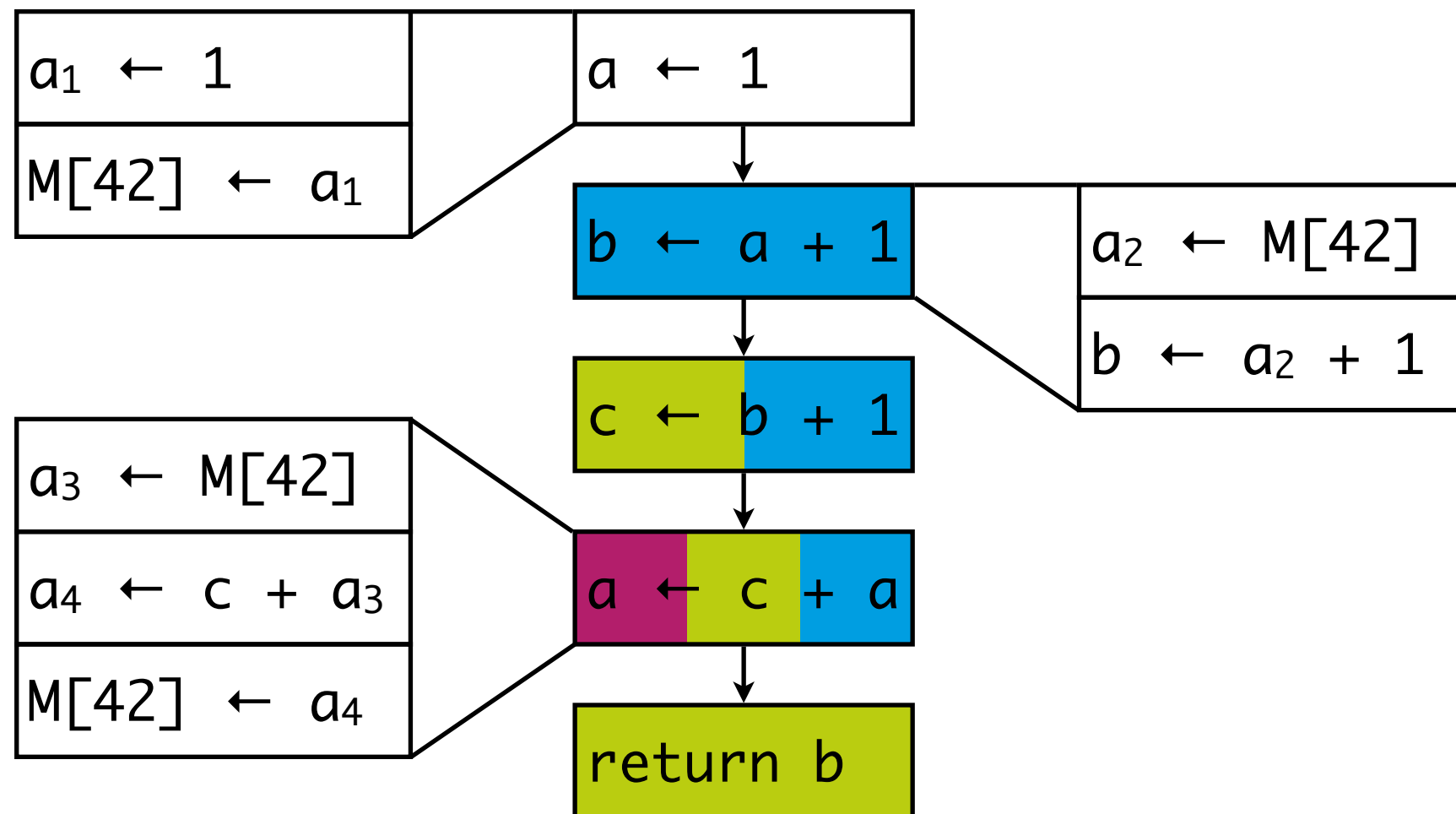
# Spilling example



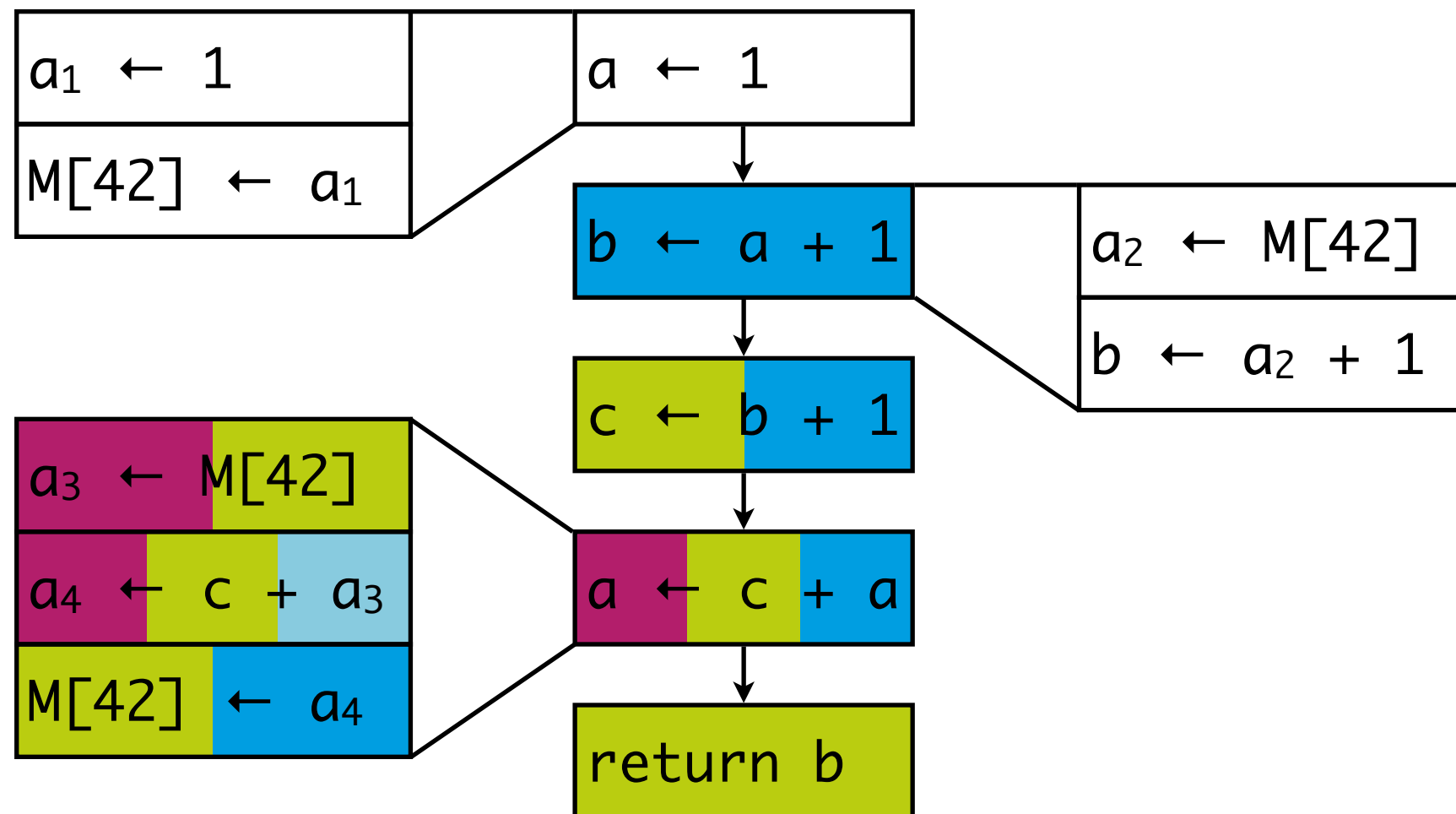
# Spilling example



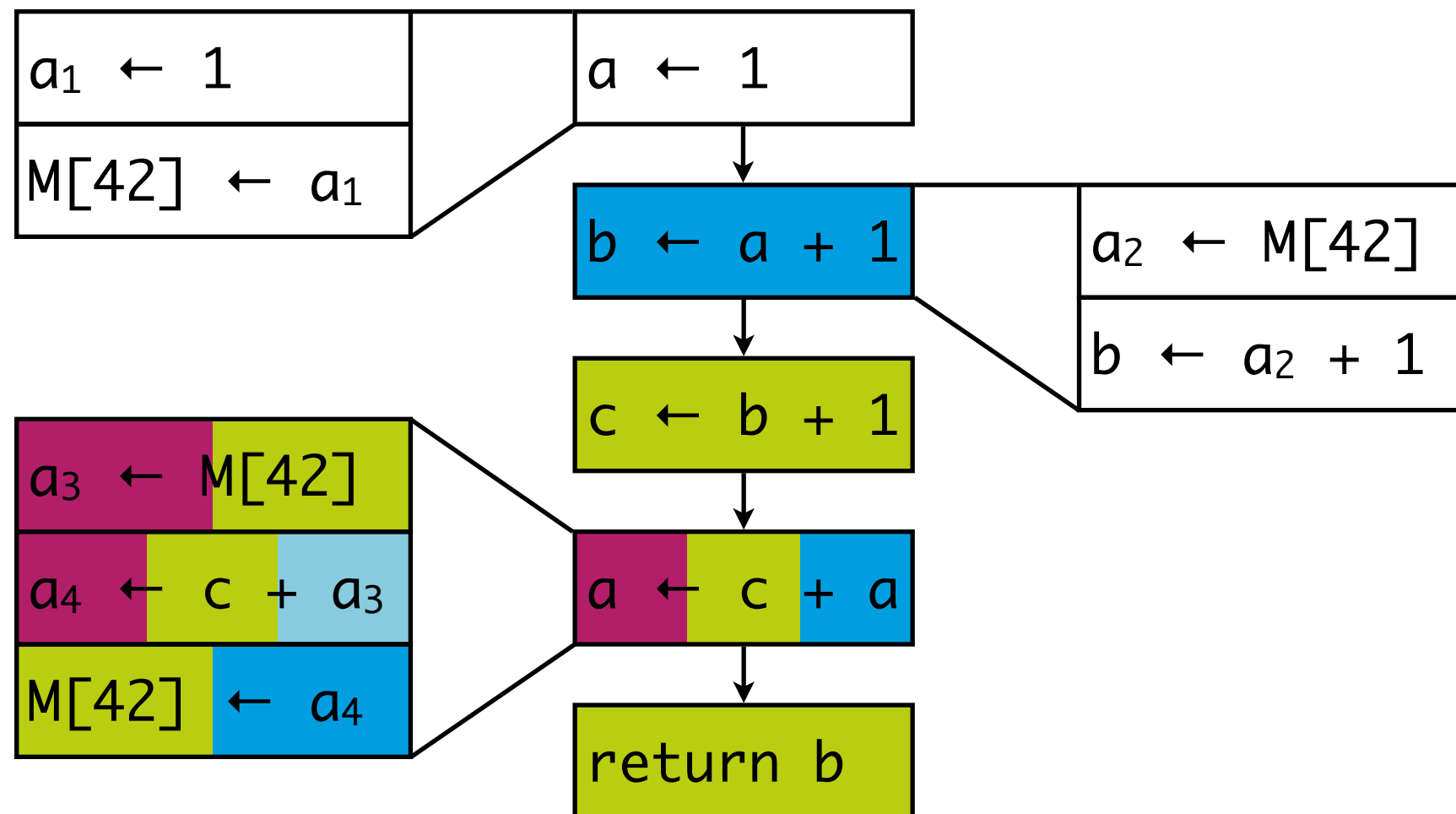
# Spilling example



# Spilling example

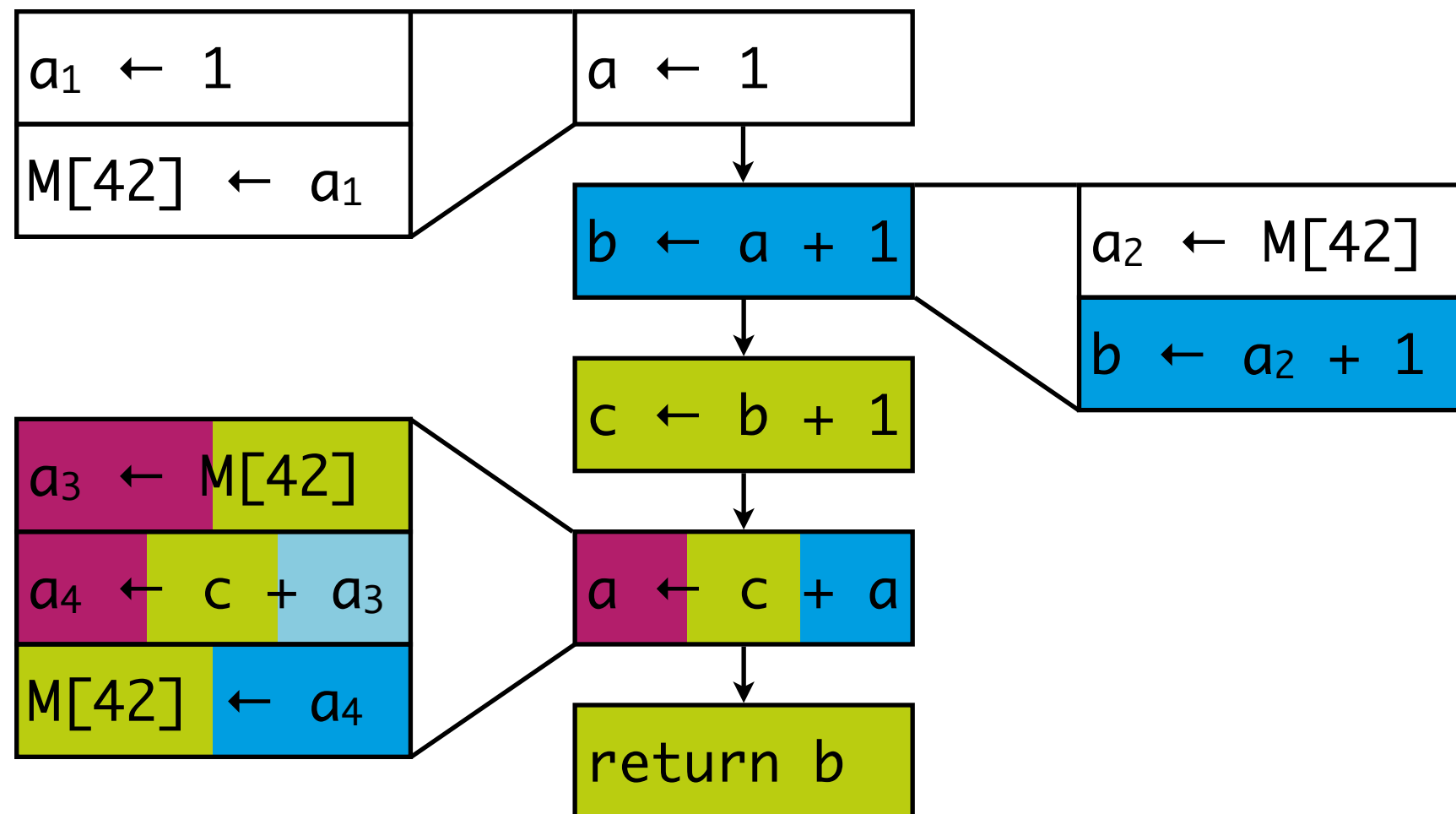


# Spilling example

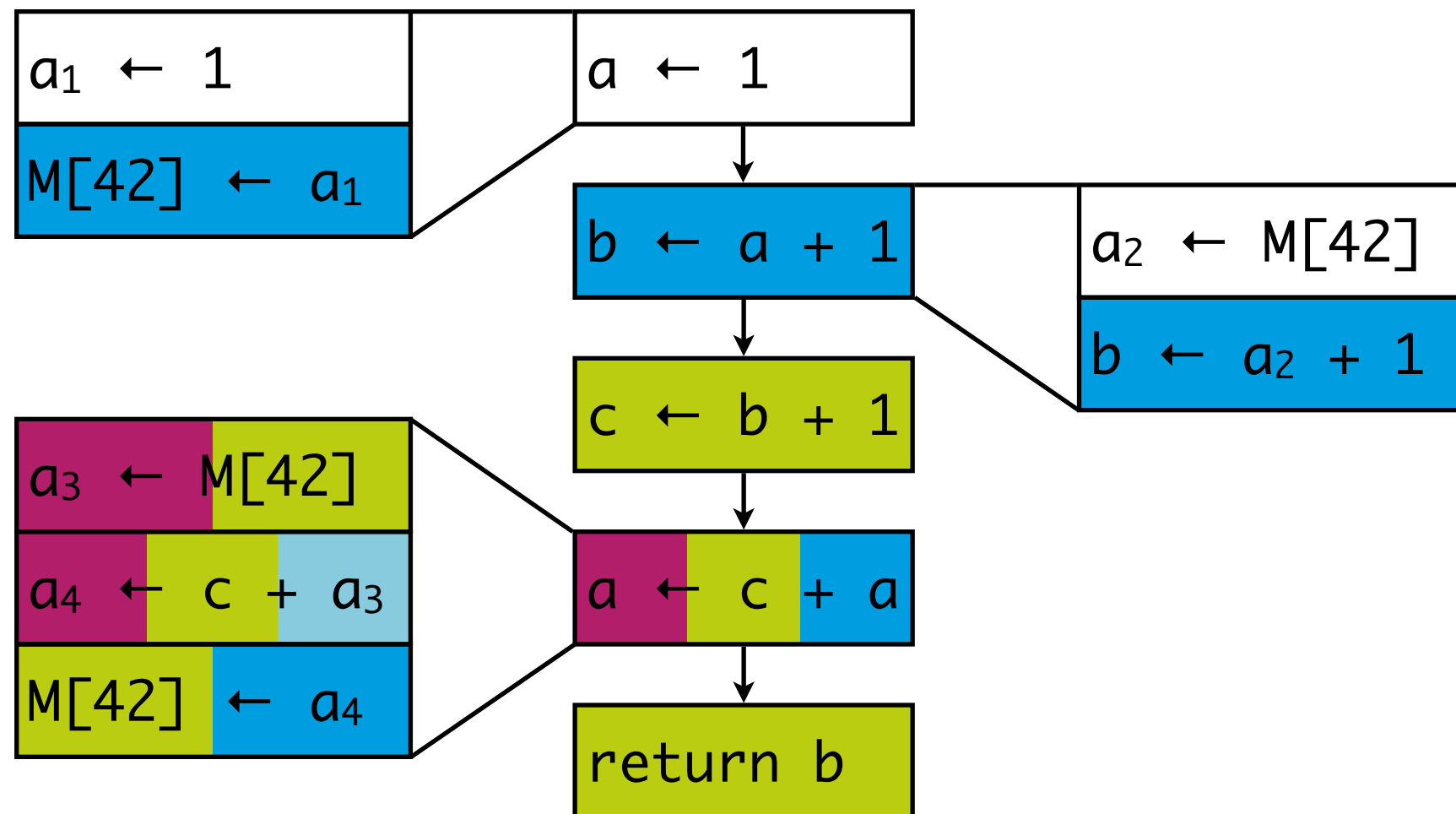


# Spilling

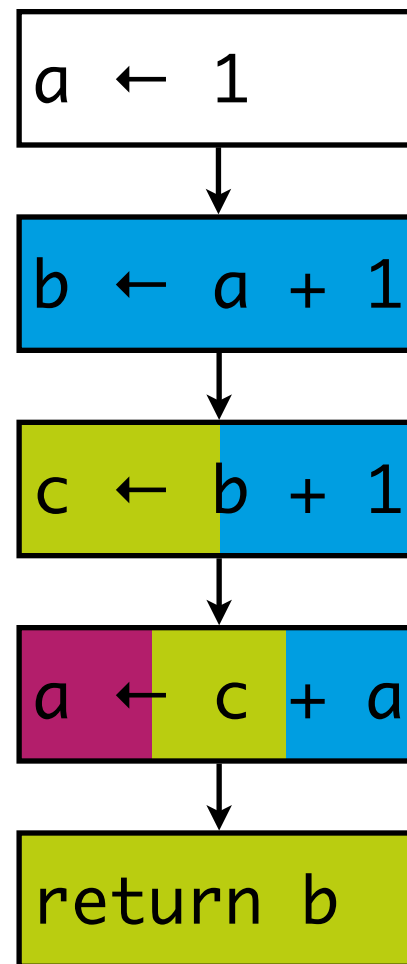
## example



# Spilling example

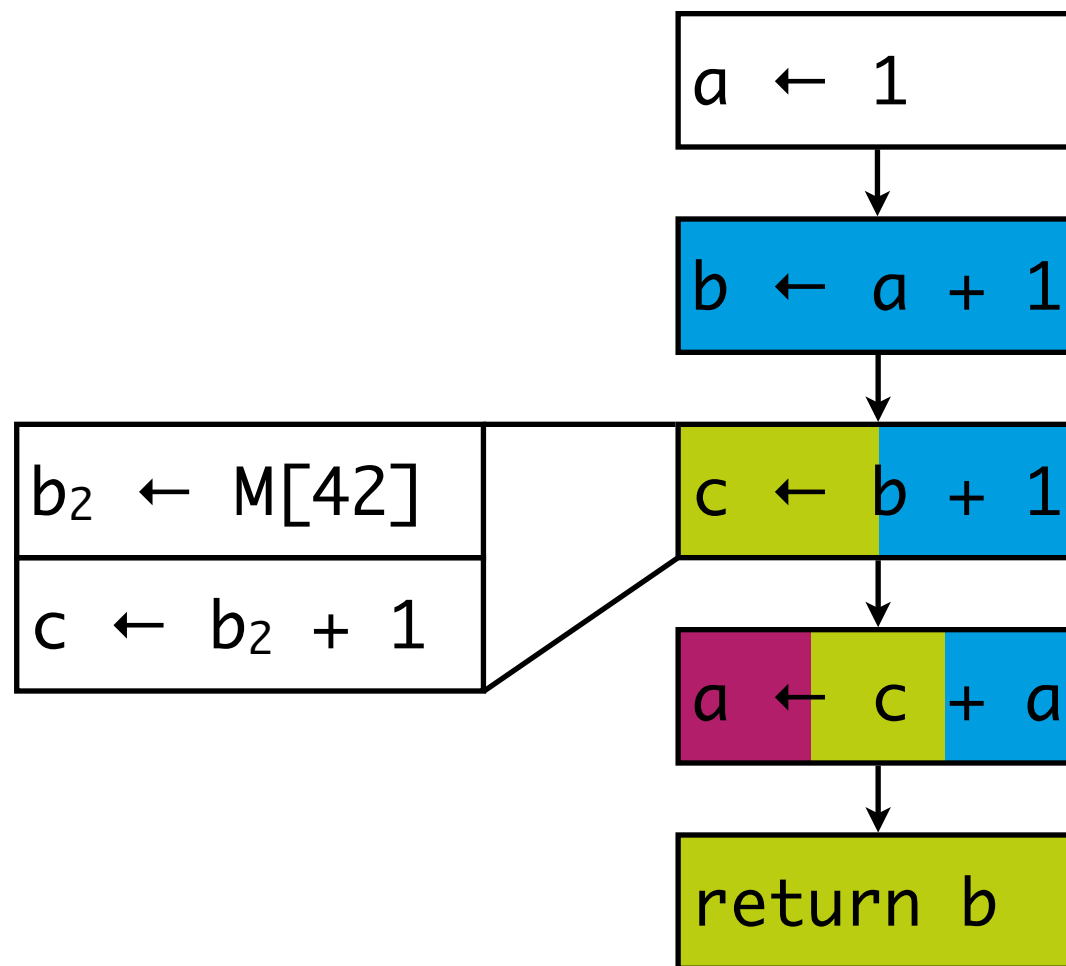


# Spilling example

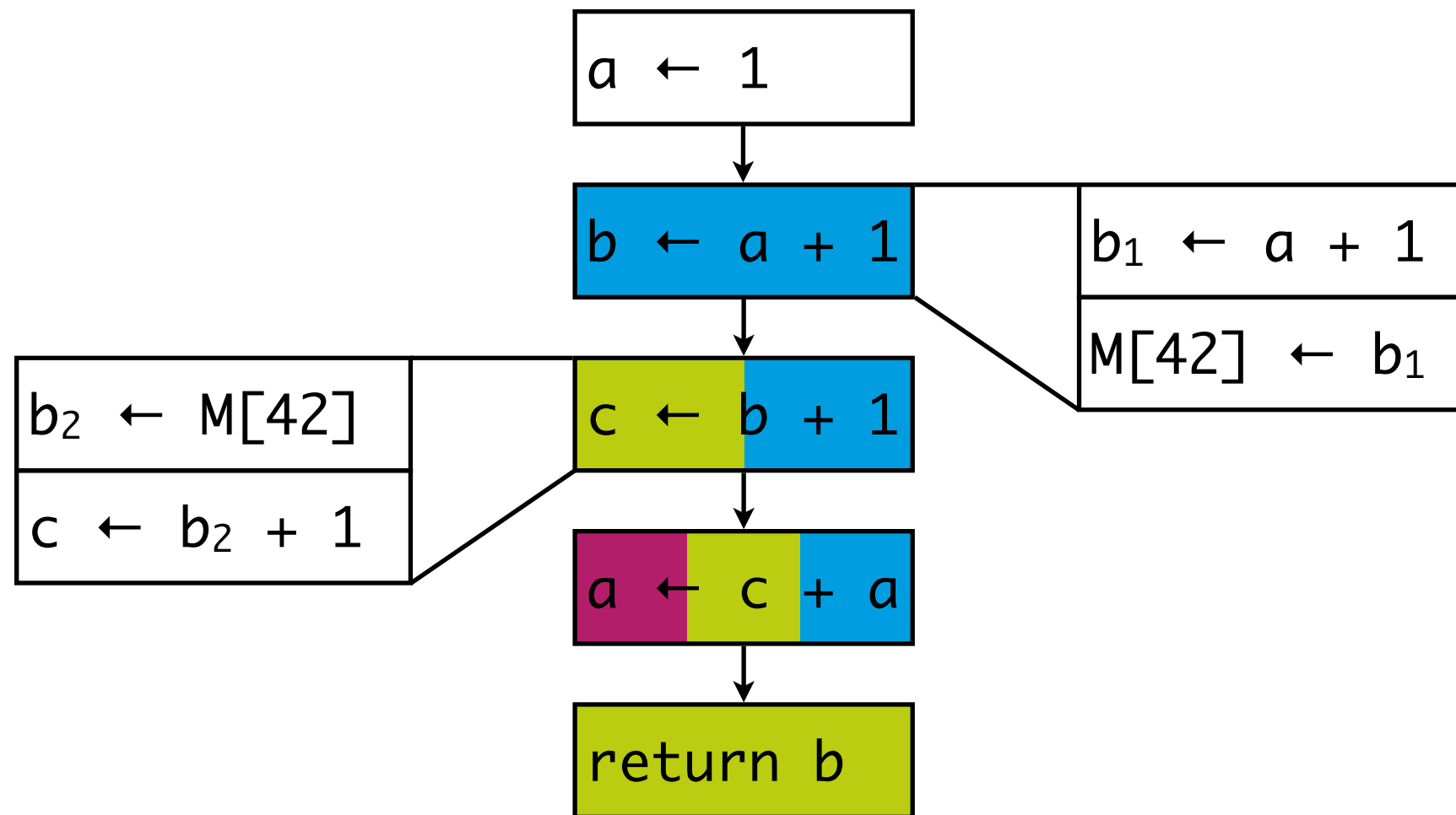




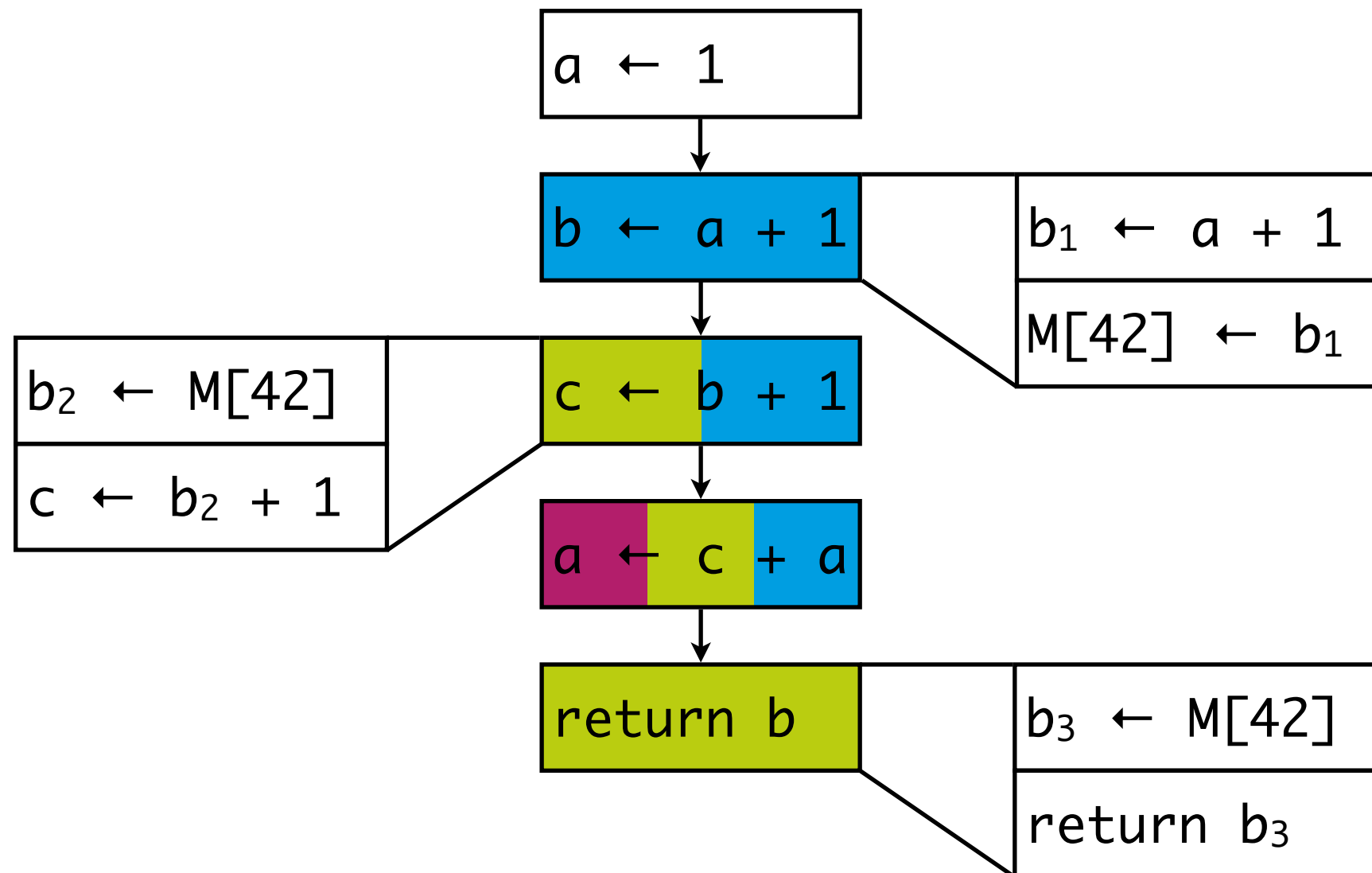
# Spilling example



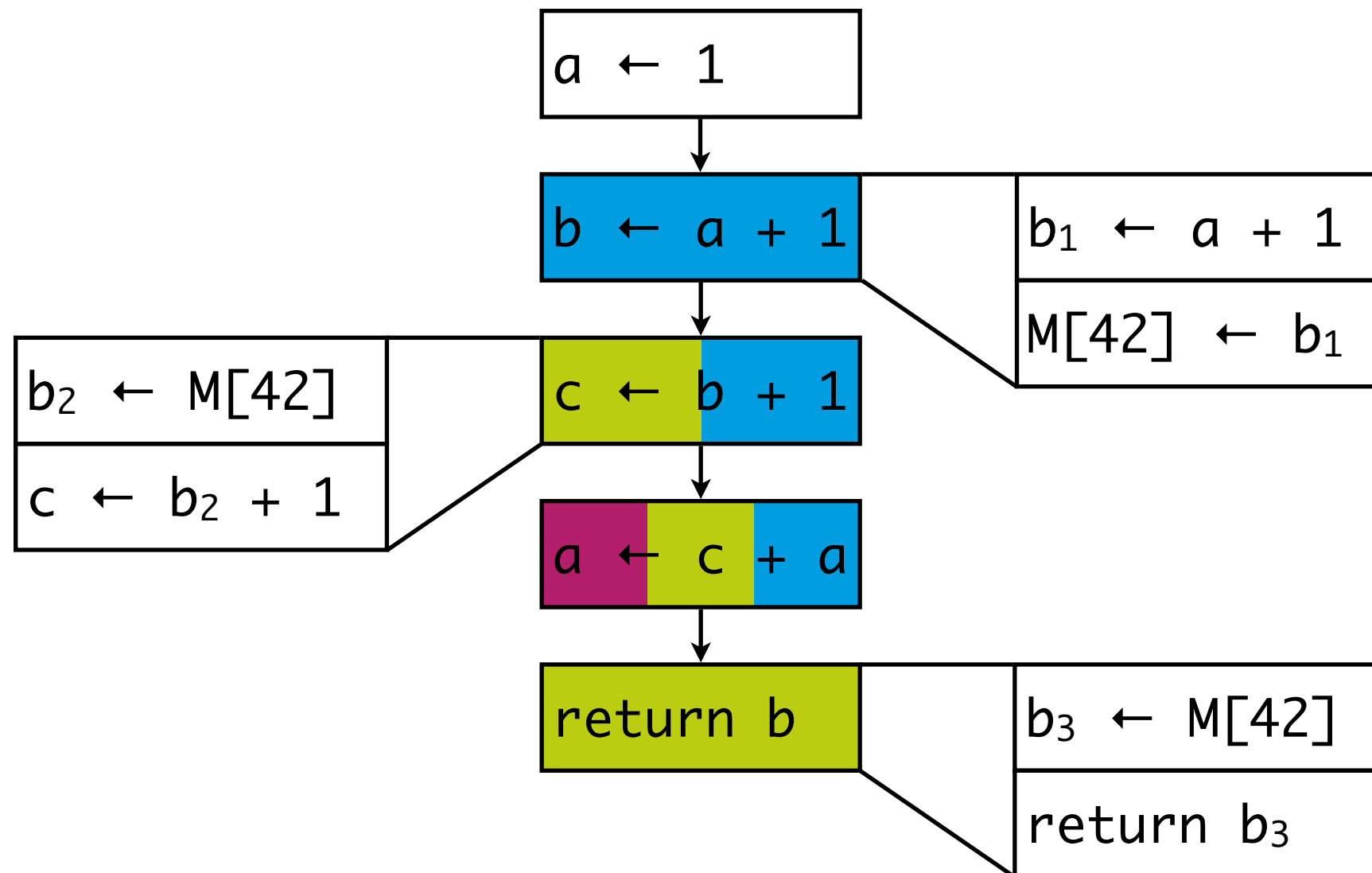
# Spilling example



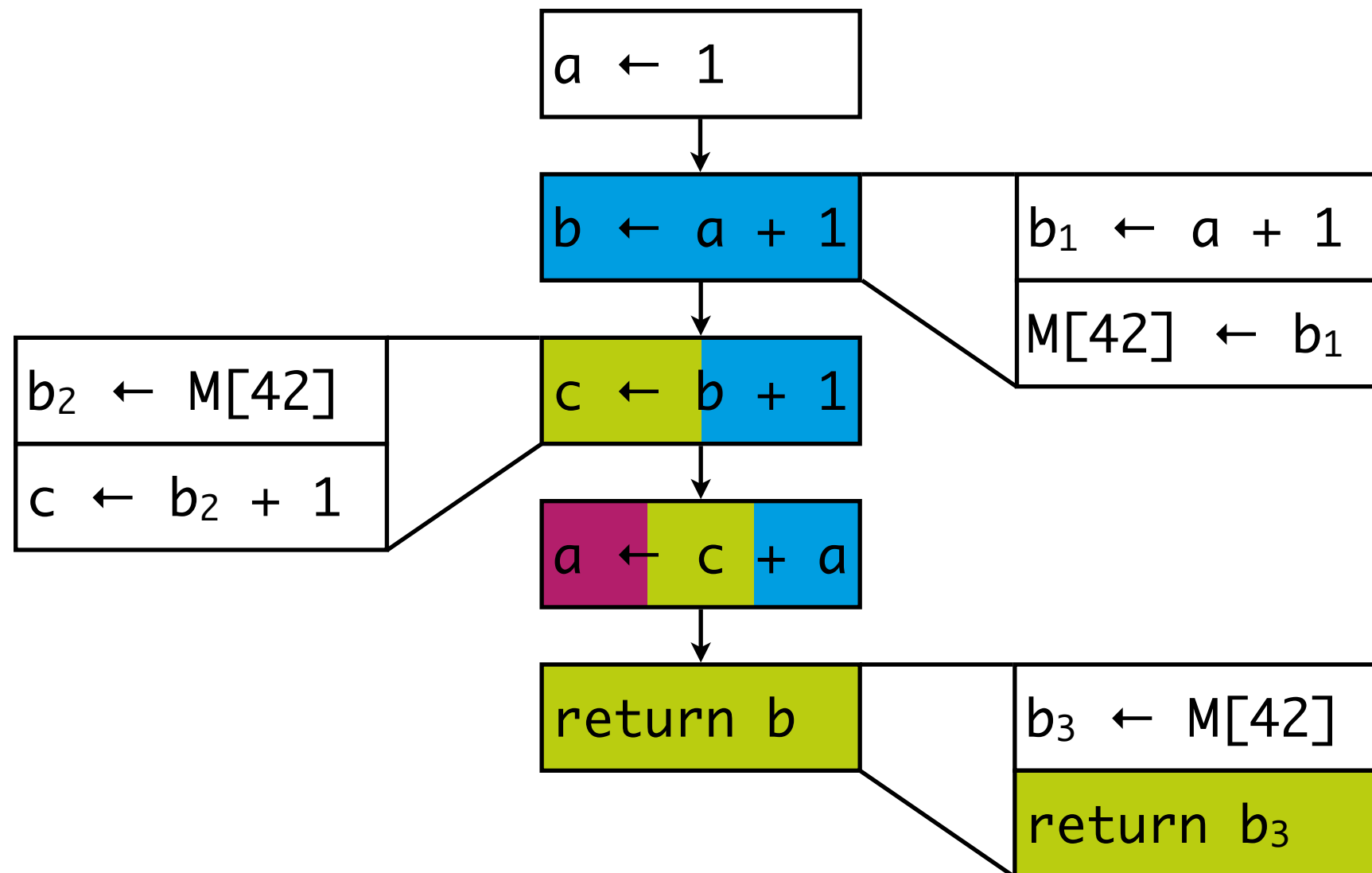
# Spilling example



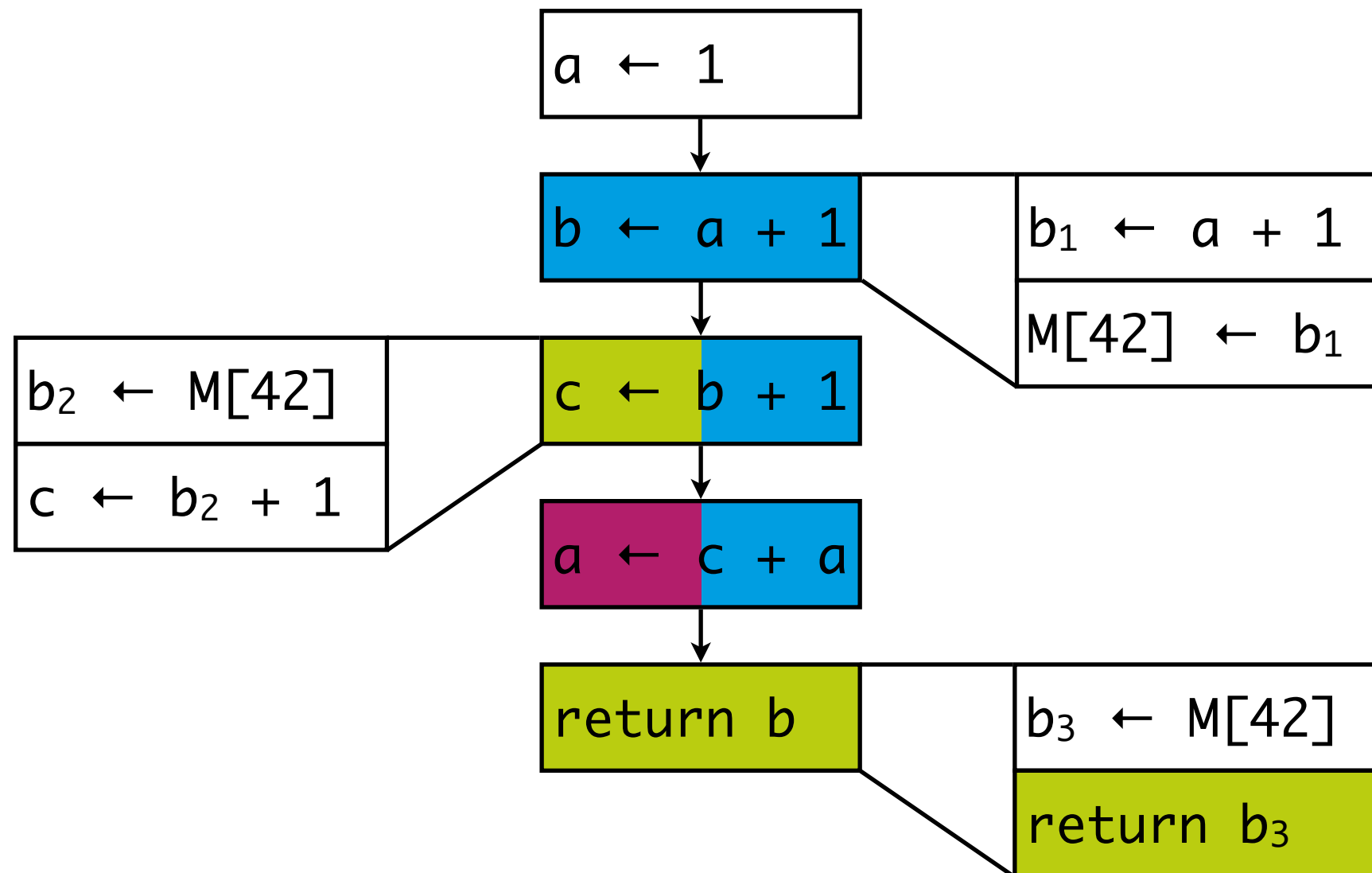
# Spilling example



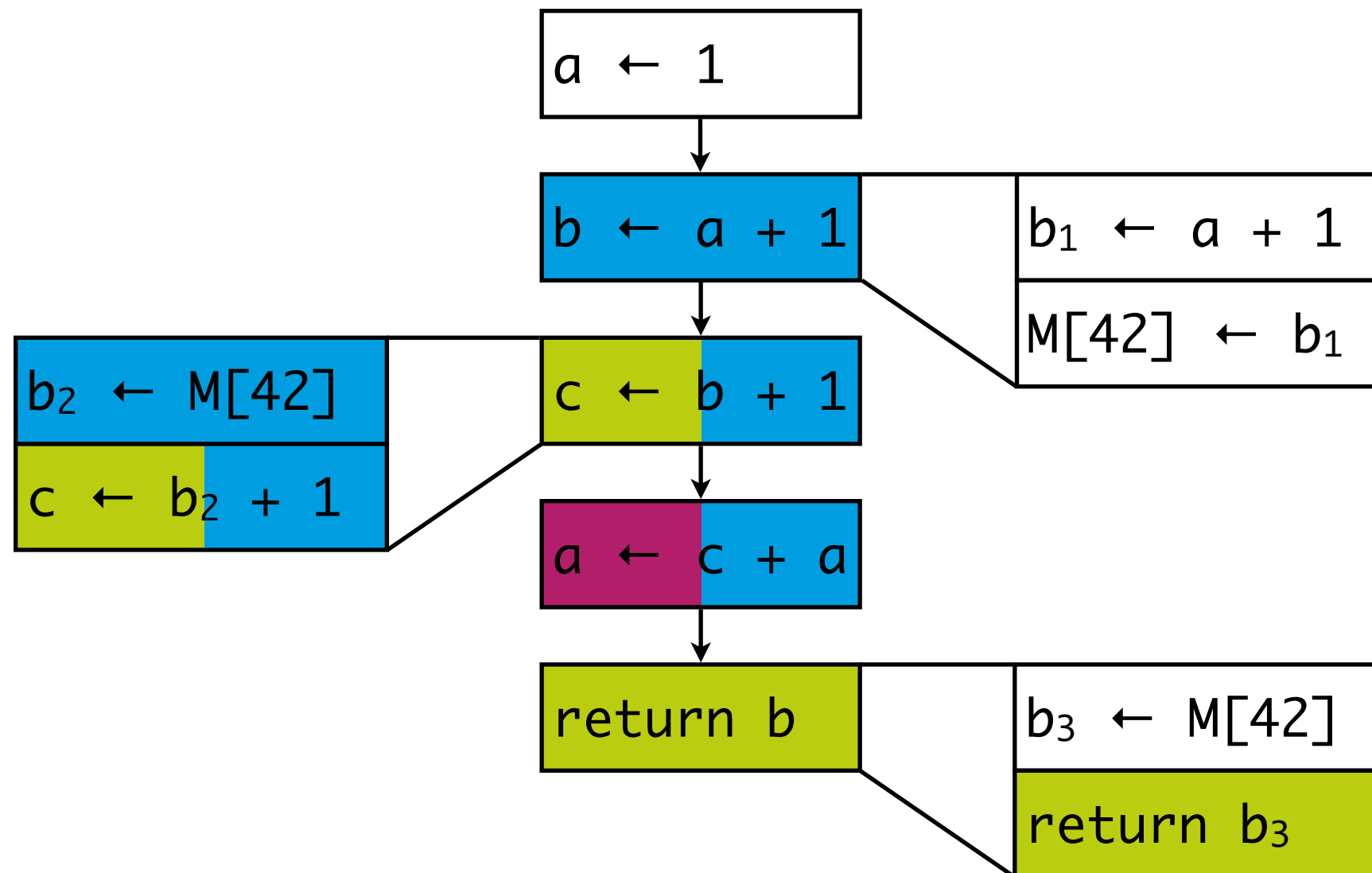
# Spilling example



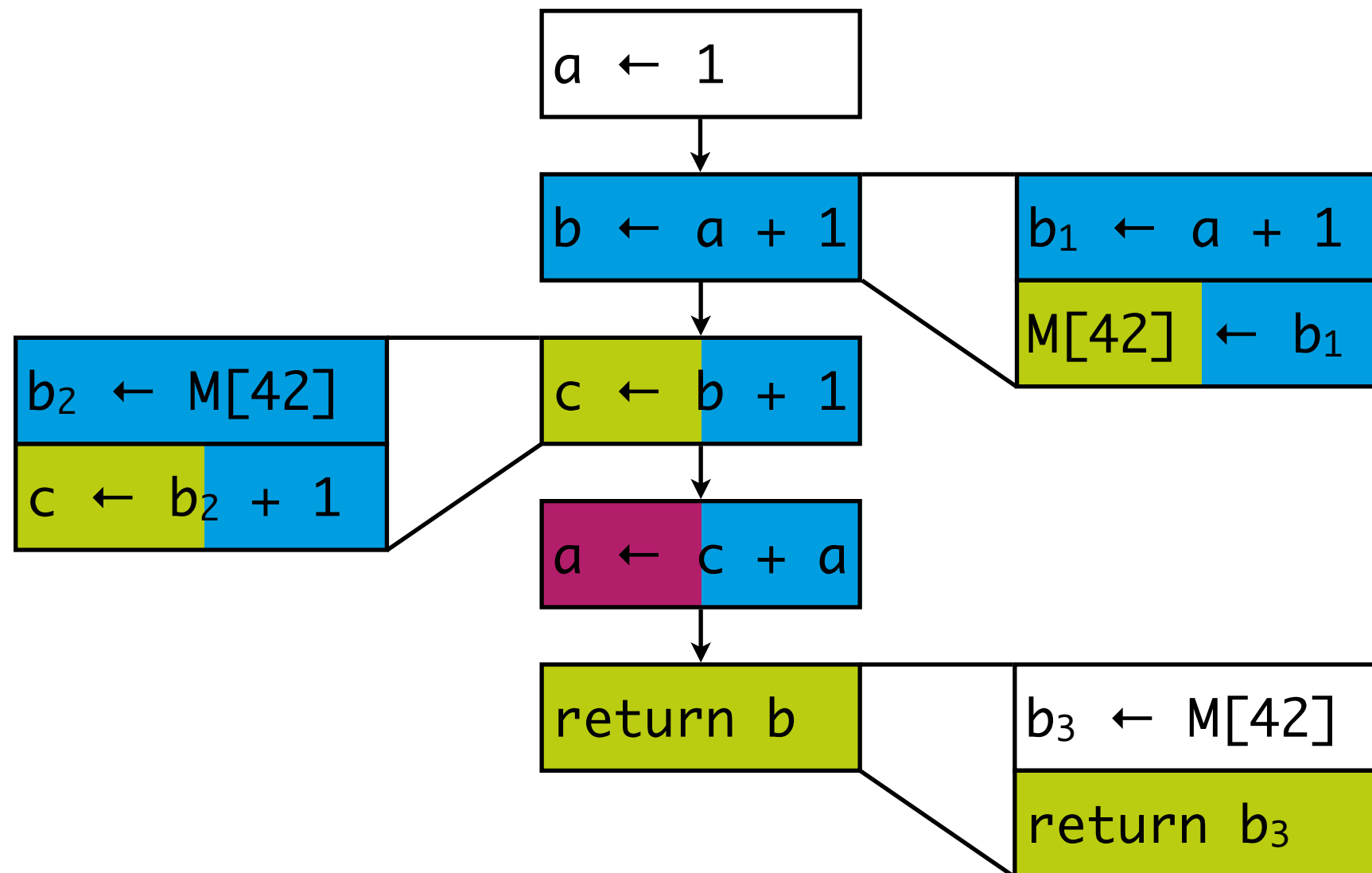
# Spilling example



# Spilling example



# Spilling example





# IV

---

## Coalescing

---

# Eliminating Move Instructions

## coalescing

```
live-in: k j
g := mem[j + 12]
h := k - 1
f := g * h
e := mem[j + 8]
m := mem[j + 16]
b := mem[f]
c := e + 8
d := c
k := m + 4
j := b
live out: d k j
```

# Eliminating Move Instructions

## coalescing

```
live-in: k j
g := mem[j + 12]
h := k - 1
f := g * h
e := mem[j + 8]
m := mem[j + 16]
b := mem[f]
c := e + 8
d := c
k := m + 4
j := b
live out: d k j
```

# Coalescing

coalesce |ˌkəʊəˈleɪs|

verb *[no object]*

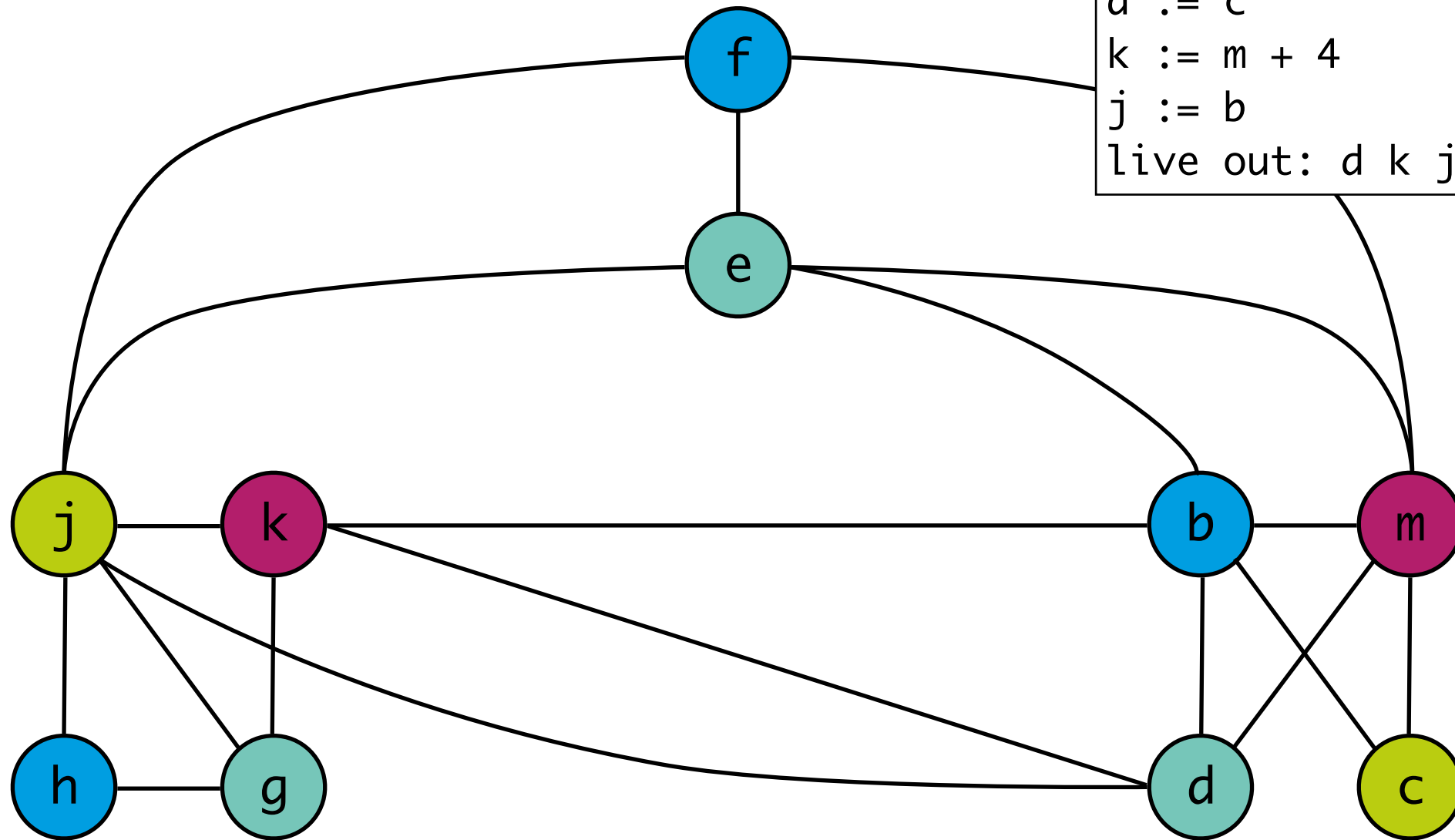
come together to form one mass or whole: *the puddles had **coalesced into** shallow streams.*

- *[with object]* combine (elements) in a mass or whole: *his idea served to **coalesce** all that happened **into** one connected whole.*

# Recap: Graph Coloring

## example

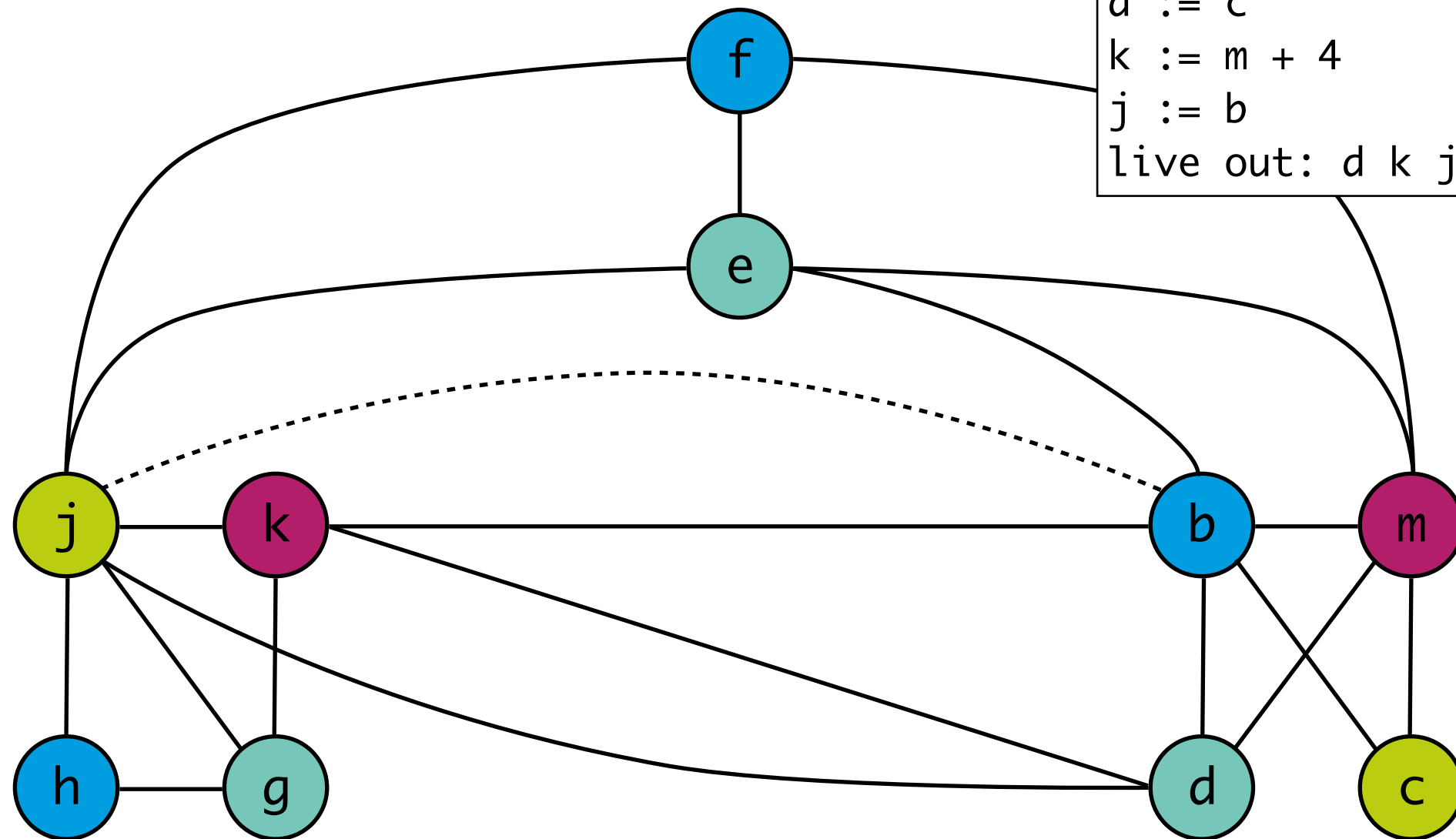
```
live-in: k j  
g := mem[j + 12]  
h := k - 1  
f := g * h  
e := mem[j + 8]  
m := mem[j + 16]  
b := mem[f]  
c := e + 8  
d := c  
k := m + 4  
j := b  
live out: d k j
```



# Recap: Graph Coloring

## example

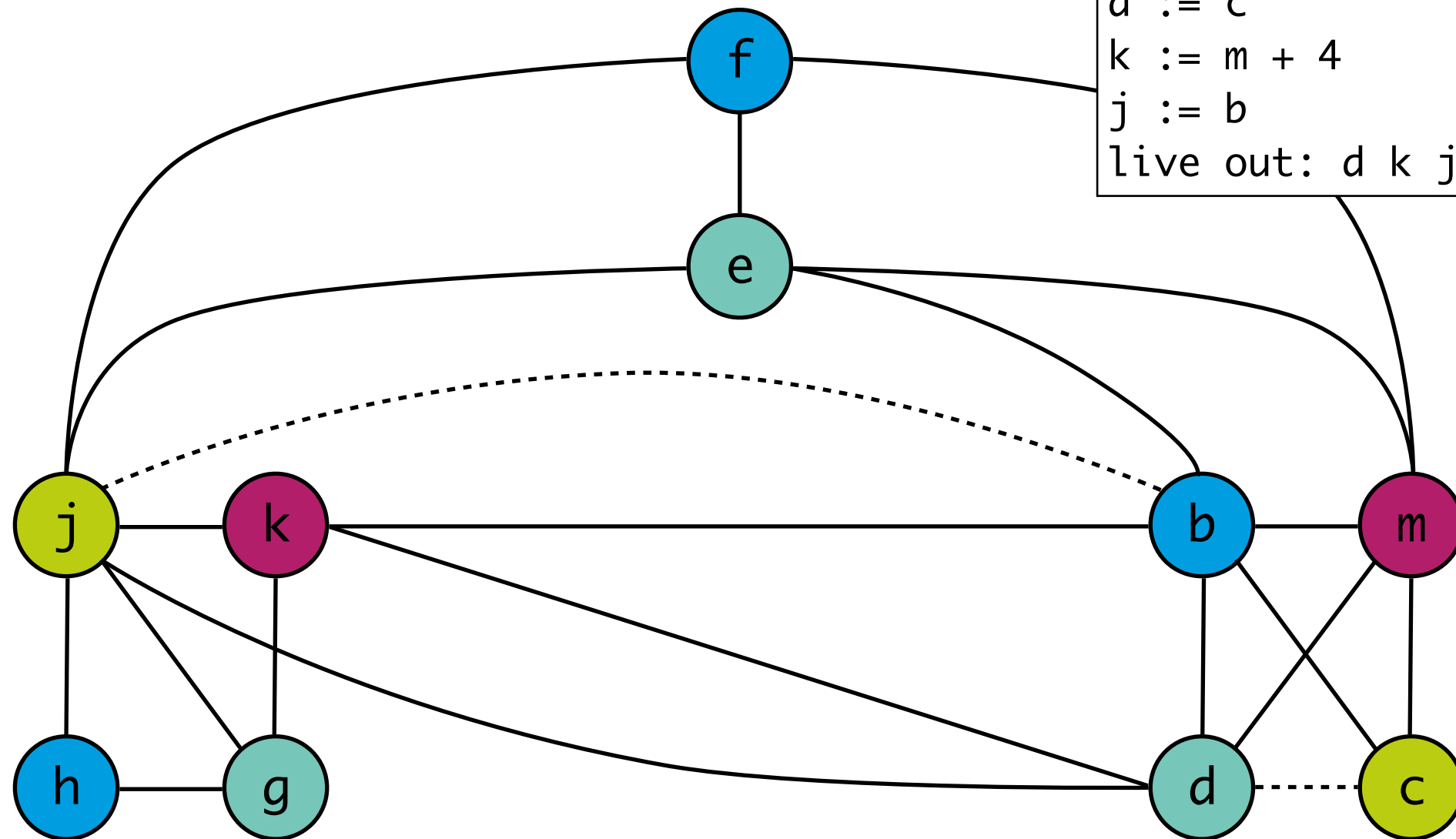
```
live-in: k j
g := mem[j + 12]
h := k - 1
f := g * h
e := mem[j + 8]
m := mem[j + 16]
b := mem[f]
c := e + 8
d := c
k := m + 4
j := b
live out: d k j
```



# Recap: Graph Coloring

## example

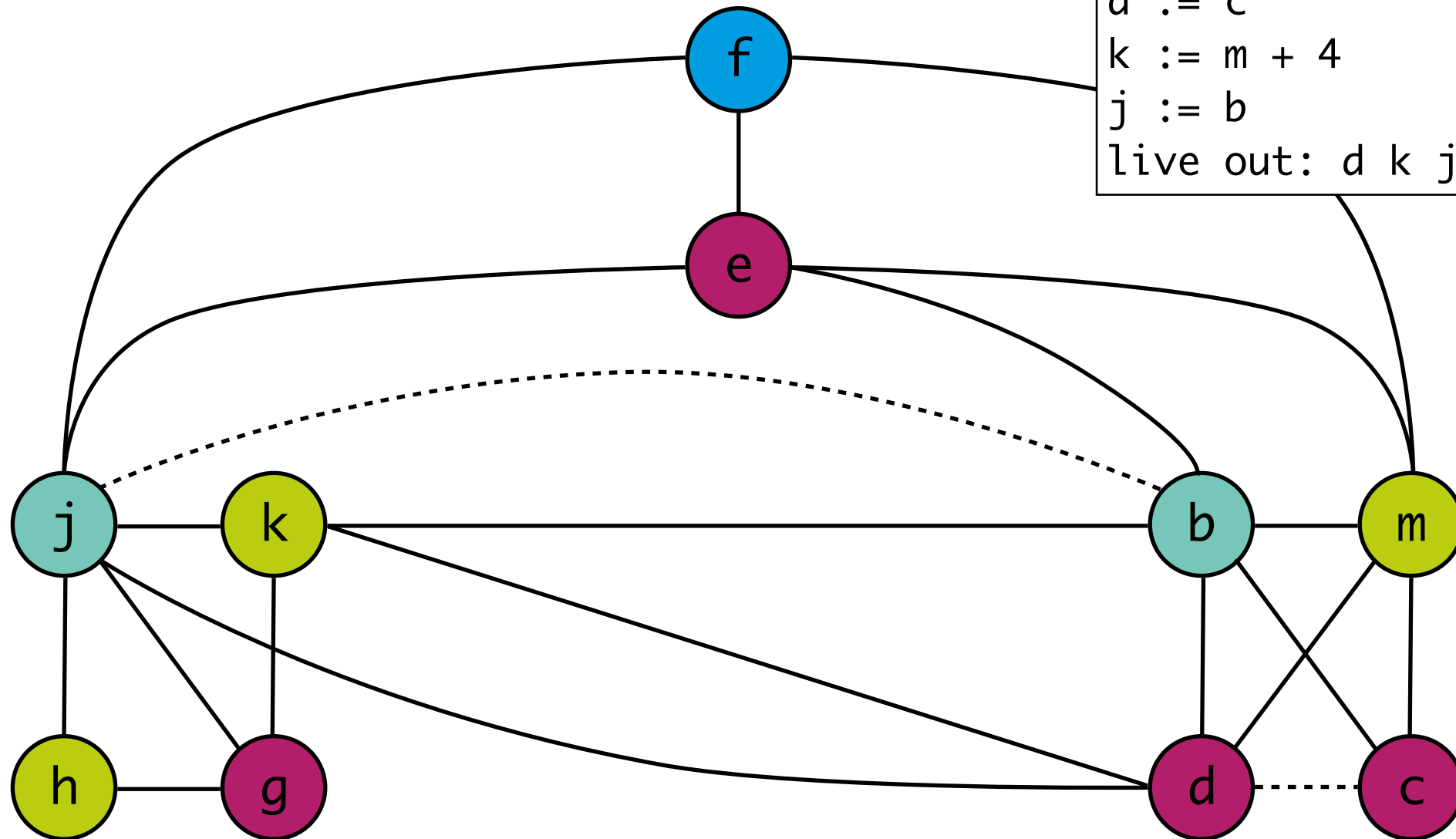
```
live-in: k j  
g := mem[j + 12]  
h := k - 1  
f := g * h  
e := mem[j + 8]  
m := mem[j + 16]  
b := mem[f]  
c := e + 8  
d := c  
k := m + 4  
j := b  
live out: d k j
```



# Coalescing

better solution

```
live-in: k j  
g := mem[j + 12]  
h := k - 1  
f := g * h  
e := mem[j + 8]  
m := mem[j + 16]  
b := mem[f]  
c := e + 8  
d := c  
k := m + 4  
j := b  
live out: d k j
```

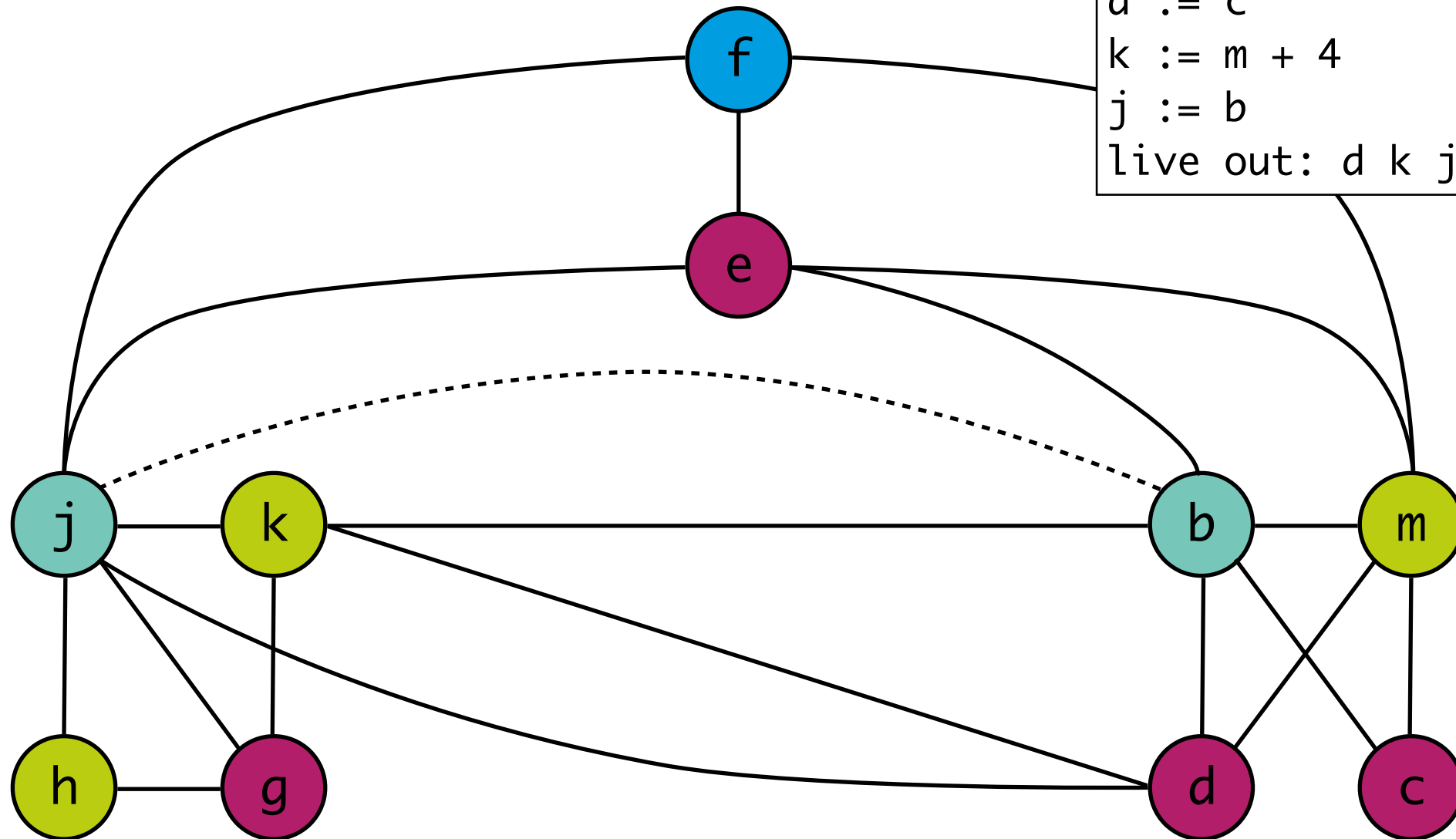




# Coalescing

better solution

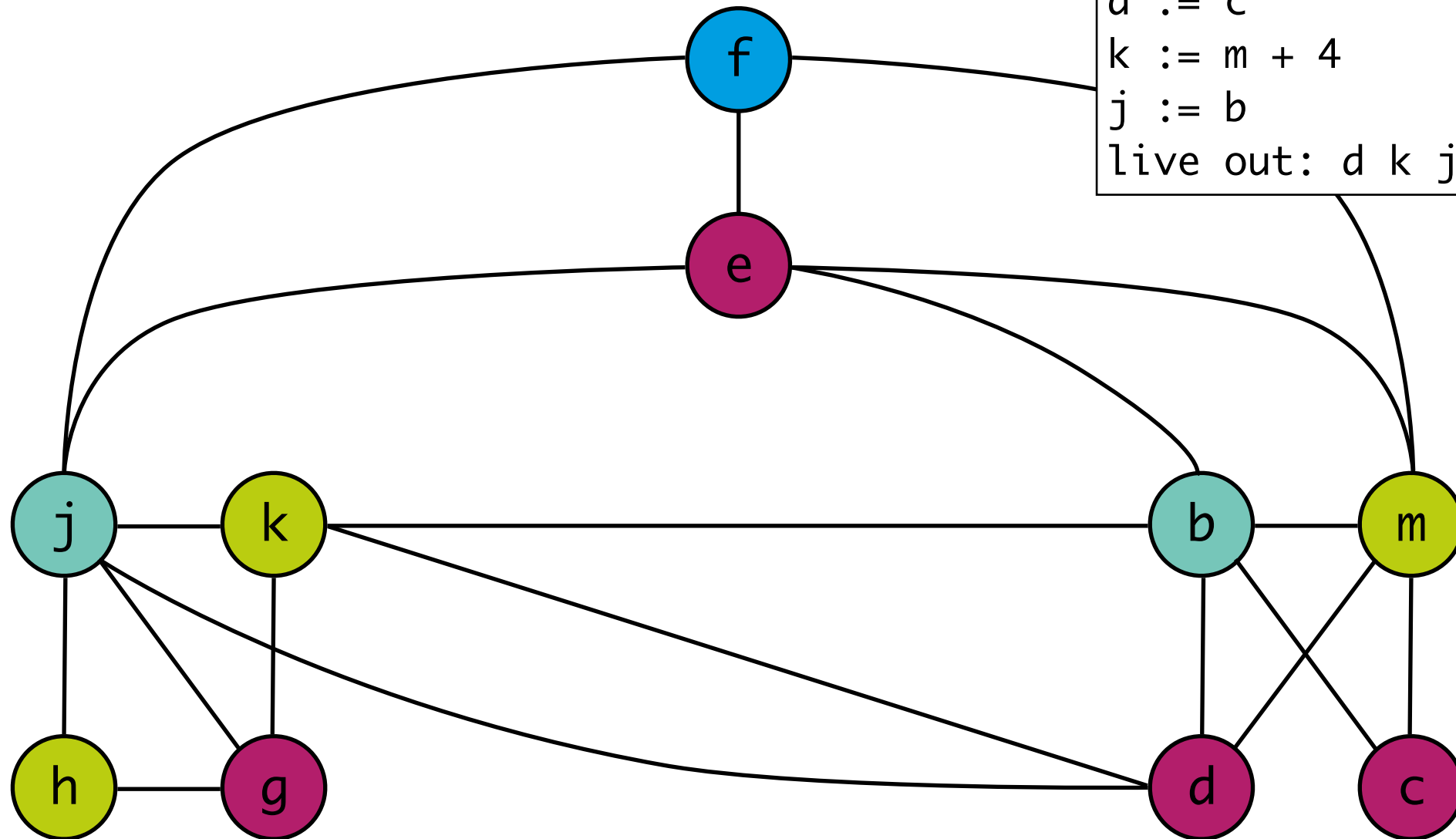
```
live-in: k j
g := mem[j + 12]
h := k - 1
f := g * h
e := mem[j + 8]
m := mem[j + 16]
b := mem[f]
c := e + 8
d := c
k := m + 4
j := b
live out: d k j
```



# Coalescing

better solution

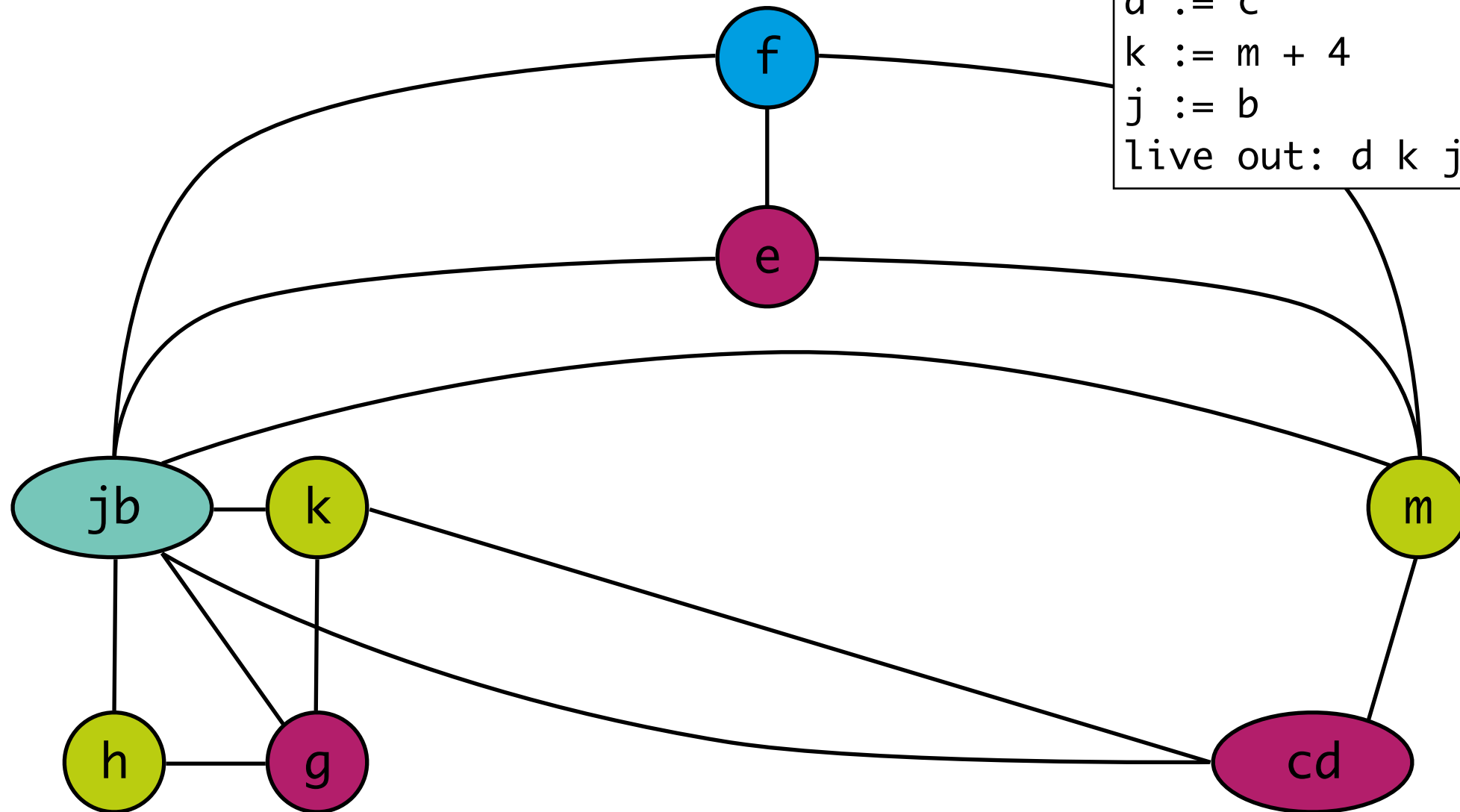
```
live-in: k j
g := mem[j + 12]
h := k - 1
f := g * h
e := mem[j + 8]
m := mem[j + 16]
b := mem[f]
c := e + 8
d := c
k := m + 4
j := b
live out: d k j
```



# Coalescing

## coalescing nodes

```
live-in: k j  
g := mem[j + 12]  
h := k - 1  
f := g * h  
e := mem[j + 8]  
m := mem[j + 16]  
b := mem[f]  
c := e + 8  
d := c  
k := m + 4  
j := b  
live out: d k j
```



# Coalescing

## conservative strategies

### Briggs

- $a/b$  has fewer than  $k$  neighbours of significant degree
- nodes of insignificant degree and  $a/b$  can be simplified
- remaining graph is colorable

### George

- all neighbours of  $a$  of significant degree interfere also with  $b$
- neighbours of  $a$  of insignificant degree can be simplified
- subgraph of original graph is colorable

# Graph Coloring

## steps

Simplify

remove **non-move-related** node of **insignificant** degree

Coalesce

Freeze

turn **move-related** node of **insignificant** degree into **non-move-related**

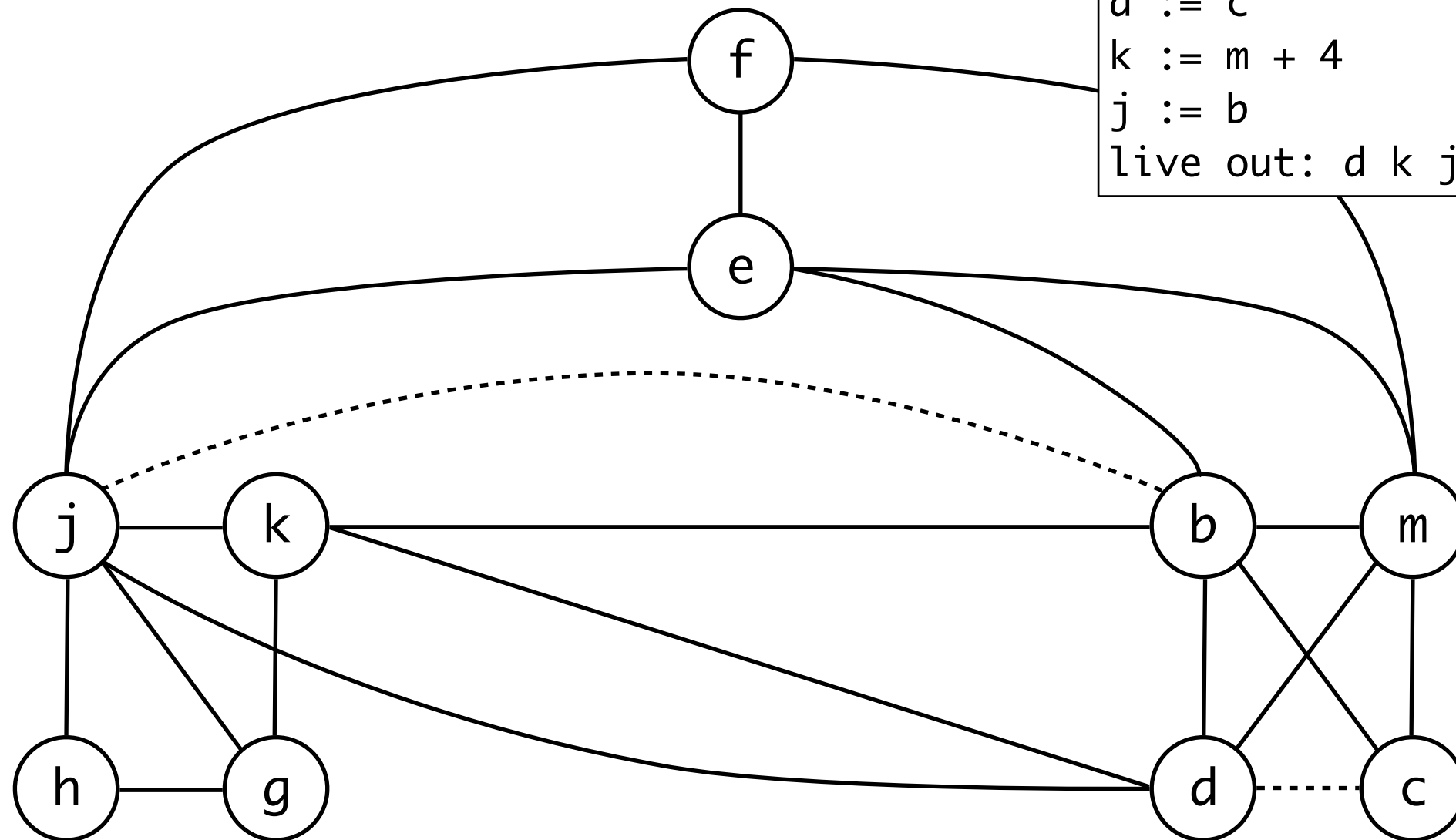
Spill

Select

Start over

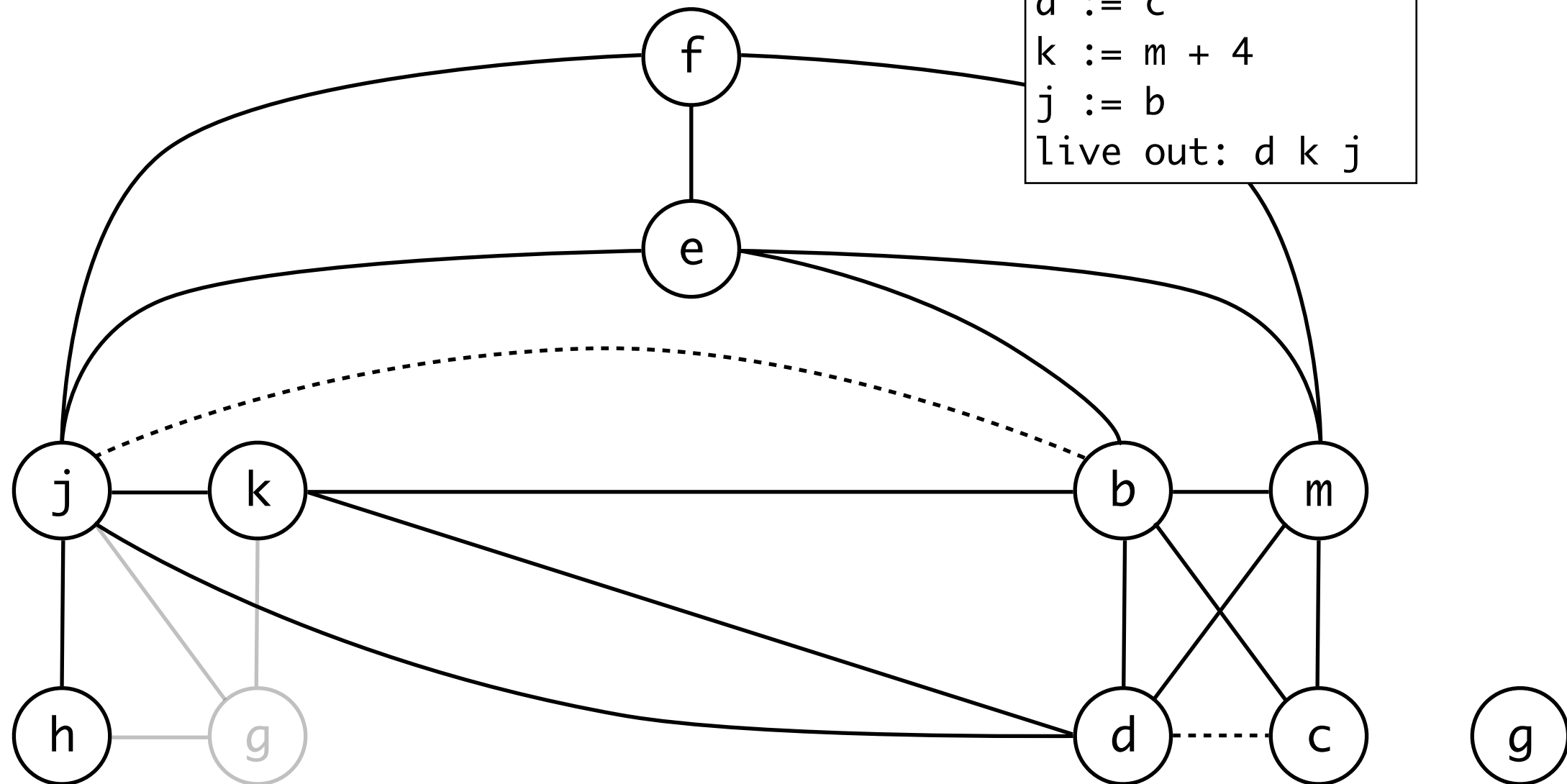
# Coalescing example

```
live-in: k j  
g := mem[j + 12]  
h := k - 1  
f := g * h  
e := mem[j + 8]  
m := mem[j + 16]  
b := mem[f]  
c := e + 8  
d := c  
k := m + 4  
j := b  
live out: d k j
```



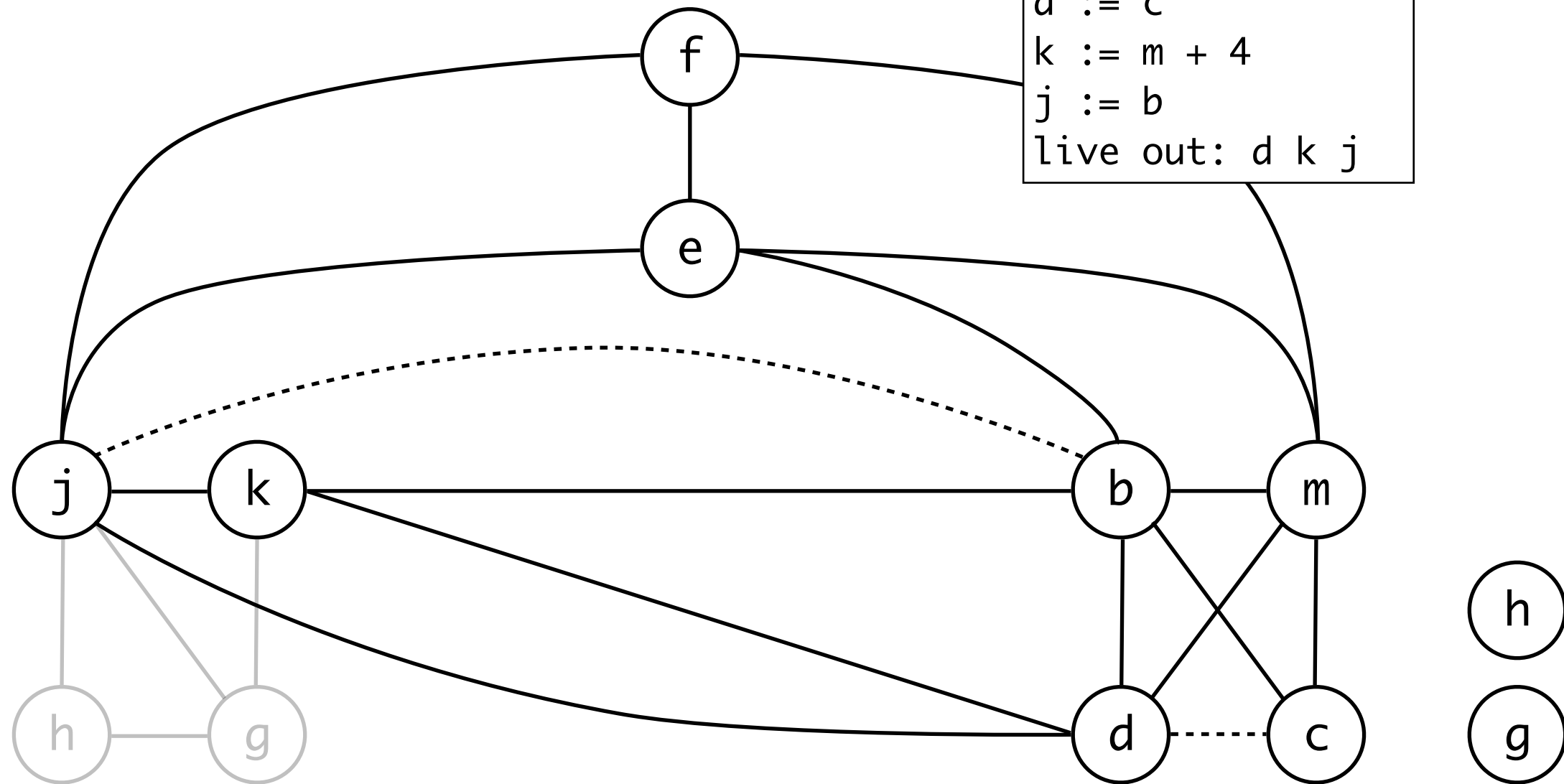
# Coalescing example

```
live-in: k j
g := mem[j + 12]
h := k - 1
f := g * h
e := mem[j + 8]
m := mem[j + 16]
b := mem[f]
c := e + 8
d := c
k := m + 4
j := b
live out: d k j
```



# Coalescing example

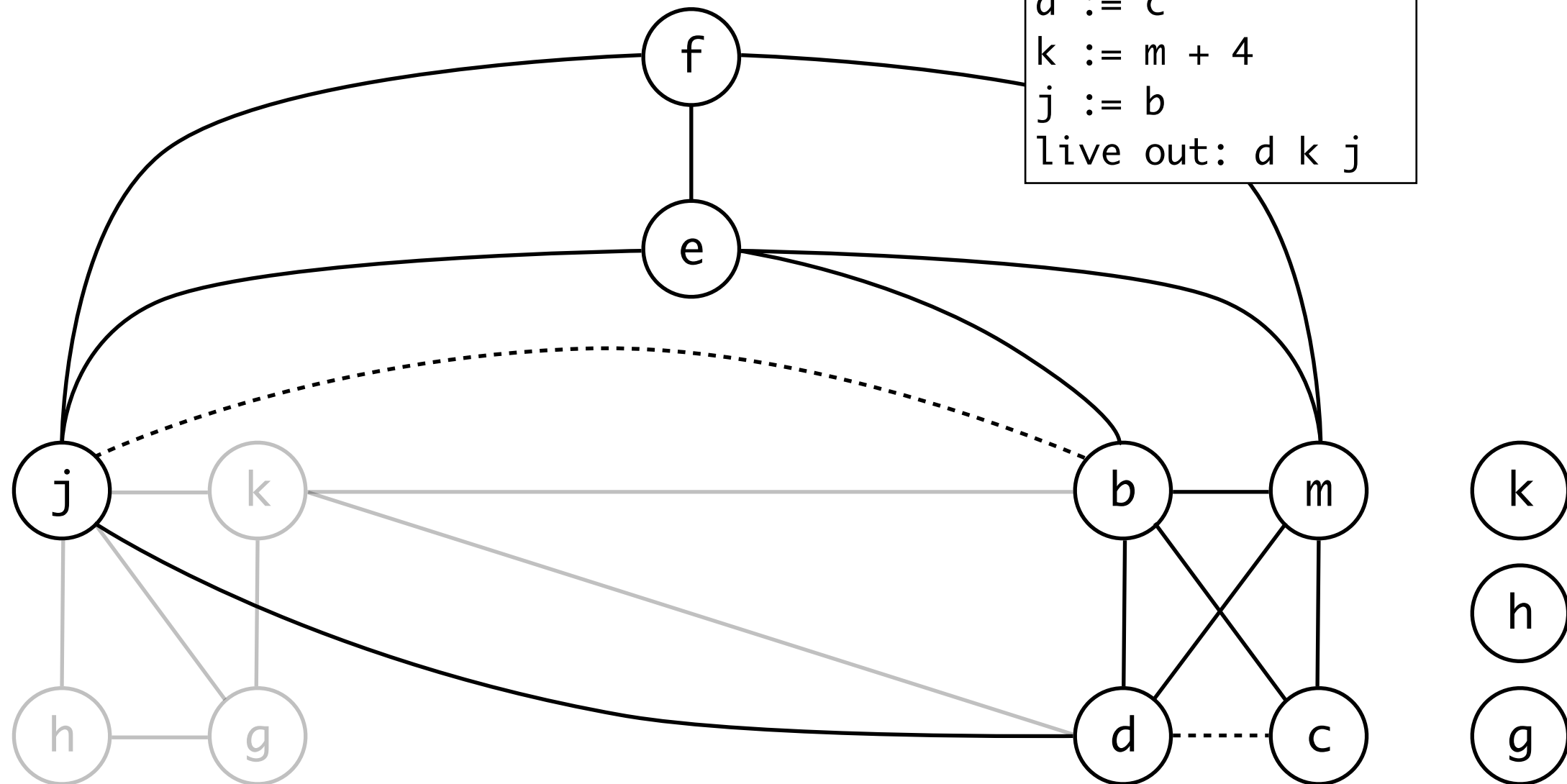
```
live-in: k j
g := mem[j + 12]
h := k - 1
f := g * h
e := mem[j + 8]
m := mem[j + 16]
b := mem[f]
c := e + 8
d := c
k := m + 4
j := b
live out: d k j
```





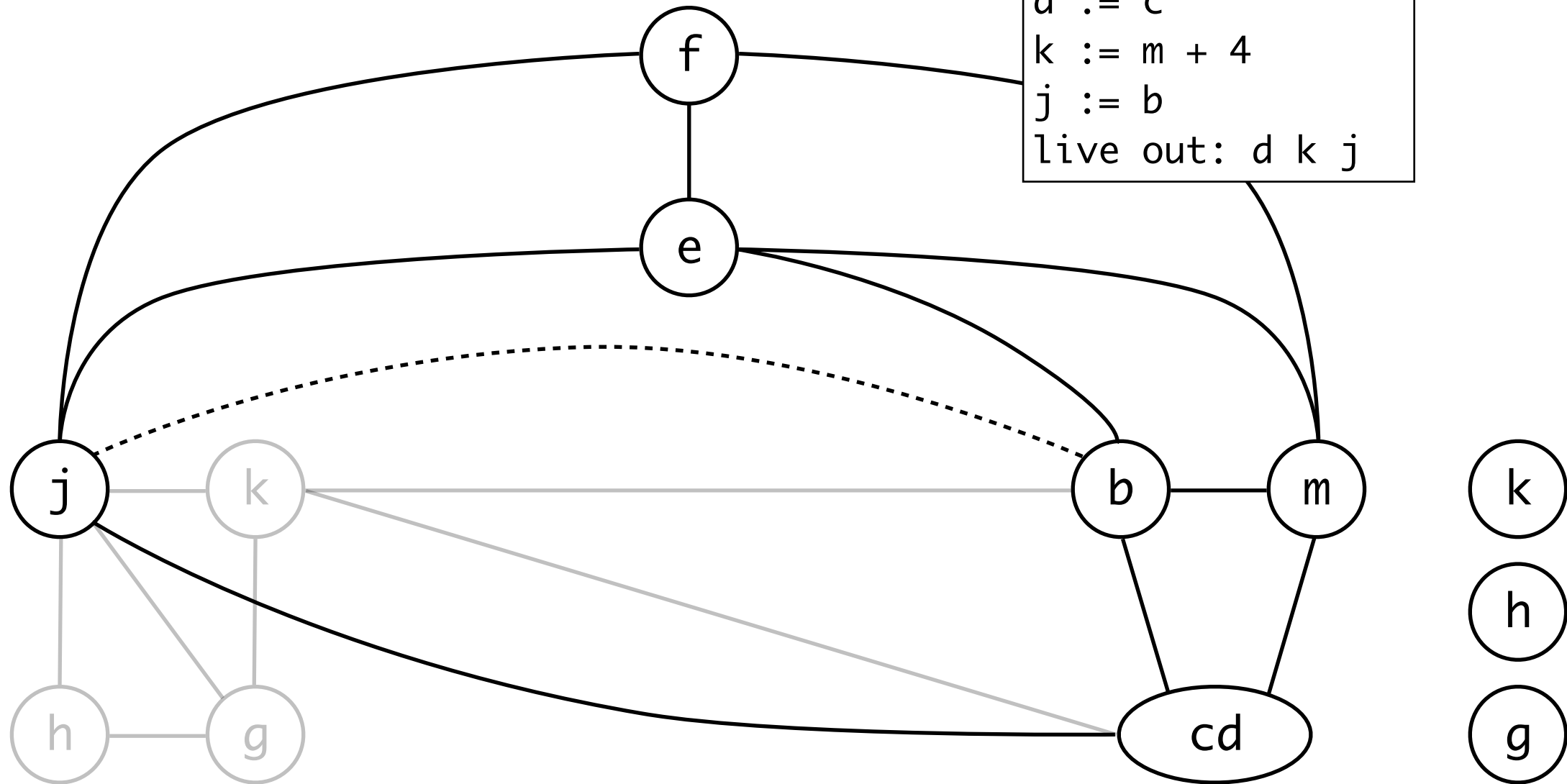
# Coalescing example

```
live-in: k j
g := mem[j + 12]
h := k - 1
f := g * h
e := mem[j + 8]
m := mem[j + 16]
b := mem[f]
c := e + 8
d := c
k := m + 4
j := b
live out: d k j
```



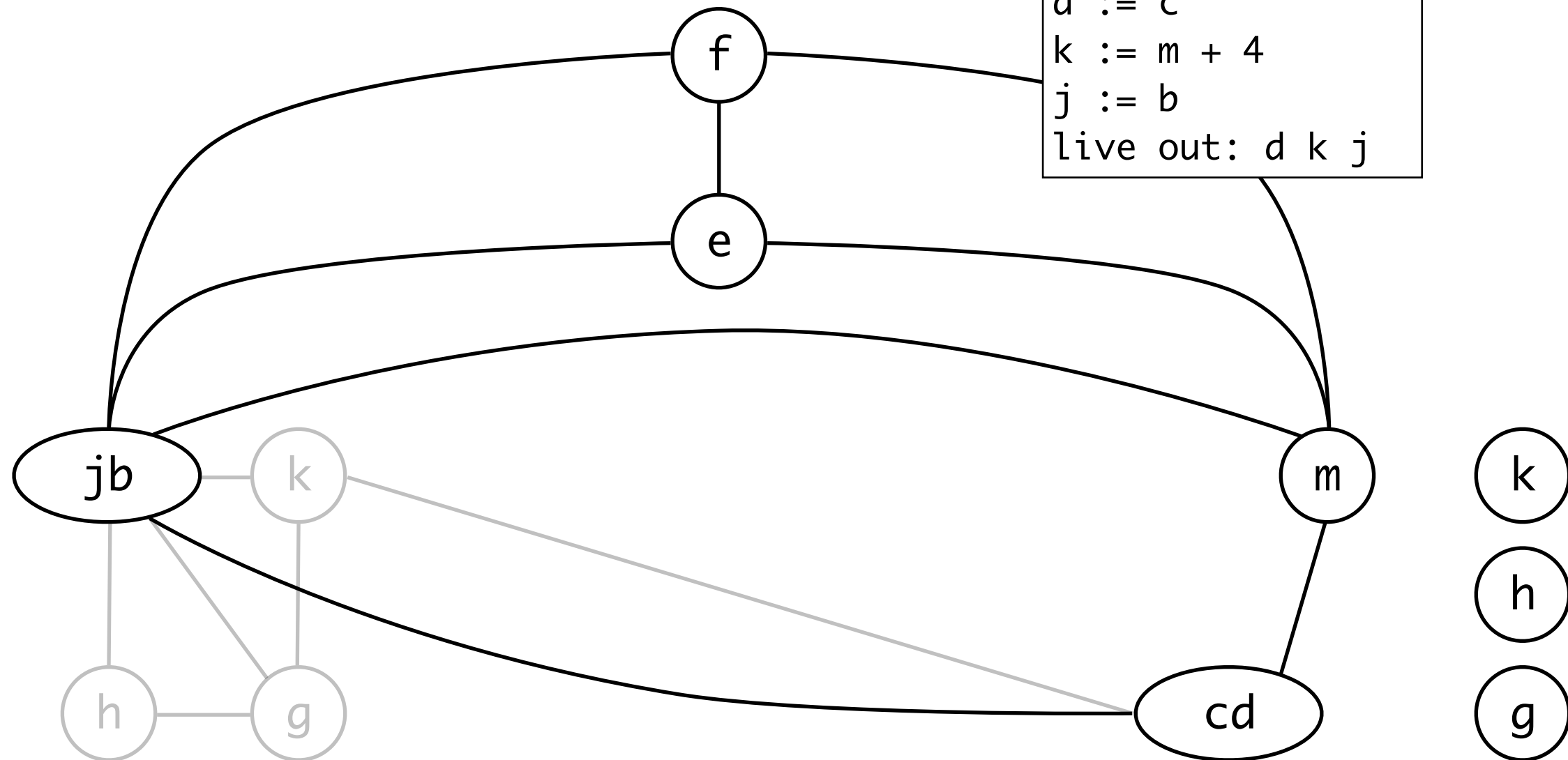
# Coalescing example

```
live-in: k j
g := mem[j + 12]
h := k - 1
f := g * h
e := mem[j + 8]
m := mem[j + 16]
b := mem[f]
c := e + 8
d := c
k := m + 4
j := b
live out: d k j
```



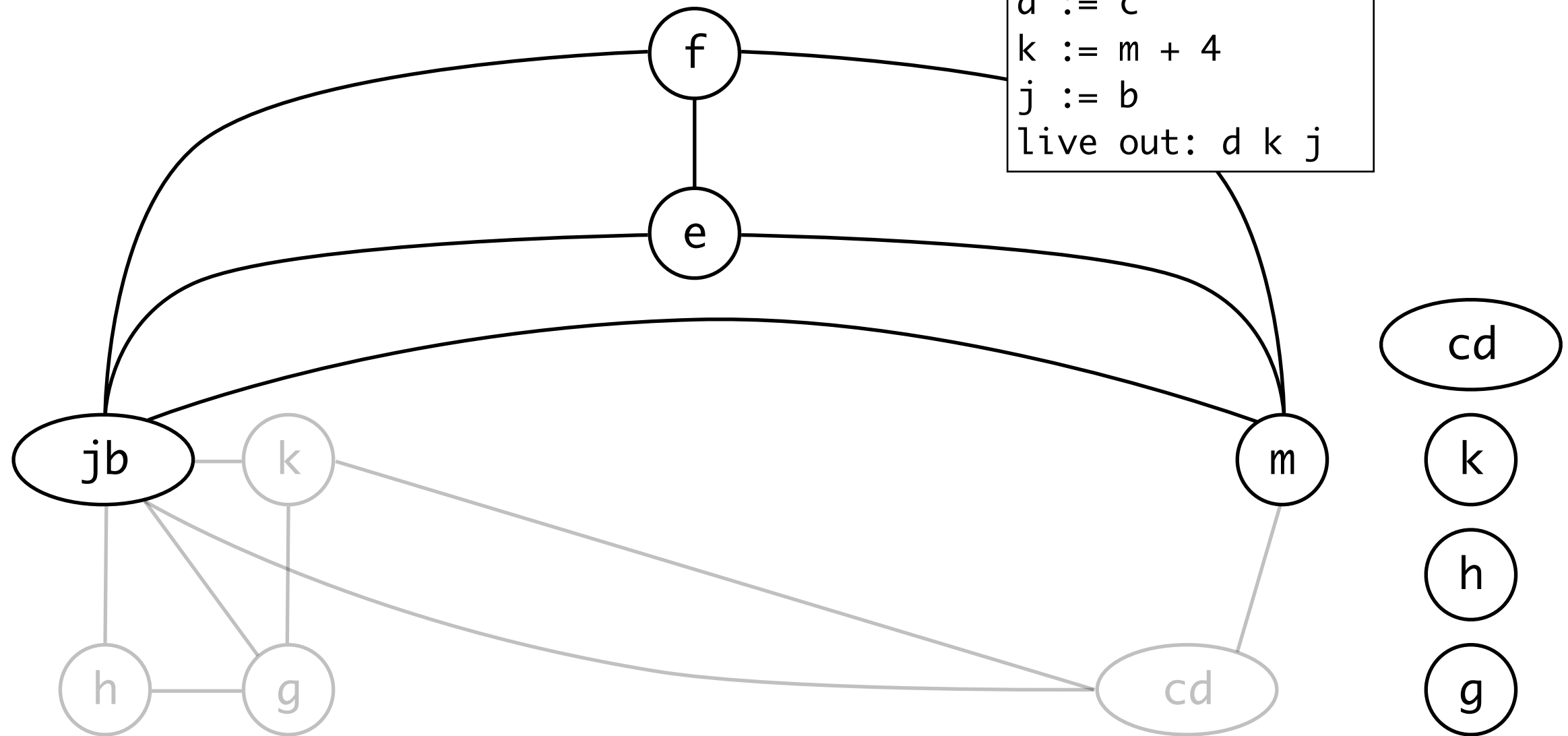
# Coalescing example

```
live-in: k j
g := mem[j + 12]
h := k - 1
f := g * h
e := mem[j + 8]
m := mem[j + 16]
b := mem[f]
c := e + 8
d := c
k := m + 4
j := b
live out: d k j
```



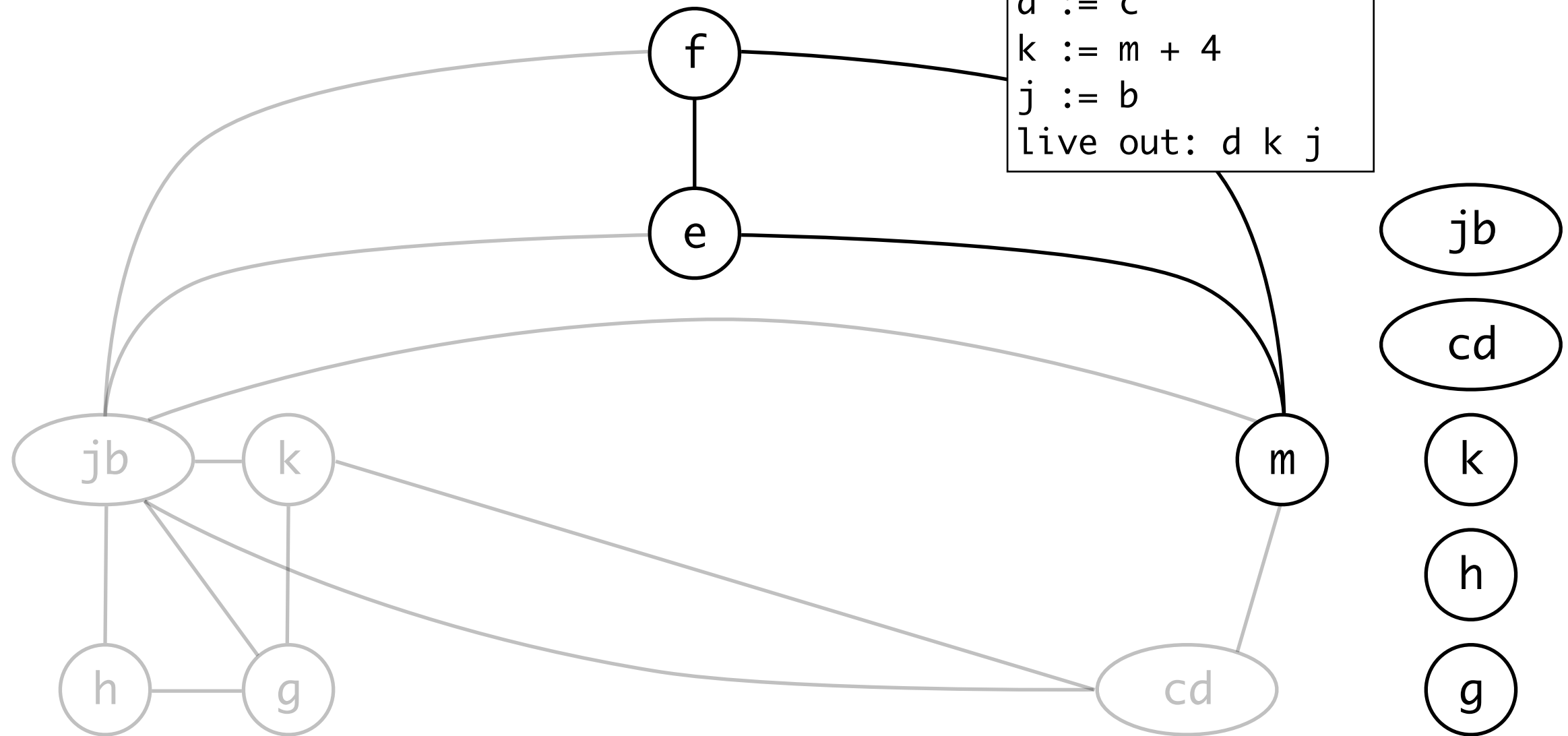
# Coalescing example

```
live-in: k j
g := mem[j + 12]
h := k - 1
f := g * h
e := mem[j + 8]
m := mem[j + 16]
b := mem[f]
c := e + 8
d := c
k := m + 4
j := b
live out: d k j
```



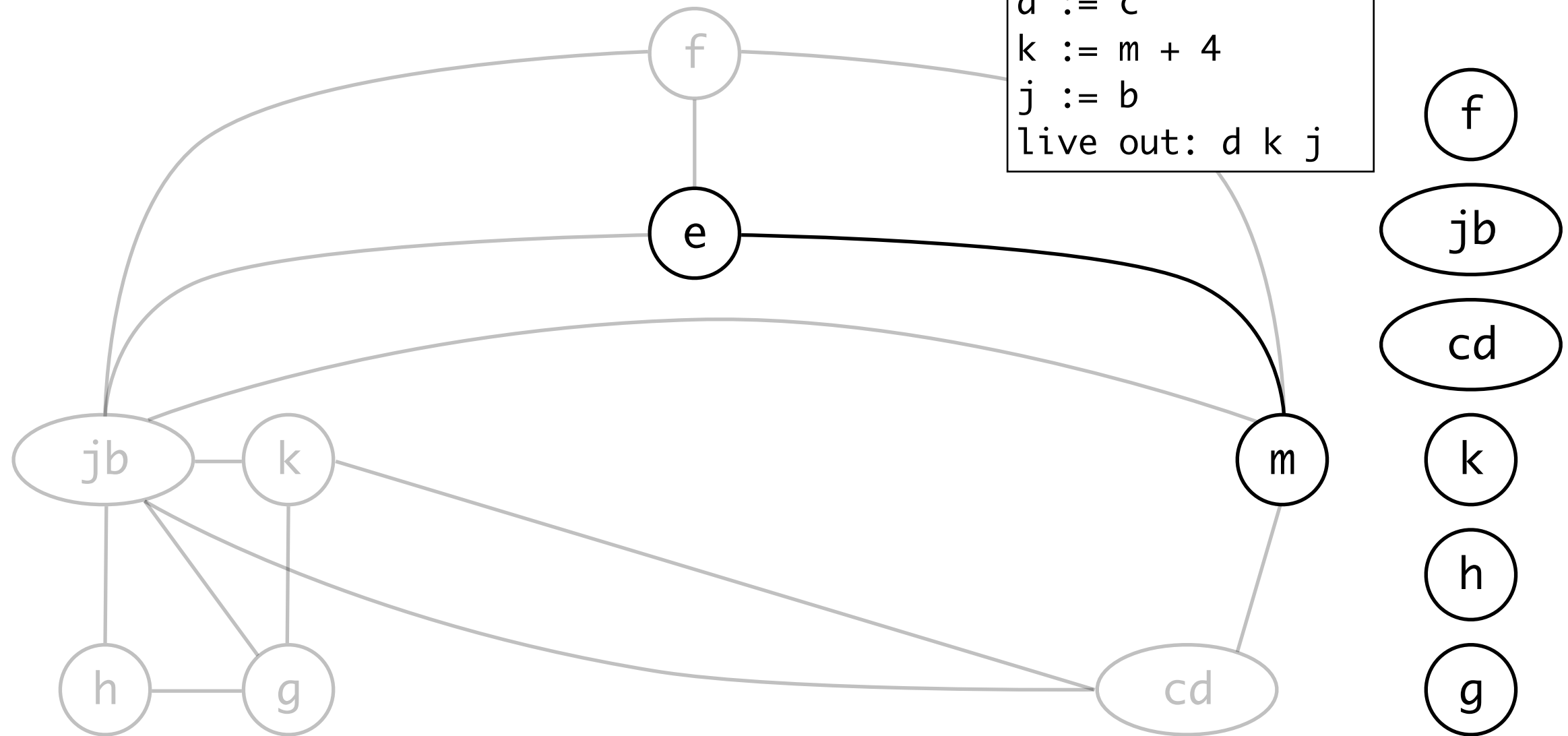
# Coalescing example

```
live-in: k j
g := mem[j + 12]
h := k - 1
f := g * h
e := mem[j + 8]
m := mem[j + 16]
b := mem[f]
c := e + 8
d := c
k := m + 4
j := b
live out: d k j
```



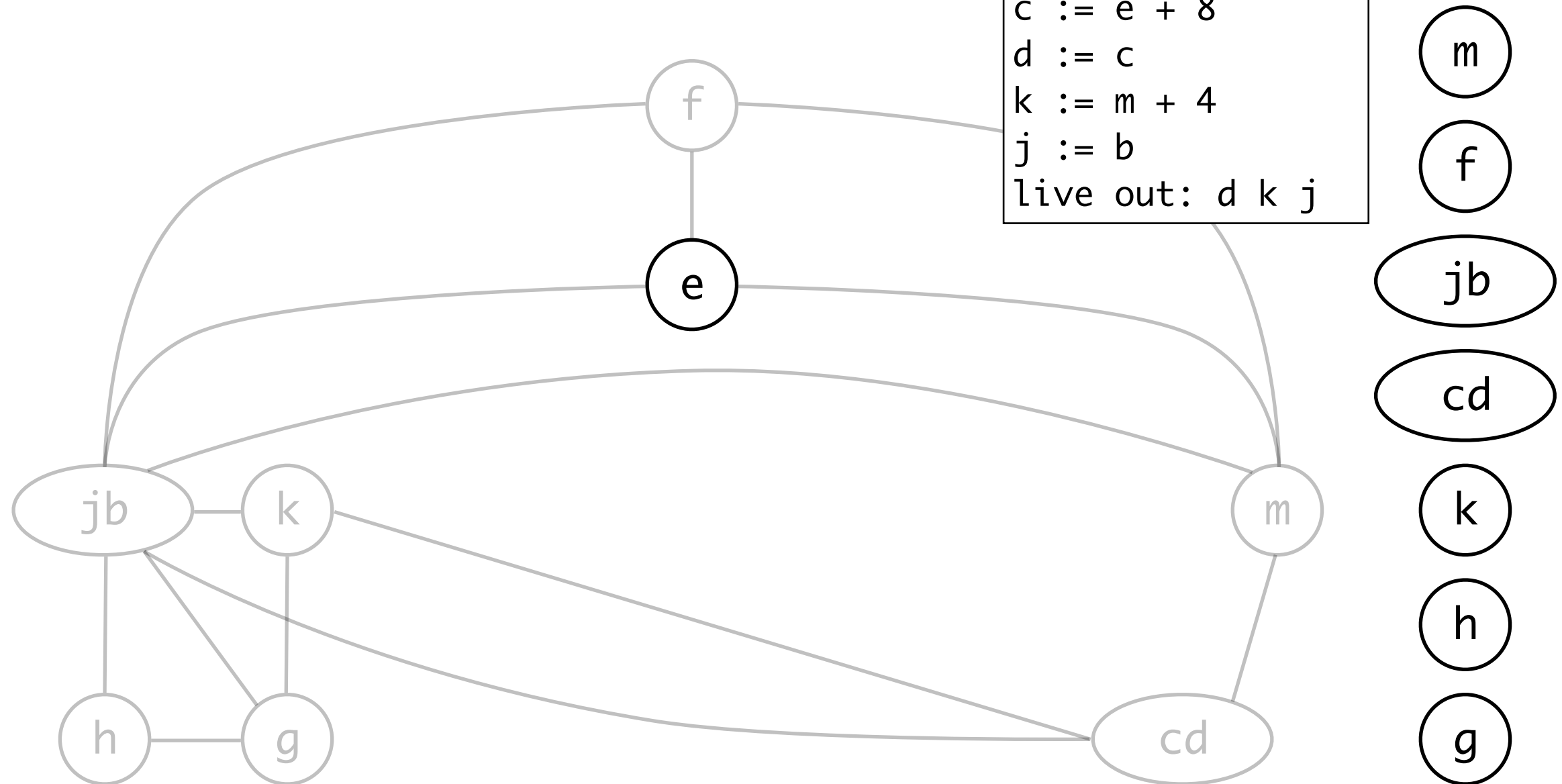
# Coalescing example

```
live-in: k j
g := mem[j + 12]
h := k - 1
f := g * h
e := mem[j + 8]
m := mem[j + 16]
b := mem[f]
c := e + 8
d := c
k := m + 4
j := b
live out: d k j
```



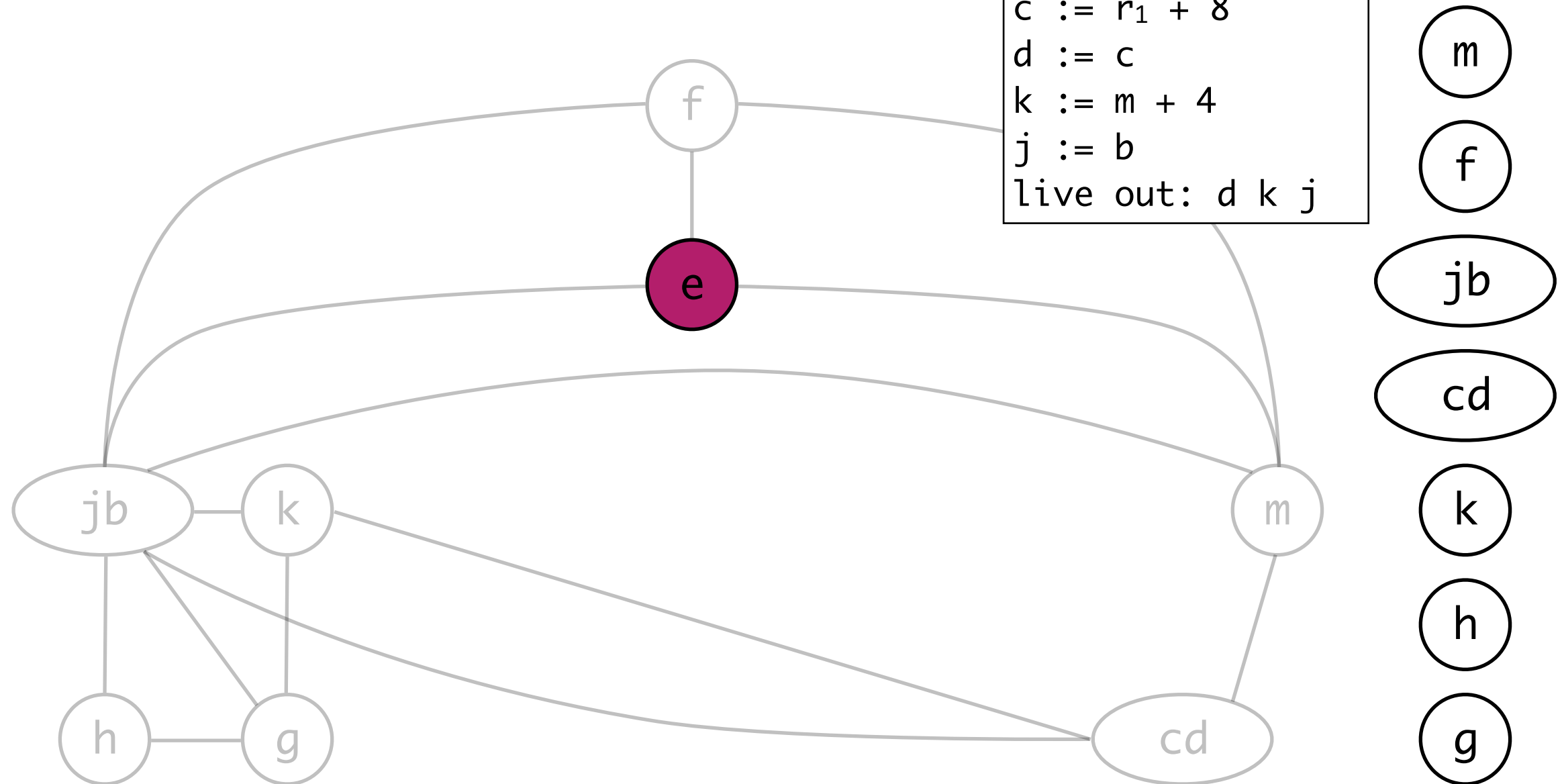
# Coalescing example

```
live-in: k j
g := mem[j + 12]
h := k - 1
f := g * h
e := mem[j + 8]
m := mem[j + 16]
b := mem[f]
c := e + 8
d := c
k := m + 4
j := b
live out: d k j
```



# Coalescing example

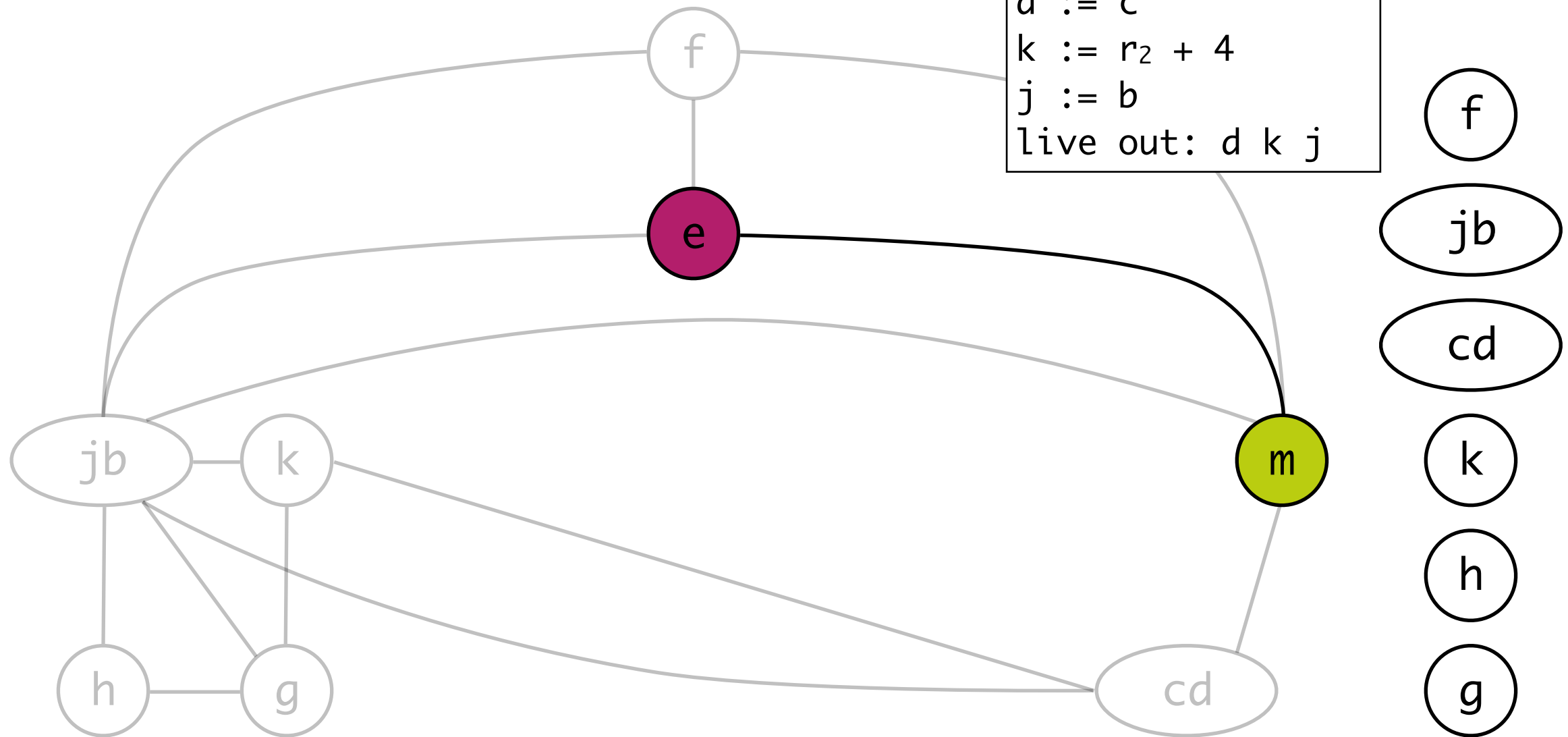
```
live-in: k j  
g := mem[j + 12]  
h := k - 1  
f := g * h  
r1 := mem[j + 8]  
m := mem[j + 16]  
b := mem[f]  
c := r1 + 8  
d := c  
k := m + 4  
j := b  
live out: d k j
```





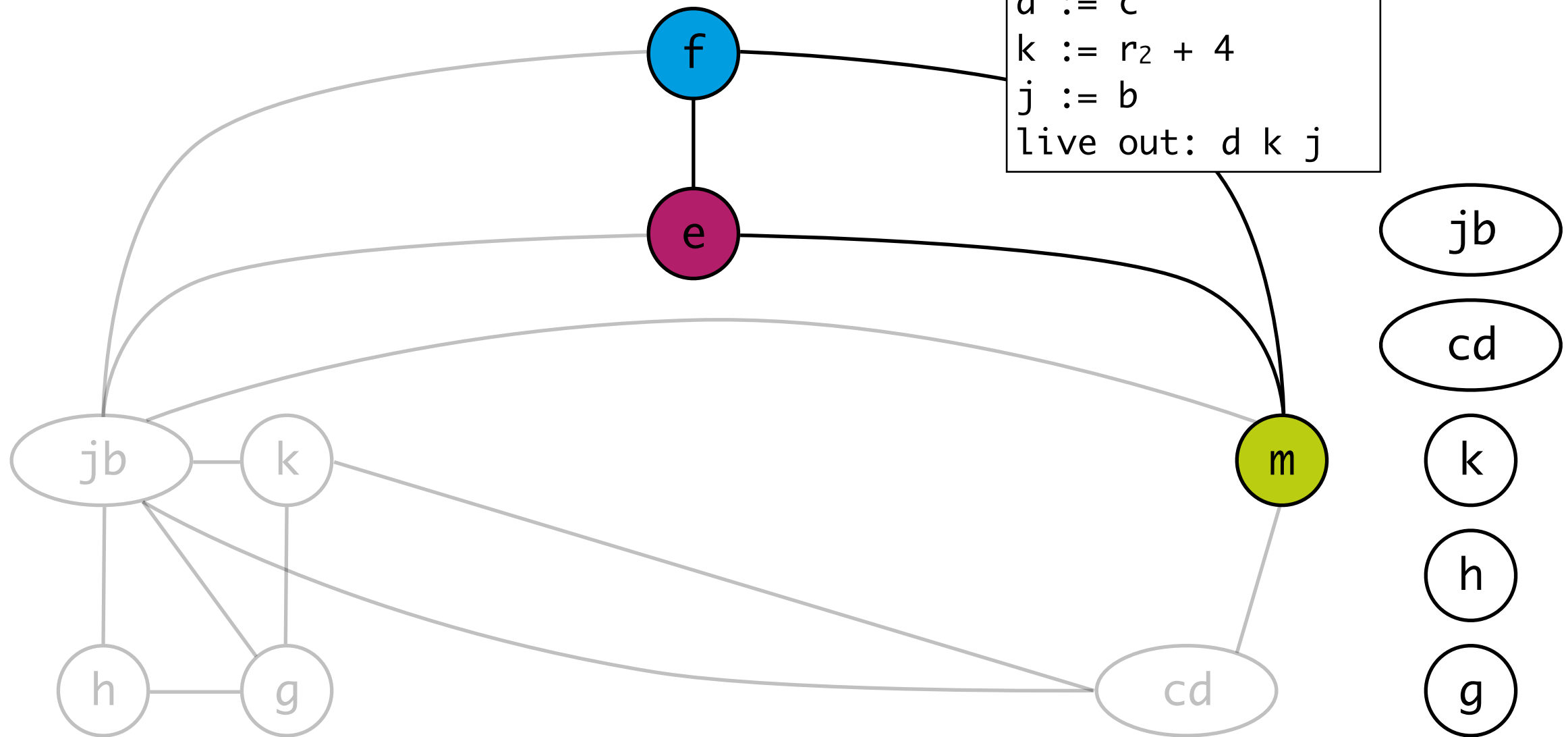
# Coalescing example

```
live-in: k j  
g := mem[j + 12]  
h := k - 1  
f := g * h  
r1 := mem[j + 8]  
r2 := mem[j + 16]  
b := mem[f]  
c := r1 + 8  
d := c  
k := r2 + 4  
j := b  
live out: d k j
```



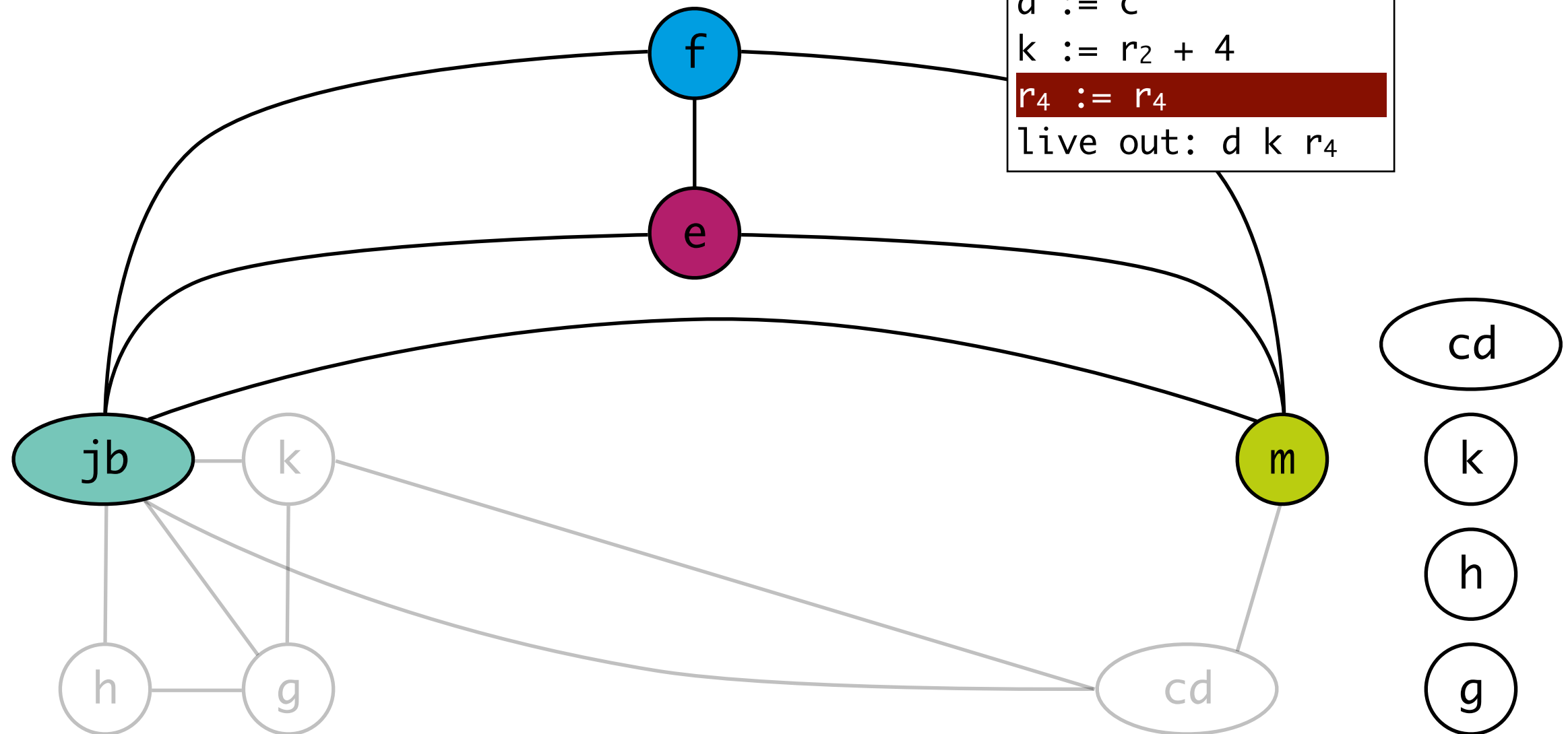
# Coalescing example

```
live-in: k j
g := mem[j + 12]
h := k - 1
r3 := g * h
r1 := mem[j + 8]
r2 := mem[j + 16]
b := mem[r3]
c := r1 + 8
d := c
k := r2 + 4
j := b
live out: d k j
```



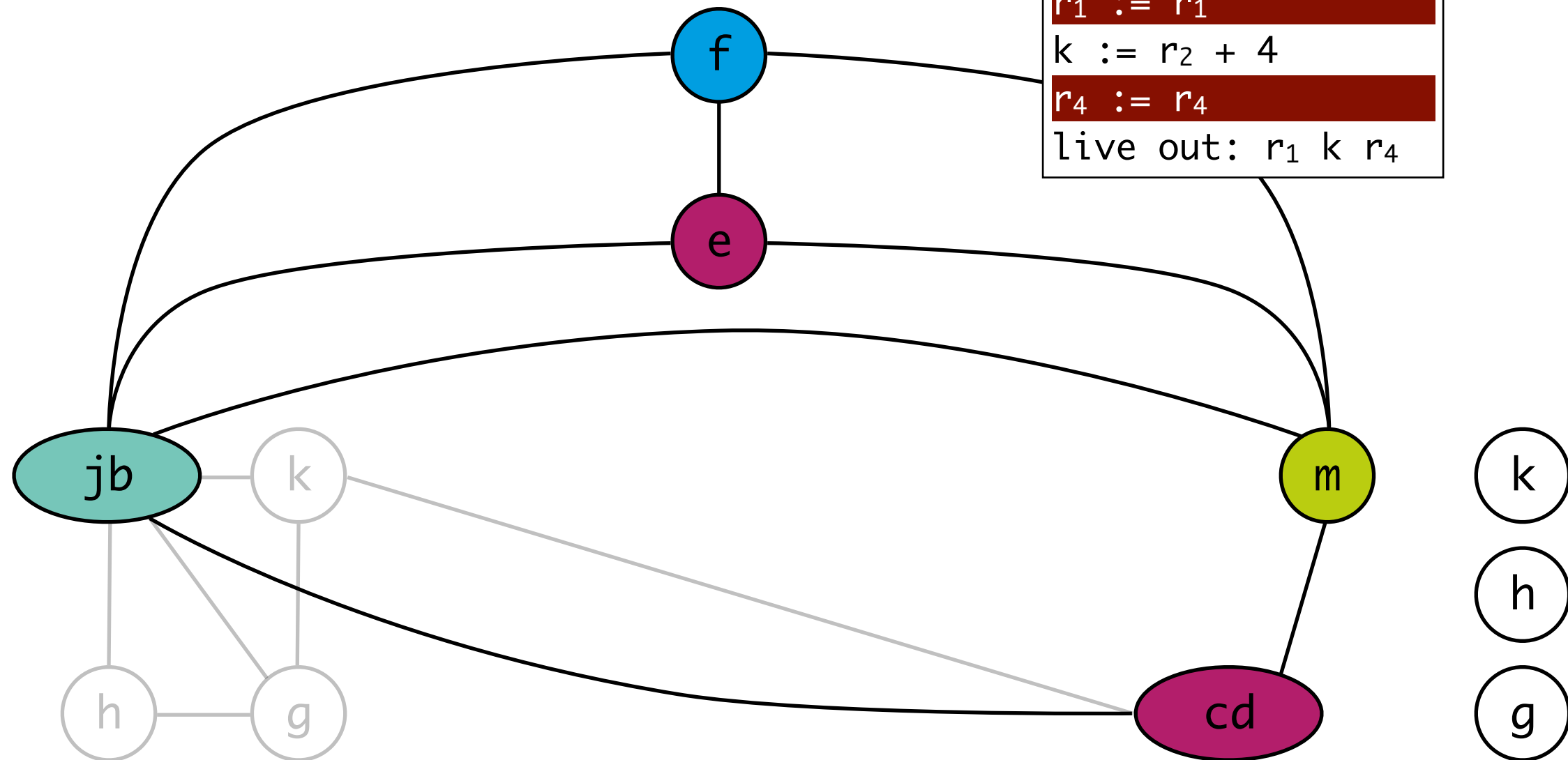
# Coalescing example

```
live-in: k r4  
g := mem[r4 + 12]  
h := k - 1  
r3 := g * h  
r1 := mem[r4 + 8]  
r2 := mem[r4 + 16]  
b := mem[r3]  
c := r1 + 8  
d := c  
k := r2 + 4  
r4 := r4  
live out: d k r4
```



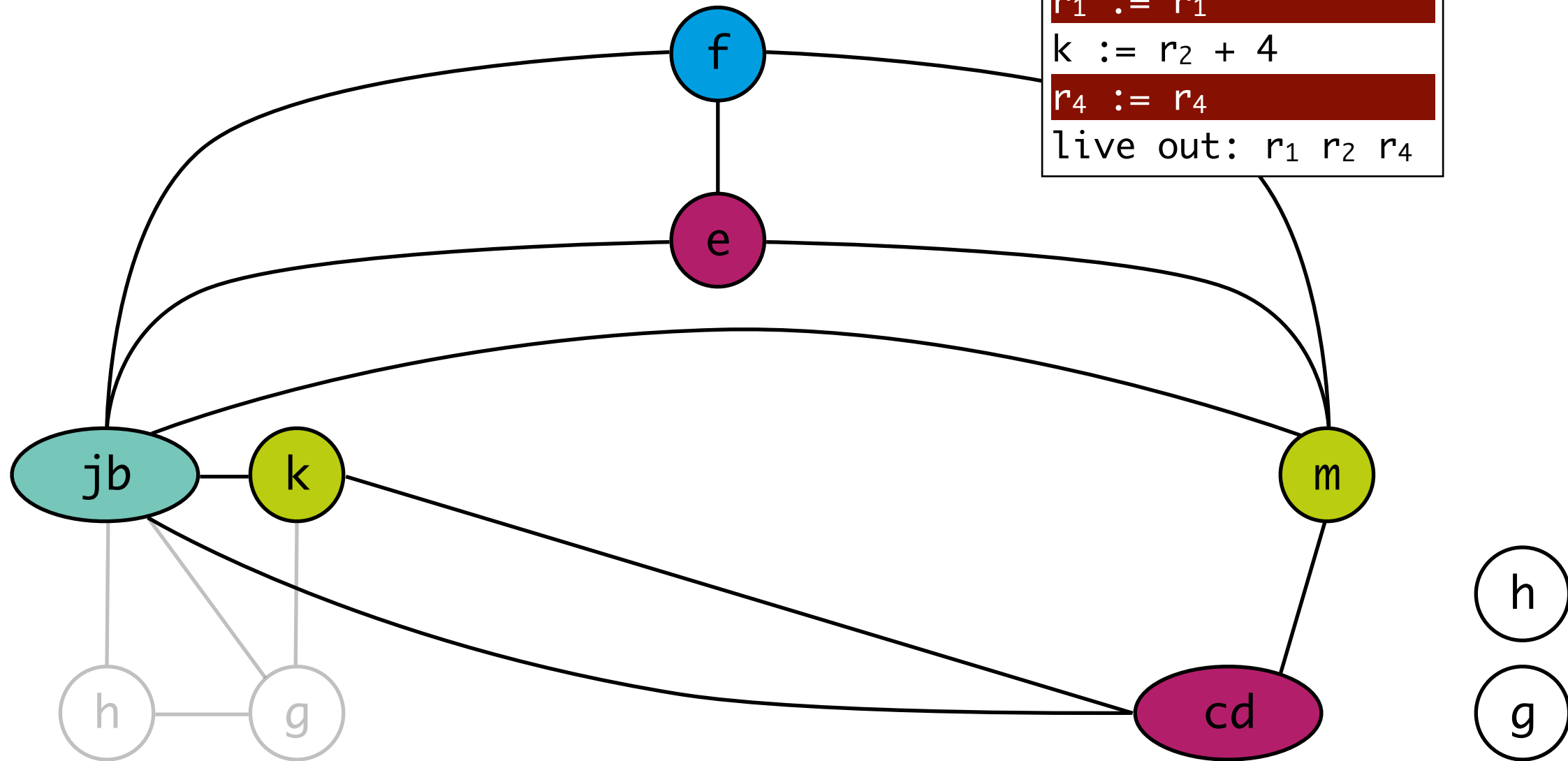
# Coalescing example

```
live-in: k r4  
g := mem[r4 + 12]  
h := k - 1  
r3 := g * h  
r1 := mem[r4 + 8]  
r2 := mem[r4 + 16]  
b := mem[r3]  
r1 := r1 + 8  
r1 := r1  
k := r2 + 4  
r4 := r4  
live out: r1 k r4
```



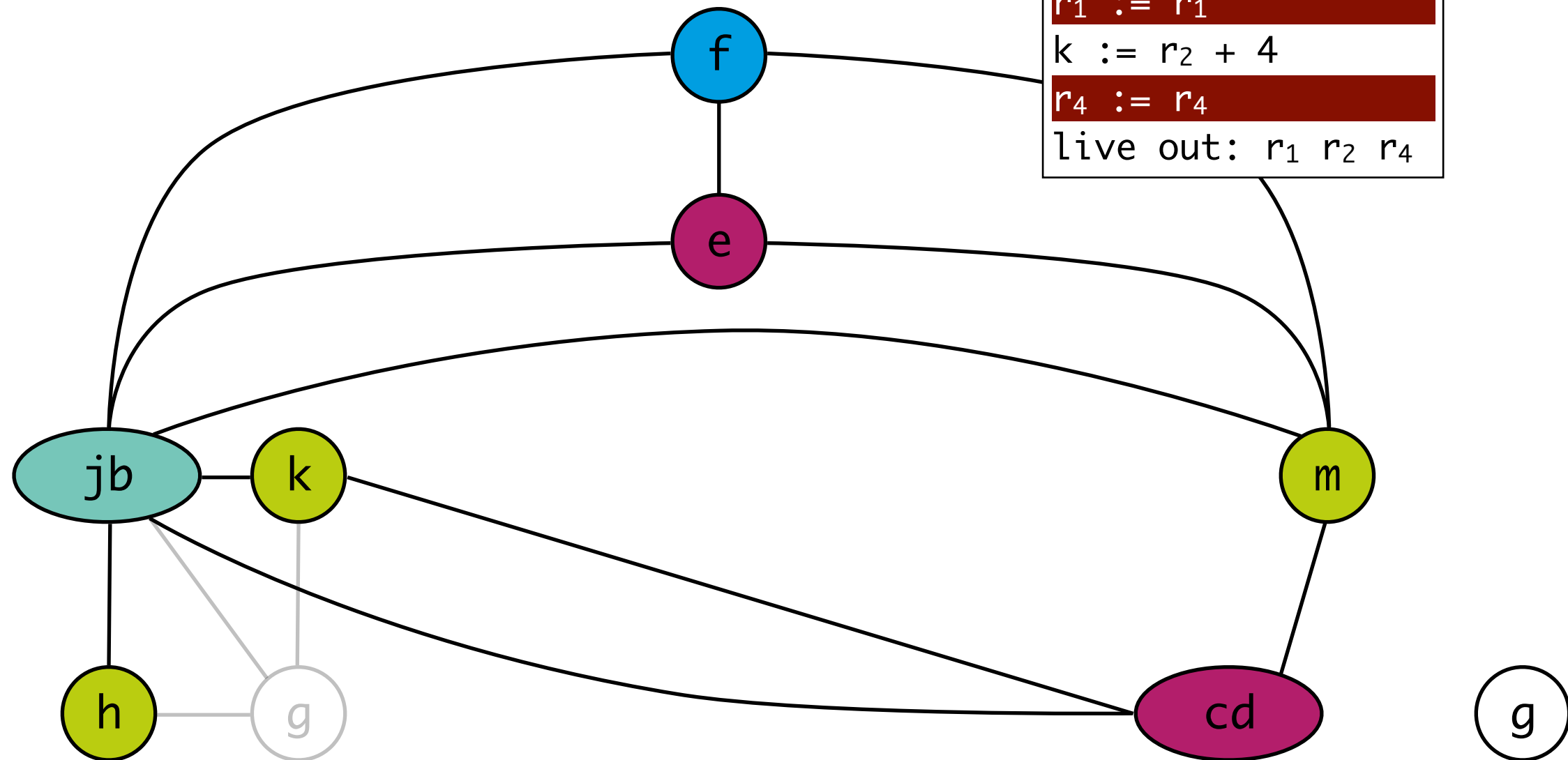
# Coalescing example

```
live-in: r2 r4  
g := mem[r4 + 12]  
h := r2 - 1  
r3 := g * h  
r1 := mem[r4 + 8]  
r2 := mem[r4 + 16]  
b := mem[r3]  
r1 := r1 + 8  
r1 := r1  
k := r2 + 4  
r4 := r4  
live out: r1 r2 r4
```



# Coalescing example

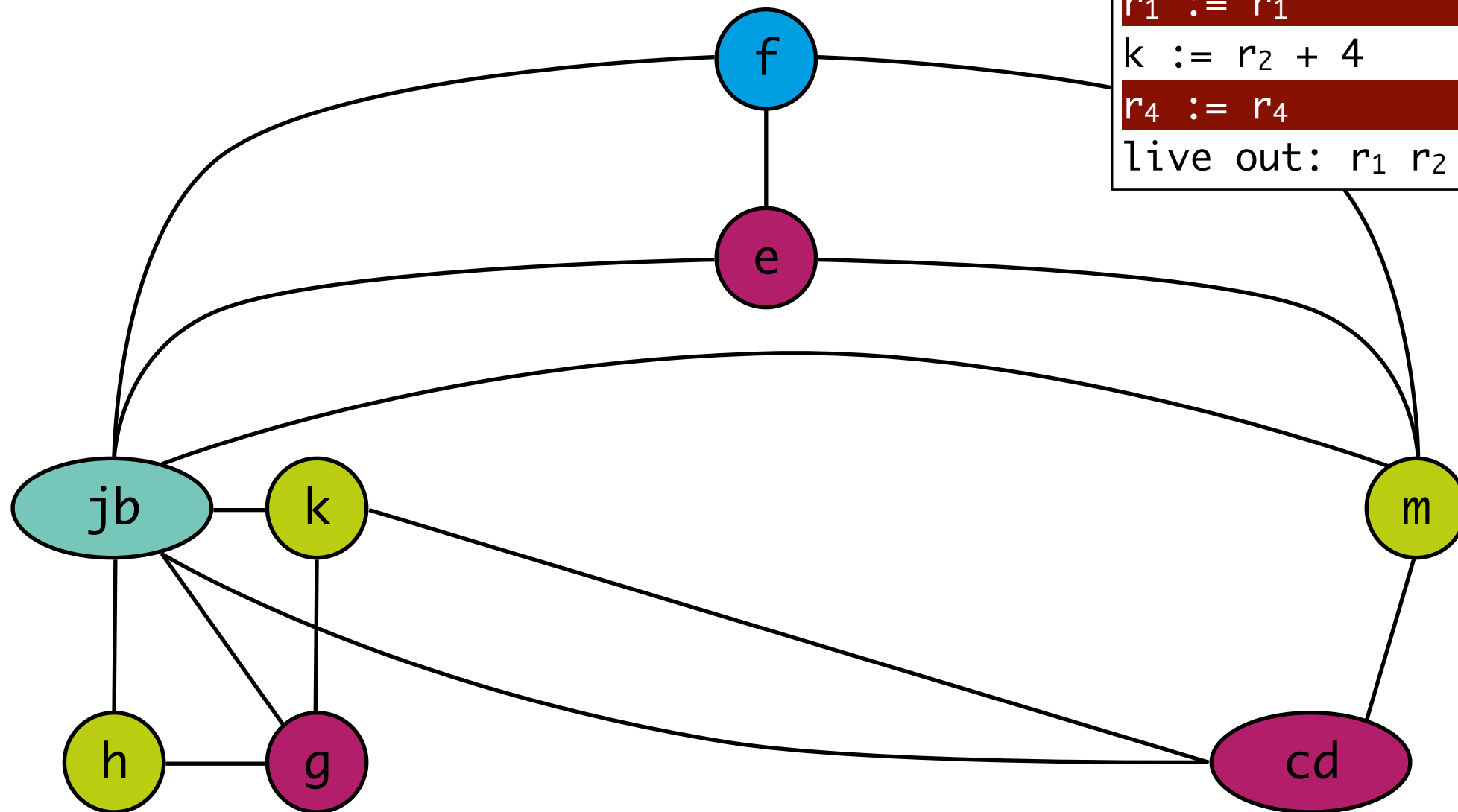
```
live-in: r2 r4  
g := mem[r4 + 12]  
r2 := r2 - 1  
r3 := g * r2  
r1 := mem[r4 + 8]  
r2 := mem[r4 + 16]  
b := mem[r3]  
r1 := r1 + 8  
r1 := r1  
k := r2 + 4  
r4 := r4  
live out: r1 r2 r4
```



# Coalescing

## coalescing nodes

```
live-in: r2 r4  
r1 := mem[r4 + 12]  
r2 := r2 - 1  
r3 := r1 * r2  
r1 := mem[r4 + 8]  
r2 := mem[r4 + 16]  
b := mem[r3]  
r1 := r1 + 8  
r1 := r1  
k := r2 + 4  
r4 := r4  
live out: r1 r2 r4
```



# V

---

## Pre-Colored Nodes

---



# Recap: Calling Conventions

## CDECL

### Caller

- push parameters right-to-left on the stack
- clean-up stack after call

```
push 21  
push 42  
call _f  
add ESP 8
```

### Callee

- save old BP
- initialise new BP
- save registers
- return result in AX
- restore registers
- restore BP

```
push EBP  
mov EBP ESP  
mov EAX [EBP + 8]  
mov EDX [EBP + 12]  
add EAX EDX  
pop EBP  
ret
```

# Recap: Calling Conventions

## STDCALL

### Caller

- push parameters right-to-left on the stack

```
push 21
push 42
call _f@8
```

### Callee

- save old BP
- initialise new BP
- save registers
- return result in AX
- restore registers
- restore BP

```
push EBP
mov EBP ESP
mov EAX [EBP + 8]
mov EDX [EBP + 12]
add EAX EDX
pop EBP
ret 8
```

# Recap: Calling Conventions

## FASTCALL

### Caller

- passes parameters in registers
- pushes additional parameters right-to-left on the stack
- cleans up the stack

```
mov  ECX 21  
mov  EDX 42  
call @f@8
```

### Callee

- save old BP, initialise new BP
- save registers
- return result in AX
- restore registers
- restore BP

```
push EBP  
mov  EBP ESP  
mov  EAX ECX  
add  EAX EDX  
pop  EBP  
ret
```

# Recap: Calling Conventions

## saving registers

Not enough registers for all local variables across life time

- save register to memory to free for other use

Caller-save registers

- Caller is responsible for saving and restoring register

Callee-save registers

- Callee is responsible for saving and restoring register

Use callee-save registers to pass parameters

# Pre-Colored Nodes

## representing registers

### Nodes

- register = pre-colored node
- no simplify, no spill
- coalesce possible

### Edges

- all registers interfere with each other
- explicit usage of registers
- call and return instructions influence liveness

# Callee-Save Register in Temporary

pre-colored nodes

```
enter: def(r7)
```

...

```
exit: use(r7)
```

```
enter: def(r7)
```

```
      t ← r7
```

...

```
      r7 ← t
```

```
exit:  use(r7)
```

# Pre-Colored Nodes

## example

```
int f(int a, int b) {  
    int d = 0;  
    int e = a;  
    do {  
        d = d + b;  
        e = e - 1;  
    } while (e > 0);  
    return d;  
}
```

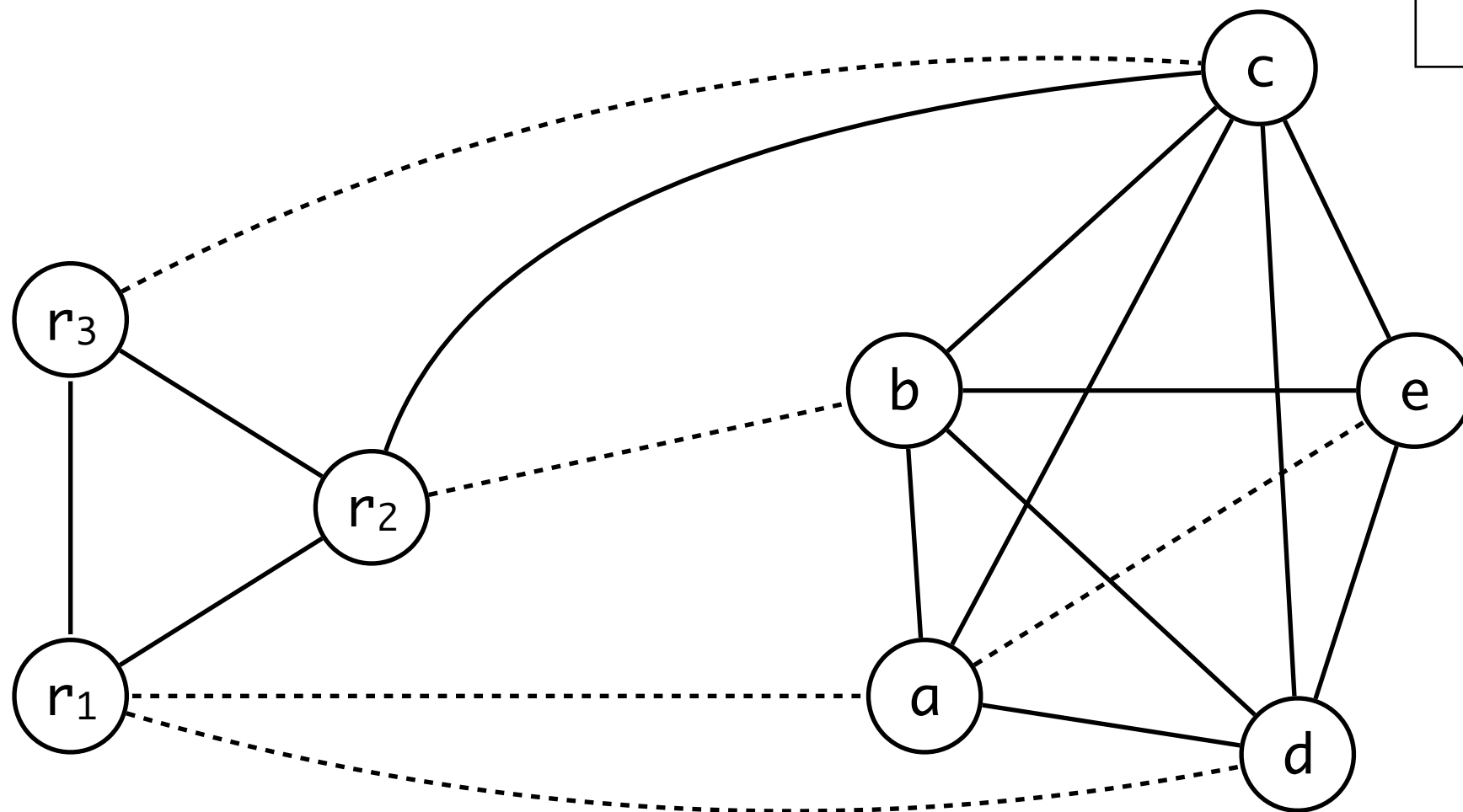
```
enter : c ← r3      // callee-save  
        a ← r1      // caller-save  
        b ← r2      // caller-save  
        d ← 0  
        e ← a  
loop :  d ← d + b  
        e ← e - 1  
        if e > 0 goto loop  
        r1 ← d  
        r3 ← c  
        return (r1, r3 live out)
```

machine has 3 registers

# Pre-Colored Nodes

## example

```
enter : c ← r3  
       a ← r1  
       b ← r2  
       d ← 0  
       e ← a  
loop  : d ← d + b  
       e ← e - 1  
       if e > 0 goto loop  
       r1 ← d  
       r3 ← c  
       return (r1, r3)
```



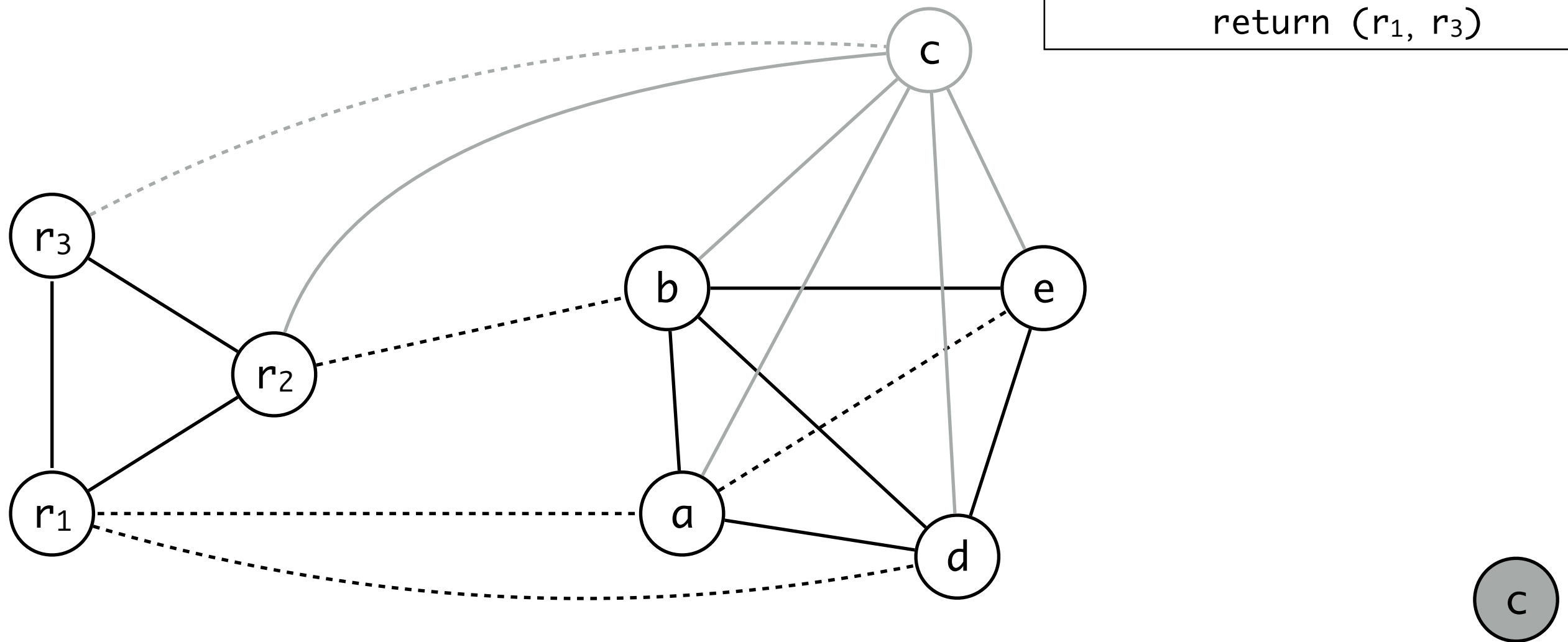


# Pre-Colored Nodes

## example

spill c

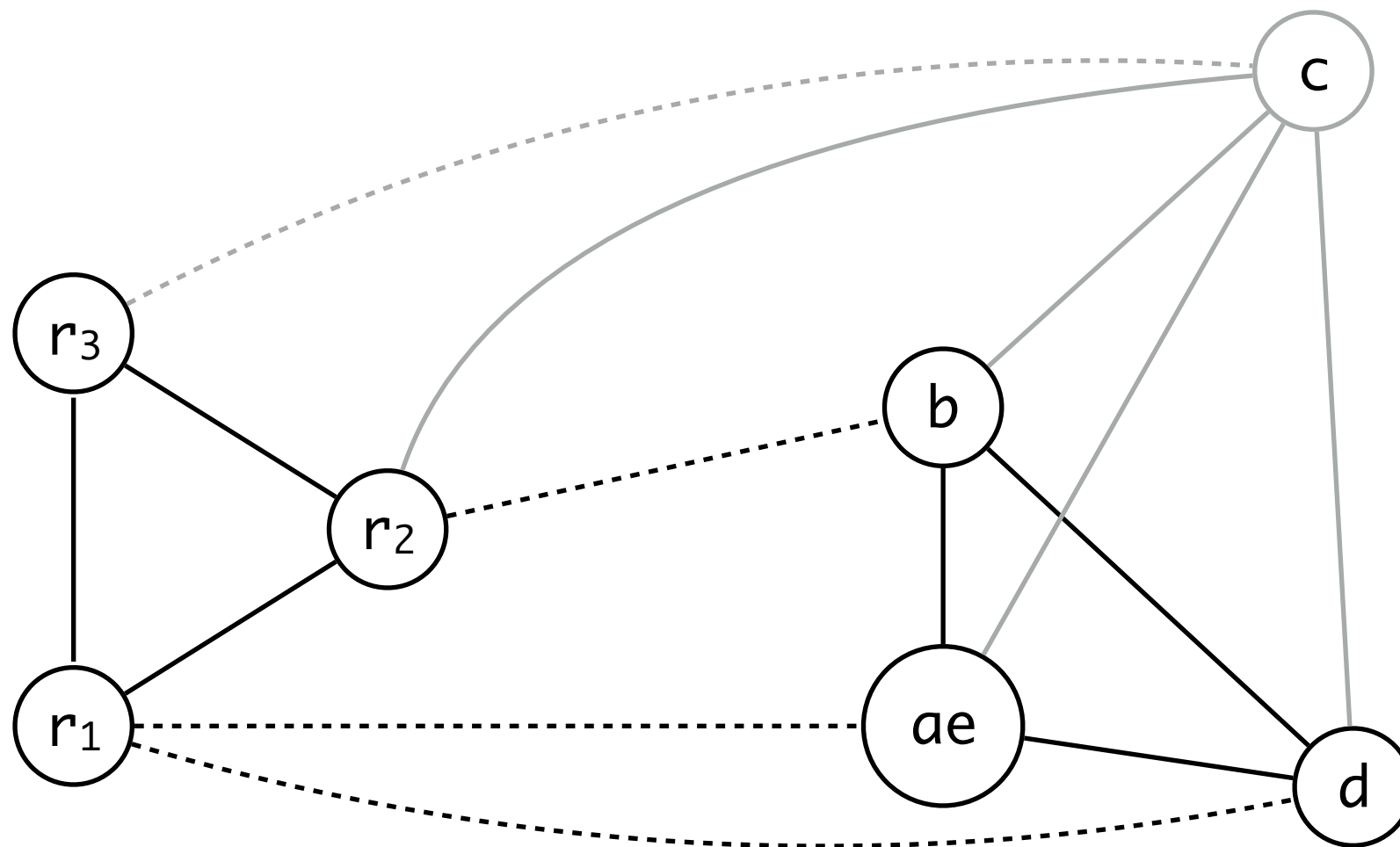
```
enter : c ← r3  
        a ← r1  
        b ← r2  
        d ← 0  
        e ← a  
loop :  d ← d + b  
        e ← e - 1  
        if e > 0 goto loop  
        r1 ← d  
        r3 ← c  
        return (r1, r3)
```



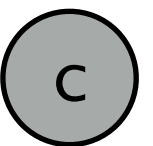
# Pre-Colored Nodes

## example

coalesce a and e



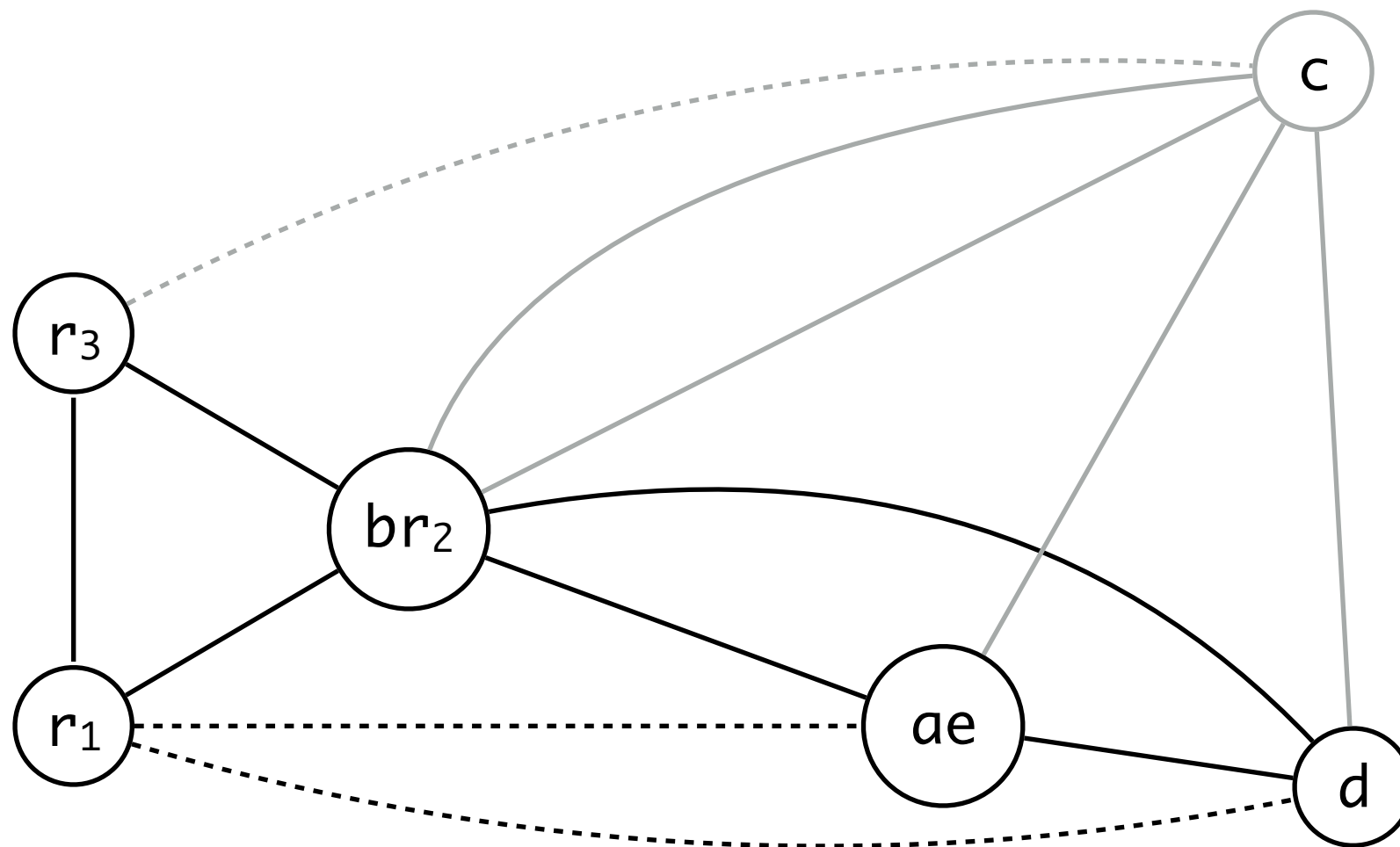
```
enter : c ← r3
        a ← r1
        b ← r2
        d ← 0
        e ← a
loop :  d ← d + b
        e ← e - 1
        if e > 0 goto loop
        r1 ← d
        r3 ← c
        return (r1, r3)
```



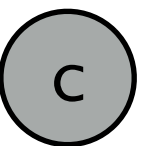
# Pre-Colored Nodes

## example

coalesce  $r_2$  and  $b$



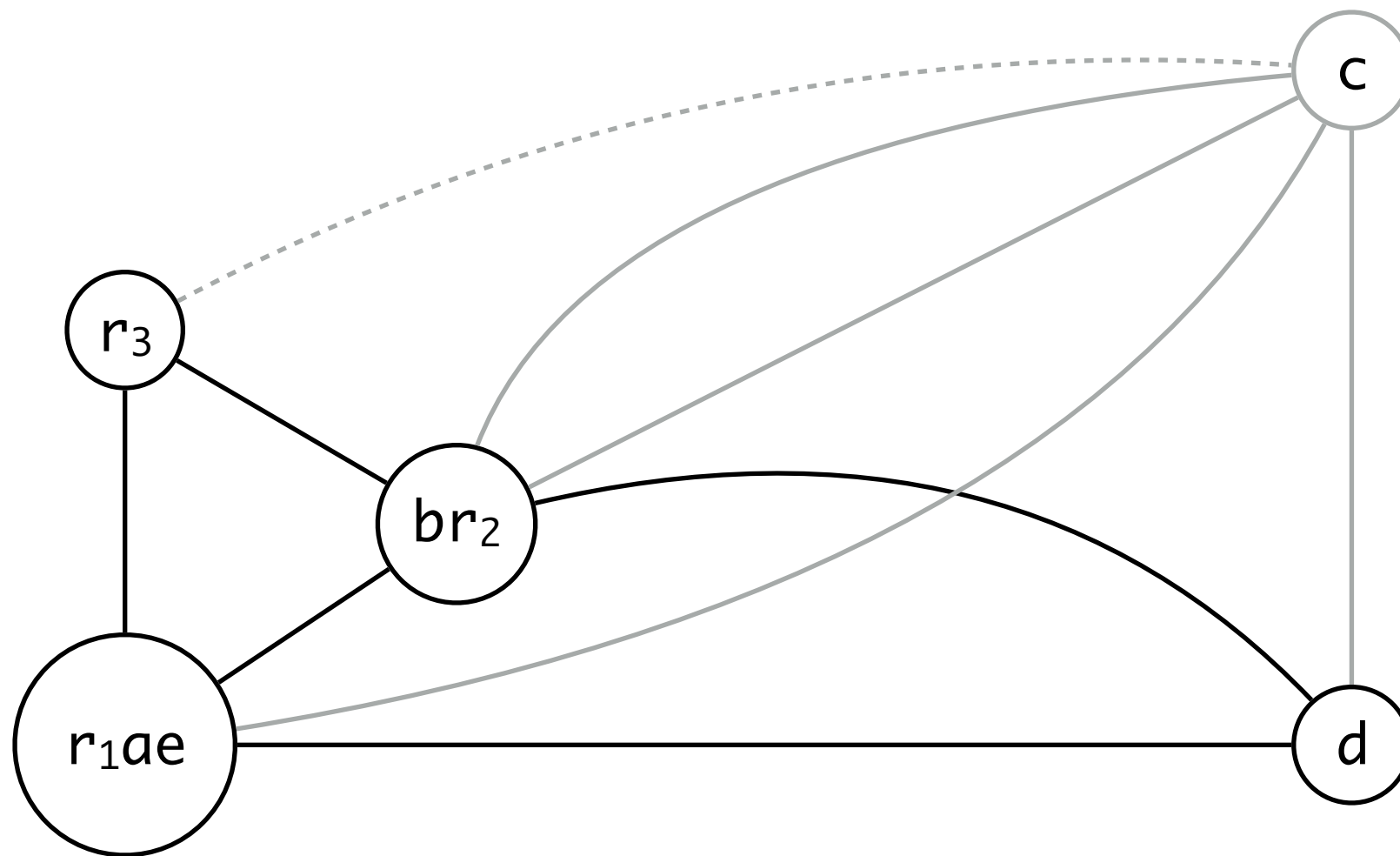
```
enter : c ← r3  
        a ← r1  
        b ← r2  
        d ← 0  
        e ← a  
loop  : d ← d + b  
        e ← e - 1  
        if e > 0 goto loop  
        r1 ← d  
        r3 ← c  
        return (r1, r3)
```



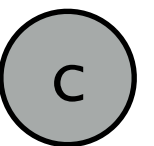
# Pre-Colored Nodes

## example

coalesce  $r_1$  and  $ae$



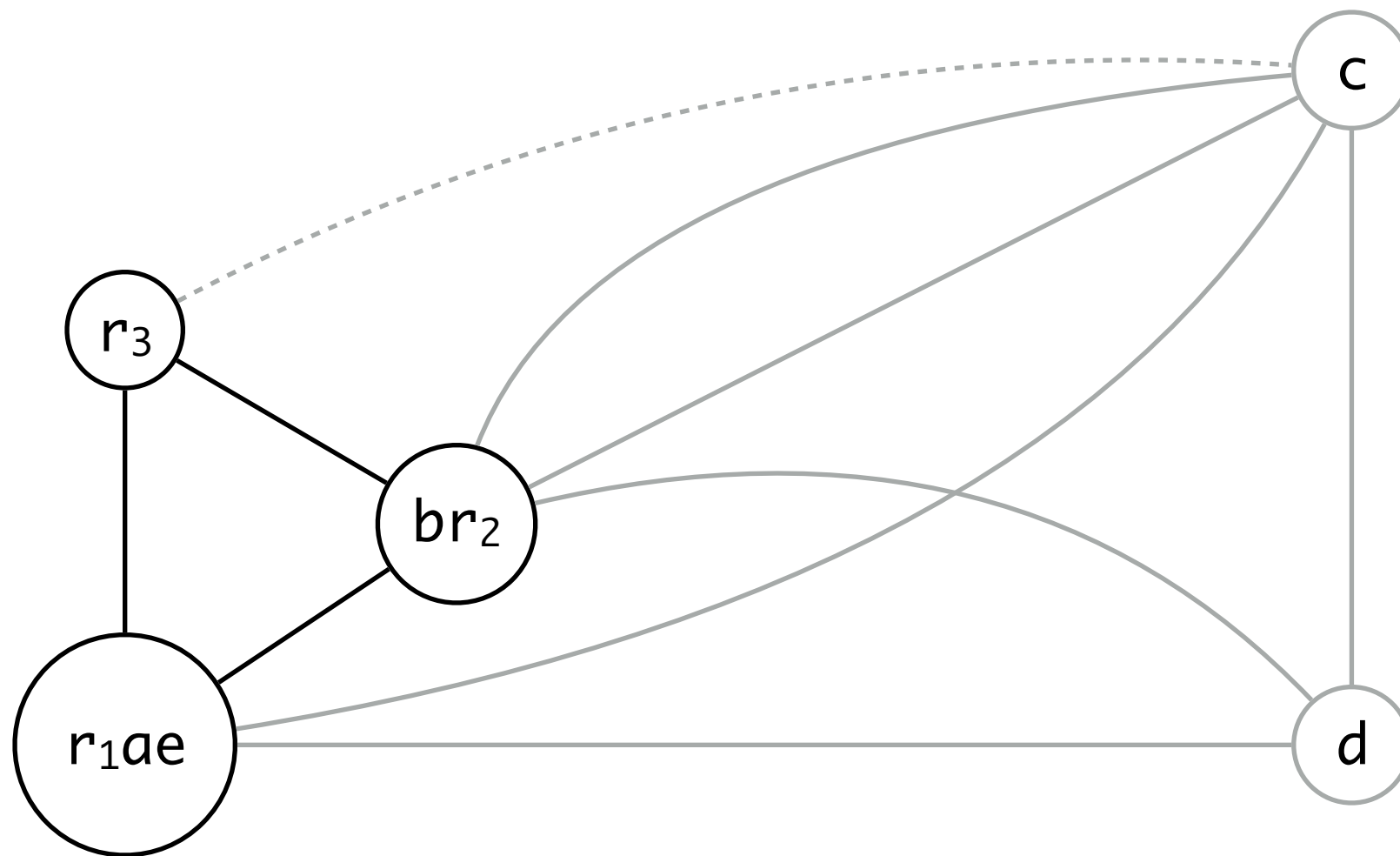
```
enter : c ← r3
        a ← r1
        b ← r2
        d ← 0
        e ← a
loop  : d ← d + b
        e ← e - 1
        if e > 0 goto loop
        r1 ← d
        r3 ← c
        return (r1, r3)
```



# Pre-Colored Nodes

example

simplify d



```
enter : c ← r3  
       a ← r1  
       b ← r2  
       d ← 0  
       e ← a  
loop  : d ← d + b  
       e ← e - 1  
       if e > 0 goto loop  
       r1 ← d  
       r3 ← c  
       return (r1, r3)
```

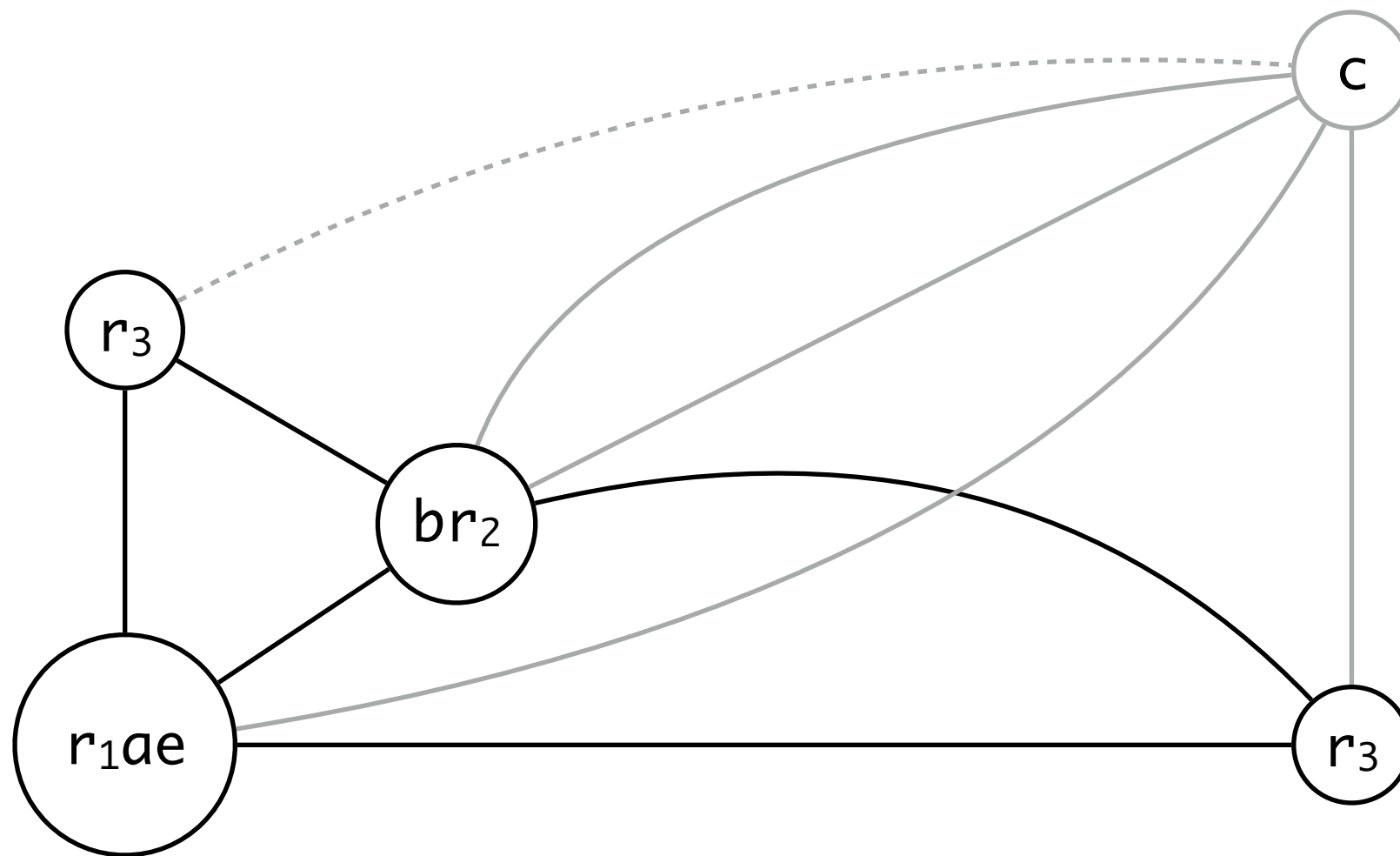
d

c

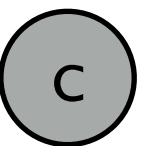
# Pre-Colored Nodes

## example

color d as r<sub>3</sub>



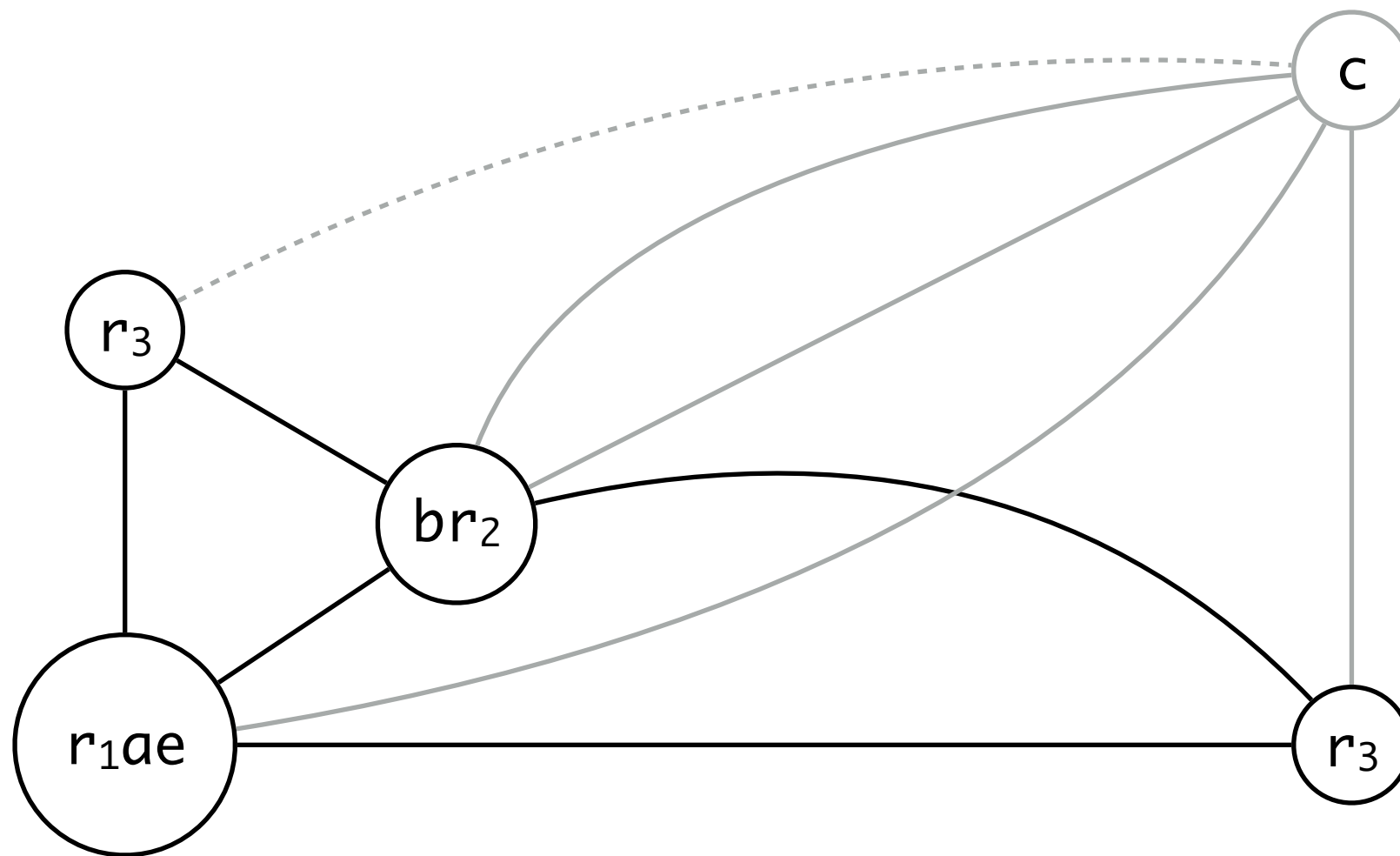
```
enter : c ← r3
        a ← r1
        b ← r2
        d ← 0
        e ← a
loop :  d ← d + b
        e ← e - 1
        if e > 0 goto loop
        r1 ← d
        r3 ← c
        return (r1, r3)
```



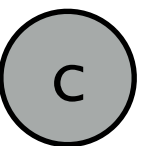
# Pre-Colored Nodes

## example

spill c



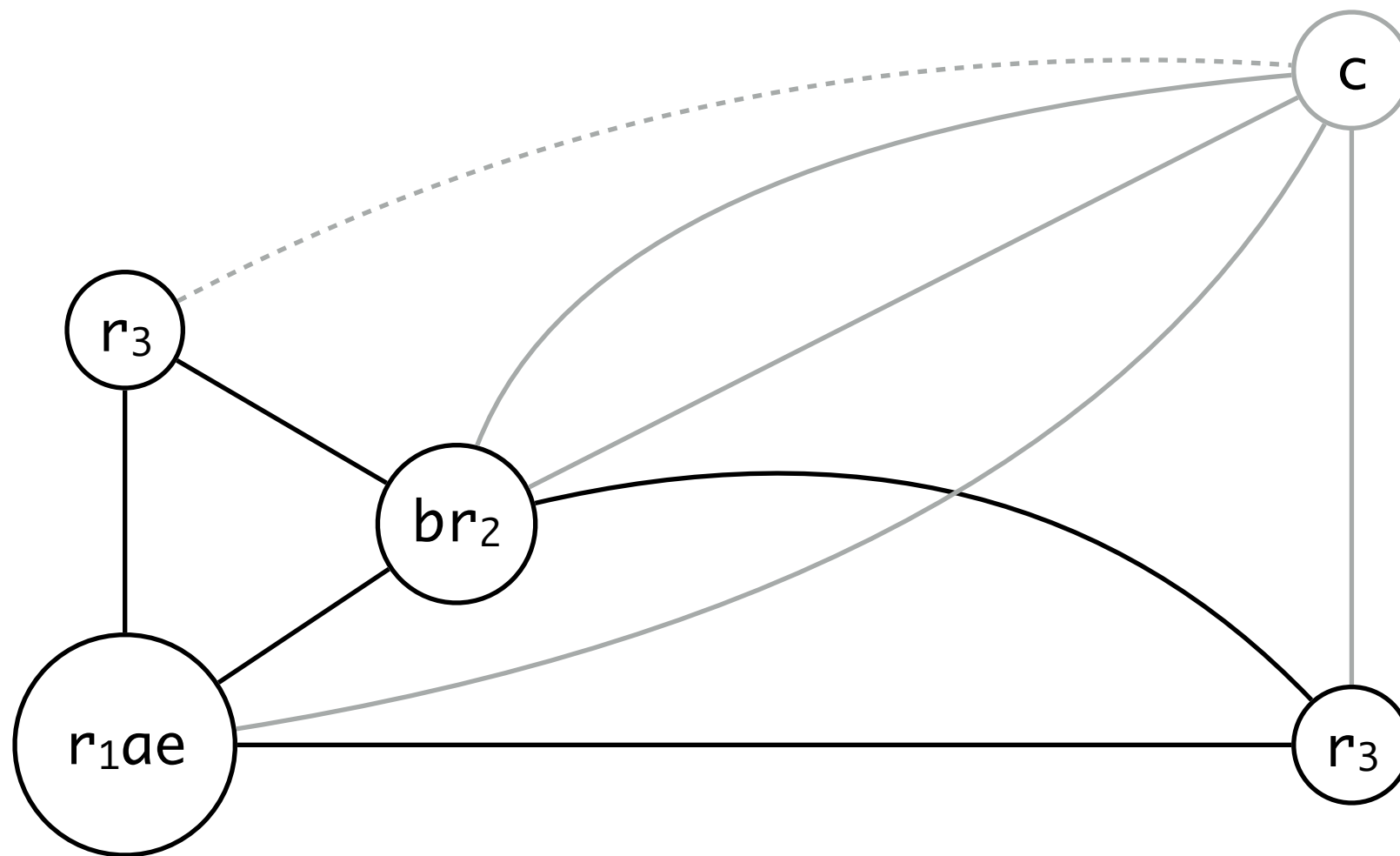
```
enter : c1 ← r3
        M[cloc] ← c1
        a ← r1
        b ← r2
        d ← 0
        e ← a
loop :  d ← d + b
        e ← e - 1
        if e > 0 goto loop
        r1 ← d
        r3 ← c2
        c2 ← M[cloc]
        return (r1, r3)
```



# Pre-Colored Nodes

## example

spill c



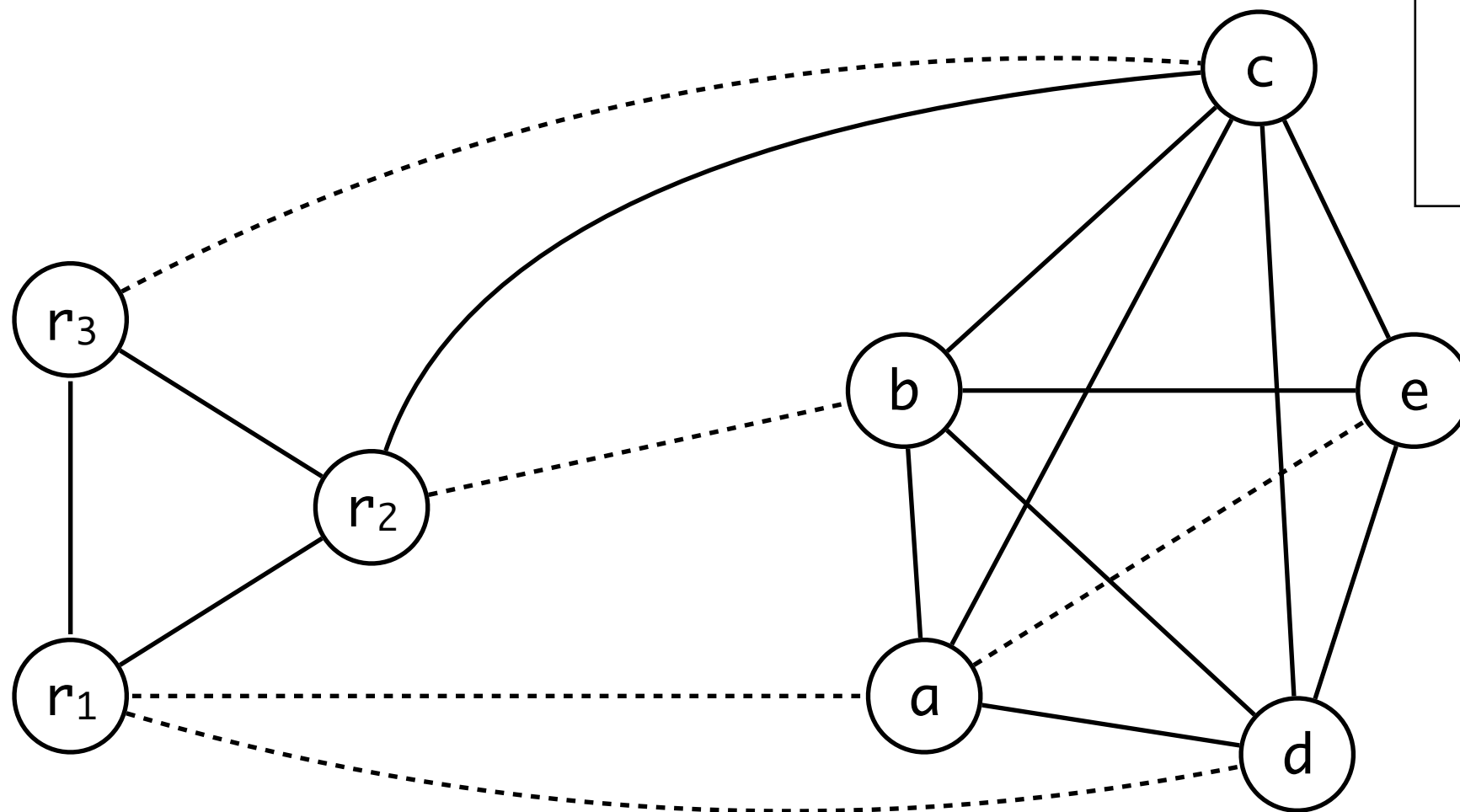
```
enter :  $c_1 \leftarrow r_3$   
         $M[c_{loc}] \leftarrow c_1$   
         $a \leftarrow r_1$   
         $b \leftarrow r_2$   
         $d \leftarrow 0$   
         $e \leftarrow a$   
loop :   $d \leftarrow d + b$   
         $e \leftarrow e - 1$   
        if  $e > 0$  goto loop  
         $r_1 \leftarrow d$   
         $r_3 \leftarrow c_2$   
         $c_2 \leftarrow M[c_{loc}]$   
        return ( $r_1, r_3$ )
```



# Pre-Colored Nodes

## examples

start over

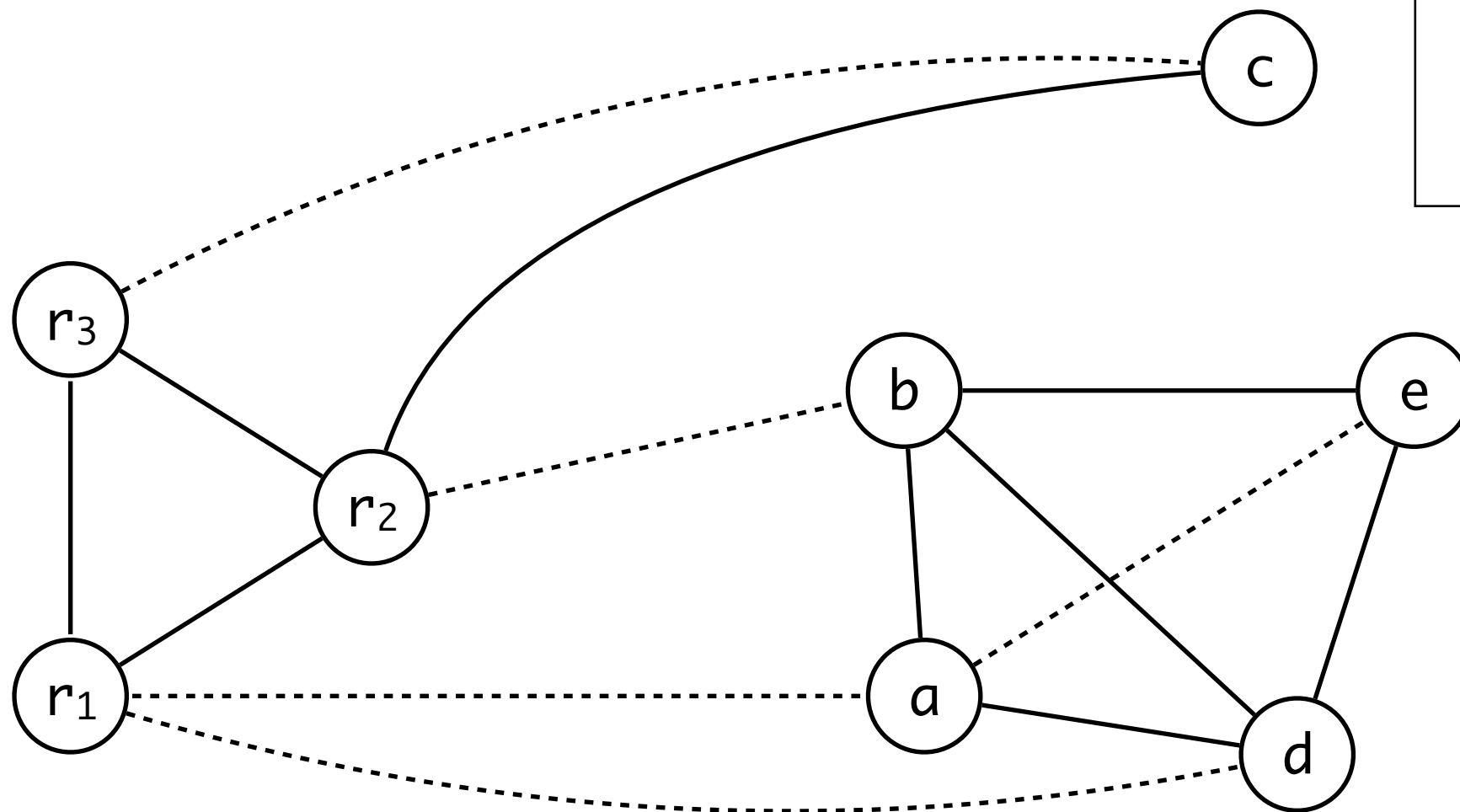


```
enter :  $c_1 \leftarrow r_3$   
         $M[c_{loc}] \leftarrow c_1$   
         $a \leftarrow r_1$   
         $b \leftarrow r_2$   
         $d \leftarrow 0$   
         $e \leftarrow a$   
loop :   $d \leftarrow d + b$   
         $e \leftarrow e - 1$   
        if  $e > 0$  goto loop  
         $r_1 \leftarrow d$   
         $r_3 \leftarrow c_2$   
         $c_2 \leftarrow M[c_{loc}]$   
        return ( $r_1, r_3$ )
```

# Pre-Colored Nodes

## examples

```
enter : c1 ← r3  
        M[cloc] ← c1  
        a ← r1  
        b ← r2  
        d ← 0  
        e ← a  
loop :  d ← d + b  
        e ← e - 1  
        if e > 0 goto loop  
        r1 ← d  
        r3 ← c2  
        c2 ← M[cloc]  
        return (r1, r3)
```

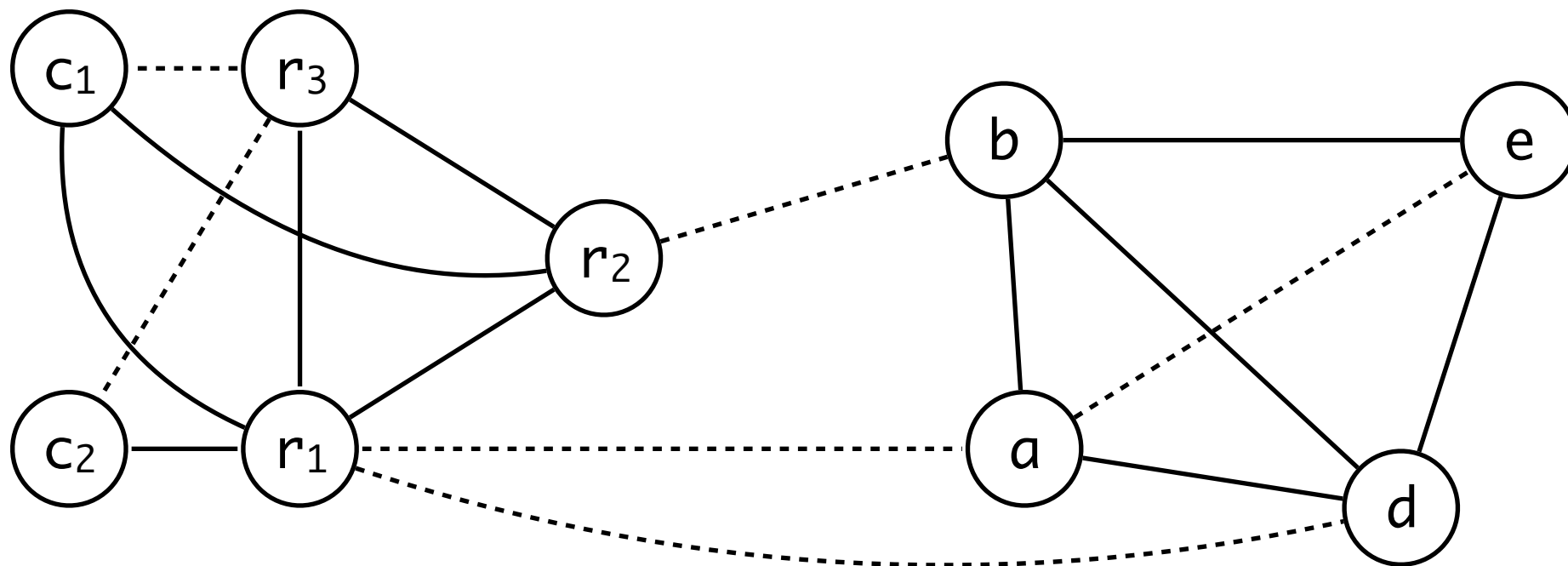


# Pre-Colored Nodes

## examples

new graph

```
enter : c1 ← r3
        M[cloc] ← c1
        a ← r1
        b ← r2
        d ← 0
        e ← a
loop  : d ← d + b
        e ← e - 1
        if e > 0 goto loop
        r1 ← d
        r3 ← c2
        c2 ← M[cloc]
        return (r1, r3)
```

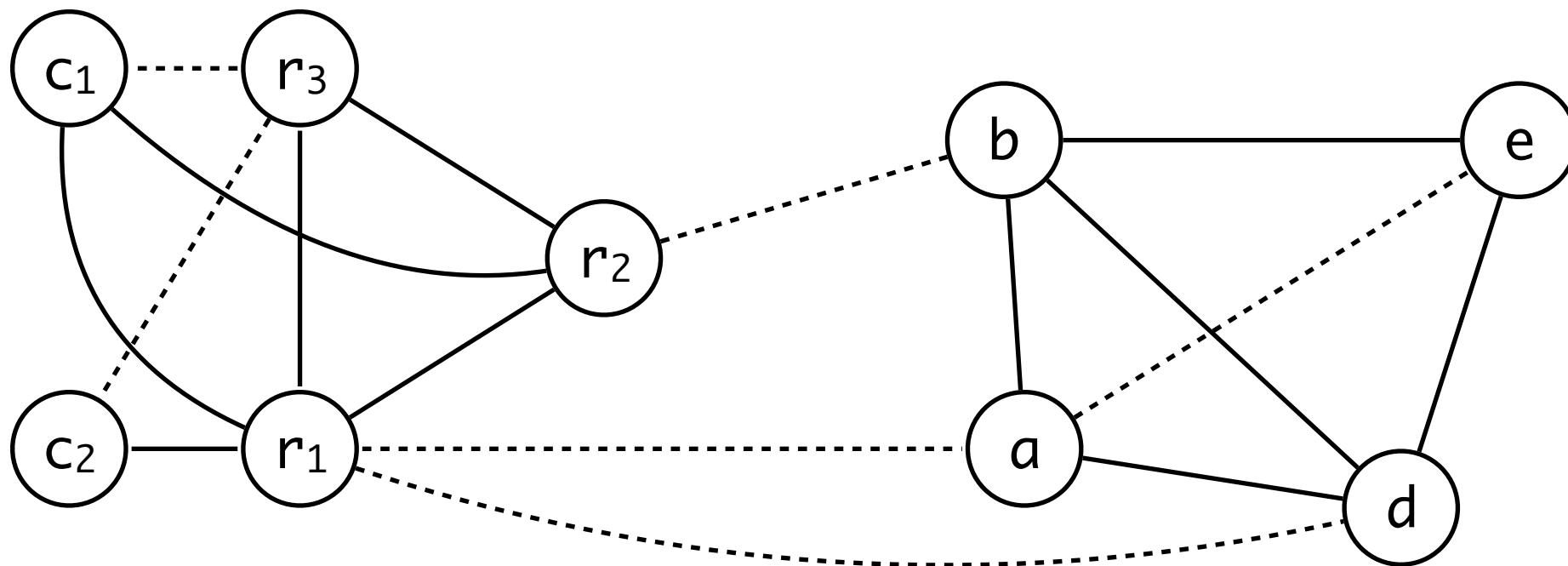


# Pre-Colored Nodes

## examples

coalesce  $c_1, c_2, r_3$

```
enter :  $c_1 \leftarrow r_3$   
         $M[c_{loc}] \leftarrow c_1$   
         $a \leftarrow r_1$   
         $b \leftarrow r_2$   
         $d \leftarrow 0$   
         $e \leftarrow a$   
loop :   $d \leftarrow d + b$   
         $e \leftarrow e - 1$   
        if  $e > 0$  goto loop  
         $r_1 \leftarrow d$   
         $r_3 \leftarrow c_2$   
         $c_2 \leftarrow M[c_{loc}]$   
        return ( $r_1, r_3$ )
```

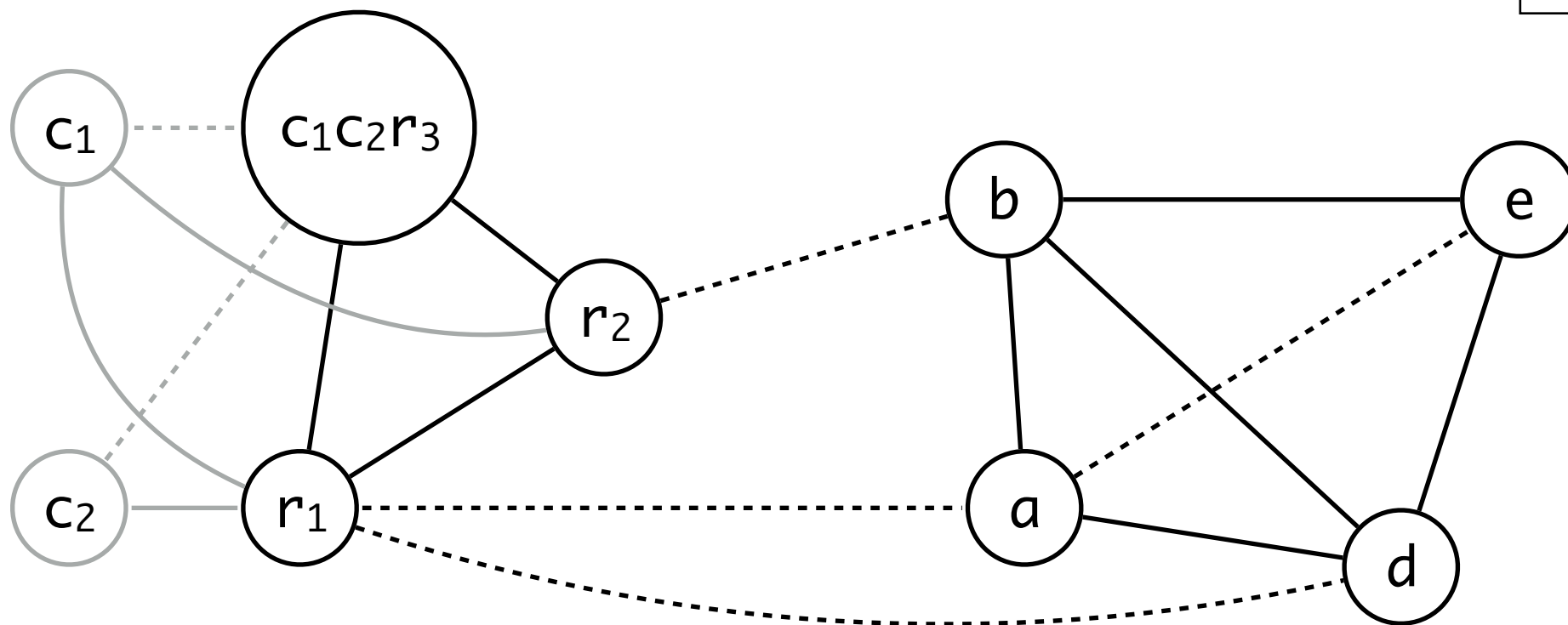


# Pre-Colored Nodes

## examples

coalesce  $c_1, c_2, r_3$

```
enter :  $c_1 \leftarrow r_3$   
         $M[c_{loc}] \leftarrow c_1$   
         $a \leftarrow r_1$   
         $b \leftarrow r_2$   
         $d \leftarrow 0$   
         $e \leftarrow a$   
loop :   $d \leftarrow d + b$   
         $e \leftarrow e - 1$   
        if  $e > 0$  goto loop  
         $r_1 \leftarrow d$   
         $r_3 \leftarrow c_2$   
         $c_2 \leftarrow M[c_{loc}]$   
        return ( $r_1, r_3$ )
```

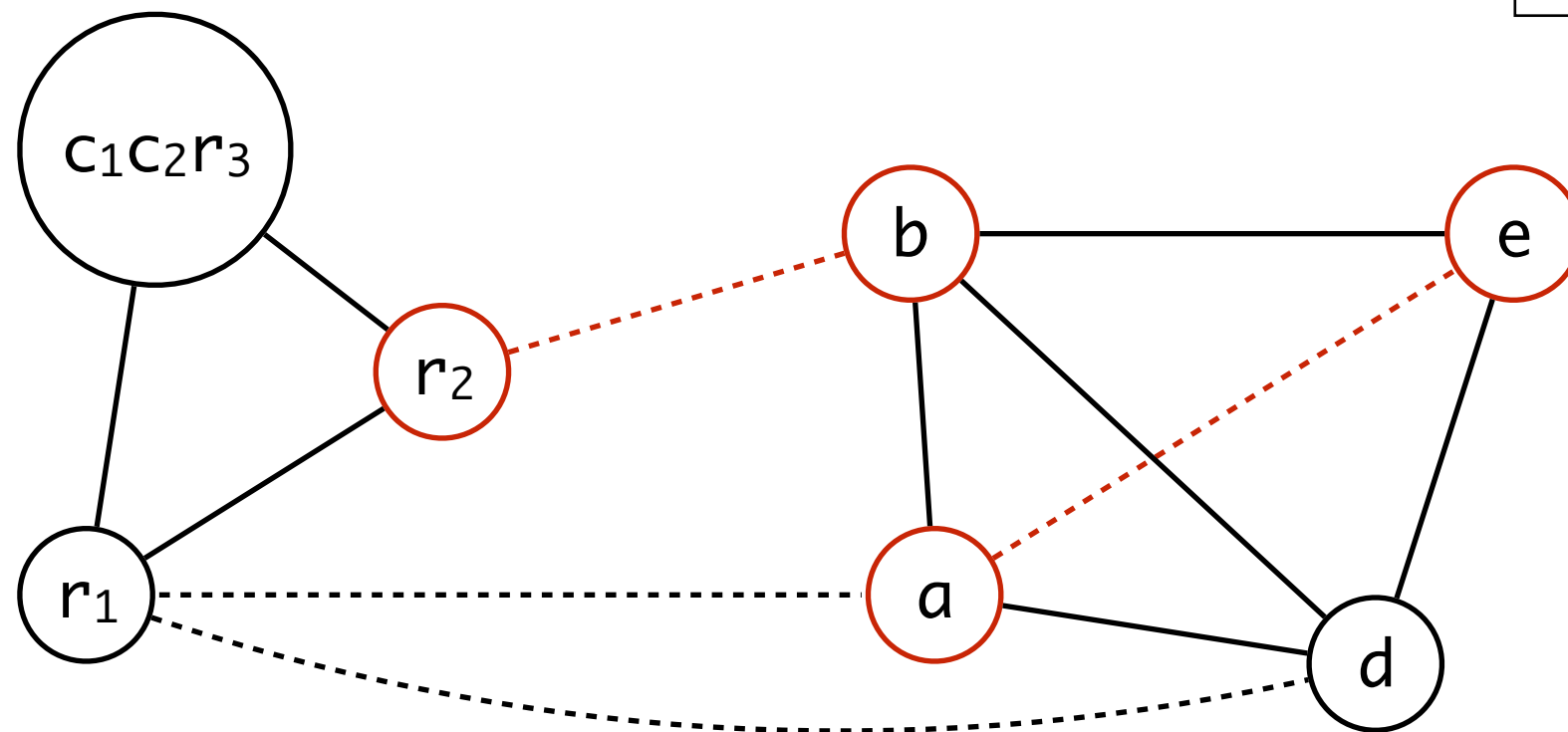


# Pre-Colored Nodes

## examples

coalesce (b, r<sub>2</sub>) and (a, e)

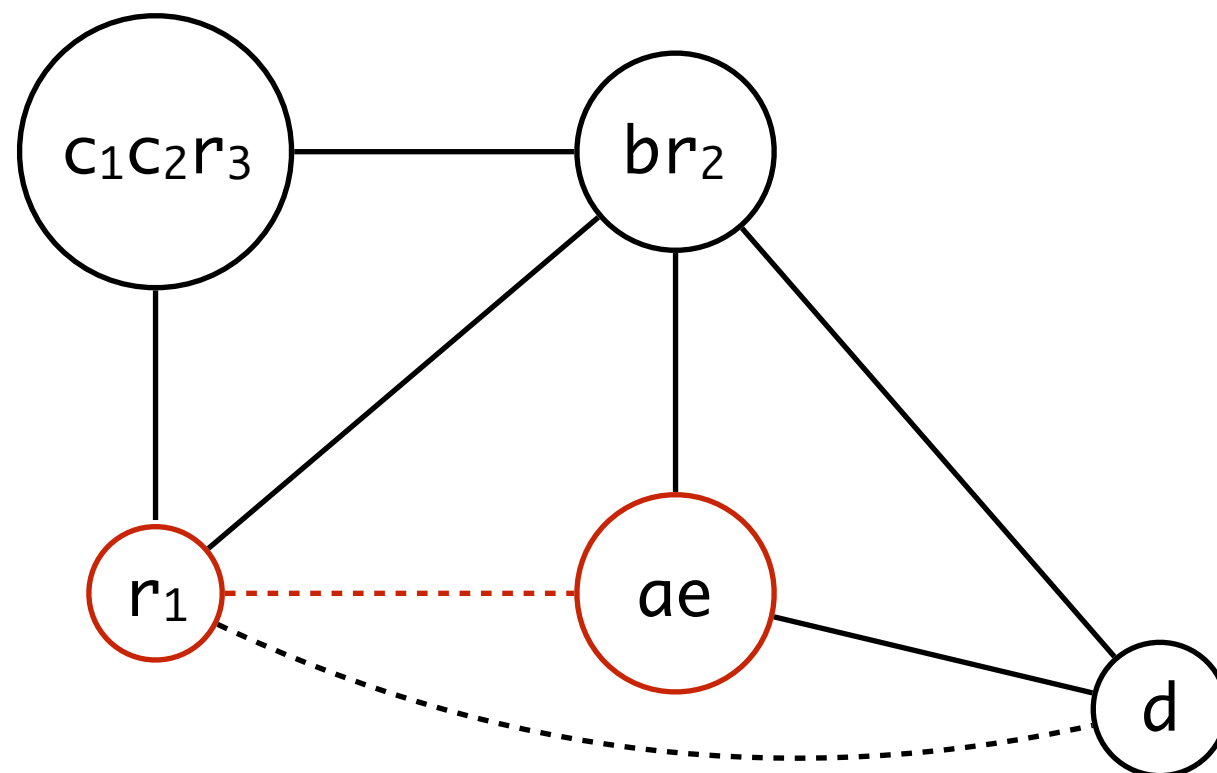
```
enter : c1 ← r3  
        M[cloc] ← c1  
        a ← r1  
        b ← r2  
        d ← 0  
        e ← a  
loop  : d ← d + b  
        e ← e - 1  
        if e > 0 goto loop  
        r1 ← d  
        r3 ← c2  
        c2 ← M[cloc]  
        return (r1, r3)
```



# Pre-Colored Nodes

## examples

coalesce (ae, r<sub>1</sub>)

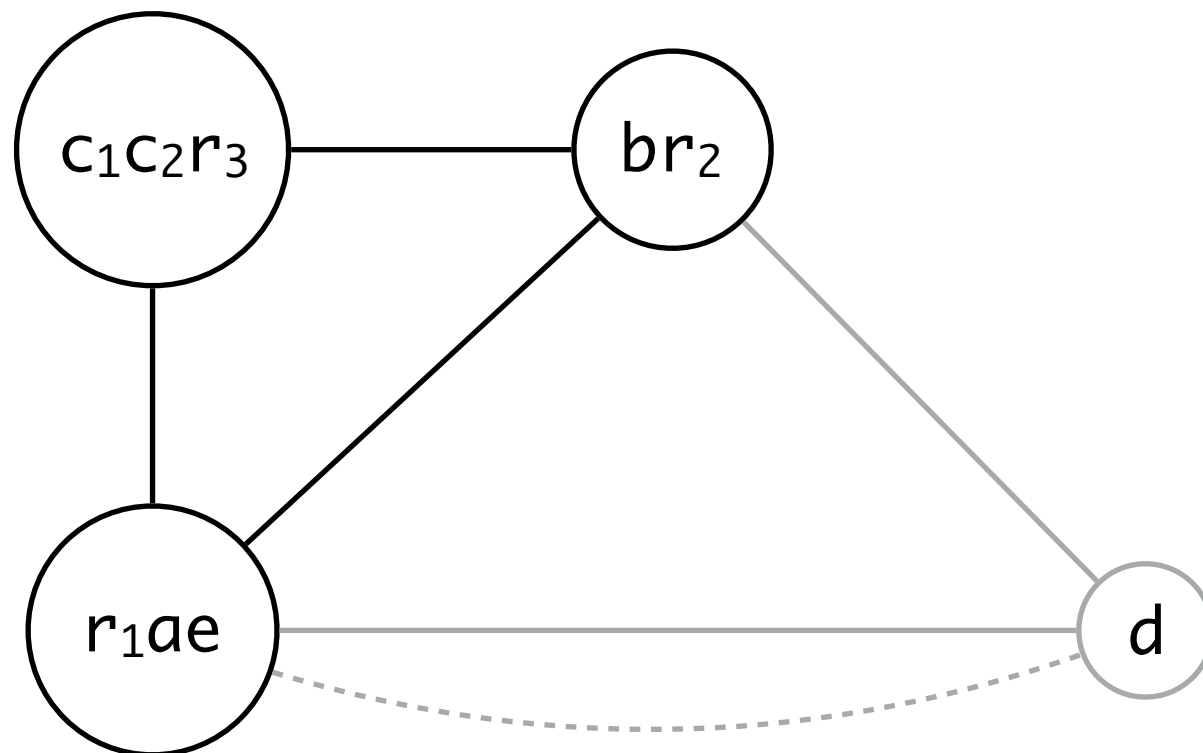


```
enter : c1 ← r3
        M[cloc] ← c1
        a ← r1
        b ← r2
        d ← 0
        e ← a
loop :  d ← d + b
        e ← e - 1
        if e > 0 goto loop
        r1 ← d
        r3 ← c2
        c2 ← M[cloc]
        return (r1, r3)
```

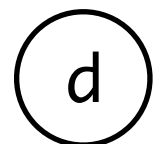
# Pre-Colored Nodes

## examples

simplify d



```
enter : c1 ← r3  
        M[cloc] ← c1  
        a ← r1  
        b ← r2  
        d ← 0  
        e ← a  
loop  : d ← d + b  
        e ← e - 1  
        if e > 0 goto loop  
        r1 ← d  
        r3 ← c2  
        c2 ← M[cloc]  
        return (r1, r3)
```

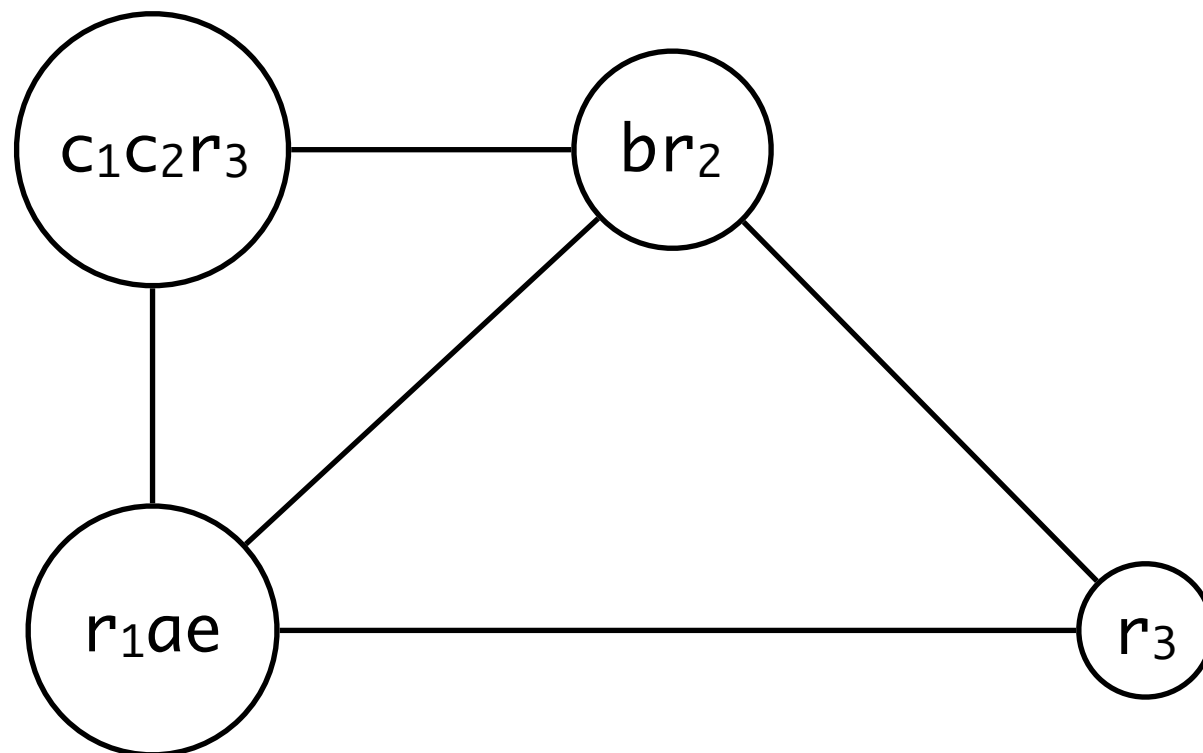




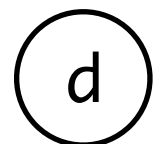
# Pre-Colored Nodes

## examples

color d as r<sub>3</sub>



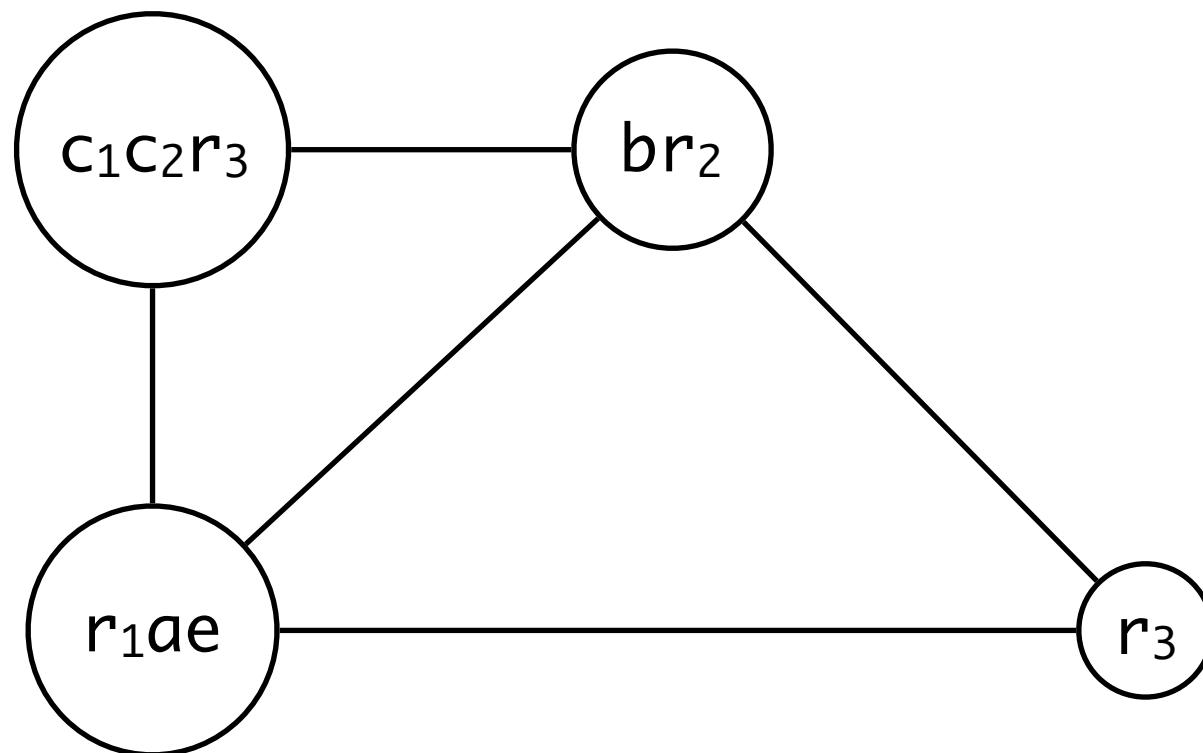
```
enter : c1 ← r3
        M[cloc] ← c1
        a ← r1
        b ← r2
        d ← 0
        e ← a
loop :  d ← d + b
        e ← e - 1
        if e > 0 goto loop
        r1 ← d
        r3 ← c2
        c2 ← M[cloc]
        return (r1, r3)
```



# Pre-Colored Nodes

## examples

apply register assignment



```
enter :  $r_3 \leftarrow r_3$   
         $M[c_{loc}] \leftarrow r_3$   
         $r_1 \leftarrow r_1$   
         $r_2 \leftarrow r_2$   
         $r_3 \leftarrow 0$   
         $r_1 \leftarrow r_1$   
loop :   $r_3 \leftarrow r_3 + r_2$   
         $r_1 \leftarrow r_1 - 1$   
        if  $r_1 > 0$  goto loop  
         $r_1 \leftarrow r_3$   
         $r_3 \leftarrow r_3$   
         $r_3 \leftarrow M[c_{loc}]$   
        return ( $r_1, r_3$ )
```

# Pre-Colored Nodes

## example

```
enter : c ← r3
        a ← r1
        b ← r2
        d ← 0
        e ← a
loop   : d ← d + b
        e ← e - 1
        if e > 0 goto loop
        r1 ← d
        r3 ← c
        return (r1, r3)
```

```
enter : r3 ← r3
        M[cloc] ← r3
        r1 ← r1
        r2 ← r2
        r3 ← 0
        r1 ← r1
loop   : r3 ← r3 + r2
        r1 ← r1 - 1
        if r1 > 0 goto loop
        r1 ← r3
        r3 ← r3
        r3 ← M[cloc]
        return (r1, r3)
```

# Pre-Colored Nodes

## example

```
enter : c ← r3
        a ← r1
        b ← r2
        d ← 0
        e ← a
loop :  d ← d + b
        e ← e - 1
        if e > 0 goto loop
        r1 ← d
        r3 ← c
        return (r1, r3)
```

```
enter : r3 ← r3
        M[cloc] ← r3
        r1 ← r1
        r2 ← r2
        r3 ← 0
        r1 ← r1
loop :  r3 ← r3 + r2
        r1 ← r1 - 1
        if r1 > 0 goto loop
        r1 ← r3
        r3 ← r3
        r3 ← M[cloc]
        return (r1, r3)
```

# Pre-Colored Nodes

## example

```
enter : c ← r3
        a ← r1
        b ← r2
        d ← 0
        e ← a
loop :  d ← d + b
        e ← e - 1
        if e > 0 goto loop
        r1 ← d
        r3 ← c
        return (r1, r3)
```

```
enter : M[cloc] ← r3
        r3 ← 0
loop :  r3 ← r3 + r2
        r1 ← r1 - 1
        if r1 > 0 goto loop
        r1 ← r3
        r3 ← M[cloc]
        return (r1, r3)
```

# Pre-Colored Nodes

## example

```
int f(int a, int b) {  
    int d = 0;  
    int e = a;  
    do {  
        d = d + b;  
        e = e - 1;  
    } while (e > 0);  
    return d;  
}
```

```
enter : M[cloc] ← r3  
        r3 ← 0  
loop :  r3 ← r3 + r2  
        r1 ← r1 - 1  
        if r1 > 0 goto loop  
        r3 ← M[cloc]  
        return (r1, r3)
```

# VI

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## Summary

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# Summary

## lessons learned

How can we assign registers to local variables and temporaries?

- perform liveness analysis
- build interference graph
- color interference graph

What to do if the graph is not colorable?

- keep local variables in memory

How to handle move instructions efficiently?

- coalesce nodes safely



# Literature

[learn more](#)

Andrew W. Appel, Jens Palsberg: Modern Compiler Implementation in Java, 2nd edition. 2002

Lal George, Andrew W. Appel: Iterative Register Coalescing. POPL 1996

Lal George, Andrew W. Appel: Iterative Register Coalescing. TOPLAS 18(3), 1996

# Outlook

## coming next

### Compiler components & their generators

- Lecture 12: Data-Flow Analysis **Dec 6**
- Lecture 13: Register Allocation **Dec 13**
- Lecture 14: LL Parsing **Dec 20**
- Lecture 15: LR Parsing **Jan 10**

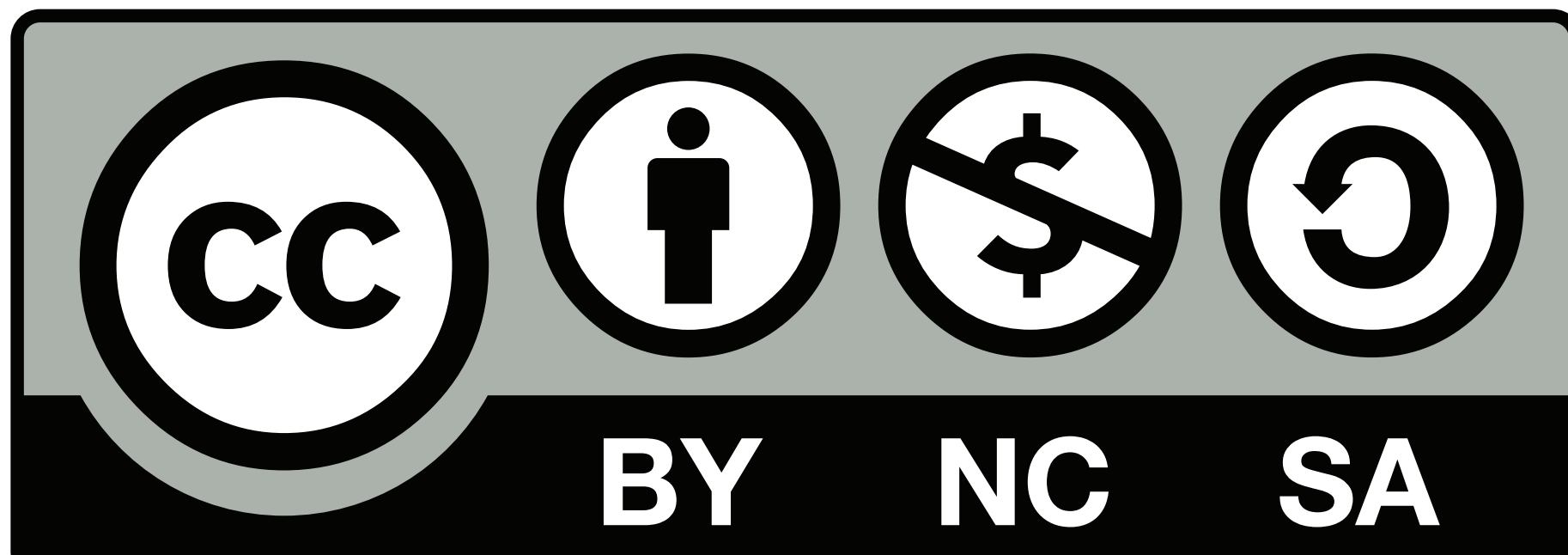
### Exam preparation

- Question & Answer & Outlook **Jan 24**
- Exam **Jan 31**

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