ML fundmentals - Company Segmentation

7/24/2020

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Challenge Summary

Your organization wants to know which companies are similar to each other to help in identifying potential customers of a SAAS software solution (e.g. Salesforce CRM or equivalent) in various segments of the market. The Sales Department is very interested in this analysis, which will help them more easily penetrate various market segments.

You will be using stock prices in this analysis. You come up with a method to classify companies based on how their stocks trade using their daily stock returns (percentage movement from one day to the next). This analysis will help your organization determine which companies are related to each other (competitors and have similar attributes).

You can analyze the stock prices using what you've learned in the unsupervised learning tools including K-Means and UMAP. You will use a combination of kmeans() to find groups and umap() to visualize similarity of daily stock returns.

Objectives

Apply your knowledge on K-Means and UMAP along with dplyr, ggplot2, and purrr to create a visualization that identifies subgroups in the S&P 500 Index. You will specifically apply:

```
• Modeling: kmeans() and umap()
```

• Iteration: purrr

• Data Manipulation: dplyr, tidyr, and tibble

• Visualization: ggplot2 (bonus plotly)

Libraries

Load the following libraries.

```
# install.packages("plotly")

library(tidyverse)
library(tidyquant)
library(broom)
library(umap)
library(ggrepel) # Addon for ggplot, so that the labels do not overlap
```

Data

We will be using stock prices in this analysis. Although some of you know already how to use an API to retrieve stock prices I obtained the stock prices for every stock in the S&P 500 index for you already. The files are saved in the session_6_data directory.

We can read in the stock prices. The data is 1.2M observations. The most important columns for our analysis are:

- symbol: The stock ticker symbol that corresponds to a company's stock price
- date: The timestamp relating the symbol to the share price at that point in time
- adjusted: The stock price, adjusted for any splits and dividends (we use this when analyzing stock data over long periods of time)

```
# STOCK PRICES
sp_500_prices_tbl <- read_rds("sp_500_prices_tbl.rds")
sp_500_prices_tbl</pre>
```

```
## # A tibble: 1,225,765 x 8
##
     symbol date
                        open high
                                     low close
                                                 volume adjusted
                       <dbl> <dbl> <dbl> <dbl> <
                                                  <dbl>
##
      <chr> <date>
                                                           <dbl>
   1 MSFT
            2009-01-02 19.5 20.4 19.4
                                          20.3 50084000
                                                            15.9
##
   2 MSFT
            2009-01-05 20.2 20.7
                                    20.1
                                          20.5 61475200
                                                            16.0
   3 MSFT
            2009-01-06 20.8 21
                                    20.6
                                          20.8 58083400
##
                                                            16.2
            2009-01-07 20.2 20.3 19.5 19.5 72709900
                                                            15.2
##
   4 MSFT
   5 MSFT
            2009-01-08 19.6 20.2 19.5 20.1 70255400
                                                            15.7
##
            2009-01-09 20.2 20.3 19.4 19.5 49815300
##
  6 MSFT
                                                            15.2
```

```
## 7 MSFT 2009-01-12 19.7 19.8 19.3 19.5 52163500 15.2
## 8 MSFT 2009-01-13 19.5 20.0 19.5 19.8 65843500 15.5
## 9 MSFT 2009-01-14 19.5 19.7 19.0 19.1 80257500 14.9
## 10 MSFT 2009-01-15 19.1 19.3 18.5 19.2 96169800 15.0
## # ... with 1,225,755 more rows
```

The second data frame contains information about the stocks the most important of which are:

- company: The company name
- sector: The sector that the company belongs to

```
# SECTOR INFORMATION
sp_500_index_tbl <- read_rds("sp_500_index_tbl.rds")
sp_500_index_tbl</pre>
```

| ## | | symbol | company | weight |
|----|----|--------|----------------------------------|--------------|
| | 1 | MSFT | Microsoft Corporation | |
| | 2 | AAPL | | 3.299844e-02 |
| | 3 | AMZN | Amazon.com Inc. | |
| ## | - | BRK.B | Berkshire Hathaway Inc. Class B | |
| ## | 5 | FB | Facebook Inc. Class A | |
| ## | 6 | JNJ | Johnson & Johnson | |
| | 7 | JPM | JPMorgan Chase & Co. | |
| ## | | GOOG | Alphabet Inc. Class C | |
| ## | 9 | GOOGL | Alphabet Inc. Class A | |
| ## | 10 | MOX | Exxon Mobil Corporation | |
| ## | 11 | BAC | Bank of America Corp | |
| ## | 12 | UNH | UnitedHealth Group Incorporated | |
| ## | 13 | V | Visa Inc. Class A | |
| ## | 14 | PG | Procter & Gamble Company | |
| ## | 15 | PFE | Pfizer Inc. | 1.052585e-02 |
| ## | 16 | INTC | Intel Corporation | |
| ## | 17 | CVX | Chevron Corporation | |
| ## | 18 | VZ | Verizon Communications Inc. | 9.784105e-03 |
| ## | 19 | CSCO | Cisco Systems Inc. | 9.544976e-03 |
| ## | 20 | T | AT&T Inc. | 9.518933e-03 |
| | 21 | BA | Boeing Company | |
| ## | 22 | HD | Home Depot Inc. | |
| ## | 23 | WFC | Wells Fargo & Company | 8.957703e-03 |
| ## | 24 | MRK | Merck & Co. Inc. | |
| ## | 25 | MA | Mastercard Incorporated Class A | |
| | 26 | KO | Coca-Cola Company | |
| ## | 27 | CMCSA | Comcast Corporation Class A | 7.368779e-03 |
| ## | 28 | DIS | Walt Disney Company | |
| | 29 | PEP | PepsiCo Inc. | |
| ## | 30 | C | Citigroup Inc. | 6.744127e-03 |
| ## | 31 | NFLX | Netflix Inc. | 6.680205e-03 |
| ## | 32 | WMT | Walmart Inc. | 6.127690e-03 |
| ## | 33 | MCD | McDonald's Corporation | 5.961227e-03 |
| ## | 34 | ABT | Abbott Laboratories | 5.673213e-03 |
| ## | 35 | ORCL | Oracle Corporation | 5.649621e-03 |
| ## | 36 | PM | Philip Morris International Inc. | 5.569381e-03 |
| ## | 37 | ADBE | Adobe Inc. | 5.423148e-03 |
| | | | | |

```
## 38
          IBM
                      International Business Machines Corporation 5.378546e-03
## 39
          UNP
                                         Union Pacific Corporation 5.373873e-03
## 40
         DWDP
                                                     DowDuPont Inc. 5.343558e-03
## 41
          MDT
                                                      Medtronic plc 5.320276e-03
## 42
         ABBV
                                                        AbbVie Inc. 5.227510e-03
## 43
                                                         3M Company 5.225519e-03
          MMM
## 44
                                                salesforce.com inc. 5.221497e-03
          CRM
                                                         Amgen Inc. 5.154364e-03
## 45
         AMGN
## 46
         AVGO
                                                      Broadcom Inc. 5.010262e-03
## 47
          LLY
                                              Eli Lilly and Company 4.959256e-03
## 48
          HON
                                      Honeywell International Inc. 4.860377e-03
         PYPL
## 49
                                                PayPal Holdings Inc 4.796215e-03
## 50
          NKE
                                                  NIKE Inc. Class B 4.662578e-03
                                   United Technologies Corporation 4.450672e-03
## 51
          UTX
## 52
          TXN
                                    Texas Instruments Incorporated 4.437206e-03
## 53
          TMO
                                     Thermo Fisher Scientific Inc. 4.363659e-03
## 54
          ACN
                                              Accenture Plc Class A 4.355615e-03
## 55
         NVDA
                                                 NVIDIA Corporation 4.119677e-03
## 56
         COST
                                      Costco Wholesale Corporation 4.072393e-03
## 57
          LIN
                                                          Linde plc 3.986931e-03
## 58
           MO
                                                   Altria Group Inc 3.917806e-03
## 59
          CVS
                                             CVS Health Corporation 3.853464e-03
## 60
         BKNG
                                             Booking Holdings Inc. 3.844550e-03
          NEE
                                                NextEra Energy Inc. 3.774455e-03
## 61
## 62
           GE
                                           General Electric Company 3.767361e-03
## 63
         SBUX
                                             Starbucks Corporation 3.765740e-03
## 64
         GILD
                                               Gilead Sciences Inc. 3.740188e-03
                                      Bristol-Myers Squibb Company 3.620328e-03
## 65
          BMY
## 66
          LOW
                                             Lowe's Companies Inc. 3.611353e-03
## 67
          COP
                                                     ConocoPhillips 3.482849e-03
                                                        Anthem Inc. 3.459557e-03
## 68
         ANTM
## 69
          CAT
                                                   Caterpillar Inc. 3.452684e-03
## 70
          AMT
                                        American Tower Corporation 3.362129e-03
          USB
                                                       U.S. Bancorp 3.355776e-03
## 71
                                United Parcel Service Inc. Class B 3.308592e-03
## 72
          UPS
## 73
          LMT
                                       Lockheed Martin Corporation 3.248902e-03
## 74
          AXP
                                           American Express Company 3.238637e-03
## 75
           CI
                                                  Cigna Corporation 3.172444e-03
## 76
         MDLZ
                               Mondelez International Inc. Class A 3.018507e-03
           GS
                                           Goldman Sachs Group Inc. 2.949052e-03
## 77
          DHR
                                                Danaher Corporation 2.945331e-03
## 78
## 79
         BTTB
                                                        Biogen Inc. 2.878567e-03
                                      Becton Dickinson and Company 2.859908e-03
## 80
          BDX
## 81
          ADP
                                    Automatic Data Processing Inc. 2.800078e-03
         CELG
## 82
                                                Celgene Corporation 2.724370e-03
         QCOM
## 83
                                              QUALCOMM Incorporated 2.704791e-03
## 84
          CME
                                             CME Group Inc. Class A 2.693005e-03
## 85
          TJX
                                                  TJX Companies Inc 2.688162e-03
## 86
         ISRG
                                            Intuitive Surgical Inc. 2.687962e-03
## 87
          DUK
                                            Duke Energy Corporation 2.677987e-03
## 88
         CHTR
                               Charter Communications Inc. Class A 2.661359e-03
## 89
          SLB
                                                    Schlumberger NV 2.656396e-03
## 90
           CB
                                                      Chubb Limited 2.635526e-03
## 91
         INTU
                                                        Intuit Inc. 2.599428e-03
```

| ## | 92 | WBA | Walaroons Roots Allianco Inc | 2 5370870-03 |
|----|-----|------|----------------------------------------------------|--------------|
| | 93 | CSX | Walgreens Boots Alliance Inc CSX Corporation | |
| | 94 | EOG | EOG Resources Inc. | |
| ## | | SYK | Stryker Corporation | |
| ## | | PNC | PNC Financial Services Group Inc. | |
| | 97 | CL | <u>-</u> | |
| | | | Colgate-Palmolive Company | |
| ## | | SPG | Simon Property Group Inc. | |
| ## | | SCHW | Charles Schwab Corporation | |
| | 100 | BSX | Boston Scientific Corporation | |
| | 101 | D | Dominion Energy Inc | |
| | 102 | MS | Morgan Stanley | |
| | 103 | FOXA | Twenty-First Century Fox Inc. Class A | |
| | 104 | BLK | BlackRock Inc. | |
| | 105 | RTN | Raytheon Company | |
| | 106 | OXY | Occidental Petroleum Corporation | |
| | 107 | GM | General Motors Company | |
| | 108 | DE | Deere & Company | |
| | 109 | SO | Southern Company | |
| | 110 | NSC | Norfolk Southern Corporation | |
| | 111 | NOC | Northrop Grumman Corporation | |
| ## | 112 | SPGI | S&P Global Inc. | |
| ## | 113 | CCI | Crown Castle International Corp | |
| ## | 114 | GD | General Dynamics Corporation | 2.084551e-03 |
| ## | 115 | BK | Bank of New York Mellon Corporation | |
| ## | 116 | VRTX | Vertex Pharmaceuticals Incorporated | 2.052085e-03 |
| ## | 117 | MU | Micron Technology Inc. | 2.021239e-03 |
| ## | 118 | EXC | Exelon Corporation | 1.989433e-03 |
| ## | 119 | MMC | Marsh & McLennan Companies Inc. | 1.961229e-03 |
| | 120 | ZTS | Zoetis Inc. Class A | 1.957868e-03 |
| | 121 | MPC | Marathon Petroleum Corporation | 1.930374e-03 |
| | 122 | PLD | Prologis Inc. | 1.912765e-03 |
| ## | 123 | MET | MetLife Inc. | 1.906152e-03 |
| ## | 124 | ITW | Illinois Tool Works Inc. | 1.901359e-03 |
| ## | 125 | AGN | Allergan plc | 1.894716e-03 |
| ## | 126 | ILMN | Illumina Inc. | 1.881459e-03 |
| ## | 127 | FDX | FedEx Corporation | 1.858768e-03 |
| ## | 128 | ICE | Intercontinental Exchange Inc. | 1.849193e-03 |
| ## | 129 | EMR | Emerson Electric Co. | 1.828073e-03 |
| ## | 130 | HUM | Humana Inc. | 1.825011e-03 |
| ## | 131 | CTSH | Cognizant Technology Solutions Corporation Class A | 1.818338e-03 |
| ## | 132 | AON | Aon plc | 1.779839e-03 |
| ## | 133 | ECL | Ecolab Inc. | 1.774246e-03 |
| ## | 134 | PGR | Progressive Corporation | 1.773456e-03 |
| ## | 135 | KMB | Kimberly-Clark Corporation | 1.754196e-03 |
| ## | 136 | PSX | Phillips 66 | 1.751575e-03 |
| ## | 137 | PRU | Prudential Financial Inc. | 1.680439e-03 |
| ## | 138 | ADI | Analog Devices Inc. | 1.677838e-03 |
| ## | 139 | BBT | BB&T Corporation | |
| ## | 140 | AEP | American Electric Power Company Inc. | |
| ## | 141 | COF | Capital One Financial Corporation | |
| ## | 142 | WM | Waste Management Inc. | |
| ## | 143 | HCA | HCA Healthcare Inc | |
| ## | 144 | AMAT | Applied Materials Inc. | 1.640689e-03 |
| ## | 145 | TGT | Target Corporation | |
| | | | e i | |

```
Air Products and Chemicals Inc. 1.629554e-03
## 146
          APD
## 147
          AFI.
                                                 Aflac Incorporated 1.614086e-03
## 148
          AIG
                                 American International Group Inc. 1.602040e-03
## 149
           EW
                                  Edwards Lifesciences Corporation 1.591745e-03
## 150
          HPQ
                                                            HP Inc. 1.572385e-03
                                         Baxter International Inc. 1.557538e-03
## 151
          BAX
## 152
          SHW
                                          Sherwin-Williams Company 1.553596e-03
## 153
          VLO
                                         Valero Energy Corporation 1.538518e-03
## 154
          FIS
                      Fidelity National Information Services Inc. 1.527503e-03
## 155
          KMI
                                         Kinder Morgan Inc Class P 1.522860e-03
## 156
         ROST
                                                   Ross Stores Inc. 1.512285e-03
## 157
         ADSK
                                                      Autodesk Inc. 1.491685e-03
## 158
                               Marriott International Inc. Class A 1.489754e-03
          MAR.
## 159
           EL
                               Estee Lauder Companies Inc. Class A 1.484361e-03
## 160
         FISV
                                                        Fiserv Inc. 1.480919e-03
          TRV
## 161
                                          Travelers Companies Inc. 1.469054e-03
## 162
          ETN
                                                    Eaton Corp. Plc 1.454436e-03
## 163
         EQIX
                                                       Equinix Inc. 1.453206e-03
         ATVI
## 164
                                          Activision Blizzard Inc. 1.451855e-03
            F
                                                Ford Motor Company 1.427123e-03
## 165
## 166
         EBAY
                                                          eBay Inc. 1.422420e-03
## 167
          WMB
                                           Williams Companies Inc. 1.408363e-03
## 168
         REGN
                                    Regeneron Pharmaceuticals Inc. 1.402270e-03
## 169
                                              Electronic Arts Inc. 1.393026e-03
## 170
          ALL
                                               Allstate Corporation 1.392405e-03
## 171
          JCI
                                Johnson Controls International plc 1.385652e-03
## 172
          SYY
                                                  Sysco Corporation 1.378898e-03
## 173
          ROP
                                           Roper Technologies Inc. 1.376557e-03
## 174
                                              Delta Air Lines Inc. 1.372395e-03
          DAL
## 175
          RHT
                                                       Red Hat Inc. 1.369004e-03
## 176
           DG
                                        Dollar General Corporation 1.350724e-03
## 177
          SRE
                                                      Sempra Energy 1.345972e-03
## 178
         ORLY
                                          O'Reilly Automotive Inc. 1.332325e-03
## 179
          PSA
                                                     Public Storage 1.328894e-03
                                                        Xilinx Inc. 1.285252e-03
## 180
         XLNX
                                               SunTrust Banks Inc. 1.279929e-03
## 181
          STI
## 182
          YUM
                                                   Yum! Brands Inc. 1.273546e-03
## 183
          T.UV
                                            Southwest Airlines Co. 1.271535e-03
## 184
          KHC
                                               Kraft Heinz Company 1.264782e-03
## 185
                                                     Welltower Inc. 1.251195e-03
         WELL
## 186
          STZ
                                 Constellation Brands Inc. Class A 1.248293e-03
         ALXN
## 187
                                      Alexion Pharmaceuticals Inc. 1.231145e-03
## 188
          TEL
                                              TE Connectivity Ltd. 1.220970e-03
## 189
         LRCX
                                          Lam Research Corporation 1.219289e-03
## 190
          PEG
                               Public Service Enterprise Group Inc 1.214677e-03
          VFC
## 191
                                                   V.F. Corporation 1.208463e-03
## 192
          MCO
                                               Moody's Corporation 1.206382e-03
## 193
          HAL
                                               Halliburton Company 1.196988e-03
## 194
          LYB
                                      LyondellBasell Industries NV 1.196237e-03
## 195
          GLW
                                                        Corning Inc 1.194216e-03
## 196
          OKE
                                                         ONEOK Inc. 1.188553e-03
## 197
          APH
                                      Amphenol Corporation Class A 1.185542e-03
## 198
          XEL
                                                   Xcel Energy Inc. 1.179399e-03
## 199
          AVB
                                        AvalonBay Communities Inc. 1.156808e-03
```

```
## 200
          MCK
                                               McKesson Corporation 1.156177e-03
## 201
          EQR
                                                Equity Residential 1.150735e-03
## 202
                                                General Mills Inc. 1.145642e-03
          GIS
## 203
                                          State Street Corporation 1.145102e-03
          STT
## 204
          CNC
                                                Centene Corporation 1.138238e-03
## 205
          PPG
                                               PPG Industries Inc. 1.127853e-03
## 206
                                                Ingersoll-Rand Plc 1.096718e-03
           TR.
## 207
          7.BH
                                       Zimmer Biomet Holdings Inc. 1.073786e-03
## 208
            Α
                                         Agilent Technologies Inc. 1.061240e-03
## 209
          MTB
                                               M&T Bank Corporation 1.058008e-03
## 210
          PXD
                                 Pioneer Natural Resources Company 1.051955e-03
## 211
          CXO
                                              Concho Resources Inc. 1.051925e-03
## 212
                                       Discover Financial Services 1.043961e-03
          DFS
## 213
           ED
                                           Consolidated Edison Inc. 1.042370e-03
## 214
          HLT
                                     Hilton Worldwide Holdings Inc 1.041860e-03
## 215
          FOX
                             Twenty-First Century Fox Inc. Class B 1.041340e-03
## 216
         PAYX
                                                       Paychex Inc. 1.035437e-03
## 217
          FTV
                                                      Fortive Corp. 1.033396e-03
## 218
         PCAR
                                                         PACCAR Inc 1.017388e-03
## 219
                                         Digital Realty Trust Inc. 1.011595e-03
          DLR
## 220
         TROW
                                                T. Rowe Price Group 1.010384e-03
## 221
          ADM
                                    Archer-Daniels-Midland Company 1.006973e-03
## 222
                                                         Kroger Co. 1.001020e-03
           KR
                                                       Cummins Inc. 9.979983e-04
## 223
          CMI
## 224
         DI.TR.
                                                   Dollar Tree Inc. 9.979783e-04
## 225
          AZO
                                                      AutoZone Inc. 9.977982e-04
## 226
          WEC
                                               WEC Energy Group Inc 9.976581e-04
## 227
         MNST
                                      Monster Beverage Corporation 9.970779e-04
## 228
                                    Anadarko Petroleum Corporation 9.903545e-04
          APC
## 229
                                               Carnival Corporation 9.873830e-04
        CCL.U
                                                        Ventas Inc. 9.864626e-04
## 230
          VTR
## 231
          HPE
                                    Hewlett Packard Enterprise Co. 9.839113e-04
## 232
           PH
                                       Parker-Hannifin Corporation 9.801494e-04
## 233
          IQV
                                                 IQVIA Holdings Inc 9.759873e-04
                                           Motorola Solutions Inc. 9.730559e-04
## 234
          MSI
## 235
         TWTR
                                                       Twitter Inc. 9.606297e-04
## 236
         WLTW
                      Willis Towers Watson Public Limited Company 9.449018e-04
## 237
           ES
                                                  Eversource Energy 9.445016e-04
## 238
          PPL
                                                    PPL Corporation 9.408298e-04
## 239
                                          Rockwell Automation Inc. 9.317452e-04
          ROK
## 240
          DTE
                                                DTE Energy Company 9.294641e-04
## 241
          SYF
                                                Synchrony Financial 9.250619e-04
## 242
                                                          Aptiv PLC 9.162075e-04
         APTV
## 243
                                 Microchip Technology Incorporated 9.087137e-04
         MCHP
## 244
          TDG
                                      TransDigm Group Incorporated 9.086637e-04
## 245
         SBAC
                                  SBA Communications Corp. Class A 9.083636e-04
                                       Stanley Black & Decker Inc. 8.942865e-04
## 246
          SWK
## 247
          AMD
                                       Advanced Micro Devices Inc. 8.933361e-04
## 248
         NTRS
                                        Northern Trust Corporation 8.885036e-04
## 249
            0
                                         Realty Income Corporation 8.874931e-04
## 250
         VRSK
                                               Verisk Analytics Inc 8.821104e-04
## 251
                                            Boston Properties Inc. 8.754071e-04
          BXP
## 252
          UAL
                                  United Continental Holdings Inc. 8.631610e-04
## 253
                                      Royal Caribbean Cruises Ltd. 8.626407e-04
          RCL
```

```
## 254
          CLX
                                                     Clorox Company 8.558573e-04
## 255
          FI.T
                                        FleetCor Technologies Inc. 8.436713e-04
## 256
          EIX
                                               Edison International 8.369679e-04
## 257
                                               Global Payments Inc. 8.353671e-04
          GPN
## 258
          HRS
                                                 Harris Corporation 8.295442e-04
## 259
           ΙP
                                       International Paper Company 8.223906e-04
## 260
           FE
                                                  FirstEnergy Corp. 8.221105e-04
## 261
           WY
                                               Weyerhaeuser Company 8.213501e-04
## 262
         INFO
                                                    IHS Markit Ltd. 8.174982e-04
## 263
         CERN
                                                 Cerner Corporation 8.136563e-04
## 264
         VRSN
                                                      VeriSign Inc. 8.048018e-04
          NUE
## 265
                                                  Nucor Corporation 8.041515e-04
## 266
          BLL
                                                   Ball Corporation 7.976183e-04
## 267
         ALGN
                                              Align Technology Inc. 7.962776e-04
## 268
          TSN
                                           Tyson Foods Inc. Class A 7.915152e-04
## 269
          AMP
                                          Ameriprise Financial Inc. 7.904947e-04
## 270
          KEY
                                                            KeyCorp 7.861025e-04
## 271
          DXC
                                                 DXC Technology Co. 7.849519e-04
## 272
          ESS
                                         Essex Property Trust Inc. 7.820805e-04
## 273
                                            IDEXX Laboratories Inc. 7.770380e-04
         IDXX
## 274
          AME
                                                        AMETEK Inc. 7.766478e-04
## 275
         FITB
                                                Fifth Third Bancorp 7.736063e-04
## 276
          WAT
                                                 Waters Corporation 7.714552e-04
## 277
         FAST
                                                   Fastenal Company 7.690040e-04
## 278
          FCX
                                              Freeport-McMoRan Inc. 7.602396e-04
                                 American Water Works Company Inc. 7.555272e-04
## 279
          AWK
## 280
          NEM
                                         Newmont Mining Corporation 7.529760e-04
## 281
         CTAS
                                                 Cintas Corporation 7.481436e-04
          CFG
## 282
                                     Citizens Financial Group Inc. 7.464627e-04
## 283
         ULTA
                                                    Ulta Beauty Inc 7.426108e-04
                            Hartford Financial Services Group Inc. 7.408799e-04
## 284
          HIG
## 285
          FRC
                                                First Republic Bank 7.325258e-04
## 286
          CBS
                                            CBS Corporation Class B 7.311351e-04
## 287
          RSG
                                             Republic Services Inc. 7.226008e-04
## 288
         KLAC
                                             KLA-Tencor Corporation 7.217504e-04
## 289
          AEE
                                                 Ameren Corporation 7.206898e-04
## 290
          MTD
                                 Mettler-Toledo International Inc. 7.184887e-04
## 291
          OMC
                                                  Omnicom Group Inc 7.175283e-04
## 292
          CAH
                                               Cardinal Health Inc. 7.103347e-04
## 293
           RF
                                     Regions Financial Corporation 7.101146e-04
## 294
         NTAP
                                                        NetApp Inc. 7.097444e-04
## 295
          T.I.I.
                                                L3 Technologies Inc 7.066829e-04
## 296
          MYL
                                                         Mylan N.V. 7.006999e-04
                                                       ABIOMED Inc. 6.935163e-04
## 297
         ABMD
## 298
         FANG
                                            Diamondback Energy Inc. 6.920756e-04
## 299
          ETR
                                                Entergy Corporation 6.896343e-04
## 300
         EVRG
                                                        Evergy Inc. 6.780386e-04
## 301
         CBRE
                                            CBRE Group Inc. Class A 6.753972e-04
## 302
         MXIM
                                    Maxim Integrated Products Inc. 6.719555e-04
## 303
          CHD
                                           Church & Dwight Co. Inc. 6.718755e-04
## 304
          GPC
                                              Genuine Parts Company 6.684037e-04
## 305
          MKC
                                  McCormick & Company Incorporated 6.650521e-04
## 306
          TSS
                                         Total System Services Inc. 6.647519e-04
                                                  MSCI Inc. Class A 6.631811e-04
## 307
         MSCI
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## 308
           LH
                       Laboratory Corporation of America Holdings 6.526559e-04
## 309
          HSY
                                                    Hershey Company 6.524658e-04
## 310
          CNP
                                           CenterPoint Energy Inc. 6.480336e-04
## 311
         EXPE
                                                 Expedia Group Inc. 6.438815e-04
## 312
         KEYS
                                         Keysight Technologies Inc 6.404798e-04
## 313
         HBAN
                                Huntington Bancshares Incorporated 6.392192e-04
## 314
         SNPS
                                                      Synopsys Inc. 6.389991e-04
## 315
          CMS
                                            CMS Energy Corporation 6.380286e-04
## 316
          CMG
                                       Chipotle Mexican Grill Inc. 6.367779e-04
## 317
         SWKS
                                           Skyworks Solutions Inc. 6.361676e-04
## 318
          VMC
                                          Vulcan Materials Company 6.352072e-04
## 319
         SYMC
                                              Symantec Corporation 6.343768e-04
## 320
                                                           HCP Inc. 6.318055e-04
          HCP
## 321
                                       Cadence Design Systems Inc. 6.312652e-04
         CDNS
## 322
         INCY
                                                 Incyte Corporation 6.284338e-04
## 323
         ANSS
                                                         ANSYS Inc. 6.232512e-04
## 324
          MRO
                                          Marathon Oil Corporation 6.196694e-04
## 325
          HES
                                                   Hess Corporation 6.190591e-04
## 326
          AJG
                                         Arthur J. Gallagher & Co. 6.175784e-04
## 327
          MGM
                                         MGM Resorts International 6.163778e-04
## 328
          GWW
                                                W.W. Grainger Inc. 6.140466e-04
## 329
            K
                                                    Kellogg Company 6.137565e-04
## 330
          AAL
                                      American Airlines Group Inc. 6.124658e-04
## 331
          LEN
                                        Lennar Corporation Class A 6.092742e-04
## 332
          ARF.
                              Alexandria Real Estate Equities Inc. 6.082837e-04
## 333
          RMD
                                                        ResMed Inc. 6.071331e-04
## 334
          BBY
                                                  Best Buy Co. Inc. 6.056024e-04
## 335
          CMA
                                              Comerica Incorporated 5.996494e-04
## 336
          WCG
                                        WellCare Health Plans Inc. 5.953673e-04
## 337
          DRI
                                           Darden Restaurants Inc. 5.935464e-04
## 338
          ABC
                                     AmerisourceBergen Corporation 5.918655e-04
## 339
          WDC
                                       Western Digital Corporation 5.916054e-04
## 340
          HST
                                        Host Hotels & Resorts Inc. 5.866429e-04
## 341
          DHI
                                                   D.R. Horton Inc. 5.829311e-04
                                                Citrix Systems Inc. 5.824008e-04
## 342
         CTXS
## 343
          TXT
                                                       Textron Inc. 5.822107e-04
## 344
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                                              Arista Networks Inc. 5.821006e-04
## 345
          COO
                                             Cooper Companies Inc. 5.809801e-04
## 346
          DOV
                                                  Dover Corporation 5.751772e-04
          PFG
## 347
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## 348
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## 349
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                                          Devon Energy Corporation 5.712452e-04
## 350
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          IFF
## 351
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                                      Lincoln National Corporation 5.692042e-04
## 352
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                                                         Xylem Inc. 5.646419e-04
## 353
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                                 Baker Hughes a GE Company Class A 5.601297e-04
## 354
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                                                       Equifax Inc. 5.579286e-04
## 355
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                                              Celanese Corporation 5.579186e-04
## 356
          CTL
                                                   CenturyLink Inc. 5.574683e-04
## 357
            L
                                                  Loews Corporation 5.549771e-04
## 358
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                                                SVB Financial Group 5.546369e-04
## 359
           IT
                                                       Gartner Inc. 5.531062e-04
## 360
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                                  Cincinnati Financial Corporation 5.520556e-04
## 361
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                      Expeditors International of Washington Inc. 5.477835e-04
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CHRW
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## 362
## 363
          APA
                                                 Apache Corporation 5.405199e-04
## 364
          EXR
                                          Extra Space Storage Inc. 5.384689e-04
## 365
         HOLX
                                                       Hologic Inc. 5.374083e-04
## 366
          AAP
                                           Advance Auto Parts Inc. 5.350071e-04
## 367
          NRG
                                                    NRG Energy Inc. 5.292443e-04
## 368
          UDR
                                                           UDR Inc. 5.268831e-04
## 369
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                                     E*TRADE Financial Corporation 5.260527e-04
## 370
          VAR
                                       Varian Medical Systems Inc. 5.234614e-04
## 371
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                                              Wynn Resorts Limited 5.205199e-04
## 372
          CAG
                                                Conagra Brands Inc. 5.101947e-04
## 373
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                                                      Fortinet Inc. 5.097445e-04
## 374
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                                            Seagate Technology PLC 5.096245e-04
## 375
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                                    Quest Diagnostics Incorporated 5.065029e-04
## 376
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                                    Martin Marietta Materials Inc. 5.062028e-04
## 377
         TSC0
                                            Tractor Supply Company 5.057225e-04
## 378
          VNO
                                               Vornado Realty Trust 5.054024e-04
## 379
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## 380
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                                          Hormel Foods Corporation 5.012603e-04
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                               Broadridge Financial Solutions Inc. 4.989791e-04
## 382
          SJM
                                               J.M. Smucker Company 4.983588e-04
## 383
          EMN
                                          Eastman Chemical Company 4.979786e-04
## 384
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                            Universal Health Services Inc. Class B 4.975784e-04
## 385
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                               Norwegian Cruise Line Holdings Ltd. 4.973683e-04
## 386
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                                                  Masco Corporation 4.912953e-04
## 387
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                                          Akamai Technologies Inc. 4.905549e-04
## 388
          ATO
                                          Atmos Energy Corporation 4.900247e-04
## 389
          TAP
                              Molson Coors Brewing Company Class B 4.867230e-04
## 390
          MOS
                                                     Mosaic Company 4.859326e-04
## 391
          FMC
                                                    FMC Corporation 4.848721e-04
## 392
          NOV
                                       National Oilwell Varco Inc. 4.833113e-04
## 393
          REG
                                       Regency Centers Corporation 4.802398e-04
## 394
          URI
                                                United Rentals Inc. 4.765079e-04
## 395
          COG
                                       Cabot Oil & Gas Corporation 4.752273e-04
## 396
          AES
                                                    AES Corporation 4.750672e-04
## 397
          KSS
                                                Kohl's Corporation 4.714254e-04
## 398
          KMX
                                                        CarMax Inc. 4.696045e-04
## 399
          KSU
                                              Kansas City Southern 4.682138e-04
## 400
         CPRT
                                                        Copart Inc. 4.660327e-04
## 401
          NBL
                                                  Noble Energy Inc. 4.633514e-04
## 402
          RJF
                                      Raymond James Financial Inc. 4.619907e-04
## 403
         TTWO
                                Take-Two Interactive Software Inc. 4.529462e-04
## 404
          DRE
                                           Duke Realty Corporation 4.512753e-04
## 405
                                                Alliant Energy Corp 4.485540e-04
          LNT
## 406
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                                           Cboe Global Markets Inc 4.448721e-04
                                                   F5 Networks Inc. 4.446620e-04
## 407
         FFIV
## 408
                                      Jack Henry & Associates Inc. 4.428011e-04
         JKHY
## 409
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                                         Lamb Weston Holdings Inc. 4.403699e-04
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          PKI
                                                   PerkinElmer Inc. 4.390992e-04
## 411
          TPR
                                                      Tapestry Inc. 4.385890e-04
## 412
         VIAB
                                                Viacom Inc. Class B 4.367881e-04
## 413
          FTI
                                                     TechnipFMC Plc 4.341868e-04
## 414
          HAS
                                                        Hasbro Inc. 4.310552e-04
## 415
                                                        Nasdag Inc. 4.308651e-04
         NDAQ
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## 416
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                                                 Iron Mountain Inc. 4.289042e-04
## 417
          PNW
                                 Pinnacle West Capital Corporation 4.272633e-04
## 418
                                                   WestRock Company 4.253424e-04
          WRK
## 419
        DISCK
                                            Discovery Inc. Class C 4.248021e-04
## 420
          BEN
                                           Franklin Resources Inc. 4.240517e-04
## 421
          TIF
                                                      Tiffany & Co. 4.230212e-04
## 422
          FRT
                                   Federal Realty Investment Trust 4.207801e-04
## 423
           NI
                                                       NiSource Inc 4.200297e-04
## 424
         JBHT
                                 J.B. Hunt Transport Services Inc. 4.181888e-04
## 425
         ZION
                                         Zions Bancorporation N.A. 4.156776e-04
## 426
           CF
                                       CF Industries Holdings Inc. 4.141368e-04
## 427
         XRAY
                                               DENTSPLY SIRONA Inc. 4.130963e-04
## 428
         HSIC
                                                  Henry Schein Inc. 4.068632e-04
## 429
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                                Huntington Ingalls Industries Inc. 4.054825e-04
## 430
         JNPR
                                              Juniper Networks Inc. 4.021908e-04
## 431
          HFC
                                         HollyFrontier Corporation 4.006400e-04
## 432
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                                               Nielsen Holdings Plc 4.002899e-04
## 433
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## 434
          AVY
                                        Avery Dennison Corporation 3.883139e-04
## 435
          IPG
                               Interpublic Group of Companies Inc. 3.825310e-04
## 436
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                                               Snap-on Incorporated 3.805400e-04
## 437
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                                              Whirlpool Corporation 3.793094e-04
## 438
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                                             Everest Re Group Ltd. 3.785190e-04
## 439
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                                             Albemarle Corporation 3.767281e-04
## 440
          MHK
                                            Mohawk Industries Inc. 3.750773e-04
## 441
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                                                    BorgWarner Inc. 3.740268e-04
## 442
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                                                       Allegion PLC 3.714054e-04
## 443
         GRMN
                                                        Garmin Ltd. 3.696846e-04
## 444
          PVH
                                                          PVH Corp. 3.696646e-04
## 445
          TMK
                                              Torchmark Corporation 3.691343e-04
## 446
          LKQ
                                                    LKQ Corporation 3.688242e-04
## 447
          ADS
                                 Alliance Data Systems Corporation 3.505650e-04
         BF.B
## 448
                                  Brown-Forman Corporation Class B 3.505650e-04
## 449
          RHI
                                    Robert Half International Inc. 3.495245e-04
## 450
          JEC
                                     Jacobs Engineering Group Inc. 3.482939e-04
## 451
          ALK
                                              Alaska Air Group Inc. 3.471433e-04
## 452
         QRVO
                                                         Qorvo Inc. 3.466931e-04
## 453
           WU
                                              Western Union Company 3.396196e-04
## 454
          UNM
                                                         Unum Group 3.383189e-04
## 455
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## 456
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## 457
          IVZ
                                                       Invesco Ltd. 3.289042e-04
## 458
            М
                                                         Macy's Inc 3.234915e-04
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## 459
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## 460
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                                          Kimco Realty Corporation 3.205200e-04
## 461
          DVA
                                                        DaVita Inc. 3.198897e-04
## 462
          NWL
                                                  Newell Brands Inc 3.183990e-04
## 463
          AOS
                                           A. O. Smith Corporation 3.176186e-04
## 464
          XEC
                                                 Cimarex Energy Co. 3.077136e-04
## 465
         NKTR
                                                Nektar Therapeutics 3.070933e-04
## 466
         FLIR
                                                  FLIR Systems Inc. 3.052424e-04
## 467
          PHM
                                                    PulteGroup Inc. 3.023210e-04
## 468
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                                  Ralph Lauren Corporation Class A 3.008902e-04
                                  DISH Network Corporation Class A 3.003400e-04
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         DISH
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## 470
          PNR
                                                        Pentair plc 2.993395e-04
## 471
           FI.
                                                   Foot Locker Inc. 2.956276e-04
## 472
          HBI
                                                   Hanesbrands Inc. 2.951674e-04
## 473
          XR.X
                                                  Xerox Corporation 2.891744e-04
## 474
         FBHS
                               Fortune Brands Home & Security Inc. 2.876636e-04
## 475
          SEE
                                             Sealed Air Corporation 2.856726e-04
## 476
         CPRI
                                             Capri Holdings Limited 2.830813e-04
## 477
          CPB
                                              Campbell Soup Company 2.824010e-04
## 478
         PBCT
                                    People's United Financial Inc. 2.756476e-04
## 479
           LB
                                                      L Brands Inc. 2.663130e-04
## 480
          FLS
                                              Flowserve Corporation 2.653125e-04
## 481
           ΗP
                                             Helmerich & Payne Inc. 2.652424e-04
## 482
          HOG
                                               Harley-Davidson Inc. 2.649123e-04
## 483
         PRGO
                                                    Perrigo Co. Plc 2.626111e-04
## 484
          JEF
                                    Jefferies Financial Group Inc. 2.601699e-04
## 485
          ROL
                                                       Rollins Inc. 2.528763e-04
## 486
          LEG
                                      Leggett & Platt Incorporated 2.523660e-04
## 487
          AMG
                                    Affiliated Managers Group Inc. 2.485041e-04
## 488
         TRIP
                                                   TripAdvisor Inc. 2.479238e-04
## 489
         IPGP
                                          IPG Photonics Corporation 2.379788e-04
## 490
          GPS
                                                           Gap Inc. 2.343470e-04
## 491
          PWR
                                               Quanta Services Inc. 2.245821e-04
## 492
                                                      Assurant Inc. 2.211204e-04
          AIZ
## 493
          JWN
                                                     Nordstrom Inc. 2.172385e-04
## 494
          FI.R.
                                                  Fluor Corporation 2.166282e-04
                                        Brighthouse Financial Inc. 2.135266e-04
## 495
          BHF
## 496
         COTY
                                                  Coty Inc. Class A 2.120159e-04
## 497
          HRB
                                                     H&R Block Inc. 2.095646e-04
## 498
         NWSA
                                           News Corporation Class A 2.074036e-04
## 499
          MAT
                                                        Mattel Inc. 2.017908e-04
## 500
          MAC
                                                   Macerich Company 1.996897e-04
## 501
        DISCA
                                             Discovery Inc. Class A 1.940669e-04
## 502
                                    Goodyear Tire & Rubber Company 1.899448e-04
           GT
## 503
          UAA
                                         Under Armour Inc. Class A 1.670134e-04
## 504
                                         Under Armour Inc. Class C 1.521260e-04
           UA
## 505
          NWS
                                          News Corporation Class B 6.290141e-05
## 506 ECA-CA
                                                 Encana Corporation 7.893942e-06
##
                        sector shares_held
## 1
       Information Technology
                                  84853600
##
   2
       Information Technology
                                  49533308
##
       Consumer Discretionary
                                   4510051
## 4
                   Financials
                                  21364490
## 5
       Communication Services
                                  26385216
##
  6
                  Health Care
                                  29452358
## 7
                                  36529800
                   Financials
## 8
       Communication Services
                                   3378423
##
       Communication Services
                                   3282939
## 10
                        Energy
                                  46493644
## 11
                   Financials
                                 100285460
## 12
                  Health Care
                                  10564454
## 13
       Information Technology
                                  19303236
## 14
             Consumer Staples
                                  27357982
## 15
                  Health Care
                                  63506110
## 16
       Information Technology
                                  50135996
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| ## | 17 | Energy | 20984748 |
|----|----|------------------------|----------|
| ## | 18 | Communication Services | 45375500 |
| ## | 19 | Information Technology | 49397930 |
| ## | 20 | Communication Services | 79917256 |
| ## | 21 | Industrials | 5801735 |
| ## | 22 | Consumer Discretionary | 12408924 |
| ## | 23 | Financials | 46556430 |
| ## | 24 | Health Care | 28576474 |
| ## | 25 | Information Technology | 9946411 |
| ## | 26 | Consumer Staples | 42067310 |
| ## | 27 | Communication Services | 49908344 |
| ## | 28 | Communication Services | 16347008 |
| ## | 29 | Consumer Staples | 15501865 |
| ## | 30 | Financials | 26843670 |
| ## | 31 | Communication Services | 4788556 |
| ## | 32 | Consumer Staples | 15677056 |
| ## | 33 | Consumer Discretionary | 8473443 |
| ## | 34 | Health Care | 19286212 |
| ## | 35 | Information Technology | 27943780 |
| ## | 36 | Consumer Staples | 17070768 |
| ## | 37 | Information Technology | 5347148 |
| ## | 38 | Information Technology | 9968187 |
| ## | 39 | Industrials | 8075142 |
| ## | 40 | Materials | 25202004 |
| ## | 41 | Health Care | 14750220 |
| ## | 42 | Health Care | 16540164 |
| ## | 43 | Industrials | 6400274 |
| ## | 44 | Information Technology | 8398198 |
| ## | 45 | Health Care | 7000953 |
| ## | 46 | Information Technology | 4546147 |
| ## | 47 | Health Care | 10358008 |
| ## | 48 | Industrials | 8109534 |
| ## | 49 | Information Technology | 12927395 |
| ## | 50 | Consumer Discretionary | 13969941 |
| ## | 51 | Industrials | 8911586 |
| ## | 52 | Information Technology | 10552200 |
| ## | 53 | Health Care | 4421107 |
| ## | 54 | Information Technology | 6997603 |
| ## | 55 | Information Technology | 6698059 |
| ## | 56 | Consumer Staples | 4812566 |
| ## | 57 | Materials | 6051462 |
| ## | 58 | Consumer Staples | 20562772 |
| ## | 59 | Health Care | 14177615 |
| ## | 60 | Consumer Discretionary | 508639 |
| ## | 61 | Utilities | 5246468 |
| ## | 62 | Industrials | 95514760 |
| ## | 63 | Consumer Discretionary | 13623676 |
| ## | 64 | Health Care | 14155833 |
| ## | 65 | Health Care | 17923948 |
| ## | 66 | Consumer Discretionary | 8862585 |
| ## | 67 | Energy | 12695394 |
| ## | 68 | Health Care | 2840374 |
| ## | 69 | Industrials | 6484917 |
| ## | 70 | Real Estate | 4836797 |
| | | | |

| ## | 71 | Financials | 16730737 |
|----|------------|---------------------------|----------------------|
| ## | 72 | Industrials | 7634037 |
| ## | 73 | Industrials | 2705191 |
| ## | 74 | Financials | 7715496 |
| ## | 75 | Health Care | 4101458 |
| ## | 76 | Consumer Staples | 16033591 |
| ## | 77 | Financials | 3800548 |
| ## | 78 | Health Care | 6773251 |
| ## | 79 | Health Care | 2212211 |
| ## | 80 | Health Care | 2945983 |
| ## | 81 | Information Technology | 4785852 |
| ## | 82 | Health Care | 7684789 |
| ## | 83 | Information Technology | 13311328 |
| ## | 84 | Financials | 3927643 |
| ## | 85 | Consumer Discretionary | 13690399 |
| ## | 86 | Health Care | 1253634 |
| ## | 87 | Utilities | 7828438 |
| ## | 88 | Communication Services | 1950416 |
| ## | 89 | Energy | 15117770 |
| ## | 90 | Financials | 5061222 |
| ## | 91 | Information Technology | 2850040 |
| ## | 92 | Consumer Staples | 8841804 |
| ## | 93 | Industrials | 8814182 |
| ## | 94 | Energy | 6326332 |
| ## | 95 | Health Care | 3389350 |
| ## | 96 | Financials | 5072966 |
| ## | 97 | Consumer Staples | 9464497 |
| ## | 98 | Real Estate | 3377012 |
| ## | 99 | Financials | 13134280 |
| ## | 100 | Health Care | 15105250 |
| ## | 101 | Utilities | 8249501 |
| ## | 102 | Financials | 14362621 |
| ## | 103 | Communication Services | 11606211 |
| ## | 104 | Financials | 1340362 |
| ## | 105 | Industrials | 3111283 |
| ## | 106 | Energy | 8356286 |
| ## | 107 | , | 14335656 |
| ## | 108 | Industrials | 3508474 |
| ## | 109 | Utilities | 11293749 |
| ## | 110 | Industrials | 2992855 |
| ## | 111 | Industrials | 1901582 |
| ## | 112 | Financials | 2744956 |
| ## | 113 | Real Estate | 4529516 |
| ## | 114 | Industrials | 3043009 |
| ## | 115 | Financials Health Care | 10046857 |
| ## | 116 | | 2791257 |
| ## | 117 | Information Technology | 12313897 10545466 |
| ## | 118 119 | Utilities Financials | 5503610 |
| ## | 120 | Health Care | 5251650 |
| ## | 120 | | 7579710 |
| ## | 121 | Energy Real Estate | 6873344 |
| ## | 123 | Financials | 10869825 |
| ## | 123 | Industrials | 3372816 |
| ## | 124 | industrials | 2217210 |

| ## | 125 | Health Care | 3485269 |
|----|-----|------------------------|----------|
| ## | 126 | Health Care | 1605308 |
| ## | 127 | Industrials | 2651972 |
| ## | 128 | Financials | 6265545 |
| ## | 129 | Industrials | 6845957 |
| ## | 130 | Health Care | 1504560 |
| ## | 131 | Information Technology | 6323489 |
| ## | 132 | Financials | 2647597 |
| ## | 133 | Materials | 2776346 |
| ## | 134 | Financials | 6366478 |
| ## | 135 | Consumer Staples | 3788826 |
| ## | 136 | Energy | 4667958 |
| ## | 137 | Financials | 4565907 |
| ## | 138 | Information Technology | 4059161 |
| ## | 139 | Financials | 8441104 |
| ## | 140 | Utilities | 5381653 |
| ## | 141 | Financials | 5228546 |
| ## | 142 | Industrials | 4299405 |
| ## | 143 | Health Care | 2948341 |
| ## | 144 | Information Technology | 10734333 |
| ## | 145 | Consumer Discretionary | 5738562 |
| ## | 146 | Materials | 2394666 |
| ## | 147 | Financials | 8378780 |
| ## | 148 | Financials | 9683932 |
| ## | 149 | Health Care | 2290413 |
| ## | 150 | Information Technology | 17278248 |
| ## | 151 | Health Care | 5426107 |
| ## | 152 | Materials | 904940 |
| ## | 153 | Energy | 4663221 |
| ## | 154 | Information Technology | 3587225 |
| ## | 155 | Energy | 20721726 |
| ## | 156 | Consumer Discretionary | 4115142 |
| ## | 157 | Information Technology | 2379755 |
| ## | | Consumer Discretionary | 3148294 |
| ## | 159 | Consumer Staples | 2449646 |
| ## | 160 | 0, | 4416413 |
| ## | 161 | Financials | 2919089 |
| ## | 162 | Industrials | 4725856 |
| ## | 163 | Real Estate | 882199 |
| ## | 164 | Communication Services | 8327456 |
| ## | 165 | Consumer Discretionary | 42749332 |
| ## | 166 | Consumer Discretionary | 9947385 |
| ## | 167 | Energy | 13211548 |
| ## | 168 | Health Care | 846096 |
| ## | 169 | Communication Services | 3335426 |
| ## | 170 | Financials | 3774086 |
| ## | 171 | Industrials | 10098861 |
| ## | 172 | Consumer Staples | 5222715 |
| ## | 173 | Industrials | 1128806 |
| ## | 174 | Industrials | 6873085 |
| ## | 175 | Information Technology | 1935077 |
| ## | 176 | Consumer Discretionary | 2903658 |
| ## | 177 | Utilities | 2987326 |
| ## | 178 | Consumer Discretionary | 878425 |
| | | | |

| ## | 179 | Real Estate | 1636418 |
|----|------------|--------------------------------|--------------------|
| ## | | Information Technology | 2755723 |
| ## | 181 | Financials | 5028027 |
| ## | 182 | Consumer Discretionary | 3461448 |
| ## | 183 | Industrials | 5637370 |
| ## | 184 | Consumer Staples | 6794417 |
| ## | 185 | Real Estate | 4124124 |
| ## | 186 | Consumer Staples | 1825683 |
| ## | 187 | Health Care | 2433510 |
| ## | 188 | 0, | 3802557 1722416 |
| ## | 189 190 | 0, | 5517268 |
| ## | 190 | Utilities Congumen Digerations | |
| | 191 | Consumer Discretionary | 3557434 |
| ## | 192 | Financials | 1823290 |
| ## | 193 | Energy | 9613979 |
| ## | 194 | Materials Tacharlam | 3491712 8852467 |
| ## | 195 | Information Technology | 4490440 |
| ## | 190 | Energy Information Technology | 3271969 |
| ## | 198 | Utilities | 5643593 |
| ## | 199 | Real Estate | 1509296 |
| ## | 200 | Health Care | 2181810 |
| ## | 201 | Real Estate | 4020945 |
| ## | 202 | Consumer Staples | 6506921 |
| ## | 203 | Financials | 4145673 |
| ## | 204 | Health Care | 4481716 |
| ## | 205 | Materials | 2644321 |
| ## | 206 | Industrials | 2678846 |
| ## | 207 | Health Care | 2221510 |
| ## | 208 | Health Care | 3467173 |
| ## | 209 | Financials | 1571095 |
| ## | 210 | Energy | 1851432 |
| ## | 211 | Energy | 2188314 |
| ## | 212 | Financials | 3746094 |
| ## | 213 | Utilities | 3396411 |
| ## | 214 | Consumer Discretionary | 3260214 |
| ## | 215 | Communication Services | 5325635 |
| ## | 216 | Information Technology | 3495366 |
| ## | 217 | Industrials | 3231765 |
| ## | 218 | Industrials | 3821761 |
| ## | 219 | Real Estate | 2249676 |
| ## | 220 | Financials | 2648802 |
| ## | 221 | Consumer Staples | 6136183 |
| ## | 222 | Consumer Staples | 8680506 |
| | 223 | Industrials | 1642124 |
| | | Consumer Discretionary | 2582660 |
| ## | 225 | Consumer Discretionary | 277521 |
| ## | 226 | Utilities | 3427101 |
| | 227 | Consumer Staples | 4343785 |
| | 228 | Energy | 5601322 |
| | | Consumer Discretionary | 4412013 |
| | 230 | Real Estate | 3869811 |
| | | Information Technology | 15643081 |
| ## | 232 | Industrials | 1443835 |

| ## | 233 | Health Care | 1760100 |
|----|------------|----------------------------------|-------------------|
| ## | 234 | Information Technology | 1795575 |
| ## | 235 | Communication Services | 7868838 |
| ## | 236 | Financials | 1425562 |
| ## | 237 | Utilities | 3441836 |
| ## | 238 | Utilities | 7901413 |
| ## | 239 | Industrials | 1343665 |
| ## | 240 | Utilities | 1984554 |
| ## | 241 | Financials | 7453370 |
| ## | 242 | Consumer Discretionary | 2895350 |
| ## | 243 | Information Technology | 2551726 |
| ## | 244 | Industrials | 528184 |
| ## | 245 | Real Estate | 1252681 |
| ## | 246 | Industrials | 1677327 |
| ## | 247 | Information Technology | 9650679 |
| ## | 248 | Financials | 2441622 |
| ## | 249 | Real Estate | 3239184 |
| ## | 250 | Industrials | 1799774 |
| ## | 251 | Real Estate | 1675955 |
| ## | 252 | Industrials | 2500381 |
| ## | 253 | Consumer Discretionary | 1870616 |
| ## | 254 | Consumer Staples | 1400955 |
| ## | 255 | Information Technology | 963283 |
| ## | 256 | Utilities | 3538982 |
| ## | 257 | Information Technology | 1733167 |
| ## | 258 | Industrials | 1287679 |
| ## | 259 | Materials | 4461923 |
| ## | 260 | Utilities | 5312109 |
| ## | 261 | Real Estate | 8226775 |
| ## | 262 | Industrials | 3914760 |
| ## | 263 | Health Care | 3594290 |
| ## | 264 | | 1173766 |
| ## | 265 | Information Technology Materials | 3457348 |
| ## | 266 | Materials | 3769475 |
| ## | | | |
| ## | 267 268 | Health Care | 798947 3234016 |
| | 269 | Consumer Staples | |
| ## | | Financials | 1547442 |
| ## | 270 | Financials | 11484608 |
| ## | 271 | Information Technology | 3067559 |
| ## | 272 | Real Estate | 717552 |
| | 273 | Health Care | 945392 |
| | 274 | Industrials | 2514572 |
| | 275 | Financials | 7283773 |
| | 276 | Health Care | 840888 |
| | 277 | Industrials | 3124053 |
| | 278 | Materials | 15837152 |
| | 279 | Utilities | 1971184 |
| ## | 280 | Materials | 5794860 |
| ## | 281 | Industrials | 939128 |
| ## | 282 | Financials | 5203126 |
| | | Consumer Discretionary | 620090 |
| ## | 284 | Financials | 3889356 |
| ## | 285 | Financials | 1843857 |
| ## | 286 | Communication Services | 3693436 |
| | | | |

| ## | 287 | Industrials | 2381179 |
|----|------------|------------------------------------|--------------------|
| ## | 288 | Information Technology | 1706564 |
| ## | 289 | Utilities | 2645846 |
| ## | 290 | Health Care | 274795 |
| ## | 291 | Communication Services | 2447402 |
| ## | 292 | Health Care | 3275280 |
| ## | 293 | Financials | 11353641 |
| ## | 294 | Information Technology | 2835577 |
| ## | 295 | Industrials | 851775 |
| ## | 296 | Health Care | 5629673 |
| ## | 297 | Health Care | 490005 |
| ## | 298 | Energy | 1678142 |
| ## | 299 | Utilities | 1963267 |
| ## | 300 | Utilities | 2951350 |
| ## | 301 | Real Estate | 3452740 |
| ## | 302 | Information Technology | 3077792 |
| ## | 303 | Consumer Staples | 2656922 |
| ## | 304 | Consumer Discretionary | 1589238 |
| ## | 305 | Consumer Staples | 1324279 |
| ## | 306 | Information Technology | 1832858 |
| ## | 307 | Financials | 968497 |
| ## | 308 | Health Care | 1111794 |
| ## | 309 | Consumer Staples | 1526384 |
| ## | 310 | Utilities | 5366678 |
| ## | 311 | Consumer Discretionary | 1296049 |
| ## | 312 | Information Technology | 2038376 |
| ## | 313 | Financials | 11671771 |
| ## | 314 | Information Technology | 1608117 |
| ## | 315 | Utilities | 3092984 |
| ## | 316 | Consumer Discretionary | 268854 |
| ## | 317 | Information Technology | 1951800 |
| ## | 318 | Materials | 1436228 |
| ## | 319 | Information Technology | 7010013 |
| ## | 320 | Real Estate | 5240775 |
| ## | 321 | Information Technology | 3071238 |
| ## | 322 | Health Care | 1910436 |
| ## | 323 | Information Technology | 913731 |
| ## | 324 | Energy | 9281057 |
| ## | 325 | Energy | 2750316 |
| | 326 | Financials | 1978764 |
| | | Consumer Discretionary | 5589458 |
| | 328 | Industrials | 496123 |
| | 329 | Consumer Staples | 2764699 |
| | 330 | Industrials | 4470119 |
| | 331 | Consumer Discretionary | 3187318 |
| | 332 | Real Estate | 1153852 |
| | 333 | Health Care | 1546184 |
| | | Consumer Discretionary | 2574321 |
| | | Financials | 1776056 |
| | 335 | | |
| ## | 336 | Health Care | 545599 |
| | | Consumer Discretionary | 1354233 |
| ## | 338 | Health Care | 1747146 |
| | 227 | Tnformo+ T | 0170075 |
| ## | 339 340 | Information Technology Real Estate | 3176075 8051085 |

| ## | 341 | Consumer Discretionary | 3730843 |
|-----|-----|------------------------|----------|
| ## | 342 | Information Technology | 1399057 |
| ## | 343 | Industrials | 2716830 |
| ## | 344 | Information Technology | 564156 |
| ## | 345 | Health Care | 532562 |
| ## | 346 | Industrials | 1613347 |
| ## | 347 | Financials | 2894667 |
| ## | 348 | Health Care | 512924 |
| ## | 349 | Energy | 5141867 |
| ## | 350 | Materials | 1105247 |
| ## | 351 | Financials | 2363409 |
| ## | 352 | Industrials | 1953788 |
| ## | 353 | Energy | 5547419 |
| ## | 354 | Industrials | 1305700 |
| ## | 355 | Materials | 1423524 |
| ## | 356 | Communication Services | 10379065 |
| ## | 357 | Financials | 3040086 |
| ## | 358 | Financials | 574548 |
| ## | 359 | Information Technology | 987044 |
| ## | 360 | Financials | 1652133 |
| ## | 361 | Industrials | 1902907 |
| ## | 362 | Industrials | 1516193 |
| ## | 363 | Energy | 4152349 |
| ## | 364 | Real Estate | 1381347 |
| ## | 365 | Health Care | 2969890 |
| ## | 366 | Consumer Discretionary | 805121 |
| ## | 367 | Utilities | 3188619 |
| ## | 368 | Real Estate | 3022753 |
| ## | 369 | Financials | 2835503 |
| ## | 370 | Health Care | 1008799 |
| ## | 371 | Consumer Discretionary | 1069451 |
| ## | 372 | Consumer Staples | 5327094 |
| ## | 373 | Information Technology | 1569001 |
| ## | 374 | Information Technology | 2852071 |
| ## | 375 | Health Care | 1475566 |
| ## | 376 | Materials | 681336 |
| ## | 377 | Consumer Discretionary | 1325791 |
| ## | 378 | Real Estate | 1879215 |
| ## | 379 | Real Estate | 1235370 |
| ## | 380 | Consumer Staples | 2968258 |
| ## | 381 | Information Technology | 1272004 |
| ## | 382 | Consumer Staples | 1233183 |
| ## | 383 | Materials | 1540210 |
| ## | 384 | Health Care | 939188 |
| ## | | Consumer Discretionary | 2399286 |
| ## | 386 | Industrials | 3355027 |
| ## | 387 | Information Technology | 1790425 |
| ## | 388 | Utilities | 1291661 |
| ## | 389 | Consumer Staples | 2044159 |
| ## | 390 | Materials | 3871360 |
| ## | 391 | Materials | 1453268 |
| ## | 392 | Energy | 4147562 |
| ## | 393 | Real Estate | 1852404 |
| ## | 394 | Industrials | 903877 |
| ıτπ | JJI | Industrials | 200011 |

| ## | | Energy | 4818499 |
|----|-----|------------------------|---------|
| ## | 396 | Utilities | 7182509 |
| ## | 397 | Consumer Discretionary | 1829183 |
| ## | 398 | Consumer Discretionary | 1935735 |
| ## | 399 | Industrials | 1113767 |
| ## | 400 | Industrials | 2206502 |
| ## | 401 | Energy | 5235531 |
| ## | 402 | Financials | 1435488 |
| ## | 403 | Communication Services | 1241900 |
| ## | 404 | Real Estate | 3876499 |
| ## | 405 | Utilities | 2551075 |
| ## | 406 | Financials | 1216629 |
| ## | 407 | Information Technology | 664116 |
| ## | 408 | Information Technology | 846668 |
| ## | 409 | Consumer Staples | 1620658 |
| ## | 410 | Health Care | 1195097 |
| ## | 411 | Consumer Discretionary | 3124383 |
| ## | 412 | Communication Services | 3833174 |
| ## | 413 | Energy | 4718422 |
| ## | 414 | Consumer Discretionary | 1276288 |
| ## | 415 | Financials | 1255942 |
| ## | 416 | Real Estate | 3124109 |
| ## | 417 | Utilities | 1214980 |
| ## | 418 | Materials | 2786398 |
| ## | 419 | Communication Services | 3930185 |
| ## | 420 | Financials | 3342977 |
| ## | 421 | Consumer Discretionary | 1191398 |
| ## | 422 | Real Estate | 794526 |
| ## | 423 | Utilities | 3967883 |
| ## | 424 | Industrials | 941785 |
| ## | 425 | Financials | 2122059 |
| ## | 426 | Materials | 2536327 |
| ## | 427 | Health Care | 2424846 |
| ## | 428 | Health Care | 1668249 |
| ## | 429 | Industrials | 472130 |
| ## | 430 | Information Technology | 3793694 |
| ## | 431 | Energy | 1770424 |
| ## | 432 | Industrials | 3893577 |
| ## | | Materials | 1024844 |
| | 434 | Materials | 946952 |
| | | Communication Services | 4185522 |
| | 436 | Industrials | 616986 |
| | | Consumer Discretionary | 696269 |
| | 438 | Financials | 446368 |
| | 439 | Materials | 1184371 |
| | | Consumer Discretionary | 689241 |
| | | Consumer Discretionary | 2282471 |
| | 442 | Industrials | 1037700 |
| | | Consumer Discretionary | 1320464 |
| | | Consumer Discretionary | 837593 |
| | 445 | Financials | 1132802 |
| | | Consumer Discretionary | 3475186 |
| | | Information Technology | 517747 |
| ## | 448 | Consumer Staples | 1832793 |

| ## | 449 | Industrials | 1334917 |
|----|-----|------------------------|---------|
| ## | 450 | Industrials | 1296545 |
| ## | 451 | Industrials | 1339031 |
| ## | 452 | Information Technology | 1361089 |
| ## | 453 | Information Technology | 4880875 |
| ## | 454 | Financials | 2382921 |
| ## | 455 | Real Estate | 943705 |
| ## | 456 | Real Estate | 1710661 |
| ## | 457 | Financials | 4461157 |
| ## | 458 | Consumer Discretionary | 3326163 |
| ## | 459 | Industrials | 4695504 |
| ## | 460 | Real Estate | 4616746 |
| ## | 461 | Health Care | 1384655 |
| ## | 462 | Consumer Discretionary | 4746547 |
| ## | 463 | Industrials | 1573427 |
| ## | 464 | Energy | 1035895 |
| ## | 465 | Health Care | 1884332 |
| ## | 466 | Information Technology | 1489880 |
| ## | 467 | Consumer Discretionary | 2851670 |
| ## | 468 | Consumer Discretionary | 615328 |
| ## | 469 | Communication Services | 2486454 |
| ## | 470 | Industrials | 1792505 |
| ## | 471 | Consumer Discretionary | 1275513 |
| ## | 472 | Consumer Discretionary | 4022810 |
| ## | 473 | Information Technology | 2428599 |
| ## | 474 | Industrials | 1552478 |
| ## | 475 | Materials | 1733776 |
| ## | 476 | Consumer Discretionary | 1627708 |
| ## | 477 | Consumer Staples | 2076504 |
| ## | 478 | Financials | 4066548 |
| ## | 479 | Consumer Discretionary | 2491820 |
| ## | 480 | Industrials | 1420509 |
| ## | 481 | Energy | 1182082 |
| ## | 482 | Consumer Discretionary | 1816851 |
| ## | 483 | Health Care | 1372418 |
| ## | 484 | Financials | 3166258 |
| ## | 485 | Industrials | 1612804 |
| ## | 486 | Consumer Discretionary | 1436217 |
| ## | 487 | Financials | 583435 |
| ## | 488 | Communication Services | 1116383 |
| ## | 489 | Information Technology | 393061 |
| ## | 490 | Consumer Discretionary | 2391279 |
| ## | 491 | Industrials | 1606564 |
| ## | 492 | Financials | 575956 |
| ## | 493 | Consumer Discretionary | 1250523 |
| ## | 494 | Industrials | 1526223 |
| ## | 495 | Financials | 1302087 |
| ## | 496 | Consumer Staples | 4912631 |
| ## | 497 | Consumer Discretionary | 2224465 |
| ## | 498 | Communication Services | 4161396 |
| ## | 499 | Consumer Discretionary | 3735261 |
| ## | 500 | Real Estate | 1169252 |
| ## | 501 | Communication Services | 1694339 |
| ## | 502 | Consumer Discretionary | 2585962 |
| | | | |

```
## 503 Consumer Discretionary 2019164
## 504 Consumer Discretionary 2043966
## 505 Communication Services 1244468
## 506 Energy 292529
```

Question

Which stock prices behave similarly?

Answering this question helps us **understand which companies are related**, and we can use clustering to help us answer it!

Even if you're not interested in finance, this is still a great analysis because it will tell you which companies are competitors and which are likely in the same space (often called sectors) and can be categorized together. Bottom line - This analysis can help you better understand the dynamics of the market and competition, which is useful for all types of analyses from finance to sales to marketing.

Let's get started.

Step 1 - Convert stock prices to a standardized format (daily returns)

What you first need to do is get the data in a format that can be converted to a "user-item" style matrix. The challenge here is to connect the dots between what we have and what we need to do to format it properly.

We know that in order to compare the data, it needs to be standardized or normalized. Why? Because we cannot compare values (stock prices) that are of completely different magnitudes. In order to standardize, we will convert from adjusted stock price (dollar value) to daily returns (percent change from previous day). Here is the formula.

$$return_{daily} = \frac{price_i - price_{i-1}}{price_{i-1}}$$

First, what do we have? We have stock prices for every stock in the SP 500 Index, which is the daily stock prices for over 500 stocks. The data set is over 1.2M observations.

```
sp_500_prices_tbl %>% glimpse()
```

```
## Rows: 1,225,765
## Columns: 8
              <chr> "MSFT", "MSFT", "MSFT", "MSFT", "MSFT", "MSFT", "MSFT", "M...
## $ symbol
## $ date
              <date> 2009-01-02, 2009-01-05, 2009-01-06, 2009-01-07, 2009-01-0...
              <dbl> 19.53, 20.20, 20.75, 20.19, 19.63, 20.17, 19.71, 19.52, 19...
## $ open
              <dbl> 20.40, 20.67, 21.00, 20.29, 20.19, 20.30, 19.79, 19.99, 19...
## $ high
## $ low
              <dbl> 19.37, 20.06, 20.61, 19.48, 19.55, 19.41, 19.30, 19.52, 19...
## $ close
              <dbl> 20.33, 20.52, 20.76, 19.51, 20.12, 19.52, 19.47, 19.82, 19...
## $ volume
              <dbl> 50084000, 61475200, 58083400, 72709900, 70255400, 49815300...
## $ adjusted <dbl> 15.86624, 16.01451, 16.20183, 15.22628, 15.70234, 15.23408...
```

Your first task is to convert to a tibble named sp_500_daily_returns_tbl by performing the following operations:

Select the symbol, date and adjusted columns

- Filter to dates beginning in the year 2018 and beyond.
- Compute a Lag of 1 day on the adjusted stock price. Be sure to group by symbol first, otherwise we will have lags computed using values from the previous stock in the data frame.
- Remove a NA values from the lagging operation
- Compute the difference between adjusted and the lag
- Compute the percentage difference by dividing the difference by that lag. Name this column pct_return.
- Return only the symbol, date, and pct_return columns
- Save as a variable named sp_500_daily_returns_tbl

```
# Apply your data transformation skills!
sp_500_daily_returns_tbl <- sp_500_index_tbl %>%
  left_join(sp_500_prices_tbl) %>%
  select(symbol,date, adjusted)%>%
  separate(col
                  = date,
                  = c("year", "month", "day"),
           into
                  = "-",
           remove = FALSE)%>%
  filter(year >= 2018) %>%
  filter(!is.na(adjusted)) %>%
  group_by(symbol) %>%
  mutate(pct_return = ('adjusted' - lag('adjusted')) / lag('adjusted')) %>%
  filter(!is.na(pct_return)) %>%
  select(symbol, date, pct_return )
sp_500_daily_returns_tbl
```

```
## # A tibble: 141,340 x 3
## # Groups:
              symbol [502]
##
      symbol date
                       pct return
##
      <chr> <date>
                             <dbl>
                          0.00465
##
   1 MSFT
            2018-01-03
## 2 MSFT
            2018-01-04
                         0.00880
## 3 MSFT
            2018-01-05
                         0.0124
## 4 MSFT
            2018-01-08
                         0.00102
## 5 MSFT
            2018-01-09 -0.000680
## 6 MSFT
            2018-01-10 -0.00453
## 7 MSFT
            2018-01-11
                         0.00296
## 8 MSFT
            2018-01-12
                          0.0173
## 9 MSFT
            2018-01-16 -0.0140
## 10 MSFT
            2018-01-17
                          0.0203
## # ... with 141,330 more rows
```

```
# Output: sp_500_daily_returns_tbl
```

Step 2 - Convert to User-Item Format

The next step is to convert to a user-item format with the symbol in the first column and every other column the value of the *daily returns* (pct_return) for every stock at each date.

We're going to import the correct results first (just in case you were not able to complete the last step).

```
sp_500_daily_returns_tbl <- read_rds("sp_500_daily_returns_tbl.rds")
sp_500_daily_returns_tbl</pre>
```

```
## # A tibble: 141,340 x 3
##
      symbol date
                        pct return
##
      <chr> <date>
                              <dbl>
##
    1 MSFT
             2018-01-03
                           0.00465
##
    2 MSFT
                          0.00880
             2018-01-04
##
   3 MSFT
             2018-01-05
                          0.0124
   4 MSFT
##
             2018-01-08
                          0.00102
    5 MSFT
             2018-01-09
                         -0.000680
##
##
   6 MSFT
             2018-01-10 -0.00453
##
   7 MSFT
             2018-01-11
                          0.00296
##
    8 MSFT
             2018-01-12
                          0.0173
## 9 MSFT
             2018-01-16 -0.0140
## 10 MSFT
             2018-01-17
                          0.0203
## # ... with 141,330 more rows
```

Now that we have the daily returns (percentage change from one day to the next), we can convert to a user-item format. The user in this case is the symbol (company), and the item in this case is the pct_return at each date.

- Spread the date column to get the values as percentage returns. Make sure to fill an NA values with zeros.
- Save the result as stock_date_matrix_tbl

```
# Convert to User-Item Format
stock_date_matrix_tbl <- sp_500_daily_returns_tbl %>%
    pivot_wider(names_from = date, values_from = pct_return, values_fill = 0) %>%
    ungroup()
stock_date_matrix_tbl
```

```
## # A tibble: 502 x 283
##
      symbol '2018-01-03' '2018-01-04' '2018-01-05' '2018-01-08' '2018-01-09'
##
      <chr>
                                  <dbl>
                                                <dbl>
                                                              <dbl>
                                                                            <dbl>
                     <dbl>
   1 MSFT
                 0.00465
                              0.00880
                                             0.0124
                                                            0.00102
                                                                       -0.000680
    2 AAPL
                -0.000174
                              0.00465
                                             0.0114
                                                           -0.00371
                                                                       -0.000115
##
##
    3 AMZN
                 0.0128
                              0.00448
                                             0.0162
                                                            0.0144
                                                                        0.00468
##
   4 FB
                 0.0179
                             -0.00184
                                             0.0137
                                                            0.00765
                                                                       -0.00218
##
   5 JNJ
                 0.00955
                             -0.0000712
                                             0.00825
                                                            0.00127
                                                                        0.0159
    6 JPM
##
                 0.00102
                              0.0143
                                            -0.00642
                                                            0.00148
                                                                        0.00507
##
   7 GOOG
                  0.0164
                              0.00362
                                             0.0146
                                                            0.00427
                                                                       -0.000614
##
    8 GOOGL
                  0.0171
                              0.00388
                                             0.0133
                                                            0.00353
                                                                       -0.00127
    9 XOM
                                                                       -0.00425
##
                 0.0196
                              0.00138
                                            -0.000806
                                                            0.00450
## 10 BAC
                -0.00334
                              0.0131
                                             0.00464
                                                           -0.00692
                                                                        0.00498
## # ... with 492 more rows, and 277 more variables: ^{\circ}2018-01-10^{\circ} <dbl>,
       '2018-01-11' <dbl>, '2018-01-12' <dbl>, '2018-01-16' <dbl>,
       '2018-01-17' <dbl>, '2018-01-18' <dbl>, '2018-01-19' <dbl>,
## #
       '2018-01-22' <dbl>, '2018-01-23' <dbl>, '2018-01-24' <dbl>,
## #
       '2018-01-25' <dbl>, '2018-01-26' <dbl>, '2018-01-29' <dbl>,
## #
       '2018-01-30' <dbl>, '2018-01-31' <dbl>, '2018-02-01' <dbl>,
       '2018-02-02' <dbl>, '2018-02-05' <dbl>, '2018-02-06' <dbl>,
## #
```

```
'2018-02-21' <dbl>, '2018-02-22' <dbl>, '2018-02-23' <dbl>,
## #
       '2018-02-26' <dbl>, '2018-02-27' <dbl>, '2018-02-28' <dbl>,
##
       '2018-03-01' <dbl>, '2018-03-02' <dbl>, '2018-03-05' <dbl>,
##
       '2018-03-06' <dbl>, '2018-03-07' <dbl>, '2018-03-08' <dbl>,
## #
       '2018-03-09' <dbl>, '2018-03-12' <dbl>, '2018-03-13' <dbl>,
## #
## #
       '2018-03-14' <dbl>, '2018-03-15' <dbl>, '2018-03-16' <dbl>,
## #
       '2018-03-19' <dbl>, '2018-03-20' <dbl>, '2018-03-21' <dbl>,
## #
       '2018-03-22' <dbl>, '2018-03-23' <dbl>, '2018-03-26' <dbl>,
       '2018-03-27' <dbl>, '2018-03-28' <dbl>, '2018-03-29'
## #
##
       '2018-04-02' <dbl>, '2018-04-03' <dbl>, '2018-04-04' <dbl>,
## #
       '2018-04-05' <dbl>, '2018-04-06' <dbl>, '2018-04-09' <dbl>,
       '2018-04-10' <dbl>, '2018-04-11' <dbl>, '2018-04-12' <dbl>,
## #
       '2018-04-13' <dbl>, '2018-04-16' <dbl>, '2018-04-17' <dbl>,
## #
       '2018-04-18' <dbl>, '2018-04-19' <dbl>, '2018-04-20' <dbl>,
## #
       '2018-04-23' <dbl>, '2018-04-24' <dbl>, '2018-04-25' <dbl>,
## #
       '2018-04-26' <dbl>, '2018-04-27' <dbl>, '2018-04-30' <dbl>,
## #
       '2018-05-01' <dbl>, '2018-05-02' <dbl>, '2018-05-03' <dbl>,
## #
## #
       '2018-05-04' <dbl>, '2018-05-07' <dbl>, '2018-05-08' <dbl>,
       '2018-05-09' <dbl>, '2018-05-10' <dbl>, '2018-05-11' <dbl>,
## #
       '2018-05-14' <dbl>, '2018-05-15' <dbl>, '2018-05-16' <dbl>,
## #
       '2018-05-17' <dbl>, '2018-05-18' <dbl>, '2018-05-21' <dbl>,
## #
## #
       '2018-05-22' <dbl>, '2018-05-23' <dbl>, '2018-05-24' <dbl>,
## #
       '2018-05-25' <dbl>, '2018-05-29' <dbl>, '2018-05-30' <dbl>,
## #
       '2018-05-31' <dbl>, '2018-06-01' <dbl>, '2018-06-04' <dbl>,
```

'2018-02-07' <dbl>, '2018-02-08' <dbl>, '2018-02-09' <dbl>, '2018-02-12' <dbl>, '2018-02-13' <dbl>, '2018-02-14' <dbl>,

'2018-02-15' <dbl>, '2018-02-16' <dbl>, '2018-02-20' <dbl>,

Step 3 - Perform K-Means Clustering

Next, we'll perform **K-Means clustering**.

Output: stock date matrix tbl

#

#

We're going to import the correct results first (just in case you were not able to complete the last step).

```
stock_date_matrix_tbl <- read_rds("stock_date_matrix_tbl.rds")
stock_date_matrix_tbl</pre>
```

```
## # A tibble: 502 x 283
##
      symbol '2018-01-03' '2018-01-04' '2018-01-05' '2018-01-08' '2018-01-09'
##
      <chr>
                     <dbl>
                                   <dbl>
                                                 <dbl>
                                                               <dbl>
                                                                             <dbl>
                  0.0254
##
                                -0.00750
                                              0.0160
                                                             0.00215
                                                                          0.0246
    1 A
##
    2 AAL
                 -0.0123
                                 0.00630
                                             -0.000380
                                                            -0.00988
                                                                         -0.000959
##
    3 AAP
                  0.00905
                                 0.0369
                                              0.0106
                                                            -0.00704
                                                                         -0.00808
                 -0.000174
                                 0.00465
                                              0.0114
                                                            -0.00371
                                                                         -0.000115
##
    4 AAPL
                                -0.00570
##
    5 ABBV
                  0.0156
                                              0.0174
                                                            -0.0160
                                                                          0.00754
##
    6 ABC
                  0.00372
                                -0.00222
                                              0.0121
                                                             0.0166
                                                                          0.00640
##
    7 ABMD
                  0.0173
                                 0.0175
                                              0.0154
                                                             0.0271
                                                                          0.00943
                                -0.00170
##
    8 ABT
                  0.00221
                                              0.00289
                                                            -0.00288
                                                                          0.00170
##
    9 ACN
                  0.00462
                                 0.0118
                                              0.00825
                                                             0.00799
                                                                          0.00333
## 10 ADBE
                  0.0188
                                 0.0120
                                              0.0116
                                                            -0.00162
                                                                          0.00897
\#\# # ... with 492 more rows, and 277 more variables: '2018-01-10' <dbl>,
```

```
'2018-01-11' <dbl>, '2018-01-12' <dbl>, '2018-01-16' <dbl>,
## #
## #
       '2018-01-17' <dbl>, '2018-01-18' <dbl>, '2018-01-19' <dbl>,
       '2018-01-22' <dbl>, '2018-01-23' <dbl>, '2018-01-24' <dbl>,
## #
       '2018-01-25' <dbl>, '2018-01-26' <dbl>, '2018-01-29' <dbl>,
## #
       '2018-01-30' <dbl>, '2018-01-31' <dbl>, '2018-02-01' <dbl>,
## #
       '2018-02-02' <dbl>, '2018-02-05' <dbl>, '2018-02-06' <dbl>,
## #
       '2018-02-07' <dbl>, '2018-02-08' <dbl>, '2018-02-09' <dbl>,
## #
       '2018-02-12' <dbl>, '2018-02-13' <dbl>, '2018-02-14' <dbl>,
## #
## #
       '2018-02-15' <dbl>, '2018-02-16' <dbl>, '2018-02-20' <dbl>,
       '2018-02-21' <dbl>, '2018-02-22' <dbl>, '2018-02-23' <dbl>,
## #
## #
       '2018-02-26' <dbl>, '2018-02-27' <dbl>, '2018-02-28' <dbl>,
       '2018-03-01' <dbl>, '2018-03-02' <dbl>, '2018-03-05' <dbl>,
## #
       '2018-03-06' <dbl>, '2018-03-07' <dbl>, '2018-03-08' <dbl>,
## #
       '2018-03-09' <dbl>, '2018-03-12' <dbl>, '2018-03-13' <dbl>,
## #
## #
       '2018-03-14' <dbl>, '2018-03-15' <dbl>, '2018-03-16' <dbl>,
       '2018-03-19' <dbl>, '2018-03-20' <dbl>, '2018-03-21' <dbl>,
## #
       '2018-03-22' <dbl>, '2018-03-23' <dbl>, '2018-03-26' <dbl>,
## #
## #
       '2018-03-27' <dbl>, '2018-03-28' <dbl>, '2018-03-29' <dbl>,
       '2018-04-02' <dbl>, '2018-04-03' <dbl>, '2018-04-04' <dbl>,
## #
       '2018-04-05' <dbl>, '2018-04-06' <dbl>, '2018-04-09' <dbl>,
## #
## #
       '2018-04-10' <dbl>, '2018-04-11' <dbl>, '2018-04-12' <dbl>,
       '2018-04-13' <dbl>, '2018-04-16' <dbl>, '2018-04-17' <dbl>,
## #
       '2018-04-18' <dbl>, '2018-04-19' <dbl>, '2018-04-20' <dbl>,
## #
       '2018-04-23' <dbl>, '2018-04-24' <dbl>, '2018-04-25' <dbl>,
## #
       '2018-04-26' <dbl>, '2018-04-27' <dbl>, '2018-04-30' <dbl>,
## #
       '2018-05-01' <dbl>, '2018-05-02' <dbl>, '2018-05-03' <dbl>.
## #
       '2018-05-04' <dbl>, '2018-05-07' <dbl>, '2018-05-08' <dbl>,
## #
       '2018-05-09' <dbl>, '2018-05-10' <dbl>, '2018-05-11' <dbl>,
## #
       '2018-05-14' <dbl>, '2018-05-15' <dbl>, '2018-05-16' <dbl>,
## #
       '2018-05-17' <dbl>, '2018-05-18' <dbl>, '2018-05-21' <dbl>,
## #
       '2018-05-22' <dbl>, '2018-05-23' <dbl>, '2018-05-24' <dbl>,
## #
## #
       '2018-05-25' <dbl>, '2018-05-29' <dbl>, '2018-05-30' <dbl>,
       '2018-05-31' <dbl>, '2018-06-01' <dbl>, '2018-06-04' <dbl>, ...
## #
```

Beginning with the stock_date_matrix_tbl, perform the following operations:

- Drop the non-numeric column, symbol
- Perform kmeans() with centers = 4 and nstart = 20
- Save the result as kmeans_obj

Use glance() to get the tot.withinss.

29.2

4.40

1 33.6

```
# Apply glance() to get the tot.withinss
broom::glance(kmeans_obj)

## # A tibble: 1 x 4

## totss tot.withinss betweenss iter

## <dbl> <dbl> <dbl> <int>
```

3

Step 4 - Find the optimal value of K

Now that we are familiar with the process for calculating kmeans(), let's use purrr to iterate over many values of "k" using the centers argument.

We'll use this **custom function** called kmeans_mapper():

```
kmeans_mapper <- function(center = 3) {
    stock_date_matrix_tbl %>%
    select(-symbol) %>%
    kmeans(centers = center, nstart = 20)
}
```

Apply the kmeans_mapper() and glance() functions iteratively using purrr.

- Create a tibble containing column called centers that go from 1 to 30
- Add a column named k_means with the kmeans_mapper() output. Use mutate() to add the column and map() to map centers to the kmeans_mapper() function.
- Add a column named glance with the glance() output. Use mutate() and map() again to iterate over the column of k_means.
- Save the output as k_means_mapped_tbl

```
# Use purrr to map
k_means_mapped_tbl <- tibble(centers = 1:30) %>%
  mutate(k_means = centers %>% map(kmeans_mapper)) %>%
  mutate(glance = k_means %>% map(glance))
k_means_mapped_tbl
```

```
## # A tibble: 30 x 3
##
      centers k_means glance
##
        <int> <list>
                      t>
##
           1 <kmeans> <tibble [1 x 4]>
  1
           2 <kmeans> <tibble [1 x 4]>
## 2
## 3
           3 <kmeans> <tibble [1 x 4]>
           4 < means > < tibble [1 x 4] >
## 4
##
  5
           5 <kmeans> <tibble [1 x 4]>
##
           6 <kmeans> <tibble [1 x 4]>
##
  7
           7 <kmeans> <tibble [1 x 4]>
## 8
           8 <kmeans> <tibble [1 x 4]>
           9 <kmeans> <tibble [1 x 4]>
## 9
          10 <kmeans> <tibble [1 x 4]>
## # ... with 20 more rows
```

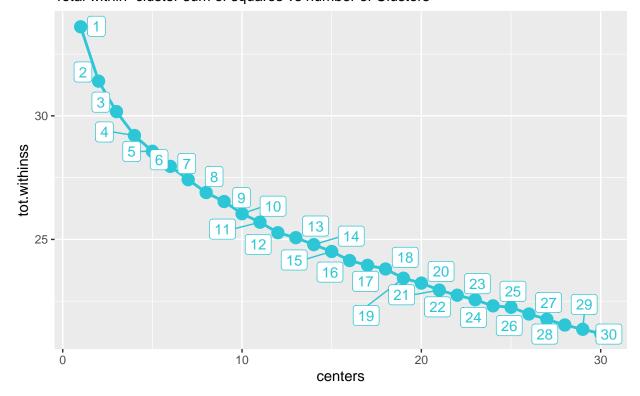
```
# Output: k_means_mapped_tbl
```

Next, let's visualize the "tot.withinss" from the glance output as a *Scree Plot*.

- Begin with the k_means_mapped_tbl
- Unnest the glance column
- Plot the centers column (x-axis) versus the tot.withinss column (y-axis) using geom_point() and geom_line()

• Add a title "Scree Plot" and feel free to style it with your favorite theme

Skree Plot Total within-cluster sum of squares vs number of Clusters



We can see that the Scree Plot becomes linear (constant rate of change) between 5 and 10 centers for K.

Step 5 - Apply UMAP

Next, let's plot the UMAP 2D visualization to help us investigate cluster assignments.

We're going to import the correct results first (just in case you were not able to complete the last step).

```
k_means_mapped_tbl <- read_rds("k_means_mapped_tbl.rds")</pre>
```

First, let's apply the umap() function to the stock_date_matrix_tbl, which contains our user-item matrix in tibble format.

- Start with stock_date_matrix_tbl
- De-select the symbol column
- Use the umap() function storing the output as umap_results

```
# Apply UMAP
umap_results <- stock_date_matrix_tbl %>% select(-symbol) %>% umap()
umap_results
# Store results as: umap_results
```

Next, we want to combine the layout from the umap_results with the symbol column from the stock_date_matrix_tbl.

- Start with umap_results\$layout
- Convert from a matrix data type to a tibble with as_tibble()
- Bind the columns of the umap tibble with the symbol column from the stock_date_matrix_tbl.
- Save the results as umap_results_tbl.

```
# Convert umap results to tibble with symbols
umap_results_tbl <- umap_results$layout %>%
   as_tibble(.name_repair = "unique") %>% # argument is required to set names in the next step
   set_names(c("x", "y")) %>%
   bind_cols(
     stock_date_matrix_tbl %>% select(symbol)
   )

umap_results_tbl
```

```
## # A tibble: 502 x 3
##
                y symbol
         X
##
      <dbl> <dbl> <chr>
## 1 -0.648 2.04 A
##
   2 1.50 0.329 AAL
## 3 -0.118 -0.319 AAP
  4 - 1.14
            3.20 AAPL
## 5 -1.71
            0.264 ABBV
## 6 -1.22 -0.437 ABC
## 7 -1.80 3.25 ABMD
## 8 -0.910 1.78 ABT
## 9 -1.33
            1.83 ACN
## 10 -1.46
            3.54 ADBE
## # ... with 492 more rows
```

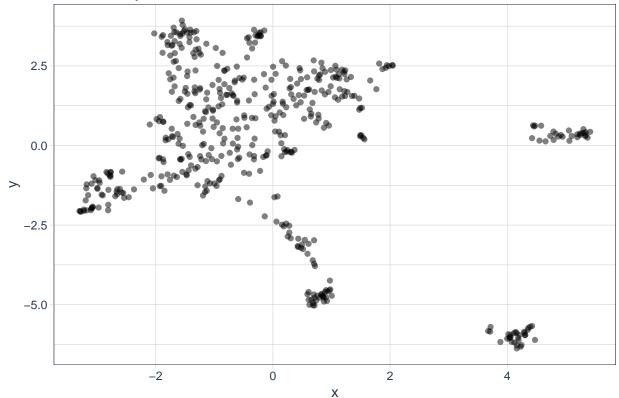
```
# Output: umap_results_tbl
```

Finally, let's make a quick visualization of the umap_results_tbl.

- Pipe the umap_results_tbl into ggplot() mapping the columns to x-axis and y-axis
- Add a geom_point() geometry with an alpha = 0.5
- Apply theme_tq() and add a title "UMAP Projection"

```
# Visualize UMAP results
umap_results_tbl %>%
    ggplot(aes(x, y)) +
    geom_point(alpha= 0.5) +
# Formatting
    labs(title = "UMAP Projection ") +
    theme_tq()
```

UMAP Projection



We can now see that we have some clusters. However, we still need to combine the K-Means clusters and the UMAP 2D representation.

Step 6 - Combine K-Means and UMAP

Next, we combine the K-Means clusters and the UMAP 2D representation

We're going to import the correct results first (just in case you were not able to complete the last step).

```
k_means_mapped_tbl <- read_rds("k_means_mapped_tbl.rds")
umap_results_tbl <- read_rds("umap_results_tbl.rds")</pre>
```

First, pull out the K-Means for 10 Centers. Use this since beyond this value the Scree Plot flattens. Have a look at the business case to recall how that works.

Next, we'll combine the clusters from the k_means_obj with the umap_results_tbl.

- Begin with the k_means_obj
- Augment the k_means_obj with the stock_date_matrix_tbl to get the clusters added to the end of the tibble
- Select just the symbol and .cluster columns
- Left join the result with the umap_results_tbl by the symbol column
- Left join the result with the result of sp_500_index_tbl %>% select(symbol, company, sector) by the symbol column.
- Store the output as umap_kmeans_results_tbl

```
# Use your dplyr & broom skills to combine the k_means_obj with the umap_results_tbl
umap_kmeans_results_tbl <- k_means_obj%>%
                          augment(stock_date_matrix_tbl) %>%
                          # Select the data we need
                         select(symbol, .cluster)
umap_kmeans_results_tbl <- umap_kmeans_results_tbl %>%
                            left join(umap results tbl)%>%
                            left_join(sp_500_index_tbl %>% select(symbol, company, sector))
umap kmeans results tbl
## # A tibble: 502 x 6
##
     symbol .cluster
                          V1
                                  V2 company
                                                               sector
      <chr> <fct>
##
                              <dbl> <chr>
                                                               <chr>>
                       <dbl>
## 1 A
                     -0.764
                            1.65
                                     Agilent Technologies Inc. Health Care
            7
## 2 AAL
            2
                     -2.70
                              0.455 American Airlines Group ~ Industrials
## 3 AAP
            10
                     0.739 -0.0320 Advance Auto Parts Inc.
                                                               Consumer Discretio~
## 4 AAPL
                      0.0130 3.09
                                     Apple Inc.
                                                               Information Techno~
            9
## 5 ABBV
            7
                     -0.965 -0.0193 AbbVie Inc.
                                                               Health Care
## 6 ABC
                     -0.506 -0.659 AmerisourceBergen Corpor~ Health Care
            5
## 7 ABMD
            9
                      0.436
                              3.10 ABIOMED Inc.
                                                               Health Care
## 8 ABT
            7
                              1.35
                                     Abbott Laboratories
                                                               Health Care
                     -0.262
## 9 ACN
            7
                      0.0598 1.63
                                    Accenture Plc Class A
                                                               Information Techno~
## 10 ADBE
                              3.43 Adobe Inc.
                                                               Information Techno~
            9
                      0.570
## # ... with 492 more rows
```

```
# Output: umap_kmeans_results_tbl
```

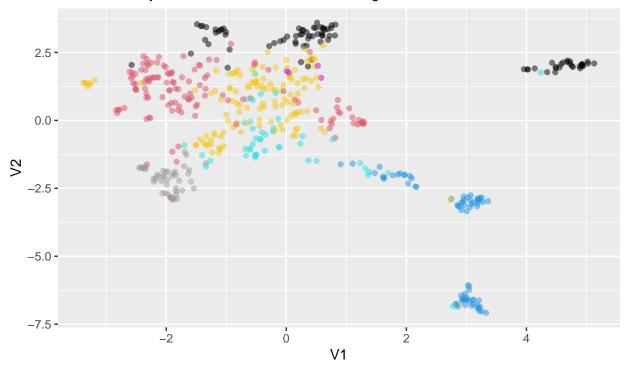
Plot the K-Means and UMAP results.

- Begin with the umap_kmeans_results_tbl
- Use ggplot() mapping V1, V2 and color = .cluster
- Add the geom_point() geometry with alpha = 0.5

• Apply colors as you desire (e.g. scale_color_manual(values = palette_light() %>% rep(3)))

Stock segmentation

UMAP 2D Projection with K-Means Cluster Assignment



Conclusion: 10 Customer Segments identified using 2 algorithms

Congratulations! You are done with the 1st challenge!