

The Equi7 Grid – V13

Grid and Tiling Definition Document – Issue 0.2

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Document History

Issue	Date	Author	Changes
0.1	2015-03-16	Bernhard Bauer-M.	adopted for Equi7 V13
0.2	2015-04-07	Bernhard Bauer-M.	included Pixel Locating

0 Preamble

Content of Document

This document describes the design, realisation and software of the Equi7 Grid. This grid was developed at the Department of Geodesy and Geoinformation at the TU Wien is aimed to use for high resolution remote sensing data.

Scientific Basis

Detailed information on the scientific background is published under:

B. Bauer-Marschallinger, D. Sabel, W. Wagner: Optimisation of global grids for high-resolution remote sensing data. Computers & Geosciences, 72 (2014), 84 - 93, DOI: 10.1016/j.cageo.2014.07.005

<http://www.sciencedirect.com/science/article/pii/S0098300414001629>

Acknowledgements

This work is the result from efforts spent during ongoing developments carried out at TU Wien across a number of projects and by various staff members. In the coarse of these developments of data processing and handling capacities, profound expertise on spatial referencing of remote sensing data was built up at the TU Wien group. Thanks to FFG, time was found to craft this design document. The major work on the scientific background was carried out in the *Soil Moisture Data Cubes* project. Rendering the grid operational was done in the *Prepare4EODC-Water* project.

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1 Overview

1.1 Rationale

Upcoming remote sensing systems onboard satellites will generate unprecedented volumes of spatial data, hence challenging processing facilities in terms of storage and processing capacities. Thus, an efficient handling of remote sensing data is of vital importance, demanding a well-suited definition of spatial grids for the data's storage and manipulation. With a suitable grid definition, one can cut down processing time, hard disk volumes, and signal distortions stemming from geometric manipulations.

For high-resolution image data, regular grids defined by map projections have been identified as practicable, cognisant of their drawbacks due to geometric distortions. The Equi7 Grid uses the Azimuthal Equidistant Projection that minimises those distortions in the sense of remote sensing and raster imagery.

Further information on the scientific aspect of grid definitions and their suitability to high resolution remote sensing can be found in Bauer-Marschallinger et al. (2014).

1.2 Key Facts

The Equi7 Grid is a spatial reference system for the entire Earth and consists of seven planar subgrids for each continent (Figure 1). The coordinates are defined by individual realisations of the Equidistant Azimuthal projection and are referenced to the ellipsoidal WGS84 datum. The Equi7 Grid is designed to handle efficiently the archiving, processing and display of high resolution remote sensing data.

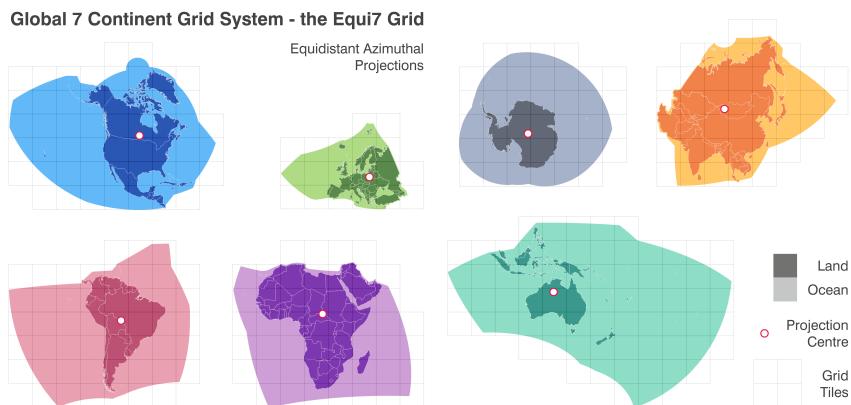


Figure 1: The Equi7 Grid: Schematic images of the (already projected) continental zones with grid tiles and projection centres.

2 Design and Geometry

2.1 Datum

As spatial reference the WGS84-ellipsoid (World Geodetic System 1984) was chosen for the ellipsoidal coordinates on the Earth's surface. These are necessary for the addressing of locations in the global perspective, e.g. during the assignment of satellite scenes to the subgrids. Here the ellipsoid's metrics:

Table 1: The WGS84 Ellipsoid parameters

Major Axis a	6378137m
Flattening f	298.257223563 ⁻¹
Prime Meridian	0.0°
Unit	0.0174532925199433°

2.2 Zones

The Equi7 Grid is a regular grid which defines each location implicitly with a fixed sampling distance relative to a set of linear axis; here two orthogonal ones. As opposed to a single grid for the whole globe, Equi7 separates the globe into seven subgrids (zones) of identical type of projection. Reducing the extent of a projected grid (in respect to the Earth curvature) reduces negative effects from geometric distortions, like data oversampling or disordered pixel neighbour relationships.

Considering findings of the study of (Bauer-Marschallinger et al., 2014), and with TU-Wien's processor- and user requirements in mind, the zone borders were optimised by following requirements:

1. Landmasses should form compact entities
2. Borders should be preferably over oceans
3. Countries should preferably be not split

The seven grids cover the Earth entirely without gap and with 50km overlap over land borders. A global overview of the delineation is shown in Figure 2.

The zones are defined by manually created shapefiles following above rules 1-3 in the WGS84 space. After transformation to the individual projections (see Section 2.3), zone borders over land are buffered to a 50km extent to allow correct spatial filter operations also on the zone limits. Table 2 lists the zones' basic facts.

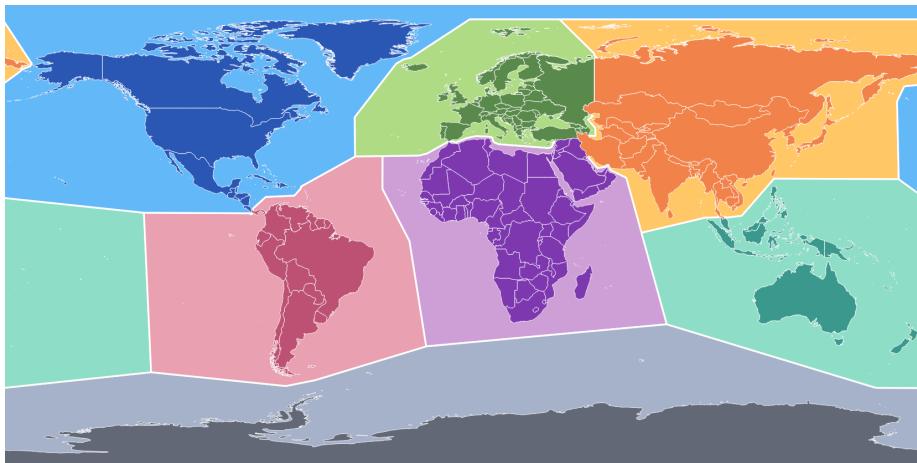


Figure 2: Continental zone partitioning into the seven subgrids, projected for global overview to the Plate Carrée (aka geographic aka Lat-Lon, using WGS84 coordinates).

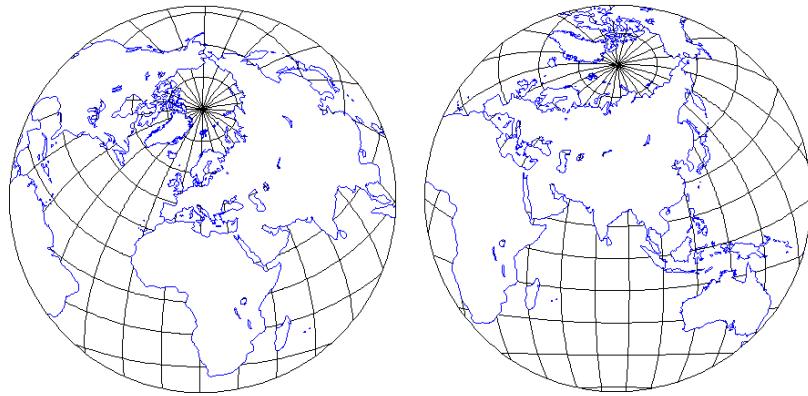
Table 2: The Equi7 Grid zones.

Zone	Short Name	Colour	Covered Land Area [Mio. km ²]
North America	NA	blue	24.2
Europe	EU	green	9.7
Asia	AS	orange	38.6
South America	SA	red	17.9
Africa	AF	purple	33.6
Oceania	OC	turquoise	11.2
Antarctica	AN	gray	12.3

2.3 Projections

All seven zone are projected from ellipsoidal coordinates (lat/lon) in WGS84 to planar grids using the *Equidistant Azimuthal Projection*. Figure 3 exemplifies the projection in oblique aspects.

2.3.1 The Azimuthal Equidistant



*Figure 3: The Azimuthal Equidistant Projection in oblique aspect centred over Austria (left) and Nepal (right). Linear scales emanating from the projection centre are undis-
torted. Distortion of angles and areas increases with distance to the centre.*

The calculation of the planar coordinates x and y (the *forward projection*) implies the solving of the *inverse geodesic problem*, that is

$$dx = c \sin Az \quad (1)$$

$$dy = c \cos Az \quad (2)$$

$$x = dx + FE \quad (3)$$

$$y = dy + FN \quad (4)$$

where x and y the are location's Easting and Northing, c is the length and Az is the azimuth from north of the geodesic line between the location and the projection centre (ϕ_0, λ_0) , FE the false Easting, and FN the false Northing. The *inverse projection* from planar to ellipsoidal coordinates (geodetic latitude ϕ and longitude λ) depicts the *direct geodetic problem* and starts with the determination of Az and c :

$$dx = x - FE \quad (5)$$

$$dy = y - FN \quad (6)$$

$$Az = \arctan \frac{dy}{dx} \quad (7)$$

$$c = \sqrt{dx^2 + dy^2} \quad (8)$$

Both, the forward and inverse projection of the ellipsoid involve the solving of elliptic integrals that are favourably computed with numerical methods. Snyder (1987) gives approximating formulae and general information on the projection. However, these formulae lead to significant geometric inaccuracies in areas far from the projection centre. Thus, a more recent approach following findings of (Karney, 2011, 2013) is selected for the transformation between geographical and projected coordinates (degrees and metres; see Section 3.1).

2.3.2 Equi7 Projections

The parameters of the Azimuthal Equidistant have been individually optimised in means of minimising data oversampling estimated by the mean *grid oversampling factor* as described in Bauer-Marschallinger et al. (2014). The optimised parameters for each zone are listed in Table 3. For Antarctica, the South Pole is conveniently chosen as origin, since it is almost co-located with the optimal origin and the additional error is insignificant. False Easting and -Northing are set so that negative coordinates are avoided.

Table 3: The Equi7 Grid projection parameters for the Azimuthal Equidistant. With λ_0 as central meridian and ϕ_0 as latitude of origin.

Parameter Zone / Unit	λ_0 $^{\circ}E$	ϕ_0 $^{\circ}N$	False Easting m	False Northing m
North America	-111.0	47.5	8264722.18	4867518.35
Europe	24.0	53.0	5837287.82	2121415.70
Asia	94.0	47.0	4340913.85	4812712.92
South America	-60.5	-14.0	7257179.24	5592024.45
Africa	21.5	8.5	5621452.02	5990638.42
Oceania	131.5	-19.5	6988408.54	7654884.54
Antarctica	0.0	-90.0	3714266.98	3402016.51

The individual *Well-Known-Text*-strings giving the full georeference information are the following:

America

```
PROJCS["Azimuthal_Equidistant",GEOGCS["GCS_WGS_1984",DATUM["D_WGS_1984",
SPHEROID["WGS_1984",6378137.0,298.257223563]],PRIMEM["Greenwich
```

```
",0.0],UNIT["Degree",0.0174532925199433]],PROJECTION["  
Azimuthal_Equidistant"],PARAMETER["false_easting",8264722.17686],  
PARAMETER["false_northing",4867518.35323],PARAMETER["  
central_meridian",-97.5],PARAMETER["latitude_of_origin",52.0],UNIT["  
Meter",1.0]]
```

Europe

```
PROJCS["Azimuthal_Equidistant",GEOGCS["GCS_WGS_1984",DATUM["D_WGS_1984",  
SPHEROID["WGS_1984",6378137.0,298.257223563]],PRIMEM["Greenwich  
,0.0],UNIT["Degree",0.0174532925199433]],PROJECTION["  
Azimuthal_Equidistant"],PARAMETER["false_easting",5837287.81977],  
PARAMETER["false_northing",2121415.69617],PARAMETER["  
central_meridian",24.0],PARAMETER["latitude_of_origin",53.0],UNIT["  
Meter",1.0]]
```

Asia

```
PROJCS["Azimuthal_Equidistant",GEOGCS["GCS_WGS_1984",DATUM["D_WGS_1984",  
SPHEROID["WGS_1984",6378137.0,298.257223563]],PRIMEM["Greenwich  
,0.0],UNIT["Degree",0.0174532925199433]],PROJECTION["  
Azimuthal_Equidistant"],PARAMETER["false_easting",4340913.84808],  
PARAMETER["false_northing",4812712.92347],PARAMETER["  
central_meridian",94.0],PARAMETER["latitude_of_origin",47.0],UNIT["  
Meter",1.0]]
```

South America

```
PROJCS["Azimuthal_Equidistant",GEOGCS["GCS_WGS_1984",DATUM["D_WGS_1984",  
SPHEROID["WGS_1984",6378137.0,298.257223563]],PRIMEM["Greenwich  
,0.0],UNIT["Degree",0.0174532925199433]],PROJECTION["  
Azimuthal_Equidistant"],PARAMETER["false_easting",7257179.23559],  
PARAMETER["false_northing",5592024.44605],PARAMETER["  
central_meridian",-60.5],PARAMETER["latitude_of_origin",-14.0],UNIT  
["Meter",1.0]]
```

Africa

```
PROJCS["Azimuthal_Equidistant",GEOGCS["GCS_WGS_1984",DATUM["D_WGS_1984",
SPHEROID["WGS_1984",6378137.0,298.257223563]],PRIMEM["Greenwich
",0.0],UNIT["Degree",0.0174532925199433]],PROJECTION[
"Azimuthal_Equidistant"],PARAMETER["false_easting",5621452.01998],
PARAMETER["false_northing",5990638.42298],PARAMETER[
"central_meridian",21.5],PARAMETER["latitude_of_origin",8.5],UNIT[
"Meter",1.0]]
```

Oceania

```
PROJCS["Azimuthal_Equidistant",GEOGCS["GCS_WGS_1984",DATUM["D_WGS_1984",
SPHEROID["WGS_1984",6378137.0,298.257223563]],PRIMEM["Greenwich
",0.0],UNIT["Degree",0.0174532925199433]],PROJECTION[
"Azimuthal_Equidistant"],PARAMETER["false_easting",5621452.01998],
PARAMETER["false_northing",5990638.42298],PARAMETER[
"central_meridian",21.5],PARAMETER["latitude_of_origin",8.5],UNIT[
"Meter",1.0]]
```

Antarctica

```
PROJCS["Azimuthal_Equidistant",GEOGCS["GCS_WGS_1984",DATUM["D_WGS_1984",
SPHEROID["WGS_1984",6378137.0,298.257223563]],PRIMEM["Greenwich
",0.0],UNIT["Degree",0.0174532925199433]],PROJECTION[
"Azimuthal_Equidistant"],PARAMETER["false_easting",3714266.97719],
PARAMETER["false_northing",3402016.50625],PARAMETER[
"central_meridian",0.0],PARAMETER["latitude_of_origin",-90.0],UNIT[
"Meter",1.0]]
```

2.4 Tiling

The seven planar grid zones are independently divided into square tiles. Point of reference is *LowerLeft* – for the tile numbering as well as for the grid coordinates. Figure 5 explains the principles of the tiling system, whereas Figure 4 illustrates them on the example of the Africa grid. Please note the projection centre that coincide with the centre of land area (indicated as white dot).

Tiles are defined in squares that are (partially) overlapping with the grid zone. Consequently, there are sections of tiles that are not defined by the individual grid zone but are actually covering area that is in realm of the neighbouring continent grid zone (bright orange areas in Fig. 4).

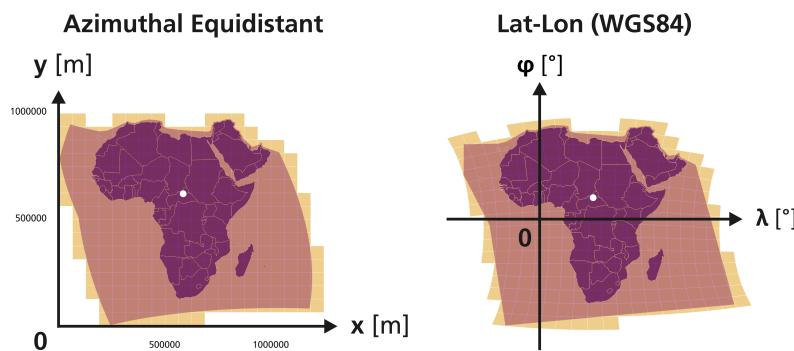


Figure 4: Realisation of the Equi7 grid tiling on the example of the African grid, displayed in the Equi7- and geographic space. Please note the different shapes of the tiles and boundaries. The white dot indicates the centre of origin of the Azimuthal Equidistant projection.

Tiling Levels

The Equi7 Grid V13 features multiple levels of tilings, meeting the different requirements during processing images of low and high spatial resolution and data volumes. By reducing the tile extent, the number of pixels per tiled image remains operable even at high resolutions. This setup ensures also that the different levels are mutually aligning and congruent.

In version 13, three levels have been chosen for low, medium and high resolution spatial data. Table 4 lists basic characteristics of these tiling levels **T6**, **T3**, and **T1**:

Shapefile Tile Naming

As evident from Fig. 5, the tiles are not ordinary numbered but named after the coordinates of the lower left corner:

Table 4: The Equi7 Grid Tiling Levels for different target samplings.

Tiling Level Code	T6	T3	T1
Tile Extents	600km	300km	100km
Typical Pixel Sampling	500m / 75m	40m	10m / 5m
Samples (1 Axis)	1200 / 8000	7500	10000 / 20000

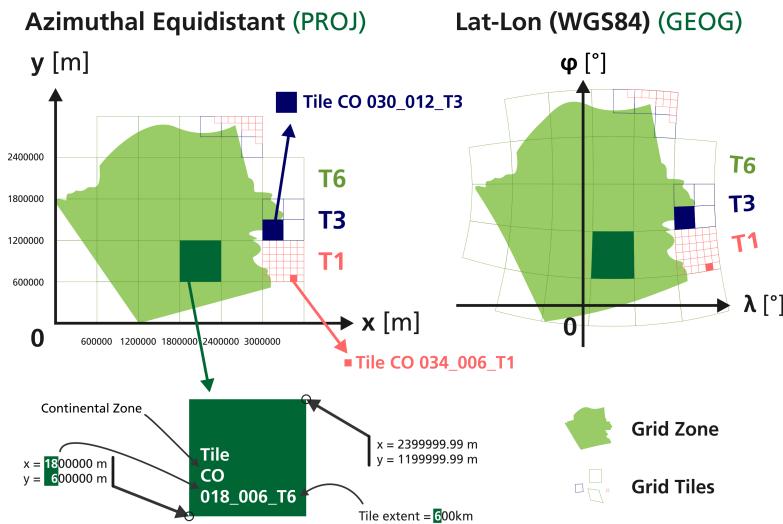


Figure 5: Schematic relationship of the Equi7 subgrids (left, folder name PROJ) and the geographic Lat-Lon coordinate system (right, folder name GEOOG). With exemplary tile namings in green, blue and orange for T6, T3, and T1 tile layer, respectively. CO is a placeholder for the grid continent's acronym as in Tab. 2.

Unique Tilename = E7G co eee_nnn Tt

E7G = Equi7 Grid

co = continental zone acronym

eee = Easting lower left corner

nnn = Northing lower left corner

Tt = tile extent

And as example:

Tilename = E7G AF 018_006 T6

Tiling Statistics

When it comes to the design of data processing engines, the number of tiles and furthermore the number of tiles covering land surfaces are of special interest. Table 5 summarises these statistics.

Table 5: Statistics of Tiling Levels in comparison to Earth's surface area as from Wikipedia. Displaying, per Tiling Level, the number of total tiles, tiles over land and the total area of all tiles and corresponding ratios.

	Area Total	Area Land	% Land
Wikipedia - Earth surface area [km²]	510072000	148940000	29%
Zone	Tiles Total	Tiles Land	% Land
Tiling Level T6			
AF	266	147	55%
AN	213	68	32%
AS	228	168	74%
EU	94	61	65%
NA	286	132	46%
OC	429	170	40%
SA	273	86	32%
WORLD	1789	832	47%
Total Tile Area [km ²]	644040000	299520000	
Ratio to Area from Wikipedia	126%	201%	
Tiling Level T3			
AF	1004	487	49%
AN	792	211	27%
AS	829	592	71%
EU	340	196	58%
NA	1065	438	41%
OC	1611	397	25%
SA	1009	273	27%
WORLD	6650	2594	39%
Total Tile Area [km ²]	598500000	233460000	
Ratio to Area from Wikipedia	117%	157%	
Tiling Level T1			
AF	8603	3788	44%
AN	6793	1504	22%
AS	7089	4504	64%
EU	2823	1341	48%
NA	9185	3149	34%
OC	13830	1966	14%
SA	8645	2051	24%
WORLD	56968	18303	32%
Total Tile Area [km ²]	569680000	183030000	
Ratio to Area from Wikipedia	112%	123%	

2.5 Pixel Locating and Indexing

The Equi7 Grid relates locations on the Earth with points defined in a set of planar subgrids. As dealing with satellite imagery, the location of image pixels with an areal extent must be efficiently handled.

In Figure 6, the Equi7 point location rules are schematically displayed. It shows exemplary how to relate location to the projected subgrids and to the tiles.

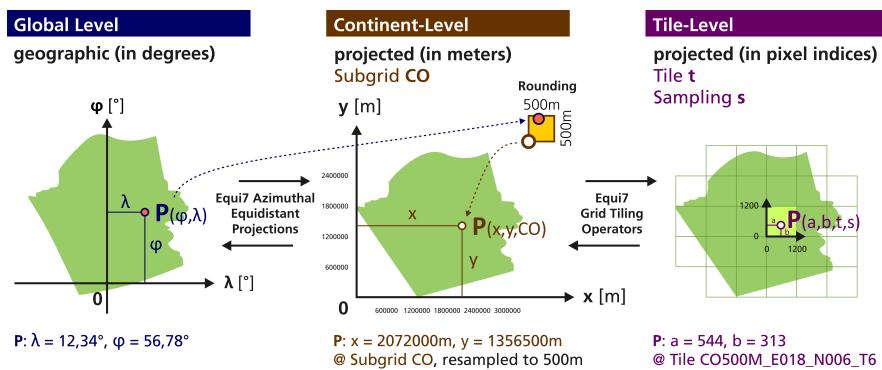


Figure 6: Schematic relationship of locations on the globe, in the Equi7 subgrids and Equi7 tiles. Below, for each level a coordinate example is given.

The following sections describe the transformation from geographic to projected to tiled. The inverse is then trivial and not described.

From Geographic to Projected

All locations on the globe should have a representation in the Equi7 Grid. Completeness is given by the Equi7 Grid, but not uniqueness in the globe-to-grid projection: Theoretically, every location can be described by all seven continental subgrids. But practically, only locations in the overlapping land areas are described by more than one subgrid. So, for some land areas, one geographic location can have two or three representations in the Equi7.

In the Equi7-Grid, the continental zone of a pixel's location is determined. Then, its projected location in the continental subgrid is calculated. This coordinate transformation from the geographic space in degrees to projected space in meters is done with the Azimuthal Equidistant Projections as defined in Equations 4, 8, and 16. The result is in the unit meters and is geo-referenced at its lower-left corner.

Depending on the pixel sampling s in meters, some coordinate rounding is necessary during coordinate transformation from geographic to projected: After precise coordinate transformation, the closest pixel centre is determined by rounding the yielded x and y :

$$x_{Equi7_CO_subgrid} = (x_{precise} \bmod s) + \frac{s}{2} \quad (9)$$

$$y_{Equi7_CO_subgrid} = (y_{precise} \bmod s) + \frac{s}{2} \quad (10)$$

Since the reference location is the lower left corner, the $\frac{s}{2}$ can be skipped and pixel's coordinate in the Equi7-subgrid is simply then:

$$x_{Equi7_CO_subgrid} = x_{precise} - (x_{precise} \bmod s) \quad (11)$$

$$y_{Equi7_CO_subgrid} = y_{precise} - (y_{precise} \bmod s) \quad (12)$$

To sum up, each location in the continental zone is defined individually by its Easting and Northing in integers of meters, rounded down to the closest lower left pixel corner of the grid's target sampling.

Applying these equations to the example in Figure 6 yields the following:

$$x_{precise} = 2072204m$$

$$y_{precise} = 1356978m$$

$$x_{Equi7_CO_subgrid} = 2072204 - (2072204 \bmod 500) = 2072000m$$

$$y_{Equi7_CO_subgrid} = 1356978 - (1356978 \bmod 500) = 1356500m$$

From Projected to Tiled

The Equi7-Grid Tiling Operators take care of addressing the location of pixels as segment of the Equi7-tiles.

According to Section 2.4, these operators as follows and yield horizontal a and vertical b pixel indices in respect to the overlapping tile (lower-left-indexing):

$$a_{tile} = \frac{x_{Equi7_CO_subgrid} \bmod t_{tile}}{s} \quad (13)$$

$$b_{tile} = \frac{y_{Equi7_CO_subgrid} \bmod t_{tile}}{s} \quad (14)$$

The Tile Extent t_{tile} is in meters and can take on values as listed in Table 4.

Applying these equations to the example in Figure 6 yields the following:

$$a_{tile} = \frac{2072000 \mod 600000}{500} = 544$$

$$b_{tile} = \frac{1356500 \mod 600000}{500} = 313$$

3 Production and Structure

3.1 Projection Implementation

At TU Wien, the Equi7-projections are computed with a python software on a Linux system, using *PROJ.4* via *GDAL/OGR*.

The Equi7 uses a precise algorithm including iterations, as described in Karney (2013), yielding effectively following equation for inverse and direct geodetic problem, here in the python-notation of the *GeographicLib* library:

$$[c, Az] = \text{Geodesic.WGS84.Inverse}(\phi_0, \lambda_0, \phi, \lambda) \quad (15)$$

$$[\phi, \lambda] = \text{Geodesic.WGS84.Direct}(\phi_0, \lambda_0, Az, c) \quad (16)$$

Above formulae (including formulae from Section 2.3) are implemented in a modified version of the *proj-4.8.0* library, replacing the approximating formulae of (Snyder, 1987) in the source code file

`PJ_aeqd.c.`

Those are called via *GDAL/OGR 1.10.0*. The enhancements were reported to the proj.4 project so that it will be included in upcoming releases. In the meantime (Equi7 V12, November 2014), a batch for Linux systems,

`proj-4.8.0_tu_wien_batch.zip`,

is set up to apply all necessary changes to the official release of proj.4. As a note, the resulting Equi7 shapefiles and DEMs are practically identical to results produced with *ArcGIS 10.2* via its Python module *arcpy*.

3.2 Grid Defining Files

The Equi7 Grid Version 13 constitutes of four main components:

- Shapefiles
 - Geometries
- DEM Geotiffs
 - 7 Zone DEMs
 - DEM Tiles
- Code and Seedfiles
 - Generating code
 - Seed shapefiles for zone and country boundaries in WGS84
 - Projection files
- Documentation

Figure 7 displays the file structure and lists all elements of the Equi7 Grid. There are five types of datasets:

Zone Shapefile EQUI7_V13_co_PROJ_ZONE.shp

A (vector-) shapefile determining the outline of the continental subgrids. co holds place for the continent name. proj for the coordinate space.

Tiles Shapefile EQUI7_V13_co_PROJ_TILE_Tt.shp

A (vector-) shapefile carrying the outline of the zone's tiles.

Land Shapefile EQUI7_V13_co_PROJ_LAND.shp

A (vector-) shapefile describing the country borders as provided by the *TM_WORLD_BORDERS-0.3*.

Zone DEM File EQUI7_V13_GT30S_co_rrrM_NOTTILED.tif

A geotiff carrying the GTOPO30SRTM DEM for the entire continental zone as one piece. In combination with the letter M, rrr holds place for the sampling in metres; with K, in kilometres.

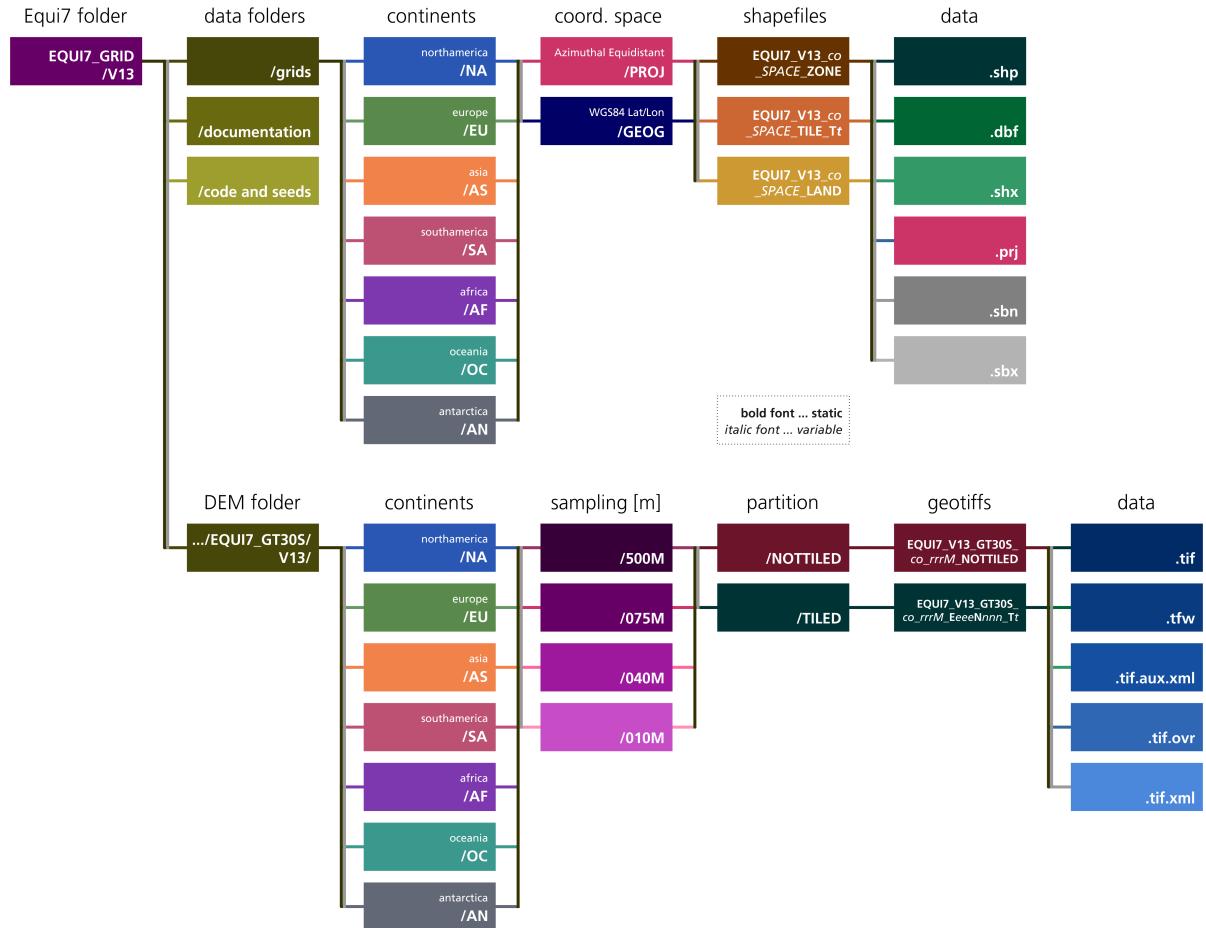


Figure 7: File structure of the Equi7 Grid Version 13. Documentation and code- and seed-files are not displayed. co is a placeholder for the continent's name; SPACE for the coordinate space (PROJ = Azimuthal Equidistant; GEOG = geographic/ellipsoidal); rrrM for the sampling in metres; rrrK for the sampling in kilometres; eee for the Easting; nnn the Northing in 10 kilometres; t for the tile extent in 100 kilometres.

Tile DEM File EQUI7_V13_GT30S_co_rrrM_EeeeNnnn.tif

A geotiff carrying the GTOPO30SRTM DEM for the individual tile. co holds place for the continent acronym; eee for the Easting of the lower left pixel; and nnn for the Northing; in 10000 metres. In combination with the letter M, rrr holds place for the sampling in metres; with K, in kilometres.

4 Usage

Apart from directly using the Equi7-projected Zone/Tile shapefiles and DEM geotiffs, a python class object named Equi7Grid is created, providing several functionalities for using it in the python processing environment.

4.1 The Equi7Grid Class

`get_grid_zone_aeqd(grid)`

returns an geometry object which represents the zone of the given grid system in azimuthal equidistant distance projection.

`get_grid_zone_wgs84(grid)`

returns an geometry object which represents the zone of the given grid system in lat/lon projections

`get_projection(grid)`

returns the projection of the given grid system in WKT formation.

`identify_grid(area)`

returns the overlapped grid IDs.

`identify_tile(grid, location, res)`

returns the tile name.

`get_tile_extent(tile_name)`

returns the extent of the tile in the terms of $[minX, minY, maxX, maxY]$.

`create_dummy_dataset(tile, filename, datatype, frmt="GTiff", options)`

creates a GDAL dataset object for the given tile.

`search_tiles(area, area_proj, grids, res)`

searches the tiles which are intersected by the polygon ROI area.

```
resample(image, res, output_dir, outshortname, compress, resampling_type,  
tile_nodata)
```

resamples an image to tiles.

5 Glossary

General Terms

Pixel A pixel is a square segment of a raster image, carrying a value.

Alignment is the property of a pixel point in level n also being a pixel point in level $n + 1$

Congruency is the capability of decomposing a tile of level n into smaller cells of level $n + 1$.

An **ellipsoid** is a closed surface formed by the rotation of an ellipse about its shorter (minor) axis.

A **coordinate system** (CS) is a set of rules to define how coordinates are assigned to points, usually by means of associated axes.

A **geographic coordinate system** (GCS) is a CS describing the location on the Earth by a set of coordinates, usually geographic latitude and longitude.

An **ellipsoidal coordinate system** (ECS) is a CS specified by geodetic latitude and longitude on an ellipsoid.

Height is the distance to a reference surface along a line perpendicular to that surface.

A **meridian** is the intersection of an ellipsoid by a plane containing the short axis of the ellipsoid.

Geodetic latitude is the angle from the equatorial plane to the perpendicular to the ellipsoid through a given point.

Geodetic longitude is the angle from the prime meridian plane to the meridian plane of a given point.

A **coordinate reference system** (CRS) is a CS that defines position, scale and orientation of its axes defined with respect to an object, which for our purposes is the Earth.

A **datum** is the information that is required to fix a CS to an object. In general terms, a datum positions and orientates a CS to turn it into a CRS.

A **geodetic datum** defines the relationship of a two or three dimensional CS to the Earth. It further defines the position of the origin, the scale, and the orientation of the axes of an ECS with respect to a particular Earth ellipsoid. For global applications, the World Geodetic System (WGS 84) is commonly used.

A **geodetic coordinate reference system** (GCRS) is an ECS defined for a particular geodetic datum.

A **coordinate conversion** is a change of coordinates from one CRS to another, in which the CRSs are either based on the same datum or, if they are based on different datums, no algorithm has been applied to transform the coordinates from one datum to the other.

A **coordinate transformation** is a change of coordinates from one CRS to another in which the CRSs are based on different datums. In this case, a coordinate transformation algorithm is applied to convert the coordinates of one CRS to conform to the datum of the other CRS.

In general, a **map projection** is a set of mathematical functions that transform geographic locations on the sphere or ellipsoid to a plane, the map. All maps distort the surface in some manner during transformation. A map projection depicts a coordinate conversion from an ECS to a plane. It is defined by various projection parameters, including the projection ellipsoid, the ECS coordinates of the projection origin in the plane, the orientation of the projected axes in the plane with respect to the ECS, and other projection-specific parameters.

A **projected coordinate reference system** (PCRS) is a CRS derived from a GCRS by applying a specified map projection. Note that the projection ellipsoid specified in the map projection may or may not match the datum specified in the GCRS.

Northing is the distance in a CS, positive northwards and negative southwards along an east-west reference line.

Easting is the distance in a CS, positive eastwards and negative westwards along an north-south reference line.

Equi7 Nomenclature

The complete definition of the spatial referencing by means of the Equi7 is called the **Equi7 Grid**.

A **continental zone** is the part of the Earth assigned to a individual continent.

The Equi7 Grid distinguishes between the ellipsoidal **geographic space** in geodetic latitude and longitude and the planar **projected space** in metres defined for each continental zone.

A **subgrid** is orthogonal axis system for each continental zone.

A **tile** is a square part of a subgrid named after 1) the continental zone, 2) the location of its lower left corner, and 3) the tiling level.

The **tiling level** describes the tiles' extent.

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