GEM

A finite element mesh generator and data preparation program for radiation transport and fluids codes

User Notes

by

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1. Introduction

These notes give basic information on the use of the program **GEM**. The program is an interactive preprocessor for the radiation transport code **EVENT**. Its main task is to prepare the finite element mesh for the problem while at the same time incorporating the physical properties. The input specifies the problem by regions to filled with specified element type and specified material and source. The output is a list of elements, nodal coordinates and other items in the format required by **EVENT**. Though primarily designed for generating two-dimensional meshes, **GEM** is also capable of preparing input for one-dimensional problems, and has a limited capability for generating three-dimensional meshes.

2. Using GEM

2.1 Input commands

Input to **GEM** is given using simple free-format commands which are executed one at a time. The first character string on an input instruction is assumed to be a keyword. Subsequent strings may comprise of reserved words, names or numerical values.

The commands may be grouped into the following categories:

GEOMETRY
MESHING
MATERIAL SPECIFICATION
I/O
GRAPHICAL OUTPUT
GENERAL
EVENT RUN

Examples of commands are:

POINT P1 0.0 0.0 ; defines a point with name P1 and x- and y-coordinates (0.0,0.0) MATERIAL MA11 1.0 0.0 0.0 0.0 1.0 ; defines cross-sectional data for material MA1 READ fred ; read command sequence from file fred

The full list of commands available and their syntax is presented in section 2.4.

2.2 Command sequence

A sequence of input commands should be constructed for each problem. This sequence should essentially:

- (i) describe the geometry of the problem in terms of simple natural geometrical objects such as points, lines and regions;
- (ii) define physical parameters such as material x/s, sources and boundary conditions, and associate them to the geometrical model;
- (iii) define main control parameters for the EVENT run;
- (iv) define mesh control parameters and generate mesh;
- (v) generate output data.

Steps (i) and (ii) are obligatory and represent the bulk of the command sequence preparation work. Step (iii) may be omitted but default values are used then. Step (iv) usually involves some experimentation with mesh

parameters in order to achieve the best compromise between effort and accuracy. This is best done interactively. Step (v) is only required if the objective of the **GEM** run is to produce an **EVENT** data file.

2.3 Command rules

(i) Keywords

The first word on cards other than comment or blank cards is the instruction keyword. The keyword is terminated by a blank, and only the first three characters are significant.

(ii) Reserved words

Further words are used in instruction parameters. These are up to six characters significant.

- (iii) Keywords and reserved words may be input in lower or uppercase. The rest of the input is case sensitive.
- (iv) Names

Identifiers for points, lines, regions, materials, and sources may be made up of any characters except *. All characters are significant in identifiers. Use of reserved words and keywords for identifiers should be avoided.

- (v) The instructions occupy one line or more line or "cards" of input.
- (vi) The character ^ indicates that the next card is a continuation card.
- (vii) Blank cards, or lines beginning with @ are ignored.

2.4 **GEM commands**

In what follows words in bold and upper case are keywords or reserved words.

{	}	denotes synonym
[]	denotes optional parameters.
	denotes	s a list of parameters of any length.

2.4.1 Geometry

DELETE	item list (not operational)								
	deletes items in the list								
	Example: DELETE R1								
LINE	$lnam p_1 p_2 [p_3] [p_n]$								
	declares a line joining point p_1 to point p_2 , with name $lnam$.								
	If p_3 is included, the line is an arc centered on p_3 . If more than four points are named then a spline is fitted through the points.								
	Examples: LINE L1 P1 P2 LINE L10 P15 P16 P3								
	N.B. Convention is anti-clockwise, i.e. when moving from p_1 to p_2 .								
MOVE	pntnam x y z								
	moves point <i>pntnam</i> to new co-ordinates (x,y,z)								
	Example: MOVE P1 10.0 20.0								
POLYGON	polynam 11 12 13 ln								
	defines a <i>n</i> -sided polygonal region								
CIRCLE	circnam p1 r n								
	defines a circular region centered at point $p1$ and radius r. The 4 quadrant circular arcs are subdivided into n intervals								

RECTANGLE	rectnam	pΙ	l	h	n		
	defines a rectanguheight <i>h</i> . The 4 sid				ttom left-corner at point $p1$ and length l and intervals		
HEXAGON	hexnam p1p	n					
	defines an hexago subdivided into <i>n</i>			red at po	pint $p1$ and pitch p The 6 sides are		
POINT {PNT}	pntnam	x-coord	d	y-coore	d z-coord		
	declares a point with name pntnam and co-ordinates (x,y,z)						
	Example: POINT P1 0.0 0.0 0.0						
REGION	regnam regnam regnam	l _I r _I p _I	l ₂ r ₂ p ₂		[14]		
	defines a three-, four-sided or many-sided region with name regnam.						
	Examples :	REGIO REGIO	ON	R1 R6 R4	L1 L2 L3 L10 L5 L20 L21 R1 R6		

2.4.2 Meshing

DEFAULT keyword value default value for lines, material, average and source Example: **DEFAULT** ITV 10 **DEFAULT** MATERIAL MA1 **DEFAULT** AVERAGE 1 **DEFAULT** SOURCE S1 DIVIDE linelist n lines in linelist are to be divided into n intervals Example: DIVIDE 10 L1 L2 L3 L4 **FILL** fills up lines and regions with nodes and elements. Effect is cancelled by command **INTERVALS** lnam [ratio] n $\{ITV\}$ line lnam is to be divided into n intervals (with an optional common ratio which defaults to 1). Example: **INTERVALS** L1 10 Default n for lines not appearing on interval cards is n = 1. Overrides previous INTERVAL cards for same line.

MESH regnam f_1 [f_2]

region regnam is to be filled according to parameters f_I and f_2 . Overrides previous mesh cards for same region. Permitted values for f_I are (see Fig. 1):

NONE no mesh for region

SKEW1

SKEW2 for 4 -sided regions

SKEW? QUAD

TRIANGLE for 3-sided regions

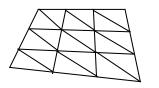
FRONT for n-sided regions

DELAUNAY

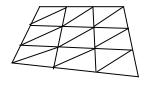
Permitted values for f2 are: **BLEND** (default)

UNIFORM

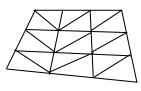
Example: MESH R1 SKEW1 BLEND
MESH R2 TRIANGLE BLEND



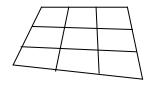
(a) skew1



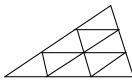
(b) skew2



(c) skew?



(d) quad



(e) triangle

Fig. 1 Region Element Fill Types

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2.4.3 Material Specification and Boundary Conditions

AVERAGE *n* reglist.....

assign regions in reglist to EVENT integrating region n,

Example: AVERAGE 1 R1 R2 R3

BOUNDARY type *linlist......*

 $\{BC\}$ $\{t\}$

t }

the lines in linlist are associated either with boundary conditions of the specified type, or with surface conditions with surface source t.

Permitted types are:

REFLECTOR

BARE ZERO

PERIODIC

Bare and surface source lines are filled with 'surface' elements.

Examples: **BOUNDARY BARE**L1

BOUNDARY REFLECTOR L3

LIBRARY libnam [format]

defines name and format of library from where **GEM** will read material parameters.

Permitted values for format are: **EVENT**

FIDO LASL

Examples: LIBRARY cask

MATERIAL [x/s....]matnam defines a material with name matnam and given cross-section list. The expected order is σ_{tg} , σ_{ag} , $\nu\sigma_{tg}$, and $\sigma_{sgg'}$, g'=g, NGRPS for energy group g. Example: **MATERIAL** MA1 1.0 0.5 0.2 0.0 0.5 **PROPERTY** regnam matnam[S]region regnam is given material matnam (and source S if present) regnam, matnam and S must have been previously declared. Example: PROPERTY R1 MA1 S1 **SOURCE** S [strength] **{VOLUME}** defines a volume source with name S and given strength. Example: **SOURCE** S1 1.0 **SURFACE** T[strength] defines a surface source with name T and given strength. Example: **SURFACE** S2 0.3 VELOCITY v **{SPEED}** particle speeds. Example: **VELOCITY** 8.0E+9 4.0E+9 **SPECTRUM** x fission spectrum

Example: **SPECTRUM** 0.7 0.2 0.15 0.05

XSTAB	iht	ihs	ihm
	materi	al x/s table	e positions and length

2.4.4 Input/Output

DATA	[file] outputs present mesh data to given file (default is last opened file or file GEMOUT), as required by program EVENT .				
	If file has been opened the output is appended. If file does not exist it is created.				
РАТН	[IN] pathnam [OUT]				
	assigns input or output to path pathnam.				
	Examples: PATH IN C:\FEMPN\FRED\GEMDATA PATH OUT C:\FEMPN\FRED\EVENTDAT				
READ	filenam				
	instructions are to be read from <i>filenam</i> until exhausted, when input is next attempted from the terminal. A blank file name redirects input to terminal.				
	Example: READ fred				
CLOSE	[file]				
	closes current input channel				
	Example: CLOSE				

REWIND channel no.

rewinds file or channel no.

Example: **REWIND** 10

WRITE [channel no.]

output is directed to the new channel no. until the next WRITE card. A blank channel

no. redirects output to terminal.

Example: **REWIND** 21

2.4.5 Graphical output

DEVICE device

initiates, or re-initiates, graphical output device.

The following are allowed: X11

PS4

PS4C PS3

TEK

SHOW items

selected items are plotted on the device last specified by the **DEVICE** card.

Possible items are :- ALL

LINES

NODES

ELEMENTS

DOMAINS

COLOURS

FLUXES

A new picture is started for each item.

2.4.6 General

HELP [keyword] invokes help facility. Example: **HELP LIST** LIST items selected items are listed on the current output channel. Possible items are: -**ALL ELEMENTS EVENT LINES MATERIALS NODES POINTS REGIONS SOURCES** or **VOLUME SURFACE** Examples: LIST ELEMENTS LIST ALL **NEWS** RENUMBER [DUG] renumber nodes to reduce matrix half-bandwidth to minimum. **RESET** [**ALL**]

and MESH cards, and possibly extension of the mesh by new PNT, LINE

A RESET card causes all mesh filling to be forgotten, to allow modifications to

and

ITV

REGION cards.

finishes the session

2.4.7 EVENT Control Parameters

TITLE	title					
	specifies a title of up to 76 coutput	characters for lineprinter and graphical				
PRINT	item					
	EVENT print option.					
	Options are :- NONE FLUXE MOME ALL					
PLOT	option					
	EVENT plot option.					
	Options are :- NONE FLUXE MOME ALL					

GRAPH option

graphical output device in EVENT run

Options are :- **NOGRAPH**

PS4C PS4C X11

CASE case

EVENT run case.

Options are :- **TEST**

EIGENVALUE

FIXED TIME

GEOMETRY geom

problem geometry.

Possible geometries are :- SLAB

SPHERICAL CYLINDRICAL

XY RZ XYZ

MODE mode

problem solution mode

Options are :- FORWARD {DIRECT}

ADJOINT BOTH

SOLUTION	scheme
	Solution scheme
	Options are :- PCG2 PCG4

ITERATIONS list eigenvalue calculation parameters. Parameters in list are: max. no. of outer iterations **MAXITS** MAXCG max. no. of pcg iterations **EIGTOL** eigenvalue error tolerance VECTOL eigenvector error tolerance TIME list time zone card containing list of control parameters Parameters in list are:-**NSTEPS** no. of time steps time-step size **DELTAT** TIMSCH time integration scheme angular card flag **NEWSCT NEWGRP** energy card flag mesh cards flag NEWMSH **NEWMIX** mixing cards flag material cards flag **NEWDAT NEWSRC** source cards flag ANGLE n {MSCTR} order of angular approximation **{PN} SCATTER** n {NSCTR} order of scattering anisotropy **GROUPS** ngrps no. of energy groups.

COLLAPSE	n list		
	collapse energy gr	oup structure to	n broad groups with structure given by list
LUMP	option		
	lumping approxim	ation of source	
	Options are :-	NONE ODD ALL	
UPSCATTER	flag		
	upscatter flag		
	Flag options are :-	NO YES	
FORMAT	format		
	material data form	at.	
	Options are :-	EVENT LASL FIDO	
MIXTURE	[mixnum mixing instruction	mixcom	mixden]
	mang madaction	S TOT ET TEITE.	

COMMENTS option

Insert **GEM** run output as comments in **EVENT** data file

Options are :- NO

YES

3. A worked example

The basic concepts concerning the use of **GEM** are best illustrated through a worked example. Consider the problem described in Fig.1 which we wish to solve with **EVENT**. The **GEM** file is constructed as follows:

(i) define geometry (see Fig. 2):

(a)

```
(a)
@ - points
(a)
PNT P1 0.0 0.0
PNT P2 5.0025714 0.0
                       @ nb. radius corrected to preserve volume
PNT P3 10.0 0.0
PNT P4 0.0 5.0025714
PNT P5 3.5373522 3.5373522
PNT P6 10.0 5.0
PNT P7 0.0 10.0
PNT P8 5.0 10.0
PNT P9 10.0 10.0
@ - lines
(a)
LINE L1 P1 P2
LINE L2 P2 P3
LINE L3 P1 P4
LINE L4 P1 P5
                         @ arc of circle
LINE L5 P2 P5 P1
LINE L6 P3 P6
LINE L7 P5 P4 P1
                         @ arc of circle
LINE L8 P5 P6
LINE L9 P4 P7
LINE L10 P5 P8
LINE L11 P6 P9
LINE L12 P7 P8
LINE L13 P8 P9
(a)
@ - regions
(a)
REGION R1 L1 L5 L4
REGION R2 L4 L7 L3
REGION R3 L2 L6 L8 L5
REGION R4 L7 L10 L12 L9
REGION R5 L8 L11 L13 L10
@ - regional averages
AVERAGE 1 R1 R2
AVERAGE 2 R3 R4 R5
```

(ii) - define ph	ysical properties of probl	lem:	
	@ MAT MA1 0.5 0.1 0.0 MAT MA2 1.0 0.9990 @ @ - sources @ SOURCE S1 1.0 SOURCE S2 0.0 @ @ - boundary condition @ BOUNDARY BARE I BOUNDARY REFLEC	0.0 0.0 0.0010 ns .6 L11 L12 L13	@ highly absorbing medium
(iii) - assign m	aterial properties and sou	arces to regions	:
	@ PROPERTIES R1 MA PROPERTIES R2 MA PROPERTIES R3 MA PROPERTIES R4 MA PROPERTIES R5 MA @	1 S1 2 S2 2 S2	
(iv) - define E	VENT run control param	neters:	
	@ TITLE Case 1 : 5.0 cm CASE FIXED GEOMETRY RZ ANGLE 7 GROUPS 1 COMMENTS NO @	@ fixed-source@ r-z geometry@ P7 expansio@ one energy	y on of the angular flux
(v) - define me	esh control parameters an	nd generate mesh	1:
	@ - define type of fill f @ MESH R1 TRIANG B! MESH R2 TRIANG B! MESH R3 QUAD BLE MESH R4 QUAD BLE MESH R5 QUAD BLE @ - line subdivisons @ DIVIDE 4 L1 L3 L4 I @ DIVIDE 4 L2 L8 L9 I @	LEND LEND END END END L5 L6 L7 L12	 @ these lines must have same no. of intervals @ ditto

```
@ - fill regions
```

<u>a</u>

FILL

<u>a</u>

(vi) - generate data:

DATA

(vii) - end run:

@ STOP

(a)

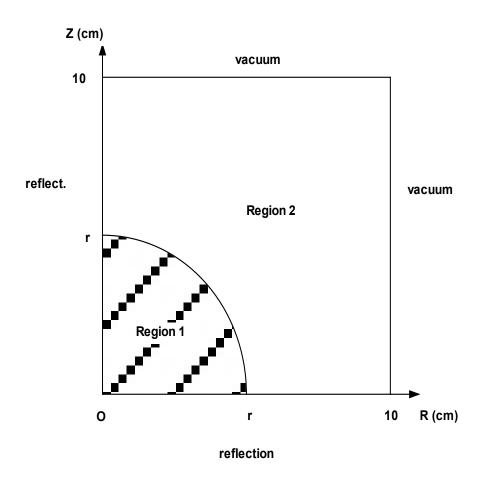
The resulting **EVENT** data file is:

Case 1 : 5.0 c	m sphere	embedded	in 10	Ocm x	10cm	cyl.	(4×4	mesh)
I/O	0 0	2 0	0	0	0			
CASE	3 5	0 4	0	0	0			
ITER 2	5 25 9	9.9999997	E-06	9.999	9997E	-05	2	
ANGLE	7 0	0						
ENERGY	1 0	0 0						
MESHFILE /hom	e/users/s	staff/cas	siano,	EVENT	!/data	/exmp	12	
SIZES 1	3 4	2 96	81	17	0	0	0	
MATFILE /hom	e/users/s	staff/cas	siano,	EVENT	!/data	/exmp	12	EVENT
MATXS	2 0	4 3	4	4	0			
NCOM	0							
ELEM 1	2 6	1 0	3	25				
ELEM 2	2 6	1 0	25	26				
ELEM 3	2 6	1 0	26	27				
ELEM 4	2 6	1 0	27	6				
ELEM 5	2 11	1 0	6	40				
ELEM 6	2 11	1 0	40	41				
ELEM 7	2 11	1 0	41	42				
ELEM 8	2 11	1 0	42	9				
ELEM 9	2 12	1 0	7	43				
ELEM 10	2 12	1 0	43	44				
ELEM 11	2 12	1 0	44	45				
ELEM 12	2 12	1 0	45	8				
ELEM 13	2 13	1 0	8	46				
ELEM 14	2 13	1 0	46	47				
ELEM 15	2 13	1 0	47	48				
ELEM 16	2 13	1 0	48	9				
ELEM 17	1 1	1 1	1	10	19			
ELEM 18	1 1	1 1	10	49	19			
ELEM 19	1 1	1 1	10	11	49			
ELEM 20	1 1	1 1	11	50	49			
ELEM 21	1 1	1 1	11	12	50			
ELEM 22	1 1	1 1	12	22	50			
ELEM 23	1 1	1 1	12	2	22			
ELEM 24	1 1	1 1	19	49	20			
ELEM 25	1 1	1 1	49	51	20			
ELEM 26	1 1	1 1	49	50	51			
ELEM 27	1 1	1 1	50	23	51			
ELEM 28	1 1	1 1	50	22	23			

ELEM	29	1	1	1	1	20	51	21	
ELEM	30	1	1	1	1	51	24	21	
ELEM	31	1	1	1	1	51	23	24	
ELEM	32	1	1	1	1	21	24	5	
ELEM	33	1	1	1	1	1	19	16	
ELEM	34	1	1	1	1	19	52	16	
ELEM	35	1	1	1	1	19	20	52	
ELEM	36	1	1	1	1	20	53	52	
ELEM	37	1	1	1	1	20	21	53	
ELEM	38	1	1	1	1	21	28	53	
ELEM	39	1	1	1	1	21	5	28	
ELEM	40	1	1	1	1	16	52	17	
ELEM	41	1	1	1	1	52	54	17	
ELEM	42	1	1	1	1	52	53	54	
ELEM	43	1	1	1	1	53	29	54	
ELEM	44	1	1	1	1	53	28	29	
ELEM	45	1	1	1	1	17	54	18	
ELEM	46	1	1	1	1	54	30	18	
ELEM	47	1	1	1	1	54	29	30	
ELEM	48	1	1	1	1	18	30	4	
ELEM	49	11	2	2	2	2	13	22	55
ELEM	50	11	2	2	2	13	14	55	56
ELEM	51	11	2	2	2	14	15	56	57
ELEM	52	11	2	2	2	15	3	57	25
ELEM	53	11	2	2	2	22	55	23	58
ELEM	54	11	2	2	2	55	56	58	59
ELEM	55	11	2	2	2	56	57	59	60
ELEM	56	11	2	2	2	57	25	60	26
ELEM	57	11	2	2	2	23	58	24	61
ELEM	58	11	2	2	2	58	59	61	62
ELEM	59	11	2	2	2	59	60	62	63
ELEM	60	11	2	2	2	60	26	63	27
ELEM	61	11	2	2	2	24	61	5	31
ELEM	62	11	2	2	2	61	62	31	32
ELEM	63	11	2	2	2	62	63	32	33
ELEM	64	11	2	2	2	63	27	33	6
ELEM	65	11	2	2	2	4	30	34	64
ELEM	66	11	2	2	2	30	29	64	65
ELEM	67	11	2	2	2	29	28	65	66
ELEM	68	11	2	2	2	28	5	66	37
ELEM	69	11	2	2	2	34	64	35	67
		11	2	2	2		65		
ELEM	70					64		67	68
ELEM	71	11	2	2	2	65	66	68	69
ELEM	72	11	2	2	2	66	37	69	38
ELEM	73	11	2	2	2	35	67	36	70
ELEM	74	11	2	2	2	67	68	70	71
ELEM	75	11	2	2	2	68	69	71	72
ELEM	76	11	2	2	2	69	38	72	39
ELEM	77	11	2	2	2	36	70	7	43
ELEM	78	11	2	2	2	70	71	43	44
ELEM	79	11	2	2	2	71	72	44	45
ELEM	80	11	2	2	2	72	39	45	8
ELEM	81	11	2	2	2	5	31	37	73
ELEM	82	11	2	2	2	31	32	73	74
ELEM	83	11	2	2	2	32	33	74	75
ELEM	84	11	2	2	2	33	6	75	40
ELEM	85	11	2	2	2	37	73	38	76
ELEM	86	11	2	2	2	73	74	76	77
ELEM	87	11	2	2	2	74	75	77	78
ELEM	88	11	2	2	2	75	40	78	41
الالمسيد	00	11	۷	۷	۷	15	- U	10	4 T

```
ELEM
        89
             11
                   2
                         2
                              2
                                  38
                                        76
                                             39
                                                  79
ELEM
        90
             11
                    2
                         2
                              2
                                  76
                                        77
                                             79
                                                  80
ELEM
        91
             11
                    2
                         2
                              2
                                  77
                                        78
                                             80
                                                  81
ELEM
        92
             11
                    2
                         2
                              2
                                  78
                                        41
                                             81
                                                  42
ELEM
        93
             11
                    2
                         2
                              2
                                  39
                                        79
                                              8
                                                  46
                              2
                                  79
        94
             11
                    2
                         2
                                        80
                                             46
                                                  47
ELEM
                              2
ELEM
        95
             11
                    2
                         2
                                  80
                                        81
                                             47
                                                  48
ELEM
        96
             11
                    2
                         2
                              2
                                  81
                                        42
                                             48
                                                   9
NODE
         1
            0.000000E+00
                            0.000000E+00
                                            0.000000E+00
                                                             3.5
         2
            5.0025716E+00
                            0.000000E+00
                                            0.000000E+00
NODE
                                                              1
            1.000000E+01
                            0.000000E+00
                                            0.000000E+00
NODE
                                                             31
            0.000000E+00
                            5.0025716E+00
                                            0.000000E+00
NODE
         4
                                                             81
         5
            3.5373521E+00
                            3.5373521E+00
                                            0.000000E+00
NODE
                                                             29
NODE
         6
            1.000000E+01
                            5.0000000E+00
                                            0.000000E+00
                                                             23
NODE
         7
            0.000000E+00
                            1.0000000E+01
                                            0.000000E+00
                                                             77
         8
            5.0000000E+00
                            1.0000000E+01
                                            0.000000E+00
NODE
                                                             7.3
NODE
         9
            1.0000000E+01
                            1.0000000E+01
                                            0.000000E+00
                                                             69
                                            0.000000E+00
NODE
            1.2506429E+00
                            0.000000E+00
                                                             22
            2.5012858E+00
                            0.000000E+00
                                            0.000000E+00
                                                             12
NODE
        11
            3.7519288E+00
NODE
        12
                            0.000000E+00
                                            0.000000E+00
                                                              5
            6.2519288E+00
                            0.000000E+00
                                            0.000000E+00
                                                              3
NODE
        13
NODE
        14
            7.5012856E+00
                            0.0000000E+00
                                            0.000000E+00
                                                             10
            8.7506428E+00 0.0000000E+00
NODE
        15
                                            0.000000E+00
                                                             2.0
            0.0000000E+00 1.2506429E+00
                                            0.000000E+00
NODE
                                                             45
NODE
        17
            0.000000E+00
                           2.5012858E+00
                                            0.000000E+00
                                                             56
NODE
        18
            0.000000E+00
                            3.7519288E+00
                                            0.000000E+00
                                                             68
NODE
        19
            8.8433802E-01
                            8.8433802E-01
                                            0.000000E+00
                                                             34
NODE
        2.0
            1.7686760E+00
                            1.7686760E+00
                                            0.000000E+00
                                                             33
NODE
        2.1
            2.6530142E+00
                            2.6530142E+00
                                            0.000000E+00
                                                             32
NODE
        22
            4.9064484E+00
                           9.7595328E-01
                                            0.000000E+00
                                                              4
NODE
            4.6217732E+00
                            1.9144014E+00
                                            0.000000E+00
                                                              8
        24
            4.1594863E+00
                            2.7792799E+00
                                            0.000000E+00
                                                             18
NODE
NODE
        25
            1.0000000E+01
                            1.2500000E+00
                                            0.000000E+00
                                                             30
            1.0000000E+01
                            2.5000000E+00
                                            0.000000E+00
                                                             27
NODE
        26
NODE
        27
            1.0000000E+01
                            3.7500000E+00
                                            0.000000E+00
                                                             26
            2.7792795E+00 4.1594863E+00
NODE
        28
                                            0.000000E+00
                                                             42
            1.9144011E+00 4.6217728E+00
                                            0.000000E+00
NODE
                                                             54
            9.7595274E-01
                            4.9064484E+00
                                            0.000000E+00
NODE
        30
                                                             67
                            3.9030142E+00
            5.1530142E+00
                                            0.000000E+00
NODE
        31
                                                             2.8
NODE
        32
            6.7686758E+00
                            4.2686758E+00
                                            0.000000E+00
                                                             25
NODE
        33
            8.3843384E+00
                            4.6343379E+00
                                            0.000000E+00
            0.000000E+00
                            6.2519288E+00
                                            0.000000E+00
                                                             80
NODE
        34
NODE
        35
            0.000000E+00
                            7.5012856E+00
                                            0.000000E+00
                                                             79
NODE
            0.000000E+00
                            8.7506428E+00
                                            0.000000E+00
                                                             78
NODE
        37
            3.9030142E+00
                            5.1530142E+00
                                            0.000000E+00
                                                             40
                            6.7686758E+00
                                            0.000000E+00
NODE
        38
            4.2686758E+00
                                                             50
NODE
        39
            4.6343379E+00
                            8.3843384E+00
                                            0.000000E+00
                                                             61
            1.0000000E+01
                            6.2500000E+00
NODE
        40
                                            0.000000E+00
                                                             37
NODE
        41
            1.0000000E+01
                            7.5000000E+00
                                            0.000000E+00
                                                             46
            1.0000000E+01
                           8.7500000E+00
                                            0.000000E+00
NODE
                                                             58
                                                             76
            1.2500000E+00
                            1.0000000E+01
                                            0.000000E+00
NODE
        43
            2.5000000E+00
                            1.0000000E+01
                                            0.000000E+00
                                                             75
NODE
        44
NODE
        45
            3.7500000E+00
                            1.000000E+01
                                            0.000000E+00
                                                             74
NODE
        46
            6.2500000E+00
                            1.0000000E+01
                                            0.000000E+00
                                                             72
        47
            7.5000000E+00
                            1.0000000E+01
                                            0.000000E+00
                                                             71
NODE
NODE
        48
            8.7500000E+00
                            1.0000000E+01
                                            0.000000E+00
                                                             70
                            9.5720041E-01
NODE
        49
            2.3108866E+00
                                            0.000000E+00
                                                             21
                            9.7107112E-01
NODE
        50
            3.6240845E+00
                                            0.000000E+00
                                                             11
NODE
        51
            3.2492657E+00
                           1.8759646E+00
                                            0.000000E+00
                                                             19
NODE
        52
            9.5720017E-01 2.3108866E+00
                                            0.000000E+00
                                                             44
```

```
NODE
        53 1.8759630E+00 3.2492661E+00 0.0000000E+00
                                                         4.3
NODE
        54
           9.7106898E-01
                          3.6240849E+00 0.0000000E+00
                                                         55
NODE
        55 6.1798358E+00 1.0444648E+00 0.000000E+00
                                                          2
NODE
        56 7.4532242E+00 1.1129766E+00 0.0000000E+00
                                                          9
NODE
        57 8.7266121E+00 1.1814882E+00 0.0000000E+00
                                                         17
       58 5.9663296E+00 2.0608010E+00 0.0000000E+00
                                                         7
NODE
           7.3108869E+00 2.2072005E+00 0.0000000E+00
NODE
        59
                                                         6
NODE
        60 8.6554441E+00 2.3536003E+00 0.0000000E+00
                                                         16
NODE
        61
           5.6196151E+00 3.0219603E+00 0.0000000E+00
                                                         15
        62 7.0797420E+00 3.2646394E+00 0.0000000E+00
NODE
                                                        14
NODE
        63 8.5398703E+00 3.5073197E+00 0.0000000E+00
        64 1.0444651E+00 6.1798368E+00 0.0000000E+00
NODE
                                                         66
        65 2.0608010E+00 5.9663305E+00 0.0000000E+00
NODE
                                                         5.3
NODE
        66 3.0219603E+00 5.6196151E+00
                                         0.000000E+00
                                                         41
NODE
        67
           1.1129768E+00
                          7.4532242E+00
                                         0.000000E+00
                                                         65
NODE
        68
           2.2072005E+00 7.3108869E+00 0.000000E+00
                                                         52
NODE
        69 3.2646394E+00 7.0797429E+00 0.0000000E+00
                                                         51
       70 1.1814884E+00 8.7266121E+00 0.0000000E+00
NODE
                                                         64
       71 2.3536003E+00 8.6554441E+00 0.000000E+00
                                                         63
NODE
       72 3.5073197E+00 8.5398703E+00 0.0000000E+00
NODE
                                                         62
NODE
        73 5.4272604E+00 5.4272604E+00 0.0000000E+00
                                                         39
NODE
       74
           6.9515061E+00 5.7015061E+00 0.0000000E+00
                                                         38
       75 8.4757538E+00 5.9757538E+00 0.0000000E+00
NODE
                                                         36
NODE
       76 5.7015061E+00 6.9515061E+00 0.0000000E+00
                                                         49
NODE
       77 7.1343379E+00 7.1343379E+00 0.0000000E+00
                                                         48
       78 8.5671692E+00 7.3171692E+00 0.0000000E+00
NODE
                                                         47
NODE
        79 5.9757538E+00 8.4757538E+00
                                        0.000000E+00
                                                         60
           7.3171692E+00 8.5671692E+00 0.0000000E+00
NODE
        80
                                                         59
           8.6585846E+00 8.6585846E+00 0.0000000E+00
NODE
        81
                                                         57
CONS
        1
             1
                 11
CONS
        2
             2
                  6
        3
             3
                  6
CONS
CONS
        4
             4
                 11
CONS
        5
             7
                 11
CONS
        6
            10
                  6
        7
CONS
            11
                  6
CONS
        8
            12
                  6
CONS
        9
            13
                  6
                  6
CONS
       10
            14
CONS
       11
            15
                  6
CONS
       12
            16
                 11
       13
            17
                 11
CONS
CONS
       14
           18
                 11
       15
CONS
           34
                 11
CONS
       16 35
                 11
           36
CONS
       17
                 11
            5.0000001E-01 1.0000000E-01 0.0000000E+00 0.0000000E+00
MA1
MA1
           4.0000002E-01
MA2
           1.0000000E+00 9.9900001E-01 0.0000000E+00 0.0000000E+00
           1.000000E-03
S1
           1.000000E+00
S2.
           0.000000E+00
```



Problem Definition:

- single energy group
- the equation solved is:

$$\boldsymbol{\Omega}.\boldsymbol{\nabla}\,\boldsymbol{\psi}+\boldsymbol{\sigma}_t\,\boldsymbol{\psi}=\boldsymbol{S}+\frac{\boldsymbol{\sigma}_s}{4\pi}\int_{4\pi}\!d\boldsymbol{\Omega}'\,\boldsymbol{\psi}(\boldsymbol{\Omega}')$$

- source S = 1 in in sphere and zero elsewhere
- radius r = 5.0 cm
- in the spherical region : $\sigma_t = 0.5$; $\sigma_s = 0.4 \ \sigma_t = 0.1$
- in the external region : $\,\sigma_t$ = 1.0 ; σ_S = 0.999

Fig 1 Sphere embedded in cylinder problem

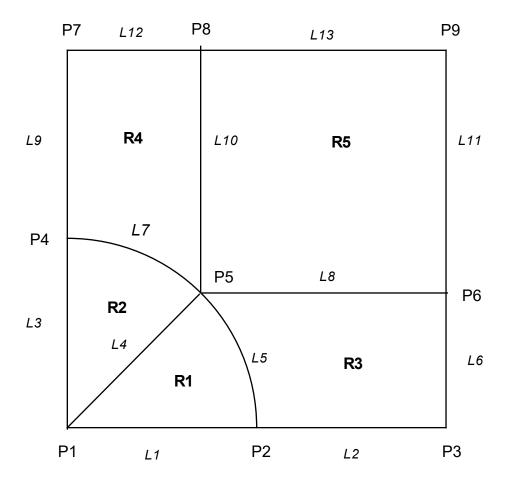


Fig. 2 Geometrical description of sphere embedded in cylinder problem as required by **GEM**