

Physics 158 Formula Sheet

Constants

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|---------------------|--|
| Coulomb's Constant | $k = \frac{1}{4\pi\epsilon_0} \approx 8.988 \times 10^9 \text{ Nm}^2/\text{C}^2$ |
| Electric Constant | $\epsilon_0 = 8.854 \times 10^{-12} \frac{\text{C}^2}{\text{Nm}^2}$ |
| Elementary Charge | $e = 1.602 \times 10^{-19} \text{ C}$ |
| Vacuum Permeability | $\mu_0 = 4\pi \times 10^{-7} \text{ N/A}^2$ |
| Speed of Light | $c = \frac{1}{\sqrt{\epsilon_0\mu_0}} = 2.998 \times 10^8 \text{ m/s}$ |

DC Circuits

Resistor Circuits

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| Ohm's Law | $V = IR$ |
| Power Dissipated | $P = IV = I^2 R = \frac{V^2}{R}$ |
| Resistors in Series | $R_{eq} = R_1 + R_2 + \dots$ |
| Resistors in Parallel | $\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$ |

RC Circuits

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|---------------|------------------------------------|
| Time Constant | $\tau = RC$ |
| Charging | $q(t) = Q_{\max}(1 - e^{-t/\tau})$ |
| Discharging | $q(t) = Q_{\max}e^{-t/\tau}$ |

RL Circuits

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|---------------|-------------------------------|
| Time Constant | $\tau = \frac{L}{R}$ |
| Charging | $i(t) = I_0(1 - e^{-t/\tau})$ |
| Discharging | $i(t) = I_0e^{-t/\tau}$ |

RLC Circuits

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| Time Constant | $\tau = \frac{2L}{R}$ |
| Resonance Frequency | $\omega_0 = \frac{1}{\sqrt{LC}}$ |
| Frequency | $\omega = \sqrt{\omega_0^2 - \frac{R^2}{4L^2}}$ |
| Charge | $q(t) = Q_{\max}e^{-t/\tau} \cos(\omega t + \phi)$ |

AC Circuits

Reactance and Impedance

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|-----------------------|-------------------------------|
| Capacitor Reactance | $X_C = \frac{1}{\omega C}$ |
| Capacitor Voltage | $V_C = X_C I$ |
| Inductor Reactance | $X_L = \omega L$ |
| Inductor Voltage | $V_L = X_L I$ |
| Impedance (in Series) | $ Z ^2 = R^2 + (X_L - X_C)^2$ |
| Voltage | $V = IZ$ |

Phase Angles

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| Phase Angle | $\tan \phi = \frac{X_L - X_C}{R}$ |
| | $\phi = \arg(v) - \arg(i)$ |
| If $v(t) = V_0 \cos(\omega t)$ | then $i(t) = I_{\max} \cos(\omega t - \phi)$ |

Power

| | |
|---------------|---|
| Power Factor | $\cos \phi = \frac{R}{Z}$ |
| Average Power | $P_{\text{avg}} = V_{\text{RMS}} I_{\text{RMS}} \cos \phi = I_{\text{RMS}}^2 R$ |
| RMS Current | $I_{\text{RMS}} = \frac{I_{\max}}{\sqrt{2}}$ |

Capacitors

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|--------------------------|---|
| Capacitance | $C = \frac{Q}{V}$ |
| Stored Energy | $U = \frac{1}{2} CV^2 = \frac{1}{2} \frac{Q^2}{C} = \frac{1}{2} QV$ |
| Capacitors in Series | $\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \dots$ |
| Capacitors in Parallel | $C_{eq} = C_1 + C_2 + \dots$ |
| Parallel Plate Capacitor | $C = \frac{\epsilon_0 A}{d}$ |
| Dielectrics | $C_{\text{dielectric}} = \kappa C_{\text{vacuum}}$ |

Inductors

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|-----------------------|--|
| Self-Induced EMF | $\mathcal{E} = -L \frac{di}{dt}$ |
| Stored Energy | $U = \frac{1}{2} LI^2$ |
| Inductors in Series | $L_{eq} = L_1 + L_2 + \dots$ |
| Inductors in Parallel | $\frac{1}{L_{eq}} = \frac{1}{L_1} + \frac{1}{L_2} + \dots$ |

Solenoids

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|----------------|-------------------------|
| Coil Density | $n = N/L$ |
| Magnetic Field | $B = \mu_0 n I$ |
| Inductance | $L = \frac{N\Phi_B}{I}$ |

Electrostatics

Electric Force

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|---------------|--|
| Coulomb's Law | $ \vec{F} = k \frac{ q_1 q_2 }{r^2} = q \vec{E} $ |
|---------------|--|

Electric Field

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| Gauss's Law | $\oiint_S \vec{E} \cdot d\vec{A} = \frac{Q_{\text{enc}}}{\epsilon_0}$ |
| \vec{E} from Point Charge | $\vec{E} = \frac{kq}{r^2} \hat{r}$ |
| \vec{E} from Charged Rod | $E(h) = \frac{kQ}{h\sqrt{h^2 + a^2}}$ |
| \vec{E} from Charged Ring | $E(z) = \frac{kQz}{(R^2 + h^2)^{3/2}}$ |
| \vec{E} from Charged Disk | $E(z) = \frac{2Qk}{R^2} \left(1 - \frac{z}{\sqrt{z^2 + R^2}} \right)$ |
| \vec{E} from Infinite Sheet | $E(z) = \frac{\sigma}{2\epsilon_0} \hat{n}$ |
| Flux | $\Phi_E = \iint_S \vec{E} \cdot d\vec{A}$ |
| Energy Density | $u_E = \frac{\epsilon_0}{2} E^2$ |

Electric Potential

Potential

| | |
|-------------------------------------|---|
| Difference Notation | $V_{ba} = V_b - V_a$ |
| V from Point Charge | $V = \frac{kq}{r} + \text{Constant}$ |
| Potential Difference from \vec{E} | $V = - \int_a^b \vec{E} \cdot d\vec{l}$ |
| Electric Field from V | $\vec{E} = -\nabla V$ |
| | $E_x = -\frac{dV}{dx}$ |

Potential Energy

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|-------------------------|---|
| Work | $W_{a \rightarrow b} = U_a - U_b = -\Delta U$ |
| Potential Energy from V | $U = qV$ |
| Between Point Charges | $U = \frac{kq_1q_2}{r}$ |

Magnetostatics

Magnetic Force

| | |
|---------------------|--|
| Lorentz Force | $\vec{F} = q\vec{E} + q\vec{v} \times \vec{B}$ |
| Force on Current | $\vec{F} = I\vec{L} \times \vec{B}$ |
| Force Between Wires | $\frac{F}{L} = \frac{\mu_0 I_1 I_2}{2\pi d}$ |

Magnetic Fields

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|-----------------|--|
| Biot-Savart Law | $d\vec{B} = \frac{\mu_0}{4\pi} \frac{I d\vec{l} \times \hat{r}}{r^2}$ |
| Ampere's Law | $\oint_C \vec{B} \cdot d\vec{l} = \mu_0 I_{\text{enc}}$ |
| Loop of Current | $\vec{B} = \frac{\mu_0 I R^2}{2(h^2 + R^2)^{3/2}} \hat{n}$ |
| Straight Wire | $B = \frac{\mu_0 I}{4\pi r} \sin \theta \Big _{\theta_L}^{\theta_R} = \frac{\mu_0 I x}{2\pi r \sqrt{x^2 + r^2}} \Big _{x_L}^{x_R}$ |
| Flux | $\Phi_B = \iint_S \vec{B} \cdot d\vec{A}$ |
| Energy Density | $\frac{1}{2\mu_0} B^2$ |

Torque on Current Loop

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|------------------------|---|
| Torque Vector | $\vec{\tau} = \vec{\mu} \times \vec{B}$ |
| Magnetic Dipole Moment | $\vec{\mu} = NI\vec{A}$ |
| Potential Energy | $U = -\vec{\mu} \cdot \vec{B}$ |

Maxwell's Equations

$$\begin{aligned}\oiint_S \vec{E} \cdot d\vec{A} &= \frac{q_{\text{enc}}}{\epsilon_0} \\ \oiint_S \vec{B} \cdot d\vec{A} &= 0 \\ \oint_C \vec{E} \cdot d\vec{l} &= -\frac{d\Phi_B}{dt} \\ \oint_C \vec{B} \cdot d\vec{l} &= \mu_0 I_{\text{enc}} + \mu_0 \epsilon_0 \frac{d\Phi_E}{dt}\end{aligned}$$

Electromagnetic Induction

$$\begin{aligned}\text{Induced EMF} \quad \mathcal{E} &= -\frac{d\Phi_B}{dt} \\ \text{Motional EMF} \quad \mathcal{E} &= \oint_C (\vec{v} \times \vec{B}) \cdot d\vec{l}\end{aligned}$$

Mechanics

Kinematics

$$\begin{aligned}\text{Linear Motion} \quad x &= x_0 + \frac{1}{2}(v_0 + v)t \\ x &= x_0 + vt + \frac{1}{2}at^2 \\ v &= v_0 + at \\ v^2 &= v_0^2 + 2a(x - x_0) \\ \text{Circular Motion} \quad a_c &= \frac{v^2}{r}\end{aligned}$$

Forces

$$\begin{aligned}\text{Newton's Second Law} \quad \vec{F} &= m\vec{a} = \frac{d\vec{p}}{dt} \\ \text{Spring Force} \quad \vec{F} &= -kx\hat{x} \\ \text{Friction Force} \quad F &= \mu N \\ \text{Damping Force} \quad \vec{F} &= -b\vec{v} \\ \text{Bouyant Force} \quad \vec{F} &= \rho V g\end{aligned}$$

Work and Energy

$$\begin{aligned}\text{Work} \quad W &= \int_{\vec{r}_i}^{\vec{r}_f} \vec{F} \cdot d\vec{r} = \vec{F} \cdot \Delta\vec{r} \\ \text{Kinetic Energy} \quad K &= \frac{1}{2}mv^2 \\ \text{Gravitational Potential} \quad \Delta U_g &= mgy \\ \text{Spring Potential Energy} \quad \Delta U_s &= \frac{1}{2}kx^2 \\ \text{Conservative Forces} \quad \vec{F} &= -\nabla U \\ \text{Power} \quad P &= \frac{dW}{dt} = \vec{F} \cdot \vec{v}\end{aligned}$$

Mathematics

Area and Volume

$$\begin{aligned}\text{Volume of a Sphere} \quad V &= \frac{4}{3}\pi r^3 \\ \text{Volume of a Cylinder} \quad V &= \pi r^2 L \\ \text{Area of a Sphere} \quad A &= 4\pi r^2 \\ \text{Area of a Cylinder} \quad A &= 2\pi r L \\ \text{Area of a Circle} \quad A &= \pi r^2 \\ \text{Circumference of a Circle} \quad C &= 2\pi r\end{aligned}$$

Trigonometry

$$\begin{aligned}\text{Pythagorean Theorem} \quad a^2 + b^2 &= c^2 \\ \text{Arc Length} \quad s &= r\theta \\ \text{Pythagorean Identity} \quad \sin^2 \theta + \cos^2 \theta &= 1 \\ \text{Double Angle} \quad \sin(2\theta) &= 2\sin \theta \cos \theta \\ \cos(2\theta) &= \cos^2 \theta - \sin^2 \theta \\ \text{Half Angle} \quad \sin^2\left(\frac{\theta}{2}\right) &= \frac{1 - \cos \theta}{2} \\ \cos^2\left(\frac{\theta}{2}\right) &= \frac{1 + \cos \theta}{2}\end{aligned}$$

Integrals

$$\int x^n dx = \begin{cases} \frac{x^{n+1}}{n+1} + \text{Constant} & n \neq -1 \\ \ln |x| + \text{Constant} & n = -1 \end{cases}$$

Vectors

$$\text{Dot Product} \quad \vec{a} \cdot \vec{b} = ab \cos \theta$$

$$\text{Cross Product} \quad \|\vec{a} \times \vec{b}\| = ab \sin \theta$$

$$\vec{a} \times \vec{b} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ a_x & a_y & a_z \\ b_x & b_y & b_z \end{vmatrix}$$

Right Hand Rule

