# Deep networks & backpropagation

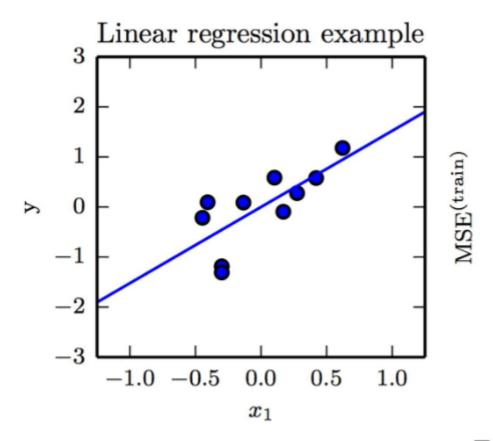
### Learning machines

"A computer program is said to learn from experience E with respect to some class of tasks T and performance measure P, if its performance at tasks in T, as measured by P, improves with experience E." (Mitchell, 1997)

- Task T: e.g., classification, regression, density estimation, etc.
- Performance measure P: e.g., accuracy, error rate
- Experience E: supervised, unsupervised, reinforcement learning

Example: Linear regression!(线性回归)

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$$\hat{y} = \boldsymbol{w}^{\top} \boldsymbol{x}$$

参数介绍:

x:輸入变量

y: 输出变量

w: 权重

b: 偏置项 (当然这个图里没有展示)

Mean squared error: our performance measure

 $P(w,b) = 1/N \sum (y_i - (wx_i + b))^2$ 

#### error/loss 介绍:

#### Training error:

the error/loss computed on the training set

Test error/loss: the error/loss on the test set

Generalization error/loss: the gab between the training error and test error

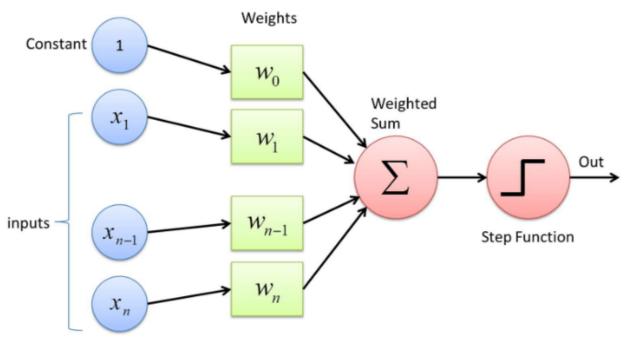
Underfitting(欠拟合) and overfitting (过拟合)

Generalisation (泛化) 与 Capacity (容量) 一句话先记住:容量是模型的"智商",泛化是它"考试"时的得分;智商太高不复习,容易作弊背答案(过拟合),考试一换题库就挂。

Capacity (容量) 抽象说法: 假设空间的大小,即模型能表示的函数集合的"丰富程度"。

Generalisation (泛化): 训练集误差 → 测试集误差的"落差"越小,泛化越好。

#### Perceptron (感知机)



Going deep - Single Hidden Layer (该章节未具体介绍)

Deep neural networks (该章节未具体介绍)

Gradient-based learning: backpropagation (反向传播):核心想,找到最合适的权重使得我的模型的误差最小化。

Cost functions: cross entropy (交叉熵损失函数)

$$L(\tilde{y}) = -\sum_{i=1}^{C} y_i \log \tilde{y}_i \qquad \frac{\partial L}{\partial \tilde{y}_i} = -\frac{y_i}{\tilde{y}_i}$$

记忆: yi是第i个样本的真实值(0/1),yi个是第i个样本的预测值(0~1)(如果默认归一化的话) log(yi个)是一个负数,在前面加上一个符号变为正数

### 三种output:

- 1. Regression: 线性输出
- 2. Binary classification: sigmoid输出 (用于激活函数来着)

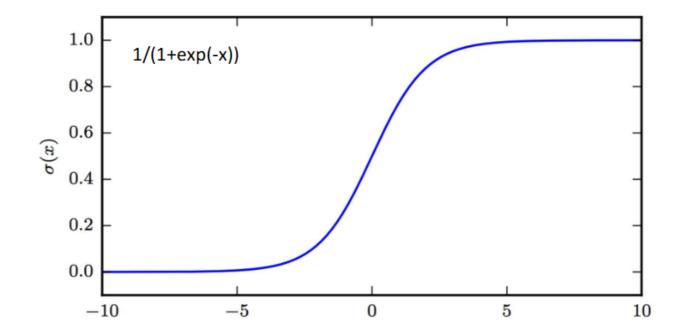


Figure 3.3: The logistic sigmoid function.

3. Multi-class classification: softmax输出 (用于结果的输出)

$$\tilde{y}_i = \operatorname{softmax}(x)_i = \frac{\exp(x_i)}{\sum_j \exp(x_j)}$$

Hidden units (注意梯度的计算公式):

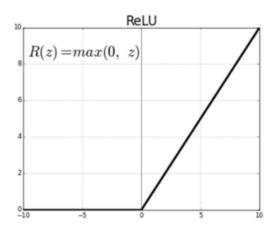
ReLU

- Most popular choice
- Activation

$$a = h(x) = \max(x, 0)$$

Gradient

$$\frac{\partial a}{\partial x} = \begin{cases} 0, & \text{if } x \le 0\\ 1, & \text{if } x > 0 \end{cases}$$



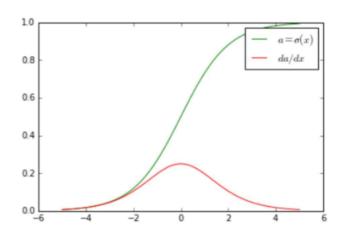
sigmoid

Activation

$$a = \sigma(x) = \frac{1}{1 + e^{-x}}$$

Gradient

$$\frac{\partial a}{\partial x} = \sigma(x)(1 - \sigma(x))$$



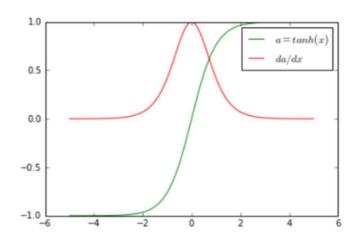
tanh

## Activation

$$a = \tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$

# Gradient

$$\frac{\partial a}{\partial x} = 1 - \tanh^2(x)$$



# Architecture design

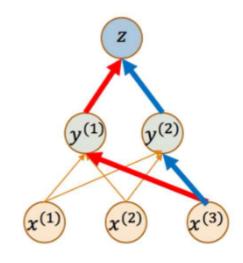
要思考的两个问题: 1. How many layers and units?

The more layers we have, the fewer units we need

2. How many connections?

Usually a complete set but in certain domains we can drop some connections

#### 反向传播和梯度下降:



$$\frac{dz}{dx^3} = \frac{dz}{dy^1} \frac{dy^1}{dx^3} + \frac{dz}{dy^2} \frac{dy^2}{dx^3}$$

主要的计算定理: chain rule:

注意: z关于y的导数有的时候消不掉, 要我们直接以隐函数的形式保留 (高数内容)