Main: Facial Expression Recognition Framework

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Introduction / Objective

Baseline Model/Proposed Model

Results

Analysis

In your final repo, there should be an R markdown file that organizes **all computational steps** for evaluating your proposed Facial Expression Recognition framework.

This file is currently a template for running evaluation experiments. You should update it according to your codes but following precisely the same structure.

Step 0 set work directories

```
set.seed(2020)
setwd("~/GitHub/Fall2020-Project3-group1/doc")

# change the working directory as needed
# if someone can make this a relative path, that would be great!!!
```

Provide directories for training images. Training images and Training fiducial points will be in different subfolders.

```
# change the directory of the data to where it's stored in your local drive as needed
# train_dir <- "../data/train_set/" # This will be modified for different data sets.

train_dir <- "~/train_set/"

train_image_dir <- paste(train_dir, "images/", sep="")
train_pt_dir <- paste(train_dir, "points/", sep="")
train_label_path <- paste(train_dir, "label.csv", sep="")</pre>
```

Step 1: set up controls for evaluation experiments.

In this chunk, we have a set of controls for the evaluation experiments.

- (T/F) cross-validation on the training set
- (T/F) reweighting the samples for training set
- (number) K, the number of CV folds
- (T/F) process features for training set
- (T/F) run evaluation on an independent test set
- (T/F) process features for test set

K <- 5 # number of CV folds

```
run.fudicial.list <- FALSE
run.feature.train <- FALSE # process features for training set
run.feature.test <- FALSE # process features for test set
sample.reweight <- TRUE # run sample reweighting in model training

run.cv.gbm <- FALSE # run cross-validation on the training set for gbm
run.train.gbm <- FALSE # run evaluation on entire train set
run.test.gbm <- TRUE # run evaluation on independent test set

run.cv.xgboost <- FALSE # run cross-validation on the training set for xgboost
run.train.xgboost <- FALSE # run evaluation on entire train set
run.test.xgboost <- TRUE # run evaluation on an independent test set

# add controls here to make if else statements to either cross-validate, test, train, or to just load s
# for xgboost, we need to also train and test each time we knit to record the time for the model
```

Using cross-validation or independent test set evaluation, we compare the performance of models with different specifications. In this Starter Code, we tune parameter lambda (the amount of shrinkage) for logistic regression with LASSO penalty.

```
# hyperparameters for our models

# gbm model (baseline)
hyper_grid_gbm <- expand.grid(
    shrinkage = c(0.001, 0.005, 0.010, 0.050, 0.100),
    n.trees = c(600, 1200, 1800)
)

# xgboost model
hyper_grid_xgboost <- expand.grid(
    eta = c(0.01, 0.05, 0.1, 0.2, 0.3),
    lambda = c(0.001, 0.005, 0.010, 0.050, 0.100),
    gamma = c(0, 5),
    nrounds = c(600, 1200, 1800)
)

# random forest model</pre>
```

```
# add more hyperparameters for each model as needed
```

Step 2: import data and train-test split

```
#train-test split
info <- read.csv(train_label_path)
n <- nrow(info)
n_train <- round(n*(4/5), 0)
train_idx <- sample(info$Index, n_train, replace = F)
test_idx <- setdiff(info$Index, train_idx)</pre>
```

Fiducial points are stored in matlab format. In this step, we read them and store them in a list.

```
n_files <- length(list.files(train_image_dir))

if (run.fudicial.list){
    #function to read fiducial points
    #input: index
    #output: matrix of fiducial points corresponding to the index
    readMat.matrix <- function(index){
        return(round(readMat(pasteO(train_pt_dir, sprintf("%04d", index), ".mat"))[[1]],0))
    }

#load fiducial points
fiducial_pt_list <- lapply(1:n_files, readMat.matrix)
    save(fiducial_pt_list, file="../output/fiducial_pt_list.RData")
} else {
    load(file="../output/fiducial_pt_list.RData")
}</pre>
```

Step 3: construct features and responses

- The follow plots show how pairwise distance between fiducial points can work as feature for facial emotion recognition.
 - In the first column, 78 fiducials points of each emotion are marked in order.
 - In the second column distributions of vertical distance between right pupil(1) and right brow peak(21) are shown in histograms. For example, the distance of an angry face tends to be shorter than that of a surprised face.
 - The third column is the distributions of vertical distances between right mouth corner(50) and the midpoint of the upper lip(52). For example, the distance of an happy face tends to be shorter than that of a sad face.

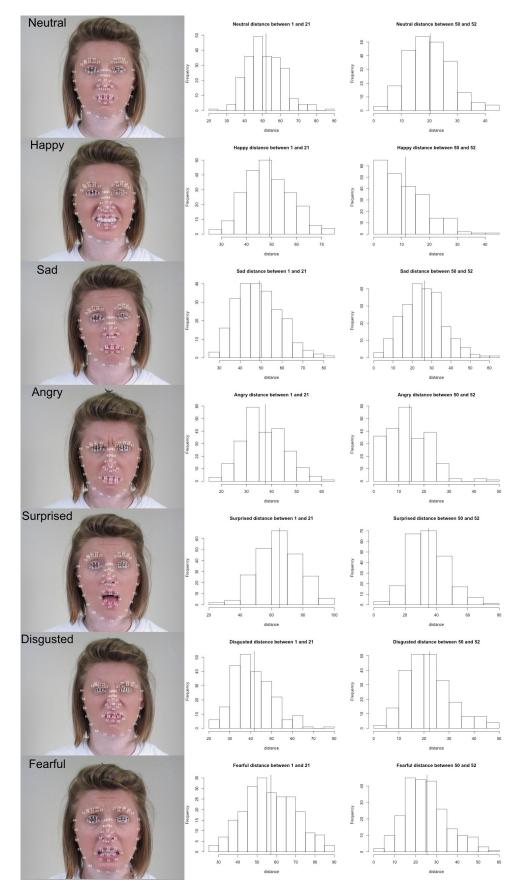


Figure 1: Figure 1

feature.R should be the wrapper for all your feature engineering functions and options. The function feature() should have options that correspond to different scenarios for your project and produces an R object that contains features and responses that are required by all the models you are going to evaluate later.

- feature.R
- Input: list of images or fiducial point
- Output: an RData file that contains extracted features and corresponding responses

```
source("../lib/feature.R")

tm_feature_train <- NA

if(run.feature.train){
    tm_feature_train <- system.time(dat_train <- feature(fiducial_pt_list, train_idx))
    save(dat_train, tm_feature_train, file="../output/feature_train.RData")
}else{
    load(file="../output/feature_train.RData")
}

tm_feature_test <- NA
    if(run.feature.test){
    tm_feature_test <- system.time(dat_test <- feature(fiducial_pt_list, test_idx))
        save(dat_test, tm_feature_test, file="../output/feature_test.RData")
}else{
    load(file="../output/feature_test.RData")
}</pre>
```

Gradient Boosted Trees (gbm model) (Baseline Model)

Step 4: Train a classification model with training features and responses

Call the train_gbm model and test_gbm model from library.

train_gbm.R and test_gbm.R should be wrappers for all your model training steps and your classification/prediction steps.

- train_gbm.R
 - Input: a data frame containing features and labels and a parameter list.
 - Output:a trained model
- test_gbm.R
 - Input: the fitted classification model using training data and processed features from testing images
 - Input: an R object that contains a trained classifier.
 - Output: training model specification

```
source("../lib/train_gbm.R")
source("../lib/test_gbm.R")
source("../lib/cross_validation_gbm.R")
```

Model selection with cross-validation

• Do model selection by choosing among different values of training model parameters.

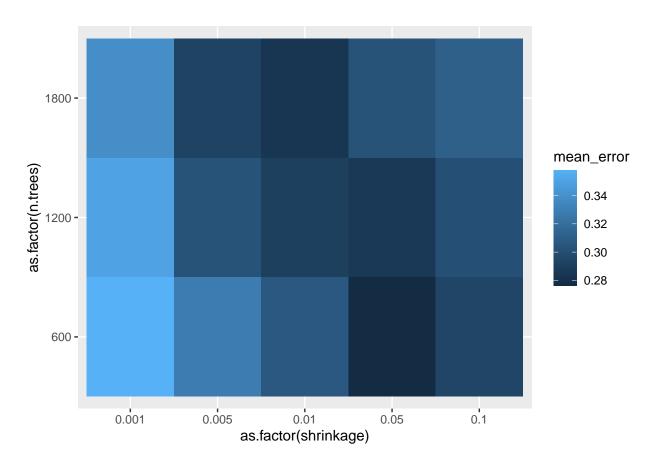
*Visualize cross-validation results.

```
res_cv_gbm <- as.data.frame(res_cv)
colnames(res_cv_gbm) <- c("mean_error", "sd_error", "mean_AUC", "sd_AUC")
gbm_cv_results = data.frame(hyper_grid_gbm, res_cv_gbm)</pre>
```

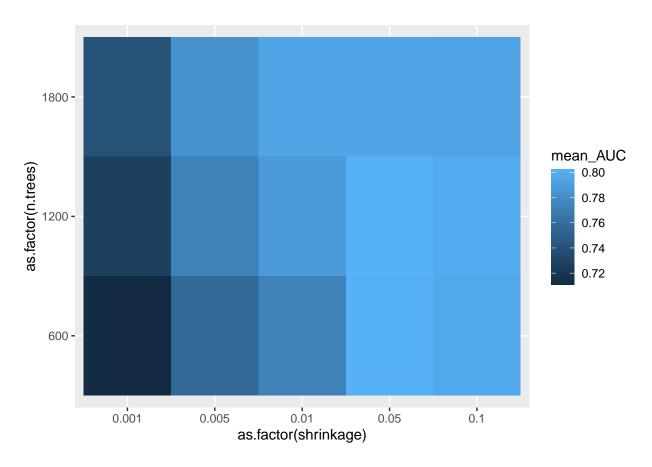
```
# a subset of cross-validated gbm models ordered by mean AUC (15 total)
# see appendix for full table
gbm_cv_results[order(gbm_cv_results$mean_AUC, decreasing = TRUE), ][1:5, ]
```

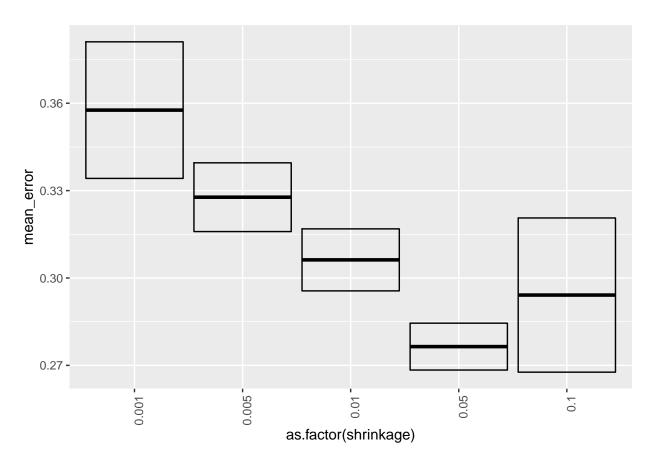
```
shrinkage n.trees mean_error
##
                                      sd_error mean_AUC
                                                              sd_AUC
## 9
           0.05
                   1200 0.2861576 0.026049925 0.8022183 0.018723658
## 4
           0.05
                         0.2764453 0.008045855 0.8015074 0.009653744
           0.10
                   1200 0.3004216 0.031100034 0.7986702 0.024253701
## 10
## 5
           0.10
                   600 0.2941406 0.026467746 0.7965060 0.021828465
## 14
           0.05
                   1800 0.3031199 0.027850857 0.7949472 0.019940282
```

```
# Mean Error
ggplot(gbm_cv_results, aes(as.factor(shrinkage), as.factor(n.trees), fill = mean_error)) +
   geom_tile()
```

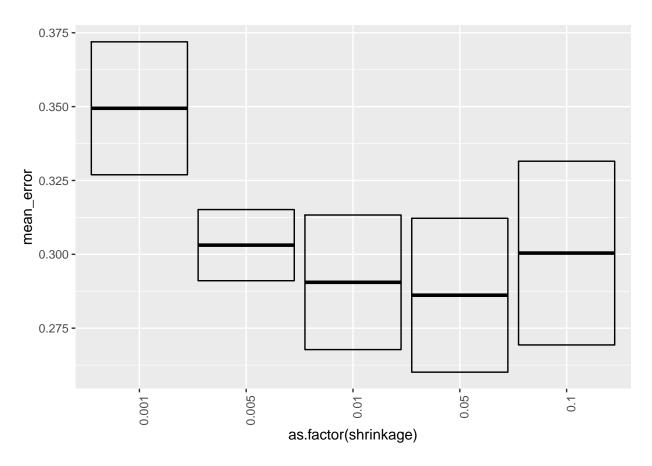


```
# Mean AUC
ggplot(gbm_cv_results, aes(as.factor(shrinkage), as.factor(n.trees), fill = mean_AUC)) +
  geom_tile()
```

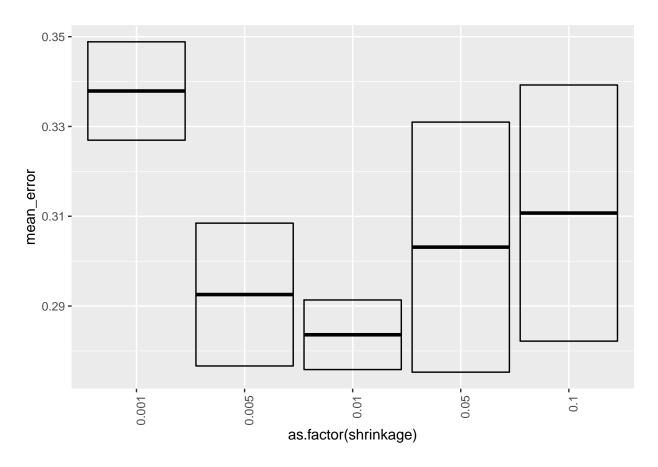




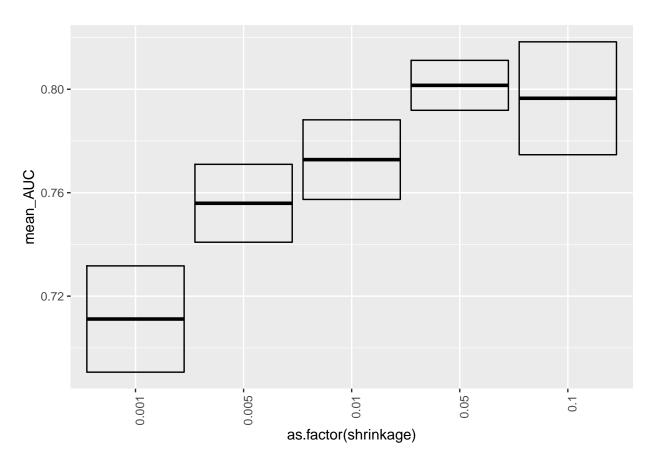
```
# N.Trees = 1200
ggplot(gbm_cv_results[gbm_cv_results$n.trees == 1200, ],
    aes(x = as.factor(shrinkage), y = mean_error,
        ymin = mean_error - sd_error, ymax = mean_error + sd_error)) +
    geom_crossbar() + theme(axis.text.x = element_text(angle = 90, hjust = 1))
```



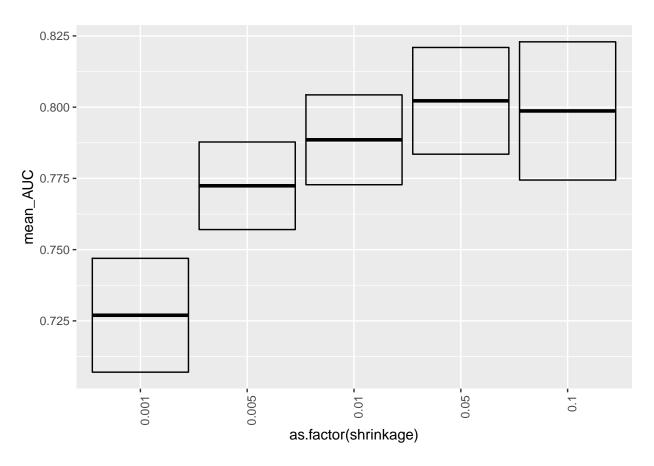
```
# N.Trees = 1800
ggplot(gbm_cv_results[gbm_cv_results$n.trees == 1800, ],
    aes(x = as.factor(shrinkage), y = mean_error,
        ymin = mean_error - sd_error, ymax = mean_error + sd_error)) +
    geom_crossbar() + theme(axis.text.x = element_text(angle = 90, hjust = 1))
```



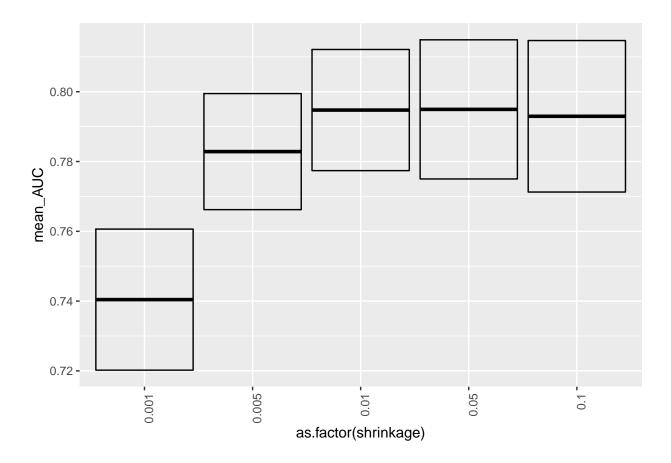
```
# Mean AUC
# N.Trees = 600
ggplot(gbm_cv_results[gbm_cv_results$n.trees == 600, ],
    aes(x = as.factor(shrinkage), y = mean_AUC,
        ymin = mean_AUC - sd_AUC, ymax = mean_AUC + sd_AUC)) +
    geom_crossbar() + theme(axis.text.x = element_text(angle = 90, hjust = 1))
```



```
# N.Trees = 1200
ggplot(gbm_cv_results[gbm_cv_results$n.trees == 1200, ],
    aes(x = as.factor(shrinkage), y = mean_AUC,
        ymin = mean_AUC - sd_AUC, ymax = mean_AUC + sd_AUC)) +
    geom_crossbar() + theme(axis.text.x = element_text(angle = 90, hjust = 1))
```



```
# N.Trees = 1800
ggplot(gbm_cv_results[gbm_cv_results$n.trees == 1800, ],
    aes(x = as.factor(shrinkage), y = mean_AUC,
        ymin = mean_AUC - sd_AUC, ymax = mean_AUC + sd_AUC)) +
    geom_crossbar() + theme(axis.text.x = element_text(angle = 90, hjust = 1))
```



• Choose the "best" parameter value

Due to the presence imbalanced data, we choose to focus out attention on highest mean AUC rather than lowest mean error. However, we notice that the second best model (model 4) is has an mean AUC comparable to that of the best model (model 9) while being much simplier—model 4 has 600 trees while model 9 has 1200—we choose to select the more parsimonious model as our best baseline gbm model.

```
gbm_cv_results[order(gbm_cv_results$mean_AUC, decreasing = TRUE), ][2, ]

## shrinkage n.trees mean_error sd_error mean_AUC sd_AUC

## 4 0.05 600 0.2764453 0.008045855 0.8015074 0.009653744

par_best_gbm_ind <- 4
par_best_gbm_shrinkage <- gbm_cv_results$shrinkage[par_best_gbm_ind]
par_best_gbm_n.trees <- gbm_cv_results$n.trees[par_best_gbm_ind]</pre>
```

• Train the model with the entire training set using the selected model (model parameter) via cross-validation.

```
if (run.train.gbm) {
    # training weights
    weight_train <- rep(NA, length(label_train))
    for (v in unique(label_train)){
        weight_train[label_train == v] = 0.5 * length(label_train) / length(label_train[label_train == v])</pre>
```

Step 5: Run test on test images

• Evaluation

```
## reweight the test data to represent a balanced label distribution

weight_test <- rep(NA, length(label_test))
for (v in unique(label_test)){
    weight_test[label_test == v] = 0.5 * length(label_test) / length(label_test[label_test == v])
}

# convert the original 1-2 class into numeric 0s and 1s
label_test <- ifelse(label_test == 2, 0, 1)

accu <- sum(weight_test * (label_pred == label_test)) / sum(weight_test)
tpr.fpr <- WeightedAUC(prob_pred, label_test, weight_test)
auc <- WeightedAUC(tpr.fpr)

## The accuracy of the gbm model (shinkage = 0.05, n.trees = 600) is 70.82105%.

## The AUC of the gbm model (shinkage = 0.05, n.trees = 600) is 0.7928758.</pre>
```

Summarize Running Time Prediction performance matters, so does the running times for constructing features and for training the model, especially when the computation resource is limited.

```
## Time for constructing training features = 2.14 seconds
## Time for constructing testing features = 0.16 seconds
## Time for training gbm model = 123.7 seconds
```

Time for testing gbm model = 14.2 seconds

xgboost Model (Proposed Model)

Step 4: Train a classification model with training features and responses

Call the train model and test model from library.

train_xgboost.R and test_xgboost.R should be wrappers for all your model training steps and your classification/prediction steps.

- train_xgboost.R
 - Input: a data frame containing features and labels and a parameter list.
 - Output:a trained model
- test_xgboost.R
 - Input: the fitted classification model using training data and processed features from testing images
 - Input: an R object that contains a trained classifier.
 - Output: training model specification

```
source("../lib/train_xgboost.R")
source("../lib/test_xgboost.R")
source("../lib/cross_validation_xgboost.R")
```

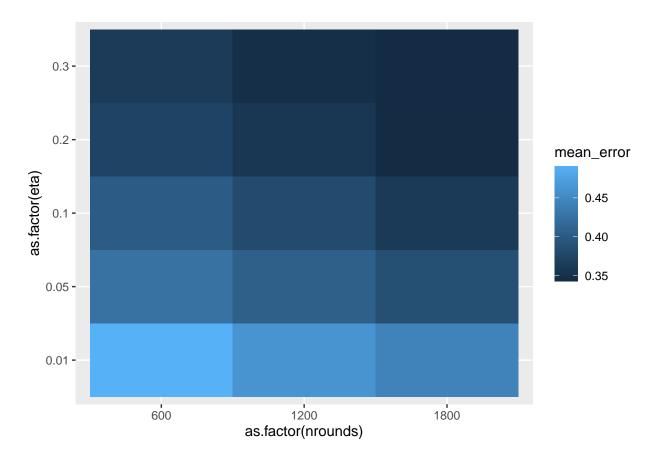
Model selection with cross-validation

• Do model selection by choosing among different values of training model parameters.

```
res_cv_xgboost <- as.data.frame(res_cv)
colnames(res_cv_xgboost) <- c("mean_error", "sd_error", "mean_AUC", "sd_AUC")
res_cv_xgboost_cv_results = data.frame(hyper_grid_xgboost, res_cv_xgboost)</pre>
```

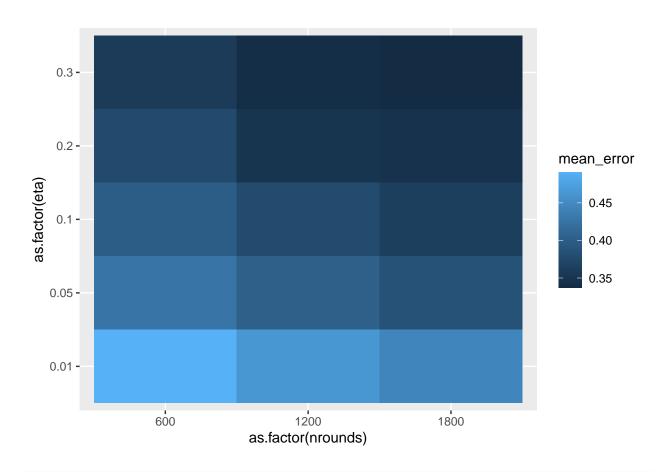
^{*}Visualize cross-validation results.

```
# a subset of cross-validated xgboost models ordered by mean AUC (150 total)
# see appendix for full table
res_cv_xgboost_cv_results[order(res_cv_xgboost_cv_results$mean_AUC, decreasing = TRUE), ][1:5, ]
       eta lambda gamma nrounds mean error
                                            sd error mean AUC
##
                          1200 0.4054330 0.01838352 0.8083090 0.01479400
## 67 0.05 0.050
                     0
## 23 0.10 0.100
                           600 0.3987534 0.01527476 0.8081563 0.01500276
                     0
## 3 0.10 0.001
                     0
                           600 0.3967334 0.01385476 0.8080448 0.01802835
## 18 0.10 0.050
                           600 0.4014677 0.01679825 0.8078401 0.01590874
                     0
                          1200 0.4048485 0.01376101 0.8074209 0.01509062
## 52 0.05 0.001
                     0
# Mean Error
\# gamma = 0, lambda = 0.05
ggplot(res_cv_xgboost_cv_results[res_cv_xgboost_cv_results$gamma == 0 & res_cv_xgboost_cv_results$lambd
```

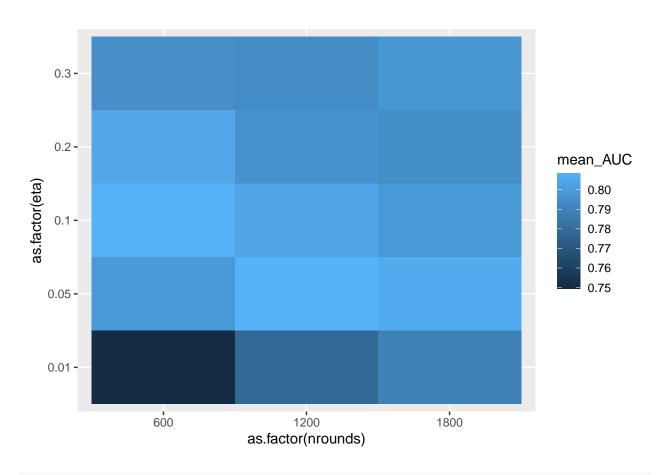


geom_tile()

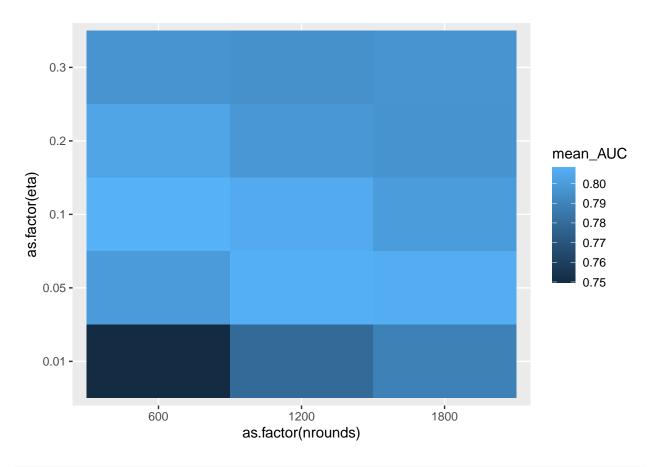
gamma = 0, lambda = 0.10
ggplot(res_cv_xgboost_cv_results[res_cv_xgboost_cv_results\$gamma == 0 & res_cv_xgboost_cv_results\$lambd
geom_tile()



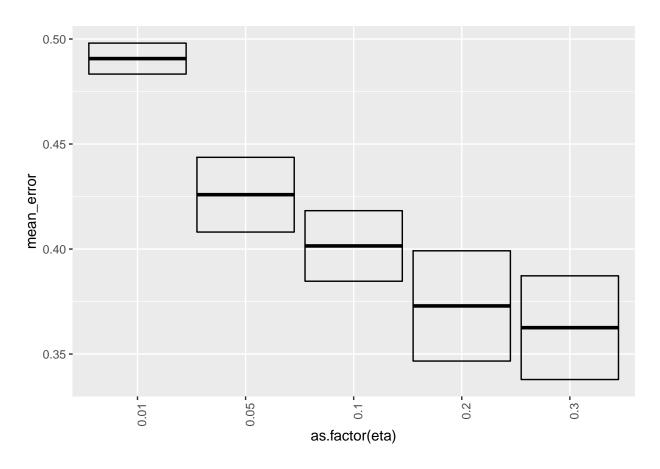
```
# Mean AUC
# # gamma = 0, lambda = 0.05
ggplot(res_cv_xgboost_cv_results[res_cv_xgboost_cv_results$gamma == 0 & res_cv_xgboost_cv_results$lambd
geom_tile()
```



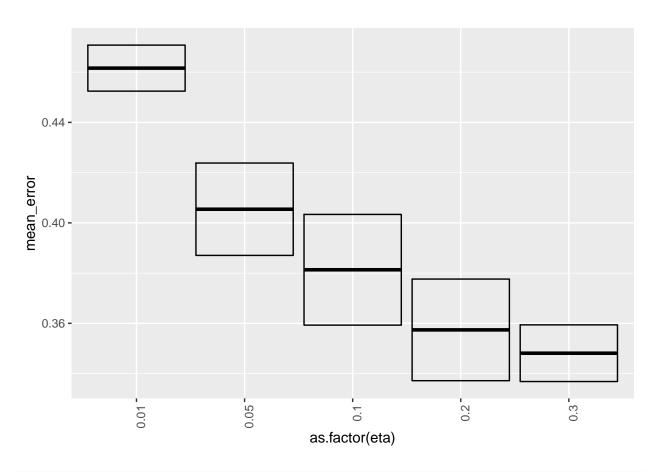
gamma = 0, lambda = 0.10
ggplot(res_cv_xgboost_cv_results[res_cv_xgboost_cv_results\$gamma == 0 & res_cv_xgboost_cv_results\$lambd
geom_tile()



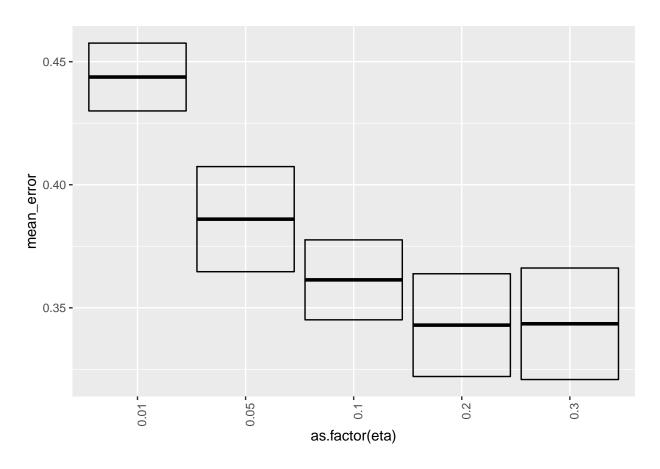
```
# Mean Error
# nrounds = 600
ggplot(res_cv_xgboost_cv_results[res_cv_xgboost_cv_results$nrounds == 600 & res_cv_xgboost_cv_results$g
    aes(x = as.factor(eta), y = mean_error,
        ymin = mean_error - sd_error, ymax = mean_error + sd_error)) +
    geom_crossbar() + theme(axis.text.x = element_text(angle = 90, hjust = 1))
```



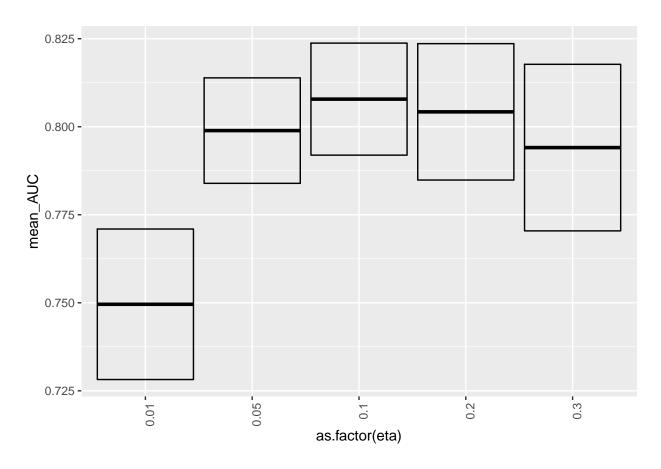
```
# nrounds = 1200
ggplot(res_cv_xgboost_cv_results[res_cv_xgboost_cv_results$nrounds == 1200 & res_cv_xgboost_cv_results$
    aes(x = as.factor(eta), y = mean_error,
        ymin = mean_error - sd_error, ymax = mean_error + sd_error)) +
    geom_crossbar() + theme(axis.text.x = element_text(angle = 90, hjust = 1))
```



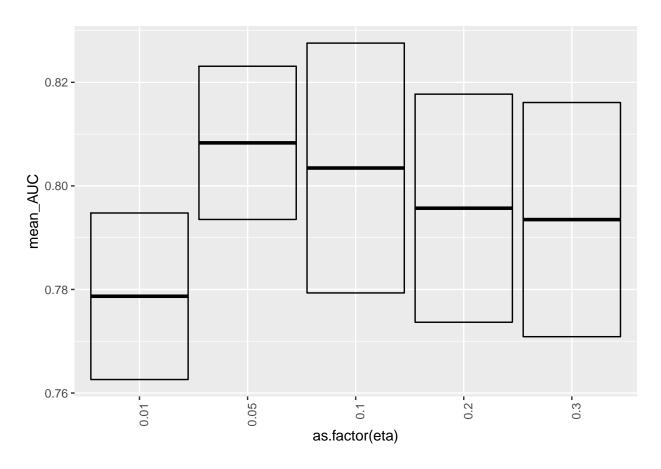
```
# nrounds = 1800
ggplot(res_cv_xgboost_cv_results[res_cv_xgboost_cv_results$nrounds == 1800 & res_cv_xgboost_cv_results$
    aes(x = as.factor(eta), y = mean_error,
        ymin = mean_error - sd_error, ymax = mean_error + sd_error)) +
    geom_crossbar() + theme(axis.text.x = element_text(angle = 90, hjust = 1))
```



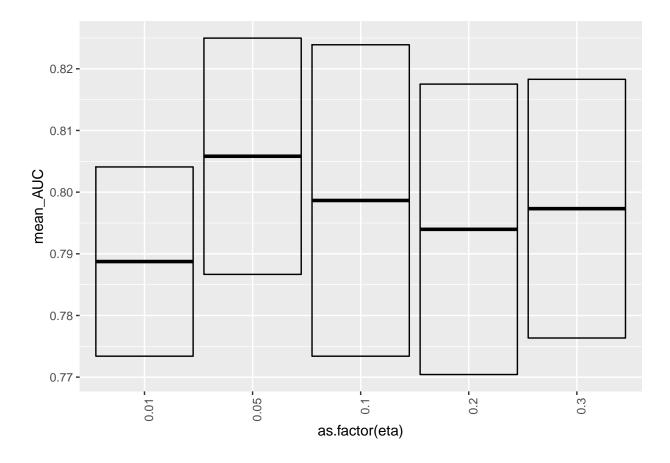
```
# Mean AUC
# nrounds = 600
ggplot(res_cv_xgboost_cv_results[res_cv_xgboost_cv_results$nrounds == 600 & res_cv_xgboost_cv_results$g
    aes(x = as.factor(eta), y = mean_AUC,
        ymin = mean_AUC - sd_AUC, ymax = mean_AUC + sd_AUC)) +
    geom_crossbar() + theme(axis.text.x = element_text(angle = 90, hjust = 1))
```



```
# nrounds = 1200
ggplot(res_cv_xgboost_cv_results[res_cv_xgboost_cv_results$nrounds == 1200 & res_cv_xgboost_cv_results$
    aes(x = as.factor(eta), y = mean_AUC,
        ymin = mean_AUC - sd_AUC, ymax = mean_AUC + sd_AUC)) +
    geom_crossbar() + theme(axis.text.x = element_text(angle = 90, hjust = 1))
```



```
# nrounds = 1800
ggplot(res_cv_xgboost_cv_results[res_cv_xgboost_cv_results$nrounds == 1800 & res_cv_xgboost_cv_results$
    aes(x = as.factor(eta), y = mean_AUC,
        ymin = mean_AUC - sd_AUC, ymax = mean_AUC + sd_AUC)) +
    geom_crossbar() + theme(axis.text.x = element_text(angle = 90, hjust = 1))
```



• Choose the "best" parameter value

Due to the presence imbalanced data, we choose to focus out attention on highest mean AUC rather than lowest mean error. However, we notice that the second best model (model 67) is has an mean AUC comparable to that of the best model (model 23) while being much simpler—model 23 has 600 trees while model 67 has 1200—we choose to select the more parsimonious model as our best proposed xgboost model.

```
res cv xgboost cv results[order(res cv xgboost cv results$mean AUC, decreasing = TRUE), ][2, ]
##
      eta lambda gamma nrounds mean_error
                                              sd_error mean_AUC
                                                                      sd_AUC
## 23 0.1
                            600 0.3987534 0.01527476 0.8081563 0.01500276
par_best_res_cv_xgboost_cv_results_ind <- 23</pre>
par_best_res_cv_xgboost_cv_results_eta <-</pre>
  res_cv_xgboost_cv_results$eta[par_best_res_cv_xgboost_cv_results_ind]
par_best_res_cv_xgboost_cv_results_lambda <-</pre>
  res_cv_xgboost_cv_results$lambda[par_best_res_cv_xgboost_cv_results_ind]
par_best_res_cv_xgboost_cv_results_gamma <-</pre>
  res_cv_xgboost_cv_results$gamma[par_best_res_cv_xgboost_cv_results_ind]
par_best_res_cv_xgboost_cv_results_nrounds <-</pre>
  res_cv_xgboost_cv_results$nrounds[par_best_res_cv_xgboost_cv_results_ind]
```

• Train the model with the entire training set using the selected model (model parameter) via cross-validation.

```
if (run.train.xgboost) {
  # training weights
  weight_train <- rep(NA, length(label_train))</pre>
  for (v in unique(label_train)){
    weight_train[label_train == v] = 0.5 * length(label_train) / length(label_train[label_train == v])
  if (sample.reweight){
    tm_train_xgboost <- system.time(fit_train_xgboost <- train(features = feature_train, labels = label</pre>
                                                                  w = weight_train,
                                                                   eta_val = par_best_res_cv_xgboost_cv_r
                                                                  lmd = par_best_res_cv_xgboost_cv_resul
                                                                   gam = par_best_res_cv_xgboost_cv_resul
                                                                  nr = par_best_res_cv_xgboost_cv_result
  } else {
   tm_train_xgboost <- system.time(fit_train_xgboost <- train(features = feature_train, labels = label</pre>
                                                                   w = NULL,
                                                                   eta_val = par_best_res_cv_xgboost_cv_r
                                                                  lmd = par_best_res_cv_xgboost_cv_resul
                                                                   gam = par_best_res_cv_xgboost_cv_resul
                                                                  nr = par_best_res_cv_xgboost_cv_result
  save(fit train xgboost, tm train xgboost, file=".../output/fit train xgboost.RData")
} else {
  load(file="../output/fit_train_xgboost.RData")
```

Step 5: Run test on test images

• Evaluation

```
## reweight the test data to represent a balanced label distribution
weight_test <- rep(NA, length(label_test))
for (v in unique(label_test)){
   weight_test[label_test == v] = 0.5 * length(label_test) / length(label_test[label_test == v])
}</pre>
```

```
# convert the original 1-2 class into numeric Os and 1s
label_test <- ifelse(label_test == 2, 0, 1)

accu <- sum(weight_test * (label_pred == label_test)) / sum(weight_test)
tpr.fpr <- WeightedROC(prob_pred, label_test, weight_test)
auc <- WeightedAUC(tpr.fpr)</pre>
```

The accuracy of the xgboost model (eta = 0.1, nrounds = 600, lambda = 0.1, gamma = 0) is 70.86316%.

The AUC of the xgboost model (eta = 0.1, nrounds = 600, lambda = 0.1, gamma = 0) is 0.7970021.

Summarize Running Time Prediction performance matters, so does the running times for constructing features and for training the model, especially when the computation resource is limited.

Time for training xgboost model = 74.75 seconds

Time for testing xgboost model = 0.11 seconds

Other Models

Principal Components Analysis (PCA) + Support Vector Machines (SVMs)

Step 4: Train a classification model with training features and responses

Call the train model and test model from library.

train.R and test.R should be wrappers for all your model training steps and your classification/prediction steps.

• train.R

- Input: a data frame containing features and labels and a parameter list.
- Output:a trained model

• test.R

- Input: the fitted classification model using training data and processed features from testing images
- Input: an R object that contains a trained classifier.
- Output: training model specification
- In this Starter Code, we use logistic regression with LASSO penalty to do classification.

Model selection with cross-validation

• Do model selection by choosing among different values of training model parameters.

*Visualize cross-validation results.

- Choose the "best" parameter value
- Train the model with the entire training set using the selected model (model parameter) via cross-validation.

Step 5: Run test on test images

• Evaluation

Summarize Running Time Prediction performance matters, so does the running times for constructing features and for training the model, especially when the computation resource is limited.

Random Forests

Step 4: Train a classification model with training features and responses

Call the train model and test model from library.

train.R and test.R should be wrappers for all your model training steps and your classification/prediction steps.

- train.R
 - Input: a data frame containing features and labels and a parameter list.
 - Output:a trained model
- test.R
 - Input: the fitted classification model using training data and processed features from testing images
 - Input: an R object that contains a trained classifier.
 - Output: training model specification
- In this Starter Code, we use logistic regression with LASSO penalty to do classification.

```
library(magrittr) #### NEED TO INSTALL THIS PACKAGE ON TO BUT ONLY IF WE STILL NEED IT
source("../lib/train.R")
source("../lib/test.R")
```

Model selection with cross-validation

• Do model selection by choosing among different values of training model parameters.

*Visualize cross-validation results.

```
res_cv <- as.data.frame(res_cv)
colnames(res_cv) <- c("mean_error", "sd_error", "mean_AUC", "sd_AUC")
res_cv$k = as.factor(lmbd)

if(run.cv){
  p1 <- res_cv %>%
```

• Choose the "best" parameter value

```
par_best <- lmbd[which.min(res_cv$mean_error)] # lmbd[which.max(res_cv$mean_AUC)]</pre>
```

• Train the model with the entire training set using the selected model (model parameter) via cross-validation.

```
# training weights
weight_train <- rep(NA, length(label_train))
for (v in unique(label_train)){
   weight_train[label_train == v] = 0.5 * length(label_train) / length(label_train[label_train == v])
}
if (sample.reweight){
   tm_train <- system.time(fit_train <- train(feature_train, label_train, w = weight_train, par_best))
} else {
   tm_train <- system.time(fit_train <- train(feature_train, label_train, w = NULL, par_best))
}
save(fit_train, file=".../output/fit_train.RData")</pre>
```

Step 5: Run test on test images

```
## reweight the test data to represent a balanced label distribution
label_test <- as.integer(dat_test$label)
weight_test <- rep(NA, length(label_test))</pre>
```

```
for (v in unique(label_test)){
    weight_test[label_test == v] = 0.5 * length(label_test) / length(label_test[label_test == v])
}
accu <- sum(weight_test * (label_pred == label_test)) / sum(weight_test)
tpr.fpr <- WeightedROC(prob_pred, label_test, weight_test)
auc <- WeightedAUC(tpr.fpr)

cat("The accuracy of model:", model_labels[which.min(res_cv$mean_error)], "is", accu*100, "%.\n")
cat("The AUC of model:", model_labels[which.min(res_cv$mean_error)], "is", auc, ".\n")</pre>
```

Evaluation

Summarize Running Time Prediction performance matters, so does the running times for constructing features and for training the model, especially when the computation resource is limited.

Reference(s)

• Du, S., Tao, Y., & Martinez, A. M. (2014). Compound facial expressions of emotion. Proceedings of the National Academy of Sciences, 111(15), E1454-E1462.

Appendix

We provide the full output of the cross-validation table for each model below.

```
gbm_cv_results
```

```
##
      shrinkage n.trees mean_error
                                       sd_error
                                                 mean_AUC
                                                                sd_AUC
## 1
          0.001
                    600
                         0.3576347 0.023447152 0.7111546 0.020548747
## 2
          0.005
                    600
                         0.3277413 0.011801334 0.7559083 0.015056717
## 3
          0.010
                         0.3062226 0.010644901 0.7727803 0.015389634
          0.050
                    600
                         0.2764453 0.008045855 0.8015074 0.009653744
## 4
## 5
          0.100
                    600
                         0.2941406 0.026467746 0.7965060 0.021828465
## 6
          0.001
                   1200
                         0.3494367 0.022503501 0.7269749 0.019971143
                         0.3031100 0.012042165 0.7724047 0.015363576
## 7
          0.005
                   1200
          0.010
                   1200
                         0.2905285 0.022779998 0.7885403 0.015763480
## 8
                         0.2861576 0.026049925 0.8022183 0.018723658
## 9
          0.050
                   1200
## 10
          0.100
                   1200
                         0.3004216 0.031100034 0.7986702 0.024253701
## 11
          0.001
                   1800
                         0.3378972 0.010955498 0.7404200 0.020218630
                         0.2925555 0.015907800 0.7828471 0.016634467
## 12
          0.005
                   1800
## 13
          0.010
                   1800
                         0.2835979 0.007752051 0.7947552 0.017362962
## 14
          0.050
                   1800
                         0.3031199 0.027850857 0.7949472 0.019940282
          0.100
                         0.3107072 0.028527596 0.7929691 0.021709803
## 15
                   1800
```

res_cv_xgboost_cv_results

```
eta lambda gamma nrounds mean error
##
                                                sd_error mean_AUC
## 1
             0.001
                                   0.4906777 0.007370532 0.7493713 0.021512810
       0.01
                              600
## 2
       0.05
             0.001
                        0
                                   0.4269490 0.017502201 0.7984128 0.015150812
       0.10 0.001
## 3
                        0
                              600
                                   0.3967334 0.013854762 0.8080448 0.018028352
       0.20
             0.001
                        0
                              600
                                   0.3802263 0.022275637 0.8004366 0.024310280
       0.30
             0.001
                              600
                                   0.3618273 0.019997257 0.7924177 0.024227634
## 5
                        0
## 6
       0.01
             0.005
                        0
                              600
                                   0.4906777 0.007370532 0.7493712 0.021511501
## 7
       0.05
             0.005
                        0
                              600
                                  0.4251475 0.019096921 0.7991652 0.015752604
## 8
       0.10
             0.005
                        0
                                   0.3976521 0.016905339 0.8068678 0.015141950
                                   0.3714554 0.028059747 0.8020856 0.021416240
## 9
       0.20
             0.005
                        0
                              600
## 10
       0.30
             0.005
                        0
                              600
                                   0.3588479 0.016613817 0.7986248 0.027706959
##
  11
       0.01
             0.010
                              600
                                   0.4906777 0.007370532 0.7493895 0.021463878
       0.05
             0.010
                        0
                              600
                                   0.4251462 0.018664204 0.7986868 0.015603221
## 12
##
  13
       0.10
             0.010
                        0
                              600
                                   0.4035937 0.012926598 0.8074199 0.016325413
##
  14
       0.20
             0.010
                        0
                                  0.3770305 0.020917023 0.8024737 0.022217211
## 15
       0.30
             0.010
                                  0.3500278 0.021987925 0.7976123 0.023782641
## 16
       0.01
             0.050
                        0
                              600
                                   0.4906777 0.007370532 0.7495704 0.021375234
  17
       0.05
             0.050
                                   0.4258744 0.017794101 0.7989016 0.014980665
##
##
  18
       0.10
             0.050
                        0
                              600
                                   0.4014677 0.016798251 0.8078401 0.015908736
                                   0.3729058 0.026252876 0.8042287 0.019369699
  19
       0.20
             0.050
                                   0.3625486 0.024690928 0.7940729 0.023655181
## 20
       0.30
             0.050
```

```
## 21
       0.01
             0.100
                        0
                                   0.4904138 0.007135743 0.7498269 0.021594887
## 22
       0.05
             0.100
                        0
                                   0.4259168 0.015373404 0.7994809 0.015485758
                              600
             0.100
##
  23
       0.10
                        0
                                   0.3987534 0.015274758 0.8081563 0.015002756
       0.20
             0.100
                        0
                                   0.3762554 0.026295556 0.8032019 0.019209179
##
  24
                              600
##
   25
       0.30
             0.100
                        0
                                   0.3575550 0.020906754 0.7963820 0.023517710
       0.01
             0.001
                        5
                                   0.4906777 0.007370532 0.7493713 0.021512810
##
  26
                              600
             0.001
                        5
                                   0.4269490 0.017502201 0.7984128 0.015150812
##
  27
       0.05
             0.001
## 28
       0.10
                        5
                              600
                                   0.4154400 0.012458015 0.8051049 0.014138614
##
   29
       0.20
             0.001
                        5
                              600
                                   0.4107942 0.014726956 0.8033595 0.016394417
             0.001
                        5
##
   30
       0.30
                              600
                                   0.4046499 0.018198233 0.7979770 0.008939835
##
   31
       0.01
             0.005
                        5
                                   0.4906777 0.007370532 0.7493712 0.021511501
       0.05
             0.005
                        5
                              600
                                   0.4251475 0.019096921 0.7991652 0.015752604
##
   32
##
   33
       0.10
             0.005
                        5
                              600
                                   0.4144201 0.015494709 0.8052435 0.015479767
             0.005
                        5
                                   0.4115338 0.016405299 0.8017982 0.016251374
##
   34
       0.20
   35
       0.30
             0.005
                                   0.4027665 0.021082382 0.8034172 0.010682815
##
                        5
                              600
##
   36
       0.01
             0.010
                        5
                                   0.4906777 0.007370532 0.7493895 0.021463878
       0.05
             0.010
                        5
                                   0.4251462 0.018664204 0.7986868 0.015603221
##
                              600
   37
##
   38
       0.10
             0.010
                        5
                                   0.4156444 0.011930234 0.8044954 0.015731661
       0.20
             0.010
                                   0.4065506 0.014654309 0.8016072 0.016248020
##
   39
                        5
                              600
##
   40
       0.30
             0.010
                        5
                                   0.4011374 0.020653877 0.7984039 0.015230475
##
  41
       0.01
             0.050
                        5
                              600
                                   0.4906777 0.007370532 0.7495704 0.021375234
       0.05
             0.050
                        5
                                   0.4258744 0.017794101 0.7989016 0.014980665
##
  42
       0.10
             0.050
                                   0.4143769 0.017366280 0.8050385 0.014988197
## 43
                        5
                              600
       0.20
             0.050
                        5
                                   0.4050338 0.014409292 0.8028591 0.010353641
##
   44
                              600
             0.050
                        5
                                   0.4057419 0.020123531 0.8003049 0.012840485
## 45
       0.30
                              600
  46
       0.01
             0.100
                        5
                                   0.4904138 0.007135743 0.7498269 0.021594887
       0.05
             0.100
                        5
                              600
                                   0.4259168 0.015373404 0.7994809 0.015485758
##
  47
                        5
##
   48
       0.10
             0.100
                              600
                                   0.4137265 0.015457852 0.8058696 0.015549654
                        5
       0.20
             0.100
                              600
                                   0.4061859 0.012503112 0.8036462 0.007516747
##
   49
##
  50
       0.30
             0.100
                        5
                              600
                                   0.4048464 0.017908749 0.7960404 0.012265871
## 51
       0.01
             0.001
                        0
                             1200
                                   0.4615955 0.009160897 0.7788102 0.015696314
##
  52
       0.05
             0.001
                        0
                             1200
                                   0.4048485 0.013761008 0.8074209 0.015090616
                        0
                             1200
##
   53
       0.10
             0.001
                                   0.3769119 0.024008194 0.8035949 0.023844967
       0.20
             0.001
                        0
                             1200
                                   0.3566192 0.012450444 0.7932479 0.027131994
##
  54
   55
       0.30
             0.001
                        0
                             1200
                                   0.3503374 0.023226630 0.7910814 0.023516309
##
       0.01
             0.005
                        0
                             1200
                                   0.4615955 0.009160897 0.7787822 0.016130688
##
  56
##
  57
       0.05
             0.005
                        0
                             1200
                                   0.4054213 0.015531547 0.8072834 0.014597854
       0.10
             0.005
                        0
                             1200
                                   0.3801714 0.021434839 0.8020552 0.022992163
## 58
       0.20
             0.005
                        0
                             1200
                                   0.3563650 0.018533892 0.7954614 0.022996039
##
   59
##
       0.30
             0.005
                        0
                             1200
                                   0.3392984 0.028925628 0.7964171 0.025232192
  60
       0.01
             0.010
                        0
                             1200
                                   0.4615955 0.009160897 0.7787671 0.015849051
##
  61
       0.05
             0.010
                        0
                             1200
                                   0.4094424 0.020839728 0.8072104 0.014290764
##
  62
##
   63
       0.10
             0.010
                        0
                             1200
                                   0.3776749 0.020324924 0.8028266 0.023601778
             0.010
                        0
       0.20
                             1200
                                   0.3575453 0.017639274 0.7947047 0.024452694
##
   64
                        0
##
  65
       0.30
             0.010
                                   0.3470346 0.027459587 0.7935134 0.025482033
             0.050
                        0
                                   0.4615955 0.009160897 0.7786848 0.016080235
       0.01
                             1200
##
  66
##
   67
       0.05
             0.050
                        0
                             1200
                                   0.4054330 0.018383518 0.8083090 0.014793996
             0.050
                        0
                                   0.3813304 0.022033539 0.8034491 0.024120929
##
   68
       0.10
                             1200
##
  69
       0.20
             0.050
                        0
                             1200
                                   0.3574039 0.020227396 0.7956913 0.022024514
##
   70
       0.30
             0.050
                        0
                             1200
                                   0.3481230 0.011280241 0.7934894 0.022611256
       0.01
                        0
                                   0.4615955 0.009160897 0.7788813 0.016026083
##
  71
             0.100
                             1200
                        0
## 72
       0.05
             0.100
                             1200
                                   0.4019064 0.011636505 0.8072567 0.014257891
## 73
       0.10
             0.100
                        0
                             1200
                                   0.3779758 0.019775270 0.8055107 0.022806607
## 74
       0.20 0.100
                             1200 0.3499127 0.019270100 0.7978881 0.023613965
```

```
## 75
       0.30 0.100
                        0
                             1200 0.3416265 0.015418106 0.7951568 0.023665776
## 76
       0.01
             0.001
                        5
                                  0.4615955 0.009160897 0.7788102 0.015696314
                             1200
       0.05
                                  0.4185294 0.015184471 0.8035309 0.013806411
##
  77
             0.001
                        5
                                  0.4154400 0.012458015 0.8051049 0.014138614
       0.10
             0.001
                        5
                             1200
##
  78
##
   79
       0.20
             0.001
                        5
                             1200
                                   0.4107942 0.014726956 0.8033595 0.016394417
       0.30
             0.001
                        5
                             1200
                                  0.4046499 0.018198233 0.7979770 0.008939835
##
  80
             0.005
                        5
                                   0.4615955 0.009160897 0.7787822 0.016130688
## 81
       0.01
                                   0.4174985 0.014086877 0.8035957 0.014111349
## 82
       0.05
             0.005
                        5
                             1200
## 83
       0.10
             0.005
                        5
                             1200
                                   0.4144201 0.015494709 0.8052435 0.015479767
       0.20
             0.005
                        5
##
  84
                             1200
                                  0.4115338 0.016405299 0.8017982 0.016251374
## 85
       0.30
             0.005
                        5
                             1200
                                  0.4027665 0.021082382 0.8034172 0.010682815
       0.01
             0.010
                        5
                             1200
                                  0.4615955 0.009160897 0.7787671 0.015849051
##
  86
                        5
##
   87
       0.05
             0.010
                             1200
                                  0.4174985 0.014086877 0.8042510 0.013930606
                        5
                             1200
                                   0.4156444 0.011930234 0.8044954 0.015731661
##
  88
       0.10
             0.010
       0.20
             0.010
                        5
                             1200
                                   0.4065506 0.014654309 0.8016072 0.016248020
## 89
## 90
       0.30
             0.010
                        5
                             1200
                                   0.4011374 0.020653877 0.7984039 0.015230475
       0.01
             0.050
                        5
                                   0.4615955 0.009160897 0.7786848 0.016080235
##
                             1200
  91
                        5
  92
       0.05
             0.050
                             1200
                                  0.4166843 0.014804206 0.8032928 0.014654747
##
       0.10
             0.050
                             1200
                                  0.4143769 0.017366280 0.8050385 0.014988197
## 93
                        5
## 94
       0.20
             0.050
                        5
                             1200
                                  0.4050338 0.014409292 0.8028591 0.010353641
##
  95
       0.30
             0.050
                        5
                             1200
                                  0.4057419 0.020123531 0.8003049 0.012840485
       0.01
             0.100
                        5
                                   0.4615955 0.009160897 0.7788813 0.016026083
## 96
       0.05
             0.100
                        5
                            1200
                                   0.4174375 0.010785276 0.8035164 0.015512558
## 97
             0.100
                        5
                                   0.4137265 0.015457852 0.8058696 0.015549654
## 98
       0.10
                             1200
             0.100
                                   0.4061859 0.012503112 0.8036462 0.007516747
       0.20
                        5
                             1200
## 99
## 100 0.30
             0.100
                        5
                             1200
                                   0.4048464 0.017908749 0.7960404 0.012265871
## 101 0.01
             0.001
                        0
                             1800
                                   0.4437645 0.013777979 0.7883131 0.015401787
                        0
## 102 0.05
             0.001
                             1800
                                   0.3835403 0.022916992 0.8057435 0.019116530
                        0
## 103 0.10
             0.001
                             1800
                                   0.3654317 0.013245676 0.7986175 0.025228027
## 104 0.20
             0.001
                        0
                             1800
                                   0.3486151 0.021180715 0.7942583 0.025609927
## 105 0.30
             0.001
                        0
                             1800
                                   0.3330139 0.024322477 0.7974005 0.023020208
## 106 0.01
             0.005
                        0
                             1800
                                   0.4437645 0.013777979 0.7883814 0.015458859
                        0
## 107 0.05
             0.005
                             1800
                                  0.3867539 0.021166860 0.8058633 0.018717227
                             1800
## 108 0.10
             0.005
                        0
                                  0.3660274 0.014305945 0.7970936 0.023052354
## 109 0.20
             0.005
                        0
                             1800
                                  0.3431298 0.022724907 0.7945000 0.023678039
## 110 0.30
             0.005
                        0
                             1800
                                  0.3410718 0.023715061 0.8003460 0.024720129
## 111 0.01
             0.010
                        0
                             1800
                                   0.4437645 0.013777979 0.7883371 0.015501306
## 112 0.05
             0.010
                        0
                             1800
                                   0.3881028 0.023279016 0.8057542 0.019197069
## 113 0.10
             0.010
                        0
                                   0.3677815 0.012072210 0.7980814 0.025349084
## 114 0.20
             0.010
                        0
                             1800
                                   0.3516864 0.016395512 0.7929924 0.024112589
             0.010
                        0
                                   0.3354363 0.021478487 0.7968150 0.021017381
## 115 0.30
## 116 0.01
             0.050
                        0
                             1800
                                  0.4437645 0.013777979 0.7887439 0.015342614
                        0
## 117 0.05
             0.050
                             1800
                                   0.3860203 0.021352695 0.8058191 0.019154772
                        0
## 118 0.10
             0.050
                             1800
                                  0.3613560 0.016238318 0.7986472 0.025248653
                        0
## 119 0.20
             0.050
                                   0.3429626 0.020871134 0.7939703 0.023545448
## 120 0.30
             0.050
                        0
                             1800
                                   0.3435116 0.022652894 0.7973209 0.020972939
## 121 0.01
             0.100
                        0
                             1800
                                   0.4437645 0.013777979 0.7888414 0.015331579
                        0
                             1800
                                  0.3859067 0.022195282 0.8064627 0.019040327
## 122 0.05
             0.100
## 123 0.10
             0.100
                        0
                             1800
                                  0.3626835 0.016047646 0.7996072 0.022850309
## 124 0.20
             0.100
                        0
                             1800
                                  0.3470822 0.011875493 0.7961901 0.022430643
                                  0.3375910 0.018733751 0.7965280 0.019744586
## 125 0.30
             0.100
                        0
                             1800
                        5
## 126 0.01
             0.001
                             1800
                                  0.4437645 0.013777979 0.7883131 0.015401787
## 127 0.05
             0.001
                        5
                                  0.4185294 0.015184471 0.8035309 0.013806411
                        5
## 128 0.10 0.001
                             1800 0.4154400 0.012458015 0.8051049 0.014138614
```

```
## 129 0.20 0.001
                     5
                           1800 0.4107942 0.014726956 0.8033595 0.016394417
## 130 0.30 0.001
                      5
                           1800 0.4046499 0.018198233 0.7979770 0.008939835
## 131 0.01 0.005
                      5
                           1800 0.4437645 0.013777979 0.7883814 0.015458859
## 132 0.05 0.005
                      5
                           1800 0.4174985 0.014086877 0.8035957 0.014111349
                      5
## 133 0.10 0.005
                           1800 0.4144201 0.015494709 0.8052435 0.015479767
## 134 0.20 0.005
                      5
                           1800 0.4115338 0.016405299 0.8017982 0.016251374
                      5
## 135 0.30 0.005
                           1800 0.4027665 0.021082382 0.8034172 0.010682815
## 136 0.01 0.010
                      5
                          1800 0.4437645 0.013777979 0.7883371 0.015501306
## 137 0.05 0.010
                      5
                           1800 0.4174985 0.014086877 0.8042510 0.013930606
## 138 0.10 0.010
                      5
                           1800 0.4156444 0.011930234 0.8044954 0.015731661
## 139 0.20
           0.010
                      5
                           1800 0.4065506 0.014654309 0.8016072 0.016248020
                      5
                           1800 0.4011374 0.020653877 0.7984039 0.015230475
## 140 0.30 0.010
## 141 0.01
                      5
                           1800 0.4437645 0.013777979 0.7887439 0.015342614
           0.050
                      5
## 142 0.05
           0.050
                           1800 0.4166843 0.014804206 0.8032928 0.014654747
## 143 0.10 0.050
                      5
                           1800
                                0.4143769 0.017366280 0.8050385 0.014988197
                      5
## 144 0.20 0.050
                           1800 0.4050338 0.014409292 0.8028591 0.010353641
## 145 0.30 0.050
                      5
                           1800 0.4057419 0.020123531 0.8003049 0.012840485
                      5
           0.100
                           1800 0.4437645 0.013777979 0.7888414 0.015331579
## 146 0.01
## 147 0.05 0.100
                      5
                           1800 0.4174375 0.010785276 0.8035164 0.015512558
                      5
## 148 0.10 0.100
                           1800 0.4137265 0.015457852 0.8058696 0.015549654
## 149 0.20 0.100
                   5
                           1800 0.4061859 0.012503112 0.8036462 0.007516747
                   5
## 150 0.30 0.100
                          1800 0.4048464 0.017908749 0.7960404 0.012265871
```