Project 4: Causal Inference Algorithms Evaluation

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Setup

First, we set working directories, install required libraries and import the data.

```
setwd("~/GitHub/Fall2020-Project4-group-4/doc")
packages.used <- c("dplyr", "ggplot2", "WeightedROC", "rpart", "rpart.plot")</pre>
# check packages that need to be installed.
packages.needed <- setdiff(packages.used, intersect(installed.packages()[,1], packages.used))</pre>
# install additional packages
if(length(packages.needed) > 0){
   install.packages(packages.needed, dependencies = TRUE)
}
library(dplyr)
## Warning: package 'dplyr' was built under R version 4.0.3
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
       intersect, setdiff, setequal, union
##
library(ggplot2)
library(WeightedROC)
## Warning: package 'WeightedROC' was built under R version 4.0.3
library(rpart)
## Warning: package 'rpart' was built under R version 4.0.3
```

```
library(rpart.plot)

## Warning: package 'rpart.plot' was built under R version 4.0.3

df_high <- read.csv("../data/highDim_dataset.csv")

df_low <- read.csv("../data/lowDim_dataset.csv")</pre>
```

Introduction

Description

About the Data

Description

Background: Trees

Description

Cross-Validation

Description

Step 1: Set Controls and Establish Hyperparameters

Description

```
K <- 5  # number of CV folds
sample.reweight <- TRUE # run sample reweighting in model training

# setting the following to false loads data generated from a previous run

# this data is the same in each run due to a set seed

run.cv.trees_high <- FALSE # run cross-validation on the training set for trees on high dim data

run.cv.trees_low <- FALSE # run cross-validation on the training set for trees on low dim data
```

Description

Step 2: Cross-Validate the Hyperparameters

Description

Description

```
# features are the predictors: V1 - Vp
# column 1 is the response Y
# column 2 is the treatment A

feature_train_high = df_high[, -1:-2]
label_train_high = df_low[, -1:-2]
label_train_low = df_low[, -1:-2]
label_train_low = df_low[, 2]
```

High Dimensional Data Description

Low Dimensional Data Description

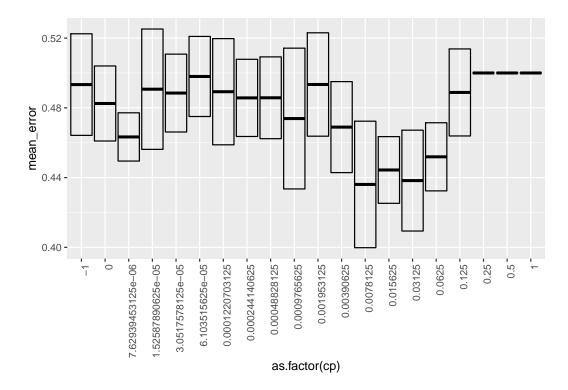
Step 3: Visualize CV Error and AUC

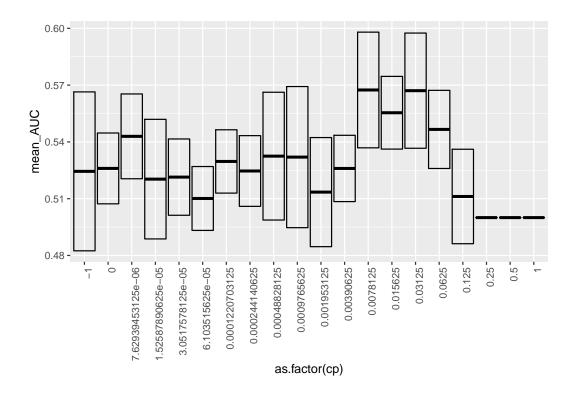
Description

High Dimensional Data Description

```
# create data frame to organize results
res_cv_trees_high <- as.data.frame(res_cv_trees_high)
colnames(res_cv_trees_high) <- c("mean_error", "sd_error", "mean_AUC", "sd_AUC")
cv_results_trees_high = data.frame(hyper_grid_trees, res_cv_trees_high)
# look at top 5 models with highest AUC
cv_results_trees_high[order(cv_results_trees_high$mean_AUC, decreasing = TRUE), ][1:5, ]</pre>
```

```
## cp mean_error sd_error mean_AUC sd_AUC
## 8 7.812500e-03 0.4360668 0.03628091 0.5674343 0.03056252
## 6 3.125000e-02 0.4382665 0.02892494 0.5670732 0.03043522
## 7 1.562500e-02 0.4443627 0.01912652 0.5554088 0.01920727
## 5 6.250000e-02 0.4519064 0.01953579 0.5466031 0.02064263
## 18 7.629395e-06 0.4633120 0.01383644 0.5429351 0.02240466
```



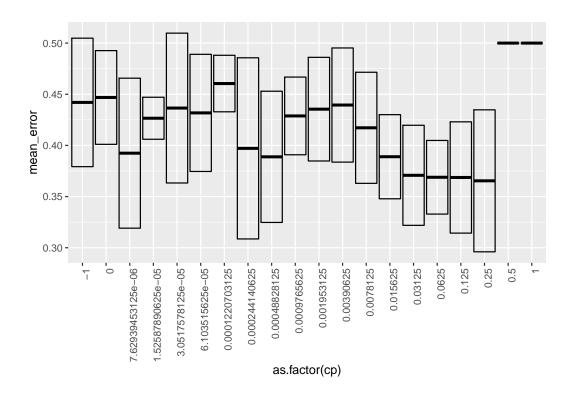


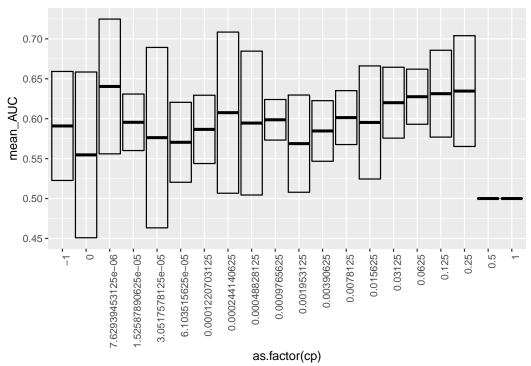
[1] 0.0078125

Low Dimensional Data Description

```
# create data frame to organize results
res_cv_trees_low <- as.data.frame(res_cv_trees_low)
colnames(res_cv_trees_low) <- c("mean_error", "sd_error", "mean_AUC", "sd_AUC")
cv_results_trees_low = data.frame(hyper_grid_trees, res_cv_trees_low)
# look at top 5 models with lowest AUC
cv_results_trees_low[order(cv_results_trees_low$mean_AUC, decreasing = TRUE), ][1:5, ]</pre>
```

```
## cp mean_error sd_error mean_AUC sd_AUC
## 18 7.629395e-06 0.3924126 0.07329778 0.6403787 0.08438962
## 3 2.500000e-01 0.3653965 0.06938198 0.6346035 0.06938198
## 4 1.250000e-01 0.3686625 0.05437925 0.6313375 0.05437925
## 5 6.250000e-02 0.3688654 0.03598451 0.6275346 0.03449488
## 6 3.125000e-02 0.3707763 0.04889355 0.6200507 0.04439815
```





[1] 7.629395e-06

Propensity Score Estimation

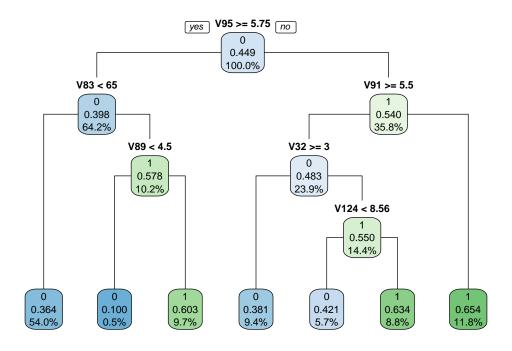
Description

```
# imbalanced dataset requires weights
# to be used in the trained model

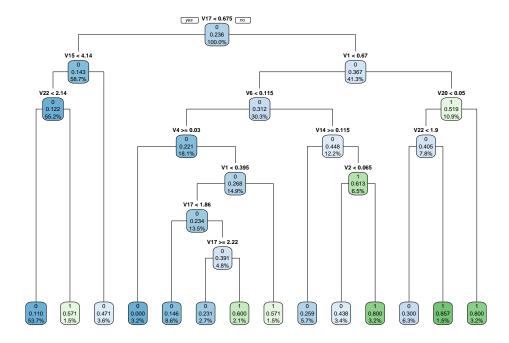
weights_high <- rep(NA, length(df_high$A))
for (v in unique(df_high$A)){
   weights_high[df_high$A == v] = 0.5 * length(df_high$A) / length(df_high$A[df_high$A == v])
}

weights_low <- rep(NA, length(df_low$A))
for (v in unique(df_low$A)){
   weights_low[df_low$A == v] = 0.5 * length(df_low$A) / length(df_low$A[df_low$A == v])
}</pre>
```

High Dimensional Data



Low Dimensional Data



ATE Estimation

Description

Stratification

Description

```
K = 5
quintiles <- seq(0, 1, by = 1/K)</pre>
```

High Dimensional Data Description

```
############ SET START TIME HERE

df_high <- cbind(df_high, prop_score_high)
quintile_values_high <- rep(NA, length(quintiles))

for (i in 1:length(quintiles)){
    quintile_values_high[i] <- quantile(prop_score_high, quintiles[i])
}

# values of quintiles for high data
quintile_values_high</pre>
```

[1] 0.1000000 0.3635523 0.3635523 0.3809524 0.6342857 0.6540084

```
df_high$quintile_class_high <- rep(NA, nrow(df_high))</pre>
# assign quintile class to each observation
for (i in 1:nrow(df_high)){
  if ((quintile_values_high[1] <= df_high$prop_score_high[i]) &</pre>
      (df_high$prop_score_high[i] < quintile_values_high[2])) {</pre>
    df_high$quintile_class_high[i] <- 1</pre>
  } else if ((quintile values high[2] <= df high$prop score high[i]) &</pre>
              (df_high$prop_score_high[i] < quintile_values_high[3])) {</pre>
    df_high$quintile_class_high[i] <- 2</pre>
  } else if ((quintile_values_high[3] <= df_high$prop_score_high[i]) &</pre>
              (df_high$prop_score_high[i] < quintile_values_high[4])) {</pre>
    df_high$quintile_class_high[i] <- 3</pre>
  } else if ((quintile_values_high[4] <= df_high$prop_score_high[i]) &</pre>
              (df_high$prop_score_high[i] < quintile_values_high[5])) {</pre>
    df_high$quintile_class_high[i] <- 4</pre>
  } else if ((quintile_values_high[5] <= df_high$prop_score_high[i]) &</pre>
              (df_high$prop_score_high[i] <= quintile_values_high[6])) {</pre>
    df_high$quintile_class_high[i] <- 5</pre>
  }
}
summary_high = expand.grid(
  A = c(0, 1),
  quintile = c(1, 2, 3, 4, 5),
  n = NA,
  prop = NA,
  avg_y = NA
for (i in 1:nrow(summary_high)) {
  subset <- df_high[(df_high$A == summary_high$A[i]) & (df_high$quintile_class_high == summary_high$qui
  summary_high$n[i] = nrow(subset)
  summary_high$prop[i] = summary_high$n[i]/nrow(df_high)
  summary_high$avg_y[i] = mean(subset$Y)
}
for (i in 1:nrow(summary_high)) {
  if (is.nan(summary_high$avg_y[i]) == TRUE) {
    summary_high$avg_y[i] <- 0</pre>
  }
}
# this table records the mean response in each quintile; needed for stratification
summary_high
##
      A quintile
                        prop
                   n
                                   avg_y
## 1 0
              1
                  9 0.0045 -1.556754
## 2 1
               1 1 0.0005 3.448809
## 3 0
               2 0 0.0000
                               0.000000
## 4 1
              2 0 0.0000
                               0.000000
```

3 688 0.3440 -13.637227

5 0

```
3 393 0.1965 -16.140803
## 6 1
## 7 0
              4 260 0.1300 -10.267325
## 8 1
             4 237 0.1185 -10.349496
## 9 0
             5 146 0.0730 -6.152075
             5 266 0.1330 -8.714239
## 10 1
quntile_prop_high <- summary_high %>% group_by(quintile) %>% summarise(sum = sum(n)/nrow(df_high))
## `summarise()` ungrouping output (override with `.groups` argument)
# this table records the proportions for each quintile; also needed for stratification
quntile_prop_high
## # A tibble: 5 x 2
   quintile sum
##
       <dbl> <dbl>
## 1
           1 0.005
## 2
           2 0
## 3
           3 0.540
           4 0.248
## 4
## 5
           5 0.206
ATE_stratification_high = quntile_prop_high$sum[1]*(summary_high$avg_y[2] - summary_high$avg_y[1]) +
  quntile_prop_high$sum[2]*(summary_high$avg_y[4] - summary_high$avg_y[3]) +
  quntile_prop_high$sum[3]*(summary_high$avg_y[6] - summary_high$avg_y[5]) +
  quntile prop high\sum [4] *(summary high\sum v[8] - summary high\sum v[7]) +
  quntile_prop_high$sum[5]*(summary_high$avg_y[10] - summary_high$avg_y[9])
ATE_stratification_high
## [1] -1.87638
############# SET END TIME HERE
```

Low Dimensional Data Description

[1] 0.0000000 0.1098039 0.1098039 0.1463415 0.3000000 0.8571429

```
df_low$quintile_class_low <- rep(NA, nrow(df_low))</pre>
# assign quintile class to each observation
for (i in 1:nrow(df low)){
  if ((quintile_values_low[1] <= df_low$prop_score_low[i]) &</pre>
       (df_low$prop_score_low[i] < quintile_values_low[2])) {</pre>
    df_low$quintile_class_low[i] <- 1</pre>
  } else if ((quintile values low[2] <= df low$prop score low[i]) &</pre>
              (df_low$prop_score_low[i] < quintile_values_low[3])) {</pre>
    df low$quintile class low[i] <- 2</pre>
  } else if ((quintile_values_low[3] <= df_low$prop_score_low[i]) &</pre>
              (df_low$prop_score_low[i] < quintile_values_low[4])) {</pre>
    df low$quintile class low[i] <- 3</pre>
  } else if ((quintile_values_low[4] <= df_low$prop_score_low[i]) &</pre>
              (df_low$prop_score_low[i] < quintile_values_low[5])) {</pre>
    df_low$quintile_class_low[i] <- 4</pre>
  } else if ((quintile_values_low[5] <= df_low$prop_score_low[i]) &</pre>
              (df_low$prop_score_low[i] <= quintile_values_low[6])) {</pre>
    df_low$quintile_class_low[i] <- 5</pre>
  }
}
summary_low = expand.grid(
  A = c(0, 1),
  quintile = c(1, 2, 3, 4, 5),
  n = NA
  prop = NA,
  avg_y = NA
for (i in 1:nrow(summary_low)) {
  subset <- df_low[(df_low$A == summary_low$A[i]) &</pre>
                      (df_low$quintile_class_low == summary_low$quintile[i]), ]
  summary_low$n[i] = nrow(subset)
  summary_low$prop[i] = summary_low$n[i]/nrow(df_low)
  summary_low$avg_y[i] = mean(subset$Y)
}
for (i in 1:nrow(summary_low)) {
  if (is.nan(summary_low$avg_y[i]) == TRUE) {
    summary_low$avg_y[i] <- 0</pre>
}
# this table records the mean response in each quintile; needed for stratification
summary_low
```

```
## A quintile n prop avg_y
## 1 0 1 15 0.03157895 18.25654
## 2 1 1 0 0.00000000 0.00000
## 3 0 2 0 0.00000000 0.00000
```

```
2 0 0.00000000 0.00000
## 4 1
## 5 0
             3 227 0.47789474 15.06273
             3 28 0.05894737 18.56302
## 6 1
## 7 0
             4 65 0.13684211 17.99996
## 8 1
             4 16 0.03368421 20.74083
## 9 0
             5 56 0.11789474 19.23768
## 10 1
             5 68 0.14315789 22.65577
quntile_prop_low <- summary_low %>% group_by(quintile) %>% summarise(sum = sum(n)/nrow(df_low))
## `summarise()` ungrouping output (override with `.groups` argument)
# this table records the proportions for each quintile; also needed for stratification
quntile_prop_low
## # A tibble: 5 x 2
##
   quintile sum
##
       <dbl> <dbl>
          1 0.0316
## 1
## 2
           2 0
          3 0.537
## 3
## 4
           4 0.171
## 5
          5 0.261
ATE_stratification_low = quntile_prop_low$sum[1]*(summary_low$avg_y[2] - summary_low$avg_y[1]) +
  quntile_prop_low$sum[2]*(summary_low$avg_y[4] - summary_low$avg_y[3]) +
  quntile_prop_low$sum[3]*(summary_low$avg_y[6] - summary_low$avg_y[5]) +
  quntile_prop_low\$sum[4]*(summary_low\$avg_y[8] - summary_low\$avg_y[7]) +
  quntile_prop_low\sum[5]*(summary_low\sum_avg_y[10] - summary_low\sum_avg_y[9])
ATE_stratification_low
## [1] 2.662275
```

Regression Adjustment

Description

High Dimensional Data Description

############# SET END TIME HERE

```
##
## Call:
## lm(formula = Y ~ A + ps_RA_high, data = high_data_ps)
## Residuals:
##
       Min
                 1Q
                     Median
                                   3Q
                                           Max
## -17.4713 -3.4878 -0.6694
                               2.7522 30.0897
##
## Coefficients: (1 not defined because of singularities)
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                5.9564
                           0.6207
                                   9.596
                                            <2e-16 ***
                           0.2569 -9.836
               -2.5271
                                            <2e-16 ***
## ps_RA_high0 -30.5718
                           1.0322 -29.617
                                            <2e-16 ***
## ps_RA_high1
                    NA
                               NA
                                       NA
                                                NA
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 5.535 on 1997 degrees of freedom
## Multiple R-squared: 0.3068, Adjusted R-squared: 0.3061
## F-statistic: 441.8 on 2 and 1997 DF, p-value: < 2.2e-16
ATE_regression_adjustment_high = pred_high$coefficients[2]
ATE regression adjustment high
##
          Α
## -2.527116
############ SET END TIME HERE
```

Low Dimensional Data Description

```
############# SET START TIME HERE
ps_RA_low <- predict(tree_low, df_low, type = "prob")</pre>
low_data_ps <- cbind(ps_RA_low, df_low)</pre>
pred_low <- lm(Y ~ A + ps_RA_low, data = low_data_ps)</pre>
summary(pred_low)
##
## Call:
## lm(formula = Y ~ A + ps_RA_low, data = low_data_ps)
##
## Residuals:
##
                  1Q
                     Median
       Min
                                     3Q
                                             Max
## -11.5153 -2.6807 -0.5655
                                1.8184 26.9282
##
## Coefficients: (1 not defined because of singularities)
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 22.5693
                            0.8535 26.445 < 2e-16 ***
## A
                3.0532
                            0.5089
                                    5.999 3.95e-09 ***
## ps_RA_low0
               -7.5200
                            1.0017 -7.507 3.04e-13 ***
## ps_RA_low1
                     NA
                                NA
                                        NA
                                                  NΑ
```

Stratification and Regression Adjustment

Description

High Dimensional Data Description

```
############# SET START TIME HERE
lm_beta_high <- rep(NA, K)</pre>
for (i in 1:K){
  subset <- df_high[df_high$quintile_class_high == i, ]</pre>
  if (nrow(subset) == 0) {
    # if the quintile is empty, let the coefficient for A automatically be O
   lm_beta_high[i] <- 0</pre>
  } else if (sum(subset$prop_score_high) == 0) {
    # if the propensity scores in the quintile are all O, let the coefficient for A automatically be O
    lm_beta_low[i] <- 0</pre>
  } else {
    # otherwise, run a linear model on the subset
    lm <- lm(Y ~ A + prop_score_high, data = subset)</pre>
    lm_beta_high[i] <- as.numeric(lm$coefficients[2])</pre>
 }
}
lm_beta_high
## [1] 5.005563 0.000000 -2.503576 -2.516297 -2.675199
ATE_stratification_regression_adjustment_high <- quntile_prop_high$sum[1]*lm_beta_high[1] +
  quntile_prop_high$sum[2]*lm_beta_high[2] +
  quntile prop high$sum[3]*lm beta high[3] +
  quntile_prop_high$sum[4]*lm_beta_high[4] +
  quntile_prop_high$sum[5]*lm_beta_high[5]
```

```
ATE_stratification_regression_adjustment_high
## [1] -2.504545
############ SET END TIME HERE
Low Dimensional Data Description
############# SET START TIME HERE
lm_beta_low <- rep(NA, 5)</pre>
for (i in 1:K){
  subset <- df_low[df_low$quintile_class_low == i, ]</pre>
  if (nrow(subset) == 0) {
    # if the quintile is empty, let the coefficient for A automatically be O
    lm_beta_low[i] <- 0</pre>
  } else if (sum(subset$prop_score_low) == 0) {
    # if the propensity scores in the quintile are all 0, let the coefficient for A automatically be 0
    lm_beta_low[i] <- 0</pre>
  } else {
    # otherwise, run a linear model on the subset
    lm <- lm(Y ~ A + prop_score_low, data = subset)</pre>
    lm_beta_low[i] <- as.numeric(lm$coefficients[2])</pre>
}
```

[1] 0.000000 0.000000 3.500291 2.452154 2.916085

```
ATE_stratification_regression_adjustment_low <- quntile_prop_low$sum[1]*lm_beta_low[1] +
   quntile_prop_low$sum[2]*lm_beta_low[2] +
   quntile_prop_low$sum[3]*lm_beta_low[3] +
   quntile_prop_low$sum[4]*lm_beta_low[4] +
   quntile_prop_low$sum[5]*lm_beta_low[5]

ATE_stratification_regression_adjustment_low
```

```
## [1] 3.058512
```

lm_beta_low

```
########## SET END TIME HERE
```

Results

 $Insert\ Comparison\ of\ ATE\ and\ all\ Runtimes\ Here\ 8\ Runtime\ values\ 6\ ATE\ estimations\ +\ 2\ true\ ATE\ create\ table\ and\ analyze\ results$

Conclusion

Description

References

Description