# Main

# Group 6

In your final repo, there should be an R markdown file that organizes all computational steps for evaluating your proposed Facial Expression Recognition framework.

This file is currently a template for running evaluation experiments. You should update it according to your codes but following precisely the same structure.

```
if(!require("EBImage")){
  source("https://bioconductor.org/biocLite.R")
  biocLite("EBImage")
if(!require("R.matlab")){
  install.packages("R.matlab")
## Warning: package 'R.matlab' was built under R version 3.6.2
if(!require("readxl")){
  install.packages("readxl")
}
if(!require("dplyr")){
  install.packages("dplyr")
}
## Warning: package 'dplyr' was built under R version 3.6.3
if(!require("readxl")){
  install.packages("readxl")
}
if(!require("ggplot2")){
  install.packages("ggplot2")
if(!require("caret")){
  install.packages("caret")
}
## Warning: package 'caret' was built under R version 3.6.2
if(!require("caTools")){
  install.packages("caTools")
}
## Warning: package 'caTools' was built under R version 3.6.2
if(!require("e1071")){
  install.packages("e1071")
```

```
## Warning: package 'e1071' was built under R version 3.6.3

library(R.matlab)
library(readxl)
library(dplyr)
library(EBImage)
library(ggplot2)
library(caret)
library(caTools)
library(e1071)

set.seed(0)
```

# Step 0 set work directories

Provide directories for training images. Training images and Training fiducial points will be in different subfolders.

```
train_dir <- "../data/train_set/"
train_image_dir <- paste(train_dir, "images/", sep="")
train_pt_dir <- paste(train_dir, "points/", sep="")
train_label_path <- paste(train_dir, "label.csv", sep="")</pre>
```

### Step 1: set up controls for evaluation experiments.

In this chunk, we have a set of controls for the evaluation experiments.

- (T/F) cross-validation on the training set
- (T/F) process features for training set
- (T/F) run evaluation on an independent test set
- (T/F) process features for test set

```
run.cv=TRUE # run cross-validation on the training set
run.feature.train=TRUE # process features for training set
run.test=TRUE # run evaluation on an independent test set
run.feature.test=TRUE # process features for test set
```

Using cross-validation or independent test set evaluation, we compare the performance of models with different specifications. This code defines the parameters that will be tested for the baseline GBM model.

```
shrinkage <- c(0.001, 0.01, 0.1)
n.minobsinnode <- c(5, 10, 15)
n.trees <- c(200, 300, 400)
param_grid <- expand.grid(shrinkage=shrinkage, n.minobsinnode=n.minobsinnode, n.trees=n.trees)</pre>
```

### Step 2: import data and train-test split

```
#train-test split
info <- read.csv(train_label_path)
n <- nrow(info)
n_train <- round(n*(4/5), 0)
train_idx <- sample(info$Index, n_train, replace = F)
test_idx <- setdiff(info$Index,train_idx)</pre>
```

We did not extract features from the images themselves, so this code chunk only determines the number of images.

```
n_files <- length(list.files(train_image_dir))

#image_list <- list()
#for(i in 1:100){
# image_list[[i]] <- readImage(pasteO(train_image_dir, sprintf("%04d", i), ".jpg"))
#}</pre>
```

Fiducial points are stored in matlab format. In this step, we read them and store them in a list.

```
#function to read fiducial points
#input: index
#output: matrix of fiducial points corresponding to the index
readMat.matrix <- function(index){
    return(round(readMat(pasteO(train_pt_dir, sprintf("%04d", index), ".mat"))[[1]],0))
}
#load fiducial points
fiducial_pt_list <- lapply(1:n_files, readMat.matrix)
#save(fiducial_pt_list, file=".../output/fiducial_pt_list.RData")</pre>
```

# Step 3: Construct features and responses

For the baseline model, we use the feature extraction from the starter code, which calculates the pairwise distances between the fiducial points.

```
source("../lib/feature.R")

tm_feature_train_base <- NA
if(run.feature.train){
   tm_feature_train_base <- system.time(dat_train <- feature(fiducial_pt_list, train_idx))
}

tm_feature_test_base <- NA
if(run.feature.test){
   tm_feature_test_base <- system.time(dat_test <- feature(fiducial_pt_list, test_idx))
}

#save(dat_train, file="../output/feature_train.RData")
#save(dat_test, file="../output/feature_test.RData")</pre>
```

# Perform PCA on features

For the advanced model, we run PCA on the features extracted in the previous step.

```
#Perform PCA analysis on training data, and transform features from training data into PCAs
start_time <- Sys.time()
dat_train_pca <- data.frame(dat_train)
dat_train_pca[,-6007] <- scale(dat_train_pca[,-6007])
pca <- preProcess(x=dat_train_pca[-6007], method="pca", thresh=0.99)
dat_train_pca <- predict(pca, dat_train_pca)
end_time <- Sys.time()
#The total advanced model feature training time is the base feature training time plus PCA time
tm_feature_train_advanced <- difftime(end_time, start_time, units="secs") + tm_feature_train_base[1]</pre>
```

```
#Transform features from test data into PCAs
start_time <- Sys.time()
dat_test_pca <- data.frame(dat_test)
dat_test_pca[,-6007] <- scale(dat_test_pca[,-6007])
dat_test_pca <- predict(pca, dat_test_pca)
end_time <- Sys.time()
#The total advanced model feature training time is the base feature training time plus PCA time
tm_feature_test_advanced <- difftime(end_time, start_time, units="secs") + tm_feature_test_base[1]</pre>
```

### Step 4: Train a classification model with training features and responses

#### Baseline model

For the baseline model, we use a GBM model.

```
source("../lib/train_gbm_mp.R")
source("../lib/test_gbm_mp.R")
```

The code below runs cross-validation for the baseline model, in order to choose the best parameters for the GBM model. (Since it takes over 24 hours to run cross-validation on all parameter combinations, we recommend keeping eval=F.)

```
source("../lib/cross_validation_gbm_mp.R")
#load("../output/feature_train.RData")
#load("../output/feature_test.RData")
#load("../output/err_cv_gbm_mp.RData")
if(run.cv){
    model_labels <- rep(NA, nrow(param_grid))
    for(i in 1:nrow(param_grid)){
        model_labels[i] <- pasteO("GBM with shrinkage = ",param_grid$shrinkage[i],", n.minobsinnode = ",par
    }
    err_cv <- matrix(0, nrow = nrow(param_grid), ncol = 2)
    for(i in 1:nrow(param_grid)){
        print(model_labels[i])
        err_cv[i,] <- cv.function(dat_train, K, param_grid$shrinkage[i], param_grid$n.minobsinnode[i], param_#save(err_cv, file="../output/err_cv_gbm_mp.RData")
}
</pre>
```

Based on the above cross-validation, choose the best parameter values. Our cross-validation found the best values to be 0.1 for shrinkage, 15 for the # of minimum observations in terminal nodes, and 400 for the # of trees.

```
if(run.cv){
   model_best <- which.min(err_cv[,1])
}
par_best <- list(shrinkage = param_grid$shrinkage[model_best], n.minobsinnode = param_grid$n.minobsinnode
#save(par_best, file="../output/par_best_gbm_mp.RData")</pre>
```

Train the model with the entire training set using the selected GBM parameters.

```
load(file="../output/par_best_gbm_mp.RData")
tm_train_base=NA
tm_train_base <- system.time(fit_train <- train(dat_train, par_best))
## Warning: package 'gbm' was built under R version 3.6.3</pre>
```

```
## Loaded gbm 2.1.5
```

```
\#save(fit\_train,\ file="../output/fit\_train\_gbm\_mp.RData")
```

#### Advanced model

For the advanced model, we use a SVM model.

The code below runs cross-validation for the advanced model, in order to choose the best cost parameter value for the SVM model.

```
c_vals <- 2^(seq(-12, -8, 0.5))
lin_tune <- tune(svm, emotion_idx~., data=dat_train_pca, kernel="linear", ranges=list(cost=c_vals), sca
c <- lin_tune$best.parameters$cost</pre>
```

Train the model with the entire training set using the selected SVM parameter.

```
tm_train_advanced=NA
tm_train_advanced <- system.time(pca_svm <- svm(emotion_idx~., data=dat_train_pca, type="C", kernel="line"
#saveRDS(pca_svm, ".../output/pca_svm_model.RDS")</pre>
```

# Step 5: Run test on test images

#### Baseline model

```
tm_test_base=NA
if(run.test){
    #load(file="../output/fit_train_gbm_mp.RData")
    tm_test_base <- system.time(pred <- test(fit_train, dat_test, par_best))
}</pre>
```

### Advanced model

```
tm_test_advanced=NA
if(run.test){
    #pca_svm <- readRDS("../output/pca_svm_model.RDS")
    tm_test_advanced <- system.time(pred_advanced <- predict(pca_svm, dat_test_pca[,-1]))
}</pre>
```

## **Evaluation**

### Baseline model

```
pred <- factor(pred, levels=1:22)
accu <- mean(dat_test$emotion_idx == pred)
cat("The accuracy of the baseline model is", accu*100, "%.\n")</pre>
```

```
## The accuracy of the baseline model is 44 %.
confusionMatrix(pred, dat_test$emotion_idx)
```

```
## Confusion Matrix and Statistics
##
##
          Reference
## Prediction 1 2 3
                   4
                      5
                         6
                           7
                              8 9 10 11 12 13 14 15 16 17 18 19 20 21 22
         1 11 0 4 2 0
                         1 0 0 0 1 0
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         2
           0 9 0 0 0 0 0 2 7 0
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            3 0 10
                   2 0 0
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                              0 0 2 0
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##
         4
            1
              0 2
                   9 1
                         1
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                              0 0 1
                                     3 2
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##
         5
            0 0 0 0 14 0 0 0 0 0 0 0 0
                                               0 1 1 1 0 0 0 0
```

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                    1
                           0
                              1
##
##
   Overall Statistics
##
##
                    Accuracy: 0.44
##
                      95% CI: (0.396, 0.4848)
##
       No Information Rate: 0.062
       P-Value [Acc > NIR] : < 2.2e-16
##
##
##
                       Kappa: 0.4133
##
    Mcnemar's Test P-Value : NA
##
##
## Statistics by Class:
##
##
                           Class: 1 Class: 2 Class: 3 Class: 4 Class: 5 Class: 6
   Sensitivity
                             0.6875
                                       0.5294
                                                 0.4000
                                                           0.4737
                                                                      0.4828
                                                                                0.4762
                             0.9773
                                       0.9731
                                                 0.9684
                                                           0.9647
                                                                      0.9936
                                                                                0.9770
  Specificity
   Pos Pred Value
                             0.5000
                                       0.4091
                                                 0.4000
                                                           0.3462
                                                                      0.8235
                                                                                0.4762
                                       0.9833
## Neg Pred Value
                                                 0.9684
                                                           0.9789
                                                                      0.9689
                             0.9895
                                                                                0.9770
## Prevalence
                             0.0320
                                       0.0340
                                                 0.0500
                                                           0.0380
                                                                      0.0580
                                                                                0.0420
## Detection Rate
                             0.0220
                                       0.0180
                                                 0.0200
                                                           0.0180
                                                                      0.0280
                                                                                0.0200
## Detection Prevalence
                             0.0440
                                       0.0440
                                                 0.0500
                                                           0.0520
                                                                      0.0340
                                                                                0.0420
## Balanced Accuracy
                                       0.7512
                                                 0.6842
                                                           0.7192
                                                                      0.7382
                                                                                0.7266
                             0.8324
##
                           Class: 7 Class: 8 Class: 9 Class: 10 Class: 11 Class: 12
## Sensitivity
                             0.6087
                                       0.7037
                                                 0.5357
                                                            0.3125
                                                                        0.4643
                                                                                   0.3214
                                                 0.9915
                                                                        0.9703
## Specificity
                             0.9811
                                       0.9852
                                                            0.9793
                                                                                   0.9746
## Pos Pred Value
                             0.6087
                                       0.7308
                                                 0.7895
                                                            0.3333
                                                                        0.4815
                                                                                   0.4286
                                                 0.9730
                                                            0.9773
## Neg Pred Value
                             0.9811
                                       0.9831
                                                                        0.9683
                                                                                   0.9603
## Prevalence
                                       0.0540
                                                 0.0560
                                                            0.0320
                                                                                   0.0560
                             0.0460
                                                                        0.0560
## Detection Rate
                             0.0280
                                       0.0380
                                                 0.0300
                                                            0.0100
                                                                        0.0260
                                                                                   0.0180
## Detection Prevalence
                             0.0460
                                       0.0520
                                                 0.0380
                                                            0.0300
                                                                        0.0540
                                                                                   0.0420
  Balanced Accuracy
                             0.7949
                                       0.8445
                                                 0.7636
                                                            0.6459
                                                                        0.7173
                                                                                   0.6480
##
                           Class: 13 Class: 14 Class: 15 Class: 16 Class: 17
                                                     0.4118
                                                                0.4167
                                                                           0.4348
## Sensitivity
                              0.2000
                                         0.8636
## Specificity
                              0.9625
                                         0.9707
                                                     0.9834
                                                                0.9916
                                                                           0.9581
## Pos Pred Value
                              0.1818
                                         0.5758
                                                     0.4667
                                                                0.7143
                                                                           0.3333
## Neg Pred Value
                              0.9665
                                         0.9936
                                                    0.9794
                                                                0.9712
                                                                           0.9723
```

```
0.0400
                                      0.0440
## Prevalence
                                                 0.0340
                                                           0.0480
                                                                      0.0460
## Detection Rate
                            0.0080
                                      0.0380
                                                 0.0140
                                                           0.0200
                                                                      0.0200
                                      0.0660
                                                                      0.0600
## Detection Prevalence
                            0.0440
                                                 0.0300
                                                           0.0280
                                                           0.7041
## Balanced Accuracy
                            0.5813
                                      0.9172
                                                 0.6976
                                                                      0.6964
                         Class: 18 Class: 19 Class: 20 Class: 21 Class: 22
## Sensitivity
                            0.4211
                                      0.2258
                                                           0.3913
                                                 0.1818
                                                                      0.1818
## Specificity
                            0.9667
                                      0.9765
                                                 0.9477
                                                           0.9560
                                                                      0.9644
## Pos Pred Value
                                                           0.3000
                            0.3333
                                      0.3889
                                                 0.1379
                                                                      0.1905
## Neg Pred Value
                            0.9769
                                      0.9502
                                                 0.9618
                                                           0.9702
                                                                      0.9624
## Prevalence
                            0.0380
                                      0.0620
                                                 0.0440
                                                           0.0460
                                                                      0.0440
## Detection Rate
                            0.0160
                                      0.0140
                                                 0.0080
                                                           0.0180
                                                                      0.0080
## Detection Prevalence
                                      0.0360
                                                 0.0580
                                                           0.0600
                                                                      0.0420
                            0.0480
## Balanced Accuracy
                            0.6939
                                      0.6012
                                                 0.5648
                                                           0.6736
                                                                      0.5731
```

#### Advanced model

##

```
pred_advanced <- factor(pred_advanced, levels=1:22)
accu_advanced <- mean(dat_test$emotion_idx == pred_advanced)
cat("The accuracy of the advanced model is", accu_advanced*100, "%.\n")</pre>
```

## The accuracy of the advanced model is 52.2 %.

```
confusionMatrix(pred_advanced, dat_test$emotion_idx)
```

```
## Confusion Matrix and Statistics
##
##
              Reference
## Prediction 1
                    2 3
                          4
                              5
                                 6
                                     7
                                        8
                                           9 10 11 12 13 14 15 16 17 18 19 20 21 22
               13
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##
## Overall Statistics
##
##
                    Accuracy: 0.522
```

95% CI: (0.4772, 0.5665)

```
##
       No Information Rate: 0.062
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
                     Kappa: 0.4993
##
   Mcnemar's Test P-Value : NA
##
## Statistics by Class:
##
##
                         Class: 1 Class: 2 Class: 3 Class: 4 Class: 5 Class: 6
## Sensitivity
                           0.8125
                                    0.7059
                                             0.4400
                                                       0.5789
                                                                0.6897
                                                                         0.4286
## Specificity
                                    0.9896
                                             0.9747
                                                       0.9522
                                                                0.9979
                                                                         0.9687
                           0.9773
                           0.5417
## Pos Pred Value
                                    0.7059
                                             0.4783
                                                       0.3235
                                                                0.9524
                                                                         0.3750
## Neg Pred Value
                           0.9937
                                    0.9896
                                             0.9706
                                                       0.9828
                                                                0.9812
                                                                         0.9748
## Prevalence
                                             0.0500
                                                       0.0380
                                                                0.0580
                           0.0320
                                    0.0340
                                                                         0.0420
## Detection Rate
                           0.0260
                                    0.0240
                                             0.0220
                                                       0.0220
                                                                0.0400
                                                                         0.0180
## Detection Prevalence
                           0.0480
                                    0.0340
                                             0.0460
                                                       0.0680
                                                                0.0420
                                                                         0.0480
                           0.8949
                                    0.8478
                                             0.7074
                                                       0.7656
                                                                0.8438
                                                                         0.6986
## Balanced Accuracy
##
                        Class: 7 Class: 8 Class: 9 Class: 10 Class: 11 Class: 12
## Sensitivity
                           0.6087
                                    0.7778
                                             0.7500
                                                        0.3125
                                                                  0.4286
                                                                             0.4286
## Specificity
                           0.9895
                                    0.9915
                                             0.9873
                                                        0.9690
                                                                  0.9809
                                                                            0.9831
## Pos Pred Value
                                             0.7778
                           0.7368
                                    0.8400
                                                        0.2500
                                                                  0.5714
                                                                            0.6000
## Neg Pred Value
                                    0.9874
                                             0.9852
                                                        0.9771
                                                                  0.9666
                                                                             0.9667
                           0.9813
## Prevalence
                           0.0460
                                    0.0540
                                             0.0560
                                                        0.0320
                                                                  0.0560
                                                                             0.0560
## Detection Rate
                           0.0280
                                    0.0420
                                             0.0420
                                                        0.0100
                                                                  0.0240
                                                                             0.0240
## Detection Prevalence
                           0.0380
                                    0.0500
                                             0.0540
                                                        0.0400
                                                                  0.0420
                                                                             0.0400
                                                                             0.7058
## Balanced Accuracy
                           0.7991
                                    0.8847
                                             0.8686
                                                        0.6408
                                                                  0.7048
                         Class: 13 Class: 14 Class: 15 Class: 16 Class: 17
## Sensitivity
                            0.3500
                                      0.8182
                                                0.5882
                                                           0.7083
                                                                     0.3478
                            0.9625
## Specificity
                                      0.9749
                                                0.9834
                                                           0.9832
                                                                     0.9769
## Pos Pred Value
                            0.2800
                                      0.6000
                                                0.5556
                                                           0.6800
                                                                     0.4211
## Neg Pred Value
                            0.9726
                                      0.9915
                                                0.9855
                                                           0.9853
                                                                     0.9688
## Prevalence
                            0.0400
                                      0.0440
                                                0.0340
                                                           0.0480
                                                                     0.0460
                            0.0140
## Detection Rate
                                      0.0360
                                                0.0200
                                                           0.0340
                                                                     0.0160
## Detection Prevalence
                            0.0500
                                      0.0600
                                                0.0360
                                                           0.0500
                                                                     0.0380
## Balanced Accuracy
                            0.6562
                                      0.8965
                                                0.7858
                                                           0.8458
                                                                     0.6624
##
                         Class: 18 Class: 19 Class: 20 Class: 21 Class: 22
                                      0.2903
                                                           0.4783
## Sensitivity
                            0.5789
                                                0.2727
                                                                     0.1364
## Specificity
                                                0.9791
                                                           0.9581
                            0.9584
                                      0.9829
                                                                     0.9791
## Pos Pred Value
                                      0.5294
                                                0.3750
                                                           0.3548
                                                                     0.2308
                            0.3548
## Neg Pred Value
                            0.9829
                                      0.9545
                                                0.9669
                                                           0.9744
                                                                     0.9610
## Prevalence
                            0.0380
                                      0.0620
                                                0.0440
                                                           0.0460
                                                                     0.0440
## Detection Rate
                            0.0220
                                      0.0180
                                                0.0120
                                                           0.0220
                                                                     0.0060
## Detection Prevalence
                            0.0620
                                      0.0340
                                                0.0320
                                                           0.0620
                                                                     0.0260
## Balanced Accuracy
                            0.7687
                                      0.6366
                                                0.6259
                                                           0.7182
                                                                     0.5577
Summarize Running Time
cat("Baseline model: Time for constructing training features=", tm_feature_train_base[1], "s \n")
## Baseline model: Time for constructing training features= 1.66 s
cat("Baseline model: Time for constructing testing features=", tm_feature_test_base[1], "s \n")
```

## Baseline model: Time for constructing testing features= 0.14 s

```
cat("Baseline model: Time for training model=", tm_train_base[1], "s \n")

## Baseline model: Time for training model= 1497.7 s

cat("Baseline model: Time for testing model=", tm_test_base[1], "s \n")

## Baseline model: Time for testing model= 15.64 s

cat("Advanced model: Time for constructing training features=", tm_feature_train_advanced, "s \n")

## Advanced model: Time for constructing training features= 78.54291 s

cat("Advanced model: Time for constructing testing features=", tm_feature_test_advanced, "s \n")

## Advanced model: Time for constructing testing features= 2.89789 s

cat("Advanced model: Time for training model=", tm_train_advanced[1], "s \n")

## Advanced model: Time for training model= 4.01 s

cat("Advanced model: Time for testing model=", tm_test_advanced[1], "s \n")

## Advanced model: Time for testing model= 0.38 s

###Reference - Du, S., Tao, Y., & Martinez, A. M. (2014). Compound facial expressions of emotion.

Proceedings of the National Academy of Sciences, 111(15), E1454-E1462.
```