0. Introduction of the Problem:

Machine Learning Fairness:

Machine Learning classifiers are increasingly being used to assit decision makings, however, it is quite possible that the classifier makes decisions for people belonging to different social groups with different misclassification rates (e.g. misclassification rates for females are higher than males), thereby placing these groups at an unfair advantage. In this problem, we implement the methods introduced by Fairness Beyond Disparate Treatment & Disparate Impact: Learning Classification without Disparate Mistreatment to avoid such unfairness. To evaluate the performance of the classifiers implemented, accuracy and calibration are used as two main metrics.

DM model explained:

Since there is a lot of fairness notion and that only one notion can be tackled at once, we should elaborate on the main notion we are tackling here. It is the disparate mistreatment we are trying to avoid. This notion of fairness can be partitioned into several sub-notions:

Overall Missclassification (OMR):

$$P[\hat{y} \neq y | z = 0] = P[\hat{y} \neq y | z = 1]$$

• False Negative Rate (FNR):

$$P[\hat{y} \neq y | z = 0, y = 0] = P[\hat{y} \neq y | z = 1, y = 0]$$

False Positive Rate (FPR):

$$P[\hat{y} \neq y | z = 0, y = 1] = P[\hat{y} \neq y | z = 1, y = 1]$$

where $z \in \{0, 1\}$ corresponds to our sensitive feature and $y \in \{0, 1\}$ is the target.

Suppose now we want to tackle the Dipsarate Mistreatment in the FNR. Let $l_w(X,y)$ be the loss of our classifier where X corresponds to the selected features, than we would like to solve the following problem :

$$\min_{w \in \mathcal{R}^d} l_w(X, y)$$
 subject to
$$P[\hat{y}_w \neq y | z = 0, y = 0] - P[\hat{y}_w \neq y | z = 1, y = 0] \leq c$$

$$P[\hat{y}_w \neq y | z = 0, y = 0] - P[\hat{y}_w \neq y | z = 1, y = 0] \geq -c$$

But as explain Zafar et al (https://arxiv.org/pdf/1610.08452.pdf) in their paper, this problem can not be solved easily and instead they proceed to estimate the covariance between the sensitive feature z and the signed distance $g_w(X)$ between the feature vectors of misclassified users and the classifier decision boundary as a way to tackle disparate mistreatment:

$$Cov(z, g_w(X)) \approx \frac{1}{N} \sum_{y, X, z \in D} (z - \overline{z}) g_w(y, X)$$

The signed distance $g_w(X)$ between the feature vectors of misclassified users and the classifier decision boundary depends on the disparate mistreatment you want to tackle as well as the boundary decision of your classifier:

For instance for OMR:

$$g_w^{OMR}(y, X) = \min(0, (2y - 1)d_w(X))$$

• For FNR:

$$g_w^{FNR}(y, X) = \min(0, (1 - y)(2y - 1)d_w(X))$$

• For FPR:

$$g_w^{FPR}(y, X) = \min(0, y(2y - 1)d_w(X))$$

For linear model, the boundary decision is $d_w(X) = Xw$ resulting that $g_w(y,X)$ is a concave function. This information is crucial because it will allow us to solve the DM problem using Convex-Concave solver. Indeed the resulting problem can be formulated as the following in spliting z into z=0 and z=1:

$$\min_{w \in \mathcal{R}^d} l_w(X, y)$$
subject to
$$-\frac{N_1}{N} \sum_{X, y \in D_0} g_w(X, y) + \frac{N_0}{N} \sum_{X, y \in D_I} g_w(X, y) \le c$$

$$-\frac{N_1}{N} \sum_{X, y \in D_0} g_w(X, y) + \frac{N_0}{N} \sum_{X, y \in D_I} g_w(X, y) \ge -c$$

This problem is Convex-Concave and can be solved using DCCP

(https://arxiv.org/pdf/2106.00772.pdf). This DCCP solver was implemented but a more robust version using the package DCCP developed in the paper is also used. Finally, for a logistic regression we end up solving the following Convex-Concave optimization problem:

$$\min_{w \in \mathcal{R}^d} \frac{\frac{1}{N} \sum_{X,y \in \mathcal{D}} \log(1 + e^{Xw}) - yXw}{\text{subject to}}$$

$$-\frac{N_1}{N} \sum_{X,y \in \mathcal{D}_0} g_w(X,y) + \frac{N_0}{N} \sum_{X,y \in \mathcal{D}_1} g_w(X,y) \le c$$

$$-\frac{N_1}{N} \sum_{X,y \in \mathcal{D}_0} g_w(X,y) + \frac{N_0}{N} \sum_{X,y \in \mathcal{D}_1} g_w(X,y) \ge -c$$

Loading the used packages

```
In [2]: #Loading the desired packages
!pip install dccp
import pandas as pd
import numpy as np
from sklearn.model_selection import train_test_split
import cvxpy as cp
import dccp
import matplotlib.pyplot as plt
from IPython.core.display import display, HTML
import warnings
warnings.filterwarnings('ignore')
```

```
Requirement already satisfied: dccp in /usr/local/lib/python3.7/dist-packages (1.0.4)
Requirement already satisfied: cvxpy>=0.3.5 in /usr/local/lib/python3.7/dist-packages
(from dccp) (1.0.31)
Requirement already satisfied: osqp>=0.4.1 in /usr/local/lib/python3.7/dist-packages (f
rom cvxpy>=0.3.5->dccp) (0.6.2.post0)
Requirement already satisfied: scipy>=1.1.0 in /usr/local/lib/python3.7/dist-packages
(from \ cvxpy \ge 0.3.5 - dccp) \ (1.4.1)
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(from \ cvxpy \ge 0.3.5 - > dccp) \ (0.70.12.2)
Requirement already satisfied: numpy>=1.15 in /usr/local/lib/python3.7/dist-packages (f
rom cvxpy \ge 0.3.5 - dccp (1.21.5)
Requirement already satisfied: ecos>=2 in /usr/local/lib/python3.7/dist-packages (from
cvxpy \ge 0.3.5 - dccp (2.0.10)
Requirement already satisfied: scs>=1.1.3 in /usr/local/lib/python3.7/dist-packages (fr
om cvxpy \ge 0.3.5 - dccp (3.2.0)
Requirement already satisfied: qdldl in /usr/local/lib/python3.7/dist-packages (from os
qp \ge 0.4.1 - cvxpy \ge 0.3.5 - dccp (0.1.5. post0)
Requirement already satisfied: dill>=0.3.4 in /usr/local/lib/python3.7/dist-packages (f
```

```
In []: !git init !git pull https://clement-micol:ghp_1SH1s2JBjx2GSYVRCXjpd7xwoFnlaG34DxZW@github.com/TZstat
```

1. Data Processing:

rom multiprocess- $\langle \text{cvxpy} \rangle = 0.3.5 - \langle \text{dccp} \rangle$ (0.3.4)

Loading the data:

In [6]: data = pd. read_csv("/content/data/compas-scores-two-years.csv") data

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	id	name	first	last	compas_screening_date	sex	dob	age	age_cat
0	1	miguel hernandez	miguel	hernandez	2013-08-14	Male	1947- 04-18	69	Greater than 45
1	3	kevon dixon	kevon	dixon	2013-01-27	Male	1982- 01-22	34	25 - 45
2	4	ed philo	ed	philo	2013-04-14	Male	1991- 05-14	24	Less than 25
3	5	marcu brown	marcu	brown	2013-01-13	Male	1993- 01-21	23	Less than 25
4	6	bouthy pierrelouis	bouthy	pierrelouis	2013-03-26	Male	1973- 01-22	43	25 - 45
7209	10996	steven butler	steven	butler	2013-11-23	Male	1992- 07-17	23	Less than 25
7210	10997	malcolm simmons	malcolm	simmons	2014-02-01	Male	1993- 03-25	23	Less than 25
7211	10999	winston gregory	winston	gregory	2014-01-14	Male	1958- 10-01	57	Greater than 45
7212	11000	farrah jean	farrah	jean	2014-03-09	Female	1982- 11-17	33	25 - 45
7213	11001	florencia sanmartin	florencia	sanmartin	2014-06-30	Female	1992 - 12-18	23	Less than 25

7214 rows × 53 columns

Selecting the relevant features:

```
In [7]: # Select only Caucasian and African-American as our sensitive feature
    data = data[data["race"].isin(["Caucasian", "African-American"])]

#Calculate length of stay
    data["length_stay"] = pd. to_datetime(data["c_jail_out"]) - pd. to_datetime(data['c_jail_in'
        data["length_stay"] = data["length_stay"].apply(lambda x: x.days)
        data = data.drop(columns = ["c_jail_in", "c_jail_out"])
        data['length_stay'] = data["length_stay"].apply(lambda x: 0 if x <= 7 else x)
        data['length_stay'] = data["length_stay"].apply(lambda x: 1 if 7< x <= 90 else x)
        data['length_stay'] = data["length_stay"].apply(lambda x: 2 if 90 < x <= 180 else x)
        data['length_stay'] = data["length_stay"].apply(lambda x: 3 if x > 180 else x)
```

```
In [8]: # Select the features to predict the target y
X = data[["sex", "age_cat", "priors_count.1", "c_charge_degree", "length_stay", "race"]]
y = data["two_year_recid"]

# Encode the categorical_features
for categorical_feature in ["sex", "age_cat", "c_charge_degree", "length_stay", "race"]:
    categorical_variable = pd. get_dummies(X[categorical_feature]).iloc[:,0]
X = pd. concat([X, categorical_variable], axis=1)
X = X. drop(categorical_feature, axis=1)
X = X. rename(columns={list(X)[-1]:categorical_feature})
```

Constructing our training and test set:

```
In [ ]: # Construct the training and test set
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=1/5, random_state=42)
```

2. Implementing the Fairness model:

Defining the logistic loss:

Implementing the DM model (<u>Fairness Beyond Disparate Treatment & Disparate Impact: Learning Classification without Disparate Mistreatment (https://arxiv.org/pdf/1610.08452.pdf)</u>):

```
In []: class boundary decision:
              This class compute the boundary decision as
              defined in the paper for different decision
              Parameters:
              decision: str
                  name of the missclassification measure tackled
                  choice in ("OMR", "FPR", "FNR")
          , , ,
          def __init__(self, decision="OMR"):
            self.decision = decision
          def __call__(self, X, y, weight):
            Return the boundary decision (g theta in the paper) according to the
            missclassification measure we want to tackled
            Parameters:
            X: arrays
                Training features
            y : arrays
                Training target
            weight: array of size num features
                The weight of our logistic regression model
            if self. decision == "OMR":
              return cp. minimum(0, cp. multiply((2*y-1), (X @ weight)))
            if self.decision == "FPR":
              return cp. minimum(0, cp. multiply((1-y)*(2*y-1), (X @ weight)))
            if self. decision == "FNR":
              return cp. minimum (0, \text{ cp. multiply } (y*(2*y-1), (X @ \text{ weight})))
          def convexified(self, X, y, weight, new_weight):
            Return the linearized boundary decision around an input weight according to the
            missclassification measure we want to tackled
            Parameters:
             _____
            X : arrays
                Training features
            y : arrays
                Training target
            weight: array of size num features
                 The weight around which the boundary decision is
                 linearized
            new weight: array of size num features
                 The weight in which we want to evaluate the
                 convexified boundary decision
```

```
if self.decision == "OMR":
    dirac = (2*y-1)*(X @ weight) <= 0
    return self(X, y, weight) + cp. multiply(y*dirac, (X @ (new_weight-weight)))

if self.decision == "FPR":
    dirac = (1-y)*(2*y-1)*(X @ weight) <= 0
    return self(X, y, weight) + cp. multiply(dirac*(1-y)*(2*y-1), X @ (new_weight-weight))

if self.decision == "FNR":
    dirac = y*(2*y-1)*(X @ weight) <= 0
    return self(X, y, weight) + cp. multiply(dirac*y*(2*y-1), X @ (new_weight-weight))</pre>
```

```
In []: class DM DMsen:
                This class compute a default solver
                to get train a classifier without disparate treatment.
                Only logistic classifier was implemented yet but new implementation
                can be seen by changing the loss.
                . . .
                Parameters:
                X: arrays
                    Training features
                y : arrays
                    Training target
                weight: array of size num features
                    Initial weight of our logistic regression model
                method : str
                    name of the missclassification measure tackled
                    choice in ("OMR", "FPR", "FNR")
                algo: str
                    choice of the algorithm to use between ("DM" and "DM-sen")
                validation: bool
                    choice of spliting the training set into
                    train and validation to evaluate the training
                    (Only useful when running solver build from scratch)
                Hyperparameters:
                c: float
                    Lower-upper bound of the constraint in the DM formulation
                tau : float
                    Initial penalization constant of the slack variables in the CCP solver
                mu : float
                    At each iteration of the solver, we increase tau by tau*mu
                Methods:
                solve subproblem:
                    This function is call by the CCP solver build from scratch.
                    Solve the subproblem as defined in the CCP solver.
                solve:
                    CCP solver build from scratch based on the proposed algorithm
                solve DCCP :
                    Solve the DM formulation using the DCCP package
                predict:
                    Compute the prediction of our logistic regression model using
                    the resulting weights.
                accuracy:
                    Return the accuracy of our model by computing
                    the average number of TPR and TNR over the
                    data set [X_test, y_test]
            def __init__(self, X, y, c=0.1, tau=0.1, mu=10, algo = "DM", method="OMR", validation
```

```
if algo == "DM-sen":
        self.X = X
    elif algo == "DM":
        self. X = X[:, 0:5]
    self.y = y
    self.c = cp. Parameter(value=c)
    if weight is None:
        self.weight = np.zeros(self.X.shape[1])
    else:
        self. weight = weight
    self. tau = tau
    self.history = {"loss": [], "accuracy": [], "DFNR": [], "DFPR": []}
    self. weight k = cp. Variable(self. X. shape[1], value = self. weight)
    self.z = X[:,-1]
    if method == "FNR+FPR":
        self. si = cp. Variable (4, nonneg=True)
        self.g = boundary decision("FPR")
        self.g_second = boundary_decision("FNR")
    else:
        self. si = cp. Variable (2, nonneg=True)
        self.g = boundary_decision(method)
    self.mu = mu
    self.algo = algo
    self. val = validation
def solve subproblem(self):
    This function is call by the CCP solver build from scratch.
    Solve the subproblem as defined in the CCP solver.
    N = len(self.z)
    N1 = sum(self.z)
    N0 = N-N1
    constraints = [
                        -N1/N*cp. sum(cp. multiply(self. z==0, self. g(self. X, self. y, self. weight k))) + N(self. y, self. weight k))) + N(self. y, self. weight k))) + N(self. y, self. y, self. weight k))) + N(self. y, self. y, self. weight k))) + N(self. y, self. y, self. y, self. weight k))) + N(self. y, self. y, self. weight k))) + N(self. y, self. weight k))) + N(self. y, self. y, sel
                        -N0/N*cp. sum(cp. multiply(self. z==1, self. g(self. X, self. y, self. weight k)))+ N
    1
    try:
        constraints.extend([
                                                      -N1/N*cp.sum(cp.multiply(self.z==0, self.g_second(self.X, self.y)
                                                     -N0/N*cp. sum(cp. multiply(self. z==1, self. g second(self. X, self. y)
    except AttributeError :
        pass
    loss = logistic_loss(self. X, self. y, self. weight_k)
    obj = cp. Minimize(loss+self. tau*cp. sum(self. si))
    prob = cp. Problem(obj, constraints=constraints)
    res = prob. solve(warm start = True)
    self. history ["loss"]. append (res)
    self. history["accuracy"]. append(self. accuracy(self. X, self. y))
    self.history["DFPR"].append(DFPR(self, self. X, self. y, self. z))
    self. history["DFNR"]. append(DFNR(self, self. X, self. y, self. z))
def predict(self, X test):
    Compute the prediction of our logistic regression model using
    the resulting weights.
```

```
Parameters:
    X test : array
              New set of features on which we make our prediction
    if self.algo == "DM":
        X_{test} = X_{test}[:, 0:5]
    prob = np. exp(X_test @ self. weight_k. value) / (1+np. exp(X_test @ self. weight_k. value))
    return np. vectorize (lambda p: int (p>=0.5)) (prob)
def accuracy(self, X_val, y_val):
    Return the accuracy of our model by computing
    the average number of TPR and TNR over the
    data set [X val, y val]
    Parameters:
    X_val : array
              Set of features on which we want to evaluate the accuracy
              of our model
    y val : array
             The target we are trying to reach when evaluating our model
    y hat = self.predict(X val)
    return np. sum(y_hat==y_val)/len(y_val)
def solve(self, T):
    CCP solver build from scratch based on the proposed algorithm
    Parameters:
    T: int
              Number of iteration the solver is run.
              Should we replace it by a termination criterion?
    for i in range(T):
         # We split the data into a training and validation set at each step
         if self.val:
              self. X, X_val, self. y, y_val, self. z, z_val = train_test_split(self. X, self. y, 
         self. solve subproblem()
         self.tau = np.minimum(self.tau*self.mu, 1)
         self.weight = self.weight_k.value
         if self.val:
              print("epoch {} - norm(s) {} :: 3f} - accuracy {} :: 3f} - val accuracy {} :: 3f} - val D
              self. X = np. concatenate([self. X, X_val])
              self. y = np. concatenate([self. y, y val])
              self.z = np. concatenate([self.z, z_val])
def solve DCCP(self):
    Solve the DM formulation using the DCCP package
    if self. val:
```

```
self. X, X_val, self. y, y_val, self. z, z_val = train_test_split(self. X, self. y, self.
N = len(self.z)
N1 = sum(self.z)
NO = N-N1
constraints = [
         -N1/N*cp. sum(cp. multiply(self. z==0, self. g(self. X, self. y, self. weight_k))) <=
         -NO/N*cp. sum(cp. multiply(self. z==1, self. g(self. X, self. y, self. weight_k))) <=
try:
  constraints.extend([
                       -N1/N*cp. sum(cp. multiply(self. z==0, self. g_second(self. X, self. y)
                       -NO/N*cp. sum(cp. multiply(self. z==1, self. g_second(self. X, self. y
except AttributeError :
  pass
loss = logistic loss(self. X, self. y, self. weight k)
obj = cp. Minimize(loss)
prob = cp. Problem(obj, constraints=constraints)
result = prob. solve(method='dccp', warm_start=True)
if self. val:
  print(prob. status)
  print ("accuracy {:.3f} - val accuracy {:.3f} - val DFPR {:.3f} - val DFNR {:.3f}".
  self. X = np. concatenate([self. X, X val])
  self.y = np.concatenate([self.y,y val])
  self. z = np. concatenate([self. z, z_val])
```

Evaluation:

Computing the metrics to evaluate our model:

```
In [ ]: | def DFPR(model, X_val, y_val, z_val):
               Compute the Difference of False Positive
               Rate in the validation set [X val, y val, z val]
                of the model.
                Parameters:
               model: the predicting model
                It should have a predict method!
               X val : array
               The set of feature to evaluate the DFPR
               y val : array
               The target to evaluate the DFPR
               z_val : array
               The sensitive feature to evaluate the DFPR
               X \text{ val } 0 = X \text{ val}[(z \text{ val}==0) \& (y \text{ val}==0)]
                y hat 0 = model.predict(X val 0)
                y \ val \ 0 = y \ val[(z \ val==0) \& (y \ val==0)]
               p1 = np. sum(y_hat_0!=0) / len(y_hat_0)
               X \text{ val } 1 = X \text{ val}[(z \text{ val}==1) \& (y \text{ val}==0)]
                y hat 1 = model.predict(X val 1)
               y_{val_1} = y_{val}[(z_{val}==1) & (y_{val}==0)]
               p2 = np. sum(y hat 1!=0)/len(y hat 1)
               return p1-p2
         def DFNR (model, X val, y val, z val):
               Compute the Difference of False Negative
               Rate in the validation set [X_val, y_val, z_val]
                of the model.
               Parameters:
               model: the predicting model
                It should have a predict method!
               X_val : array
               The set of feature to evaluate the DFPR
               y_val : array
               The target to evaluate the DFPR
               z val: array
               The sensitive feature to evaluate the DFPR
               X_{val_0} = X_{val}[(z_{val}==0) & (y_{val}==1)]
               y hat 0 = model.predict(X val 0)
                y_val_0 = y_val[(z_val==0)&(y_val==1)]
               p1 = np. sum(y_hat_0!=1)/1en(y_hat_0)
```

```
X_{val_1} = X_{val}[(z_{val}==1) & (y_{val}==1)]
      y_hat_1 = model.predict(X_val_1)
      y_{val_1} = y_{val}[(z_{val}=1) & (y_{val}=1)]
      p2 = np. sum(y_hat_1!=1)/len(y_hat_1)
      return p1-p2
def calibration(model, X_val, y_val, z_val):
      Compute the calibration in the validation set [X_val, y_val, z_val]
      of the model.
      Parameters:
      model: the predicting model
      It should have an accuracy/score method!
      X val : array
      The set of feature to evaluate the DFPR
      y val : array
      The target to evaluate the DFPR
      z_val : array
      The sensitive feature to evaluate the DFPR
      X \text{ val } 0 = X \text{ val}[z \text{ val}==0]
      y val 0 = y val[z val==0]
      try:
        p1 = model.accuracy(X val 0, y val 0)
      except AttributeError:
        p1 = model. score(X_val_0, y_val_0)
      X \text{ val } 1 = X \text{ val}[z \text{ val}==1]
      y_val_1 = y_val[z_val==1]
      try:
        p2 = model.accuracy(X_val_1, y_val_1)
      except AttributeError:
        p2 = model.score(X_val_1, y_val_1)
      return p1-p2
```

Evaluation of the DM/DM-sen algorithm:

For the baseline regression:

```
In []: from sklearn.linear model import LogisticRegression
                        model = LogisticRegression(random state=42).fit(X train, y train)
                        score logistic = {"accuracy" : model.score(X test, y test),
                                                                            "DFNR": DFNR(model, X_test, y_test, X_test.iloc[:,-1]),
                                                                             "DFPR" : DFPR(model, X test, y test, X test.iloc[:,-1]),
                                                                            "calibration" : calibration(model, X test, y test, X test.iloc[:,-1])
                        print(pd. Series(score logistic))
                                                                    0.627642
                        accuracy
                        DFNR
                                                                    0.366570
                        DFPR
                                                                 -0.258211
                                                                   0.030596
                        calibration
                        dtype: float64
In [ ]: # Calculate the covariance of the unconstrained classifier
                        # to get an upper bound of the hy
                        d = 2*model.predict proba(X train)[:,1]-1
                        z = X_{train.iloc[:,-1].to_numpy()
                        z_{hat} = np. mean(z)
                        print("Covariance OMR: ", np. mean((z-z \text{ hat})*np. \min \min(0, (2*y \text{ train. to numpy})-1)*d)))
                         print("Covariance FNR : ", np. mean((z-z_hat)*np. minimum(0, (1-y_train. to_numpy())*(2*y_train. to
                        print("Covariance FPR: ", np. mean((z-z hat)*np. minimum(0, (y train. to numpy())*(2*y train. t
                        Covariance OMR: 0.004048143425567252
                        Covariance FNR : -0.006192004580140546
                        Covariance FPR: 0.010240148005707798
```

For the OMR constraints:

```
In [ ]: |
         score OMR = \{\}
         solver = DM DMsen(X train. to numpy(), y train. to numpy(), method="OMR", c=0.002)
         solver.solve DCCP()
         score OMR["acc"] = [solver.accuracy(X test.to numpy(), y test.to numpy())]
         score_OMR["DFNR"] = [DFNR(solver, X_test.to_numpy(), y_test.to_numpy(), X_test.to_numpy()[
         score OMR["DFPR"] = [DFPR(solver, X test. to numpy(), y test. to numpy(), X test. to numpy()[
         score OMR["cal"] = [calibration(solver, X test. to numpy(), y test. to numpy(), X test. to numpy
         solver = DM DMsen(X train.to numpy(), y train.to numpy(), method="OMR", algo="DM-sen", c=0.
         solver.solve DCCP()
         score OMR["acc"].append(solver.accuracy(X test.to numpy(), y test.to numpy()))
         score_OMR["DFNR"].append(DFNR(solver, X_test.to_numpy(), y_test.to_numpy(), X_test.to_numpy
         score_OMR["DFPR"].append(DFPR(solver, X_test.to_numpy(), y_test.to_numpy(), X_test.to_numpy
         score OMR["cal"].append(calibration(solver, X test. to numpy(), y test. to numpy(), X test. to
         pd. DataFrame(score OMR, index=["DM", "DM-sen"])
Out[14]:
                                         DFPR
                       acc
                               DFNR
                                                    cal
              DM 0.619512 0.165646 -0.089024 0.003722
```

DM-sen 0.627642 0.232764 -0.219117 0.050854

For the FNR constraints

```
In []:
         score FNR = \{\}
         solver = DM DMsen(X train. to numpy(), y train. to numpy(), method="FNR", c=0.005)
         solver. solve DCCP()
         score FNR["acc"] = [solver.accuracy(X test.to numpy(), y test.to numpy())]
         score FNR["DFNR"] = [DFNR(solver, X test. to numpy(), y test. to numpy(), X test. to numpy()[
         score FNR["DFPR"] = [DFPR(solver, X test. to numpy(), y test. to numpy(), X test. to numpy()[
         score_FNR["cal"] = [calibration(solver, X_test.to_numpy(), y_test.to_numpy(), X_test.to_num
         solver = DM DMsen(X train. to numpy(), y train. to numpy(), method="FNR", algo="DM-sen", c=0.
                 -0.2137754 ]))
         solver. solve DCCP()
         score_FNR["acc"].append(solver.accuracy(X_test.to_numpy(), y_test.to_numpy()))
         score FNR["DFNR"]. append(DFNR(solver, X test. to numpy(), y test. to numpy(), X test. to numpy
         score_FNR["DFPR"].append(DFPR(solver, X_test.to_numpy(), y_test.to_numpy(), X_test.to_numpy
         score FNR["cal"].append(calibration(solver, X test. to numpy(), y test. to numpy(), X test. to
In []: pd. DataFrame(score FNR, index=["DM", "DM-sen"])
Out [27]:
                               DFNR
                                         DFPR
                       acc
                                                     cal
                   0.532520 0.040324
                                     -0.140562
                                               -0.032624
          DM-sen 0.621951 0.124087 -0.076437
                                                0.019887
```

For the FPR constraints

```
In []: pd. DataFrame(score_FPR, index=["DM", "DM—sen"])

Out[29]: acc DFNR DFPR cal

DM 0.563415 0.034928 -0.036200 0.114738

DM-sen 0.614634 0.012860 -0.000709 0.025413
```

For the FNR+FPR constraints:

```
In [ ]:
         score FNPR = {}
         solver = DM_DMsen(X_train.to_numpy(), y train.to numpy(), method="FNR+FPR", c=0.005)
         solver. solve DCCP()
         score_FNPR["acc"] = [solver.accuracy(X_test.to_numpy(), y_test.to_numpy())]
         score_FNPR["DFNR"] = [DFNR(solver, X_test.to_numpy(), y_test.to_numpy(), X_test.to_numpy()
         score_FNPR["DFPR"] = [DFPR(solver, X_test. to_numpy(), y_test. to_numpy(), X_test. to_numpy()
         score_FNPR["cal"] = [calibration(solver, X_test. to_numpy(), y_test. to_numpy(), X_test. to_n
         solver = DM DMsen(X train. to numpy(), y train. to numpy(), method="FNR+FPR", algo="DM-sen",
         solver. solve DCCP()
         score_FNPR["acc"].append(solver.accuracy(X_test.to_numpy(),y_test.to_numpy()))
         score FNPR["DFNR"].append(DFNR(solver, X test. to numpy(), y test. to numpy(), X test. to num
         score FNPR["DFPR"].append(DFPR(solver, X test. to numpy(), y test. to numpy(), X test. to num
         score FNPR["cal"].append(calibration(solver, X test. to numpy(), y test. to numpy(), X test.
         pd. DataFrame(score FNPR, index=["DM", "DM-sen"])
In [ ]:
Out [56]:
                       acc
                               DFNR
                                         DFPR
                                                    cal
                  0.560976
                           0.027116
                                     -0.036200 0.118830
          DM-sen 0.612195 0.007651
                                      0.008757 0.022753
```

Summary of our results:

Racolina

	logisitc	DM			DM-sen			
		OMR	FNR	FPR	FNR+FPR	OMR	FNR	FP
Accuracy	0.627642	0.619512	0.532520	0.563415	0.560976	0.627642	0.621951	0.61463
DFNR	0.366570	0.165646	0.040324	0.034928	0.027116	0.232764	0.124087	0.01286
DFPR	-0.258211	-0.089024	-0.140562	-0.036200	-0.036200	-0.219117	-0.076437	-0.0007C
Calibration	0.030596	0.003722	-0.032624	0.114738	0.118830	0.050854	0.019887	0.02541