PROJECT 4: GROUP 3

Paper A4: Fairness Beyond Disparate Treatment & Disparate Impact: Learning Classification without Disparate Mistreatment vs Paper A1: Learning Fair Representations

The aim of the 2 papers is to formulate fairness as an optimization problem of finding a good representation of the data with two competing goals: to encode the data as well as possible, while simultaneously obfuscating any information about membership in the sensitive group.

Across the nation, judges, probation and parole officers are increasingly using algorithms to assess a criminal defendant's likelihood of becoming a recidivist – a term used to describe criminals who re-offend. There are dozens of these risk assessment algorithms in use. Many states have built their own assessments, and several academics have written tools.

The Northpointe's tool, called COMPAS (which stands for Correctional Offender Management Profiling for Alternative Sanctions), found that black defendants were far more likely than white defendants to be incorrectly judged to be at a higher risk of recidivism, while white defendants were more likely than black defendants to be incorrectly flagged as low risk.

Hence we use the Compas scores of 2 years and try to find a good representation of accuracy along with fairness and check if there is a discrimination or not

In []:

```
In [75]:
           import pandas as pd
           import numpy as np
           import pickle
           import scipy.optimize as optim
           from sklearn import preprocessing
           from sklearn.model selection import train test split
           from sklearn import feature extraction
           #from future import division
           import os,sys
           import numpy as np
           from collections import defaultdict
           from random import seed, shuffle
           from collections import defaultdict
           from copy import deepcopy
           import numpy.core.multiarray
           import cvxpy as cvx
           import dccp
           from dccp.problem import is dccp
           import traceback
           import matplotlib.pylab as plt
           import math
           import copy
```

In [3]: !pip install dccp

```
Looking in indexes: https://pypi.org/simple, (https://pypi.org/simple,) h
ttps://us-python.pkg.dev/colab-wheels/public/simple/ (https://us-python.p
kg.dev/colab-wheels/public/simple/)
Collecting dccp
  Downloading dccp-1.0.4.tar.gz (8.0 kB)
Requirement already satisfied: cvxpy>=0.3.5 in /usr/local/lib/python3.7/d
ist-packages (from dccp) (1.2.2)
Requirement already satisfied: numpy>=1.15 in /usr/local/lib/python3.7/di
st-packages (from cvxpy>=0.3.5->dccp) (1.21.6)
Requirement already satisfied: ecos>=2 in /usr/local/lib/python3.7/dist-p
ackages (from cvxpy>=0.3.5->dccp) (2.0.10)
Requirement already satisfied: osqp>=0.4.1 in /usr/local/lib/python3.7/di
st-packages (from cvxpy>=0.3.5->dccp) (0.6.2.post0)
Requirement already satisfied: scs>=1.1.6 in /usr/local/lib/python3.7/dis
t-packages (from cvxpy>=0.3.5->dccp) (3.2.2)
Requirement already satisfied: scipy>=1.1.0 in /usr/local/lib/python3.7/d
ist-packages (from cvxpy>=0.3.5->dccp) (1.7.3)
Requirement already satisfied: qdldl in /usr/local/lib/python3.7/dist-pac
kages (from osqp>=0.4.1->cvxpy>=0.3.5->dccp) (0.1.5.post2)
Building wheels for collected packages: dccp
  Building wheel for dccp (setup.py) ... done
  Created wheel for dccp: filename=dccp-1.0.4-py3-none-any.whl size=7386
 sha256=518fa5a6964f826d958b50c8fef07c8ea8b36030bd539ba6297aea3950ad2eb9
  Stored in directory: /root/.cache/pip/wheels/44/a0/2b/8944fc49959e6ae8c
c9584719c236016c214a04baf6516e24d
Successfully built dccp
Installing collected packages: dccp
Successfully installed dccp-1.0.4
```

```
In [226]: import time
start_dm = time.time()
```

```
In [227]: #df = pd.read_csv('../data/compas-scores-two-years.csv')
    df = pd.read_csv('compas-scores-two-years.csv')
    df['length_of_stay']=df['c_jail_out'].apply(pd.to_datetime) - df['c_jail_df['length_of_stay']=df['length_of_stay'].dt.days
    df['length_of_stay'] = df.length_of_stay.apply(lambda x:'greater than 100
```

```
In [228]: ▼ #Selecting features
            features = ["age_cat", "race", "sex", "priors_count", "c_charge_degree","
            cont_feature = ["priors_count"]
            sensitive_attributes = ["race"]
            x_control = defaultdict(list)
            data=df.copy()
            # Data Filtering
           idx = np.where((data['days_b_screening_arrest']<=30) & (data['days_b_screening_arrest']
             & (data['is recid']!=-1) & (data['c charge degree']!="0") & (data['score
             ((data['race']=="African-American") | (data['race']=="Caucasian")))
            data=data.iloc[idx]
            # convert class label 0 to -1
            y = data['two_year_recid']
            y[y==0] = -1
            #adding intercept
            intercept = np.ones(data.shape[0]).reshape(data.shape[0], 1)
            X=pd.DataFrame(intercept, columns=['intercept'])
            feature names = []
            for attr in features:
                vals = data[attr]
                if attr in cont feature:
                    vals = [float(v) for v in vals]
                    vals = preprocessing.scale(vals) #makes it into a 0 mean and varia
                    vals = np.reshape(vals, (len(y), -1))
                else:
                    lb = preprocessing.LabelBinarizer()
                    lb.fit(vals)
                    vals = lb.transform(vals)
            # Creating list called feature names which contains column names
                # Checking continuous features
                if attr in cont feature:
                    feature names.append(attr)
                #Checking categorical features
                else:
                    # Binary features
                    if vals.shape[1] == 1:
                        feature_names.append(attr)
                    #Non Binary features - adding the names for every category
                    else:
                        for k in lb.classes :
                            feature_names.append(attr + "_" + str(k))
                X[feature_names]=vals
                feature names=[]
```

```
# Splitting the data into train and test
from sklearn.model_selection import train_test_split
x_train, x_test, y_train, y_test = train_test_split(X, y, test_size=0.5, :
x_control_train=x_train[sensitive_attributes]
x_control_test = x_test[sensitive_attributes]
feature_names= x_train.columns
x_train,x_test, y_train, y_test,x_control_train,x_control_test=x_train.vai

#Making x_control_train and x_control_test into a dictionary
x_control_train={sensitive_attributes[0]:x_control_train.flatten()}
x_control_test={sensitive_attributes[0]:x_control_test.flatten()}
```

In []:

PAPER 4: Fairness Beyond Disparate Treatment & Disparate Impact: Learning Classification without Disparate Mistreatment

The overall goal of this algorithm is to build a fair classifier. In pratical scenarios when we are building a predictive model, a lot of festures are sensitive like gender, race, religion which can lead to a biased model. One example can be creating a predictive model to predict salaries of individuals and gender is included in the model. To avoid this, we add constraints to the model when we are optimizing. Under an ideal scenario, while building any type of model, our aim is to minimize the loss function. To make the model fair, we add contraints to the model, i.e we minimize the loss function while also making sure the contraints are met. In this algorithm those constraints were FPR and FNR. We cannot directly add the FPR abd FNR contraints to optimization funtion because they make the optimization problem non convex which are difficult to solve. Therefore we use a substitute which is the covariance between the users' sensitive attributes and the signed distance between the fea- ture vectors of misclassified users and the classifier decision boundary. The result in the algorithm is that we can find a balance which balances accuracy and fairness

```
In [229]: v def train model(x, y, x control, EPS, cons params, tau, mu):
              max iters = 100
              max_iter_dccp = 50
              num_points, num_features = x.shape
              w = cvx.Variable(num_features)
              np.random.seed(0)
              w.value = np.random.rand(x.shape[1])
              loss = cvx.sum( cvx.logistic( cvx.multiply(-y, x*w) ) / num point
              #loss = cvx.sum(cvx.logistic(x @ w) - cvx.multiply(y, x @ w) )
              constraints = []
              if cons params is not None:
                 for attribute in cons params["sensitive attrs to cov thresh"].key
                     attribute_list = x_control_train[attribute]
                     s val to total = {param:{} for param in [0,1,2]}
                     s_val_to_avg = {param:{} for param in [0,1,2]}
                     cons_sum_dict = {param:{} for param in [0,1,2]}
                     for val in set(attribute list):
                         s val to total[0][val] = sum(x control train[attribute] =
                         s_val_to_total[1][val] = sum(np.logical_and(x_control_tra)
                         s val to total[2][val] = sum(np.logical and(x control tra:
                     for param in [0,1,2]:
                         s_val_to_avg[param][0] = s_val_to_total[param][1] / float
                         s_val_to_avg[param][1] = 1.0 - s_val_to_avg[param][0]
                     for v in set(attribute list):
                         idx = x control train[attribute] == v
                         # #DCCP constraints
                         dist bound prod = cvx.multiply(y train[idx], x train[idx]
                         cons sum dict[0][v] = cvx.sum( cvx.minimum(0, dist bound )
                         cons sum dict[1][v] = cvx.sum( cvx.minimum(0, cvx.multiply
                         cons sum dict[2][v] = cvx.sum( cvx.minimum(0, cvx.multipl)
                         if cons params["cons type"] == 4:
                         params = [1,2]
                     elif cons params["cons type"] in [0,1,2]:
                         params = [cons_params["cons_type"]]
```

```
for param in params:
           threshold = abs(cons_params["sensitive_attrs_to_cov_thres|
           constraints.append( cons_sum_dict[param][1] <= cons_sum_d.</pre>
           constraints.append( cons sum dict[param][1] >= cons sum d
       if cons params is not None:
   if cons params.get("take initial sol") is None: # true by default
       take_initial sol = True
   elif cons params["take initial sol"] == False:
       take_initial_sol = False
   if take initial sol == True: # get the initial solution
       p = cvx.Problem(cvx.Minimize(loss), [])
       p.solve()
prob = cvx.Problem(cvx.Minimize(loss), constraints)
try:
   prob.solve(method='dccp', tau=tau, mu=mu, tau_max=1e10,
       solver='ECOS', verbose=False,
       feastol=EPS, abstol=EPS, reltol=EPS, feastol inacc=EPS, abstol
       max_iters=max_iters, max_iter=max_iter_dccp)
except:
   traceback.print exc()
   sys.stdout.flush()
   sys.exit(1)
# check that the fairness constraint is satisfied
for f c in constraints:
  # assert(f c.value == True) # can comment this out if the solver f
   pass
w = np.array(w.value).flatten() # flatten converts it to a 1d array
return w
```

```
In [231]: v def sensitive features (y true, y pred, x control, sensitive attributes, f
                x_control_internal = deepcopy(x_control)
                data_dictionary = {}
                s = sensitive_attributes[0]
                s_vals = x_control_internal[s]
                for s_type in set(s_vals):
                    data_dictionary[s_type] = {}
                    y_true_local = y_true[s_vals==s_type]
                    y pred local = y pred[s vals==s type]
                    acc = float(sum(y true local==y pred local)) / len(y true local)
                    fp = sum(np.logical_and(y true local == -1.0, y pred local == +1.0)
                    fn = sum(np.logical and(y true local == +1.0, y pred local == -1.
                    tp = sum(np.logical_and(y true_local == +1.0, y pred_local == +1.
                    tn = sum(np.logical and(y true local == -1.0, y pred local == -1.
                    all_neg = sum(y_true_local == -1.0)
                    all_pos = sum(y_true_local == +1.0)
                    fpr = float(fp) / float(fp + tn)
                    fnr = float(fn) / float(fn + tp)
                    tpr = float(tp) / float(tp + fn)
                    tnr = float(tn) / float(tn + fp)
                    data_dictionary[s_type]["fp"] = fp
                    data dictionary[s type]["fn"] = fn
                    data dictionary[s type]["fpr"] = fpr
                    data_dictionary[s_type]["fnr"] = fnr
                    data_dictionary[s_type]["tpr"] = tpr
                    data_dictionary[s_type]["tnr"] = tnr
                    data dictionary[s type]["acc"] = (tp + tn) / (tp + tn + fp + fn)
                return data dictionary
```

```
In [236]: | def accuracy_1(threshold, flag):
              cons type = 0 # No constraint
              sensitive_attrs_to_cov_thresh = {"race": {0:{0:0, 1:threshold}, 1:{0:0
              cons_params = { "cons_type": cons_type, "tau": tau, "mu": mu, "sensiti
              w uncons, acc cons, data dictionary = classifier(EPS,tau,mu,cons para
              if flag == True:
                 print("Unconstrained classifier")
                 print("Accuracy: " + str(round(acc_cons,4)))
                                            TNR.
                                                   TPR. Accuracy")
                 print("s
                            FPR.
                                    FNR.
                 for key in data_dictionary:
                     print("-----
                     " +str(round(data dictionary[key]['tpr'],2))+ " "+ s-
                 print()
              return (acc cons, abs(data dictionary[0]['fpr']-data dictionary[1]['f
              abs(data dictionary[0]['fnr']-data dictionary[1]['fnr']), data diction
```

```
In [237]: v def accuracy_2(threshold, flag):
                                                        cons type = 1 # FPR constraint
                                                        sensitive attrs to cov thresh = \{"race": \{0:\{0:0, 1:0\}, 1:\{0:0, 1:threensemble attrs to cov thresh = \{"race": \{0:\{0:0, 1:0\}, 1:\{0:0, 1:threensemble attrs to cov thresh = \{"race": \{0:\{0:0, 1:0\}, 1:\{0:0, 1:threensemble attrs to cov thresh = \{"race": \{0:\{0:0, 1:0\}, 1:\{0:0, 1:threensemble attrs to cov thresh = \{"race": \{0:\{0:0, 1:0\}, 1:\{0:0, 1:threensemble attrs to cov thresh = \{"race": \{0:\{0:0, 1:0\}, 1:\{0:0, 1:threensemble attrs to cov thresh = \{"race": \{0:\{0:0, 1:0\}, 1:\{0:0, 1:threensemble attrs to cov thresh = \{"race": \{0:\{0:0, 1:threensemble attrs to cov thresh = \{"race": \{0:\{0:0, 1:threensemble attrs to cov thresh = \{"race": \{0:\{0:0, 1:threensemble attrs to cov threensemble attrs to cov threensemble attra to
                                                        cons_params = {"cons_type": cons_type, "tau": tau, "mu": mu, "sensiti"
                                                        w cons, acc cons, data dictionary = classifier(EPS, tau, mu, cons param
                                                        if flag == True:
                                                                      print("FPR constraint classifier")
                                                                      print("Accuracy: " + str(round(acc cons,4)))
                                                                      print("s FPR.
                                                                                                                                              FNR.
                                                                                                                                                                             TNR.
                                                                                                                                                                                                      TPR. Accuracy")
                                                                       for key in data dictionary:
                                                                                    print("-----
                                                                                     "+ str(data dictionary[key]['acc']))
                                                                      print()
                                                        #print("accuracy cons",acc cons)
                                                        return (acc cons, abs(data dictionary[0]['fpr']-data dictionary[1]['f
                                                        abs(data dictionary[0]['fnr']-data dictionary[1]['fnr']), data diction
```

```
In [238]: v def accuracy_3(threshold, flag):
              cons type = 2 # FNR constraint
              sensitive_attrs_to_cov_thresh = {"race": {0:{0:0, 1:0}, 1:{0:0, 1:0},
              cons_params = {"cons_type": cons_type, "tau": tau, "mu": mu, "sensitive"
              w_cons, acc_cons, data_dictionary = classifier(EPS,tau,mu,cons_param
              if flag == True:
                 print("FNR constraint classifier")
                 print("Accuracy: " + str(round(acc cons,4)))
                           FPR.
                                   FNR.
                                          TNR. TPR. Accuracy")
                 print("s
                 for key in data_dictionary:
                     print("-----
                     " +str(round(data_dictionary[key]['tpr'],2))+ " "+ s
                     print()
              return (acc cons, abs(data_dictionary[0]['fpr']-data_dictionary[1]['f
              abs(data_dictionary[0]['fnr']-data_dictionary[1]['fnr']),data_diction
```

```
In [239]: ▼ def accuracy 4(threshold, flag):
              cons_type = 4 # FPR & FNR constraint
              sensitive_attrs_to_cov_thresh = {"race": {0:{0:0, 1:0}, 1:{0:0, 1:thre
              cons_params = {"cons_type": cons_type, "tau": tau, "mu": mu, "sensiti"
              w_cons, acc_cons, data_dictionary = classifier(EPS,tau,mu,cons_param
              if flag == True:
                 print("FPR & FNR constraint classifier")
                 print("Accuracy: " + str(round(acc cons,4)))
                 print("s FPR.
                                   FNR.
                                           TNR. TPR. Accuracy")
                 for key in data dictionary:
                     print("-----
                     " +str(round(data dictionary[key]['tpr'],2))+ " "+ s
                     print()
              return (acc cons, abs(data dictionary[0]['fpr']-data dictionary[1]['f
              abs(data_dictionary[0]['fnr']-data_dictionary[1]['fnr']),data_diction
```

```
In [240]: import warnings
warnings.filterwarnings("ignore")
```

```
In [241]: tau = 3.0
mu = 1.5
EPS = 1e-6
```

```
In [242]:
         threshold = 0
         print("Threshold is " + str(threshold))
         print("-----
         print()
         acc_cons, diff_fpr, diff_fnr,acc_w,acc_b = accuracy_1(threshold, True)
         acc cons, diff fpr, diff fnr,acc w,acc b = accuracy 2(threshold, True)
         acc_cons, diff_fpr, diff_fnr,acc_w,acc_b = accuracy_3(threshold, True)
         acc cons, diff fpr, diff fnr,acc w,acc b = accuracy 4(threshold, True)
         print()
        Threshold is 0
       Unconstrained classifier
       Accuracy: 0.676
       s FPR. FNR. TNR. TPR. Accuracy
        0 0.38 0.27 0.62 0.73 0.6719643992371265
        1 0.16 0.57 0.84
                              0.43 0.6819887429643527
       FPR constraint classifier
       Accuracy: 0.6669
       s FPR. FNR. TNR. TPR. Accuracy
        -----
          0.27 0.39 0.73 0.61 0.6757787666878576
        _____
                 0.4 0.68 0.6 0.6538461538461539
           0.32
       FNR constraint classifier
       Accuracy: 0.6756
       s FPR. FNR. TNR. TPR. Accuracy
        _____
           0.28
                  0.37
                        0.72
                              0.63 0.6745073108709473
        1 0.25 0.44 0.75 0.56 0.6772983114446529
       FPR & FNR constraint classifier
       Accuracy: 0.6707
        s FPR. FNR. TNR. TPR. Accuracy
           0.24
                 0.4
                       0.76
                             0.6 0.6776859504132231
        1 0.29 0.42 0.71 0.58 0.6604127579737336
```

Runtime of the code is 113.56461477279663 seconds

```
In [203]: tau = 3.0
    mu = 1.5
    EPS = 1e-6
    cons_type7 = 0 # No constraint
    sensitive_attrs_to_cov_thresh7 = {"race": {0:{0:0, 1:threshold}, 1:{0:0, cons_params7 = {"cons_type": cons_type7, "tau": tau, "mu": mu, "sensitive w_uncons7, acc_cons7, data_dictionary7 = classifier(EPS,tau,mu,cons_params data_dictionary7[1]['acc']
```

Out[203]: 0.6819887429643527

Analysis on varying the 'c' constant

```
In [195]: v for threshold in range(0, 50, 5):
            threshold = threshold/1000
            print("Threshold is " + str(threshold))
            print("-----
            print()
            acc cons, diff fpr, diff fnr,acc w,acc b = accuracy 1(threshold, True
            acc_cons, diff_fpr, diff_fnr,acc_w,acc_b = accuracy_2(threshold, True
            acc cons, diff fpr, diff fnr,acc w,acc b = accuracy 3(threshold, True
            acc cons, diff fpr, diff fnr,acc w,acc b = accuracy 4(threshold, True
            print()
        Threshold is 0.0
        Unconstrained classifier
        Accuracy: 0.676
                FNR. TNR. TPR. Accuracy
           FPR.
        -----
           0.38 0.27
                              0.73 0.6719643992371265
                       0.62
        1 0.16 0.57 0.84 0.43 0.6819887429643527
        FPR constraint classifier
        Accuracy: 0.6669
          FPR. FNR. TNR. TPR. Accuracy
        _____
            0.27 0.39 0.73 0.61 0.6757787666878576
                       0.68
           0.32
                 0.4
                             0.6 0.6538461538461539
       FNR constraint classifier
       Accuracy: 0.6756
          FPR. FNR.
                       TNR. TPR. Accuracy
           0.28 0.37 0.72 0.63 0.6745073108709473
        _____
           0.25
                 0.44 0.75 0.56 0.6772983114446529
       FPR & FNR constraint classifier
        Accuracy: 0.6707
          FPR. FNR. TNR. TPR. Accuracy
        -----
           0.24
                 0.4 0.76 0.6 0.6776859504132231
           0.29 0.42 0.71 0.58 0.6604127579737336
        Threshold is 0.005
        Unconstrained classifier
       Accuracy: 0.6745
            FPR. FNR. TNR. TPR. Accuracy
```

				•	mmtz-z - Jupyter Notebook	
0	0.38		0.62	0.73	0.6706929434202161	
1		0.57			0.6801125703564728	
FPR	constrai	int clas	sifier			
	racy: (
	FPR.				Accuracy	
	0.31				0.684043229497775	
1	0.33	0.38	0.67	0.62	0.651031894934334	
	constrai		sifier			
	racy: (שואים	ממיזי	Accuracy	
0	0.3	0.36	0.7	0.64	0.6719643992371265	
 1	0.25	0.45	0.75	0.55	 0.6726078799249531	
FPR	& FNR co	onstrain	t classi	fier		
	racy: (CIUBBI			
s	_	FNR.			Accuracy	
					0.684043229497775	
 1	0.33	0.37	0.67	0.63	0.6557223264540337	
Thre	shold is	s 0.01				
Unco	nstraine	ed class	ifier			
Accu	racy: (
s 	FPR.	FNR.	TNR.	TPR.	Accuracy	
0	0.38			0.73	0.6706929434202161	
1	0.17				0.6801125703564728	
	constrai		sifier			
	racy: (•	
s 	FPR.	FNR.	TNR.	TPR.	Accuracy	
0	0.3	0.34	0.7	0.66	0.677050222504768	
1	0.3	0.4	0.7	0.6 0.	.6632270168855535	
	constrai		sifier			
	racy: (mxr	מתח	Agguragy	
s 					Accuracy 	
0	0.31	0.35	0.69	0.65	0.673871582962492	

```
0.24 0.46 0.76 0.54 0.6754221388367729
FPR & FNR constraint classifier
Accuracy: 0.6715
   FPR. FNR. TNR. TPR. Accuracy
        0.34
   0.3
              0.7 0.66 0.677050222504768
1 0.3 0.4 0.7 0.6 0.6632270168855535
Threshold is 0.015
Unconstrained classifier
Accuracy: 0.6745
   FPR. FNR. TNR. TPR. Accuracy
  0.38 0.27 0.62
                     0.73 0.6706929434202161
1 0.17 0.57 0.83 0.43 0.6801125703564728
FPR constraint classifier
Accuracy: 0.673
   FPR. FNR. TNR. TPR. Accuracy
_____
    0.31
         0.34
               0.69
                     0.66
                           0.6776859504132231
   0.28
         0.42 0.72
                     0.58
                           0.6660412757973734
FNR constraint classifier
Accuracy: 0.6749
s FPR. FNR. TNR. TPR. Accuracy
  0.31 0.34 0.69 0.66 0.673871582962492
-----
         0.47 0.77 0.53 0.6763602251407129
   0.23
FPR & FNR constraint classifier
Accuracy: 0.6726
               TNR. TPR. Accuracy
   FPR. FNR.
-----
                           0.677050222504768
   0.31 0.34
                0.69
                     0.66
  0.28 0.42 0.72 0.58 0.6660412757973734
Threshold is 0.02
```

	racy: (ТИВ -	ТР В .	Accuracy
			0.62		0.6706929434202161
					0.6801125703564728
FPR	constra	int class	sifier		
	racy: (
s 	FPR.	FNR.	TNR.	TPR.	Accuracy
0	0.3	0.34	0.69	0.66	0.6789574062301335
1	0.25	0.45	0.75	0.55	0.6707317073170732
		int class	sifier		
	racy: (шит	mDD.	A a a u w a =
s 			TNR.		Accuracy
0	0.33	0.33	0.68	0.67	0.6713286713286714
1	0.22	0.48	0.78	0.52	0.6782363977485929
			t classi:	fier	
	racy: (mn=	7
s 			TNR.		Accuracy
0	0.3	0.34	0.69	0.66	0.6789574062301335
 1	0.25	0.45	0.75	0.55	 0.6707317073170732
Thre	eshold is	5 0.025			
Unco	nstraine	ed class:	ifier		
	racy: (TTTCT		
	_		TNR.	TPR.	Accuracy
0			0.62		0.6706929434202161
1			0.83		0.6801125703564728
		int class	sifier		
	racy: (
		FNR.		TPR.	Accuracy
				0.67	0.6815003178639543
1	0.23	0.47	0.77	0.53	0.6744840525328331

FNR constraint classifier Accuracy: 0.6772

				Paper4_com	mit2-2 - Jupyter Notebook
s	FPR.	FNR.	TNR.	TPR.	Accuracy
0	0.33	0.32	0.67	0.68	0.6726001271455817
1	0.2	0.5	0.8	0.5 0.	 6838649155722326
FPR	& FNR co	onstrain	t classi	fier	
	iracy: (
s				TPR.	Accuracy
0					0.6815003178639543
1	0.23	0.47	0.77	0.53	0.6744840525328331
Thre	eshold is	s 0.03			
	onstraine		ifier		
	ıracy: (•
				TPR.	Accuracy
0	0.38	0.27	0.62	0.73	0.6706929434202161
				0.43	0.6801125703564728
FPR	constrai	int clas	sifier		
	ıracy: (
s 	FPR.	FNR.	TNR.	TPR.	Accuracy
0	0.32	0.33	0.68	0.67	0.6789574062301335
1	0.21	0.51	0.79	0.49	0.6754221388367729
	constrai		sifier		
	ıracy: (
s 				TPR.	Accuracy
0					0.6745073108709473
1	0.2	0.5	0.8	0.5 0.	 6857410881801126
FPR	& FNR co	onstrain	t classi	fier.	
Accu	ıracy: (0.6772			
s 	FPR.	FNR.	TNR.	TPR.	Accuracy
0	0.32	0.32	0.68	0.68	0.6795931341385887
1				0.49	 0.6735459662288931

Threshold is 0.035

Unconstrained classifier

Accuracy: 0.6745

S	FPR.	FNR.	TNR.	TPR.	Accuracy
0	0.38	0.27	0.62	0.73	0.6706929434202161
1	0.17	0.57	0.83	0.43	0.6801125703564728

FPR constraint classifier

Accuracy: 0.676

s	FPR.	FNR.	TNR.	TPR.	Accuracy
0	0.33	0.32	0.67	0.68	0.673871582962492
1	0.19	0.53	0.81	0.47	0.6791744840525328

FNR constraint classifier

Accuracy: 0.6779

s	FPR.	FNR.	TNR.	TPR.	Accuracy
0	0.35	0.3	0.65	0.7	0.6745073108709473

1 0.2 0.51 0.8 0.49 0.6829268292682927

FPR & FNR constraint classifier

Accuracy: 0.6768

s	FPR.	FNR.	TNR.	TPR.	Accuracy
0	0.33	0.32	0.67	0.68	0.673871582962492
1	0.19	0.53	0.81	0.47	0.6810506566604128

Threshold is 0.04

Unconstrained classifier

Accuracy: 0.6745

s	FPR.	FNR.	TNR.	TPR.	Accuracy
0	0.38	0.27	0.62	0.73	0.6706929434202161
1	0.17	0.57	0.83	0.43	0.6801125703564728

FPR constraint classifier

Accuracy: 0.6753

s 	FPR.	FNR.	TNR.	TPR.	Accuracy
0	0.34	0.32	0.66	0.68	0.6726001271455817
1	0.18	0.55	0.82	0.45	0.6791744840525328

	racy: 0		Фил	ጥጋጋ	Accuracy
		FNK.			•
0	0.36	0.29	0.64	0.71	0.677050222504768
1	0.19	0.53	0.81	0.47	 0.6782363977485929
FPR	& FNR co	nstraint	classif	ier	
	racy: 0		min		•
s 		FNR.			Accuracy
0	0.34	0.31	0.66	0.69	0.6732358550540368
1	0.19		0.81		 0.6782363977485929
Πh νο	eshold is	0 045			
			· 		
	onstraine uracy: 0		fier		
	_		TNR.	TPR.	Accuracy
0	0.38	0.27	0.62	0.73	 0.6706929434202161
 1		0.57			 0.6801125703564728
	constrai				
	racy: 0		iller		
			TNR.	TPR.	Accuracy
0					0.677050222504768
1		0.56			0.6801125703564728
FNR	constrai	nt class	ifier		
	racy: 0				
s 	FPR.	FNR.	TNR.	TPR.	Accuracy
0	0.38	0.27	0.62	0.73	0.673871582962492
 1	0.18	0.55	0.82	0.45	 0.6782363977485929
FPR	& FNR co	nstraint	classif	ier	
	racy: 0				
s					Accuracy
0		0.29			0.677050222504768
 1	 Λ 1Ω	0.55			 0.6782363977485929
Τ.	0.10	0.55	0.02	0.40	0.0102303311403323

PLOTS

Constraints on FPR

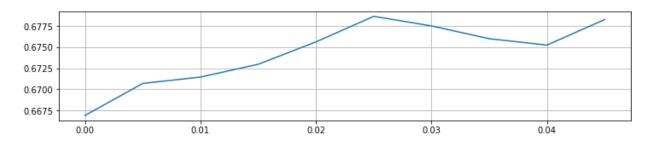
```
In [89]: accuracy_dictionary = {}
diff_fpr_dictionary = {}
diff_fnr_dictionary = {}

v for threshold in range(0, 50, 5):
    threshold = threshold/1000

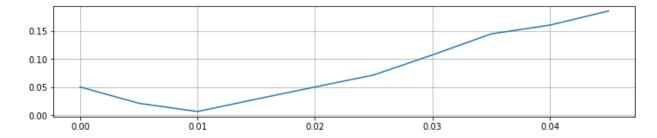
acc_cons, diff_fpr, diff_fnr = accuracy_2(threshold, False)
diff_fpr_dictionary[threshold] = diff_fpr
diff_fnr_dictionary[threshold] = diff_fnr
accuracy_dictionary[threshold] = acc_cons
```

```
In [90]:
           import seaborn as sns
           print("Constraints on FPR")
           print("Accuracy Plot vs Threshold")
           lists = sorted(accuracy_dictionary.items()) # sorted by key, return a lis
           fig=plt.figure(figsize=(12, 8))
           x, y = zip(*lists) # unpack a list of pairs into two tuples
           plt.subplot(3, 1,1)
           plt.plot(x, y)
           plt.grid()
           plt.show()
           print("Differnce between FPR in Sensitive Variables Plot vs Threshold")
           lists = sorted(diff_fpr_dictionary.items()) # sorted by key, return a lis
           plt.figure(figsize=(12, 8))
           x, y = zip(*lists) # unpack a list of pairs into two tuples
           plt.subplot(3, 1, 2)
           plt.plot(x, y)
           plt.grid()
           plt.show()
           print("Differnce between FNR in Sensitive Variables Plot vs Threshold")
           lists = sorted(diff fnr dictionary.items()) # sorted by key, return a lis
           plt.figure(figsize=(12, 8))
           x, y = zip(*lists) # unpack a list of pairs into two tuples
           plt.subplot( 3,1, 3)
           plt.plot(x, y)
           plt.grid()
           plt.show()
```

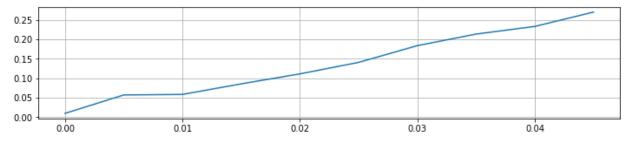
Constraints on FPR Accuracy Plot vs Threshold



Differnce between FPR in Sensitive Variables Plot vs Threshold



Differnce between FNR in Sensitive Variables Plot vs Threshold

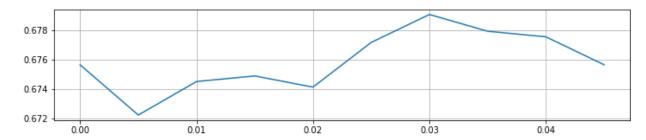


Here we see that as threshold(unfairness) rises the accuracy increases. With rise of unfairness the fpr and well as fnr increases

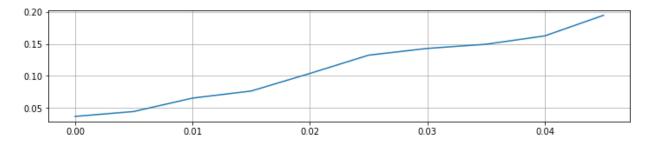
Constraints on FNR

```
print("Constraint of FNR")
In [92]:
           print("Accuracy Plot vs Threshold")
           lists = sorted(accuracy_dictionary.items()) # sorted by key, return a lis
           plt.figure(figsize=(12, 8))
           x, y = zip(*lists) # unpack a list of pairs into two tuples
           plt.subplot( 3, 1,1)
           plt.plot(x, y)
           plt.grid()
           plt.show()
           print("Differnce between FPR in Sensitive Variables Plot vs Threshold")
           lists = sorted(diff fpr dictionary.items()) # sorted by key, return a lis
           plt.figure(figsize=(12, 8))
           x, y = zip(*lists) # unpack a list of pairs into two tuples
           plt.subplot(3, 1, 2)
           plt.plot(x, y)
           plt.grid()
           plt.show()
           print("Differnce between FNR in Sensitive Variables Plot vs Threshold")
           lists = sorted(diff_fnr_dictionary.items()) # sorted by key, return a lis
           plt.figure(figsize=(12, 8))
           x, y = zip(*lists) # unpack a list of pairs into two tuples
           plt.subplot( 3,1, 3)
           plt.plot(x, y)
           plt.grid()
           plt.show()
```

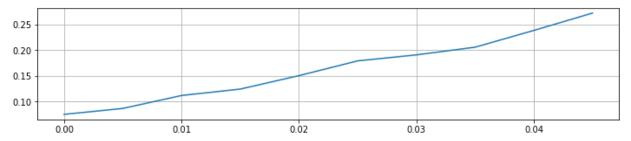
Constraint of FNR
Accuracy Plot vs Threshold



Differnce between FPR in Sensitive Variables Plot vs Threshold



Differnce between FNR in Sensitive Variables Plot vs Threshold

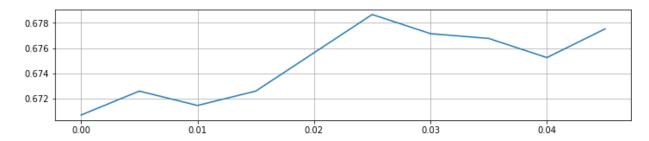


Here we see that as threshold(unfairness) rises the accuracy increases in first half but slightly decreases after threshold of 0.03. With rise of unfairness the fpr and well as fnr increases

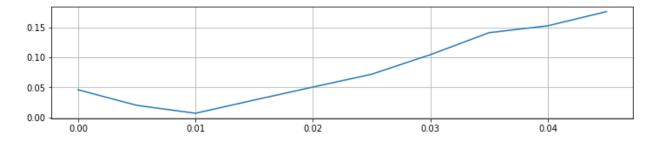
Constraints on FPR and FNR

```
print("Constraints of FNR and FPR")
In [94]:
           print("Accuracy Plot vs Threshold")
           lists = sorted(accuracy_dictionary.items()) # sorted by key, return a lis
           plt.figure(figsize=(12, 8))
           x, y = zip(*lists) # unpack a list of pairs into two tuples
           plt.subplot( 3, 1,1)
           plt.plot(x, y)
           plt.grid()
           plt.show()
           print("Differnce between FPR in Sensitive Variables Plot vs Threshold")
           lists = sorted(diff fpr dictionary.items()) # sorted by key, return a lis
           plt.figure(figsize=(12, 8))
           x, y = zip(*lists) # unpack a list of pairs into two tuples
           plt.subplot(3, 1, 2)
           plt.plot(x, y)
           plt.grid()
           plt.show()
           print("Differnce between FNR in Sensitive Variables Plot vs Threshold")
           lists = sorted(diff_fnr_dictionary.items()) # sorted by key, return a lis
           plt.figure(figsize=(12, 8))
           x, y = zip(*lists) # unpack a list of pairs into two tuples
           plt.subplot(3, 1,3)
           plt.plot(x, y)
           plt.grid()
           plt.show()
```

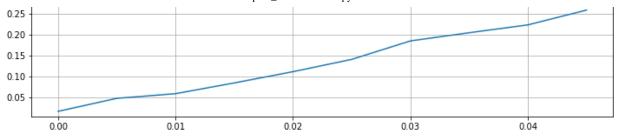
Constraints of FNR and FPR Accuracy Plot vs Threshold



Differnce between FPR in Sensitive Variables Plot vs Threshold



Differnce between FNR in Sensitive Variables Plot vs Threshold



Here also we see that as threshold(unfairness) rises the accuracy increases. With rise of unfairness the fpr and well as fnr increases

In []:

PAPER 1: Learning Fair Representations

This is a feature selection algorithm. Given data of x's, y and a sensitive variable (in the case of Compas, race), our goal was to calculate shapely values using observed conditional probabilities and the set structure of the data to estimate marginal accuracy and discrimination trade-off if a target variable is eliminated from the x matrix.

To build the code we basically tried to translate the proofs in the appendix to code, and were able to successfully implement this algorithm.

We ran this algorithm on a set of five candidate variables, and determined, on the basis of a high discrimination coefficient, we could likely remove priors_count from training sets.

Following this prescription modeled a logistic regression problem on the edited data. We looked at train and test accuracy and found that Black and White accuracies were comparable, but African American test accuracies were about 3.5% lower than those of White group.

```
In [140]: ▼ #helper function testing environment::
                          def helper data cleaning(x):
                                    #This code subsets the dataframe to relevant fields for the purpose of
                                    df = x[x['race'].isin(['African-American','Caucasian'])]
                                    idx = np.where((df['days b screening arrest'] <= 30) & (df['days b screening arrest'] 
                                                                      (df['is recid']!=-1) & (df['c charge degree']!="0") &
                                                                      ((df['race']=="African-American") | (df['race']=="Cauca:
                                    df = df.iloc[idx]
                                    df=df.filter(items=['raw_data', 'age', 'c_charge_degree', 'race', 'age'
                                                                        'days_b_screening_arrest', 'decile_score', 'is_recid'
                                    return df
                      v def encoding data(x):
                                    x['race'] = x['race'].apply(lambda x: 1 if x == "Caucasian" else 0)
                                    #print(x['race'])
                                    x['sex'] = x['sex'].apply(lambda x: 1 if x == "Female" else 0)
                                    df1 = x
                                    df1['length_of_stay']=df1['c_jail_out'].apply(pd.to_datetime) - df1['c
                                    df1['length of stay']=df1['length of stay'].dt.days
                                    df1['length_of_stay'] = df1.length_of_stay.apply(lambda x: 2 if x >1
                                    df1['priors_count'] = df1['priors_count'].apply(lambda x: 0 if x == 0
                                    df1['priors count'] = df1['priors count'].apply(lambda x: 1 if (1 <= :
                                    df1['priors_count'] = df1['priors_count'].apply(lambda x: 2 if x > 3
                                    # Label Encoding
                                    #df1['race'] = df1['race'].apply(lambda x: 1 if x == 'Caucasian' else
                                    #df1['race'] = df1['race 2']
                                    #df1.loc[df1.race=='Caucasian']=1
                                    #df1.loc[df1.race=='African-American']=0
                                    categorical variables = ['c charge degree','sex','age cat','score tex
                                    for var in categorical variables:
                                            df1[var] = df1[var].astype('category').cat.codes
                                    final vars = ['sex', 'age cat', 'race', 'priors count', 'c charge degree'
                                    df1 = df1[final vars]
                                    y = x['two year recid']
                                    return y, df1
```

```
In [141]: 
#cleaning/prepping data

df_1 = helper_data_cleaning(df)
y, df_1 = encoding_data(df_1)
```

```
In [142]: ▼ def unique information_coef(x, y):
                import itertools
                nrow = x.shape[0]
                x_{shap} = x.shape[1]
                z = np.concatenate((x,y), axis=1)
                #unique combinations of possible encodings
                unique combo = []
                for r in z.T:
                    unique_combo.append(np.unique(r).tolist())
                cartesian = list(itertools.product(*unique combo))
                running p = 0
                for possible in cartesian:
                    #print(ff," ", possible)
                    mutual_ct, r_1_ct, r_2_ct = 0,0,0
                    mutual ct = np.sum(np.all(possible == z, axis=1))
                    r_1_ct = np.sum(np.all(possible[:x_shap] == z[:,:x_shap], axis=1)
                    r_2 ct = np.sum(np.all(possible[x_shap:] == z[:,x_shap:], axis=1)
                    #for row in z:
                        #checking if joint
                         if possible == row:
                             mutual ct = mutual ct+1
                        #checking x
                       # if possible[:x shap]== z[:x shap]:
                            r 1 ct = r 1 ct +1
                        #checking y
                        #if possible[x shap:]== z[x shap:]:
                           r 2 ct = r 2 ct +1
                    #saving computation in the event there's a zero result
                    if (mutual ct == 0 or r 1 ct == 0 or r 2 ct == 0):
                        intermed = 0
                    else:
                        mutual p = mutual ct/nrow
                        pr1 = r_1_ct/nrow
                        pr2 = r 2 ct/nrow
                        intermed = mutual p * np.log(mutual p / pr1) / pr1
                    running p += abs(intermed)
                return running_p
           def conditional info coef(x,y,c):
                import itertools
                nrow = x.shape[0]
                x shap = x.shape[1]
                y shap = y.shape[1]
                #print(x.shape,y.shape,c.shape)
                z = np.concatenate((y,x,c), axis=1)
```

```
#unique combinations of possible encodings
    unique_combo = []
    for r in z.T:
        unique combo.append(np.unique(r).tolist())
    cartesian = list(itertools.product(*unique_combo))
    running p = 0
    for possible in cartesian:
        #print(ff," ", possible)
        mutual_ct, r_1_ct, r_2_ct, r_cond = 0,0,0,0
        mutual ct = np.sum(np.all(possible == z, axis=1))
        # r 1 ct = np.sum(np.all(possible[:1] == z[:,:1], axis=1))
        \# r 2 ct = np.sum(np.all(possible[1:-x shap] == z[:,1:-x shap], a.
        r_1_ct = np.sum(np.all(possible[:y_shap] == z[:,:y_shap], axis=1)
        r 2 ct = np.sum(np.all(possible[y shap:-x shap] == z[:,y shap:-x shap]
        cond ct num = np.sum(np.where((possible[:y shap] == z[:,:y shap])
        cond ct den = np.sum(np.where((possible[-x shap:] == z[:,-x shap:
        if cond_ct_den == 0:
            r cond = 0
        else:
            r_cond = cond_ct_num/cond_ct_den
        #saving computation in the event there's a zero result
        if (mutual ct == 0 or r 1 ct == 0 or r 2 ct == 0 or r cond ==0):
            intermed = 0
        else:
            mutual p = mutual ct/nrow
            pr1 = r 1 ct/nrow
            pr2 = r 2 ct/nrow
            intermed = mutual p * np.log(mutual p / pr2) / r cond
        running p += abs(intermed)
    return running p
def powerset(seq):
    if len(seq) <= 1:</pre>
        yield seq
        yield []
    else:
        for item in powerset(seq[1:]):
            yield [seq[0]]+item
            yield item
```

```
In [143]: ▼ def shapelydiscrimination(x,y):
                features = list(x.columns)
                features = [ele for ele in features if ele != 'race'] #removing race
                nfeat = len(features)
                shapely_coeff = []
                #identifying a feature sequentially to exclude from infoset calc
                for i in range(nfeat):
                    features 2 = features.copy()
                    rem = features_2.pop(i) #removing a feature i programmatically
                    pow set = [elm for elm in powerset(features 2)] #generating power
                    shapely_inter = 0 #for summing the shapelys
                    #now, iterating over the subsets
                    for subset in pow_set:
                        s_{len} = len(subset)
                        f len = nfeat - 1 - len(subset)
                        m_coefficient = math.factorial(s_len) * math.factorial(f_len)
                        #inclusive discrimination metric
                        inc sub = subset.copy()
                        inc_sub.append(rem)
                        x 1 = np.array(x[inc sub])
                        #print("x:",)
                        protected attribute = np.array(x['race']).reshape(-1,1)
                        #print(protected attribute.shape)
                        y_1 = np.array(y).reshape(-1,1)
                        info in = np.concatenate((x 1,protected attribute), axis = 1
                        incl a = unique information coef(info in ,y 1)
                        incl b = unique information coef(x 1,protected attribute)
                        incl c = conditional info coef(x 1, protected attribute, y 1)
                        incl = incl a * incl b * incl c
                        #call info right here
                        #exclusive discrimination metric
                        x 2 = np.array(x[subset])
                        info ex = np.concatenate((x 2,protected attribute), axis = 1
                        excl a = unique information coef(info ex ,y 1)
                        excl_b = unique_information_coef(x_2,protected_attribute)
                        excl c = conditional info coef(x 2,protected attribute,y 1)
                        excl = excl a * excl b * excl c
                        #call info right here
                        marginal discrimination = incl-excl
                        #marginal = disc incl - disc excl
                        #shapley coeff[i] = shapley coeff[i] + coef * marginal
                        shapely inter = shapely inter + m coefficient * marginal disc
                    shapely coeff.append(shapely inter)
```

```
return shapely coeff
▼ def shapelyaccuracy(x,y):
      features = list(x.columns)
      features = [ele for ele in features if ele != 'race'] #removing race
      nfeat = len(features)
      shapely_coeff = []
      #identifying a feature sequentially to exclude from infoset calc
      for i in range(nfeat):
          features 2 = features.copy()
          rem = features 2.pop(i) #removing a feature i programmatically
          pow set = [elm for elm in powerset(features 2)] #generating power
          shapely inter = 0 #for summing the shapelys
          #now, iterating over the subsets
          for subset in pow set:
              s len = len(subset)
              f_len = nfeat - 1 - len(subset)
              m_coefficient = math.factorial(s_len) * math.factorial(f_len)
              #inclusive accuracy metric
              inc sub = subset.copy()
              inc sub.append(rem)
              inc sub diff = list(set(features)-set(inc sub))
              x 1c = np.array(x[inc sub diff])
              x_1 = np.array(x[inc_sub])
              protected attribute = np.array(x['race']).reshape(-1,1)
              y 1 = np.array(y).reshape(-1,1)
              c = np.concatenate((x_1c,protected_attribute), axis = 1)
              #print( "out2: ",get conditional info coef(y 1,x 1,c))
              accuracy inclusive = conditional info coef(x 1,y 1,c)
              #call info right here
              #exclusive accuracy metric
              x 2 = np.array(x[subset])
              excl sub = features 2
              excl sub diff = list(set(features 2)-set(subset))
              x 2c = np.array(x[excl sub diff])
              d = np.concatenate((x 2c,protected attribute), axis = 1)
              accuracy_exclusive = conditional_info_coef(x_2,y_1,d)
              #marginal accuracy by including
              marginal acc = accuracy inclusive - accuracy exclusive
              shapely inter = shapely inter + m coefficient * marginal acc
          if shapely inter> 0:
              shapely coeff.append(shapely inter)
      return shapely coeff
```

```
In [144]:
    import time
    start = time.time()
    accuracy = shapelyaccuracy(df_1,y)
    discrimination = shapelydiscrimination(df_1,y)
    end = time.time()
    print(end - start)
26.75325107574463
```

```
variable accuracy discrimination

0 sex 0.607707 5933.746182

1 age_cat 0.892485 8871.607730

2 priors_count 0.984446 9024.280430

3 c_charge_degree 0.730598 7155.980280

4 length_of_stay 0.668507 8352.821957

['sex', 'age_cat', 'c_charge_degree', 'length_of_stay']
```

Type Markdown and LaTeX: α^2

Logistic regression

We now remove variable with highest discrimination and are left with tolerble or unaviodable

```
from sklearn.linear_model import LogisticRegression
from sklearn.model_selection import train_test_split
from sklearn.metrics import accuracy_score
from sklearn.metrics import confusion_matrix
df_m = df_1[varlist_for_model]
x_train, x_test, y_train, y_test = train_test_split(df_m, y, test_size=0.model = LogisticRegression()
model.fit(x_train,y_train)
y_hat = model.predict(x_test)
test_acc = accuracy_score(y_hat,y_test)
y_hat_train = model.predict(x_train)
train_acc = accuracy_score(y_hat_train,y_train)
```

```
In [147]:
           x_train = pd.merge(x_train, df_1, left_index=True, right_index=True)
           x train['pred'] = y hat train
           x_train['act'] = y_train
           x_test = pd.merge(x_test, df_1, left_index=True, right_index=True)
           x_{\text{test['pred']}} = y_{\text{hat}}
           x_test['act'] = y_test
In [148]:
           x_train_c = x_train[x_train['race'] == 1]
           x_test_c = x_test[x_test['race'] == 1]
           x train nc = x train[x train['race'] == 0]
           x test nc = x test[x test['race'] == 0]
           White train acc = accuracy score(x train c['pred'], x train c['act'])
           Black train acc = accuracy score(x train nc['pred'],x train nc['act'])
           white test acc = accuracy score(x test c['pred'], x test c['act'])
           Black test acc = accuracy score(x test nc['pred'],x test nc['act'])
In [149]:
           print("Race.
                               Train
                                                          Test")
                             print("Overall.
           print("White(0)
                               ",Black_train_acc,"
           print("Black(1)
                                                    ",Black_test_acc)
         Race.
                        Train
                                                  Test
         Overall.
                        0.5709258256632377
                                                0.55555555555556
         White(0)
                        0.5740868366643694
                                                0.5782208588957055
         Black(1)
                        0.5688809629959876
                                                0.5396995708154506
In [150]: ▼ # Overall confusion matrix
           tn, fp, fn, tp = confusion matrix(x test['act'], x test['pred']).ravel()
           print("True Negative: ",tn," True Positive: ",tp," False Negative: ", fn,
           print('----')
           print("FPR
                                               FNR")
           print(fp/(fp+tp),' ',fn/(fn+tn))
         True Negative: 598 True Positive: 282 False Negative: 432 False Posi
         tive: 272
         FPR
                                       FNR
          0.49097472924187724
                                    0.41941747572815535
```

```
In [151]: ▼ # Races confusion matrix
            # White
            w_tn, w_fp, w_fn, w_tp= confusion_matrix(x_test_c['act'],x_test_c['pred']
            #Black
            b_tn, b_fp, b_fn, b_tp= confusion_matrix(x_test_nc['act'],x_test_nc['pred
            #Print
            print(print("Race.
                                                                  FNR"))
                                 FPR
            print("White(0)",'
                                ',w_fp/(w_fp+w_tp),'
                                                             ',w_fn/(w_fn+w_tn))
            print("Black(1)",' ',b_fp/(b_fp+b_tp),'
                                                             ',b_fn/(b_fn+b_tn))
                   FPR
                                                   FNR
          Race.
          None
                       0.5566037735849056
                                                   0.3568181818181818
          White(0)
          Black(1)
                       0.4502923976608187
                                                   0.4661016949152542
In [151]:
```

COMPARISON BETWEEN THE 2 PAPERS

From Paper A4

```
In [223]:
         threshold = 0
         print("Threshold is " + str(threshold))
         print("-----
         print()
         # Baseline
         acc cons bas, diff fpr bas, diff fnr bas, acc w bas, acc b bas = accuracy
         # With constraint
         acc cons fpr, diff fpr fpr, diff fnr fpr, acc w fpr, acc b fpr= accuracy 2
         acc cons fnr, diff fpr fnr, diff fnr fnr, acc w fnr, acc b fnr = accuracy 3
         acc cons fpr fnr, diff fpr fpr fnr, diff fnr fpr fnr,acc w fpr fnr,acc b
        Threshold is 0
        Unconstrained classifier
        Accuracy: 0.676
            FPR. FNR. TNR. TPR. Accuracy
           0.38 0.27 0.62 0.73 0.6719643992371265
        1 0.16 0.57 0.84 0.43 0.6819887429643527
        FPR constraint classifier
        Accuracy: 0.6669
           FPR. FNR. TNR. TPR. Accuracy
        _____
           0.27 0.39 0.73 0.61 0.6757787666878576
           0.32 0.4 0.68 0.6 0.6538461538461539
        FNR constraint classifier
        Accuracy: 0.6756
           FPR. FNR. TNR. TPR. Accuracy
           0.28 0.37 0.72 0.63 0.6745073108709473
        _____
           0.25
                  0.44
                        0.75 0.56
                                     0.6772983114446529
        FPR & FNR constraint classifier
        Accuracy: 0.6707
           FPR. FNR.
                        TNR. TPR. Accuracy
        _____
           0.24 0.4 0.76 0.6 0.6776859504132231
```

0.58 0.6604127579737336

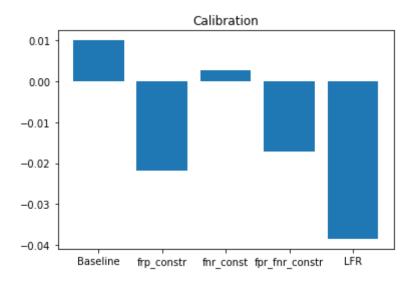
Callibration

0.29 0.42 0.71

```
In [224]: # Callibration

plt.bar(np.arange(5),[acc_b_bas-acc_w_bas,acc_b_fpr-acc_w_fpr,acc_b_fnr-acc_b_t.xticks(np.arange(5),['Baseline','frp_constr','fnr_const','fpr_fnr_construction')
```

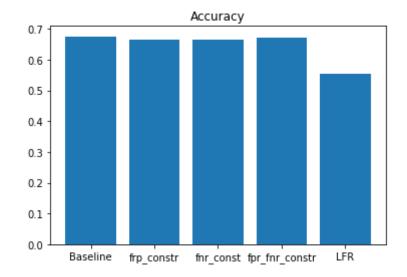
Out[224]: Text(0.5, 1.0, 'Calibration')



Accuracy

```
In [225]: # Accuracy
plt.bar(np.arange(5),[acc_cons_bas,acc_cons_fpr,acc_cons_fpr,acc_cons_fpr]
plt.xticks(np.arange(5),['Baseline','frp_constr','fnr_const','fpr_fnr_constructions)
plt.title("Accuracy")
```

Out[225]: Text(0.5, 1.0, 'Accuracy')



```
In [ ]:  # FPR
#plt.bar(np.arange(5),[diff_fpr_bas,diff_fpr_fpr,diff_fpr_fnr,diff_fpr_fp.
#plt.xticks(np.arange(5),['Baseline','frp_constr','fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','fpr_fnr_const','
```

CONCLUSION:

- 1. We see that usually when unfairness rises accuracy increases.
- 2. Paper A4 algorithms(Having fpr constraint, fpr and fnr constraint) provides a better accuracy as well as better calibration than LFR algorithm
- We also see discrimination against blacks are more than white.FNR of blacks is always higher than whites. We can see that in callibration also where accuracy of blacks is mostly lesser than whites

In []:	