The Ninth Grade Math Competition Class

Logarithm Challenging Problems

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0. What is the logarithm of $27\sqrt[4]{9}\sqrt[3]{9}$ base 3?

$$|\log_{3}(27^{4}\sqrt{9}^{3}\sqrt{9}) = |\log_{3}(3^{3}\sqrt{3}^{2}\sqrt{3}^{2}\sqrt{3}^{2})$$

$$= |\log_{3}(3^{*}) = \times$$

$$= |\log_{3}(3^{3}\sqrt{3}^{2}\sqrt{3}^{2}\sqrt{3}^{2})$$

$$= |\log_{3}(3^{3}\sqrt{3}^{2}\sqrt{3}^{2}\sqrt{3}^{2}\sqrt{3}^{2})$$

$$= |\log_{3}(3^{3}\sqrt{3}^{2$$

1. Find x if
$$\log_{3}(2x-7) = \frac{3}{2}$$
.

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2. Find $\log_{3}(2x-$

3. Solve the equation
$$\log_{2x} 216 = x$$
, where x is real

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, where x is real.

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\end{pmatrix}$$

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4. Find base b such that
$$\log_b 5\sqrt{5} = \frac{5}{2}$$
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$$b$$
 such that $\log_b 5\sqrt{5} = \frac{5}{2}$.

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5. If
$$\log_2 b - \log_2 a = 3$$
, then $b^2 - a^2 = Ma^2$, compute M .

$$|6g_{2}(\frac{b}{a}) = 3 \qquad 8 = \frac{b}{a}$$

$$\frac{b^{2}}{-1} = \frac{63}{a^{2}} = \frac{b}{a}$$

$$\frac{b^{2}}{-1} = \frac{63}{a^{2}}$$

6. If
$$\frac{\log_{10}}{\log_{10}} = \frac{10^{-1}}{10^{-1}} = e^{t}$$
, find the value of t .

$$\begin{vmatrix} \log_{10} b \\ d \\ d \end{vmatrix} = \frac{1}{\log_{10} a}$$

$$\begin{vmatrix} \log_{10} b \\ \log_{10} d \\ \log_{10} d \end{vmatrix} = \frac{\log_{10} c}{\log_{10} a}$$

$$\begin{vmatrix} \log_{10} b \\ \log_{10} d \\ \log_{10} d \end{vmatrix} = \frac{\log_{10} c}{\log_{10} a}$$

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$$\begin{vmatrix} \log_{10} b \\ \log_{10} d \\ \log_{10} d \\ \log_{10} d \end{vmatrix} = \frac{\log_{10} c}{\log_{10} a}$$

$$\begin{vmatrix} \log_{10} b \\ \log_{10} d \\ \log_{10} d$$

$$\frac{1}{3} = 109 \times 15 =) \times \frac{1}{3} = 15 =) \times = 15^{\frac{2}{3}}$$

$$\frac{3}{2} = 109 \times 15 =) \times \frac{3}{2} = 15 =) \times = 15^{\frac{2}{3}}$$

9. Evaluate
$$\frac{1}{\log \left(\frac{1}{6}\right)} - \frac{1}{\log \left(\frac{1}{6}\right)} - \frac{1}{\log \left(\frac{1}{6}\right)}$$

$$|og_{\frac{1}{2}} 2 - log_{\frac{1}{6}} 3 - log_{\frac{1}{6}} 4 = |og_{\frac{1}{6}} 3 \cdot 4| = |og_{\frac{1}{6}$$

10. Compute the value of
$$n$$
 for which $\frac{1}{\log_2 100} + \frac{1}{\log_3 100} + \frac{1}{\log_6 100} + \frac{1}{\log_9 100} = \frac{2}{\log_N 100}$.

11. Given the points $A(\log 2, \log 3)$ and $B(\log(\log T^2), \log(\log T^3))$, compute the slope of the line \overleftrightarrow{AB} .

12. Given that $\log_6 a + \log_6 b + \log_6 c = 6$, and a, b, c are positive integers that form an increasing geometric sequence and b-a is the square of an integer. Find a+b+c.