

Palindromes

The same forwards and backwards

Ex: 5, 22, 313, 123454321

Find the # of 4-digit palindromes

$$\frac{a}{9} \cdot \frac{b}{10} \cdot \frac{b}{1} \cdot \frac{a}{1} = \boxed{90}$$

Find the ^{greatest} # that divides all 4-digit palindromes

$$\underline{a} \underline{b} \underline{b} \underline{a} = 1000a + 100b + 10b + a = \underline{1001a} + \underline{110b}$$

$$\gcd(1001, 110) = \gcd(7 \cdot 11 \cdot 13, 2 \cdot 5 \cdot 11) = \boxed{11}$$

Find the smallest 3-digit palindrome whose product with 101 is not a 5-digit palindrome

$$\begin{array}{r} \underline{a} \underline{b} \underline{a} \\ \cdot 101 \\ \hline a b a \\ 0000 \\ \hline a b a 00 \\ \hline \underline{a b a b a} \end{array}$$

$$\begin{array}{l} a=5 \\ b=0 \end{array}$$

$$\begin{array}{r} \textcircled{505} \\ \times 101 \\ \hline 505 \\ 505 \\ \hline 51005 \end{array}$$