

# Homework Assignment 2 Answered

## Binary Addition Practice Problems

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### Unsigned Binary Addition (perform the addition)

Assume you have a byte (8 bits) of memory to work with. There's no need to track overflow.

1.  $101 + 11$

$$\begin{array}{r} \text{Carry Bits} \quad 1 \ 1 \ 1 \\ \phantom{+} \quad \quad 1 \ 0 \ 1 \\ \text{Sum} \quad \quad + \quad \underline{0 \ 1 \ 1} \\ \phantom{+} \quad \quad 1 \ 0 \ 0 \ 0 \end{array}$$

2.  $1101 + 101$

$$\begin{array}{r} \text{Carry Bits} \quad 1 \ 1 \ 0 \ 1 \\ \phantom{+} \quad \quad 1 \ 1 \ 0 \ 1 \\ \text{Sum} \quad \quad + \quad \underline{0 \ 1 \ 0 \ 1} \\ \phantom{+} \quad \quad 1 \ 0 \ 0 \ 1 \ 0 \end{array}$$

3.  $110 + 111$

$$\begin{array}{r} \text{Carry Bits} \quad 1 \ 1 \ 0 \\ \phantom{+} \quad \quad 1 \ 1 \ 0 \\ \text{Sum} \quad \quad + \quad \underline{1 \ 1 \ 1} \\ \phantom{+} \quad \quad 1 \ 1 \ 0 \ 1 \end{array}$$

4.  $10011 + 110$

$$\begin{array}{r} \text{Carry Bits} \quad 0 \ 1 \ 1 \ 0 \\ \phantom{+} \quad \quad 1 \ 0 \ 0 \ 1 \ 1 \\ \text{Sum} \quad \quad + \quad \underline{0 \ 0 \ 1 \ 1 \ 0} \\ \phantom{+} \quad \quad 1 \ 1 \ 0 \ 0 \ 1 \end{array}$$

5.  $1110 + 10$

$$\begin{array}{r}
 \text{Carry Bits} \quad 1 \ 1 \ 1 \ 0 \\
 \phantom{+} \phantom{000} 1 \ 1 \ 1 \ 0 \\
 + \phantom{000} 0 \ 0 \ 1 \ 0 \\
 \hline
 \text{Sum} \phantom{0000} 1 \ 0 \ 0 \ 0 \ 0
 \end{array}$$

6.  $101101 + 1001$

$$\begin{array}{r}
 \text{Carry Bits} \quad 0 \ 1 \ 0 \ 0 \ 1 \\
 \phantom{+} \phantom{0000} 1 \ 0 \ 1 \ 1 \ 0 \ 1 \\
 + \phantom{0000} 0 \ 0 \ 1 \ 0 \ 0 \ 1 \\
 \hline
 \text{Sum} \phantom{00000} 1 \ 1 \ 0 \ 1 \ 1 \ 0
 \end{array}$$

7.  $101 + 10101$

$$\begin{array}{r}
 \text{Carry Bits} \quad 0 \ 1 \ 0 \ 1 \\
 \phantom{+} \phantom{000} 0 \ 0 \ 1 \ 0 \ 1 \\
 + \phantom{000} 1 \ 0 \ 1 \ 0 \ 1 \\
 \hline
 \text{Sum} \phantom{0000} 1 \ 1 \ 0 \ 1 \ 0
 \end{array}$$

8.  $111111 + 1$

$$\begin{array}{r}
 \text{Carry Bits} \quad 1 \ 1 \ 1 \ 1 \ 1 \ 1 \\
 \phantom{+} \phantom{00000} 1 \ 1 \ 1 \ 1 \ 1 \ 1 \\
 + \phantom{00000} 0 \ 0 \ 0 \ 0 \ 0 \ 1 \\
 \hline
 \text{Sum} \phantom{000000} 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0
 \end{array}$$

9.  $1000 + 111$

$$\begin{array}{r}
 \text{Carry Bits} \quad 0 \ 0 \ 0 \\
 \phantom{+} \phantom{000} 1 \ 0 \ 0 \ 0 \\
 + \phantom{000} 0 \ 1 \ 1 \ 1 \\
 \hline
 \text{Sum} \phantom{0000} 1 \ 1 \ 1 \ 1
 \end{array}$$

10. 11001 + 1010

$$\begin{array}{r} \text{Carry Bits} \quad 1 \ 1 \ 0 \ 0 \ 0 \\ \phantom{+} \quad \quad 1 \ 1 \ 0 \ 0 \ 1 \\ \phantom{+} \quad \quad 0 \ 1 \ 0 \ 1 \ 0 \\ \hline \text{Sum} \quad \quad 1 \ 0 \ 0 \ 0 \ 1 \ 1 \end{array}$$

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## Two's Complement on Signed Binary numbers

1. 0011

One's Complement: 0011 => 1100

$$\begin{array}{r} \text{Carry Bits} \quad 0 \ 0 \ 0 \\ \phantom{+} \quad \quad 1 \ 1 \ 0 \ 0 \\ \phantom{+} \quad \quad 0 \ 0 \ 0 \ 1 \\ \hline \text{Sum} \quad \quad 1 \ 1 \ 0 \ 1 \end{array}$$

Answer = 1101

2. 01101

One's Complement: 01101 => 10010

$$\begin{array}{r} \text{Carry Bits} \quad 0 \ 0 \ 0 \ 0 \\ \phantom{+} \quad \quad 1 \ 0 \ 0 \ 1 \ 0 \\ \phantom{+} \quad \quad 0 \ 0 \ 0 \ 0 \ 1 \\ \hline \text{Sum} \quad \quad 1 \ 0 \ 0 \ 1 \ 1 \end{array}$$

Answer = 10011

3. 1101

One's Complement: 1101 => 0010

$$\begin{array}{r} \text{Carry Bits} \quad 0 \ 0 \ 0 \\ \phantom{+} \quad \quad 0 \ 0 \ 1 \ 0 \\ \phantom{+} \quad \quad 0 \ 0 \ 0 \ 1 \\ \hline \text{Sum} \quad \quad 0 \ 0 \ 1 \ 1 \end{array}$$

Answer = 0011

4. 1110

One's Complement: 1110  $\Rightarrow$  0001

$$\begin{array}{r} \text{Carry Bits} \quad \quad \quad \textcolor{red}{0} \textcolor{red}{0} \textcolor{red}{1} \\ \quad \quad \quad \quad \quad \quad 0 \ 0 \ 0 \ 1 \\ + \quad \quad \quad \quad \quad \quad 0 \ 0 \ 0 \ 1 \\ \hline \text{Sum} \quad \quad \quad \quad \quad 0 \ 0 \ 1 \ 0 \end{array}$$

Answer = 0010

5. 1001

One's Complement: 1001  $\Rightarrow$  0110

$$\begin{array}{r} \text{Carry Bits} \quad \quad \quad \textcolor{red}{0} \textcolor{red}{0} \textcolor{red}{0} \\ \quad \quad \quad \quad \quad \quad 0 \ 1 \ 1 \ 0 \\ + \quad \quad \quad \quad \quad \quad 0 \ 0 \ 0 \ 1 \\ \hline \text{Sum} \quad \quad \quad \quad \quad 0 \ 1 \ 1 \ 1 \end{array}$$

Answer = 0111

6. 011111

One's Complement: 011111  $\Rightarrow$  100000

$$\begin{array}{r} \text{Carry Bits} \quad \quad \quad \textcolor{red}{0} \textcolor{red}{0} \textcolor{red}{0} \textcolor{red}{0} \textcolor{red}{0} \\ \quad \quad \quad \quad \quad \quad 1 \ 0 \ 0 \ 0 \ 0 \ 0 \\ + \quad \quad \quad \quad \quad \quad 0 \ 0 \ 0 \ 0 \ 0 \ 1 \\ \hline \text{Sum} \quad \quad \quad \quad \quad 1 \ 0 \ 0 \ 0 \ 0 \ 1 \end{array}$$

Answer = 100001

7. 1011

One's Complement: 1011  $\Rightarrow$  0100

$$\begin{array}{r} \text{Carry Bits} \quad \quad \quad \textcolor{red}{0} \textcolor{red}{0} \textcolor{red}{0} \\ \quad \quad \quad \quad \quad \quad 0 \ 1 \ 0 \ 0 \\ + \quad \quad \quad \quad \quad \quad 0 \ 0 \ 0 \ 1 \\ \hline \text{Sum} \quad \quad \quad \quad \quad 0 \ 1 \ 0 \ 1 \end{array}$$

Answer = 0101

8. 0100

One's Complement: 0100  $\Rightarrow$  1011

$$\begin{array}{r} \text{Carry Bits} \quad 0 \ 1 \ 1 \\ \quad 1 \ 0 \ 1 \ 1 \\ + \quad 0 \ 0 \ 0 \ 1 \\ \hline \text{Sum} \quad 1 \ 1 \ 0 \ 0 \end{array}$$

Answer = 1100

9. 111111

One's Complement: 111111  $\Rightarrow$  000000

$$\begin{array}{r} \text{Carry Bits} \quad 0 \ 0 \ 0 \ 0 \ 0 \\ \quad 0 \ 0 \ 0 \ 0 \ 0 \ 0 \\ + \quad 0 \ 0 \ 0 \ 0 \ 0 \ 1 \\ \hline \text{Sum} \quad 0 \ 0 \ 0 \ 0 \ 0 \ 1 \end{array}$$

Answer = 000001

10. 0001001

One's Complement: 0001001  $\Rightarrow$  1110110

$$\begin{array}{r} \text{Carry Bits} \quad 0 \ 0 \ 0 \ 0 \ 0 \ 0 \\ \quad 1 \ 1 \ 1 \ 0 \ 1 \ 1 \ 0 \\ + \quad 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 1 \\ \hline \text{Sum} \quad 1 \ 1 \ 1 \ 0 \ 1 \ 1 \ 1 \end{array}$$