

# Binary to Octal, and Hexadecimal

Binary	Octal
000	0
001	1
010	2
011	3
100	4
101	5
110	6
111	7

Binary	0000	0001	0010	0011	0100	0101	0110	0111	1000	1001	1010	1011	1100	1101	1110	1111
Hex	0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F

# Signed Numbers: Binary, Octal, and Hexadecimal

For any binary, octal, or hexadecimal number, the most significant digit represents the sign of the number. If the MSD is less than half the base of the number, the sign of the number is positive. If the MSD is greater than or equal to the base of the number, the sign of the number is negative.

Example:  $01010_2$  is positive...  $0 < (2/2) = 0 < 1$   
:  $11010_2$  is negative...  $1 \geq (2/2) = 1 \geq 1$

Example:  $2025_8$  is positive...  $2 < (8/2) = 2 < 4$   
:  $6547_8$  is negative...  $6 \geq (8/2) = 6 \geq 4$

Example:  $4A2E_{16}$  is positive...  $4 < (16/2) = 4 < 8$   
:  $954F_{16}$  is negative...  $9 \geq (16/2) = 9 \geq 8$

# Padding

When padding a binary, octal, or hexadecimal number, there are only two options. If the number is positive, the number is padded with 0. If the number is negative, the number is padded with the largest digit in the base. The largest number of the base is the base minus 1.

Example:  $01010_2$  pad to length 10 => 0000001010  
:  $11010_2$  pad to length 8 => 11111010

Example:  $2025_8$  pad to length 7 => 0002025  
:  $6547_8$  pad to length 8 => 77776547

Example:  $4A2E_{16}$  pad to length 10 => 0000004A2E  
:  $954F_{16}$  pad to length 6 => FF954F

# Trimming

When trimming a binary, octal, or hexadecimal number, there are only two options for removal. If the number is positive, the only digits that get removed are 0s. If the first digit that's not 0 is less than half the base, the remaining 0 digit can be removed. If the number is negative, the only digits that get removed are the largest digit for the base. The largest number of the base is the base minus 1. If the first digit that's not the largest number for the base is greater than or equal to half the base, the remaining largest digit can be removed.

Example:  $000001010_2 \Rightarrow 01010$

:  $11111010_2 \Rightarrow 1010$

Example:  $000002025_8 \Rightarrow 2025$   
:  $777776547_8 \Rightarrow 6547$

Example:  $000005025_8 \Rightarrow 05025$   
:  $777772547_8 \Rightarrow 72547$

Example:  $0004A2E_{16} \Rightarrow 4A2E$   
:  $FFFF954F_{16} \Rightarrow 954F$

Example:  $000BA2E_{16} \Rightarrow 0BA2E$   
:  $FFFF154F_{16} \Rightarrow F154F$

# One's Complement

The one's complement of a binary, octal or hexadecimal number is the number with each of its digits subtracted from the largest number in the base. The largest number of the base is the base minus 1.

Example:  $01010_2 \Rightarrow 10101\dots$  1-0=1, 1-1=0, 1-0=1, 1-1=0, 1-0=1  
:  $11010_2 \Rightarrow 00101\dots$  1-1=0, 1-1=0, 1-0=1, 1-1=0, 1-0=1

Example:  $2025_8 \Rightarrow 5752\dots$  7-2=5, 7-0=7, 7-2=5, 7-5=2  
:  $6547_8 \Rightarrow 1230\dots$  7-6=1, 7-5=2, 7-4=3, 7-7=0

Example:  $4A2E_{16} \Rightarrow B5D1\dots$  15-4=B, 15-A=5, 15-2=D, 15-E=1  
:  $954F_{16} \Rightarrow 6AB0\dots$  15-9=6, 15-5=A, 15-4=B, 15-F=0

# Two's Complement

The two's complement of a binary, octal or hexadecimal number is the number with each of its digits subtracted from the largest number in the base. The largest number of the base is the base minus 1. The result is the one's complement. Afterwards a positive value of 1 is added to it.

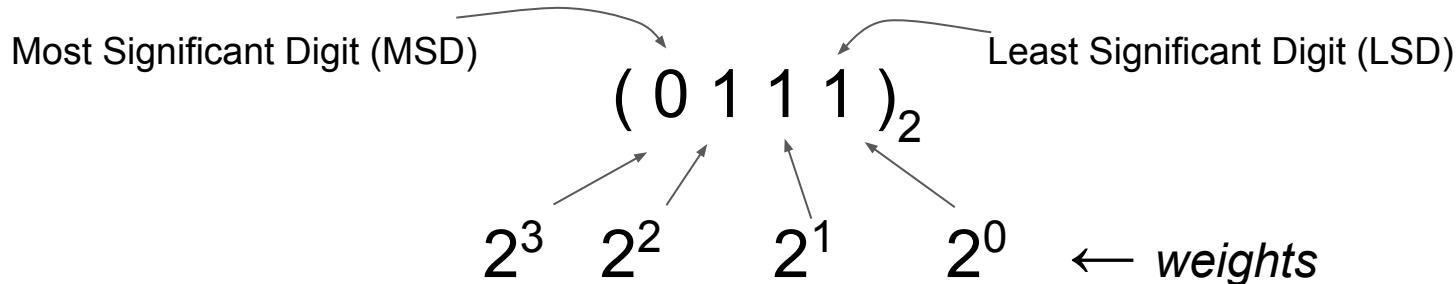
Example:  $01010_2 \Rightarrow 10101 + 01 = 10110$   
:  $11010_2 \Rightarrow 00101 + 01 = 00110$

Example:  $2025_8 \Rightarrow 5752 + 01 = 5753$   
:  $6547_8 \Rightarrow 1230 + 01 = 1231$

Example:  $4A2E_{16} \Rightarrow B5D1 + 01 = B5D2$   
:  $954F_{16} \Rightarrow 6AB0 + 01 = 6AB1$

# To Decimal

Example: Consider 0111, signed binary number (base-2 number)

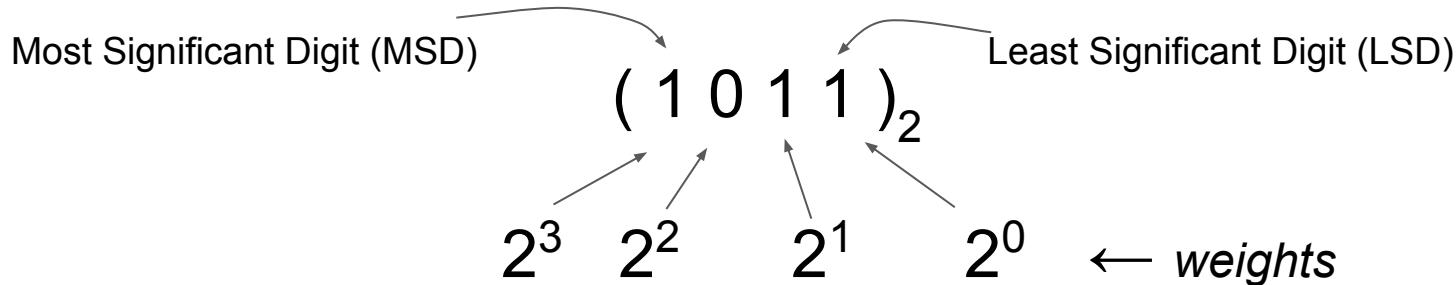


- starting with lowest weight of  $2^0$ , moving from right-to-left
- the **weight** of each digit, increases by a factor of 2
- The decimal conversion is the sum of all the weights multiplied by the digits. If the most significant digit is greater than or equal to half the base, subtract the base raised to the power of the number of digits.

$$(0111)_2 = (0 \times (2^3)) + (1 \times 2^2) + (1 \times 2^1) + (1 \times 2^0)$$
$$(0111)_2 = 0 + 4 + 2 + 1 = 7$$

# To Decimal

Example: Consider 1011, signed binary number (base-2 number)

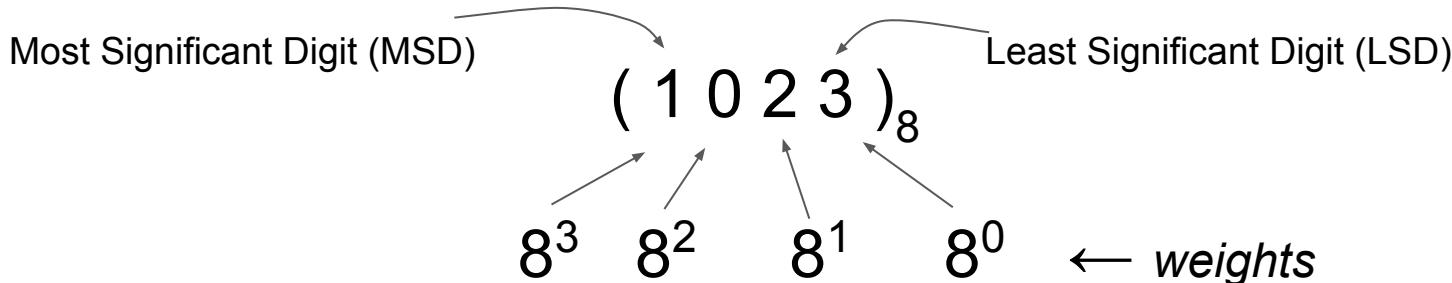


- starting with lowest weight of  $2^0$ , moving from right-to-left
- the **weight** of each digit, increases by a factor of 2
- The decimal conversion is the sum of all the weights multiplied by the digits. If the most significant digit is greater than or equal to half the base, subtract the base raised to the power of the number of digits.

$$(1011)_2 = -2^4 + (1 \times 2^3) + (0 \times 2^2) + (1 \times 2^1) + (1 \times 2^0)$$
$$(1011)_2 = -16 + 8 + 0 + 2 + 1 = -5$$

# To Decimal

Example: Consider 1023, signed hexadecimal number (base-8 number)

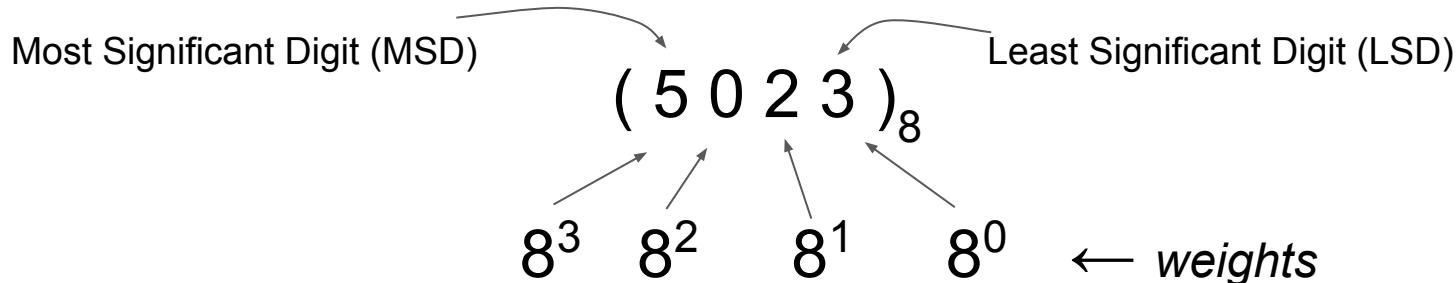


- starting with lowest weight of  $8^0$ , moving from right-to-left
- the **weight** of each digit, increases by a factor of 8
- The decimal conversion is the sum of all the weights multiplied by the digits. If the most significant digit is greater than or equal to half the base, subtract the base raised to the power of the number of digits.

$$(1023)_8 = (1 \times (8^3)) + (0 \times 8^2) + (2 \times 8^1) + (3 \times 8^0)$$
$$(1023)_8 = 512 + 0 + 16 + 3 = 531$$

# To Decimal

Example: Consider 5023, signed hexadecimal number (base-8 number)

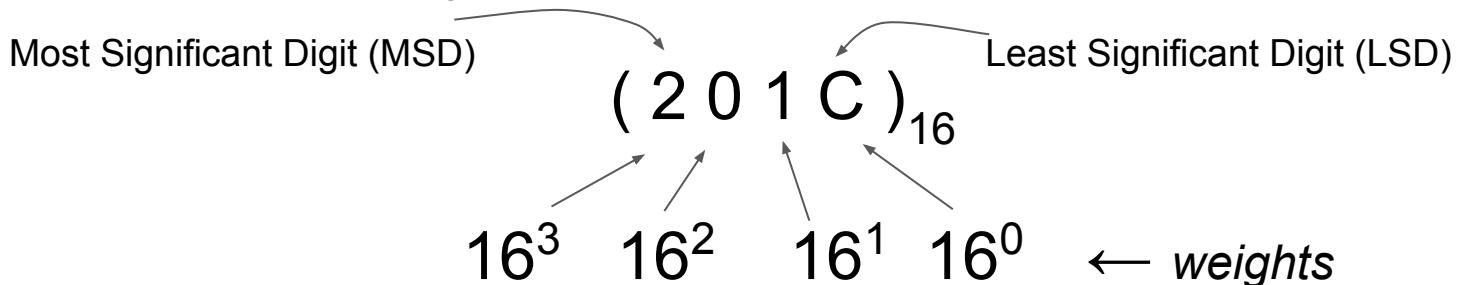


- starting with lowest weight of  $8^0$ , moving from right-to-left
- the **weight** of each digit, increases by a factor of 8
- The decimal conversion is the sum of all the weights multiplied by the digits. If the most significant digit is greater than or equal to half the base, subtract the base raised to the power of the number of digits.

$$(5023)_8 = -8^4 + (5 \times 8^3) + (0 \times 8^2) + (2 \times 8^1) + (3 \times 8^0)$$
$$(5023)_8 = -4,096 + 2,560 + 0 + 16 + 3 = -2,541$$

# To Decimal

Example: Consider 201C, signed hexadecimal number (base-16 number)



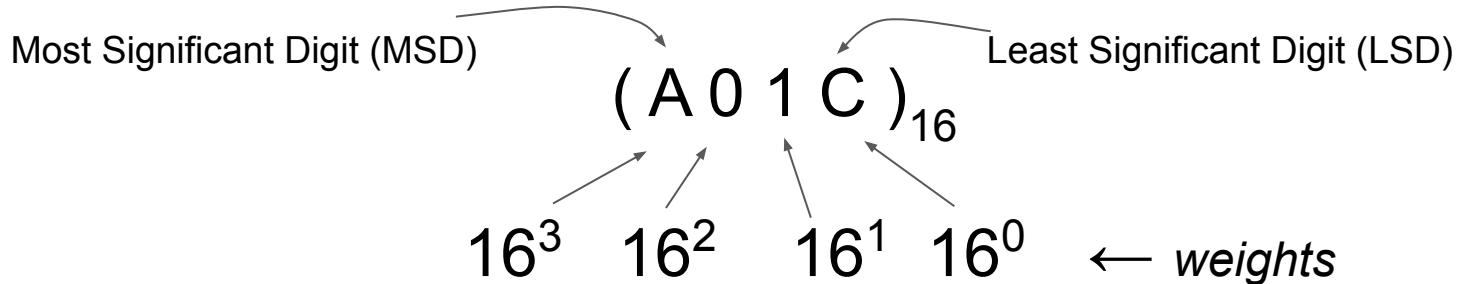
- starting with lowest weight of  $16^0$ , moving from right-to-left
- the **weight** of each digit, increases by a factor of 16
- The decimal conversion is the sum of all the weights multiplied by the digits. If the most significant digit is greater than or equal to half the base, subtract the base raised to the power of the number of digits.

$$(201C)_{16} = (2 \times (16^3)) + (0 \times 16^2) + (1 \times 16^1) + (C \times 16^0)$$

$$(201C)_{16} = 8,192 + 0 + 16 + 12 = 8,220$$

## To Decimal

Example: Consider A01C, signed hexadecimal number (base-16 number)



- starting with lowest weight of  $16^0$ , moving from right-to-left
  - the **weight** of each digit, increases by a factor of 16
  - The decimal conversion is the sum of all the weights multiplied by the digits. If the most significant digit is greater than or equal to half the base, subtract the base raised to the power of the number

$$(A01C)_{16} = -16^4 + (A \times (16^3)) + (0 \times 16^2) + (1 \times 16^1) + (C \times 16^0)$$

$$(A01C)_{16} = -65,536 + 40,960 + 0 + 16 + 12 = -24,548$$

# Decimal to Signed Binary $(25)_{10} \rightarrow (?)_2$

## Repeated Division

Divide the given decimal number by base=2.

Write the remainder after each division until a quotient of zero is obtained.

Division	Quotient	Remainder
$25/2$	12	1
$12/2$	6	0
$6/2$	3	0
$3/2$	1	1
$1/2$	0	1
-	-	0

LSB

MSB

We read the answer from the remainder column, bottom-up, adding 0 as the sign bit. If the decimal number is negative. Find the two's complement to get the final answer.

$011001_2$

# Decimal to Signed Binary $(-25)_{10} \rightarrow (?)_2$

## Repeated Division

Divide the given decimal number by base=2.

Write the remainder after each division until a quotient of zero is obtained.

Division	Quotient	Remainder
25/2	12	1
12/2	6	0
6/2	3	0
3/2	1	1
1/2	0	1
-	-	0

LSB

MSB

We read the answer from the remainder column, bottom-up, adding 0 as the sign bit. If the decimal number is negative. Find the two's complement to get the final answer.

$$(011001)_2 = 100111_2$$

answer =  $100111_2$

# Decimal to Signed Octal $(2625)_{10} \rightarrow (?)_8$

## Repeated Division

Divide the given decimal number by base=8.

Write the remainder after each division until a quotient of zero is obtained.

Division	Quotient	Remainder	
2625/8	328	1	LSB
328/8	41	0	
41/8	5	1	
5	0	5	
-	-	0	MSB

We read the answer from the remainder column, bottom-up. If the most significant digit is  $>=$  half the base, prepend a 0. If the decimal number is negative, find the two's complement to get the final answer.

05101<sub>8</sub>

# Decimal to Signed Octal $(-2625)_{10} \rightarrow (?)_8$

## Repeated Division

Divide the given decimal number by base=8.

Write the remainder after each division until a quotient of zero is obtained.

Division	Quotient	Remainder	
2625/8	328	1	LSB
328/8	41	0	
41/8	5	1	
5	0	5	
-	-	0	MSB

We read the answer from the remainder column, bottom-up. If the most significant digit is  $\geq$  half the base, prepend a 0. If the decimal number is negative, find the two's complement to get the final answer.

$$(05101)_8 = 72677_8$$

answer =  $72677_{16}$

# Decimal to Signed Hexadecimal $(2625)_{10} \rightarrow (?)_{16}$

## Repeated Division

Divide the given decimal number by base=16.

Write the remainder after each division until a quotient of zero is obtained.

Division	Quotient	Remainder	
2625/16	164	1	LSB
164/16	10	4	
10/16	0	A	
-	-	0	MSB

We read the answer from the remainder column, bottom-up. If the most significant digit is  $\geq$  half the base, prepend a 0. If the decimal number is negative, find the two's complement to get the final answer.

$$0A41_{16} = F5BF_{16}$$

answer = F5BF<sub>16</sub>

# Decimal to Signed Hexadecimal $(-2625)_{10} \rightarrow (?)_{16}$

## Repeated Division

Divide the given decimal number by base=16.

Write the remainder after each division until a quotient of zero is obtained.

Division	Quotient	Remainder	
$2625/16$	164	1	LSB
$164/16$	10	4	
$10/16$	0	A	
-	-	0	MSB

We read the answer from the remainder column, bottom-up. If the most significant digit is  $\geq$  half the base, prepend a 0. If the decimal number is negative, find the two's complement to get the final answer.

0A41<sub>16</sub>

# Signed Addition

When performing addition on two signed numbers, going from least significant digit (LSD) to most significant digit (MSD), we add the digit of each number at the current position plus any carry-over (0 or 1) from the previous addition. The remainder of this position sum becomes the digit for the current position of the larger sum. The carry-over for the next position's addition is the floor of the current position's sum divided by the base.

$$\begin{array}{r} 1 + 1 + 1 = 3 \\ \lfloor 3 / 2 \rfloor = 1 \\ 3 \% 2 = 1 \end{array} \quad \begin{array}{r} 1 \\ + 1 \\ \hline 1 \end{array}$$

$$\begin{array}{r} 0 + 4 + 2 = 6 \\ \lfloor 6 / 8 \rfloor = 0 \\ 6 \% 8 = 6 \end{array} \quad \begin{array}{r} 0 \\ + 2 \\ \hline 6 \end{array}$$

$$\begin{array}{r} 0 + 8 + 10 = 18 \\ \lfloor 18 / 16 \rfloor = 1 \\ 18 \% 16 = 2 \end{array} \quad \begin{array}{r} 1 \\ + A \\ \hline 2 \end{array}$$

# Signed Binary Addition

**Overflow** occurs when the result of an operation is too large to fit in allowed number of digits.

- When adding two signed numbers of different signs, the sign of the sum is the correct sign.
- When adding two signed numbers of the same sign, if the sign of the sum matches the sign of the two numbers, no need for further action.
- If the two numbers are negative and the MSD of the sum is less than half of the base, the sum must be padded with a negative sign. The base minus 1.
- If the two numbers are positive and the MSD of the sum is greater than or equal to half the base, the sum must be padded with a positive sign of 0.

Start at LSB

$$\text{Example: } 01010_2 + 1111110_2 \quad (10 + (-2) = 8)$$

**carry:**

1	1	1	1	1	1	1	0	0
0	0	0	0	1	0	1	1	0
+	1	1	1	1	1	1	1	0
	0	0	0	0	1	0	0	0

# Signed Binary Addition

**Overflow** occurs when the result of a binary operation is too large to fit in allowed number of bits.

- When adding two signed numbers of different signs, the sign of the sum is the correct sign.
- **When adding two signed numbers of the same sign, if the sign of the sum matches the sign of the two numbers, no need for further action.**
- If the two numbers are negative and the MSD of the sum is less than half of the base, the sum must be padded with a negative sign. The base minus 1.
- If the two numbers are positive and the MSD of the sum is greater than or equal to half the base, the sum must be padded with a positive sign of 0.

Start at LSB

$$\text{Example: } 1111001_2 + 111110_2 (-7 + (-2)) = -9$$

**carry:**

1	1	1	1	1	0	0	0	0
1	1	1	1	1	0	0	0	1
+	1	1	1	1	1	1	1	0
	1	1	1	1	0	1	1	1

# Signed Binary Addition

**Overflow** occurs when the result of a binary operation is too large to fit in allowed number of bits.

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- **If the two numbers are negative and the MSD of the sum is less than half of the base, the sum must be padded with a negative sign. The base minus 1.**
- If the two numbers are positive and the MSD of the sum is greater than or equal to half the base, the sum must be padded with a positive sign of 0.

Start at LSB

$$\text{Example: } 10000001_2 + 10000001_2 \quad (-127 + (-127) = -254)$$

<b>carry:</b>	1	0	0	0	0	0	0	1	0
	1	0	0	0	0	0	0	1	
<b>+</b>	1	0	0	0	0	0	0	1	
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1	0	0	0	0	0	0	1	0	

# Signed Binary Addition

**Overflow** occurs when the result of a binary operation is too large to fit in allowed number of bits.

- When adding two signed numbers of different signs, the sign of the sum is the correct sign.
- **When adding two signed numbers of the same sign, if the sign of the sum matches the sign of the two numbers, no need for further action.**
- If the two numbers are negative and the MSD of the sum is less than half of the base, the sum must be padded with a negative sign. The base minus 1.
- If the two numbers are positive and the MSD of the sum is greater than or equal to half the base, the sum must be padded with a positive sign of 0.

Start at LSB

Example:  $00010001_2 + 00011_2$  ( $17 + 3 = 20$ )

**carry:**

0	0	0	0	0	0	1	1	0
0	0	0	1	0	0	0	0	1
+	0	0	0	0	0	0	1	1
	0	0	0	1	0	1	0	0

# Signed Binary Addition

**Overflow** occurs when the result of a binary operation is too large to fit in allowed number of bits.

- When adding two signed numbers of different signs, the sign of the sum is the correct sign.
- When adding two signed numbers of the same sign, if the sign of the sum matches the sign of the two numbers, no need for further action.
- If the two numbers are negative and the MSD of the sum is less than half of the base, the sum must be padded with a negative sign. The base minus 1.
- **If the two numbers are positive and the MSD of the sum is greater than or equal to half the base, the sum must be padded with a positive sign of 0.**

Start at LSB

$$\text{Example: } 01000001_2 + 01000001_2 \quad (65 + 65 = 130)$$

<b>carry:</b>	0	1	0	0	0	0	0	1	0
	0	1	0	0	0	0	0	1	
<b>+</b>	0	1	0	0	0	0	0	1	
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0	1	0	0	0	0	0	1	0	

# Signed Octal Addition

**Overflow** occurs when the result of an operation is too large to fit in allowed number of digits.

- When adding two signed numbers of different signs, the sign of the sum is the correct sign.
- When adding two signed numbers of the same sign, if the sign of the sum matches the sign of the two numbers, no need for further action.
- If the two numbers are negative and the MSD of the sum is less than half of the base, the sum must be padded with a negative sign. The base minus 1.
- If the two numbers are positive and the MSD of the sum is greater than or equal to half the base, the sum must be padded with a positive sign of 0.

Start at LSB

$$\text{Example: } 23400751_8 + 73476230_8$$

The diagram illustrates the addition of two signed octal numbers:  $23400751_8$  and  $73476230_8$ . The numbers are aligned by their least significant bits (LSBs). A red arrow labeled "Start at LSB" points to the rightmost column. The first row shows the carry bits, which are 1, 0, 1, 0, 0, 1, 1, 0, 0. The second row shows the digits of the first number: 2, 3, 4, 0, 0, 7, 5, 1. The third row shows the digits of the second number: 7, 3, 4, 7, 6, 2, 3, 0. A plus sign (+) is placed to the left of the second row. The fourth row shows the sum digits: 1, 7, 0, 7, 7, 2, 0, 1. A horizontal line separates the second and third rows from the fourth row.

carry:	1	0	1	0	0	1	1	0	0
	2	3	4	0	0	7	5	1	
+	7	3	4	7	6	2	3	0	
	1	7	0	7	7	2	0	1	

# Signed Octal Addition

**Overflow** occurs when the result of a binary operation is too large to fit in allowed number of bits.

- When adding two signed numbers of different signs, the sign of the sum is the correct sign.
- **When adding two signed numbers of the same sign, if the sign of the sum matches the sign of the two numbers, no need for further action.**
- If the two numbers are negative and the MSD of the sum is less than half of the base, the sum must be padded with a negative sign. The base minus 1.
- If the two numbers are positive and the MSD of the sum is greater than or equal to half the base, the sum must be padded with a positive sign of 0.

Start at LSB

$$\text{Example: } 77771125_8 + 57210364_8$$

The diagram illustrates the addition of two signed octal numbers:  $77771125_8$  and  $57210364_8$ . The numbers are aligned by their least significant bits (LSBs). A red arrow labeled "Start at LSB" points to the rightmost column. The first row, labeled "carry" in red, shows the sequence of carries from left to right: 1, 1, 1, 1, 0, 0, 1, 1, 0. Below this row are the digits of the first number: 7, 7, 7, 7, 1, 1, 2, 5. The second row shows the digits of the second number: 5, 7, 2, 1, 0, 3, 6, 4. A horizontal line separates the carry row from the sum row. The sum row contains the digits of the resulting octal number: 5, 7, 2, 0, 1, 5, 1, 1. A plus sign (+) is placed to the left of the first number, and a horizontal line is under the sum row.

carry:	1	1	1	1	0	0	1	1	0
	7	7	7	7	1	1	2	5	
+	5	7	2	1	0	3	6	4	
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	5	7	2	0	1	5	1	1	

# Signed Octal Addition

**Overflow** occurs when the result of a binary operation is too large to fit in allowed number of bits.

- When adding two signed numbers of different signs, the sign of the sum is the correct sign.
- When adding two signed numbers of the same sign, if the sign of the sum matches the sign of the two numbers, no need for further action.
- **If the two numbers are negative and the MSD of the sum is less than half of the base, the sum must be padded with a negative sign. The base minus 1.**
- If the two numbers are positive and the MSD of the sum is greater than or equal to half the base, the sum must be padded with a positive sign of 0.

Start at LSB

$$\text{Example: } 50000001_8 + 60000001_8$$

The diagram illustrates the addition of two signed octal numbers:  $50000001_8$  and  $60000001_8$ . The numbers are aligned by their least significant bits (LSBs). A vertical arrow labeled "Start at LSB" points downwards between the two numbers. The first column contains a red "1" above the first bit of the top number, indicating a carry. The second column contains a red "0". The third column contains a red "0". The fourth column contains a red "0". The fifth column contains a red "0". The sixth column contains a red "0". The seventh column contains a red "0". The eighth column contains a red "0". The ninth column contains a red "1". Below the first column is a box containing the digit "5". Below the second column is a box containing the digit "0". Below the third column is a box containing the digit "0". Below the fourth column is a box containing the digit "0". Below the fifth column is a box containing the digit "0". Below the sixth column is a box containing the digit "0". Below the seventh column is a box containing the digit "0". Below the eighth column is a box containing the digit "0". To the left of the first column is a plus sign (+) symbol. Below the first column is a red box containing the digit "7". Below the second column is a box containing the digit "3". Below the third column is a box containing the digit "0". Below the fourth column is a box containing the digit "0". Below the fifth column is a box containing the digit "0". Below the sixth column is a box containing the digit "0". Below the seventh column is a box containing the digit "0". Below the eighth column is a box containing the digit "0". Below the ninth column is a box containing the digit "2".

carry:	1	0	0	0	0	0	0	0	1
	5	0	0	0	0	0	0	0	
+	6	0	0	0	0	0	0	0	1
	7	3	0	0	0	0	0	0	2

# Signed Octal Addition

**Overflow** occurs when the result of a binary operation is too large to fit in allowed number of bits.

- When adding two signed numbers of different signs, the sign of the sum is the correct sign.
- **When adding two signed numbers of the same sign, if the sign of the sum matches the sign of the two numbers, no need for further action.**
- If the two numbers are negative and the MSD of the sum is less than half of the base, the sum must be padded with a negative sign. The base minus 1.
- If the two numbers are positive and the MSD of the sum is greater than or equal to half the base, the sum must be padded with a positive sign of 0.

Start at LSB

Example:  $27210406_8 + 06104413_8$

<b>carry:</b>	0	1	0	0	0	1	0	1	0
	2	7	2	1	0	4	0	6	
<b>+</b>	0	6	1	0	4	4	1	3	
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	3	5	3	1	5	0	2	1	

# Signed Octal Addition

**Overflow** occurs when the result of a binary operation is too large to fit in allowed number of bits.

- When adding two signed numbers of different signs, the sign of the sum is the correct sign.
- When adding two signed numbers of the same sign, if the sign of the sum matches the sign of the two numbers, no need for further action.
- If the two numbers are negative and the MSD of the sum is less than half of the base, the sum must be padded with a negative sign. The base minus 1.
- **If the two numbers are positive and the MSD of the sum is greater than or equal to half the base, the sum must be padded with a positive sign of 0.**

Start at LSB

$$\text{Example: } 31000001_8 + 11000001_8$$

<b>carry:</b>	0	0	0	0	0	0	0	0	0
	3	1	0	0	0	0	0	0	1
<b>+</b>	1	1	0	0	0	0	0	0	1
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0	4	2	0	0	0	0	0	0	2

# Signed Hexadecimal Addition

**Overflow** occurs when the result of an operation is too large to fit in allowed number of digits.

- When adding two signed numbers of different signs, the sign of the sum is the correct sign.
- When adding two signed numbers of the same sign, if the sign of the sum matches the sign of the two numbers, no need for further action.
- If the two numbers are negative and the MSD of the sum is less than half of the base, the sum must be padded with a negative sign. The base minus 1.
- If the two numbers are positive and the MSD of the sum is greater than or equal to half the base, the sum must be padded with a positive sign of 0.

Start at LSB

$$\text{Example: } 23A00F51_{16} + FA478C30_{16}$$

The diagram illustrates the addition of two 16-bit signed hexadecimal numbers. The top row shows the numbers:  $23A00F51_{16}$  and  $FA478C30_{16}$ . The bottom row shows the sum:  $1DDEB810_{16}$ . The leftmost column contains a '+' sign and a 'carry' value of 1. Red numbers in boxes indicate the carry bit for each column. An arrow points down to the first digit of the sum, labeled 'Start at LSB'. The columns are labeled from right to left: 1, 0, 0, 0, 0, 1, 0, 0, 0, 0, F, 5, A, 3, 2, and 1.

+	F	A	4	7	8	C	3	0
<hr/>								
1	D	E	7	9	B	8	1	

# Signed Hexadecimal Addition

**Overflow** occurs when the result of a binary operation is too large to fit in allowed number of bits.

- When adding two signed numbers of different signs, the sign of the sum is the correct sign.
- **When adding two signed numbers of the same sign, if the sign of the sum matches the sign of the two numbers, no need for further action.**
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- If the two numbers are positive and the MSD of the sum is greater than or equal to half the base, the sum must be padded with a positive sign of 0.

Start at LSB

Example:  $\text{FFFFAA1A}_{16} + \text{989ACD0B}_{16}$

<b>carry:</b>	1	1	1	1	1	1	0	1	0
	F	F	F	F	A	A	1	A	
+	9	8	9	A	C	D	0	B	
<hr/>									
	9	8	9	A	7	7	2	5	

# Signed Hexadecimal Addition

**Overflow** occurs when the result of a binary operation is too large to fit in allowed number of bits.

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  - If the two numbers are positive and the MSD of the sum is greater than or equal to half the base, the sum must be padded with a positive sign of 0.

## Start at LSB

Example:  $90000001_{16} + A0000001_{16}$

## **carry:**

# Signed Hexadecimal Addition

**Overflow** occurs when the result of a binary operation is too large to fit in allowed number of bits.

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Start at LSB

Example:  $37A10B01_{16} + 2CE08011_{16}$

<b>carry:</b>	0	1	1	0	0	0	0	0	0
	3	7	A	1	0	B	0	1	
<b>+</b>	2	C	E	0	8	0	1	1	
<hr/>									
	6	4	8	1	8	B	1	2	

# Signed Hexadecimal Addition

**Overflow** occurs when the result of a binary operation is too large to fit in allowed number of bits.

- When adding two signed numbers of different signs, the sign of the sum is the correct sign.
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- **If the two numbers are positive and the MSD of the sum is greater than or equal to half the base, the sum must be padded with a positive sign of 0.**

Start at LSB

$$\text{Example: } 41000001_{16} + 71000001_{16}$$

<b>carry:</b>	0	0	0	0	0	0	0	0	0
	4	1	0	0	0	0	0	0	1
<b>+</b>	7	1	0	0	0	0	0	0	1
<hr/>									
0	B	2	0	0	0	0	0	0	2

# Signed Subtraction

For signed subtraction, find the two's complement of the second number (subtrahend) and add it to the first number (minuend).

$$\begin{aligned}\text{Difference} &= \text{minuend} - \text{subtrahend} \\ &= \text{minuend} + (-\text{subtrahend})\end{aligned}$$

$$\begin{aligned}01010_2 - 1111110_2 &= 01010_2 + 00000010_2 = 01100_2 \\1111001_2 - 111110_2 &= 1111001_2 + 000010_2 = 10111_2 \\10000001_2 - 10000001_2 &= 10000001_2 + 0111111 = 0_2 \\00010001_2 - 00011_2 &= 00010001_2 + 11101_2 = 01110_2 \\01000001_2 - 01000001_2 &= 01000001_2 + 1011111 = 0_2\end{aligned}$$

$$\begin{aligned}23400751_8 - 73476230_8 &= 23400751_8 + 04301550_8 = 27702521_8 \\77771125_8 - 57210364_8 &= 77771125_8 + 20567414_8 = 20560541_8 \\50000001_8 - 60000001_8 &= 50000001_8 + 17777777_8 = 70000000_8 \\27210406_8 - 06104413_8 &= 27210406_8 + 71673365_8 = 21103773_8 \\31000001_8 - 11000001_8 &= 31000001_8 + 66777777_8 = 20000000_8\end{aligned}$$

$$\begin{aligned}23A00F51_{16} - FA478C30_{16} &= 23A00F51_{16} + 5B873D0_{16} = 29588321_{16} \\FFFFAA1A_{16} - 989ACD0B_{16} &= FFFF AA1A_{16} + 676532F5_{16} = 6764DD0F_{16} \\90000001_{16} - A0000001_{16} &= 90000001_{16} + 5FFFFFF_{16} = \\F0000000_{16} \\37A10B01_{16} - 2CE08011_{16} &= 37A10B01_{16} + D31F7FEF_{16} = 0AC08AF0_{16} \\41000001_{16} - 71000001_{16} &= 41000001_{16} + 9FFFFFFF_{16} = B0000000_{16}\end{aligned}$$