

- (1) $\{ \langle N \rangle : N = p \cdot q \}$ where N 's product of two primes p and q
- (2) $\{ x : (x \in N) : x = p \cdot q \text{ where } p, q \text{ are prime number} \}$
- (3) all strings of the prime instance of the problem with NFA A into $\{ \langle s : A \rangle \text{ an NFA } A \text{ accept } s \}$.
- (4) the string for a NFA: $\{ \langle s \rangle : \text{An NFA } A \text{ accept } s \}$
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proof $2n^3 - 18n$ is $O(n^3)$

Take $C=3$. Then we have.

$$\lim_{n \rightarrow \infty} \frac{2n^3 - 18n}{3 \cdot n^3} = \frac{2}{3} < 1$$

proof $2n^3 - 18n$ is $O(n^4)$

Take $C=1$. Then we have

$$\lim_{n \rightarrow \infty} \frac{2n^3 - 18n}{1 \cdot n^4} = 0 < 1.$$

proof $2n^3 - 18n$ is not $O(n^2 \log n)$

there is a constant $C > 0$

$$\lim_{n \rightarrow \infty} \frac{2n^3 - 18n}{C \cdot n} = \frac{2n^2 - 18}{C} = +\infty > 1.$$

Thus, $2n^3 - 18n$ is $O(n^3)$, $O(n^4)$, is not $O(n^2 \log n)$

$$3n^2 2^{2n} \text{ is } 2^{o(n)}$$

take $C = 3$. we have.

$$\frac{3n^2 2^{2n}}{2^{3n}} = \frac{3n^2}{2^n} = o < 1.$$

$$\text{Thus } 3n^2 2^{2n} \text{ is } 2^{o(n)}$$