

Assignment -4 -Quiz

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Problem 1:

B)

$$T(n) = T(n/2) + T(n/2) + C$$

$$T(n/2) = T(n/4) + T(n/4) + C$$

$$T(n/4) = T(n/8) + T(n/8) + C$$

Total N Entries so $n * \log n = n \log n$

Problem 2:

Solution :

A)

selectionSort(vector<int> v, int n)

if n is greater than 1 base case

max = FindMaxIndex(v, n) find Max

swap(v, max, n - 1) swap Max with last index

selectionSort(v, n - 1) recursively for n-1

B)

$$T(N) = T(n-1) + n + 1$$

C)

$$T(n) = T(n-1) + n$$

$$T(n-1) = T(n-2) + n$$

$$T(n-2) = T(n-3) + n$$

$$\rightarrow n + (n-1) + (n-2) + (n-3) + \dots + 2 + 1 \rightarrow n(n+1)/2$$

by back substitution, we get $n + n + n + n + \dots$

$$n(n+1)/2 \rightarrow n^2$$

complexity is $O(n^2)$

Problem 3:

$$(a) T(n) = 4T(n/7) + 1$$

Series of Cost:

$$1 + 4^1(1) + 4^2(1) + 4^3(1) + \dots + 4^{\log_7 n}(1)$$

$$1 + 4^1(1) + 4^2(1) + 4^3(1) + \dots + n \log^4$$

Increasing series

$$\text{Cost} = O(n)$$

$$(b) T(n) = 3T(2n/3) + 2n.$$

increasing series

$$\text{Cost} = O(3 \log_3 2n)$$

$$(c) T(n) = 3T(n/3) + 2n.$$

$$\text{Cost} = O(n \log n)$$

$$(d) T(n) = T(n) + 1, \text{ and } T(2) = 1.$$

E)

$$i) T(n) = 4T(n/2) + 5n^2$$

$$\text{Cost} = O(n^2 \log n)$$

$$ii) T(n) = 4T(n/2) + 10n^2$$

$$\text{Cost} = O(n^2 \log n)$$

Problem 4:

Solution :

Assuming Array {2,0,0,1,2,1,0,2,1,0,1,1,0}

Expected output {0,0,0,0,0,1,1,1,1,1,2,2,2}

Zero Means= **RED**

One Means= **White**

Two Means= **BLUE**

we have to Sorted The data in Such a way that **RED** Comes Before **White** and **BLUE** Should Come after

Enum={**Red**,**Blue**,**White**};

Red_White_Blue_Sort(**vector**<int>keys, int n)

low = 0, high = n-1 mid = 0;

while (mid <= high)

If Keys[mid] == Red => swap(key [low++], key [mid++]) break

If Keys[mid] == White => mid ++ break

If Keys[mid] == Blue => swap(key [mid], key [high--]) break

one traversal of the Array will sort them

Swap in $O(1)$

So $O(N)$ Time Complexity