Tutorial Letter 102/0/2024

Theoretical Computer Science III

COS3701

School of Computing

Assignment 01

BAR CODE



ASSIGNMENT 01

UNIQUE ASSIGNMENT NUMBER: 170585

STUDY MATERIAL: Cohen, chapters 12 - 15

Question 1 [6]

Consider the following CFG:

$$S \rightarrow aS \mid ba$$

Prove that this generates the language defined by the regular expression a^*ba

Question 2 [8]

Find CFGs for the following languages over the alphabet $\Sigma = \{a \ b\}$:

All words that do not have the substring ab.

Question 3 [14]

Investigate each of the CFGs provided and decide whether the word *abba* is generated by the given CFGs. In the case where *abba* is not generated a brief discussion why a particular CFG does not generate *abba*. If abba is indeed generated, then draw the corresponding syntax tree illustrating the generation of *abba*.

- 1. CFG 1: $S \rightarrow aSb \mid ab$
- 2. CFG 2: $S \rightarrow aS \mid bS \mid a$
- 3. CFG 3 $S \rightarrow aS \mid aSb \mid X$ $X \rightarrow aXa \mid a$
- 4. CFG 4: $S \rightarrow aAS \mid a$ $A \rightarrow SbA \mid SS \mid ba$
- 5. CFG 5: $S \rightarrow aB \mid bA$ $A \rightarrow a \mid aS \mid bAA$ $B \rightarrow b \mid bS \mid aBB$

Question 4 [10]

Convert the grammar below to CNF.

$$\begin{array}{ll} S \rightarrow & aX \mid Yb \\ X \rightarrow & ZXZY \mid a \\ Y \rightarrow & b \mid bY \mid \Lambda \\ Z \rightarrow & a \mid \Lambda \end{array}$$

Question 5 [12]

Develop a DPDA accepting the language $L = \{b^{n+1}(ab)a^{n-1} \mid n \ge 2\}$

@ Unisa 2024