Technical Report on Integrating Data Lake Tables

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ABSTRACT

We have made tremendous strides in providing tools for data scientists to discover new tables useful for their analyses. But despite these advances, the proper integration of discovered tables has been under-explored. An interesting semantics for integration, called Full Disjunction, was proposed in the 1980's, but there has been little advancement in using Full Disjunction for data science to integrate tables culled from data lakes. We provide ALITE, the first proposal for scalable integration of tables that may have been discovered using join, union or related table search. We show that ALITE can outperform (both theoretically and empirically) previous algorithms for computing the Full Disjunction. ALITE relaxes previous assumptions that tables share common attribute names (which completely determine the join columns), are complete (without null values), and have acyclic join patterns. To evaluate our work, we develop and share three new benchmarks for integration that use real data lake tables.

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The source code, data, and/or other artifacts have been made available at https://github.com/northeastern-datalab/alite.

1 INTRODUCTION

The number of public datasets has grown immensely in open data platforms [55, 56, 79]. In addition, individual corporations have a wealth of data stored in their own data lakes. Analyzing and integrating such datasets can help governments and enterprises in making decisions and plans. Data scientists, as the main users of data, use different techniques to discover and explore the available datasets using methods such as keyword search [11, 12, 58, 76] and table search (using the data within their table as a query) [10, 48, 49, 56]. The output of such a discovery process usually includes a collection of data lake tables that may be used to enrich their analysis [15, 57]. Existing discovery techniques usually aim to discover unionable [12, 48, 56], joinable [28, 54, 76, 78–80], and related tables [10, 21, 78].

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Proceedings of the VLDB Endowment, Vol. 14, No. 1 ISSN 2150-8097. doi:XX.XX/XXX.XX Example 1. Consider the data lake tables about football stadiums shown in Fig. 1. We have added a TID (Tuple ID) column in each table to permit us to refer to tuples. Assume that a data scientist uses table T_1 as a query table to search for the top-2 unionable tables [56] and the top-2 joinable tables [81] from a data lake. Let T_2 and T_3 be the union search results and T_4 and T_5 be the join search results. Join search finds tables that join on an indicated column (in this case Location), but does not discover if there are other common (integratable) columns. For simplicity, assume that the common columns on these tables are already detected and have identical column headers. Note that in practice this will not be the case.

In real-world, after discovery, data scientists would often integrate the discovered tables before analyzing and applying statistical tools. Such integration not only extends their data but also allows them to answer queries that go beyond a single table. For instance, consider Tables T_2 , T_3 and T_4 in Fig. 1 and assume a football team has data scientists assisting in finding a new coach. Specifically, the team looks for an experienced coach that has handled teams playing in front of large crowds in new stadiums. So, they may use queries such as "coaches who coach teams having stadiums established after 2000, that accommodate at least 50 thousand spectators". Obviously, the information required here goes beyond a single table. In our example, one needs (at least) to integrate tables T_2 , T_3 and T₄ to obtain such facts, for example, Dan Campbell who coaches the Detroit Lions that has Ford Field Stadium established in 2002 and having 65k capacity (f7 in Fig. 2). Previously mentioned search methods do not address this "post-discovery" phase and do not answer the important question of how to integrate the tables (relations) obtained by the table search technique(s).

EXAMPLE 2. The standard relational union operator needs all tables to have exactly the same schema. However, this is not the case even for union search results (where tables that union on a subset of attributes can be retrieved) [56]. So to integrate the tables in Fig. 1, one can project out non-common columns and union on only the common columns. For T_1 , T_2 , and T_3 , this would just leave Location. For the joinable tables, a join on Location of T_1 with T_4 leads to tuples like t_{11} being omitted and other tuples having two attributes Stadium and Team. Worse, the natural join operator, i.e. $T_1 \bowtie T_4 \bowtie T_5$, returns an empty set because T_4 and T_5 do not have joining tuples. The problem gets more complicated if we try to integrate all five tables using these operators.

Within the data integration literature, *Full Disjunction (FD)* [33] has been understood as a natural way of assembling partial pieces of information (facts) in such a way that maximizes the connections among these facts [66]. Indeed, Rajamaran and Ullman describe the Full Disjunction as a relation with nulls (represented by \perp) such that every set of join-consistent tuples appears within a tuple of the Full

T ₁				T_2					T_3						
TID	Stadium	Location	Team	TID	Stadium	Locatio	n Oper	ned	TID		Tear	m	Location	Coach	
t ₁	NRG Stadium	Texas	Houston Texans	t _s	Soldier Field	Chicag	192	4	t ₇		Houston '	Texans	Texas	Lovie Smi	th
t ₂	AT&T Stadium	Texas	Dallas Cowboys	t ₆	Ford Field	Michiga	n 200	12	t ₈	G	reen Bay	Packers	Wisconsir	Matt LaFle	eur
t ₃	Paul Brown	Ohio	±	T					t ₉		Detroit	Lions	Michigan	Dan Campl	oell T ₅
t ₄	Sofi Stadium	California	Angeles Chargers	TIE	Stadium	1 Lo	cation	Ca	pacit	ty	TID	Stac	lium	Location	Team
			t ₁₀	NRG Stadi	um 1	exas		±		t ₁₂	Lambe	au Field	Wisconsin	Green Bay Packers	
				t ₁₁	1 Ford Field Michigan 6			65k		t ₁₃		ŧ	Ohio	Cleveland	
											t.,	Sofi St	adium	California	±

Figure 1: Tables about football stadiums, their locations and home teams. The objective is to integrate the five tables. TID is not a real data column, used for illustration. Also, metadata like column headers may not be available in real data lake tables and are used for illustration purpose. The symbol \pm represents null values present in the input tables (missing nulls).

Disjunction, with a concrete value or \perp in each attribute not found within the set of tuples. Here, join-consistent is defined as common attributes (attributes with the same name), so this is effectively a *natural Full Disjunction*. The widely known outer-join [46, 67] is not associative (hence the result depends on the order in which tables are integrated) and does not aim to maximize the connections among the integrated tuples [33, 51].

Example 3. Outer-join and outer-union keep all tuples and columns and pad non-matching tuples (respectively, columns) with nulls [18, 46]. The outer-union of the tables from Fig. 1 is depicted in Fig. 2(a). In this example, outer-union does not maximally connect the facts in the original tables. Here, \pm indicates a missing value in the original tables and \perp represents a null introduced by the outerunion operator. In particular, outer union includes partial facts like t_{10} that are made redundant by more complete facts like t_1 . Similar observations can be made of the outer-join results. Hence, Galindo-Legario defined the Full Disjunction (FD) [33]. Informally, it removes redundant facts and produces, in this example, the first 8 tuples (mustard colored) of Fig. 2(b). FD can be viewed as an associative version of outer join [19] and has been used to integrate information across relational tables [19, 59] and web tables [59]. Notice in this example, FD uses information from all five tables so it is important to be able to compute FD over (possibly large) sets of tables.

However, using FD in data lakes poses several important challenges: 1) First, we cannot rely on common attributes having the same name as in our example. Instead, we must discover what the common attributes are [55]. We will use schema matching for this purposed [64]. Notice that we are not given just two schemas that need to be matched, rather we have a set of tables all of which could potentially share attributes with some or many of the other tables. Hence, we will use holistic schema matching [65]. 2) Second, we cannot assume that integrated datasets are complete (that is, they may actually contain null values or partial (redundant) facts). 3) Finally, previous work on Full Disjunction has been done on relatively small relations (with only 1000 or so tuples per relation [19]) or assumes the common attributes form graphs with specific acyclic structures [66]. To the best of our knowledge, the only work on using FD on larger datasets requires that all joins be done on attributes having a key-to-foreign-key relationships [59], a strict requirement that makes the technique only applicable within well-designed enterprise scenarios, not the possibly messy tables retrieved from data lakes commonly used in data science.

We assume data scientists use table discovery algorithms to identify a set of tables that they wish to integrate. Regardless of the search technique, we wish to find the best way to integrate the tables. Specifically, we propose a table integration technique ALITE (Align and Integrate) that first applies schema matching to identify common columns in a set of tables to be integrated. Matched columns are given the same integration ID. We then apply a natural FD over the tables using integration IDs as attribute names.

Contributions. Our main contributions are as follows: (1) To the best of our knowledge, we introduce the problem of integrating data lake tables obtained using table discovery algorithms. (2) A new holistic schema matching algorithm for sets of tables that we show out-performs the state-of-the-art matchers on real data lake tables. (3) We compare the FD used as the integration semantics in ALITE to several other semantics and show the difference and superiority of FD. (4) We propose a novel scalable algorithm to compute the FD by using complementation and subsumption operators in a novel way. We show that the use of these operators permits optimizations that make the computation faster than the state-of-the-art techniques, both theoretically and experimentally. Specifically, ALITE scales better than the state-of-the-art FD algorithms on data lake tables, which are typically large and may have complex join graphs. (5) We introduce and share several open data integration benchmarks.

2 PRELIMINARIES

We now provide the building blocks for integrating tables in a data lake setting, namely, specifying the notation and the basic integration operators, after which we formally define the problem.

Table 1: Symbols used in this paper and their definitions

Symbol	Definition	Symbol	Definition
$\mathcal{T}(n= \mathcal{T})$	Set of Tables	r	Set of tuples
$T(T_i)$	Table (the i_{th} table in T)	t[A]	Value of t on the column A
A(T.A)	Column (Column A in Table T)	S(S = S)	Set of all input tuples
m_i	Arity of Table T_i	$\mathcal{F}(F = \mathcal{F})$	Set of output tuples
$\mathcal{A}(T)$	Schema (set of columns) of T	±	Null denoting a missing value
t	Tuple	1	Null produced by an operator

Notation. Table 1 summarizes the notation we use in the paper. For any operator, let S (and its size S) and F (and its size F) denote the collective set of all input and output tuples, respectively. We use two types of nulls, \pm denotes a *missing value* from an incomplete input relation to be integrated and \perp denotes a *produced null*, a null value that is introduced by an operator during integration.

TID	Stadium	Location	Team	Opened	Coach	Capacity
t ₁	NRG Stadium	Texas	Houston Texans	T	1	T
t ₂	AT&T Stadium	Texas	Dallas Cowboys	T	1	T
t ₃	Paul Brown	Ohio	±	T	1	T
t ₄	Sofi Stadium	California	Angeles Chargers	T	1	T
t ₅	Soldier Field	Chicago	1	1924	1	T
t ₆	Ford Field	Michigan	1	2002	1	T
t,	1	Texas	Houston Texans	T	Lovie Smith	T
t ₈	1	Wisconsin	Green Bay Packers	T	Matt LaFleur	T
t ₉	1	Michigan	Detroit Lions	T	Dan Campbell	T
t ₁₀	NRG Stadium	Texas	1	T	1	±
t ₁₁	Ford Field	Michigan	1	T	1	65k
t ₁₂	Lambeau Field	Wisconsin	Green Bay Packers	Ţ	1	T
t ₁₃	±	Ohio	Cleveland	1	1	1
t ₁₄	Sofi Stadium	California	±	1	1	1
		(a) T1	⊌ T2 ⊌ T3 ⊌ T4 ⊌ 1	Γ5		

OID	TID	Stadium	Location	Team	Opened	Coach	Capacity
f ₁	{t1, t, t10}	NRG Stadium	Texas	Houston Texans	1	Lovie Smith	±
f ₂	{t ₂ }	AT&T Stadium	Texas	Dallas Cowboys	1	1	T
f ₃	{t ₃ }	Paul Brown	Ohio	±	1	1	T
f ₄	{t ₁₃ }	±	Ohio	Cleveland	1	1	T
f ₅	{t ₄ }	Sofi Stadium	California	Angeles Chargers	1	1	T
f ₆	{t ₅ }	Soldier Field	Chicago	1	1924	1	T
f ₇	{t ₆ ,t ₉ ,t ₁₁ }	Ford Field	Michigan	Detroit Lions	2002	Dan Campbell	65k
f ₈	{t ₈ , t ₁₂ }	Lambeau Field	Wisconsin	Green Bay Packers	1	Matt LaFleur	T
f ₉	{t ₃ , t ₁₃ }	Paul Brown	Ohio	Cleveland	1	1	T
f ₁₀	t ₁₄	Sofi Stadium	California	±	1	1	T

- FD(T₁, T₂, T₃, T₄, T₅) = {f₁, f₂, f₃, f₄, f₅, f₆, f₇, f₈}
- FD_{tuple-set}(T₁, T₂, T₃, T₄, T₅) = FD(T₁, T₂, T₃, T₄, T₅) ∪ {f₁₀}
- $T_1 \boxplus T_2 \boxplus T_3 \boxplus T_4 \boxplus T_5 = \mathsf{FD}(\mathsf{T}_1, \mathsf{T}_2, \mathsf{T}_3, \mathsf{T}_4, \mathsf{T}_5) \{f_3, f_4\} \cup \{f_9, f_{10}\}$ (b) Output tuples generated using different operators

Figure 2: Result of integrating the tables in Fig. 1 using different techniques. The table in (a) is the result of outer unioning the five tables. The table in (b) is the union of tuples obtained using FD (first eight tuples in mustard), a variant called tuple-set FD (which is the FD plus f_{10}) and Complement Union (\boxplus). A unique Output ID (OID) is provided for each output tuple for clarity.

EXAMPLE 4. Consider Table T_1 of Fig. 1. The schema of T_1 is $\mathcal{A}(T_1) = \{Stadium, Location, Team\}$. Tuple $t_3 = \{Paul Brown, Ohio, \pm\}$ has attribute value $t_3[Stadium] = Paul Brown$ and a missing null on the Team column, i.e., $t_3[Team] = \pm$.

2.1 Finding Common Columns

Our introductory example is unrealistic because common (or in relational terms join-consistent) columns from different tables have the same name and columns that are not common have different names. This will not be the case in most realistic examples. Hence, we will begin by using schema matching to assign *integration ids* to columns such that two matched columns will have the same id and two columns that are not matched will have different ids. We will ensure no two columns in the same table share an integration id. Accordingly, we will set $\mathcal{A}(T)$ to be the set of integration ids of T's columns. This problem can also be seen as a form of holistic schema matching [65] (see Section 3 and Section 4).

2.2 Integration Operators

We assume that the reader is familiar with the elementary relational algebra operators like union (\cup) , join (\bowtie) and outer join (\bowtie) [67] based on which, we now introduce some (less well known) operators that we use as components of an integration solution.

Outer Union (\uplus) is an extension to the union operator. It unions tables even if they do not have the same schema [18]. The outer union between T_1 and T_2 is denoted by $T_1 \uplus T_2$. For each $A \in \mathcal{A}(T_1) - \mathcal{A}(T_2)$, we pad T_2 with a new column A containing nulls (specifically \bot). Similarly, for each $A \in \mathcal{A}(T_2) - \mathcal{A}(T_1)$, we pad T_1 with a new column A containing nulls. We then union the padded relations.

EXAMPLE 5. The outer union of the tables in Fig. 1 is shown in Fig. 2(a). Here, the input size (|S| = 14) is the same as the output size ($|\mathcal{F}| = 14$) but the output may be smaller if there are duplicates.

Subsumption (β). Given two different tuples t_1 and t_2 having the same schema, the tuple t_1 (subsuming tuple) *subsumes* t_2 (subsumed tuple), denoted by $t_1 \supset t_2$, if all the non-null values of t_2 are equal to that of t_1 on the respective columns and t_1 has fewer null values (either missing or produced) than t_2 [7, 33]. We denote the subsumption operation using β where $\beta(r)$ contains all tuples of r that are not subsumed by another tuple in r. Applying subsumption

to the outer union result is called the *minimum union* (\bigoplus) [33]. An example of minimal union (\bigoplus) of tables in Fig. 1 is the set $\{t_1, t_2, t_3, t_4, t_5, t_6, t_7, t_8, t_9, t_{11}, t_{12}, t_{13}\}$. This is because the tuple t_{10} is subsumed by t_1 and t_{14} is subsumed by t_4 . In this example, the size of the input (|S| = 14) is larger than the output (|F| = 12).

Complementation (κ). Two different tuples t_1 and t_2 having the same schema complement each other if: 1) there is at least one column A on which they have equal and non-null values; 2) for every column A where both tuples are non-null, the tuples must have the same value on A; 3) there is at least one column A on which t_1 is non-null and t_2 is null (missing or produced); and 4) there is at least one column A on which t_2 is non-null and t_1 is null (missing or produced) [7, 9]. The complementation of t_1 and t_2 is a tuple t_3 where for any column A, $t_3[A] = t_1[A]$ if either $t_1[A]$ is non-null or both $t_1[A]$ and $t_2[A]$ are non-null (and therefore equal) or $t_1[A] = \pm$. Otherwise, if $t_2[A]$ is non-null $t_3[A] = t_2[A]$. For the case where both values are null, if $t_1[A] = t_2[A] = \bot$ then $t_3[A] = \bot$ otherwise (at least one of the nulls is missing) $t_3[A] =$ \pm . The complementation operator (κ) replaces all complemented pairs of tuples with their complementation. Note that a tuple that results from complementation could be complemented by other tuples so the complementation operator is the iterative result of applying complementation to a relation until it contains no further complementing tuples. Applying complementation over a set of outer unioned tuples, is known as *complement union* (⊞).

Example 6. In Table(a) of Fig. 2, tuples t_3 and t_{13} complement each other. Their complementation is denoted as f_9 in Fig. 2(b), i.e., $\kappa(t_3,t_{13})=f_9$. So complementation can overcombine tuples that do not agree on all their common attributes. In this example, T_5 asserts that Cleveland is a team in Ohio with an unknown stadium while T_1 asserts that Paul Brown is a stadium in Ohio. But we do not definitively know that Paul Brown is the stadium of Cleveland. The complement union of the tables in Fig. 1, i.e., $T_1 \boxplus T_2 \boxplus \cdots \boxplus T_5$ is the set of tuples in Table (b) of Fig. 2 excluding tuples $\{f_3,f_4\}$. Note that complementation union may not remove all subsumable tuples (e.g. f_{10} , which can be subsumed by f_5 , is not complemented by f_5 since the fourth condition of complementation is not met).

2.3 Full Disjunction

The operators of the previous section offer possible semantics for integrating tables. In 1994, Galindo-Legario proposed a different semantics called Full Disjunction (FD). His proposal is essentially a commutative, associate form of outer-join. We will now define the terms that we need to define FD. We say that $t_1 \in T_1$ and $t_2 \in T_2$ are connected tuples if their schemas overlap, i.e., $\mathcal{A}(T_1) \cap \mathcal{A}(T_2) \neq \emptyset$. As in outer join, two connected tuples $t_1 \in T_1$ and $t_2 \in T_2$ can be integrated (or joined) if and only if $t_1[A] = t_2[A]$, $t_1[A] \neq \pm$ and $t_2[A] \neq \pm, \forall A \in \mathcal{A}(T_1) \cap \mathcal{A}(T_2)$. The tuples generated after an integration are referred to as integrated tuples. When more than two tables are involved, the integration can be viewed as an iterative process in which an integrated tuple can be further integrated with another connected tuple, following the same conditions as before. Finally, like in outer join, if an input tuple t can not be integrated with other tuples, it will be padded by produced nulls (\bot) and considered as integrated tuple. Note that integrating those tuples that have missing nulls on their common columns may produce semantically incorrect tuples. Consider tuples t_3 from T_1 , and t_{13} from T_5 , while they share the value Ohio on Location, the value of Stadium is known in t_3 (Paul Brown), it is unknown in t_{13} . Therefore, we will not integrate these tuples. Notably, FD was later proposed as the right semantics for integrating web data [66].

EXAMPLE 7. The FD of the five tables from Fig. 1 is the set of tuples $\{f_1, ..., f_8\}$ depicted in mustard in Fig. 2(b). Unlike complementation union (Example 6), FD does not overcombine tuples t_3 and t_{13} since Team in t_3 is unknown. Hence, it contains f_3 and f_4 after integration and does not produce f_9 . Also, f_{10} is subsumed by f_5 .

FD has been shown to produce what has been called *maximally integrated tuples* [41]. We follow Kanza and Sagiv [41] by defining FD based on maximally integrated tuples.

DEFINITION 8 (MAXIMALLY INTEGRATED TUPLE). Given a set of integrated tuples r. Any tuple $t \in r$ is said to be a maximally integrated tuple if it is not subsumed by any other tuples of r [41].

DEFINITION 9 (FULL DISJUNCTION (FD)). The Full Disjunction of the tables $T_1, T_2, ... T_n$ is the set of all maximally integrated tuples that can be generated from S input tuples of $T_1, T_2, ... T_n$ [41].

In Section 5, we will introduce an algorithm that computes FD based on Definition 9. The FD definition we use [41] is based on tuples [33], rather than tuple-sets $(FD_{tuple-set})$ [19, 20]. $FD_{tuple-set}$ applies subsumption based on sets of tuples rather than the actual tuples [20] and considers a tuple set r_1 as the subsumption of tuple set r_2 if r_1 is a superset of r_2 . Note that $FD_{tuple-set}$ yields a set of maximally integrated tuple sets, but might contain tuples that subsume each other, as we discuss in the next example.

EXAMPLE 10. To illustrate the difference between FD and $FD_{tuple-set}$, consider Fig. 2(b). To understand the subsumption in $FD_{tuple-set}$, first consider f_3 and f_9 as tuple sets having tuples $\{t_3\}$ and $\{t_3, t_{13}\}$ respectively. As f_9 contains all tuples of f_3 (t_3 in this case), f_3 is contained in f_9 and hence, f_9 is the superset of f_3 . Therefore, according to [19, 20], f_{10} subsumes f_4 . However, if we consider tuple sets f_5 and f_{10} having tuples $\{t_4\}$ and $\{t_{14}\}$, respectively, f_5 is not a superset of f_{10} so, accordingly, f_5 does not subsume f_{10} .

Therefore, $FD_{tuple-set}$ returns the tuple f_{10} , which is not produced by FD as it gets subsumed by f_5 .

2.4 Solution Overview

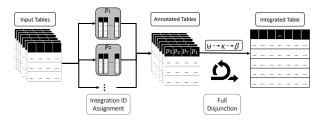


Figure 3: An overview of ALITE.

We introduced and formally defined our problem of integrating data lake tables. Fig. 3 illustrates the entire ALITE pipeline that we propose as a solution. We assume that we are given a set of tables. The first step (Fig. 3 left part) is to assign each column with a column header which we call *Integration ID* (Section 4). After assigning such IDs, the tables are annotated (Figure 3 middle part) and can be used to in applying FD to integrate the tables (Section 5).

3 RELATED WORK

We now discuss related work mainly revolving around assigning the column integration IDs and applying FD.

Assigning Column Integration IDs. The problem of assigning column integration IDs aims at providing correspondences between columns that can be integrated. In a traditional database setting, this problem is usually referred to as schema matching [64], a longstanding problem of identifying correspondences among database attributes. Numerous algorithmic attempts have been suggested over the years for handling the matching problem, e.g., COMA [27], Similarity Flooding [52], BigGorilla [16], and ADnEV [70]. A common assumption for most of this work is the existence of consistent and complete metadata, an unrealistic assumption in data lake tables [55]. Recently, Koutras et al. explored the use of traditional schema matching methods in the scope of data lakes [45]. However, the work covered is limited to finding pairs of matching columns whereas, our objective is to assign integration IDs to a set of tables to be integrated in a holistic manner. Holistic schema matching, i.e., matching a set of schemas at the same time, has received some attention in the literature [36, 62, 71], mainly revolving around web tables and assuming metadata is reliable and complete. Specifically, some work [3, 62] presents a clustering-based approach. While similar to what we will present (Section 4), their clustering method uses schema information rather than data values as we suggest here. Recall that data lake tables generally lack reliable metadata [30, 55].

Other related work includes searching for unionable [12, 48, 56], joinable [28, 54, 76, 78–80], and related [10, 21, 78] tables, for which the designed methods are usually based on column relationships. For example, in order to find unionable tables, TUS [56] first aims at finding unionable columns. Similarly, T3L [10] assesses table relatedness by assessing their attribute relatedness. Our work uses a similar methodology to TUS [56] and T3L [10] based on embeddings. However, here we make use of an embedding that was designed for

tables, namely, TURL [25]. We are also, to the best of our knowledge, the first to make use of TURL [25] for data lake tables.

Full Disjunction. Full disjunction (FD) was initially defined by Galindo-Legaria as an associative alternative for the outer join operator [33]. Galindo-Legaria used algebraic relationships to express the outer join in terms of inner join and minimum union, which is known as join-disjunctive form or Full Disjunction (FD) [33]. The inner joins between each table pair, triple, etc., are computed. The resulting tuples are then outer-unioned and the subsumable tuples are removed to get the FD. Rajaraman and Ullman showed that a fixed ordering of outer joins can give the FD iff the input tables form a y-acylic hypergraph. Hence, for the y-acylic case, the FD can be computed in linear time in the output size [66]. Kanza and Sagiv showed that FD can be computed for any arbitrary set of tables in $O(n^5S^2F^2)$ time [41] where, recall n is the number of input tables, S is the total of number of input tuples, and F is the number of FD output tuples. This is the first work to show that FD can be computed for any set of tables in polynomial time in input-output complexity [75]. Other work considers FD in terms of tuple sets rather than actual tuples [19, 20]. Cohen and Sagiv introduced an algorithm that computes k FD tuples in a given ranking order [20] and improved the worst-case time complexity over Kanza and Sagiv [41] to compute the full results. Cohen et al. also proposed an algorithm called BICOMNLO7 that computes each FD tuple with polynomial delay [19]. As we want to integrate all input tables, we compute the full FD result instead of a partial result. The worst-case time complexity of BICOMNLO7 to compute full FD is linear in the output size which is an improvement over the prior work [20]. Note that both INCREMENTALFD [20] and BICOMNLO [19] perform subsumption in terms of tuple sets rather than actual tuples. Hence, they may produce subsumable tuples in their FD result (specifically, they may produce a proper superset of the FD). Note that, when there are no missing values (±) and subsumable tuples in the input relations, these algorithms compute the FD [33]. The difference between the FD and tuple-set based FD is illustrated in Example 10. As data lake tables may contain many missing nulls and subsumable tuples, we use FD. Our experiments (Section 6) show that in real data lakes the difference between the FD and the tuple-set FD [19, 20] can be substantial and that the original definition of FD, which maximally integrates tuples, is preferred.

Recently, Paganelli et al. [59] revised Cohen and Sagiv's INCRE-MENTALFD [20] and Cohen et al.'s BICOMNLOf [19] to compute the FD in a distributed environment. They also introduced a new algorithm called ParaFD that outperforms INCREMENTALFD and BICOMNLO3 while computing FD using multiple machines. ParaFD first finds all the spanning trees in the scheme graph of the input table schemas. Then, it applies outer join based on Hash-star join to integrate tables following the order on each spanning trees by using Primary Key-Foreign Key relationship. Finally, it applies subsumption to obtain FD result. Note that, ParaFD can be used only for sets of relational tables on which all joins are key to foreign-key joins. In our work, we consider the general case of arbitrary joins. To modify ParaFD for arbitrary join, one needs to use full outer join without Hash-star join over each spanning tree. But for real data lake tables forming complex scheme graphs, the number of spanning trees can be very large. For instance, for a complete scheme graph (i.e. each table is connected to each of other tables) having n tables, the

number of spanning trees is equal to n^{n-2} [1]. One needs to apply outer join over each spanning tree that makes ParaFD inefficient similar to the baseline suggested by Galindo-Legaria [33].

Other research considers integrating data from relational and web tables and handling conflicts between the data values [6-9]. Bleiholder et al. introduced complement union operator that integrates tuples under uncertainty(a conflict between a null value and a non-null value) [9]. In the absence of missing nulls (\pm), the complement union operator is the same as FD. Yet, in the common case of tables with missing nulls, complement union may over-combine the tuples having null values on the join columns (see Example 6).

4 ASSIGNING COLUMN INTEGRATION IDS

We now explain the first stage of ALITE, namely assigning integration IDs to the columns of the input tables. We assume that the schemas $\mathcal{A}(T) = A_1, A_2, \ldots, A_m$ of all the tables $T \in \mathcal{T}$ are opaque [40]. So, our goal, in this stage, is to annotate the columns with *integration IDs*. An integration ID $p(A) \in \mathcal{P}$ is associated with each column. The same integration ID can be associated with a set of columns – these column match (and will be integrated). We now formally define the column integration ID assignment problem.

Definition 11 (Integration ID Assignment Problem). Given a set of input tables $\mathcal{T} = \{T_1, T_2, \dots T_n\}$, the column integration ID assignment problem is to assign each column an integration ID in \mathcal{P} such that columns in the same table get distinct integration IDs.

$$\forall T \in \mathcal{T} \not\exists A \in \mathcal{A}(T), A' \in \mathcal{A}(T) \land A \neq A' p(A) = p(A')$$

As discussed in Section 3, this problem can also be seen as a variation of holistic schema matching [71]. Specifically, it can be seen as a 1 : 1 matching constraint, in which an attribute can match at most one attribute from each of the other tables and cannot be matched with an attribute from the same table.

Finding Column Integration IDs with ALITE. We now aim to find column integration IDs by positioning the problem as clustering over the columns. In order to apply clustering over columns, we use their values (assuming the metadata is missing or unreliable) to create embeddings over which a clustering algorithm can be applied. Formally, a column A is embedded into a numeric vector vec(A), allowing the creation of a similarity matrix. Obtaining an embedding for data lake columns is far from trivial. TUS [56], for example, uses embeddings from fastText [39], a word embedding method based on natural text representations, to assess column unionability of string columns. Recently, Deng et al., have proposed TURL that creates embeddings based on a representation of each table [25]. In this work, we explore the use of TURL to represent columns of data lake tables. Once the embeddings for the columns are set, we need to define a similarity/distance measure to be used in the clustering algorithm (in our experiments we use euclidean distance). Having defined the embeddings and the distance measure, we follow a hierarchical clustering methodology to create the clusters out of which the column integration IDs are obtained. We ensure that the clustering algorithm does not allow columns from the same table to be assigned to the same cluster. Hierarchical clustering works iteratively. First, each data point (in our case attribute) is assigned with a cluster. Then, at each iteration the two closest clusters (by some metric) are merged to generate a new cluster. The algorithm terminates when all the data points are assigned to the

same cluster. The hierarchical clustering result is usually described using a dendrogram, which is a type of tree that illustrates the different clusters that can be generated at each iteration [47]. Using the dendrogram, we select a specific cluster as we discuss next.

Selecting the Number of Integration IDs. An important parameter in any clustering algorithm is the number of clusters [35], which, in our case corresponds to the number of column integration IDs. While traditional approaches assume that the number of clusters is a given parameter, an alternative is to tie this number to clustering quality [42]. Several clustering quality evaluation methods exist in the literature based on inter-cluster and intracluster distances [13, 24, 68]. The objective, which we also share in this paper, is to cluster similar columns together (i.e., reduce intracluster distance) and avoid similar columns in different clusters (i.e., increase inter-cluster distance).

We follow an approach similar to the elbow method [5] to determine the number of clusters that maximizes some (unsupervised) clustering quality measure. Specifically, in the experiments we use the well-known Silhouette Coefficient [68]. Let $\{p_1, p_2, ..., p_K\}$ be K clusters, each containing a set of attributes. The silhouette coefficient $\psi_s(A)$ for an attribute A in a cluster is defined as:

$$in(A) = \frac{\sum_{A' \in p \setminus \{A\}} d(A, A')}{|p|} \quad out(A) = \min_{1 \le i \le K, i \ne j} \frac{\sum_{A' \in p_i} d(A, A')}{|p_i|}$$
$$\psi_s(A) = \frac{out(A) - in(A)}{\max(in(A), out(A))}$$

where $d(\cdot, \cdot)$ is a distance measure . The silhouette of a set of clusters is calculated by averaging over all attributes of all clusters.

We also need to define the scope of this search, i.e., what are the possible values for the number of clusters. Recall that the columns from the same input table cannot be assigned to the same cluster. Therefore, if $m_1, m_2 \dots m_n$ are the number of columns in the input tables $T_1, T_2 \dots T_n$, the minimum number of clusters is given by $\max(m_1, m_2 \dots m_n)$. Also, the maximum number of clusters is given by $\sum_{i=1}^n m_i$. The latter represents the case when each input column forms a separate cluster and the bound can be even tighter if we know that the scheme graph of the input tables is connected. A figure that zooms in the left part of Fig. 3 and summarizes the Column Integration ID assignment is in Appendix A.1.

Example 12. Consider Fig. 1, we need to assign integration IDs to the columns of tables. Here, we expect to have six clusters, each for [Stadium, Location, Team, Opened, Coach, Capacity] as our columns labels show the ground truth. We use a clustering algorithm that computes the clustering quality score starting from the minimum number of clusters (3), to the maximum (15). Recall TID is not a real column and was added so we can clearly refer to tuples. The Silhouette coefficient over the TURL embeddings is computed for all values from 3 to 15 and plotted in Appendix A.1. It starts from 3 and has a maximum at 6. Then it decreases monotonically from 7 to 15. Hence, we would pick 6 as the optimal number of clusters and the clustering created in this simple example does reflect the ground truth. The four Stadium attributes are assigned the same integration ID, and the single Opened attribute is assigned a different integration ID not shared by other columns.

5 INTEGRATING TABLES

Once we find the column integration IDs, ALITE uses them to integrate the tables using a novel algorithm for computing Full Disjunction. We show that our algorithm is correct and that both asymptotically and in practice is faster than existing algorithms.

Algorithm 1: ALITE Full Disjunction

- Input: A set of tables with integration IDs as column names $\mathcal{T} = \{T_1, T_2, \dots T_n\}$ 2 Output: The Natural Full Disjunction of \mathcal{T} $FD(\mathcal{T})$ 3 $\mathcal{T} :=$ GenerateLabeledNulls(\mathcal{T})
 4 $U_{\text{ou}} \leftarrow T_1 \uplus T_2 \uplus \cdots \uplus T_n$ //Apply outer union
 5 $U_{\text{comp}} :=$ Complement(U_{ou} , n)
- 6 $U_{\text{comp}} := \text{RemoveLabeledNulls}(U_{\text{comp}})$
- 7 $T' \leftarrow \beta(U_{comp})$ //Apply subsumption
- 8 Output T'

5.1 ALITE FD Algorithm

The input of Algorithm 1 is a set of tables \mathcal{T} to be integrated with each column labeled with its integration ID. A table $T \in \mathcal{T}$ is a set of tuples. The two main properties the algorithm uses are that the output is composed of all maximally integrated tuples over the input tuples (Definition 9) and should not contain subsumable tuples. ALITE's pseudo code is provided in Algorithm 1. We make use of the following property, complementation (Line 5) over the outer union (Line 4) generates all maximally integrated tuples if the input relations contain no null values. Of course, our data lake tables will contain null values (\pm) so we begin by replacing these with distinct labeled nulls (Line 3). We then apply complementation treating the labeled nulls as distinct so they cannot be equated. We can then replace all distinct labeled nulls with the same missing value (\pm) (Line 6) and apply subsumption (Line 7) as a final step to compute the FD. Next, we will explain each step in detail.

Generating Labeled Nulls. Complementation produces all maximally integrated tuples only if the input tables have no null values (\pm) . Hence, to prevent over-jealous combining of tuples, we replace nulls (\pm) , with distinct labeled nulls which are not equal to each other, to \pm , \bot , or any constant (non-null) in any table. This avoids undesirable complementation (and generates only integrated tuples). Specifically, the first step of Algorithm 1 (Line 3) is to replace missing nulls in the input tables with the *distinct labeled nulls* and store them in a set N. This step ensures that the complementation will not integrate tuples having null values on join columns.

Example 13. We use our running example (Fig. 1) throughout the description of the algorithm for clarity. Since we have four missing nulls in the tables (one each on T_1 and T_4 and two in T_5), we replace them with four distinct labeled nulls. After replacement, they are treated similar to other non-null values.

Now we outer union all the input tables and store the resulting tuples in a set U_{ou} (Line 4). The result of outer unioning the tables in Fig. 1 is shown in Fig. 2(a). Next, Line 5 passes the set of outer unioned tuples (U_{ou}) and the total number of tables (n) to Algorithm 2 which returns all the maximally integrated tuples along with (possibly) subsumable tuples.

Algorithm 2: Complement

```
1 Input: A set of outer unioned tuples U_{ou} and the no. of tables n
 <sup>2</sup> Output: A set of tuples after complementation U_{comp}
 U_{temp} := U_{ou}
 U_{\text{comp}} \leftarrow \emptyset
 5 for i in range(1,n) do
         for t_1 \in U_{temp} do
              complement_count = 0
              for t_2 \in U_{ou} do
                   R, complement_status = \kappa(t_1, t_2)
                   if complement_status then
10
                        U_{comp} \leftarrow U_{comp} \cup R
                        complement\_count \leftarrow complement\_count + 1
12
13
              if complement_count = 0 then
               U_{comp} \leftarrow U_{comp} \cup \{t_1\}
14
15
         if U_{temp} = U_{comp} then
16
17
         else
             U_{temp} \leftarrow U_{comp}; U_{comp} \leftarrow \emptyset
19 Output Ucomp
```

Complementation Step (Algorithm 2). As we mentioned before, the objective of this step is to generate all the maximally integrated tuples. First, we prepare two sets to perform the complementation, namely, U_{temp} , initially a duplicate of U_{ou} , and U_{comp} which will hold the complementation result Line 3-4. We start complementing the tuples in U_{temp} with outer unioned tuples (Line 5). For each tuple in U_{temp} , we find a complementing partner in U_{ou} and if at least one complementing partner is found, we add the result of complementation to U_{comp} (Line 9-12). However, if a tuple in U_{temp} does not have any complementing tuples, we add the tuple to U_{comp} (Line 13-14). This ensures that the tuples having no join partners are also included in the FD results. After we go through all the tuples in U_{temp} , we check if U_{temp} and U_{comp} have the same tuples. If this is true, it means that there are no more complementing tuples left and hence, we stop the complementation (Line 15-17). If they are not equal, there may be tuples that can be complemented. Therefore, we go for another round of complementation.

Example 14. Consider Table (a) and (b) of Fig. 2. Table (a) is the result of outer unioning the tables in Fig. 1 and Table (b) holds the resulting tuples given by different integration techniques. Consider Algorithm 2 which has as input a set of tuples to be complemented along with the total number of tables. In the complementation first round (Line 5-18 for i = 1), both U_{ou} and U_{temp} are the same and they contain the tuples t_1 , t_7 and t_{10} . All these three tuples integrate with each other. Assume that the labeled null in t_{10} was replaced by a distinct non-null value nan1. So, the complementation operator integrates them pairwise (Line 9) to generate intermediate tuples $\kappa(t_1, t_7)$ (equal to f_1 except Capacity = \perp), $\kappa(t_1, t_{10})$ (equal to f_1 except Coach = \perp and Capacity = nan1), and $\kappa(t_7, t_{10})$ (equal to f_1 except Capacity = nan1) (see Section 2.2). All these tuples are added to U_{comp} . Similarly, tuples t_8 and t_{12} complement each other producing f_8 , which is added to U_{comp} (Line 11). On the other hand, t_5 does not have any integrating partners and, hence, is added to U_{comp} itself (Line 14). After the first complementation round, $U_{comp} = U_{ou} \setminus \{t_1, t_6, t_7, t_8, t_9, t_{10}, t_{11}, t_{12}\} \cup$ $\{\kappa(t_1, t_7), \kappa(t_1, t_{10}), \kappa(t_7, t_{10}), \kappa(t_6, t_9), \kappa(t_6, t_{11}), \kappa(t_9, t_{11}), f_8\}$

which is different from U_{ou} . Hence, we move U_{comp} to U_{temp} , and empty U_{comp} . Then the algorithm starts a second round of complementation, i.e., Line 5-18 for i=2. As mentioned earlier, U_{ou} is always the same. So, tuples $\kappa(t_1,t_7)$ and $\kappa(t_1,t_{10})$ in U_{temp} complement with tuples t_{10} and t_7 respectively. They both produce the same tuple that is equal to $\kappa(t_7,t_{10})$ which is already in U_{temp} from the first iteration. As U_{temp} is the set, the newly generated duplicates are discarded. After this round, we again move U_{comp} to U_{temp} and empty U_{comp} . In the next round, no tuples in U_{temp} have complementing partners in U_{ou} . So, the complementation terminates and $U_{comp} = U_{temp} = \{\kappa(t_7,t_{10}), f_2, f_3, f_4, f_5, f_6, f_7, f_8, t_{14}\}$.

Subsumption. Once the complementation is done, we remove the subsumable tuples to get FD. Notice however, we have replaced the missing nulls (\pm) with the distinct labeled nulls before complementation. This is to prevent the complementation on the missing nulls. However, to get the maximally integrated tuples, we ensure that there are no subsumable tuples—both on missing nulls and produced nulls. Therefore, we revert each labeled null to its original missing value (\pm) (Line 6 of Algorithm 1) and then use subsumption (Line 7) to remove the non-maximally integrated tuples.

EXAMPLE 15. We now replace the unique labeled nulls in each tuple with a missing null (\pm) . This step converts $\kappa(t_7, t_{10})$ to f_1 . Finally, we apply subsumption to U_{comp} and get rid of tuple t_{14} (Algorithm 1, Line 7). This ensures that the final result is the set of FD tuples i.e., $\{f_i\}$, $i \in [1, 8]$.

5.2 Full Disjunction Algorithm Analysis

We now analyze Algorithm 1 time complexity and correctness.

Time Complexity. The worst case time complexity of performing subsumption is quadratic in the number of input tuples [8]. However, we apply subsumption using the *Null-value based partitioning Algorithm* [8] that takes $O[S\log S]$ time where, S is the number of input tuples. The idea is to first partition the input tuples according to their null value pattern. This helps to reduce the number of tuple comparisons for the subsumption check and hence, we can apply subsumption only on tuples within a partition. Note that the number of columns in the integrated table is constant for a given set of tables. Next we present our time complexity. ¹

THEOREM 16. The worst-case time complexity of ALITE on input tables $T_1, T_2, ... T_n$ is $O[n \cdot \max(F, S) \cdot S + F \log F]$ where, S is the total number of tuples in all input tables and F is the output size.

Note that FD is exponential in terms of input complexity due to which its time complexity is expressed in terms of inputoutput complexity [75]. Also, we follow the FD definition (Definition 9) of Galindo-Legaria [33, 41] rather than tuple-set version [19, 20]. Therefore, the algorithm presented by Kanza and
Sagiv [41] ($O[n^5S^2F^2]$) is the best algorithm to compare against
our time complexity. The best theoretical guarantee for the tupleset based FD is given by BICOMNLOJ [19] whose worst-case time
complexity to compute tuple-set FD is $O[F(n^2S + S^2 + nSlogS)]$.
However, one needs to apply subsumption to make the output
of tuple-set FD equivalent to the FD. By applying the same subsumption algorithm we use in our technique, the worst-case time

complexity of BICOMNLOJ [19] to compute full FD result becomes $O[F(n^2S + S^2 + nSlogS) + FlogF]$. This shows that our algorithm gives the best theoretical guarantee to compute FD.

Also, when there are no subsumable tuples in the input relations, both BICOMNLOJ and our algorithm give the same result. In that case, our algorithm does not need to perform subsumption and hence, the worst case time complexity is dependent only on the complementation step i.e., $O[n \cdot max(F,S) \cdot S]$ which is also an improvement over Cohen et al. [19]. Note that BICOMNLOJ does some extra work to compute the tuples with polynomial delay. This is also a reason for it being slower than us. We quantify this difference in the time taken by both algorithms to integrate the tables having different input and output sizes in Section 6 experimentally.

Like subsumption, we also optimize complementation step. Similar to what Bleiholder et al. suggested [9], the idea is to block the comparison between the tuples that cannot complement each other by partitioning them into different partitions . This helps to reduce the computation time taken by Line 5-18 in Algorithm 2. The details on this optimization is available in Appendix A.2.

Correctness. Algorithm 1 computes the Full Disjunction [33]. 1

THEOREM 17. The relation computed by ALITE over a set of input tables $T_1, T_2, ..., T_n$ is exactly the natural full disjunction of $T_1, T_2, ..., T_n$.

5.3 FD vs Outer join in Practice

Recall Section 1 that integrating tables is beneficial for answering queries over multiple tables and also for other downstream applications. However, the accuracy of such answers depends on the accuracy of integration process. A straightforward example is aggregation queries. For instance, recalling Fig. 2, if a user is interested in counting the number of teams from *Texas*, a simple aggregation over Fig. 2(a) (outer union) would (incorrectly) return 4 while aggregating Fig. 2(b) (FD) returns 2.

T_6					T ₇					T ₈			
TIC	Playe	r	Tea	Team			Team		adium	TID	Player	Stadium	
t ₁₅	Dez Bry	ant	Dallas C	owboys	t ₁₇ Dallas Cowboy		las Cowboys	AT and	l T Stadium	t ₁₉	Tony Romo	AT and T stadium	
t ₁₆	T. Rom	10	3		t ₁₈		±	A	т&т	t ₂₀	T. Romo	AT & T	
$T_6 \bowtie T_7 \bowtie T_8$ (a) Input Tables													
OID	TID	P	layer	Tea	ım		Stadiun	n	Player		Team	Stadium	
f ₁₁	{t ₁₅ , t ₁₇ }	Dez	Bryant	Dallas C	owbo	oys	AT and T Sta	dium	Dez Bryant	Dall	as Cowboys	AT and T Stadium	
f ₁₂	{t ₁₆ }	T.	Romo	4		1			T. Romo	±		1	
f ₁₃	{t ₁₈ }		1	4	AT & T			1		±	AT & T		
f ₁₄	{t ₁₈ }	Ton	y Romo		AT and T st		AT and T sta	dium	Tony Romo		1	AT and T stadium	
f ₁₅	{t ₂₀ }	_	Romo							Res	olution ove	r outer join result	
(b)	Output T	abl	e gener	ated us	sing	oute	er join oper	ator					
FD(T ₆ , T ₇ , T	8)											
OID	TID	-	Player	Te	am		Stadiun	n	Player		Team	Stadium	
f ₁₁	{t ₁₅ , t ₁₇ }	De	z Bryant	Dallas C	owb	oys	AT and T Sta	dium	Dez Bryant	Dal	llas Cowboys	AT and T Stadium	
f ₁₆	{t ₂₀ }	T.	Romo		1		AT & T		Tony Romo	Dal	llas Cowboys	AT and T stadium	
f ₁₇	{t ₁₇ , t ₁₉ }	Tor	ny Romo	Dallas C	owb	oys	AT and T sta	dium	(e) Ent	ity R	esolution (over FD result	
	(c) Outpu	ut Ta	able ge	nerated	l usi	ng F	D operato	r					

Figure 4: Entity resolution after integrating the tables.

Furthermore, we now discuss the benefit of applying FD (instead of outer join/union) also for another downsteam application, the one of Entity Resolution (ER). ER aims to find and remove duplicate tuples in a table [17, 44, 60]. Using a real example from our experiments , we now show that by applying FD instead of outer join, we

better prepare the ground for applying ER. The same concept can be used to understand the difference of using union operator.

EXAMPLE 18. Consider tables T_6 , T_7 and T_8 shown in Fig. 4 (a) that describe home stadiums of football players who play for different teams. The results of applying outer join and FD over these tables are shown in Fig. 4 (b) and Fig. 4 (c) respectively. The remaining tuples after applying a distance-based ER algorithm [43] on outer join and FD results are shown in Fig. 4(d) and Fig. 4(e) respectively. Outer join produces more output tuples than FD; yet, it does not produce any tuple about Tony Romo's Team. FD, on the other hand, produces output tuple f_{17} that provides this information. Furthermore, since outer join produces incomplete tuples, ER could not resolve f_{13} and f_{14} . Hence, it is better to use FD instead of outer join to integrate the tables. We further provide experimental evidence in Section 6.

6 EXPERIMENTS

We now evaluate the two steps involved in ALITE.

6.1 Experimental Setup

We implement ALITE and all the baselines using Python 3.7 and performed experiments using a CentOS server having Intel(R) Xeon(R) Gold 5218 CPU @ 2.30GHz processor. The main objective of our experiments are to answer: (1) How accurate is our Column Integration ID Assignment method in comparison to the existing attribute matching techniques? (2) How well does our FD algorithm scale in comparison to the state-of-the-art FD algorithms? (3) Is it worthwhile to use FD instead of the faster (and widely available) outer-join operator? Specifically, we study how many FD tuples are missed by outer-join when integrating real data lake tables.

Embedding Generation. Recall that we use pre-trained embeddings to represent the columns for clustering (and integration ID assignment). Before using TURL [25], our method of choice to generate embeddings, we pre-process the tables using their implementation [73]. This phase includes, for example, generating a Wikipedia entity dictionary to map values in the tables. TURL was designed for web tables and, hence, has a limited capacity in terms of the number of rows and columns it can use to create embeddings (mean of ~20 rows and ~2 columns [25]). Since typical data lake tables are much larger (see Fig. 5), to cope with such a limitation, we designed an iterative embedding generation approach for each column. First, we randomly sample 50 rows and generate the corresponding column embedding by averaging the representations of each row. Then, we iteratively sample 50 additional rows and combine them with the current embedding until convergence. Convergence is achieved if the euclidean distance between two consecutive embeddings is less than some value (0.05 in our setup).

Hierarchical Clustering. The generated embeddings are used to represent columns for clustering (see Section 4). We implement the clustering algorithm using Agglomerative Clustering module available in scikit learn library [61]. Based on our objective of obtaining dense, but well-separated clusters, we use the Silhouette Coefficient as a clustering quality measure [68]. We select the number of clusters (column predicates) that maximizes the Silhouette Coefficient (Section 4). We use euclidean distance as a distance metric throughout the experiments.

¹ Proof in Appendix A.2

6.2 Evaluation Measures

To the best of our knowledge, no prior work considers the integration of data lake tables after discovery. So, we compare the different components of our pipeline to some approximate baselines.

Column Integration ID Assignment: The column integration ID assignment can be addressed using schema matching. Generally, precision, recall and their harmonic mean, i.e., F_1 -score are used as the evaluation measures for schema matching [14, 32, 70]. So, we use the same three metrics to compare our column integration ID assignment against existing schema matching methods. To assess the quality of a clustering-based solution using binary measures, we consider a pair of columns belonging to the same cluster as a match. Note that a column having no matches forms a singleton cluster, i.e., a cluster having one column. We count each such cluster as a true match during the evaluation. Specifically, the total number of matches is the sum of the number of column pairs belonging to the same cluster and the number of singleton clusters. Formally, let $\mathcal{T}_{\mathcal{M}}$ be true column pair matches according to the ground truth and $\hat{\mathcal{T}}_M$ be the matches according to a method. We define Precision (P), Recall (R) and F_1 -score (F_1) as follows:

$$P = \frac{\mathcal{T}_M \cap \hat{\mathcal{T}}_M}{\hat{\mathcal{T}}_M}, R = \frac{\mathcal{T}_M \cap \hat{\mathcal{T}}_M}{\mathcal{T}_M}, F_1 = \frac{2 \cdot P \cdot R}{P + R}$$
(1)

We compute precision, recall and F_1 -score for each set of tables to be integrated and report the average. In addition, we also report the time taken by each method to determine the column predicates.

Full Disjunction: Our objective is to show that our proposed FD algorithm is faster in integrating data lake tables in comparison to the state-of-the-art methods for computing the FD. Therefore. we will report the time taken to compute Full Disjunction by each method. A cut-off of 10k seconds is used when applying FD. Furthermore, it is interesting to see how many tuples generated by FD can also be generated by the relatively faster outer-join over real data lake tables. Recall that outer-join is not an associative operator and there may exist outer-join orderings that yield the semantics of Full Disjunction when the scheme graph of the input tables does not contain a γ-cycle [66]. But the data lake tables to be integrated may contain gamma cycles in which case an outer join may not compute the FD. We quantify this using the Tuple Difference Ratio (TDR) as a success metric. Let F be the FD output size and F' be output size of a competing method (e.g. outer join). The TDR is given by $\frac{F \cap F'}{F}$. If the competing method produces all FD tuples, TDR is equal to 1 and it is equal to 0 if it produces none of them.

6.3 Baselines

Column Integration ID Assignment. Recall that we use a clustering approach and pre-trained embeddings created for the tables's columns [25] to find the column integration IDs. Other existing natural language embeddings were successfully adopted for similar tasks such as table search [10, 56] and column annotation [72]. Here, we compare the performance of such embeddings also for our task. Like in table search [10, 56], we use fastText [39, 53] embeddings of columns and as done for column annotation [72], we use BERT [26] embeddings. We use a publicly available Fasttext model [31] using Gensim python package [34]. We generate BERT embeddings [4] using the commonly used hugging face package [29].

We also compare our Column Integration ID Assignment with existing schema matching methods. There are numerous matching approaches in the literature [27, 45, 50, 70]. However, most work relies on metadata, which we aim to avoid in our setting. Recently, in Valentine Koutras et al. performed a detailed analysis of existing schema matching methods in a data lake setting [45]. Based on their analysis, we select the Distribution Based method (DB), proposed by Zhang et al., as a baseline [77]. DB discovers clusters of similar attributes in tables using information that includes attribute data types, overlap of the attribute values, and their distribution. Earth Mover's Distance is used to measure the similarity between the column pairs [69]. A threshold is applied over this score to decide the column similarity. We use a threshold of 0.15 suggested by Zhang et al. [77]. Also, we reproduce *DB* using the open source code in Valentine [74]. For completeness, we compare ALITE against other schema-based matching methods available in Valentine over a benchmark having real schemas. Specifically, we compare CU-PID [50], COMA [27] and Similarity Flooding (SF) [52]. We also report a Jaccard Similarity and Levenshtein Distance method (ILM) used as a baseline in Valentine [45]. We use default parameters from the respective papers. Note that the holistic schema matching works with a set of tables whereas the pairwise schema matching methods work only between a pair of tables (or schemas). So, for fair evaluation, we make all the pairwise methods holistic. We apply pairwise schema matching between every pair of tables in the set of tables to be integrated. Then, the method returns all the column pair matches, which we use to compute Precision, recall and F_1 -score (Section 6.2).

Full Disjunction. Paganelli et al. recently suggested **ParaFD** to compute the FD of relational tables where all joins are between keys and foreign keys using multiple machines [59]. In data lake, we are often not joining on keys and foreign keys, so we mainly compare ALITE against ParaFD in a benchmark having such relationships. However, to understand how accurate ParaFD can be in the real tables that may not necessarily have PK-FK relations, we report its TDR on a benchmark having real data lake tables.

We also use **BICOMNLOJ**, which computes the FD with a polynomial delay between tuples [19]. As our focus is to compute full FD, we report the performance of BICOMNLOJ for computing the full FD. Also, BICOMNLOJ is based on the tuple sets and hence, if the input contains nulls its output may contain some subsumable tuples (see Example 10). So, to ensure that the output produced by this algorithm is the same as other algorithms, we apply subsumption to its final result. For fair comparison, we apply the same subsumption algorithm that we use for our approach [8]. Since an open-source implementation is not available for either ParaFD or BICOMNLOJ, we reproduce them using the information provided in the paper. We implement ParaFD to run on a single machine for fair comparison. The reproduced implementations are publicly available in our github repository [2]. Also, we run outer join to integrate the tables and use its output size to report TDR. As outer join is not associative, the order of integration makes a significant difference [33]. Applying outer join in a connected-prefix ordering of the input tables can yield FD for γ -acylic case [19]. So, we find the connected-prefix ordering by performing DFS transversal over the input scheme graph and use it to compute the outer join [19].

6.4 Benchmarks

Benchmark	Tables	Columns	Tuples	Integration sets	Experiments
Align	606	4,584	2.2M	65	Integration ID
Real	102	1, 195	219k	11	Integration ID, FD
Join	302	2, 309	1.1M	28	FD
IMDB	6	33	3k - 30k	1	FD

Figure 5: Benchmarks used in the experiments.

Figure 5 summarizes all benchmarks used in different experiments along with their statistics. Each benchmark contains multiple tables with different schemas and each schema may be used by multiple tables. All the benchmarks are made publicly available [2].

Align. To the best of our knowledge, there are no available data lake benchmarks that could be adapted to evaluate the column integration ID assignment task. So we create a new benchmark called Align containing 606 tables divided into 65 non-overlapping sets of tables, which we call integration sets. For example, T1-T5 (Fig. 1) is an integration set containing 5 tables to be integrated. We run the column integration ID Assignment over the columns of tables of each integration set and report the average performance. To create this benchmark, we follow a similar technique used to create a table union benchmark [56]. First, we select 65 real data lake tables from US Open Data [37], Canada Open Data [22], and UK Open Data [23] and consider them as seed tables. Each seed has a different schema and is used to generate an integration set. We partitioned the seed tables by projecting columns and selecting rows (without replacement) to get 606 smaller tables such that all the columns of the small tables that originated from the same seed column have the same integration ID. Accordingly, we have labeled ground truth for the column integration ID assignment. Based on the number of columns and rows in the seed tables, each integration set contains 2 to 30 tables. Note that we do not add or remove missing nulls in the seed tables before partitioning. Therefore, if there is a missing null in the seed table row, it gets copied to the small tables. On average, since these are real data lake tables, we have null values in 50% of the rows. This ensures that our benchmark well-represents the real data lake scenario where such nulls are prevalent.

Real. To understand the performance of different methods in a real data lake environment, we also created the Real Benchmark that contains 102 real data lake tables divided into 11 disjoint integration sets. We ensure that the scheme graph of the tables in each integration set is connected. Furthermore, two real tables can have different column headers for the join columns. Therefore, we manually marked the join columns and labeled the groundtruth. We use this benchmark to evaluate the effectiveness of column integration ID assignment and efficiency of FD. It is interesting to evaluate FD computation for different input sizes (S) and output sizes (F). Therefore, we also ensure that the benchmark covers F < S, $F \approx S$ and F > S cases. Precisely, in this benchmark, there are three integration sets where F < S, five integration sets where $F \approx S$, and three integration sets where F > S.² The number of tables (n) on each integration set ranges from 5 to 14. Also, S and F ranges from 588 to 76k and 580 to 60k respectively.

Join. Except renaming column headers, we do not modify the Real Benchmark and it contains raw tables searched from the data

lakes. Therefore, to experiment our algorithm in broader contexts, like for variation in the input size, output size and the number of tables in each integration set, we create Join Benchmark that contains 28 integration sets generated using 27 seed tables—at most two integration sets from each seed. Each integration set contains 2 to 20 tables. We follow a similar methodology as used in Nargesian et al. [56] as explained in the Align Benchmark, but this time we also consider broader variation in the number of input and output tuples and also their ratio. The input tuple size (S) varies from 266 to 100k and range of output size is from 234 to 12M. There are 17 integration sets with F < S among which six have F < 0.5S. Also, five integration sets have F > S.

IMDB. As ParaFD can only be used accurately for the tables having PK-FK relationships, we also use an IMDB dataset, having such relationships for our experiments [38]. This is a dataset about movies and their details including ratings, crews, etc. The full dataset contains about 106.8 M tuples in 6 tables. We use this benchmark to study the effect of different input size on the run time. Previous work uses 1k tuples in each table to evaluate the run time [19]. Therefore, to study the trend on similar setting, we sample tuples randomly and vary the input size between 500 to 5000 for each table— around 3k to 30k input tuples in total for our experiments. We preserve PK-FK relationships during sampling.

6.5 Column Integration ID Assignment Results

We now report the effectiveness of column integration ID assignment, followed by an empirical analysis of its efficiency. Fig. 6 shows the evaluation results for the *Align* and *Real* benchmarks.

Benchmark			Method											
			В	aseline)			ALITE						
		CUPID	СОМА	SF	JLM	DB	fastText	BERT	TURL					
	P	-	-	-	-	0.953	0.956	0.922	0.934					
Align	R	-	-	-	-	0.892	0.923	0.965	0.968					
	F ₁	-	-	-	-	0.911	0.940	0.939	0.947					
	Р	0.821	0.448	0.494	0.255	0.807	0.689	0.706	0.776					
Real	R	0.631	0.695	0.912	0.914	0.708	0.806	0.756	0.762	Best score				
	F ₁	0.685	0.465	0.562	0.296	0.710	0.722	0.743	0.755	Second Best sc				

Figure 6: Precision, recall and F_1 over the *Align* and *Real* benchmarks for column integration ID assignment.

Recall that ALITE uses a clustering-based approach to find the column integration IDs that uses pre-trained embeddings created using TURL [25]. So, first we compare ALITE's precision, recall and F_1 -Score using TURL-based embeddings against fastText and BERT. We use the same experimental setups for all three methods (Section 6.1). It is seen that TURL gives comparable or even better precision and recall against the baselines. In terms of F_1 -score, TURL performs better than the baselines. This validates our choice of using table-based embedding (TURL) instead of natural language embeddings (fastText and BERT) for data lake tables. We will explore other ways to represent data lake tables in future research.

Next, we compare the effectiveness of ALITE's embedding-based technique against DB that uses attribute data types, values and distribution to find the similar columns. The DB approach has a slightly better precision than our method on the Align benchmark. However, ALITE outperforms DB by more than 8% and 3% in terms of Recall and F_1 -score respectively. Also, in Real benchmark, DB is precise than our method by around 3%, but ALITE is better in

²We consider $F \approx S$ when $\frac{|F-S|}{S} \leq 0.05$.

recall and F_1 -score. A possible reason for the preciseness of DB is the use of a threshold in pairwise comparisons. Specifically, the default threshold is set to 0.15 and so the precision is fairly high. However, note that accordingly the recall also drops. An additional reason for the lower recall is that DB relies on value overlap and semantics (e.g., synonyms) are ignored.

Moreover, we analyze the performance of schema-based methods for column ID assignment in Real Benchmark. Recall that Align Benchmark's tables are generated using seed tables such that the aligning columns have the same column headers (Section 6.4). So, we do not evaluate schema-based methods (CUPID, COMA, SF and JLM) in Align Benchmark. In Real Benchmark, we observe that CU-PID has better P and F_1 than other schema-based methods but it has lower R and F_1 than DB (baseline) and ALITE. Specifically, ALITE outperforms CUPID, the best schema-based method, by ~10 % in F_1 -score. This is because the tables contain unreliable schemas and applying similarity measures over them leads to incorrect aligning. COMA also shows weaker performance due to the same reason. We observe that JLM and SF have the top-2 recalls among all the methods. However, they have low precision and F_1 -score. This is because they align most columns within the same cluster which increases their recall but penalizes precision. Hence, the schemabased methods are not effective in the data lake setting.

The column integration ID assignment is considered as an offline task. Yet, we note that applying ALITE's clustering is much faster than the pair-wise comparison done by the *DB* baseline. Specifically, ALITE takes about 10 minutes for *Align* and about 15 minutes for *Real* while *DB* takes about 45 minutes (×4.5) for *Align* and about 2 hours (×8) for *Real*. Comparing the embedding generation, fastText is the fastest (total of 28 seconds for *Align* and 3 seconds for *Real*) as the embeddings are pre-defined. TURL and BERT, for which a pre-trained model is used, show somewhat different trends. For the *Align* benchmark BERT takes a total of 80 minutes while TURL takes about 7 minutes. For the *Real* benchmark they take approximately the same time (about 15 minutes).

6.6 Full Disjunction Results

Now we compare ALITE's FD algorithm efficiency (Algorithm 1) against the baselines (see Section 6.3). We also analyze the run time of our algorithm by varying the input and output sizes. Finally, we compare the FD output with the outer join output in terms of *TDR* (the relative size of the outputs, see Section 6.1).

ALITE against baselines. Before experimenting with our data lake benchmarks, we conducted a preliminary analysis over three synthetic integration sets $(\mathcal{R}_1, \mathcal{R}_2, \mathcal{R}_3)$ introduced in Cohen et al. [19]. We reproduced these by randomly generating 1000 input tuples in each of the 10 tables in each integration set. Unsurprisingly, since these schema contain biconnected components [19], BICOMNLOJ splits the tables into smaller integration sets, computes FD for each of them separately and combine them. Therefore, BICOMNLOJ is much faster than ALITE. As a second step, we created a new, more complex, integration set having eight tables that better represents data lake tables (see repository [2]). We again fix the number of tuples on each input table to 1k for each of the 8 tables, i.e., S = 8000. We added tuples to the tables in such a way as to create three cases: F < S (F = 3868), $F \approx S$ (F = 7445) and F > S (F = 7445) and F > S

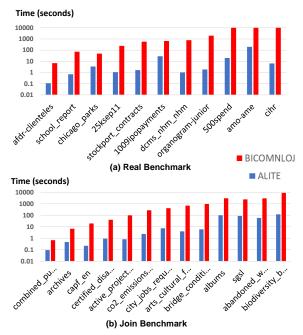


Figure 7: Time taken to integrate tables in (a) Real Benchmark and (b) Join Benchmark. The integration sets in X-axis are arranged in ascending order of input size. Y-axis (log scale) shows the integration time. A 10k second cut-off was used in both benchmarks. Some integration set names are truncated for concise representation. Due to space considerations, we only show the integration sets on which the baseline integrates the tables before the cut-off time in Join Benchmark. Other integration sets' details are provided with the supplementary materials [2].

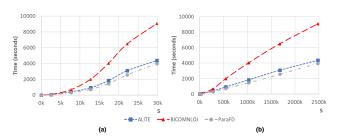


Figure 8: Integration time in the IMDB benchmark for (a) different input size and (b) different output size.

= 14204). For all three cases, ALITE outperforms *BICOMNLOJ* by at least one order of magnitude. *BICOMNLOJ* could not optimize the computation because there is only one biconnected component. Note that this is a common case in data lakes due to the presence of complex cycles in the scheme graphs.

We also compare the time taken by ALITE's FD algorithm against the baseline *BICOMNLOJ* in *Real* Benchmark. Fig. 7(a) summarizes this experiment. Each pair of bars on the X-axis represents a schema and the Y-axis shows the time taken to integrate the tables by ALITE (blue) and *BICOMNLOJ* (red). The tables in an integration set are ordered by input size such that the smallest is shown on the left and

the largest in the right. ALITE's FD algorithm (blue bars) is significantly faster than BICOMNLOJ (red bars) over all 11 integration sets. Specifically, the cases where the cut-off was not applied (all but the last three), ALITE boosts the performance of BICOMNLOJ by around two orders of magnitude. The reason for this gain comes from the fact that our algorithm partitions tuples according to their complementation patterns and iterates over the tuples only within the partitions. This leads to an interesting insight, showing the impact of the complementation operator in optimizing the FD computation for data lake tables. Another reason is that data lake tables have complex join connections that limit the chances of dividing the tables of integration sets into biconnected components, which is used in BICOMNLOJ. We see the same trend on Join Benchmark (shown in Fig. 7 (b)) where, ALITE outperforms BICOMNLOJ on all integration sets by around one and half orders of magnitude. As in Real, we are much faster for the integration sets having different output to input ratio. Also, it is notable that out of 28 integration sets, BICOMNLOI computes the full FD result within the cutoff time for only 13 integration sets that are shown in Fig. 7(b). Generally, BICOMNLOJ is able to compute FD within the cutoff time for input sizes less than 45k. For the remaining 15 integration sets, the average integration time by ALITE ranges from 20 seconds to 3827 seconds with an average of 598 seconds-well below the cut-off time (10k seconds) that we used in the experiments. This shows that ALITE is more applicable than the baseline for the data lake tables with large input size, we also observed that tuple-set FD produces over 300 subsumable tuples per integration set in the Real Benchmark which supports the subsumption step in ALITE.

Furthermore, we apply ParaFD over the Real Benchmark to see if it can yield FD results in data lake tables. Out of 11 integration sets, ParaFD completes the integration for only 3 integration sets within the cut-off time and only 2 of them are equal to FD result. ParaFD is slow in this benchmark because it computes all the spanning trees over the schema graph and computes outer join over each of them (see Section 3). Accordingly, we also implement an approximate version of ParaFD where we do not apply the cut-off time but compute output tuples using at most 100 spanning trees. The approximate version yields FD result for only 5 out of 11 integration sets. For other 6 sets, the average TDR is 0.82, i.e., ParaFD misses around 18 % of tuples. Also, it takes an average of 9268 seconds per integration set, which is slower by magnitudes than ALITE (see Fig. 7(a)). The integration time and TDR on each integration set is available in the github repository [2]. This experiment shows the importance of ALITE's FD algorithm and hints that the modification of ParaFD to work on the general case is not straight-forward.

Moreover, we compare ALITE's FD algorithm against both *BICOMNLOJ* and *ParaFD* in *IMDB*— a benchmark having six tables and large number of join connections. As shown in Fig. 8 (a), we vary input tuples (*S*) from 0 to 30k and observe the runtime. Note that, when we increase the number of input tuples, the output size also increases in this benchmark. Therefore, we also show the integration time with respect to the output size (Fig. 8 (b)). It is seen that ALITE gives comparable performance against *ParaFD* and is more than two times faster than *BICOMNLOJ*. Recall that *ParaFD* needs all joins to be key to foreign-key joins to compute FD. It uses this property to optimize the computations and hence, performs relatively better than other techniques on *IMDB*. However, *ParaFD*

cannot be used for the tables without PK-FK relationship. Due to space constraints, we provide other details like number of tables on each integration set, number of columns, input size, output size, missing nulls size with the supplementary materials [2].

Comparison against outer join. Lastly, we show the importance of using FD against outer join empirically in real data lake tables (Real Benchmark). We provide a bargraph in our technical report Appendix A.3 that shows each integration set of this benchmark on the X-axis and TDR in Y-axis. We show the schemas based on three categories: S < F, $S \approx F$ and S > F. Recall that all these schemas contain complex cycles. Out of 11 integration sets, only once is TDR equal to one (school report), i.e., all FD tuples are generated by outer join. It is interesting that even in the presence of complex cycles, outer join can sometimes produce the full FD. For two integration sets (chicago_parks and 1009ipopayments), outer join is able to generate more than half of the FD tuples. But for other sets, TDR is very low, which shows the importance of FD to best integrate real tables. Also, the low TDR indicates that the outer join produces incomplete tuples and hence, as discussed in Section 5.3, FD is more beneficial than outer join before applying entity resolution.

Integration Method	Integrated Table Size	T	$ T \cap T^* $	P	R	F ₁
Full Disjunction	121	98	78	0.795	0.838	0.816
Outer join	114	109	37	0.339	0.397	0.366

Figure 9: Results of applying Entity Resolution (ER) over FD and outer join results. Here, Integrated Table Size refers to the number of input tuples to ER algorithm which is equal to the output size of integration methods.

Entity Resolution (ER) as Downstreaming Task. Finally, we explicitly analyze the effect of applying FD (rather than outer join) for the downstream application of entity resolution (ER). We generate a scenario similar to Section 5.3 by taking a real table containing information about players, teams, facilities, etc. and injecting the duplicate tuples on them. We then partition the table into four tables and integrate them back using outer join and FD. Over these tables, we apply entity resolution and verify if the tuples in the original table are reproduced. Specifically, we use Magellan's py_entitymatching [63] to find matching tuples and remove them. Additional experimental details are provided in a technical report Appendix A.3. We report P, R and F_1 of applying ER over FD and outer join results in Fig. 9. It is seen that ER over FD table outperforms that over outer join table in terms of both precision and recall and by around 123 % in terms of F_1 -score. Since outer join is not able to integrate the maximal information, its result contains incomplete tuples having null values. So it reduces the information available for the entity resolution algorithm and impacts de-duplication accuracy.

7 CONCLUSION

We introduce a novel problem of integrating data lake tables after discovery. We also introduce ALITE, a technique to solve this problem in two steps. ALITE first assigns an integration ID to each column and then applies natural full disjunction to integrate the tables. We present and share three open data integration benchmarks

that may be of interest to the research community. We show that ALITE's new FD algorithm is more efficient than existing baselines and ALITE does not require tables to have common schemas.

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A APPENDIX

A.1 Assigning Column Integration IDs

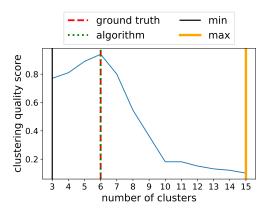


Figure 10: An example scenario of determining the number of clusters for the input tables in Fig. 1. Here, X-axis shows the number of clusters and Y-axis shows the clustering quality score. The green and red lines show the number of clusters according to the algorithm and ground truth respectively.

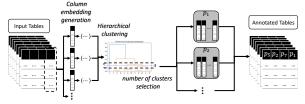


Figure 11: Assigning Column Integration IDs sketch

Fig. 11 zooms in the left part of Fig. 3, described in Section 4. We get a set of tables as input, generate column embeddings, which are used in hierarchical clustering of columns to generate integration ids that are used to annotate the input tables.

A.2 Integrating Tables

Proof of Theorem 16 (Time Complexity).

PROOF. In Algorithm 1, the asymptotic time complexity of replacing missing nulls with unique placeholders (Line 3) and outer unioning the input tuples (Line 4) is linear to the input size i.e. O[S]. The runtime of Algorithm 1 mainly depends on complementation (Line 5) and subsumption (Line 7). To show the time complexity of Algorithm 1, first we need to determine the maximum number of tuples that can be produced by Algorithm 2, Line 5-18. Note that, the number of tuples in U_{ou} is always constant i.e., S and the number of tuples changes only for U_{temp} which we update with the integrated tuples in each iteration. In some round of iteration, the total tuples in U_{temp} reaches the number of output tuples along with some subsumable tuples b i.e., (F + b). We can consider b as some factor of F. Therefore, the number of tuples in U_{temp} is bounded by O[F] if F > S else, it is bounded by

O[S]. On what follows, the upper bound of the number of tuples in U_{temp} is O[max(F,S)] and hence, the asymptotic time complexity of Algorithm 2 is $O[n \cdot max(F,S) \cdot S]$. After that we feed the complementation results i.e., O[F] tuples to Line 7 in Algorithm 1, which performs subsumption in O[FlogF] time. Hence, the worst-case time complexity is $O[n \cdot max(F,S) \cdot S + FlogF]$.

Proof of Theorem 17 (FD Correctness).

PROOF. Let, \mathcal{F} be the set of tuples in the natural full disjunction of $T_1, T_2, ..., T_n$. Let, t be any tuple such that $t \in \mathcal{F}$. Now, $t \in \mathcal{F}$ iff t is a maximally integrated tuple i.e., t can be in the FD result iff:

- either, t is a maximally integrated tuple because on integrating T₁, T₂,... T_k where, k ≤ n, t is produced and not subsumed by any other tuple.
- or, t is a maximally integrated tuple because $t \in \{T_1, T_2, ... T_n\}$ and $t' \notin \mathcal{F}$ such that $t' \supset t$.

Now we show that ALITE does not miss any maximally integrated tuple that fulfills the first condition. For this, we show that the complementation operator produces the maximally integrated tuple that fulfills the first condition. Two tuples $t_i \in T_i$ and $t_i \in T_i$ can be integrated (or joined) iff for each join column $A \in \mathcal{A}(T_i) \cap \mathcal{A}(T_i), t_i[A] = t_i[A] \text{ and } t_i[A] \neq \pm \text{ and } t_i[A] \neq \pm.$ Also, for joinable tuples $t_i \in T_i$, $t_j \in T_j$ having same value in join columns and having column $A_i \in T_i$ and $A_j \in T_j$, $t_i[A_i]$ and $t_i[A_i]$ are always non-null. Even if there are missing nulls, we replace them with distinct labeled nulls. Due to the way outer union operator works, $t_i[A_i] = t_i[A_i] = \bot$ i.e., they fulfill the complementation condition. This ensures that the complementation operator combines the joining tuples. Now, for each tuple in outer unioned partition, ALITE applies up to n iterations of complementation operator. As the setup ensures that complementation operator joins a pair of tuples from two tables in each iteration, it generates all possible maximally integrated tuples after at most n rounds even if the input tuples has join partner in all n input tables. Hence, we do not miss any maximally integrated tuples after this step. i.e., $t \in \mathcal{F}$.

For the second type of maximally integrated tuples, let t be a tuple from any table $T \in \mathcal{T}$ having no join partners. Such a tuple will not complement with any other tuples and remains on the complementation output in its original form padded with produced nulls at non-join columns (Line 13- 14 of Algorithm 2). Hence, $t \in \mathcal{F}$.

As we apply subsumption after complementation, any non-maximally integrated tuples get subsumed. Hence, ALITE neither misses a maximally integrated tuple, nor produces a subsumable tuples i.e., the relation computed by ALITE over the input tables is exactly equal to the natural full disjunction. This completes the proof.

Efficient Complementation. Note that Algorithm 2 receives S tuples from Algorithm 1 for complementation, and the time taken by Line 5- 18 in Algorithm 2 is $O[n \cdot max(F, S) \cdot S]$. However, we know that for two tuples to complement each other, they must have the same non-null values on the common column. We illustrate this with an example.

Example 19. Consider column Stadium and tuples t_1 , t_2 , t_7 and t_{10} of table (a) in Fig. 2. Also recall the necessary conditions for two tuples to complement each other described in Section 2. Since $t_1[Stadium] = NRG$ Stadium and $t_2[Stadium] = AT&T$ Stadium, they cannot complement each other as they have different nonnull values on the common column Stadium. Hence, we can safely escape the comparison between t_1 and t_2 while applying complementation. Also, as $t_{10}[Stadium] = AT&T$ Stadium, it has a possibility of complementing t_2 . So, we need to compare t_2 and t_{10} . Notice however, tuple t_7 complements t_{10} even though it has a missing null on Stadium-different from $t_{10}[Stadium] = AT&T$ Stadium. Therefore, a tuple having a missing null on the common column should still be compared with all other tuples.

In general, we can partition the tuples having different non-null values on common columns and apply complementation within each partition using Algorithm 2. This helps to reduce the computation time taken by Line 5-18 in Algorithm 2. Our objective is to make each partition fairly small, i.e., keep the number of tuples in each partition less than a positive integer θ where, $\theta < S$. Bleiholder et al. suggested to partition tuples using the values of selected partitioning column(s) [9]. The selection of the partitioning column(s) is based on a heuristic that considers the number of non-null and unique values on each column. At first, the tuples having the same non-null values in the partitioning column are kept in separate partitions. If there are tuples having null values in the partitioning column(s), they are added to all the partition. Now, the complementation can be applied on the tuples within each partition. However, partitioning with a single or even a group of columns may still produce large partitions. Therefore, instead of stopping after the first partitioning, we continue the process using other columns one after another until the number of tuples in each partition is less than θ . Recall that the tuples in the null partitions should be added to each of other partitions. Hence, in order to reduce the number of tuples in the null partitions, we first sort the columns in ascending order of the number of nulls they contain. Then, we partition the tuples by value of each column one by one.

A.3 Experiments

ER experiment setup: We generate this scenario in a similar fashion to Section 5.3. We start with a real table containing information about players, teams, facilities, etc. and consider it as ground truth i.e., a clean table. Next, we randomly select 10 % of its tuples and add their duplicates/noise (at most two for each) in the clean table, which we call dirty table. For example, for tuple having (player name, team, facility) = (Mark Andrews, Ravens, M & T Bank Stadium), we add a duplicate (Andrews, Ravens, MT Stadium). Then we partition the dirty table into four tables having different schema and randomly add the rows on each of them such that they retrieve information in the dirty table.

To evaluate, we integrate four generated tables using outer join and FD. Over these tables, we apply entity resolution and verify if the tuples in the clean table are reproduced. Specifically, we use Magellan's *py_entitymatching* package to find matching tuples in the integrated tables [63]. Based on the matching results, we remove the duplicates from the tables. Given a table *T* (resulting table after

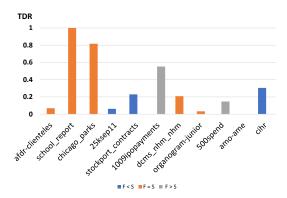


Figure 12: Tuple Difference Ratio (TDR) of the integration sets in the *Real* Benchmark. We show each integration set of this benchmark on the X-axis and TDR in Y-axis (see Section 6.2). We show the schemas based on three categories: S < F, $S \approx F$ and S > F.

applying ER and removing duplicates from outer joined or FD table) and a ground truth table T^* (i.e. clean table), we compute precision (P), recall (R) and F1-score (F_1) as follows:

$$P = \frac{|T \cap T^*|}{|T|}, R = \frac{|T \cap T^*|}{|T^*|}, F_1 = \frac{2 * P * R}{P + R}$$

In other words, precision and recall measure the portion of clean tuples in T and the portion of clean tuples that are covered by T respectively.