Simulation study for LM(normal) vs GLM(Poisson)

For *Poisson* regression, the estimates are centred around the true value, and they are within one SE of true value, so we have good efficiency and unbiasedness. But using *Normal* model shows bias and the estimated values fell far from the real value. So we cant trust confidence interval results for the wrong model.

#means of coefficient estimates

$B0_{pois} = 0.2021$

 $B1_{pois} = 0.4971$

 $B0_norm = 1.1929$

 $B1_norm = 0.7868$

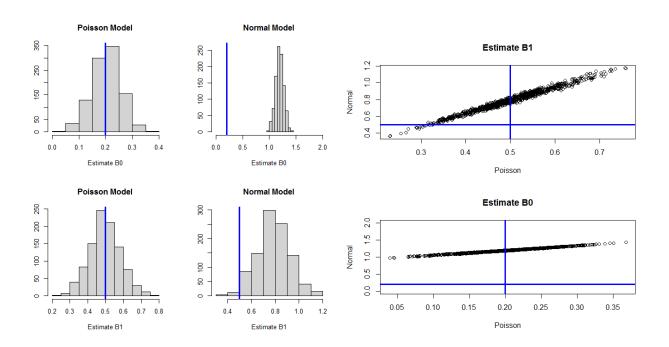
#SE of coefficient estimates

 $B0_{pois} = 0.0017$

 $B1_{pois} = 0.0027$

 $B0_norm = 0.0024$

 $B1_norm = 0.0043$



R Code:

```
### Simulation study for LM(normal) vs GLM(link=Poisson) ###
set.seed(3759) ## for reproducibility
reps <- 1000 ## number of simulated data sets
par.est.pois <- matrix(NA, nrow=reps, ncol = 4)
par.est.norm <- matrix(NA, nrow=reps, ncol = 4)
b0 <- .2
b1 <- .5
n<- 1000
X<- runif(n, 0, 1)
for(i in 1:reps)
{
 Y \leftarrow rpois(n, exp(b0 + b1*X))
 ## poisson regression fit and estimates
 glm1 <- glm(Y ~ X, family = 'poisson')
 vcv <- vcov(glm1)
 par.est.pois[i,1] <- glm1$coef[1]
 par.est.pois[i,2] <- glm1$coef[2]
 par.est.pois[i,3] <- sqrt(diag(vcv)[1])
```

```
par.est.pois[i,4] <- sqrt(diag(vcv)[2])</pre>
## normal regression fit and estimates
 Im1 \leftarrow Im(Y \sim X)
vcv <- vcov(lm1)
 par.est.norm[i,1] <- lm1$coef[1]</pre>
 par.est.norm[i,2] <- lm1$coef[2]
par.est.norm[i,3] <- sqrt(diag(vcv)[1])</pre>
par.est.norm[i,4] <- sqrt(diag(vcv)[2])</pre>
}
#means of coefficient estimates
print(mean(par.est.pois[ , 1]))
print(mean(par.est.pois[ , 2]))
print(mean(par.est.norm[, 1]))
print(mean(par.est.norm[, 2]))
#SE of coefficient estimates
print(sqrt( var(par.est.pois[ , 1]) / reps) )
print(sqrt( var(par.est.pois[ , 2]) / reps) )
print(sqrt( var(par.est.norm[ , 1]) / reps) )
print(sqrt( var(par.est.norm[ , 2]) / reps) )
##plots
par(mfrow=c(2,2))
hist(par.est.pois[, 1], xlab="Estimate BO", ylab="", main="Poisson Model")
```

```
abline(v=b0, col='blue', lwd=3)
hist(par.est.norm[, 1], xlim = c(0,2), xlab="Estimate B0", ylab="", main="Normal Model")
abline(v=b0, col='blue', lwd=3)
hist(par.est.pois[ , 2], xlab="Estimate B1", ylab="", main="Poisson Model")
abline(v=b1, col='blue', lwd=3)
hist(par.est.norm[, 2], xlab="Estimate B1", ylab="", main="Normal Model")
abline(v=b1, col='blue', lwd=3)
par(mfrow=c(2,1))
plot(par.est.pois[, 2], par.est.norm[, 2],xlab="Poisson",ylab="Normal",main="Estimate B1")
abline(h=b1, col='blue', lwd=3)
abline(v=b1, col='blue', lwd=3)
plot(par.est.pois[, 1], par.est.norm[, 1], ylim = c(0,2), xlab="Poisson",ylab="Normal",main="Estimate
B0")
abline(h=b0, col='blue', lwd=3)
abline(v=b0, col='blue', lwd=3)
```