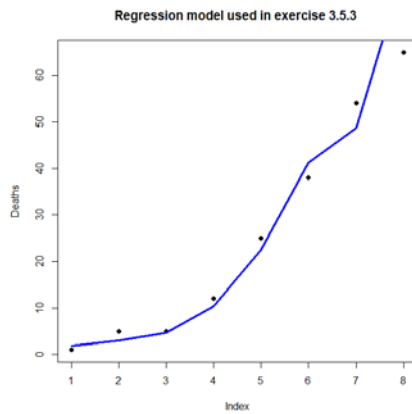


The book's model is $\log(\text{deaths}) \sim \log(\text{population}) + i$ □

where $i = 1$ for the age group 30–34 years, ..., $i = 8$ for 65–69 years.

Plot below shows the implementation for this model.

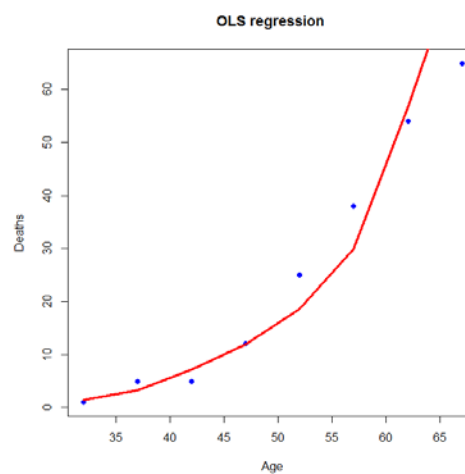
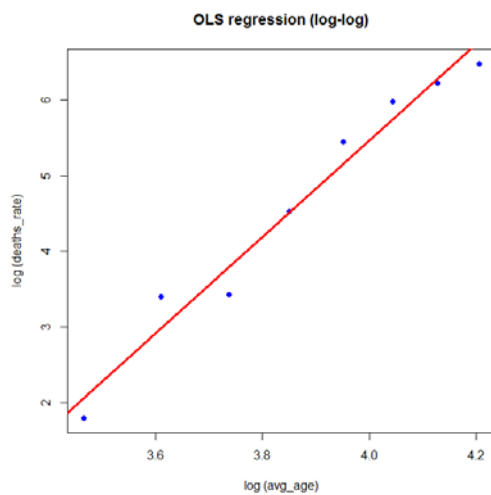


Now we use an OLS model: $\log(\text{deaths_rate}) \sim \log(\text{avg_age})$ where

$\text{deaths_rate} = (\text{deaths}/\text{population}) * 100000$ and

$\text{avg_age} = \text{avg}(30, 34)$ for the age group 30–34 years, ..., $= \text{avg}(65, 69)$ for 65–69 years.

This model has $R^2 = 0.96$ which is a good approximate although it is based on the Normal distribution not the Poisson distribution.



Finally, we use a GLM model for the deaths_rate:

```
glm(deaths ~ avg_age, offset=log(population +1), family="poisson")
```

The comparison of GLM and OLS for death rate shows that our OLS model provides a good prediction.

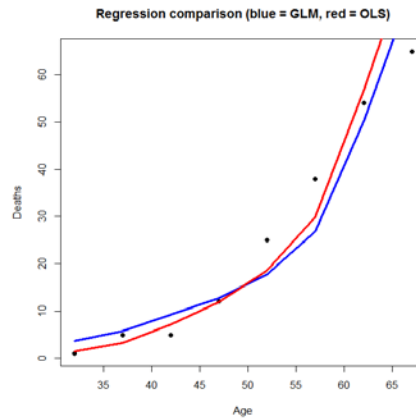


Table below shows the comparisons of the three models with actual data

age group	actual deaths	book model	OLS	GLM
30-34	1	2	1	4
35-39	5	3	3	6
40-44	5	5	7	9
45-49	12	10	12	13
50-54	25	22	19	18
55-59	38	41	30	27
60-64	54	49	57	50
65-69	65	83	87	79

Appendix: R Code

```
#preparation of Data
```

```
#install.packages('dobson')
```

```
mortality <- dobson::mortality
```

```
mortality$age_index <- c(1:8)
```

```
age<-seq(from=30 , to=70, by=5)
```

```
for(i in 1:length(age)-1)
```

```
{avg_age[i]<- floor((age[i] + age[i+1]) /2)}
```

```
mortality$avg_age<- avg_age
```

```
mortality$deaths_rate<- round(mortality$deaths/mortality$population*100000, 0)
```

```
log.deaths <- log(mortality$deaths)
```

```
log.avg_age <- log(mortality$avg_age)
```

```
log.population <- log(mortality$population)
```

```
log.deaths_rate<- log(mortality$deaths_rate)
```

```
#regression - OLS
```

```
lm1<- lm(log.deaths_rate ~ log.avg_age)
```

```
#plots
```

```
#plot( lm1$fitted , resid(lm1))
```

```
plot( y= log.deaths_rate, x= log.avg_age, type='p', pch=19, col='blue',
```

```
      ylab = "log (deaths_rate)" , xlab= "log (avg_age)" , main= "OLS regression (log-log)" )
```

```
abline(lm1,col='red', lwd=3)
```

```
plot( mortality$avg_age, mortality$deaths, pch=19,col="blue",
```

```

      xlab= "Age", ylab="Deaths", main= "OLS regression ")

lines(mortality$avg_age, (exp(lm1$fitted)*mortality$population)/100000, col="red",lwd=3)


#regression - book, exercise 3.5.3

lm0_age_index<- lm(log.deaths ~ log.population + mortality$age_index )

#plots

plot( exp(lm0_age_index$fitted ))

plot( mortality$age_index, mortality$deaths, pch=19,col="black",

      xlab= "Index", ylab="Deaths", main= "Regression model used in exercise 3.5.3 ")

lines(mortality$age_index, exp(lm0_age_index$fitted) ,col="blue",lwd=3)


#regression - poisson - rate

glm2 <- glm(mortality$deaths ~ mortality$avg_age, offset=log(mortality$population +1),

            family="poisson",data=mortality)

#plots

plot( mortality$avg_age, mortality$deaths, pch=19,col="black",

      xlab= "Age", ylab="Deaths", main="Regression comparison (blue = GLM, red = OLS)")

lines(mortality$avg_age, glm2$fitted ,col="blue",lwd=3)

lines(mortality$avg_age, (exp(lm1$fitted)*mortality$population)/100000, col="red",lwd=3)

```