

SOME CALCULUS FUNCTIONS

DERIVATIVES OF UNIVERSE TRIGONOMETRIC FUNTIONS

- $y = \arcsin x (x \in (-1; 1)) \rightarrow y' = \frac{1}{\sqrt{1-x^2}}$
- $y = \arccos x (x \in (-1; 1)) \rightarrow y' = \frac{-1}{\sqrt{1-x^2}}$
- $y = \arctan x \rightarrow y' = \frac{1}{1+x^2}$
- $y = \operatorname{arccot} x \rightarrow y' = \frac{-1}{1+x^2}$

DERIVATIVE OF HYPERBOLIC FUNCTION

- $y = \sinh x \rightarrow y' = \cosh x$
- $y = \cosh x \rightarrow y' = \sinh x$
- $y = \tanh x \rightarrow y' = \frac{1}{\cosh^2 x}$
- $y = \coth x \rightarrow y' = \frac{-1}{\sinh^2 x}$

LEINIZ FORMULA

"If $f(x)$ and $g(x)$ have n^{th} derivative then $f(x) \times g(x)$ also have n^{th} derivative"

$$(f(x) \times g(x))^n = \sum_{k=0}^n (C_n^k f^{n-k}(x) g^k(x))$$

SOME BASIC FORMULA

- $(a^x)^n = a^x \ln^n a$
- $(e^x)^n = e^x$
- $(\sin ax)^n = a^n \sin(ax + \frac{n\pi}{2})$
- $(\cos ax)^n = a^n \cos(ax + \frac{n\pi}{2})$
- $((ax+b)^\alpha)^n = a^n \alpha(\alpha-1) \dots (\alpha-n+1)(ax+b)^{\alpha-n}$
- $\log_a |x|^n = \frac{(-1)^{n-1}(n-1)!}{x^n \ln a}$
- $\ln |x|^n = \frac{(-1)^{n-1}(n-1)!}{x^n}$

LINEAR APPROXIMATION

$f(x) \approx f(a) + f'(a)(x-a)$ is called the linear approximation or tangent line approximation of f at a

THE 1ST ORDER DIFFERENTIAL

"The 1st order differential dy of $y = f(x)$ at a is defined in term of dx by equation"

$$df(a) = f'(a)dx$$

THE 2ND ORDER DIFFERENTIAL

"The 2nd order differential of $y = f(x)$ at a is defined in term of dx by equation"

$$d^2f(a) = f''(a)dx^2$$

THE NTH ORDER DIFFERENTIAL

"The nth order differential of $y = f(x)$ at a is defined in term of dx by equation"

$$d^n f(a) = f^{(n)}(a)dx^n$$