

Bending Mathematical Rules

A book by Behrad.B([TadavomnisT](#))

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Introduction:

Join me on a journey into the fascinating world of mathematics. My aim is to discover unbreakable rules and push their limits by bending them as much as possible. I strive to achieve the impossible, challenging the notion that some things cannot be done. Through my exploration, I seek to uncover patterns and reveal the hidden magic beneath the numbers and eventually questioning the fundamental principles of mathematics. In this book, we will challenge the rumor that math is merely an abstract concept or something that's poorly taught in schools. However, be warned, once you step a foot in world of math, you may become addicted to the wonders of it:3

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