## **Hadamard Matrix**

Time limit: 1 sec

a Hadamard matrix, named after the French mathematician Jacques Hadamard, is a square matrix. There are several Hadamard matrices, each is identified by an integer  $\mathbf{n}$ . The Hadamard matrix of the order  $\mathbf{n}$  is denoted by  $H_n$  and has the size of  $\mathbf{n}$  row and  $\mathbf{n}$  column. The Hadamard matrix of rank 2n can be constructed from the Hadamard matrix of rank  $\mathbf{n}$ . The construction of the Hadamard matrix of rank  $\mathbf{n}$  can be defined recursively as follow.

$$H_{1}=[1]$$

$$H_2 = \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$$

$$H_{n} = \begin{bmatrix} H_{2^{n-1}} & H_{2^{n-1}} \\ H_{2^{n-1}} & -H_{2^{n-1}} \end{bmatrix}$$

Given a column vector of size n  $v = \begin{bmatrix} v_1 \\ v_2 \\ \vdots \\ v_n \end{bmatrix}$ , calculate  $H_n v$  which is the production

of the metrix H<sub>n</sub> and a vector v

## Input

- The first line of input contains an integers n. It is guaranteed that n = 2<sup>k</sup> where 0
  k <= 18.</li>
- The second line contains  ${\bf n}$  integers representing  $v_1, v_2, ..., v_n$  where -1,000 <  $v_n$  < 1000.

## **Output**

The output must be exactly 1 lines that contains N integers that described the vector  $H_n v$  .

## **Example**

Input	Output
1	10
10	
2	30 -10
10 20	
4	15 -5 -9 3
1 2 4 8	