Debugging and expanding MetaCasanova

Bachelor Thesis

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Written by

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Abstract

Write shit here as very short summary mc needs testing and expanding standard library has been expanded test programs have been created conclusion has been made

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Part I

Preface

Chapter 1

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Chapter 2

Introduction

Chapter 3

Assignment

3.1 Company

The graduation assignment is be carried out at Kenniscentrum Creating 010. The company is located in Rotterdam. *Kenniscentrum Creating 010 is a transdisciplinary design-inclusive Research Center enabling citizens, students and creative industry making the future of Rotterdam*[1].

The assignment is carried out within a research group, who is building a new programming language. The new programming language is called *Casanova*.

3.2 Motive

MetaCasanova (from now on called *MC*) comes forth from the language Casanova, hence the name.

Casanova is a language made for building games. It uses higher order types to make the programming of complex constructs easier. These constucts are often used in game development. A few of these constructs will be explained in detail from chapter 6 onward.

Because of the higher order types the compiler for Casanova became complex. The compiler for Casanova worked, but was still in development. So when a bug was found in the compiler, fixing it was becoming more and more time consuming. This frustrated the developers so much a new language was created.

MC was this new language. MC serves as the language in which the compiler for Casanova will be written.

At the beginning of the assignment MC was still in development. The syntax was nearly complete, but untested, and the standard library of MC was just beginning to take shape. The assignment was created to debug and expand the language.

I took this assignment and have written my bachelor thesis on it.

3.3 Goal

As stated the main goal of the assignment is to debug and expand the language. Which translates to the following research question: *How can the programming language MetaCasanova be improved from its current state within the timeframe of the internship?* This goal is quite broad and I have created a few subgoals to define a scope for the assignment.

1. Double checking the existing design of the language.
2. Participating in the design of the language.
3. Extending the standard library.
4. Creating test programs.

I will now explain the subgoals in greater detail.

3.3.1 Double checking the existing design of the language

At the start of the assignment MC will have to be checked for any existing faults. This way we can ensure that the language has a safe base point from which it can be developed further.

The checking of MC will consist of the existing syntax and the ideas for which the syntax was created. This will be done by exploring the current syntax and understanding the reasons why it is this way.

3.3.2 Participating in the design of the language

As MC is still in development and my assignment consists of debugging and expanding, I will propose design changes and new designs. These designs will be discussed and reviewed with the rest of the team.

This will be done in an exploratory way as the language grows and changes.

3.3.3 Extending the standard library

The standard library of every language is an extention of the functionality of the language. It contains often used constructs and functions which makes the language more productive for the programmer.

MC has but a small standard library and this needs to be expanded in order to be of any practical use. This also could help make MC a success [2].

The standard library of MC will be completely written in MC itself. This will show how powerfull the simple and effective syntax of MC is.

Extending the library also gives me the position of a user of MC. For now the only people that have used MC are the developers themselves. Now that I

will join the research team they will get a fresh and new look at the language through me.

3.3.4 Creating test programs

Writing the standard library is one aspect of a language. Another are actual applications.

The standard library can be seen as an application, but it is different in the sense that they create standard functions to be used by programmers. Applications are not part of the code base and also serve users outside of the programming community.

Because the only users so far have been the developers, there have only been small test programs written. They often test a specific function of the compiler. The test applications will test the entire language.

Because of the timelimit I will not be able to create a huge application, but I will be able to create bigger ones than those currently used for testing.

I have chosen to create game or game-like test prog

3.4 Correlation with other projects

During the internship the research team keeps developing MC. There are also two other students doing an internship on MC. They are both working on the compiler, one is developing the back-end of the compiler and the other the front-end. The student will cooperate with the research team and both these students.

Part II

Preliminary research

Chapter 4

MC in detail

Here we will look at MC and learn what the language is and how it works. **FIX THIS SENTENCE:** Because the current version of MC is not documented, the following information comes from interviews with the research team.

4.1 What is MC

MC stands for MetaCasanova and is a declaritive functional language. It tries to be a completely pure language, which means no side-effects are allowed directly.

MC can use . The exception to this rule is the .NET functionality. **.NET ALLOWS MANIPULATIVES, EXPAND**

4.2 Goal

DOUBLE CHECK The goal of MC is to use higher order types with type safety, in a natural way of programming. These higher order types gives the ability to resolve certain computations on compile time, which can normally be resolved at run time only. This can substantially increase performance at run time.

It also supports the .NET library natively. Because .NET allows for manipulation of values, MC supports this when using .NET.

MC also aims to be as flexible as possible with the safety of a strong type system.

4.3 Basics

We will now go through the basics of MC. What systems MC uses, learn how the syntax works and use small code samples to explain the workings.

The evolution of these basics will be given in part III. This will give us a better understanding of why and how MC evolved.

4.3.1 Terms, types & kinds

With MC you program on three different levels:

1. Terms
2. Types
3. Kinds

Terms are the values of variables, like 5, 'c' or "Hello". Types are the types of variables, like Integer, String or Boolean. Kinds are for types, what types are to terms. You could say the kinds are the types of the types.

4.3.2 Runtime and compile time

Kinds are resolved or inlined at compile time. Types are also resolved or inlined, except when they create datastructures. These data structures keep existing on runtime.

The syntax reflects this in the arrows used with the functions. The `=>` arrow indicates a function operates on compile time and the `->` arrow indicates a function operates on runtime.

4.3.3 Func

First we need to declare a function before defining it. For this we use the keyword `Func`.

```
Func "computeNumber" -> Boolean -> Int -> Int
    ↪ -> Int
```

Here we see that the function *computeNumber* is a function which goes from a Boolean and two Interegers to an Integer.

The parameters are seperated by the `->`. The last parameter is the return type of the function and all the parameters between the name and the return type, are the arguments of the function.

A function is defined by one or multiple *rules*. A *rule* consists of a *conclusion* and one or more *premises*. They are separated by the *bar*. The conclusionstands underneath the bar and the premises above.

Now let's define a rule for `computeNumber`.

```
1 a == True
2 add b c -> res
3 ---------------
4 computeNumber a b c -> res
```

The conclusion is on the fourth line, the bar on the third and the premise on the first and second. The conclusion has the name of the function and the input arguments on the left of the arrow and the output argument on the right. This syntax is similiar to that of natural deduction [].

Local defined variables

The variables named in the conclusion of a function are locally defined. With the function `computeNumber` the variables `a`, `b` and `c` are examples of these local variables.

4.3.4 Multiple rules

There can also be multiple rules which form function definition.

```
a == True
add b c -> res
---------------
computeNumber a b c -> res

a == False
mul b c -> res
---------------
computeNumber a b c -> res
```

When this happens the rules are attempted in order of definition. If the above rule fails and the rule beneath it is attempted. A rule fails when the arguments do not match. If none of the rules match the program fails.

Let us go through this process with an example.

First we will try the following function call:

```
computeNumber False 5 3 -> newValue
```

The first rule to be attempted is the one written first in the source code, so:

```
a == True
add b c -> res
---------------
computeNumber a b c -> res
```

This rule will fail, because the first argument has the value `False` and not `True`. So this rule will not be executed.

The next rule to be attempted is:

```
a == False
mul b c -> res
---------------
computeNumber a b c -> res
```

The first argument is set to `False` and the second and third are both Integers, so the rule matches. The rule will be executed and the result will be put in `newValue`.

4.3.5 Constants

Constants can be created by using `Func` without any parameters. The return type still has to be declared.

```
Func "bar" -> Int
bar -> 5
```

Here the constant `bar` is set to the value `5`.

As we have seen `Func` uses types in its declaration and terms in its definition. The types enables the detection of wrong function calls during compile time.

Important to note is that functions declared by `Func` are on runtime. As we will see in section 4.3.9, MC also has the ability to declare and define functions on compile time.

4.3.6 Functions as parameters

Aside from variables, functions can also be given as parameters. This needs to be specified in the declaration of the function.

```
Func "isThisEven" -> ( 'a -> 'b ) -> 'a -> 'd
```

Here we see that the first argument `( 'a -> 'b )` is a function. This is can be seen when we declare a function which takes one argument.

```
Func "x" -> 'a -> 'b
```

When we strip away the name of the function and the keyword `Func`, we are left with just the function.

```
'a -> 'b
```

This we can use in declarations to indicate a function is used as the argument.

4.3.7 Data

With `Data` we can declare a constructor and deconstructors for a new type. Effectively making it an alias.

Say that we want to create a union, a type which can be any of the predefined types within a set []. For this we need a way to construct the union type and a way to deconstructed the union back to its original type. The deconstructor is needed to get know which of the types inside the union is actually used. Only then can we know which of the types inside the inion is used.

As an example we will create a union of a String and a Float.

```
Data "Left"  -> String -> String | Float
Data "Right" -> Float  -> String | Float
```

Here we create two constructors whom both go to the same type, `String | Float`. `Left` and `Right` can be seen as an alias for the `String | Float` union.

Let us see how this is used. We need a function which takes a union as argument.

```
Func "isFloat" -> ( String | Float ) -> Boolean
```

The parentheses in the declaration can be left out, but are used to clarify that the union is one argument.

In the definition we want to check which type the union is. This can be done directly in the conclusion of a rule.

```
isFloat Float -> True
```

The deconstructor of the argument given, automatically checks if the types match. This can be done because they are aliases. Aliases are automatically resolved to their basic types by the compiler.

Conditionals using aliases can be put in the conclusion. Other conditionals have to be put in the premises, because they need to be computed. As can be seen in section 4.3.3.

To make the definition of `IsFloat` complete we also need a rule that checks for `String`.

```
isFloat String -> False
```

Now we will test the function `isFloat` with the help of constant `iAmFloat`.

```
Right 9.27 -> iAmFloat
```

`iAmFloat` has type `String | Float` and can now be passed to `isFloat`.

```
isFloat iAmFloat -> output
```

When `iAmFloat` is deconstructed to its original type it will match with the first rule of `isFloat`. The variable `output` now contains the value `True`.

4.3.8 TypeAlias

Because the | (*pipe*) operator, used in section 4.3.7, is not built in the language we need to create it. To do this we need to manipulate types.

We have already seen that `TypeFunc` can do this, see section 4.3.9. But to make | work, we now need a constructor and deconstructor that works with kinds.

`TypeAlias` is the same as `Data` only on a higher level of abstraction. It constructs and deconstructs kinds.

With `TypeAlias` we can create a generic | with which we can create unions. Unlike `Data`, `TypeAlias` needs both a declaration and a definition. The declaration shows what happens on kind level and the definition shows what happens on type level.

```
TypeAlias Type => "|" => Type => Type
```

Here we see how the generic | is declared. It takes two paramaters of any type and returns a type.

The `Type` is a kind and indicates an unknown type is used.

As shown parameters can be infix.

Infix parameters

There is a limitation to the use left arguments, there may only be one. This is because of the parser used. The parser would become overly complex when adding multiple arguments on the left.

Because the benefits of having multiple arguments in front of the function name do not outway the time it consumes to expand the parser, the choice was made to only allow one argument in front.

When defining | we want to use generic types. This way a union can be created from all types.

Generic type identifiers

To indicate generic types the `'` notation is used.

This is enhanced with the use of *identifiers* after `'`. These give the generic type a name and can be used to express if one generic type is the same as another generic type.

We will use this in the definition of |:

```
'a | 'b => pipe<'a 'b>
```

Now we can say that two different types are used as the arguments and in the created pipe.

Type annotiatons

The angle brackets are used as type annotation for `pipe`. They indicate that `'a` and `'b` are part of the type `pipe`. This is only used with generic types, because it makes it easier for the parser to resolve the types. More on this in section 5.3.

4.3.9 TypeFunc

`TypeFunc` creates a function on type level. It can do computations with both types and terms.

We will demonstrate the power of `TypeFunc` with a function which manipulates a type. The function will take a tuple and return the same tuple, but with switched types.

First we need to declare a tuple with `TypeAlias`.

```
TypeAlias Type => "*" => Type => Type
'a * 'b => tuple<'a 'b>
```

Now that we have a tuple we can use it in the function declaration. The tuple argument will have generic types so it can work with any tuple.

```
TypeFunc "switch" => tuple<'a 'b> => tuple<'b '
    ↪ a>
```

Next we have the definition. Here we need to deconstruct the tuple to its original arguments. These arguments can then be used to create the return tuple.

```
a => (c * d)
(d * c) => res
---------------
switch a => res
```

Here we can see how the types inside the tuple are switched and returned as a new tuple.

Parameters

Important to note is that both `TypeAlias` and `TypeFunc` can use kinds, types and terms. Because they work on compile time only, they cannot replace `Data` and `Func`.

`Data` and `Func` exist for explicit runtime functions.

4.3.10 Module

`Module` is used to create a container on compile time. It is a collection of function declarations and definitions.

It does not fit within the levels defined in section 4.3.1. Modules can only be declared by `TypeFunc`.

Say we want to create a container for every type which does an addition of two variables of those types. The could be declared when we need them or we can put them in a `Module`.

When we create an addition container using a module, we do not have to type out the addition functions for every type. We can just call the module to create the functions for us.

A `Module` is declared with a `TypeFunc`.

```
TypeFunc "Add" => Type => Module
```

Here we declare the `Add` to take a type and return a `Module`.

We then want to define the module `Add` with the `+` operator and the `identityAdd` constant.

```
Add 'a => Module {
  Func 'a -> "+" -> 'a -> 'a
  Func "identityAdd" -> 'a
}
```

This creates a basic container with generic addition functionality.

As shown it can contain `Func`, but can also contain `Data`, `TypeFunc`, `TypeAlias` and another `Module`.

The declarations within the Module do not have to be defined. This way we can define different behavior for every instance of the module.

It is possible to have a function declared and defined within a module.

When we want to define the above declared `Add` with an integer, we instanciate the module with `Int`. We then define the functions which are declared within `Add` to finish the module.

```
MonoidAdd Int = {
  Int -> "+" -> Int -> Int
  identityAdd -> 0
}
```

The `Func`s are defined as they normally are, only now they are wrapped within a `Module`.

The caret

When we want to call a function within a module from outside the module the `^` is used.

```
Func "caretTest" -> Int
caretTest -> identityAdd^Int
```

This creates a constant named `caretTest` with the same value as the `identityAdd` from the module `Int`. The `^` can be seen as the '`.`' (the dot) used in C#. The hierarchy used in MC is different from most languages.

Say we have a C# class `Int` containing the constant `identityAdd`, the constant is called like this:

```
Int.identityAdd
```

As seen in the example MC does it the other way around. This has the advantage of knowing immediately what you are using, instead of knowing where it comes from.

Inherit

Modules can also inherit from other modules. This is done with `inherit`.

We will create a module which inherits from the `Add` module. The operator `-` will then be added aswell.

```
TypeFunc "GroupAdd" => Type => Module
GroupAdd 'a => Module {
  inherit Add 'a
  Func 'a -> "-" -> 'a -> 'a
}
```

The module `Add` from section **??** is instantiated with `'a`. The created `Add` module is then inherited into `GroupAdd`.

The function declarations and definitions of the inherited module are directly usable within the new module.

If a module takes another module as an argument, the module can also directly inherit.

```
TypeFunc "GroupAdd" => Add => Module
GroupAdd M => Module {
  inherit M
}
```

Now everything from module `M` is inherited into `GroupAdd`.

When inheriting a module which contains an inherit, these are also inherited in to the current module. This works recursively.

4.3.11 priority

We can also give a priority together with a declaration. The priority indicitates the order of function execution.

The priority is indicated by the `#>` and is placed after the declaration. When we look at `Data` it will look like this:

```
Data "Left"  -> String -> String | Float  #> 7
Data "Right" -> Float  -> String | Float  #> 5
```

And with `Func` and `TypeFunc` it is used like this:

```
Func "bar" -> Int #> 12
TypeFunc "foo" => Float => 'a => 'b #> 9
```

The `#>` is also used to indicate associativity. Everything is left associative by default, but if we want to make it right associative we can do that by placing an `R` after the `#>`.

```
Func Int -> "\" -> Int -> Int #> R
```

The priority and associativity can also be used in combination with each other.

```
Func Int -> "\" -> Int -> Int #> 25 R
```

4.3.12 Import

`Import` is used when importing other files in the current file.

If the file imported has any imports, they are ignored. Unlike `inherit`, `import` is not recursive.

The programmer can directly use the declarations and definitions used in the imported file. When the programmer wants to explicitely specify to use a function from the imported file the `^` is used.

We will import the file “vector” and use the `Vector2` type from it.

```
import vector

Func "location" -> Vector2
location -> createVector2^vector 8.9 19.0
```

The importing of MC files always works with non capitalized import statements, even when the actual files does contains capitals. This is done to differentiate between MC imports and .NET imports.

The order of elments is the same as with modules, only when using .NET imports there is a difference in syntax. When calling a .NET function the elements are in the same order as with .NET, instead of doing it the other way around when using the `^` with modules.

```
import System

Func "dotNetTest" -> String
dotNetTest -> DateTime^Now^ToString()
```

Here `dotNetTest` becomes a String which contains the current date and time.

In keeping constistency with the .NET way of calling, the programmer does not have to reverse the order of the elements in the call. This might seem like a trivial thing to do, but from experiments we concluded that it confused the programmer more than initially thought. For this reason the order of elements in a .NET call will stay in synchonicity with the .NET standard.

4.3.13 Builtin

Some things cannot be created out of nothing and need to be built in the compiler. An example of this is boolean.

When using such a builtin literal the keyword `builtin` is used. We can now correctly implement the function `foo` from section 4.3.3 using the `builtin` keyword:

```
add b c -> res
---------------
foo True^builtin b c -> res

mul b c -> res
---------------
foo False^builtin b c -> res
```

It can be seen as if they are imported

4.3.14 Comments

There are two sorts of comments in MC: a single line comment, indicated by `$$`, and a block comment, indicated by `$* *$`. With these two options the programmer can sufficiently insert comments in the code.

4.3.15 Lambdas

MC also has a fully implemented lambdas.

The basic syntax is as one would expect of a lambda, it has arguments and returns what the functionBody returns

```
(\ arguments -> functionBody )
```

In practice this would look like:

```
(\ a -> divide^Int 10 a )
```

Lambdas do not need to be declared because they always are generic functions. The typechecker will check the lambdas the same way as any other generic function. From the context of what the function body does together with the types of the arguments, it can deduce what the output type should be.

4.3.16 ArrowFunc

`ArrowFunc` always needs an argument on the left of the name and atleast one function to the right. A unique feature of `ArrowFunc` is the two syntax options it has when the function gets called.

The first is like a normal function and the second converts it to a lambda.

As with `Func` it needs a declaration and a definition.

```
ArrowFunc Int -> ":~>" -> (Int -> Int) -> Int
f a -> res
-------------
a :~> f -> res
```

Here `:~>` takes an integer and a function that takes an integer and returns an integer.

The declaration and definition are the same as the rest of MC.

When we call `:~>`, there is the normal way:

```
a :~> f -> res
```

And there is the second way of calling:

```
{a :~> out
  f out} -> res
```

The brackets are used to indicate everything inside it belongs together. When an `ArrowFunc` is called like this it gets converted to a lambda. The first argument is then used a the argument for that lambda.

```
(\ out -> f out ) a -> res
```

The result from this is then returned as the output in `res`.

This syntax exists for when the nesting of lambdas occur. Lambdas become unreadable when nested.

```
(\ b -> (\ c -> f c ) b ) a -> res
```

When using the `ArrowFunc` syntax it nests neatly.

```
{a :~> b
  {b :~> c
    f c}} -> res
```

This syntax stems from the use of the bind of monads, which will be explained in further detail in section 6.4.

4.3.17 Partial application

Lastly MC supports partial application. This means that you do not have to give all the arguments to a function. When this is done a closure is created and given as output.

We will create a closure with the function `add`. `add` takes two Integers and returns an Integer.

In the definition we will say the two arguments will be added together.

```
Func "add" -> Int -> Int -> Int

a + b -> res
--------------
add a b -> res
```

Now we will give only one argument to `add` and create a new function `addThree`.

```
add 3 -> addThree
```

With this construct we have created the partially applied function `addThree`. When we look what it contains we see that it has a closure with a partly implemented `add`.

```
3 + b -> res
--------------
add 3 b -> res
```

We can now give `addThree` its second argument to complete the closure. This can be done multiple times.

```
addThree 6 -> foo

addThree 7 -> bar
```

The variable `foo` has a value of `9` and `bar` has a value of `10`.

When type annotations are used there can be no partial application. The type annotations need to know what types it gets or they will fail. This is further explained in section .

Now that we know the basics of MC lets take a look at the syntax has evolved.

Part III

MC expanded

Chapter 5

Syntax evolution

Here we will look into the overal syntax changes of the language. The changes concerning the standard library, will be discussed in chapter 6.

5.1 Generic type identifiers

As described in section 4.3.8 generic type identifiers are indicated by `'` together with a name, `'a`. The `'` is derived from the *prime* notation, which indicates a derivative of the original [].

For example when we have variable `i`, this variable might get changed and is then indicated by `i'`. This shows that `i'` is derived from `i`.

Instead of placing the *prime* at the end, it is placed before the variable name to indicate it is a generic type.

5.2 Generic kind identifiers

Generic kind identifiers are currently unused, but it was thought to be necessary after the implementation of `TypeAlias`.

When working with kinds they are always generic, as they indicate an unknown type. That was why they were indicated by an *asteriks*, `*`.

When `TypeAlias` was created it became apparent that the type would be the same in some cases. This resulted in generic kind identifiers.

The notation devised was similiar to the generic type identifiers. Instead of the *prime* the *hash* was used.

```
TypeFunc "unknownKinds" -> #a -> #b -> #a -> #c
```

Here we can see that the first and third arguments are of the same kind and the second argument and the return value are different kinds.

However this was an error in reasoning.

The fact that they are kinds means that they can be any type. The official notation used for kinds is either `Type` or `*`.

The syntax of kinds was changed to `Type`. This way the the `*` was free to be used for other things, like the tuple in section 4.3.9.

5.3 Type annotations

Generic type annotations were created during development to lower the complexity of the parser.

We use a data declaration which creates an array. It takes a generic type and a Integer.

Using the notation without type annotations it looks like this:

```
Data "array" -> 'a -> Int -> Array
```

The Integer sets the lenght and the generic type will be the type the array consists of.

When this is called we can use parentheses to indicate which arguments are grouped together.

```
array(Int 12) -> arrayOfInts
```

The Integer array is created with twelve elements.

But when we use a variable which contains the type, there is confusion what really happens.

```
array(var 12) -> arrayOfInts
```

This could imply that `var` is a function which uses `12` as its argument and returns a type. `arrayOfInts` is then a closure which still needs an argument which tells the lenght of the array.

We can only be sure what happens if we look at the declaration of `var`.

To avoid this and clarify what happens the type annotations were created. They are used in the data declaration, to specify the types used.

```
Data "array" -> 'a -> Int -> Array<'a Int>
```

Types using the type annotations cannot be partial applied, because they need to know the types they contain to be declared correctly.

When this is not done a compile time error is generated.

So now when we call `array` we know that `var` must be a type. When `var` is declared as a function which returns a type, we will have to call `array` like this:

```
TypeFunc "var" => Int => Type

nr == 12
------------
var nr -> Int

array((var 12) 9) -> arrayOfInts
```

This also lowers the complexity of the parser. With the use of type annotations, the parser does not have to look at `var` and what it is.

For these reasons the type annotations were implemented into the syntax.

5.4 TypeAlias

Before there was `TypeAlias`, `TypeFunc` was used for the same functionality. However `TypeFunc` cannot deconstruct.

When constructing a new kind with `TypeFunc` it can not be deconstructed to its original kind.

This error was noticed when updating the monadic part of the standard library, see section 6.4.

`Data` could not be used as it cannot manipulate types it can only construct and deconstruct them. That is why `TypeAlias` was created. It provides contructing and deconstructing functionality with type manipulation.

5.5 Module

5.5.1 Signature

Earlier in development `Module` was called `Signature`. It performed the same functionality as `Module`.

From the language creators perspective `Module` creates a specific signature on compile time. For the user it looks more like a container or class, when coming from object-oriented programming.

Because the user will be the one actually using the language, the name was changed to what it resembles to the user.

5.5.2 Expanding

During the development there were two ways of inheriting a module, via `inherit` and via expanding an existing module. Expanding modules is removed from MC, because of inconsistency issues.

A `Module` could be expanded via a function. The function takes a module as argument and expands this module by adding declarations and, optionally, definitions.

```
TypeFunc "expandModule" => Module => Module
expandModule M => M{
  Func "modulo" -> Float -> Float

  a % 10 -> res
  ---------------
  modulo a -> res
}
```

The module `M` is opened up again and `modulo` is added. Module `M` is then returned and contains the new function `modulo`.

This would have been syntactic sugar for creating a new module which inherits from `M`. In this new module `modulo` is then added.

```
TypeFunc "expandModule" => Module => Module
expandModule M => Module{
  inherit M

  Func "modulo" -> Float -> Float

  a % 10 -> res
  ---------------
  modulo a -> res
}
```

The expand syntax makes it look like modules are mutable, which they are not. This makes it inconsistent with the rest of MC and the expand-syntax was removed.

5.6 .NET libraries

When importing and calling .NET libraries the current syntax is using the element order of .NET with `^` as divider.

```
Func "dotNetTest" -> String
dotNetTest -> System^DateTime^Now^ToString()
```

This was not always used. The syntax for .NET imports went through several stages.

The first implementation was the original .NET manner:

```
dotNetTest -> System.DateTime.Now.ToString()
```

This seemed to strange considering the rest of the MC syntax. The order of the elements was then switched.

```
dotNetTest -> ToString().Now.DateTime.System
```

This made it more like MC but it was still out op place because of the dot used. It also looked strange when calling a method.

In the next itteration the dot was replaced with the caret.

```
dotNetTest -> ToString()^Now^DateTime^System
```

This seemed more in sync with the rest of MC. The only problem was with the method calls.

That is how we arrived at the current syntax used. The .NET order of elements is used and the `^` is used as seperator.

5.7 Builtin

The keyword `builtin` was first called `primitives`.

For the developers this was a good choice, as they indicate the primitives that needed to be built in the compiler.

For the user however this seemed confusing. The user sees the `primitives` as types that are built into the language.

The name was changed to `builtin`, to better reflect the way how the user sees them.

5.8 Conditionals

5.8.1 Inside the conclusion

During development we tried implementing conditionals inside the conclusion of a rule. This could make the code more compact.

We will take the example of `Func` from section 4.3.3, and implement this. The code is then compacted to this:

```
add b c -> res
---------------
computeNumber True b c -> res
```

This is just as easy to read as the original.

It does make the conclusion less conclusive as there is now something happening inside the conclusion. The conclusion is meant to show the input and output of the rule, it is not meant to tell what the function does.

That is where the premises are for.

The compiler also needed to be modified heavily. It now needed to do computations inside the conclusion.

To keep the language and the compiler modular, a comprise was done. Types created with `Data` and `TypeAlias` can be used as conditionals inside the conclusion. This is possible because they act as aliases and need no computation to be checked.

Conditionals requiring computation, a comparison of values, will be done in the premises.

5.8.2 Equals

When comparing values the `==` operator is used. This is done to keep the the single equals sign free to be used by the programmer.

Chapter 6

Standard library

We will now look at the standard library and explain the evolution it went through during the assignment. For readability only the neccesary parts of the code is shown. The complete code samples can be found in [].

Each item will be explained with the evolution after the explanation. When we have an idea of how it should work, the choices made during the development will be clearer.

6.1 Prelude

Prelude contains a few definitions making basic programming easier. The .NET *System* is imported and the type `Unit` is created.

```
import System

Data "unit" -> Unit
```

The `Unit` is used as an empty or null value.

Next we have the declaration and definition of a generic tuple and union. Because they are generic `TypeAlias` is needed for the type manipulation.

```
TypeAlias Type => "*" => Type => Type
'a * 'b => tuple<'a 'b>
Data 'a -> "," -> 'b -> 'a * 'b    #> 5

TypeAlias Type => "|" => Type => Type
'a | 'b => pipe<'a 'b>
Data "Left" -> 'a -> 'a | 'b       #> 5
Data "Right" -> 'b -> 'a | 'b      #> 5
```

Then a standard if-else construct is implemented.

```
Data "then" -> Then
Data "else" -> Else

Func "if" -> Boolean^System -> Then -> 'a ->
    ↪ Else -> 'a -> 'a
if True^builtin then f else g -> f
if False^builtin then f else g -> g
```

The `then` and `else` `Data`s are syntatic sugar and could be left out. We have left them in to enhance the clarity of the if-else construct.

Here we see how *System* of .NET is used. The boolean of .NET can be imported as shown, however the values `True` and `False` cannot be imported. They are built in .NET itself. This is why these literals are built into MC as well and need to be called using `builtin`.

6.1.1 Match

Next we have the `match` function. It takes a variable, matches it on either `Left` or `Right` and executes the function specified.

```
Data "with" -> With

Func "match" -> ('a | 'b) -> With -> ('a -> 'c)
    ↪  -> ('b -> 'c) -> 'c
```

First there some syntactic sugar created to make it clearer how `match` works. The first argument is the union which needs to get matched. The arguments (`'a -> 'c`) and (`'b -> 'c`) are the functions to be executed on a match.

In this case the two functions both take an argument from the union, the `'a` and the `'c`.

Next we have the definition of `match`. This gives a definition for both cases of the match, namely the `Right` and the `Left`.

```
match (Left x) with f g -> f x
match (Right y) with f g -> g y
```

When it matches the `Left` it executes function `f` with `x` as its argument. And when it matches the `Right` it executes function g with y as its argument.

However this does not take into account the possibility of nested pipes. For this we have written a third definition of `match`:

```
match y with g h -> res
--------------------
match (Right y) with f (g h) -> res
```

This definition is placed above the previous defined `match` which matches on `Right`. Then there is first checked on nested pipes and when there are none the actual value is checked.

In this manner there is no possibility of skipping any nested pipes.

6.1.2 List

Then we have a generic list implementation. For this we need to create a list that can work with types.

The list is declared with a union. This is necessary because we need an end to the list.

fix code?

```
TypeAlias "List" => Type => Unit | (Type * (
    ↪ List Type))
List unit => Left unit
List ('a * 'b) => Right ('a * 'b)
```

The list is created with a tuple. An end to the list is created with a union of the list tuple and `Unit`.

A list is then defined with either a unit or type.

We also need the basic operators to create lists. This is done with `::`, which takes a type and a list. And with `empty` an empty list is created.

fix code?

```
TypeAlias Type => "::" => List => List
'a :: 'b => List ('a * 'b)

TypeAlias "empty" => List
empty => List unit
```

With `::` we can specify the head and tail of a list.

But we would also like to concat lists together. This is done with the `@` operator.

```
Func List 'a -> "@" -> List 'a -> List 'a  #>
    ↪ 200
empty @ l -> l
(x :: xs) @ l -> x :: (xs @ l)
```

And when we want to apply a function to the entire list we call `map`. This executes a function and creates a new list, which it then returns.

```
Func "map" -> List 'a -> ('a -> 'b) -> List 'b
map empty f -> empty
map (x :: xs) f -> (f x) :: (map xs)
```

When we want to find one or more elements in the list we can call `filter`. It checks the entire list using a predicate function and returns the matching elements.

```
Func "filter" -> List 'a -> ('a -> Boolean^
    ↪ System) -> List 'a
filter empty p -> empty

(if p x then
  (x :: (filter xs p))
  else
  (filter xs p)) -> res
-------------------------
filter (x :: xs) p -> res
```

The programmer can specify the predicate function p.

6.1.3 Evolution of prelude

Boolean

Boolean currently does not exist anymore as a separate part of the standard library. Here we will see why this is the case.

Boolean was created to implement boolean logic. After many itterations it was discarded due to the evolution of the language.

When first implementing Boolean it was part of *Prelude*.

```
Data "True" -> Boolean^System
Data "False" -> Boolean^System
```

This might seem correct at first glance, but `True` and `False` have no meaning here. There is no way to check if a boolean value is true or false. That is why there had to come a new notation for the boolean literals.

It was turned into a module with the literals as `Funcs`.

```
import System

TypeFunc "Boolean" => Module
Boolean => Module {
  Func "True" -> Boolean^System
  Func "False" -> Boolean^System
}
```

Which could then be implemented in *prelude*.

```
boolean => Boolean {
   True -> True^builtin
   False -> False^builtin
}
```

The boolean literals could now be called using `True^boolean`. This was noticably the same as what happened inside the implementation of `boolean`. The choice was then made to call the boolean literals directly with `True^builtin`, which made the boolean module obsolete.

Which brings us to the current state of the boolean literals.

Match

Match started as a separate part of the standard library containing the `match` module. We will now look at how it was first created and how it has evolved into *prelude*.

The first iteration of the `match` module started with the import of *prelude* and the declaration of `match` module.

```
import prelude

TypeFunc "match" => Type => Module
```

So far there are no problems yet with us a module for `match`.

Next we see the first part of implementation of the `match` module: Some syntactic sugar is created and the actual function is defined which will do the matching.

```
match ('a | 'b) => Module {
  Data "with" -> With

  TypeFunc "Head" => Type
  Head => 'a

  TypeFunc "Tail" => Type
  Tail => 'b

  Func "doMatch" -> 'c -> With -> (Head -> 'd)
    ↪ -> (Tail -> 'd) -> 'd
```

Now we see why the module is needed. It was thought that the `match` module would get a separate instance for every match that was executed.

The `Head` and `Tail` are the checks to ensure the first function takes the `Left` as input and the second function takes the `Right`. As `Head` gets set to `'a` and `Tail` to `'b`.

When seperate functions, like these, are needed to check the validity of another function it is better to group them together inside a module.

The definitions of `doMatch` haven't changed compared to what they are currently.

```
  doMatch (Left x) with f g -> f x

  doMatch y with g h -> res
  --------------------
  doMatch (Right y) with f (g h) -> res

  doMatch (Right y) with f g -> g y
}
```

It became clear that `Head` and `Tail` were not necessary, because they were simply passing on type of the union.

With this removal the use of a module became obsolete, because we do not need to group a single function. The `doMatch` function was then renamed `match` and placed inside *prelude*.

Recursive match

The first itteration of match could not match nested pipes. It could only detect a direct match. As it only had the direct matches without the function that checks if `Right` is nested.

The solution could have been left to the programmer. He would have to create a separate match statement for every level of nesting. This would be quite inconvenient for the programmer.

For that reason the recursive functionality was added.

List

The first list was put together with the list monad. This seemed the logical choice at the time, because the list monad needed a list implementation to use inside the monad.

Monads will be explained in section 6.4 and the list monad in section 6.6.2.

When coming back to the list it became apparent that `List` was not only useful for the list monad. It could be used without the monad as a regular list implementation.

The choice was then made to move it to *prelude*.

6.2 Number

Number was created to give the user a generic interface to create numbers.

However because of the import system of MC it can directly import the integer and float types with all their functions from .NET. It can still be used for self defined number types.

Number is built up from different modules to give the programmer the freedom to choose what their custom numbers can do. The modules are aranged according to the mathematical way to built up numerical operators [].

It starts with the `MonoidAdd` module. It declares the + operator for the custom number.

```
TypeFunc "MonoidAdd" => Type => Module
MonoidAdd 'a => Module {
  Func 'a -> "+" -> 'a -> 'a #> 60
  Func "identityAdd" -> 'a
}
```

This needs the identity as a base number from which the operations will work.

Next we have the `GroupAdd` module. This inherits everything from the module `MonoidAdd` and adds the – operator.

```
TypeFunc "GroupAdd" => Type => Module
GroupAdd 'a => Module {
  inherit MonoidAdd 'a
  Func 'a -> "-" -> 'a -> 'a #> 60
}
```

We do the same for multiplication and dividing.

```
TypeFunc "MonoidMul" => Type => Module
MonoidMul 'a => Module {
  Func 'a -> "*" -> 'a -> 'a #> 70
  Func "identityMul" -> 'a
}

TypeFunc "GroupMul" => Type => Module
GroupMul 'a => Module {
  inherit MonoidMul 'a
  Func 'a -> "/" -> 'a -> 'a #> 70
}
```

Now we have declared the basic number operations of addition, substraction, multiplication and dividing.

We can combine them into a basic number like so:

```
TypeFunc "Number" => Type => Module
Number 'a => Module {
  inherit GroupAdd 'a
  inherit GroupMul 'a
}
```

Or create a Vector without the dividing operator, because vectors cannot be divided [].

```
TypeFunc "Vector" => Type => Module
Vector 'a => Module {
  inherit GroupAdd 'a
  inherit MonoidMul 'a
}
```

Ofcourse all the operators still have to be defined, but that is up to the programmer. This gives the programmer the freedom to choose what the operators do.

6.2.1 Evolution of number

During development *number* was used to create integers and floats. This was before the .NET import system was in place and it was thus needed. Currently it is only needed for user defined number types.

The first iteration of *number* was just one module with all the operators declared. This works for the standard number types like Integer and Float.

When using it to create a vector the module will have functions which are never used, because vectors cannot be divided.

For this reason the current *number* design is similiar to the mathematical way. It costs a bit more code to set things up, but there is less overhead.

6.3 Record

With *Record* we can create a list of key/value pairs which can be searched and manipulated. The special thing about this record is that is does all the searching on compile time. This makes the runtime code much faster.

When using records in practice we see that not everything can will be known on compile time. Which makes a record that works on compile time useless.

The way MC fixes this is to inline the code on compile time. In this way the code that needs to be actually executed can be optimised by the compiler after which it is executed on runtime.

Record is declared as a module and contains TypeFuncs to make it work on compile time.

```
TypeFunc "Record" => Module
Record => Module{
  TypeFunc "Label" => String
  TypeFunc "Field" => Type
  TypeFunc "Rest" => Record
```

Here we see a the declarations which are the basis of a list of key/value pairs. `Label` acts as the key, `Field` as the value paired with the key and `Rest` contains the rest of the record.

When there is just one pair in the record we can get that record out easily, we already have it. But when there are multiple record entries in a record we need a function to searches through the record to find the record we want to have. For this the `get` function was created.

```
  TypeFunc "get" => String => Record => Record

  (if (l == label^rs) then
    rs
  else
    get l rest^rs) => res
  ----------------------
  get l rs => res
```

The `get` function takes a labels and a record. It checks the label of the record and if it is the same it returns the current record and if not the it recursively calls itself with the rest of the record.

To manupilate these records there the `set` function was created.

```
  TypeFunc "set" => String => Type => Record =>
    ↪  Record
  (if (l == label^rs) then
    RecordEntry l f rs
  else
    set l f rest^rs) => res
  ------------------------
  set l f' rs => res
}
```

The `set` function takes a label, a field and a record. The field is the new value that needs to be paired with the label. Because MC does not allow direct manipulation of values the set function returns a new record instead of changing the value of the specified record.

With this the declaration of the record is complete. Now we can look at how the definition of a record works.

First we need to create a record entry. This is done with the `RecordEntry` TypeFunc.

```
TypeFunc "RecordEntry" => String => * => Record
    ↪  => Record
RecordEntry label field rest => Record{
  Field => field
  Label => label
  Rest => rest
}
```

We also need to create an empty record entry so we can end the record. This is done by the `EmptyRecord` TypeFunc.

```
TypeFunc "EmptyRecord" => RecordEntry
EmptyRecord => RecordEntry {
  Field => Unit
  Label => Unit
  Rest => Unit
}
```

The programmer has to use `EmptyRecord` as the `rest` argument of the first record entry. This creates an end to the record.

6.3.1 Updatable record

The current record can only be instantiated and not updated. To expand the record to be updatable we need to add the update function.

First we declare and define a TypeFunc which creates a new record from the original with inherit.

```
TypeFunc "updatableRecord" => Record => Record
updatableRecord r => Module {
   inherit r
```

The new module now contains everything of record r.

The we declare and define the update function.

```
  TypeFunc "update" => Record => Type => Record
  r == Empty
  --------------------
  update r dt => Empty
}
```

Only the definition of update which checks for an empty record can be defined. It is the only situation in which we can be certain what the return value will be, namely Empty.

If the record is not Empty we cannot know what the programmer wants to do with update. That is why we leave that definition of update up to the programmer.

6.3.2 Evolution of record

FIX THIS !!!!!!!!!!!!!!!!!!!!!!

Set and get

With the original version of set and get the field-argument was checked to be the same type offor the same type of the current value of the field for this fields was needed because of a fault, there needs to be no checking of the field, because field con be anything, fields became obsolete.

Now the record also has a its own type signature, because Field can be anything the type signature of every record is different. For this we created Cons.

```
  TypeFunc "Cons" => Type
  Cons => (Label,Field,Rest)
```

It acts as a getter of the type signature of the current record.

We also want this for the fields of the record, which is done with Fields.

```
  TypeFunc "Fields" => Type
  Fields => (Field,Fields^Rest)
```

The reason we want to know both the type signature of the fields and the record itself, is so we can use the signatures in declarations of functions. Say we want to create a function that takes all the fields of a record and manipulate them. Then we need to specify what the type is of the argument which contains these fields.

INSERT OLD SET AND GETTER AND EXPLAIN FURTHER

OLD CONS FUNC IN STILL OBSOLETE AS THE TYPE OF A RECORD IS ALWAYS RECORD

One which contains the current type of the record and one which updates the current record. The update function needs to be able to check if the newly created record has the same type of the original record. This ensures type safety. When the programmer would be able to change the type of the record, the new type could behave in a such a way that unpredicted things will happen. This problem could be left for the programmer to solve, but it is better to fix the problem before it happens.

If the programmer still wants to create a updatable record without the type safety, a new update function can be created by hand to circumvent the ready made update function.

The Cons function was created to hold the type information of the record and is added in r.

```
  TypeFunc "Cons" => Type
  Cons => (Label,Field,Rest)
```

The types of Label, Field and Rest make up the type of the entire

6.3.3 Apply

Here we will see how apply was thought to be needed and why it is not needed.

When we have a record with alot of nested or complex datastructures that we want to update, we have to go through the entire structure to be able to call the update function. To fix this apply was created.

apply takes a record a record and calls the update function directly, without going through the datastructure of the record.

```
TypeFunc "apply" => Record => Type => Record
update^r dt => res
------------------
apply r dt => res
```

Here we can see that all that apply does, is call the update function. When calling apply we go through the record to get the record we need. This way we only have to go through the structure of the record once and not everytime the we need to call the update function of a specific record.

We can now call apply to call the update function indirectly, without going to the entire record.

When implementing this we discovered we needed more than one apply function. **revisit this sentence** This could not be done as apply was already named.

We then put `apply` inside a module called `Rule`. `Rule` could then be called when declaring an `apply` for a record.

This seemed like the wrong direction to go. There was only one function inside the module of `Rule`, which makes having a module redundant. The complexity and performance was also impacted by the use of a module instead of directly calling the update function.

It was decided that the `Rule` module would be disregarded. The problem of not being able to create multiple `apply` functions is fixed by removing `apply` all together.

The programmer can create functions like `apply` fi he feels the need to. The programmer can then choose different names for the different `update` funtions that are being called.

6.4 Monad

Now we come to the module `Monad`. This module takes a mathematical concept and makes into practical programming construct.

Monads are the main reason MC has type manipulation.

First we are going to look at what monads exactly are within programming. Then we will see how they are implemented within MC.

6.4.1 Monads

Monads are a container-like generic interface. They contain atleast two functions, *return* and *bind*.

These two functions are the basic way we can use monads.

The return

The return function takes a value and wraps it inside a monad.

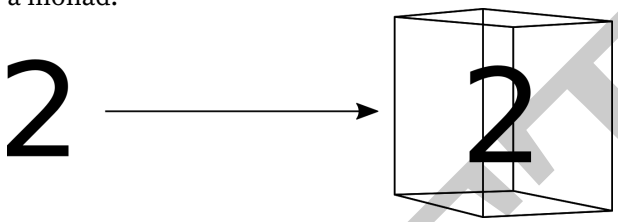

Figure 6.1: The return

The box in figure 6.1 visualizes the monad and 2 is the value that is being put inside the monad. With the return function any value can be put inside a monad. When it is inside the monad it cannot be seen by the outside world.

This is where the bind comes in.

The bind

Having a monad is fine, but what if you want to manupilate the value of the monad? The >>= (pronounced *bind*) function supplies this functionality.

When we want to apply the function `(+3)` to the monad containing 2, we call the bind. The bind unpacks the monad, as visualised in figure 6.2.

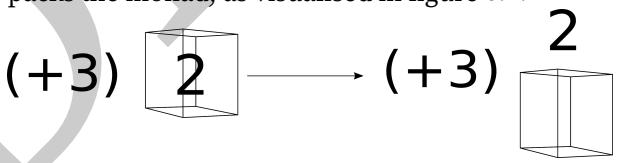

Figure 6.2: A function and a monad

It then applies the function to the value. And the the new value gets packed inside the monad by the function, as visualised in figure 6.3.

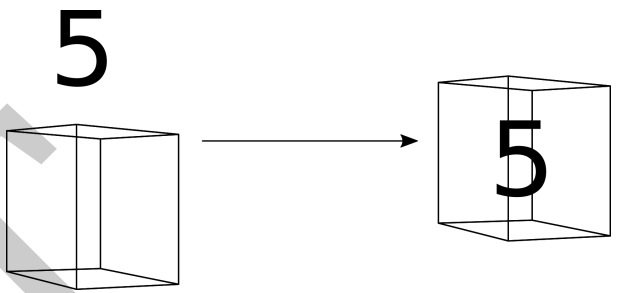

Figure 6.3: The return

Using these two basic functions, we can always work with monads and the values they contain.

To use the monads further we will need a few more functions. These functions are generic for all the monads and will be given an implementation.

Returnfrom

Sometimes we want to directly pass the value inside the monad instead of wrapping it. This is done with `returnFrom`.

```
Func "returnFrom" -> 'a -> 'a
returnFrom a -> a
```

As we can see the variable `a` is directly passed on.

Lift

Lift is used when a regular function, it takes a value and returns a value, needs to be executed over a monad. Lift unwraps the monad, executes the function with the value of the monad and then wraps the new value inside the monad.

An important difference with the bind, is that the function given to the lift does not pack the value

in a monad. The function passed to the bind does pack the value inside the monad.

```
Func "lift" -> ('a -> 'b ) -> 'M 'a -> 'M 'b
{a >>= a'
   return f a'} -> res
----------------------
lift f a -> res
```

Here we can see clearly that the lift repacks the value with `return`.

The `Lift` can also be declared with functions which take two arguments. It is then called `Lift2`.

`Lift2` has to bind twice, once for each monad.

```
Func "lift2" -> ('a -> 'b -> 'c) -> 'M 'a ->
  ↪ 'M 'b -> 'M 'c
{a >>= a'
   b >>= b'
     return f a' b'} -> res
---------------------------
lift2 f a b -> res
```

This can be expanded to functions which take any number of arguments.

LiftM

There are of course functions which work with the wrapped monad. For this `liftM` is created.

For this we have to use the bind and return of the wrapped monad.

```
  Func "liftM" -> (MCons^'M 'a -> MCons^M' 'b)
    ↪ -> 'M (MCons^'M 'a) -> 'M (Mcons^'M 'b)
  {M >>=^'M a
    f a -> b
    return^'M b} -> res
  ---------------------
  liftM f M -> res
}
```

It works the same as the other lift functions, with the specification of using the bind and return of the wrapped monad, `'M`, instead of the bind and return of the current monad.

FIX THE NEXT SENTENCE With these functions implemented the monad can be used with a wider range.

More than a wrapper

But just a monad offers very little besides being a wrapper for values. **FIX THE NEXT SENTENCE** This means a lot of ..... map to monads. That is why there have been created a few different sorts of monads.

We will discuss two of these for now. More will be explained when looking at the implemented monads in MC, see section 6.6.

The state monad gives monads the ability to behave like mutables. It takes a *state* and returns a new state and a return value.

Say we want a random number generator. The state monad will simulate the *state* of the number being generated. The state monad is given a *state* in the form of a number and from this it will compute the new state of the number and the random number generated.

In MC the functionality might look like this:

```
Func "state" -> 's -> ('a,'s)
state number -> (randomGeneratedNumber,
    ↪ newNumber)
```

The maybe monad offers the ability of the value to be either a value or nothing. For example we could utilize the pipe operator for this:

```
Data "Maybe" -> 'a -> 'a | Unit

Func "test" -> Maybe -> Boolean^System
(match a with
  (\ x -> True^builtin)
  (\ unit -> False^builtin)) -> res
-----------------------------------
test a -> res
```

Here we use `Unit` as the nothing and 'a as the value. In the example the term a is checked for a being a value, the `Left`, or being nothing, the `Right`.

This is a very basic example of how the maybe works. It acts like a pipe and can contain either a value, `Left`, or nothing, `Right`.

MOVE THIS UP MAYBE The implementations of these monads are far from complete, these examples simply show the functionality of the monad. The actual implementation will be given in section 6.4.3.

Combining monads

Monads can also be combined. Since they have the same generic interface they can be combined into another generic inteface. These new monads can utilise the functionality of the all combined monads.

In this way the functionality of a monad can be extended. Combining monads can be seen as putting one monad inside another monad.

We will take the state and maybe monad and combine these into a parser monad. A parser monad can parse through a piece of text and scan for certain elements.

The state monad will be used for the scanning functionality and the maybe monad will be used to determine of the element has been found. The state monad returns the maybe monad as its result. When the maybe monad has a value as result the parser monad stops.

Like the normal monads they have to be build manually. This is a very error prone process when combining more than two monads or when using more complex monads.

What we actually want is to write the monads once and combine them automatically. This is where monad transformers come in.

6.4.2 Monad transformers

Monad transformers are a way to automatically combine monads. Instead of simply having a monad which takes the arguments it needs, it also takes another monad transformer as one of its arguments. This monad transformer is then used to given the actual value.

MC has an implementation of the basic monad transformer with which all monad transformers and monads can be created.

For monad transformers to work a generic function is added which contains the signature of the monad wrapped inside the transformer.

```
TypeFunc "MCons" -> Type
MCons -> 'M
```

The variable `'M` is the monad given to the monad transformer. `MCons` can be called when this monad is needed directly.

6.4.3 Implementation

Now we will look at how the monad transformer is implemented. With this monad transformer we will be able to create actual monads, this can be seen as the base module for monads.

First we take a look at the declaration:

```
TypeFunc "Monad" => (Type => Type) => Module
```

Monads are implemented as modules. This way we can put the return and bind functions inside a monad.

The first argument is a function on type level. It represents the monad transformer it uses to wrap the result in.

When looking at the implementation we see that a module is created with the return and the bind:

```
Monad 'M => Module {
  ArrowFunc 'M 'a -> ">>=" -> ('a -> 'M 'b) ->
    ↪ 'M 'b   #> 10
  Func "return" -> 'a -> 'M 'a
```

PUT »= EARLIER The bind is declared with `ArrowFunc` and is called `>>=`. It takes a monad as its first argument and a function as its second argument.

The function creates the new monad which is then returned.

The return takes a value, `'a`, and wraps it inside the monad, `'M`.

Both the bind and the return are only declared and not defined, because they are different for every monad created. When creating a new monad the bind and return will need to be defined.

The functions explained and implemented in section **??** will be added to this aswell.

With those we have the complete interface of the monad transformer. With this we can combine and built monads automatically.

6.4.4 Evolution of monad

DO THIS !!!!!!!!!!!!!!!!!!! started with MCons, bind, return and returnFrom. added lift, lift2 and liftM

6.5 Tryable monad

Apart from the regular monadic module there is also the tryable monadic module. The tryable monad has as extra functionality that a function can be attempted.

This means that we can have functions that fail, without breaking the program.

It uses the regular monadic module to create a new interface. It also takes a monad as an argument which it then inherits.

```
TypeFunc "TryableMonad" => (Type => Type) =>
    ↪ Module
TryableMonad 'M => Monad(MCons^'M) {
  inherit 'M
```

It uses the type signature of `'M` to create a new monad.

Here we see how `MCons` is used to get the signature of the original monad.

Then we declare the `try` function. It takes a monad and two functions.

```
  Func "try" => MCons^'M 'a => ('a -> MCons^'M
    ↪ 'b) => ('e -> MCons^'M 'b) => MCons^'M '
    ↪ b
```

The value inside the monad is checked and then one of the functions is executed. This will be done in the definition.

First the value inside the monad is put into a `match`.

```
  {pm >>=^'M x
    (match x with
```

If `x` contains an error the error function processes it. And if it contains a value the value is passed to the function.

```
      (\e -> err e)
      (\y -> k y)) -> z
```

The result of the `match` is then wrapped in monad `'M` and returned.

```
    return^'M z} -> res
  --------------------
  try pm k err -> res
}
```

With `try` we can now check if the monad contains a value or an error and process them.

The `try` function was put to the test by manually typechecking it. The resulting proof can be found in appendix A.

We also want to be able to get the original monad out of the tryable monad. This is done with `getMonad`.

```
  Func "getMonad" -> MCons^'M
  getMonad -> 'M
}
```

INSERT CONCLUSION

6.5.1 Evolution of tryable monad

DO THIS !!!!!!!!!!!!!!!!!! No clue what to say here..... evolved from the either monad????

6.6 Implemented monads

6.6.1 Id

If monad transformers always take another monad, there has to be atleast one to end the chain. That is where the *id* monad transformer comes in.

It takes no monad as argument and simply returns all values as the are.

First we need a type signature to tell the monad interface which monad we are creating.

```
TypeAlias "Id" => Type => Type
Id 'a => 'a
```

Here we can see what the id monad should do, simply pass the type on as it was given.

Now we will declare and define the id monad. The type signature is created with `Id` and the bind and return are defined.

```
TypeFunc "id" => Monad
id => Monad(Id) {
  bind x k -> k x
  return x -> x
}
```

`Id` also takes an `'a`, but this is never used as the id monad does not need an extra type to say which type it really uses. While the `'a` is not used, it necessary to have them in the type signature. Else `Id` cannot be used to instantiate `Monad`, as evident from section 6.4.3.

Other monad transformers which do actually use the `'a` also do not instantiate them immediatly. The programmer can decide for which type the monads will be created, therefor it is left open. This effectively creates an interface for the defined monad to be instantiated with a type later specified.

The `return` simply returns the exact same value and `bind` executes the function `k` with `x` as its argument. It is the monad which *passes through* the values.

When using the `id` monad transformer with another transformer, it becomes that monad.

As an example we pass the `id` monad to the maybe monad transformer. When the return of the created maybe monad is called, it first calls the return of the inner monad. In this case is the `id` monad.

The return of the `id` monad returns the value directly as a result. This result is then passed back to the maybe monad, where it gets wrapped inside the maybe monad and returned.

In this way the `id` monad will always end the cycle.

6.6.2 List

The list monad uses a list to store the values.

The list monad transformer uses `List` from *prelude* to create the transformer.

First we have to declare and define the signature.

```
TypeAlias "ListT" => (Type => Type) => Type =>
    ↪ Type
ListT 'M 'a => 'M(List 'a)
```

Using `ListT` together with the signature of `'M` we create the `list` monad.

```
TypeFunc "list" => Monad => Monad
list 'M => Monad(ListT MCons^'M) {
```

`ListT` also takes a `'a`, which is the type for the list created. As stated in section 6.6.1 the programmer has to decide which type the list monad uses.

The `return` simply puts the value in a one-element list wrapped inside a monad.

```
  return x -> return^'M(x :: empty)
```

The bind looks a bit more complicated. It uses the `ArrowFunc` syntax together with a match.

```
  {lm >>= l
    (match l with
```

The match checks whether the list is empty.

```
      (\empty -> return^'M empty)
```

When a list is present the first element of the list gets unpacked by the bind of `'M`, which gets named `y`. The function `k` gets executed with `y` as its argument and the result gets repacked by the return.

```
      (\(x :: xs) ->
        {x >>=^'M y
          return^'M k y} -> z
```

Now the rest of the list, `xs`, gets passed to the bind of `list` so the entire list gets passed to `k`. The results of processing `x` and `xs` are then concatenated into a single list.

```
        xs >>= k -> zs
        (z @ zs))} -> res
  -------------------------------
  lm >>= k -> res
}
```

All the nested functions are closed with the proper brackets and the resulting list is returned as the result of the bind.

If the use of the different syntaxes of the `ArrowFunc` seems confusing, take extra look at section 4.3.16.

Evolution of list

DO THIS!!!!!!!!

6.6.3 Either

The either monad is an implementation of the `TryableMonad` module.

It creates a monad which can be either a value or a list of error messages. The type signature is as follows:

```
TypeAlias "EitherT" => (Type => Type) => Type
    ↪ => Type => Type
EitherT 'M 'e 'a => 'M('a | 'e)
```

It uses the pipe to be able to be either failed or a value. In the definition of `either`, `'e` will be specified as a list.

The `TryableMonad` is then called with the signature of the monadic argument.

```
TypeFunc "either" => Monad => Type =>
    ↪ TryableMonad
either 'M 'e => TryableMonad(EitherT MCons^'M (
    ↪ List 'e)) {
```

The `'a` is again not used, like the id monad in section 6.6.1.

Next we have is the `fail` function. It takes an error message and concatenates it with the existing error messsages.

```
  Func "fail" -> 'e -> MCons^'M
  fail e -> return^'M(Right (Right^'M :: e))
```

The `fail` is needed when we call the `try`. It will provide the error function to the `try`.

Because `either` is a `TryableMonad` it can contain a value or an error message. When calling the bind of `either` this needs to be checked.

That is why the bind calls `try`.

```
  pm >>= k -> try pm k fail
```

The monad and the function is passed on to `try` together with the function `fail`.

The `return` passes the value to `'M`. `Left` is used because `x` is a value.

```
  return x -> return^'M(Left x)
```

maybe put a sort of conclusion here The `either` can now be

Evolution of either

DO THIS!!!!!!!!! Was first implemented without tyable monad

6.6.4 Option

explain that it is obsolete because of either CAN THIS BE LEFT OUT?????????? probably yes

```
TypeFunc "Option" => Type => Type
Option 'a => Unit | 'a

Func "Some" -> 'a -> Option 'a
Some x -> Right x

Func "None" -> Option 'a
None -> Left Unit

TypeFunc "option" => TryableMonad
option => either Option None {
  return
}
```

Evolution of option

6.6.5 Result

The result monad is complete implementation of the either monad from section 6.6.3.

The `either` monad still needs an error type and a type for the values it takes. The result monad specifies the error type, leaving the type of the value for the programmer to specify.

Because all the functions in `either` are defined, result can directly call `either` with an error type. No further function declarations or definitions are needed.

In the declaration we specify it returns a `TryableMonad`, which `either` is. And in the definition we specify the error type to be `String`.

```
TypeFunc "result" => Monad => TryableMonad
result 'M => either MCons^'M (List String)
```

This creates an `either` with `String` as error type.

Evolution of result

god knows what to put here.

6.6.6 State

We have had a basic explanation of the state monad in section 6.4.

Now we will see how it is implemented. The type signature of the state monad shows that it is a function.

```
TypeAlias "StateT" => (Type => Type) => Type =>
    ↪  Type => Type
StateT 'M 's 'a => ('s -> 'M('a * 's))
```

It takes a state and returns a monad containing a tuple af the resulting value and the new state.

We use `StateT` in the call to `Monad` so it knows what the type signature will be.

```
TypeFunc "state" => Monad => Type => Monad
state 'M 's => Monad(StateT MCons^'M 's) {
```

When looking at the return we see something new. A lambda is created to match the type signature of the state monad.

```
  return x -> (\ s -> return^'M(x,s))
```

The x is set as the result of the state.

We see this happening also in the bind. A lambda is created and in the function body of the lambda the computation happens.

```
  (\ s ->
    {sm s >>=^'M x
      x -> (x',s')
      k x' s'}) -> res
  ---------------------
  sm >>= k -> res
```

The bind of `'M` is called and the result is then deconstructed to get to the tuple which it contains. We know `x` is a tuple because it lives inside a state monad. As is evident by the type signature of the state monad.

The state monad also contains two extra functions. They make it possible to get and set the state.

To get the state we call `getState`.

```
  Func "getState" -> MCons 's
  getState -> (\ s -> return^'M(s,s))
```

It sets the state as the result in the return lambda. By which you will get the state back when it is entered into the lambda.

To set the state we call `setState`.

```
  Func "setState" -> 's -> MCons Unit
  setState s -> (\ unit -> return^'M(unit,s))
}
```

It sets the result to unit and the state to the input state.

Evolution of state

6.6.7 IO

Evolution

Chapter 7

Test programs

There have been two test programs written to test the language.

The first of these is a simple bouncing ball.

7.1 Bouncing ball

Bouncing ball is used as a preliminary test of the updatable records. It will show how the updatable records are used in practice.

This program bounces a ball up and down.

The ball will have two properties, velocity and position, which will implemented as records. Both of these will then be put inside the updatable record of the ball.

The update function will then add implement how the ball bounces.

First we import prelude, record and the XNA framework The Microsoft XNA library will be used for the `Vector2` it has and the Thread library will be used to call the `Sleep` function.

```
import Microsoft^Xna^Framework
import System^Threading^Thread
import record
import prelude
```

The record of the ball will be build bottom-up. This is done because every record needs to have a `rest` as an argument.

`Velocity` is created first, because it needs to be updated less. It keeps deep searches of the record to a minimum.

```
RecordEntry "Velocity" Vector2(0.0f, 98.1f)
    ↪ Empty
```

Then `Position` will be created with `Velocity` as its `rest` argument.

```
RecordEntry "Position" Vector2(100.0f, 0.0f)
    ↪ Velocity
```

Lastly we create the updatable record `Ball`. This is done in one line by creating a record entry and passing it directly as argument to `updatableRecord`. `Position` is used as `rest` argument to complete the record.

```
updatableRecord (RecordEntry "Ball" unit
    ↪ Position) => Ball {
```

We then need to define the `update` function.

The `Position` and `Velocit` records are put in a variable, so we can use them directly.

```
  get^e "Position" Rest^e => position
  get^e "Velocity" Rest^e => velocity
```

```
  (if ((Field^position).Y <= 500.0f) then
    ((set^e "Position"
           (Field^position +^Vector2 (Field^
    ↪ velocity *^Vector2 dt))
          Rest^position)
     (set^e "Velocity"
            (Field^velocity +^Vector2 (Vector2
    ↪ (0.0f, 98.1f) *^Vector2 dt))
           Rest^velocity))
  else
    (set^e "Position"
           Vector2((Field^position).X, 500.0f)
           -^Vector2(Field^velocity))) -> res
  ------------------------------------------
  update e dt -> res
}
```

The final step is to create the `run` function to start the program. It will call the update function of `Ball`, sleep for a set amount of time and then call itself.

```
Func "run" -> Record -> String

update^ball ball time -> ball'
Sleep(1000)
run ball' (time +^Int 1000) -> res
---------------
run ball time -> res
```

This creates an infinite loop, so the ball will keep on bouncing.

The return will never be set as it will keep calling itself until the program stops.

7.2 Tron

Tron is a more advanced program which will utilise user input. The game tron [] has been chosen because of the minimalistic graphics. This allows us to focus on the internal workings of the game.

7.2.1 Bike

```
import Framework^Xna^Microsoft
import Input^Windows^System
import entity^Casanova
import prelude

TypeFunc "PositionEntity" => String => Vector2
    ↪ => EntityField => EntityField
```

```
Entity label pos rest => e
--------------------------
PositionEntity label pos rest =>
    ↪ UpdatableEntity e{
  dts -> (dt,speed)
  Field^p +^Vector2 dt *^Vector2 speed ->
    ↪ newPos
  Entity label^p newPos Rest^p -> res
  ----------------------------------
  update p dts -> res
}

TypeFunc "PositionRule" => Rule
PositionRule => (Rule PositionEntity){
  update^e dt -> res
  ------------------
  apply e dt -> res
}

TypeFunc "TrailEntity" => String => Vector2 =>
    ↪ EntityField => EntityField
Entity label field rest => e
----------------------------
TrailEntity label field rest => UpdatableEntity
    ↪  e{
  Entity label^t pos fields^t => res
  ----------------------------------
  update t pos => res
}

TypeFunc "TrailRule" => Rule
TrailRule => (Rule TrailEntity){
  update^e dt -> res
  ------------------
  apply e dt -> res
}

TypeFunc "Keys" => Key => Key => Key => Key =>
    ↪ EntityField
Entity "Left" left Empty
Entity "Right" right Left
Entity "Up" up Right
Entity "Down" down Up => res
----------------------------
Keys left right up down => res
```

```
TypeFunc "Bike" => String => Int => Keys =>
    ↪ Vector2 => TrialEntity => EntityField =>
    ↪  EntityField
Entity "Colour" rgb Empty
Entity "IsAlive" True^builtin Colour
Entity "Controls" keys IsAlive
Entity "Speed" speed Controls
PositionEntity "Position" position Speed
Entity "Trail" trail Position => field
Entity label field rest => e
---------------------------------------
Bike label rgb keys speed position trail rest
    ↪ => UpdatableEntity e{
  $$ check if alive
  (if Field^IsAlive then
    get^b "Trial" Field^b => trial
    get^trail "Position" Rest^trail => position
    $$ update trail
    apply^TrialRule Field^trial Field^position
    ↪ => newTrailEntity
    $$ update position
    get^position "Speed" Rest^position => speed
    apply^PositionRule position (dt,Field^speed
    ↪ ) -> newPos
    Entity label^trial newTrialEntity newPos =>
    ↪  newTrial
    Entity Label^b newTrail Rest^b
  else
    b) -> res
  ------------------------------------
  update b dt -> res
}

TypeFunc "BikeRule" => Rule
BikeRule => (Rule BikeEntity){
  update^e dt -> res
  ------------------
  apply e dt -> res
}
```

7.2.2 Playfield

```
import Framework^Xna^Microsoft
import entity^Casanova
import prelude
```

```
import bike


TypeFunc "BikeEntity" => String => EntityField
    ↪ => EntityField => EntityField
BikeEntity label bikes rest => Entity label
    ↪ bikes rest{

  Func "updateIsAliveAll" -> EntityField ->
    ↪ Vector2 -> EntityField
  Func "updateIsAliveAll" -> EntityField ->
    ↪ Vector2 -> EntityField
  Field^bs -> bikeEntities
  updateBikes bikeEntities dt ->
    ↪ newBikeEntities
  set^bs label^bs newBikeEntities bs -> res
  ------
  updateIsAlive bs fieldsize -> updatedBikes

  Func "updateBikes" -> EntityField -> Float ->
    ↪  EntityField
  update^b b dt
  updateBikes Rest^b dt
  ---------------------
  updateBikes b dt -> res

  updateBikes Empty dt -> Empty

  Field^bs -> bikeEntities
  updateBikes bikeEntities dt ->
    ↪ newBikeEntities
  set^bs label^bs newBikeEntities bs -> res
  ----------------------------------------
  update bs dt -> res
}

TypeFunc "Playfield" => String => EntityField
    ↪ => Vector2 => EntityField => EntityField
Entity "Winner" Unit Empty
BikeEntity (label + "bikes") bikes Winner
Entity "FieldSize" size BikeEntity
-> field
-----------
Playfield label bikes size rest => Entity label
    ↪  field rest{
```

```
Func "checkBikeCollisions" -> EntityField ->
  ↪ EntityField -> EntityField

-> newBikes
------
checkBikeCollisions b bs -> newBikes

Func "checkFieldCollisions" -> Playfield ->
  ↪ EntityField -> EntityField
get "Position" b -> bikePosition
get "FieldSize" p -> playfieldSize
(if ((X.bikePosition > X.playfieldSize) ||^
  ↪ System
     (X.bikePosition < 0.0) ||^System
     (Y.bikePosition > Y.playfieldSize) ||^
  ↪ System
     (Y.bikePosition < 0.0))then
  set^b "IsAlive" False^builtin b
else
  b) -> newBike
--------
checkFieldCollisions p b -> newBike

Func "checkCollisions" -> Playfield ->
  ↪ EntityField -> Playfield
checkFieldCollisions p b -> newBike
(if (Rest^newBike = Empty) then
  set^p
else
  checkBikeCollisions b Rest^b -> newNewBike
  checkCollisions p Rest^b
  ) -> newPlayfield
------
checkCollisions p b -> newPlayfield

Func "checkDeaths" -> Playfield -> Playfield

checkDeaths p -> newP



get^p (Label^p + "bikes") Field^p -> bikes
update^bikes bikes dt -> newBikes
set^p (Label^p + "bikes") newBikes Fields^p
  ↪ -> newPlayfield
checkDeaths newPlayfield ->
--------
  update p dt -> res
}
```

7.2.3 Powerups

```
Func "dottedLine" -> Bike -> Bike
Func "ghostMode" -> Bike -> Bike
Func "thickerLine" -> Bike -> Bike
```

Part IV

Results

Chapter 8

Conclusion

To summerize the main research question was: *How can the programming language MetaCasanova be improved from its current state within the timeframe of the internship?*

The answer to this research question is: *MetaCasanova can be improved by bringing in someone with a fresh view on the language. This person will be taught the basics of the language and use it to build test programs. He or she will also extend the standard library with what is needed for these programs to work.*

Chapter 9

Recommendations

These recommendations are for people who continue with the project.

9.1 Improving a programming language

When first learning about a language, keep on asking until you have specifics. Most of the developers have general ideas of a language. These ideas have very little specifics, but will come to the surface when really digging.

By having these ideas before hand, bugs will become apparent when first looking at the actual language.

9.2 Further development

When developing MC further I would recommend to expand the standard library even more. Especially when the focus of the language is put more on monads.

9.2.1 Monads

First we would need a proper IO monad for interacting with the unpure functions and get real output.

Coroutines would be next. Both as a separate entity and as a monad. They would give the ability of multi threading directly in the language. This would improve performance.

9.2.2 The compiler

I would also recommend to keep syntax changes to a minimum. This will give the compiler developers a fighting chance. During the development the compiler developers have thrown away alot of work, because the syntax became too different.

When creating a new itteration of the language, first get a clear picture of the language before starting work on the compiler. This creates less work for the compiler developers as they do not have to change the compiler mid build.

Chapter 10

Evaluation

Here I will provide proof of having the competentions which are associated with computer science according to the university of Rotterdam [].

10.1 multi discipliniar

kunnen werken in ... team en zelfstandig hun taken uitvoeren.

10.2 klant en probleem gericht opereren

10.3 methodical

10.4 openstaan voor technologische ontwikkelingen in die eigen kunnen maken

10.5 able to reflect and adapt on their beroepsmatig handelen

Here I will provide proof of having mastered the dublin descriptors and the extra competentions as set in the graduation module guidelines [].

10.6 Dublin descriptors

10.6.1 Knowledge and understanding

During the project I have used type-theory as described in [] to check the programs I was writing. This can be explicitly seen in section 6.5 and appendix A.

Further more I have learned the monadic theory to be able to implement them in the standard library.

Both of these build on the knowledge gained during my four years of studying at the University of Rotterdam. Here I have learned the basis which was needed during this project.

The programming skills learned were needed to expand these skills with the type theory. The mathematical skills gained were needed when learning about the monadic constructs.

10.6.2 Applying knowledge and understanding

The knowledge gained in the research phase of this project combined with the knowledge gained in my study years, have been put into practical use. When building upon MC I had to use all the type theory knowledge gained to be certain no function failed.

When implementing the monadic part of the standard library, I have combined the programming- with the mathematical skills to translate mathematical ideas into a practical code base.

10.6.3 Making judgements

At the start of this project I have done research into a new language, MC, type theory and monadic mathematical concepts. These were all needed to build upon the existing codebase of MC.

DO CITATIONS I have made descisions while keeping both the practical aspects and goals in mind, as seen in sections **??**,**??** and **??**.

10.6.4 Communication

During this project I have worked in a research team where I have had to explain myself to fellow team members and supervisors.

This was done in the form of presentations, discussions and meetings. I also had to understand their ideas about concepts.

10.6.5 Lifelong learning skills

10.7 Extra competentions

18-03-2016.

Chapter 11

Bibliography

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Part V

Appendices

Appendix A

Typeproofs

This contains the type proof of the `try` function of the `TryableMonad`, as described in section 6.5.

$$
\begin{aligned}
&Mcons_{\alpha} && : M\alpha \\
&Mcons^{st}_{\alpha} && : (\sigma \to \alpha\sigma) \\
&Mcons^{res}_{\alpha} && : (\alpha|\epsilon) \\
&Mcons^{prs}_{\alpha} && : (\sigma \to (\sigma \to (\alpha|\epsilon) \times \sigma) \times \sigma)
\end{aligned}
$$

$$try^{prs}\ k\ err\ pm = lift^{st}(lift^{st}(try^{res}k(\lambda e_1.try^{res}(>>=)^{id}(\lambda e_2.fail^{prs}(e_1+e_2)))err))pm : (\alpha \to M\beta) \to (\epsilon \to M\beta) \to Mcons^{prs}_{\alpha} \to Mcons^{prs}_{\beta}$$

$$\dfrac{\dfrac{\dfrac{try^{res} : (\alpha \to M\beta) \to (\epsilon \to M\beta) \to Mcons^{res}_{\alpha} \to Mcons^{res}_{\beta} \qquad (>>=)^{id} : (\alpha \to M\beta)}{try^{res}(>>=)^{id} : (\epsilon \to M\beta) \to Mcons^{res}_{\alpha} \to Mcons^{res}_{\beta}} \qquad \dfrac{fail^{prs} : \epsilon \to Mcons^{prs}_{\alpha} \qquad \dfrac{e_1 : \epsilon \qquad e_2 : \epsilon}{e_1 + e_2 : \epsilon}}{fail^{prs}(e_1+e_2) : Mcons^{prs}_{\alpha}}}{\lambda e_2.fail^{prs}(e_1+e_2) : \epsilon \to Mcons^{prs}_{\alpha}}}{try^{res}(>>=)^{id}\ (\lambda e_2.fail^{prs}(e_1+e_2)) : Mcons^{res}_{\alpha} \to Mcons^{res}_{\beta}}}{\lambda e_1.try^{res}(>>=)^{id}\ (\lambda e_2.fail^{prs}(e_1+e_2)) : \epsilon \to Mcons^{res}_{\alpha} \to Mcons^{res}_{\beta}}$$

$$\dfrac{\dfrac{try^{res} : (\alpha \to M\beta) \to (\epsilon \to M\beta) \to Mcons^{res}_{\alpha} \to Mcons^{res}_{\beta} \qquad k : (\alpha \to M\beta)}{try^{res}k : (\epsilon \to M\beta) \to Mcons^{res}_{\alpha} \to Mcons^{res}_{\beta}} \qquad \lambda e_1.try^{res}(>>=)^{id}\ (\lambda e_2.fail^{prs}(e_1+e_2)) : \epsilon \to Mcons^{res}_{\alpha} \to Mcons^{res}_{\beta}}{\textbf{Contradiction:}\ \text{application of } try^{res}\ k \text{ expects } (\epsilon \to M\beta) \text{ but got } (\epsilon \to Mcons^{res}_{\alpha} \to Mcons^{res}_{\beta})}$$

$$try^{prs}\ k\ err\ pm = lift^{st}(lift^{st\_ctxt}(try^{res}k(\lambda e_1.try^{res}return^{id}(\lambda e_2.fail^{prs}(e_1+e_2))err)))pm : (\alpha \to Mcons_\beta^{prs}) \to (\epsilon \to Mcons_\beta^{prs}) \to Mcons_\alpha^{prs} \to Mcons_\beta^{prs}$$

$$\dfrac{\dfrac{\dfrac{\dfrac{try^{res} : (\alpha \to Mcons_\beta^{res}) \to (\epsilon \to Mcons_\beta^{res}) \to Mcons_\alpha^{res} \to Mcons_\beta^{res} \qquad return^{id} : (\alpha \to Mcons_\beta^{res})}{try^{res}return^{id} : (\epsilon \to Mcons_\beta^{res}) \to Mcons_\alpha^{res} \to Mcons_\beta^{res}} \qquad \dfrac{fail^{prs} : \epsilon \to Mcons_\alpha^{prs} \qquad \dfrac{e_1 : \epsilon \qquad e_2 : \epsilon}{e_1 + e_2 : \epsilon}}{fail^{prs}(e_1+e_2) : Mcons_\alpha^{prs}}}{\lambda e_2.fail^{prs}(e_1+e_2) : \epsilon \to Mcons_\alpha^{prs}}}{try^{res}return^{id}\ (\lambda e_2.fail^{prs}(e_1+e_2)) : Mcons_\alpha^{res} \to Mcons_\beta^{res}} \qquad err : Mcons_\alpha^{res}}{try^{res}return^{id}\ (\lambda e_2.fail^{prs}(e_1+e_2))err : Mcons_\beta^{res}}}{\lambda e_1.try^{res}return^{id}\ (\lambda e_2.fail^{prs}(e_1+e_2))err : \epsilon \to Mcons_\beta^{res}}$$

$$\dfrac{\dfrac{try^{res} : (\alpha \to Mcons_\beta^{res}) \to (\epsilon \to Mcons_\beta^{res}) \to Mcons_\alpha^{res} \to Mcons_\beta^{res} \qquad k : (\alpha \to Mcons_\beta^{prs})}{try^{res}k : (\epsilon \to Mcons_\beta^{res}) \to Mcons_\alpha^{res} \to Mcons_\beta^{res}} \qquad \lambda e_1.try^{res}return^{id}\ (\lambda e_2.fail^{prs}(e_1+e_2))err : \epsilon \to Mcons_\beta^{res}}{try^{res}k\ (\lambda e_1.try^{res}return^{id}\ (\lambda e_2.fail^{prs}(e_1+e_2))err) : Mcons_\alpha^{res} \to Mcons_\beta^{res}}$$

$$\dfrac{\dfrac{lift^{st} : (\alpha \to \beta) \to Mcons_\alpha^{st} \to Mcons_\beta^{st\_ctxt} \qquad \dfrac{lift^{st\_ctxt} : (\alpha \to \beta) \to Mcons_\alpha^{st\_ctxt} \to Mcons_\beta^{res} \qquad try^{res}k\ (\lambda e_1.try^{res}return^{id}\ (\lambda e_2.fail^{prs}(e_1+e_2))\ err) : Mcons_\beta^{res}}{lift^{st\_ctxt}(try^{res}k\ (\lambda e_1.try^{res}return^{id}\ (\lambda e_2.fail^{prs}(e_1+e_2))\ err)\ pm) : Mcons_\beta^{res}}}{lift^{st}(lift^{st\_ctxt}(try^{res}k\ (\lambda e_1.try^{res}return^{id}\ (\lambda e_2.fail^{prs}(e_1+e_2))\ err)))\ pm : Mcons_\beta^{res}}$$

Appendix B

Monads in Python

B.1 State

Appendix C

Monads in ...

C.1 State