# Debugging and expanding MetaCasanova

Bachelor Thesis

Rotterdam, 2016

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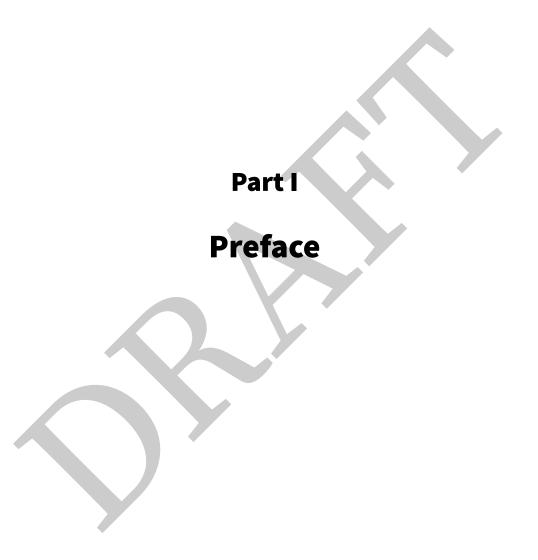
## **Abstract**

This document describes the new programming language MetaCasanova and its improvements.

The author was part of the research group which was developping MetaCasanova.

This document is the thesis that was issued by the Rotterdam University of Applied Sciences, as a test of skill and knowledge gained after four years of education at their Computer Science department. The goal of this document is to demonstrate the skill of the student, the author of this document.

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# Introduction

# 1.0.1 Company

The graduation assignment is be carried out at Kenniscentrum Creating 010. The company is located in Rotterdam. Kenniscentrum Creating 010 is a transdisciplinary design-inclusive Research Center enabling citizens, students and creative industry mak- created to debug and expand the language. *ing the future of Rotterdam*[1].

The assignment is carried out within a research group, who is building a new programming language. The new programming language is called Casanova.

# The assignment

#### **1.1.1** Motive

MetaCasanova (from now on called MC) comes forth from the language Casanova, hence the name.

Casanova is a language made for building games. It uses higher order types to make the programming of complex constructs easier. These constucts are often used in game development. A few of these constructs will be explained in detail from chapter 5 onward.

Because of the higher order types the compiler for Casanova became complex. The compiler for Casanova worked, but was still in development. So when a bug was found in the compiler, fixing it was becoming more and more time consuming. This frustrated the developers so much a new language was created.

MC was this new language. MC serves as the language in which the compiler for Casanova will be written.

At the beginning of the assignment MC was still in development. The syntax was nearly complete, but untested, and the standard library of MC was just beginning to take shape. The assignment was

# 1.1.2 Research guestion

As stated the main goal of the assignment is to debug and expand the language. Which translates to the following research question:

How can the programming language Meta-Casanova be improved for the user within the timeframe of the internship?

Where the user is a programmer using the language to create applications.

This research question is quite broad and I have created a few subquestions to define a scope for the assignment.

- 1. What to the user is a good programming language?
- 2. How can the current syntax be improved to serve the user?
- 3. How can the standard library be improved to serve the user?

After we have a clear image of what a good programming language is, we can look at MC. MC can then be checked and improved where necessary.

The definitions and scope of the improvments will become clear after the preliminary research.

#### Correlation with other projects

During the internship the research team keeps developing MC. There are also two other students doing an internship on MC. They are both working on the compiler, one is developing the back-end of the compiler and the other the front-end. The student will cooperate with the research team and both these students.

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# Part II Preliminary research

# A good programming language

For a programming language to be practically usable it needs to be tested on the following criteria[2, 3]:

- 1. Read- & Writability
- 2. Simplicity
- 3. Definiteness
- 4. Predictability
- 5. Expressiveness
- 6. Implementability
- 7. Efficiency

- 8. Libraries
- 9. Time
- 10. Hackability
- 11. Succintness
- 12. Redesign
- 13. External Factors

connect them to MC.

# 2.1 Read- & Writability

The read- and writability of a programming language determines how good the connection between man and machine is. The programmer must be able to write programs he understands easily, even after months or years of not looking at it.

With easy to read and write programs comes also the ease if debugging. As we can quickly notice any faults in the source code.

Documentation makes up a basic part of read-& writability. But to really be able to make a program readable, even after a prolonged absence, the language needs to be it's own documentation. This can be done via a manner of ways:

- Keywords
- · Abbreviations and concise notation
- Comments
- Layout or format of programs
- No overuse of notation

These points will be explained later on with examples off MC in section ??.

# **Simplicity**

The simplicity of a language is decided by it's features. These should be easy to learn and remember. To make this more provable we will make use of these sub points:

- Structure
- Number of features
- Multiple ways of specification
- Multiple ways of expressing

But the main concept through which simplicity Let's touch on each of these briefly, before we is achieved, is through basing the language around a few simple well-defined concepts. [2]

# **Definiteness**

The definitness clarifies for which purpose the language is designed and how it is to be used. When a language has a clear view and definition of itself, it will also be clear to the user for what purposes to use tho language.

# **Predictability**

The predictability makes use of the language easy for the user. When one user programs the same as another user, the result should be the same. This implies that if the user understands the basics of the language, he can then expand beyond them by combining these basics.

However, the rules of the language should not hinder the user by making the available combinations too complex.

# **Expressiveness**

The expressiveness goes hand in hand with abstraction. The language should be able to show the user the program in a way that matches with his thoughts.

Machine language is hard to understand and use for a human, it has nearly no abstraction and the programmer has te keep track of the registerers by hand. This can however be remedied by the language the user is using. It is the link between what the user has in his mind and what the machine will execute. Therefor the language should be similar to the way the user thinks. This makes it easier for the user to express his thoughts in code.

# Efficiency

Efficiency is something most users want out of their computer. Programmers like to write fast programs. The language should facilitate this. Even if the language is very abstract, which usually means it is less efficient[3], it should be able to generate fast code, or making visible to the user where the bottlenecks are.

#### Libraries 2.7

Libraries are a necessity for every programming language. Without them the language would be useless and the programmer would have to build every feature from the ground up. This makes programming in the language take a long time.

#### 2.8 Time

mentum and a stable user base, even programming languages cannot escape this. For now we will not be able to really test this, as MC is still in its development stages. For this reason we will leave this out.

# **Hackability**

Hackability is the ability to bend the language to one's will or to form the language to one's needs. In other words how much you can do with the language and how malleable and versatile it is. This also depends on the ability, of the programmer, to think outside the pre-defined box of the language. We will

try to see how well MC supports this type of think-

#### **Succinctness** 2.10

The succinctness makes a language more abstract. When you have to say less to make the computer do precisely what you want, that is something very powerful. It also makes the programs shorter and clearer to read.

#### Redesign 2.11

This enables the evolution of a program written in the language. This makes it easier to go from a rough prototype to a fully featured program.

# 2.12 External Factors and Implementability

Time is something everything needs to build mo- These play a big role in the adaptation of a language. Without some use for the language, it might as well not exist. Having a platform for the language plays a major part in the way it will be adopted as a standard. This does not have to be a physical platform, like UNIX or Windows. It can be a virtual platform, like an already existing major library. The only problem with the latter is, that the new language has to compete with other languages who already implement the library.

> Do keep in mind that most of these criteria can be subjective to the user of the language and are not 100% provable. Thus we will try to discuss the most objective parts for provability's sake.

# MC in detail

We will now look at MC in the state after the project. After we have a basic understanding of MC, we will look at the improvements made.

Because the current version of MC is not documented, the following information comes from interviews with the research team [?].

This document can serve as a basis for anyone interested in learning about MC.

# What is MC

MC stands for MetaCasanova and is a declaritive functional language. It tries to be a completely pure language, which means no side-effects are allowed directly.

## Goal

The goal of MC is to use higher order types with type safety, in a natural way of programming. These higher order types gives the ability to resolve certain it. For this we use the keyword Func.

computations on compile time, which can normally be resolved at run time only. This can substantially increase performance at run time.

It also supports the .NET library natively. Because .NET has mutables [?], MC can have sideeffects through the use of .NET.

MC also aims to be as flexible as possible with the safety of a strong type system.

# Basics

We will now go through the basics of MC. We will look at how the syntax works and use small code samples to explain these workings.

The improvements made to these basics will be given in part III. This will give us a better understanding of why and how MC evolved.

Inside the codeblocks a line wrap is indicated by

# 3.3.1 Terms, types & kinds

With MC you program on three different levels:

- 1. Terms
- 2. Types
- 3. Kinds

Terms are the values of variables, like 5, 'c' or "Hello". Types are the types of variables, like Integer, String or Boolean. Kinds are for types, what types are to terms. You could say the kinds are the types of the types.

## 3.3.2 Func

First we need to declare a function before defining

```
Func "computeNumber" -> Boolean -> Int -> Int
    \hookrightarrow -> Int
```

Here we see that the function *computeNumber* is a function which goes from a Boolean and two Interegers to an Integer.

The parameters are seperated by the ->. The last parameter is the return type of the function and all the parameters between the name and the return type, are the arguments of the function.

A function is defined by one or multiple *rules*. A rule consists of a conclusion and can contain multiple premises. They are separated by the bar. The conclusion is placed underneath the bar and the premises above.

Now let's define a rule for computeNumber.

```
a == True
add b c -> res
computeNumber a b c -> res
```

The conclusion is on the fourth line, the bar on the third and the premise on the first and second. The conclusion has the name of the function and the input arguments on the left of the arrow and the output argument on the right. This syntax is similiar to that of natural deduction [].

## **Locally defined identifiers**

The identifiers named in the conclusion of a function are locally defined. With the function computeNumber the identifiers a, b and c are examples of these local identifiers.

# 3.3.3 Multiple rules

There can also be multiple rules which form function definition.

```
a == True
add b c -> res
------
computeNumber a b c -> res
a == False
mul b c -> res
------
computeNumber a b c -> res
```

When this happens the rules are attempted in order of definition. A rule fails when the arguments do not match. If the above rule fails and the rule beneath it is attempted. If none of the rules match the program crashes.

Let us go through this process with an example. First we will try the following function call, from inside a premise:

```
computeNumber False 5 3 -> newValue
```

The first rule to be attempted is the one written first in the source code, so:

```
a == True
add b c -> res
-----computeNumber a b c -> res
```

This rule will fail, because the first argument has the value False and not True. So this rule will not be executed.

The next rule to be attempted is:

```
a == False
mul b c -> res
-----
computeNumber a b c -> res
```

The first argument is set to False and the second and third are both Integers, so the rule matches. The rule will be executed and the result will be put in newValue.

#### 3.3.4 Constants

Constants can be created by using Func without any parameters. The return type still has to be declared.

```
Func "bar" -> Int bar -> 5
```

Here the constant bar is set to the value 5.

We also see that not every rule has a *bar*. This is possible only when no premise is needed in the rule.

As we have seen Func uses types in its declaration and terms in its definition. The types enables the detection of wrong function calls during compile time.

Important to note is that functions declared by Func are on runtime. As we will see in section 3.3.9, MC also has the ability to declare and define functions that run on compile time.

# 3.3.5 Functions as parameters

Aside from variables, functions can also be given as parameters. This needs to be specified in the declaration of the function.

```
Func "isThisEven" -> ( 'a -> 'b ) -> 'a -> 'd
```

Here we see that the first argument ( 'a - > 'b ) is a function. This is can be seen when we declare the following function:

```
Func "x" -> 'a
```

When we strip away the name of the function and the keyword Func, we are left with just the function.

```
(x -> 'b)
```

We can use this syntax in declarations to indicate a function is used as the argument.

## 3.3.6 Data

With Data we can declare a constructor and deconstructors for a new type. Because it can work two ways it effectively creates an alias.

Say that we want to create a union, a type which can be any of the predefined types within a set []. For this we need a way to construct the union type and a way to deconstructed the union back to its original type. The deconstructor is needed to get know which of the types inside the union is actually used. Only then can we know which of the types inside the union is used.

As an example we will create a union of a String and a Float.

```
Data "Left" -> String -> String | Float
Data "Right" -> Float -> String | Float
```

Here we create two constructors whom both go to the same type, String | Float. Left and Right can be seen as an alias for the String | Float union.

Let us see how this is used. We need a function which takes a union as argument.

```
Func "isFloat" -> ( String | Float ) -> Boolean
```

The parentheses in the declaration can be left out, but are used to clarify that the union is one argument.

In the definition we want to check which type the union is. This can be done directly in the conclusion of a rule.

```
isFloat Float -> True
```

The deconstructor of the argument given, automatically checks if the types match. This can be done because they are aliases. Aliases are automatically resolved to their basic types by the compiler.

Conditionals using aliases can be put in the conclusion. Other conditionals have to be put in the premises, because they need to be computed.<sup>1</sup>

To make the definition of IsFloat complete we also need a rule that checks for String.

```
isFloat String -> False
```

Now we will test the function is Float with the help of constant iAmFloat.

```
Right 9.27 -> iAmFloat
```

iAmFloat has type String | Float and can now be passed to isFloat.

```
isFloat iAmFloat -> output
```

When iAmFloat is deconstructed to its original type it will match with the first rule of isFloat. The identifier output now contains the value True.

# **Runtime and compile time**

So far we have seen the -> arrow, which indicates a type is used. function is executed on runtime.

To indicate a function is resolved or inlined on **Infix parameters** compile time, the => arrow is used.

Types are also resolved or inlined, except when they create datastructures. These data structures keep existing on runtime. Kinds are resolved or inlined at compile time.

We will see this starting from the next section onwards.

# 3.3.8 TypeAlias

Because the | (pipe) operator<sup>2</sup> is not built in the language we need to create it. To do this we need to manipulate types.

We have already seen that TypeFunc can do this.<sup>3</sup> But to make | work, we now need a constructor and deconstructor that works with kinds.

TypeAlias is the same as Data only on a higher level of abstraction. It constructs and deconstructs kinds.

With TypeAlias we can create a generic with which we can create unions. Unlike Data, TypeAlias needs both a declaration and a definition. The declaration shows what happens on kind level and the definition shows what happens on type level.

Here we see how the generic | is declared. It takes two paramaters of any type and returns a type.

The Type is a kind and indicates an unknown

As shown parameters can be infix.

There is a limitation to the use left arguments, there may only be one. This is because of the parser used. The parser would become overly complex when adding multiple arguments on the left.

Because the benefits of having multiple arguments in front of the function name do not outway the time it consumes to expand the parser, the choice was made to only allow one argument in front.

When defining | we want to use generic types. This way a union can be created from all types.

## **Generic type identifiers**

To indicate generic types the 'notation is used.

This is enhanced with the use of identifiers after '. These give the generic type a name and can be used to express if one generic type is the same as another generic type.

We will use this in the definition of 1:

```
'a | 'b => pipe<'a 'b>
```

Now we can say that two different types are used as the arguments and in the created pipe.

# **Type annotiatons**

The angle brackets are used as type annotation for pipe. They indicate that 'a and 'b are part of the type pipe. This is only used with generic types, because it makes it easier for the parser to resolve the types.4

<sup>&</sup>lt;sup>1</sup>As can be seen in section 3.3.2

<sup>&</sup>lt;sup>2</sup>As used in section 3.3.6

<sup>&</sup>lt;sup>3</sup>See section 3.3.9

<sup>&</sup>lt;sup>4</sup>More on this in section 4.3

# 3.3.9 TypeFunc

do computations with both types and terms.

We will demonstrate the power of TypeFunc with a function which manipulates a type. The function will take a tuple and return the same tuple, but tion 3.3.1. with switched types.

First we need to declare a tuple with TypeAlias.

```
TypeAlias Type => "*" => Type => Type
'a * 'b => tuple<'a 'b>
```

Now that we have a tuple we can use it in the function declaration. The tuple argument will have generic types so it can work with any tuple.

```
TypeFunc "switch" => tuple<'a 'b> => tuple<'b '
   → a>
```

Next we have the definition. Here we need to deconstruct the tuple to its original arguments. These arguments can then be used to create the return tuple.

```
a \Rightarrow (c * d)
(d * c) \Rightarrow res
switch a => res
```

Here we can see how the types inside the tuple are switched and returned as a new tuple.

#### **Parameters**

Important to note is that both TypeAlias and TypeFunc can use kinds, types and terms. Because they work on compile time only, they cannot replace Data and Func.

Data and Func exist for explicit runtime functions.

#### 3.3.10 Module

TypeFunc creates a function on type level. It can Module is used to create a container on compile time. It is a collection of function declarations and definitions.

> It does not fit within the levels defined in sec-Modules can only be declared by TypeFunc.

> Say we want to create a container for every type which does an addition of two identifiers of those types. The could be declared when we need them or we can put them in a Module.

> When we create an addition container using a module, we do not have to type out the addition functions for every type. We can just call the module to create the functions for us.

A Module is declared with a TypeFunc.

```
TypeFunc "Add" => Type => Module
```

Here we declare the Add to take a type and return a Module.

We then want to define the module Add with the + operator and the identity Add constant.

```
Add 'a => Module {
  Func 'a -> "+" -> 'a -> 'a
  Func "identityAdd" -> 'a
```

This creates a basic container with generic addition functionality.

As shown it can contain Func, but can also contain Data, TypeFunc, TypeAlias and another Module.

The declarations within the Module do not have to be defined. This way we can define different behavior for every instance of the module.

It is possible to have a function declared and defined within a module.

When we want to define the above declared Add with an integer, we instanciate the module with Int. We then define the functions which are declared within Add to finish the module.

```
MonoidAdd Int = {
 Int -> "+" -> Int -> Int
 identityAdd -> 0
```

The Funcs are defined as they normally are, only now they are wrapped within a Module.

#### The caret

When we want to call a function within a module from outside the module the ^ is used.

```
Func "caretTest" -> Int
caretTest -> identityAdd^Int
```

This creates a constant named caretTest with the same value as the identity Add from the module Int. The 'can be seen as the '.' (the dot) used in C#. The hierarchy used in MC is different from most languages.

Say we have a C# class Int containing the constant identityAdd, the constant is called like this:

```
Int.identitvAdd
```

As seen in the example MC does it the other way around. This has the advantage of knowing immediately what you are using, instead of knowing where it comes from.

#### Inherit

Modules can also inherit from other modules. This is done with inherit.

We will create a module which inherits from the Add module. The operator – will then be added aswell.

```
TypeFunc "GroupAdd" => Type => Module
GroupAdd 'a => Module {
  inherit Add 'a
  Func 'a -> "-" -> 'a -> 'a
}
```

The module  $Add^5$  is instantiated with 'a. The created Add module is then inherited into GroupAdd.

The function declarations and definitions of the inherited module are directly usable within the new module.

If a module takes another module as an argument, the module can also directly inherit.

```
TypeFunc "GroupAdd" => Add => Module
GroupAdd M => Module {
  inherit M
}
```

Now everything from module M is inherited into GroupAdd.

When inheriting a module which contains an inherit, these are also inherited in to the current module. This works recursively.

# 3.3.11 Priority

We can also give a priority together with a declaration. The priority indicitates the order of function execution.

The priority is indicated by the #> and is placed after the declaration. When we look at Data it will look like this:

```
Data "Left" -> String -> String | Float #> 7
Data "Right" -> Float -> String | Float #> 5
```

And with Func and TypeFunc it is used like this:

```
Func "bar" -> Int #> 12
TypeFunc "foo" => Float => 'a => 'b #> 9
```

The #> is also used to indicate associativity. Everything is left associative by default, but if we want to make it right associative we can do that by placing an R after the #>.

```
Func Int -> "\" -> Int -> Int #> R
```

The priority and associativity can also be used in combination with each other.

```
Func Int -> "\" -> Int -> Int #> 25 R
```

## 3.3.12 **Import**

Import is used when importing other files in the current file.

If the file imported has any imports, they are ignored. Unlike inherit, import is not recursive.

The programmer can directly use the declarations and definitions used in the imported file. When the programmer wants to explicitly specify to use a function from the imported file the ^ is used.

We will import the file "vector" and use the Vector2 type from it.

```
import vector
Func "location" -> Vector2
location -> createVector2^vector 8.9 19.0
```

The importing of MC files always works with non capitalized import statements, even when the actual files does contains capitals. This is done to differentiate between MC imports and .NET imports.

The order of elments is the same as with modules, only when using .NET imports there is a difference in syntax. When calling a .NET function the elements are in the same order as with .NET, instead of doing it the other way around when using the ^ with modules.

```
import System
Func "dotNetTest" -> String
dotNetTest -> DateTime^Now^ToString()
```

Here dotNetTest becomes a String which contains the current date and time.

In keeping constistency with the .NET way of calling, the programmer does not have to reverse the order of the elements in the call. This might seem like a trivial thing to do, but from experiments we concluded that it confused the programmer more than initially thought. For this reason the order of elements in a .NET call will stay in synchonicity with the .NET standard.

#### 3.3.13 **Builtin**

Some things cannot be created out of nothing and need to be built in the compiler. An example of this is boolean.

When using such a builtin literal the keyword builtin is used. We can now correctly implement the function foo<sup>6</sup> using the builtin keyword:

```
add b c -> res
```

<sup>&</sup>lt;sup>5</sup>As used in section 3.3.10

<sup>&</sup>lt;sup>6</sup>As used in section 3.3.2

```
foo True^builtin b c -> res
mul b c -> res
------
foo False^builtin b c -> res
```

It can be seen as if they are imported

#### 3.3.14 Comments

#### 3.3.15 Lambdas

MC also has a fully implemented lambdas.

The basic syntax is as one would expect of a lambda, it has arguments and returns what the functionBody returns

```
(\ arguments -> functionBody )
```

In practice this would look like:

```
(\ a \rightarrow divide^Int 10 a )
```

Lambdas do not need to be declared because they always are generic functions. The typechecker will check the lambdas the same way as any other generic function. From the context of what the function body does together with the types of the arguments, it can deduce what the output type should be.

## 3.3.16 ArrowFunc

ArrowFunc always needs an argument on the left of the name and atleast one function to the right. A neatly.

unique feature of ArrowFunc is the two syntax options it has when the function gets called.

The first is like a normal function and the second converts it to a lambda.

As with Func it needs a declaration and a definition.

Here :~> takes an integer and a function that takes an integer and returns an integer.

The declaration and definition are the same as the rest of MC.

When we call :~>, there is the normal way:

```
a :~> f -> res
```

And there is the second way of calling:

```
{a :~> out f out} -> res
```

The brackets are used to indicate everything inside it belongs together. When an ArrowFunc is called like this it gets converted to a lambda. The first argument is then used a the argument for that lambda.

```
(\ out -> f out ) a -> res
```

The result from this is then returned as the output in res.

This syntax exists for when the nesting of lambdas occur. Lambdas become unreadable when nested.

```
(\ b -> (\ c -> f c ) b ) a -> res
```

When using the ArrowFunc syntax it nests neatly.

```
{a :~> b
{b :~> c
f c}} -> res
```

This syntax stems from the use of the bind of monads, which will be explained in further detail in section 5.4.

# 3.3.17 Partial application

Lastly MC supports partial application. This means that you do not have to give all the arguments to a function. When this is done a closure is created and given as output.

We will create a closure with the function add. add takes two Integers and returns an Integer.

In the definition we will say the two arguments will be added together.

```
Func "add" -> Int -> Int -> Int

a + b -> res
-----add a b -> res
```

Now we will give only one argument to add and create a new function addThree.

```
add 3 -> addThree
```

With this construct we have created the partially applied function addThree. When we look what it contains we see that it has a closure with a partly implemented add.

```
3 + b -> res
-----add 3 b -> res
```

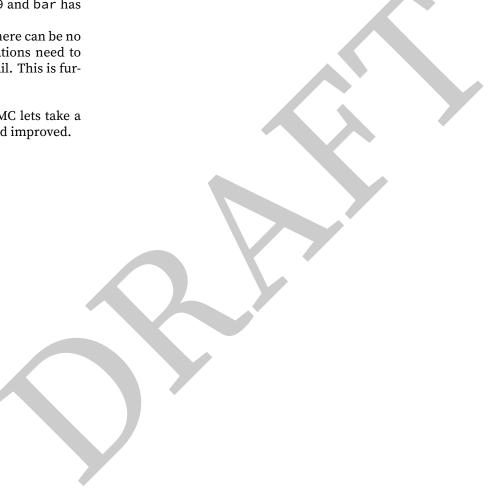
We can now give addThree its second argument to complete the closure. This can be done multiple times.

addThree 6 -> foo addThree 7 -> bar

The identifier foo has a value of 9 and bar has a value of 10.

When type annotations are used there can be no partial application. The type annotations need to know what types it gets or they will fail. This is further explained in section .

Now that we know the basics of MC lets take a look at how the syntax has evolved and improved.





# **Syntax evolution**

Here we will look into the overal syntax changes of the language. The changes concerning the standard library, will be discussed in chapter 5.

# 4.1 Generic type identifiers

As described in section 3.3.8 generic type identifiers are indicated by ' together with a name, 'a. The ' is derived from the *prime* notation, which indicates a derivative of the original [?].

For example when we have identifier i, this identifier might get changed and is then indicated by i'. This shows that i' is derived from i.

Instead of placing the *prime* at the end, it is placed before the identifier name to indicate it is a generic type.

This improved the readability of the language. It is now clear to the user when generic types are the same of different from each other.

# 4.2 Generic kind identifiers

Generic kind identifiers are currently unused, but it was thought to be necessary after the implementation of TypeAlias.

When working with kinds they are always generic, as they indicate an unknown type. That was why they were indicated by an *asteriks*, \*.

When TypeAlias was created it became apparent that the type would be the same in some cases. This resulted in generic kind identifiers.

The notation devised was similar to the generic type identifiers. Instead of the *prime* the *hash* was used.

Here we can see that the first and third arguments are of the same kind and the second argument and the return value are different kinds.

However this was an error in reasoning.

The fact that they are kinds means that they can be any type. The official notation used for kinds is either Type or  $\star$ .

The syntax of kinds was changed to Type. This way the the  $\star$  was free to be used for other things, like the tuple in section 3.3.9.

This also improved the readability of the language. It is now clear when a kind is used.

Because of the use of Type it is also instanly clear what a kind is. This reduces the complexity of the language.

# 4.3 Type annotations

Generic type annotations were created during development to lower the complexity of the parser.

We use a data declaration which creates an array. It takes a generic type and a Integer.

Using the notation without type annotations it looks like this:

```
Data "array" -> 'a -> Int -> Array
```

The Integer sets the lenght and the generic type will be the type the array consists of.

When this is called we can use parentheses to indicate which arguments are grouped together.

```
array(Int 12) -> arrayOfInts
```

The Integer array is created with twelve elements.

But when we use a variable which contains the type, there is confusion what really happens.

```
array(var 12) -> arrayOfInts
```

This could imply that var is a function which uses 12 as its argument and returns a type. arrayOfInts is then a closure which still needs an argument which tells the length of the array.

We can only be sure what happens if we look at the declaration of var.

To avoid this and clarify what happens the type annotations were created. They are used in the data declaration, to specify the types used.

```
Data "array" -> 'a -> Int -> Array<'a Int>
```

Types using the type annotations cannot be partial applied, because they need to know the types they contain to be declared correctly.

When this is not done a compile time error is generated.

So now when we call array we know that var must be a type. When var is declared as a function which returns a type, we will have to call array like this:

```
TypeFunc "var" => Int => Type
nr == 12
------var nr -> Int
array((var 12) 9) -> arrayOfInts
```

This also lowers the complexity of the parser. With the use of type annotations, the parser does not have to look at var and what it is.

The use of the type annotations provides greater predictability to the language. It is now always clear what happens when working with generic types.

# 4.4 TypeAlias

Before there was TypeAlias, TypeFunc was used for the same functionality. However TypeFunc cannot deconstruct.

When constructing a new kind with TypeFunc it can not be deconstructed to its original kind.

This error was noticed when updating the monadic part of the standard library, see section 5.4.

Data could not be used as it cannot manipulate types it can only construct and deconstruct them. That is why TypeAlias was created. It provides contructing and deconstructing functionality with type manipulation.

This adds expessivity and functionality to the language. Which is especially usefull for the user when creating complex programs.

## 4.5 Module

# 4.5.1 Signature

Earlier in development Module was called Signature. It performed the same functionality as Module.

From the language creators perspective Module creates a specific signature on compile time. For the user it looks more like a container or class, when coming from object-oriented programming.

Because the user will be the one actually using the language, the name was changed to what it resembles to the user. It clarifies the syntax and makes it more predictable for the user.

# 4.5.2 Expanding

During the development there were two ways of inheriting a module, via inherit and via expanding an existing module. Expanding modules is removed from MC, because of inconsistency issues.

A Module could be expanded via a function. The function takes a module as argument and expands this module by adding declarations and, optionally, definitions.

```
TypeFunc "expandModule" => Module => Module
expandModule M => M{
   Func "modulo" -> Float -> Float

a % 10 -> res
   -----
modulo a -> res
}
```

The module M is opened up again and modulo is added. Module M is then returned and contains the new function modulo.

This would have been syntactic sugar for creating a new module which inherits from M. In this new module modulo is then added.

```
TypeFunc "expandModule" => Module => Module
expandModule M => Module{
  inherit M

Func "modulo" -> Float -> Float

a % 10 -> res
  ______
modulo a -> res
}
```

The expand syntax makes it look like modules are mutable, which they are not. This makes it inconsistent with the rest of MC and the expand-syntax was removed.

By not using the expanding functionality the language becomes more coherent and in line with itself. This makes the language friendly to the user, because there is no two ways of doing things. It is clear how inherit works and there is no confusion possible.

# 4.6 .NET libraries

When importing and calling .NET libraries the current syntax is using the element order of .NET with ^ as divider.

```
Func "dotNetTest" -> String
dotNetTest -> System^DateTime^Now^ToString()
```

This was not always used. The syntax for .NET imports went through several stages.

The first implementation was the original .NET manner:

```
dotNetTest -> System.DateTime.Now.ToString()
```

This seemed to strange considering the rest of **4.8** the MC syntax. The order of the elements was then switched.

```
dotNetTest -> ToString().Now.DateTime.System
```

This made it more like MC but it was still out op place because of the dot used. It also looked strange when calling a method.

the caret.

```
dotNetTest -> ToString()^Now^DateTime^System
```

This seemed more in sync with the rest of MC. The only problem was with the method calls.

That is how we arrived at the current syntax used. The .NET order of elements is used and the ^ is used as seperator.

The current syntax is the best compromise from a user perspective. It takes the most central elements of both syntaxes and combines them into a clear definite syntax.

# **Builtin**

The keyword builtin was first primitives.

For the developers this was a good choice, as they indicate the primitives that needed to be built in the compiler.

For the user however this seemed confusing. The user sees the primitives as types that are built into the language.

The name was changed to builtin, to better reflect the way how the user sees them.

# **Conditionals**

#### 4.8.1 Inside the conclusion

During development we tried implementing conditionals inside the conclusion of a rule. This could make the code more compact.

We will take the example of Func from sec-In the next itteration the dot was replaced with tion 3.3.2, and implement this. The code is then compacted to this:

```
add b c -> res
computeNumber True b c -> res
```

This is just as easy to read as the original.

It does make the conclusion less conclusive as there is now something happening inside the conclusion. The conclusion is meant to show the input and output of the rule, it is not meant to tell what the function does.

That is where the premises are for.

The compiler also needed to be modified heavily. It now needed to do computations inside the conclusion.

To keep the language and the compiler moducalled lar, a comprise was done. Types created with Data and TypeAlias can be used as conditionals inside the conclusion. This is possible because they act as aliases and need no computation to be checked.

> Conditionals requiring computation, a comparison of values, will be done in the premises.

> This is also syntactically predictable. Especially so because the Data and TypeAlias used in conditionals, are aliases. They could be replaced with that from which they are constructed.

## **4.8.2 Equals**

When comparing values the == operator is used. This is done to keep the the single equals sign free to be used by the programmer.

It is also immediately clear to the programmer a conditional is done. The single = could be mistaken for an alias creation of value assignment. With the double == there is no such confusion.

# **Standard library**

We will now look at the standard library and explain the evolution it went through during the project.

Each item will first be explained with the evolution and improvements afterwards. When we have an idea of how it should work, the choices made during the development will be clearer.

# Prelude

Prelude contains a few definitions making basic programming easier. The .NET System is imported Next we have the match function. It takes a variand the type Unit is created.

```
import System
Data "unit" -> Unit
```

The Unit is used as an empty or null value. Next we have the declaration and definition of a generic tuple and union. Because they are generic TypeAlias is needed for the type manipulation.

```
TypeAlias Type => "*" => Type => Type
'a * 'b => tuple<'a 'b>
Data 'a -> "," -> 'b -> 'a * 'b
```

```
TypeAlias Type => "|" => Type => Type
'a | 'b => pipe<'a 'b>
Data "Left" -> 'a -> 'a | 'b
                                   #> 5
Data "Right" -> 'b -> 'a | 'b
                                   #> 5
```

Then a standard if-else construct is implemented.

```
Data "then" -> Then
Data "else" -> Else
Func "if" -> Boolean^System -> Then ->
   if True^builtin then f else g -> f
if False^builtin then f else g -> g
```

The then and else Datas are syntatic sugar and could be left out. We have left them in to enhance the clarity of the if-else construct.

Here we see how System of .NET is used. The boolean of .NET can be imported as shown, however the values True and False cannot be imported. They are built in .NET itself. This is why these literals are built into MC as well and need to be called using builtin.

## 5.1.1 Match

able, matches it on either Left or Right and executes the function specified.

```
Data "with" -> With
Func "match" -> ('a | 'b) -> With -> ('a -> 'c)
    → -> ('b -> 'c) -> 'c
```

First there some syntactic sugar created to make it clearer how match works. The first argument is the union which needs to get matched. The arguments ('a -> 'c) and ('b -> 'c) are the functions to be executed on a match.

In this case the two functions both take an argument from the union, the 'a and the 'c.

Next we have the definition of match. This gives a definition for both cases of the match, namely the Right and the Left.

```
match (Left x) with f g \rightarrow f x
match (Right y) with f g -> g y
```

When it matches the Left it executes function f with x as its argument. And when it matches the Right it executes function g with y as its argument.

However this does not take into account the possibility of nested pipes. For this we have written a third definition of match:

```
match y with g h -> res
match (Right y) with f (g h) -> res
```

This definition is placed above the previous defined match which matches on Right. Then there is first checked on nested pipes and when there are none the actual value is checked.

In this manner there is no possibility of skipping any nested pipes.

## 5.1.2 List

Then we have a generic list implementation. For this we need to create a list that can work with types.

The list is declared with a union. This is necessarv because we need an end to the list.

#### fix code?

```
TypeAlias "List" => Type => Unit | (Type * (
    → List Type))
List unit => Left unit
List ('a * 'b) => Right ('a * 'b)
```

The list is created with a tuple. An end to the list is created with a union of the list tuple and Unit.

A list is then defined with either a unit or type. We also need the basic operators to create lists.

This is done with ::, which takes a type and a list. And with empty an empty list is created.

#### fix code?

```
TypeAlias Type => "::" => List => List
'a :: 'b => List ('a * 'b)

TypeAlias "empty" => List
empty => List unit
```

With: we can specify the head and tail of a list. But we would also like to concat lists together. This is done with the @ operator.

And when we want to apply a function to the entire list we call map. This executes a function and creates a new list, which it then returns.

```
Func "map" -> List 'a -> ('a -> 'b) -> List 'b map empty f -> empty map (x :: xs) f -> (f x) :: (map xs)
```

When we want to find one or more elements in the list we can call filter. It checks the entire list using a predicate function and returns the matching elements.

The programmer can specify the predicate function p.

# 5.1.3 Evolution of prelude

#### Boolean

Boolean currently does not exist anymore as a separate part of the standard library. Here we will see why this is the case.

Boolean was created to implement boolean logic. After many itterations it was discarded due to the evolution of the language.

When first implementing Boolean it was part of *Prelude*.

```
Data "True" -> Boolean^System
Data "False" -> Boolean^System
```

This might seem correct at first glance, but True and False have no meaning here. There is no way to check if a boolean value is true or false. That is why a new notation had to be created for the boolean literals.

It was turned into a module with the literals as Funcs.

```
import System

TypeFunc "Boolean" => Module
Boolean => Module {
  Func "True" -> Boolean^System
  Func "False" -> Boolean^System
}
```

Which could then be implemented in *prelude*.

```
| boolean => Boolean {
| True -> True^builtin
| False -> False^builtin
|}
```

The boolean literals could now be called using True^boolean. This was noticably the same as what happened inside the implementation of boolean. The choice was then made to call the boolean literals directly with True^builtin, which made the boolean module obsolete.

Which brings us to the current state of the boolean literals.

#### Match

*Match* started as a separate part of the standard library containing the match module. We will now look at how it was first created and how it has evolved into *prelude*.

The first iteration of the match module started with the import of *prelude* and the declaration of match module.

```
import prelude

TypeFunc "match" => Type => Module
```

So far there are no problems yet with us a module for match.

Next we see the first part of implementation of the match module: Some syntactic sugar is created and the actual function is defined which will do the matching.

Now we see why the module is needed. It was thought that the match module would get a separate instance for every match that was executed.

The Head and Tail are the checks to ensure the first function takes the Left as input and the second function takes the Right. As Head gets set to The first list was put together with the list monad. 'a and Tail to 'b.

to check the validity of another function it is better inside the monad. to group them together inside a module.

The definitions of doMatch haven't changed list monad in section 5.6.2. compared to what they are currently.

```
doMatch (Left x) with f g \rightarrow f x
doMatch y with g h -> res
doMatch (Right y) with f (g h) -> res
doMatch (Right y) with f g -> g y
```

It became clear that Head and Tail were not necessary, because they were simply passing on type of the union.

With this removal the use of a module became obsolete, because we do not need to group a single function. The doMatch function was then renamed match and placed inside *prelude*.

#### Recursive match

The first itteration of match could not match nested pipes. It could only detect a direct match. As it only had the direct matches without the function that checks if Right is nested.

The solution could have been left to the programmer. He would have to create a separate match statement for every level of nesting. This would be quite inconvenient for the programmer.

For that reason the recursive functionality was

#### List

This seemed the logical choice at the time, because When seperate functions, like these, are needed the list monad needed a list implementation to use

Monads will be explained in section 5.4 and the

When coming back to the list it became apparent that List was not only useful for the list monad. It could be used without the monad as a regular list implementation.

The choice was then made to move it to *prelude*.

#### Number 5.2

*Number* was created to give the user a generic interface to create numbers.

However because of the import system of MC it can directly import the integer and float types with all their functions from .NET. It can still be used for self defined number types.

Number is built up from different modules to give the programmer the freedom to choose what their custom numbers can do. The modules are aranged according to the mathematical way to built up numerical operators [].

It starts with the MonoidAdd module. It declares the + operator for the custom number.

```
TypeFunc "MonoidAdd" => Type => Module
MonoidAdd 'a => Module {
 Func 'a -> "+" -> 'a -> 'a #> 60
 Func "identityAdd" -> 'a
```

This needs the identity as a base number from which the operations will work.

Next we have the GroupAdd module. This inherits everything from the module MonoidAdd and adds the - operator.

```
TypeFunc "GroupAdd" => Type => Module
GroupAdd 'a => Module {
 inherit MonoidAdd 'a
 Func 'a -> "-" -> 'a -> 'a #> 60
```

We do the same for multiplication and dividing.

```
TypeFunc "MonoidMul" => Type => Module
MonoidMul 'a => Module {
 Func 'a -> "*" -> 'a -> 'a #> 70
 Func "identityMul" -> 'a
TypeFunc "GroupMul" => Type => Module
GroupMul 'a => Module {
 inherit MonoidMul 'a
 Func 'a -> "/" -> 'a -> 'a #> 70
```

Now we have declared the basic number operations of addition, substraction, multiplication and dividing.

We can combine them into a basic number like so:

```
TypeFunc "Number" => Type => Module
Number 'a => Module {
 inherit GroupAdd 'a
 inherit GroupMul 'a
```

Or create a Vector without the dividing operator, because vectors cannot be divided [].

```
TypeFunc "Vector" => Type => Module
Vector 'a => Module {
 inherit GroupAdd 'a
 inherit MonoidMul 'a
```

Ofcourse all the operators still have to be defined, but that is up to the programmer. This gives the programmer the freedom to choose what the operators do.

#### 5.2.1 Evolution of number

During development *number* was used to create integers and floats. This was before the .NET import system was in place and it was thus needed. Currently it is only needed for user defined number types.

The first iteration of *number* was just one module with all the operators declared. This works for the standard number types like Integer and Float.

When using it to create a vector the module will have functions which are never used, because vectors cannot be divided.

For this reason the current *number* design is similiar to the mathematical way. It costs a bit more code to set things up, but there is less overhead.

# 5.3 Record

With *Record* we can create a list of key/value pairs which can be searched and manipulated. The special thing about this record is that is does all the searching on compile time. This makes the runtime code much faster.

When using records in practice we see that not everything can will be known on compile time.

Which makes a record that works on compile time useless.

TypeFunc "set"

Record

(if () == labeless.

The way MC fixes this is to inline the code on compile time. In this way the code that needs to be actually executed can be optimised by the compiler after which it is executed on runtime.

Record is declared as a module and contains \[ \] TypeFuncs to make it work on compile time.

```
TypeFunc "Record" => Module
Record => Module{
   TypeFunc "Label" => String
   TypeFunc "Field" => Type
   TypeFunc "Rest" => Record
```

Here we see a the declarations which are the basis of a list of key/value pairs. Label acts as the key, Field as the value paired with the key and Rest contains the rest of the record.

When there is just one pair in the record we can get that record out easily, we already have it. But when there are multiple record entries in a record we need a function to searches through the record to find the record we want to have. For this the get function was created.

```
TypeFunc "get" => String => Record => Record

(if (l == label^rs) then
    rs
    else
      get l rest^rs) => res
      get l rs => res
```

The get function takes a labels and a record. It checks the label of the record and if it is the same it returns the current record and if not the it recursively calls itself with the rest of the record.

To manupilate these records there the set function was created.

```
}
```

The set function takes a label, a field and a record. The field is the new value that needs to be paired with the label. Because MC does not allow direct manipulation of values the set function returns a new record instead of changing the value of the specified record.

With this the declaration of the record is complete. Now we can look at how the definition of a record works.

First we need to create a record entry. This is done with the RecordEntry TypeFunc.

We also need to create an empty record entry so we can end the record. This is done by the EmptyRecord TypeFunc.

```
TypeFunc "EmptyRecord" => RecordEntry
EmptyRecord => RecordEntry {
  Field => Unit
  Label => Unit
  Rest => Unit
}
```

The programmer has to use EmptyRecord as the rest argument of the first record entry. This creates an end to the record.

# 5.3.1 Updatable record

The current record can only be instantiated and not updated. To expand the record to be updatable we need to add the update function.

First we declare and define a TypeFunc which creates a new record from the original with inherit.

```
TypeFunc "updatableRecord" => Record => Record
updatableRecord r => Module {
  inherit r
```

The new module now contains everything of record r.

The we declare and define the update function.

```
TypeFunc "update" => Record => Type => Record
r == Empty
update r dt => Empty
```

Only the definition of update which checks for an empty record can be defined. It is the only situation in which we can be certain what the return value will be, namely Empty.

If the record is not Empty we cannot know what the programmer wants to do with update. That is why we leave that definition of update up to the programmer.

#### Evolution of record 5.3.2

#### Cons

During the development the idea occured that every Record had to have its own type signature. Because the field can be anything, it was thought to impact the type of the Record.

This would be a problem when trying to declare the use of a specific Record.

would be the type signature of that perticular through the record to get the record we need. This Record.

It would consist of the types of the Label, Field and Rest.

```
TypeFunc "Cons" => Type
Cons => (Label, Field, Rest)
```

The prime example of the need for Cons came when creating the updatableRecord function. It would check if the new Field was the same as the original Field.

It became apparent that every record is of type update. Record and that the type of Field had no impact on the type of the record. Cons was then removed.

This also reduced the complexity of the records for the user. Now the user can use the records without having to keep in mind which type belongs to which record.

# 5.3.3 Apply

Here we will see how apply was thought to be needed and why it is not needed.

When we have a record with alot of nested or complex datastructures that we want to update, we have to go through the entire structure to be able to call the update function. To fix this apply was created.

apply takes a record a record and calls the update function directly, without going through the datastructure of the record.

```
TypeFunc "apply" => Record => Type => Record
update^r dt => res
apply r dt => res
```

Here we can see that all that apply does, is call This resulted in the creation of Cons. Cons the update function. When calling apply we go way we only have to go through the structure of the record once and not everytime the we need to call the update function of a specific record.

We can now call apply to call the update function indirectly, without going to the entire record.

When implementing this we discovered we needed more than one apply function. This can only be done by creating seperate functions which call the apply. But this would negate apply, as these functions could also directly call the specific

We then put apply inside a module called Rule. Rule could then be called when declaring an apply for a record.

This seemed like the wrong direction to go. There was only one function inside the module of Rule, which makes having a module redundant. The complexity and performance was also impacted by the use of a module instead of directly calling the update function.

It was decided that the Rule module would be disregarded. The problem of not being able to create multiple apply functions is fixed by removing apply all together.

The programmer can create functions like apply fi he feels the need to. The programmer can then choose different names for the different update funtions that are being called.

# Monad

Now we come to the module Monad. This module takes a mathematical concept and makes into practical programming construct.

Monads are the main reason MC has type manip-

First we are going to look at what monads exactly are within programming. Then we will see how they are implemented within MC.

#### **5.4.1** Monads

Monads are a container-like generic interface. They contain atleast two functions, return and bind.

These two functions are the basic way we can use monads.

#### The return

The return function takes a value and wraps it inside a monad.

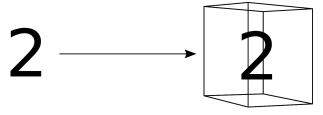


Figure 5.1: The return

The box in figure 5.1 visualizes the monad and 2 is the value that is being put inside the monad. With the return function any value can be put inside seen by the outside world.

This is where the bind comes in.

#### The bind

Having a monad is good, but what if you want to manipulate the value of the monad? The >>= (pronounced bind) function supplies this functionality.

When we want to apply the function (+3) to the monad containing 2, we call the bind. The bind unpacks the monad, as visualised in figure 5.2.

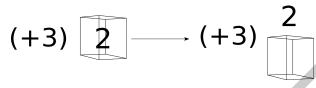


Figure 5.2: A function and a monad

It then applies the function to the value. And the the new value gets packed inside the monad by the function, as visualised in figure 5.3.

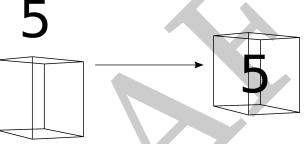


Figure 5.3: The return

Using these two basic functions, we can always work with monads and the values they contain.

To use the monads further we will need a few a monad. When it is inside the monad it cannot be more functions. These functions are generic for all the monads and will be given an implementation.

#### Returnfrom

Sometimes we want to directly pass the value inside the monad instead of wrapping it. This is done with returnFrom.

```
Func "returnFrom" -> 'a -> 'a
returnFrom a -> a
```

As we can see the identifier a is directly passed on.

#### Lift

Lift is used when a regular function, it takes a value and returns a value, needs to be executed over a monad. Lift unwraps the monad, executes the function with the value of the monad and then wraps the new value inside the monad.

An important difference with the bind, is that the function given to the lift does not pack the value in a monad. The function passed to the bind does pack the value inside the monad.

```
Func "lift" -> ('a -> 'b ) -> 'M 'a -> 'M 'b
   return f a'} -> res
lift f a -> res
```

Here we can see clearly that the lift repacks the value with return.

The Lift can also be declared with functions which take two arguments. It is then called Lift2.

Lift2 has to bind twice, once for each monad.

```
Func "lift2" -> ('a -> 'b -> 'c) -> 'M 'a ->
 \{a >>= a'
  h >>= h'
    return f a' b'} -> res
lift2 f a b -> res
```

This can be expanded to functions which take any number of arguments.

#### LiftM

There are of course functions which work with the wrapped monad. For this liftM is created.

For this we have to use the bind and return of the wrapped monad.

```
Func "liftM" -> (MCons^'M 'a -> MCons^M' 'b)
  → -> 'M (MCons^'M 'a) -> 'M (Mcons^'M 'b)
  return^'M b} -> res
liftM f M -> res
```

It works the same as the other lift functions, with the specification of using the bind and return of the wrapped monad, 'M, instead of the bind and return of the current monad.

The monad can now be used with a wider aspect within programming.

#### More than a wrapper

But just a monad offers very little besides being a wrapper for values. That is why there have been created a few different sorts of monads. This means a lot of different functionalities can be mapped to monads.

We will discuss two of these for now. More will be explained when looking at the implemented monads in MC in section 5.6.

The state monad gives monads the ability to behave like mutables. It takes a state and returns a new state and a return value.

state monad will simulate the *state* of the number being generated. The state monad is given a *state* in the form of a number and from this it will compute the new state of the number and the random number generated.

In MC the functionality might look like this:

```
Func "state" -> 's -> ('a,'s)
state number -> (randomGeneratedNumber,
    → newNumber)
```

**The maybe monad** offers the ability of the value to be either a value or nothing. For example we could utilize the pipe operator for this:

```
Data "Maybe" -> 'a -> 'a | Unit
Func "test" -> Maybe -> Boolean^System
(match a with
  (\ x -> True^builtin)
  (\ unit -> False^builtin)) -> res
test a -> res
```

Here we use Unit as the nothing and 'a as the value. In the example the term a is checked for a being a value, the Left, or being nothing, the Right.

This is a very basic example of how the maybe works. It acts like a pipe and can contain either a value, Left, or nothing, Right.

The implementations of these monads are far from complete, these examples simply show the functionality of the monad. The actual implementation will be given in section 5.4.3.

# **Combining monads**

Monads can also be combined. Since they have the Say we want a random number generator. The same generic interface they can be combined into another generic inteface. These new monads can utilise the functionality of the all combined mon-

> In this way the functionality of a monad can be extended. Combining monads can be seen as putting one monad inside another monad.

We will take the state and maybe monad and combine these into a parser monad. A parser monad can parse through a piece of text and scan for certain elements.

The state monad will be used for the scanning functionality and the maybe monad will be used to determine of the element has been found. The state monad returns the maybe monad as its result. When the maybe monad has a value as result the parser monad stops.

Like the normal monads they have to be build manually. This is a very error prone process when combining more than two monads or when using more complex monads.

What we actually want is to write the monads once and combine them automatically. This is where monad transformers come in.

## 5.4.2 Monad transformers

Monad transformers are a way to automatically combine monads. Instead of simply having a monad which takes the arguments it needs, it also takes another monad transformer as one of its arguments. This monad transformer is then used to given the actual value.

MC has an implementation of the basic monad transformer with which all monad transformers and monads can be created.

For monad transformers to work a generic function is added which contains the signature of the monad wrapped inside the transformer.

```
TypeFunc "MCons" -> Type
MCons -> 'M
```

The identifier 'M is the monad given to the monad transformer. MCons can be called when this monad is needed directly.

# 5.4.3 Implementation

Now we will look at how the monad transformer is implemented.

Because monad transformers need to be able to manipulate type information, it is a good example of what MC is useful for.

With this monad transformer we will be able to create actual monads, this can be seen as the base module for monads. First we take a look at the declaration:

```
TypeFunc "Monad" => (Type => Type) => Module
```

Monads are implemented as modules. This way we can put the return and bind functions inside a monad.

The first argument is a function on type level. It represents the monad transformer it uses to wrap the result in.

When looking at the implementation we see that a module is created with the return and the bind:

The bind is declared with ArrowFunc and is called >>=. It takes a monad as its first argument and a function as its second argument.

The function creates the new monad which is then returned.

The return takes a value, 'a, and wraps it inside the monad, 'M.

Both the bind and the return are only declared and not defined, because they are different for every monad created. When creating a new monad the bind and return will need to be defined.

The functions explained and implemented in section ?? will be added to this aswell.

With those we have the complete interface of the monad transformer. With this we can combine and built monads automatically.

## 5.4.4 Evolution of monad

The monad was first implemented with just the MCons, >>=, return and returnFrom functions. This enabled basic use of the monad.

The lift, lift2 and liftM were then added to extend the usecases of monads.

# 5.5 Tryable monad

Apart from the regular monadic module there is also the tryable monadic module. The tryable monad has as extra functionality that a function can be attempted.

This means that we can have functions that fail, without breaking the program.

It uses the regular monadic module to create a new interface. It also takes a monad as an argument which it then inherits.

It uses the type signature of 'M to create a new monad.

Here we see how MCons is used to get the signature of the original monad.

Then we declare the try function. It takes a monad and two functions.

```
Func "try" => MCons^'M 'a => ('a -> MCons^'M

→ 'b) => ('e -> MCons^'M 'b) => MCons^'M '

→ b
```

The value inside the monad is checked and then one of the functions is executed. This will be done in the definition.

First the value inside the monad is put into a match.

```
{pm >>=^'M x
  (match x with
```

If x contains an error the error function processes it. And if it contains a value the value is passed to the function.

```
(\e -> err e)
(\y -> k y)) -> z
```

The result of the match is then wrapped in monad 'M and returned.

```
return^'M z} -> res
------
try pm k err -> res
}
```

With try we can now check if the monad contains a value or an error and process them.

The try function was put to the test by manually typechecking it. The resulting proof can be found in appendix A.

We also want to be able to get the original monad out of the tryable monad. This is done with getMonad.

```
Func "getMonad" -> MCons^'M
  getMonad -> 'M
}
```

Now we can create a Monad which has two options when calling the bind. This can be used for error handling or for creating complex dataflows within monads.

# 5.5.1 Evolution of tryable monad

It occured then that we could also create more complex dataflows, when creating a generic tryable monad. This was then implemented as the TryableMonad.

# 5.6 Implemented monads

#### 5.6.1 Id

If monad transformers always take another monad, there has to be atleast one to end the chain. That is where the *id* monad transformer comes in.

It takes no monad as argument and simply returns all values as the are.

First we need a type signature to tell the monad monad. interface which monad we are creating.

```
TypeAlias "Id" => Type => Type
Id 'a => 'a
```

Here we can see what the id monad should do, simply pass the type on as it was given.

Now we will declare and define the id monad. The type signature is created with Id and the bind and return are defined.

```
TypeFunc "id" => Monad
id => Monad(Id) {
  bind x k -> k x
  return x -> x
}
```

Id also takes an 'a, but this is never used as the id monad does not need an extra type to say which

type it really uses. While the 'a is not used, it necessary to have them in the type signature. Else Id cannot be used to instantiate Monad, as evident from section 5.4.3.

Other monad transformers which do actually use the 'a also do not instantiate them immediatly. The programmer can decide for which type the monads will be created, therefor it is left open. This effectively creates an interface for the defined monad to be instantiated with a type later specified.

The return simply returns the exact same value and bind executes the function k with x as its argument. It is the monad which *passes through* the values.

When using the id monad transformer with another transformer, it becomes that monad.

As an example we pass the id monad to the maybe monad transformer. When the return of the created maybe monad is called, it first calls the return of the inner monad. In this case is the id monad.

The return of the id monad returns the value directly as a result. This result is then passed back to the maybe monad, where it gets wrapped inside the maybe monad and returned.

In this way the id monad will always end the cycle.

# 5.6.2 List

The list monad uses a list to store the values.

The list monad transformer uses List from *pre-lude* to create the transformer.

First we have to declare and define the signature.

Using ListT together with the signature of 'M we create the list monad.

```
TypeFunc "list" => Monad => Monad
list 'M => Monad(ListT MCons^'M) {
```

ListT also takes a 'a, which is the type for the list created. As stated in section 5.6.1 the programmer has to decide which type the list monad uses.

The return simply puts the value in a oneelement list wrapped inside a monad.

```
return x -> return^'M(x :: empty)
```

The bind looks a bit more complicated. It uses the ArrowFunc syntax together with a match.

```
{lm >>= l
(match l with
```

The match checks whether the list is empty.

```
(\empty -> return^'M empty)
```

When a list is present the first element of the list gets unpacked by the bind of 'M, which gets named y. The function k gets executed with y as its argument and the result gets repacked by the return.

```
(\(x :: xs) ->
{x >>=^'M y
return^'M k y} -> z
```

Now the rest of the list, xs, gets passed to the bind of list so the entire list gets passed to k. The results of processing x and xs are then concatenated into a single list.

All the nested functions are closed with the proper brackets and the resulting list is returned as the result of the bind.

If the use of the different syntaxes of the ArrowFunc seems confusing, take extra look at section 3.3.16.

#### **Evolution of list**

The list that the is used within the list monad, was first implemented within the list monad. But the list could be used outside of the monad as well.

It was then moved to prelude.

#### 5.6.3 Either

The either monad is an implementation of the because x is a value. TryableMonad module.

It creates a monad which can be either a value or a list of error messages. The type signature is as follows:

```
TypeAlias "EitherT" => (Type => Type) => Type
    → => Type => Type
EitherT 'M 'e 'a => 'M('a | 'e)
```

It uses the pipe to be able to be either failed or a value. In the definition of either, 'e will be specified as a list.

The TryableMonad is then called with the signature of the monadic argument.

```
TypeFunc "either" => Monad => Type =>
    → TryableMonad
either 'M 'e => TryableMonad(EitherT MCons^'M (
    → List 'e)) {
```

section 5.6.1.

Next we have is the fail function. It takes an error message and concatenates it with the existing error messsages.

```
Func "fail" -> 'e -> MCons^'M
fail e -> return^'M(Right (Right^'M :: e))
```

provide the error function to the try.

Because either is a TryableMonad it can contain a value or an error message. When calling the bind of either this needs to be checked.

That is why the bind calls try.

```
pm >>= k -> try pm k fail
```

The monad and the function is passed on to try together with the function fail.

The return passes the value to 'M. Left is used

```
return x -> return^'M(Left x)
```

maybe put a sort of conclusion here The either can now be

#### **Evolution of either**

The either was first implemented without the use of TyableMonad. It had the same functionality. All the functions of the TryableMonad were implemented directly within either.

When the idea occured of using a generic tryable monad, these were ported to the TryableMonad. The either was then implemented by using the TryableMonad.

## **5.6.4** Result

The 'a is again not used, like the id monad in The result monad is complete implementation of the either monad from section 5.6.3.

The either monad still needs an error type and a type for the values it takes. The result monad specifies the error type, leaving the type of the value for the programmer to specify.

Because all the functions in either are defined, result can directly call either with an error type. The fail is needed when we call the try. It will No further function declarations or definitions are needed.

> In the declaration we specify it returns a TryableMonad, which either is. And in the definition we specify the error type to be String.

```
TypeFunc "result" => Monad => TryableMonad
result 'M => either MCons^'M (List String)
```

This creates an either with String as error

#### **Evolution of result**

The original idea of the result monad was a maybe monad with error handling in the form of a string.

The result monad was first implemented in much the same way as the either monad, but with explicit use of String as the error handler. When this was noticed, the result monad was implemented by using either.

#### 5.6.5 State

We have had a basic explanation of the state monad in section 5.4.

Now we will see how it is implemented. The type signature of the state monad shows that it is a function.

```
TypeAlias "StateT" => (Type => Type) => Type =>

→ Type => Type

StateT 'M 's 'a \Rightarrow ('s \rightarrow 'M('a \star 's))
```

It takes a state and returns a monad containing a tuple af the resulting value and the new state.

We use StateT in the call to Monad so it knows what the type signature will be.

```
TypeFunc "state" => Monad => Type => Monad
state 'M 's => Monad(StateT MCons^'M 's) {
```

When looking at the return we see something new. A lambda is created to match the type signature of the state monad.

```
return x -> (\ s -> return^'M(x,s))
```

The x is set as the result of the state.

We see this happening also in the bind. A lambda is created and in the function body of the lambda the computation happens.

The bind of 'M is called and the result is then deconstructed to get to the tuple which it contains.

We know x is a tuple because it lives inside a state monad. As is evident by the type signature of the state monad.

the need for higher of the transformers [?], but MC implemntation.

This shows what

The state monad also contains two extra functions. They make it possible to get and set the state.

To get the state we call getState.

```
Func "getState" -> MCons 's
getState -> (\ s -> return^'M(s,s))
```

It sets the state as the result in the return lambda. By which you will get the state back when it is entered into the lambda. To set the state we call setState.

```
Func "setState" -> 's -> MCons Unit
setState s -> (\ unit -> return^'M(unit,s))
}
```

It sets the result to unit and the state to the input state.

# 5.7 Other monad implementations

When comparing the monad transformers of MC with monad implementations of other languages, we quickly come to the conclusion that MC is very compact.

When looking at a monad implementation in Python<sup>1</sup>, we see that the code for most monads is much longer. And these are the direct implementations, not using monad transformers.

There are only few attempts made when it comes to monad transformers. The main reason for this is the need for higher order types.

Haskell has a few implementations of monad transformers [?], but these are far longer than the MC implemntation.<sup>2</sup>

This shows what MC is capable of compared to most other languages. With the use of higher order types the high abstractions used for monad transformers can be implemented with very little code.

<sup>&</sup>lt;sup>1</sup>Appendix ??

<sup>&</sup>lt;sup>2</sup>See appendix C for the source code of a few of these monadic transformers

# **Test programs**

There have been two test programs written to test the language.

The first of these is a simple bouncing ball.

# 6.1 Bouncing ball

Bouncing ball is used as a preliminary test of the updatable records. It will show how the updatable recordentry are used in practice.

This program bounces a ball up and down.

The ball will have two properties, velocity and position, which will implemented as records. Both of these will then be put inside the updatable recordentry of the ball.

The update function will then add implement how the ball bounces.

First we import prelude, recordentry and the XNA framework The Microsoft XNA library will be used for the Vector2 it has and the Thread library will be used to call the Sleep function.

```
import Microsoft^Xna^Framework
import System^Threading^Thread
```

```
import record
import prelude
```

The recordentry of the ball will be build bottomup. This is done because every recordentry needs to have a rest as an argument.

Velocity is created first, because it needs to be updated less. It keeps deep searches of the recordentry to a minimum.

```
Record "Velocity" Vector2(0.0f, 98.1f) Empty
```

Then Position will be created with Velocity as its rest argument.

```
Record "Position" Vector2(100.0f, 0.0f)

→ Velocity
```

Lastly we create the updatable recordentry Ball. This is done in one line by creating a recordentry entry and passing it directly as argument to updatableRecord. Position is used as rest argument to complete the record.

We then need to define the update function. The Position and Velocity RecordEntry are put in a identifiers, so we can use them directly.

```
get^e "Position" Rest^e => position
get^e "Velocity" Rest^e => velocity
```

Then the height of the ball is check and the according calculations executed.

```
Rest^velocity))
else
(set^e "Position"
Vector2(X^Field^position, 500.0f)
-^Vector2(Field^velocity))) -> res

update e dt -> res
}
```

The final step is to create the run function to start the program. It will call the update function of Ball, sleep for a set amount of time and then call itself.

```
Func "run" -> RecordEntry -> String

update^ball ball time -> ball'
Sleep(1000)
run ball' (time +^Int 1000) -> res
-----
run ball time -> res
```

This creates an infinite loop, so the ball will keep on bouncing. The return will never be set as it will keep calling itself until the program stops.

# 6.2 Tron

Tron is a more advanced program which will utilise user input.

The game tron is played with two or more players. Each controlling a bike which leaves a trail. The bikes can move freely within the playingfield, but cannot stop, slow down or speed up. The trails the bikes leave behind become walls.

A bike may not hit a wall or trail, when it does it is destroyed. The player who remains driving is the winner.

The game tron [] has been chosen because of the minimalistic graphics. This allows us to focus on the internal workings of the game.

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Tron has been split up in two three parts, bike, playfield and main. The main file will calls all the needed parts and starts the game. The playfield will contain all the bikes.

This will keep all the parts clear and specific to their function.

The bikes and playfield will be records. Some of the recordentry will be made updatable recordentry when necessary.

We will start by looking at the bike.

## 6.2.1 Bike

First we import a few things. The XNA framework is needed for the vector2. The System.Windows.Input will be needed for the controls of the bike. Lastly we will import recordentry and prelude.

```
import Framework^Xna^Microsoft
import System^Windows^Input
import record
import prelude
```

The bike will need to have several things to work in the game.

A bike will need to have a recordentry which will keep track of its current position. The position will need to be updated so we will use an updatable record. The position recordentry will be created seperately and included in the bike later.

This is done make the definition of the bike smaller.

The RecordEntry is created in the premise and then passed to UpdatableRecord.

```
| PositionRecord label pos rest =>

→ UpdatableRecord r => Module{
```

The created record r will not be explicitly inherited as that happens with the UpdatableRecord function. We only need to define the update function.

The update function takes a record and a tuple. The tulpe conists of the delta time and the speed. This is then used to calculate the new position.

A new record containing the new position is then created and returned as the result.

Now that we have an updatable position we also need an updatable trail. This trail changes when the bike moves.

As with PositionRecord an we first create a record which is then passed to UpdatableRecord.

The update function only needs to create a new trail record with the original record as its Rest. This way the trail is a record of points.

```
RecordEntry label^t pos fields^t => res
-----
update t pos => res
}
```

Next we need the controls for each bike. As the bike is always moving forward we only need to steer left or right.

The two buttons used for this are placed in a record.

Then we come to the bike itself. It will use the Keys, TrailRecord and PositionRecord. And with those it also uses records to store the colour, speed and a boolean to check if it has not crashed.

The bike will also be given a name to give it a unique identifier.

In the definition we will see how the bike is build with multiple records.

All the records are ordered according to how often it is needed.

The update function will take a bike and the delta time as argument. It first checks if the bike is still active and returns the bike if it is dead.

```
(if Field^IsAlive then
```

Next the trail, position are put in variables.

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```
get^b "Trail" Field^b => trail
get^trail "Position" Rest^trail => position
get^position "Speed" Rest^position => speed
```

Then the trail and position get updated.

```
update^TrailRecord Field^trail Field^

→ position => newTrailRecord

update^PositionRecord position (dt,Field^

→ speed) -> newPos
```

A new trail record is created and lastly a new bike record is created and returned.

```
RecordEntry label^trail newTrailRecord

→ newPos => newTrail

RecordEntry Label^b newTrail Rest^b
else
b) -> res

-----
update b dt -> res
}
```

We now have a complete bike that can be updated.

#### **Evolution**

During the development of tron the apply function was used to call all the update functions. After its removal the update functions are directly called.

# 6.2.2 Playfield

The playfield contains a record with the bikes, the filed size and a winner. When the winner is set it will be returned to the main function and the game will end.

First we import the XNA framework, System, record, prelude and bike.

```
import Framework^Xna^Microsoft
import record
```

```
import prelude
import bike
```

For the bikes a separate record will be created. This enables a dynamic number of bikes without interfering with the playfield.

When defining the update function we need a few extra functions to make it all work. These functions are necessary because they do recursive operations. This would be impossible without a separate function.

The first function is checkTrails. It goes over through the trail of a bike and check for any collisions. It takes a position and trail and returns a boolean. If any collisions are detected the boolean returns false, otherwise it returns true.

First we check for any collisions with the current point in the trail.

If there are no collisions and there are more points in the trail, checkTrails is recursively called.

Next we have checkCollisions, which calls checkTrials for the trail of every bike. It takes a bike and a record of bikes. The position of the current bike and the trail of the first bike in the record, will be passed to checkTrails.

Then we have the function which will update the IsAlive status of the current bike. First it checks if the position of the bike is within the playfield.

If the bike is within the playing field, any collisions with its own trail and the other bikes is tested.

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through all the bikes and calls their update function. three. It then returns the updated bikes.

Empty.

```
Func "updateBikes" -> Record -> Float ->
  → Record
(if (b == Empty) then
  Empty
else
  (update^b b dt -> newBike
  updateBikes Rest^b dt -> newRest
  RecordEntry Label^newBike Field^newBike
  → newRest)) -> res
updateBikes b dt -> res
```

In the update function we want to get the actual bikes.

```
Field^bs -> bikeRecords
```

We also need the fieldsize and the delta time. These are given to the function as a tuple, because

We then come to updateBikes. This goes update can only take two parameters and we need

The update functions first calls updateBikes. But first we have to check if the bike record is And when the bikes are updated they are passed to updateIsAlive. The new bike record is then returned.

```
dtfs -> (dt,fs)
updateBikes bikeRecords dt -> newBikeRecords
updateIsAlive newBikeRecords fs ->
 → aliveBikeRecords
set^bs label^bs aliveBikeRecords bs -> res
______
update bs dtfs -> res
```

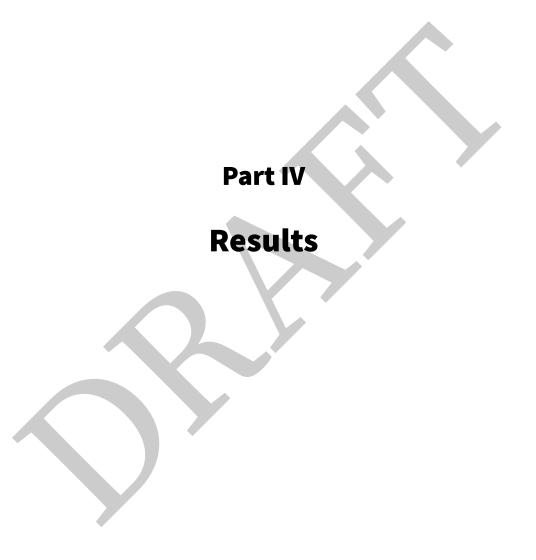
## When defining the actual playfield

```
TypeFunc "Playfield" => String => Record =>
    → Vector2 => Record
RecordEntry "Winner" unit Empty
BikeRecordEntry "Bikes" bikes Winner -> rest
Playfield label bikes size => updatableRecord (

→ RecordEntry label size rest) {
```

```
Func "checkDeaths" -> bike -> amountAlive ->
(if (amountAlive > 1) then
 unit
else
  ((if ((get^bike "IsAlive" Field^bike) ==
  → True^builtin) then
   amountAlive + 1
 else
   amountAlive -> newAmountAlive
 checkDeaths Rest^bike newAmountAlive) ->
checkDeaths bike amountAlive -> res
get^p "Bikes" Rest^p -> bikes
update^bikes bikes (dt,Field^p) -> newBikes
checkDeaths Field^newBikes 0 -> winner
set^p "Winner" winner Rest^p ->
  → updatedPlayfield
set^p "Bikes" newBikes Rest^p -> newPlayfield
update p dt -> newPlayField
```

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# **Conclusion**

To summerize the main research question was: How can the programming language MetaCasanova be improved for the user within the timeframe of the internship?

The answer to this research question is: *Meta-Casanova can be improved by creating a clear definition of what a good programming language is and using that as a basis for further development.* 

It can also be improved by changing the viewpoint from developer to user of the language. This provides new insights in to how the language works and how it is expected to work.

Extending the standard library also has an impact on the usability of the language.

Other conclusions that were found during the project were:

- 1. Complex datastructures can be improved in performance when doing most of the work in compile time.
- 2. Higher order types enable the writing of complex concepts in fewer lines of code with more clarity.



## **Chapter 8**

## **Recommendations**

These recommendations are for the people continueing with the project.

# 8.1 Improving a programming language

When first learning about a language, keep on asking until you have specifics. Most of the developers have general ideas of a language. These ideas have very little specifics, but will come to the surface when really digging.

By having these ideas before hand, bugs will become apparent when first looking at the actual language.

#### 8.2 Further development

When developing MC further I would recommend to expand the standard library even more. Especially when the focus of the language is put more on monads.

#### 8.2.1 **Monads**

First we would need a proper IO monad for interacting with the unpure functions and get real output.

Coroutines would be next. Both as a separate entity and as a monad. They would give the ability of multi threading directly in the language. This would improve performance.

#### 8.2.2 The compiler

I would also recommend to keep syntax changes to a minimum. This will give the compiler developers a fighting chance. During the development the compiler developers have thrown away alot of work, because the syntax became too different.

When creating a new itteration of the language, first get a clear picture of the language before starting work on the compiler. This creates less work for the compiler developers as they do not have to change the compiler mid build.

## **Chapter 9**

## **Evaluation**

Here I will provide proof of having the competentions which are associated with computer science according to the university of Rotterdam [].

### 9.1 Multi-discipliniar

By working in a research team there are many different people to deal and communicate with. This kunnen werken in ... team en zelfstandig hun taken uitvoeren.

### 9.2 klant en probleem gericht opereren

#### 9.3 methodical

## 9.4 openstaan voor technologische ontwikkelingen in die eigen kunnen maken

# 9.5 able to reflect and adapt on their beroepsmatig handelen

Here I will provide proof of having mastered the dublin descriptors and the extra competentions as set in the graduation module guidelines [].

### 9.6 Dublin descriptors

#### 9.6.1 Knowledge and understanding

During the project I have used type-theory as described in [] to check the programs I was writing. This can be explicitly seen in section 5.5 and appendix A.

Further more I have learned the monadic theory to be able to implement them in the standard library.

Both of these build on the knowledge gained during my four years of studying at the University of Rotterdam. Here I have learned the basis which was needed during this project.

The programming skills learned were needed to expand these skills with the type theory. The math-

ematical skills gained were needed when learning about the monadic constructs.

#### 9.6.2 Applying knowledge and understanding

The knowledge gained in the research phase of this project combined with the knowledge gained in my study years, have been put into practical use. When building upon MC I had to use all the type theory knowledge gained to be certain no function failed.

When implementing the monadic part of the standard library, I have combined the programming- with the mathematical skills to translate mathematical ideas into a practical code base.

#### 9.6.3 Making judgements

At the start of this project I have done research into a new language, MC, type theory and monadic mathematical concepts. These were all needed to build upon the existing codebase of MC.

**DO CITATIONS** I have made descisions while keeping both the practical aspects and goals in mind, as seen in sections ??,?? and ??.

#### 9.6.4 Communication

During this project I have worked in a research team where I have had to explain myself to fellow team members and supervisors.

This was done in the form of presentations, discussions and meetings. I also had to understand their ideas about concepts.

Part IV Chapter 9. Evaluation

## 9.6.5 Lifelong learning skills

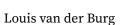


## **Chapter 10**

# **Bibliography**

[2] U. P. Khedker, "What makes a good programming language," tech. rep., Technical Report TR-97-upk-1, Department of Computer Science University of Pune, 1997.

- http://creating010.com/en/. Accessed:
- [1] "Creating 010 kenniscentrum creating 010." [3] P. Graham, Hackers & painters: big ideas from the computer age. "O'Reilly Media, Inc.", 2004.





## **Appendix A**

 $Mcons_{\alpha}^{prs}$ 

# **Typeproofs**

This contains the type proof of the try function of the TryableMonad, as described in section 5.5.

 $Mcons_{\alpha}$  $: M\alpha$  $Mcons_{\alpha}^{st}$  $: (\sigma \to \alpha \sigma)$  $Mcons_{\alpha}^{res}$  $: (\alpha | \epsilon)$  $: (\sigma \to (\sigma \to (\alpha | \epsilon) \times \sigma) \times \sigma)$ 

$$try^{prs} \ k \ err \ pm = lift^{st}(lift^{st}(try^{res}k(\lambda e_1.try^{res}(>>=)^{id}(\lambda e_2.fail^{prs}(e_1+e_2)))err))pm : (\alpha \rightarrow M\beta) \rightarrow (\epsilon \rightarrow M\beta) \rightarrow Mcons^{prs}_{\alpha} \rightarrow Mcons^{prs}_{\beta} \rightarrow Mcons^{prs}$$

$$\frac{try^{res}: (\alpha \rightarrow M\beta) \rightarrow (\epsilon \rightarrow M\beta) \rightarrow Mcons_{\alpha}^{res} \rightarrow Mcons_{\beta}^{res}}{(>>=)^{id}: (\alpha \rightarrow M\beta)} \underbrace{\frac{fail^{prs}: \epsilon \rightarrow Mcons_{\alpha}^{prs}}{fail^{prs}(e_1 + e_2): Mcons_{\alpha}^{prs}}}_{fail^{prs}(e_1 + e_2): Mcons_{\alpha}^{prs}} \underbrace{\frac{try^{res}(>>=)^{id}: (\epsilon \rightarrow M\beta) \rightarrow Mcons_{\alpha}^{res} \rightarrow Mcons_{\beta}^{res}}{(\lambda e_2.fail^{prs}(e_1 + e_2)): Mcons_{\alpha}^{res} \rightarrow Mcons_{\beta}^{res}}}}_{\lambda e_1.try^{res}(>>=)^{id}(\lambda e_2.fail^{prs}(e_1 + e_2)): \epsilon \rightarrow Mcons_{\alpha}^{res} \rightarrow Mcons_{\beta}^{res}}}$$

$$\frac{try^{res}:(\alpha\to M\beta)\to(\epsilon\to M\beta)\to Mcons^{res}_{\alpha}\to Mcons^{res}_{\beta} \quad k:(\alpha\to M\beta)}{try^{res}k:(\epsilon\to M\beta)\to Mcons^{res}_{\alpha}\to Mcons^{res}_{\beta} \qquad \qquad \\ \lambda e_1.try^{res}(>>=)^{id}\left(\lambda e_2.fail^{prs}(e_1+e_2)\right):\epsilon\to Mcons^{res}_{\alpha}\to Mcons^{res}_{\beta} \\ \textbf{Contradiction: application of } try^{res}k \text{ expects } (\epsilon\to M\beta) \text{ but got } (\epsilon\to Mcons^{res}_{\alpha}\to Mcons^{res}_{\beta})$$

 $fail^{prs}:\epsilon
ightarrow Mcons^{prs}_{lpha} \quad rac{e_{1}:\epsilon \quad e_{2}:\epsilon}{e_{1}+e_{2}:\epsilon}$ 

 $try^{prs}\ k\ err\ pm = lift^{st}(lift^{st\_ctxt}(try^{res}k(\lambda e_1.try^{res}return^{id}(\lambda e_2.fail^{prs}(e_1 + e_2))err)))pm : (\alpha \to Mcons_{\beta}^{prs}) \to (\epsilon \to Mcons_{\beta}^{prs}) \to Mcons_{\beta}^{prs}) \to Mcons_{\beta}^{prs}$ 

 $\begin{array}{c} try^{res}: (\alpha \rightarrow Mcons^{res}_{\beta}) \rightarrow (\epsilon \rightarrow Mcons^{res}_{\beta}) \rightarrow Mcons^{res}_{\alpha} \rightarrow Mcons^{res}_{\beta} & return^{id}: (\alpha \rightarrow Mcons^{res}_{\beta}) \\ \hline try^{res}return^{id}: (\epsilon \rightarrow Mcons^{res}_{\beta}) \rightarrow Mcons^{res}_{\alpha} \rightarrow Mcons^{res}_{\beta} & \hline \\ \hline ke_{2}.fail^{prs}(e_{1}+e_{2}): \kappa \rightarrow Mcons^{prs}_{\alpha} \\ \hline \lambda e_{2}.fail^{prs}(e_{1}+e_{2}): \kappa \rightarrow Mcons^{prs}_{\alpha} \\ \hline \end{array}$ 

 $try^{res}return^{id} (\lambda e_2.fail^{prs}(e_1 + e_2)) : Mcons_{\alpha}^{res} \to Mcons_{\beta}^{res}$ 

 $err: Mcons^{res}_{\alpha}$ 

 $\frac{try^{res}return^{id} (\lambda e_2.fail^{prs}(e_1 + e_2))err: Mcons_{\beta}^{res}}{\lambda e_1.try^{res}return^{id} (\lambda e_2.fail^{prs}(e_1 + e_2))err: \epsilon \to Mcons_{\beta}^{res}}$ 

 $try^{res}: (\alpha \to Mcons^{res}_{\beta}) \to (\epsilon \to Mcons^{res}_{\beta}) \to Mcons^{res}_{\alpha} \to Mcons^{res}_{\beta} \qquad k: (\alpha \to Mcons^{prs}_{\beta})$ 

 $try^{res}k: (\epsilon \to Mcons^{res}_{\beta}) \to Mcons^{res}_{\alpha} \to Mcons^{res}_{\beta}$ 

 $\lambda e_1.try^{res}return^{id} (\lambda e_2.fail^{prs}(e_1 + e_2))err : \epsilon \to Mcons^{res}_{\beta}$ 

 $try^{res}k\left(\lambda e_1.try^{res}return^{id}\left(\lambda e_2.fail^{prs}(e_1+e_2)\right)err\right):Mcons_{\alpha}^{res}\to Mcons_{\beta}^{res}$ 

 $lift^{st}: (\alpha \rightarrow \beta) \rightarrow Mcons_{\alpha}^{st\_ctxt} \rightarrow Mcons_{\beta}^{res} \qquad try^{res}k\left(\lambda e_1.try^{res}return^{id}\left(\lambda e_2.fail^{prs}(e_1+e_2)\right)err\right): Mcons_{\beta}^{res}$   $lift^{st}: (\alpha \rightarrow \beta) \rightarrow Mcons_{\beta}^{st\_ctxt} \qquad lift^{st\_ctxt}(try^{res}k\left(\lambda e_1.try^{res}return^{id}\left(\lambda e_2.fail^{prs}(e_1+e_2)\right)err\right)pm): Mcons_{\beta}^{res}$ 

 $\overline{lift^{st}(lift^{st\_ctxt}(try^{res}k\ (\lambda e_1.try^{res}return^{id}\ (\lambda e_2.fail^{prs}(e_1+e_2))\ err)))\ pm:Mcons^{res}_{\beta}}$ 

## **Appendix B**

# **Monads in Python**

These are found in the *PyMonad* library [?].

#### **B.1** State

```
def amap(self, functorValue):
       Applies the function contained within the monad to the result of 'functorValue'
       and passes along the state unchanged.
       11 11 11
       @State
       def newState(state):
                function = self.getResult(state)
                value = functorValue.getResult(state)
                return (function(value), state)
        return newState
def bind(self, function):
       Chains together a series of stateful computations. 'function' accepts a single value
       and produces a new 'State' value which may or may not alter the state when it is
       executed.
       11 11 11
       @State
       def newState(state):
                result, st = self(state)
                return function(result)(st)
       return newState
@classmethod
def unit(cls, value):
       Produces a new stateful calculation which produces 'value' and leaves the passed in
       state untouched.
       return State(lambda state: (value, state))
def getResult(self, state):
        """ Returns only the result of a stateful calculation, discarding the state. """
       return self.value(state)[0]
def getState(self, state):
       """ Returns only the final state of a stateful calculation, discarding the result. """
       return self.value(state)[1]
def __call__(self, state):
       Executes the stateful calculation contained within the monad with an initial 'state'.
       Returns the result and the final state as a 2-tuple.
```

return self.value(state)

def \_\_eq\_\_(self, other):
 """

Always raises a TypeError.
 The State monad contains functions which can not be directly compared for equality,
 so attempting to compare instances of State with anything will always fail.

"""

raise TypeError("State: Can't compare functions for equality.")

## **Appendix C**

## Monads transformers in haskell

These are found in the transformers package [?].

#### C.1 State

```
{-# LANGUAGE CPP #-}
#if GLASGOW HASKELL >= 702
{-# LANGUAGE Safe #-}
#endif
#if __GLASGOW_HASKELL__ >= 710
{-# LANGUAGE AutoDeriveTypeable #-}
#endif
              : Control.Monad.Trans.State.Lazy
-- Module
-- Copyright : (c) Andy Gill 2001,
                 (c) Oregon Graduate Institute of Science and
   → Technology, 2001
              : BSD-style (see the file LICENSE)
-- Maintainer : R.Paterson@city.ac.uk
-- Stability : experimental
-- Portability: portable
-- Lazy state monads, passing an updatable state through a computation.
-- See below for examples.
```

```
state,
   runState,
   evalState.
   execState,
   mapState,
   withState.
   -- * The StateT monad transformer
   StateT(..),
   evalStateT.
   execStateT,
   mapStateT.
   withStateT,
   -- * State operations
   get,
   put,
   modify,
   modify'.
   gets,
   -- * Lifting other operations
   liftCallCC,
   liftCallCC',
   liftCatch.
   liftListen,
   liftPass.
   -- * Examples
   -- ** State monads
   -- $examples
   -- ** Counting
   -- $counting
   -- ** Labelling trees
   -- $labelling
 ) where
import Control.Monad.IO.Class
import Control.Monad.Signatures
import Control.Monad.Trans.Class
import Data.Functor.Identity
import Control.Applicative
import Control.Monad
#if MIN_VERSION_base(4,9,0)
import qualified Control.Monad.Fail as Fail
#endif
import Control.Monad.Fix
```

```
-- | A state monad parameterized by the type @s@ of the state to carry.
-- The 'return' function leaves the state unchanged, while @>>=@ uses
-- the final state of the first computation as the initial state of
-- the second.
type State s = StateT s Identity
-- | Construct a state monad computation from a function.
-- (The inverse of 'runState'.)
state :: (Monad m)
    => (s -> (a, s)) -- ^pure state transformer
     -> StateT s m a -- ^equivalent state-passing computation
state f = StateT (return . f)
{-# INLINE state #-}
-- | Unwrap a state monad computation as a function.
-- (The inverse of 'state'.)
runState :: State s a -- ^state-passing computation to execute
    -> s -- ^initial state
       -> (a, s) -- ^return value and final state
runState m = runIdentity . runStateT m
{-# INLINE runState #-}
 - | Evaluate a state computation with the given initial state
-- and return the final value, discarding the final state.
* @'evalState' m s = 'fst' ('runState' m s)@
evalState :: State s a -- ^state-passing computation to execute
         -> s -- ^initial value
         -> a -- ^return value of the state computation
evalState m s = fst (runState m s)
{-# INLINE evalState #-}
-- | Evaluate a state computation with the given initial state
-- and return the final state, discarding the final value.
-- * @'execState' m s = 'snd' ('runState' m s)@
execState :: State s a -- ^state-passing computation to execute
         -> s -- ^initial value
         -> s
                    -- ^final state
execState m s = snd (runState m s)
{-# INLINE execState #-}
-- | Map both the return value and final state of a computation using
```

```
-- the given function.
                                                                           ||{-# INLINE execStateT #-}
-- * @'runState' ('mapState' f m) = f . 'runState' m@
mapState :: ((a, s) \rightarrow (b, s)) \rightarrow State s a \rightarrow State s b
                                                                            -- the given function.
mapState f = mapStateT (Identity . f . runIdentity)
{-# INLINE mapState #-}
-- | @'withState' f m@ executes action @m@ on a state modified by
-- applying @f@.
                                                                            {-# INLINE mapStateT #-}
-- * @'withState' f m = 'modify' f >> m@
withState :: (s -> s) -> State s a -> State s a
                                                                            -- applying @f@.
withState = withStateT
{-# INLINE withState #-}
                                                                            f-#-INLINE withStateT #-}
  | A state transformer monad parameterized by:
    * @s@ - The state.
                                                                                {-# INLINE fmap #-}
    * @m@ - The inner monad.
-- The 'return' function leaves the state unchanged, while @>>=@ uses
-- the final state of the first computation as the initial state of
                                                                                {-# INLINE pure #-}
-- the second.
newtype StateT s m a = StateT { runStateT :: s -> m (a,s) }
                                                                                   ~(f, s') <- mf s
                                                                                    \sim (x, s'') \leftarrow mx s'
-- | Evaluate a state computation with the given initial state
                                                                                    return (f x, s'')
-- and return the final value, discarding the final state.
                                                                                {-# INLINE (<*>) #-}
-- * @'evalStateT' m s = 'liftM' 'fst' ('runStateT' m s)@
evalStateT :: (Monad m) => StateT s m a -> s -> m a
evalStateT m s = do
                                                                                {-# INLINE emptv #-}
   ~(a, _) <- runStateT m s
                                                                                {-# INLINE (<|>) #-}
   return a
{-# INLINE evalStateT #-}
-- | Evaluate a state computation with the given initial state
-- and return the final state, discarding the final value.
                                                                                {-# INLINE return #-}
-- * @'execStateT' m s = 'liftM' 'snd' ('runStateT' m s)@
                                                                            #endif
execStateT :: (Monad m) => StateT s m a -> s -> m s
execStateT m s = do
   ~( , s') <- runStateT m s
                                                                                    runStateT (k a) s'
    return s'
                                                                                {-# INLINE (>>=) #-}
```

```
-- | Map both the return value and final state of a computation using
-- * @'runStateT' ('mapStateT' f m) = f . 'runStateT' m@
mapStateT :: (m (a, s) \rightarrow n (b, s)) \rightarrow StateT s m a \rightarrow StateT s n b
mapStateT f m = StateT $ f . runStateT m
-- | @'withStateT' f m@ executes action @m@ on a state modified by
-- * @'withStateT' f m = 'modify' f >> m@
withStateT :: (s -> s) -> StateT s m a -> StateT s m a
withStateT f m = StateT $ runStateT m . f
instance (Functor m) => Functor (StateT s m) where
    fmap f m = StateT $ \ s ->
        fmap (\ \sim (a, s') \rightarrow (f a, s')) $ runStateT m s
instance (Functor m. Monad m) => Applicative (StateT s m) where
    pure a = StateT $ \ s -> return (a, s)
    StateT mf <*> StateT mx = StateT $ \ s -> do
instance (Functor m. MonadPlus m) => Alternative (StateT s m) where
    empty = StateT $ \ -> mzero
    StateT m <|> StateT n = StateT $ \ s -> m s `mplus` n s
instance (Monad m) => Monad (StateT s m) where
#if !(MIN_VERSION_base(4,8,0))
    return a = StateT $ \ s -> return (a, s)
    m >>= k = StateT $ \ s -> do
        ~(a, s') <- runStateT m s
```

```
fail str = StateT $ \ _ -> fail str
   {-# INLINE fail #-}
#if MIN VERSION base(4,9,0)
instance (Fail.MonadFail m) => Fail.MonadFail (StateT s m) where
   fail str = StateT $ \ _ -> Fail.fail str
   {-# INLINE fail #-}
#endif
instance (MonadPlus m) => MonadPlus (StateT s m) where
               = StateT $ \ _ -> mzero
   {-# INLINE mzero #-}
   StateT m `mplus` StateT n = StateT $ \ s -> m s `mplus` n s
   {-# INLINE mplus #-}
instance (MonadFix m) => MonadFix (StateT s m) where
   mfix f = StateT $ \ s -> mfix $ \ ~(a. ) -> runStateT (f a) s
   {-# INLINE mfix #-}
instance MonadTrans (StateT s) where
   lift m = StateT $ \ s -> do
       a <- m
        return (a, s)
   {-# INLINE lift #-}
instance (MonadIO m) => MonadIO (StateT s m) where
   liftIO = lift . liftIO
   {-# INLINE liftIO #-}
-- | Fetch the current value of the state within the monad.
get :: (Monad m) => StateT s m s
{-# INLINE get #-}
-- | @'put' s@ sets the state within the monad to @s@.
put :: (Monad m) => s -> StateT s m ()
put s = state $ \ _ -> ((), s)
{-# INLINE put #-}
-- | @'modify' f@ is an action that updates the state to the result of
-- applying @f@ to the current state.
-- * @'modify' f = 'get' >>= ('put' . f)@
modify :: (Monad m) \Rightarrow (s \rightarrow s) \rightarrow StateT s m ()
modify f = state $ \setminus s \rightarrow ((), f s)
{-# INLINE modify #-}
```

```
-- | A variant of 'modify' in which the computation is strict in the
-- new state.
-- * @'modify'' f = 'get' >>= (('$!') 'put' . f)@
modify' :: (Monad m) \Rightarrow (s \Rightarrow s) \Rightarrow StateT s m ()
modify' f = do
   s <- get
    put $! f s
{-# INLINE modify' #-}
-- | Get a specific component of the state, using a projection function
-- supplied.
-- * @'gets' f = 'liftM' f 'get'@
gets :: (Monad m) \Rightarrow (s \rightarrow a) \rightarrow StateT s m a
gets f = \text{state } \ \ \ \ s \rightarrow (f s, s)
{-# INLINE gets #-}
-- | Uniform lifting of a @callCC@ operation to the new monad.
-- This version rolls back to the original state on entering the
-- continuation.
liftCallCC :: CallCC m (a,s) (b,s) -> CallCC (StateT s m) a b
liftCallCC callCC f = StateT $ \ s ->
  callCC $ \ c ->
   {-# INLINE liftCallCC #-}
-- | In-situ lifting of a @callCC@ operation to the new monad.
-- This version uses the current state on entering the continuation.
It does not satisfy the uniformity property (see "Control.Monad.
    → Signatures").
liftCallCC' :: CallCC m (a,s) (b,s) -> CallCC (StateT s m) a b
liftCallCC' callCC f = StateT $ \ s ->
    callCC $ \ c ->
    runStateT (f (\ a \rightarrow StateT $ \ s' \rightarrow c (a, s'))) s
{-# INLINE liftCallCC' #-}
-- | Lift a @catchE@ operation to the new monad.
liftCatch :: Catch e m (a,s) -> Catch e (StateT s m) a
liftCatch catchE m h =
    StateT $ \ s -> runStateT m s `catchE` \ e -> runStateT (h e) s
{-# INLINE liftCatch #-}
-- | Lift a @listen@ operation to the new monad.
liftListen :: (Monad m) => Listen w m (a,s) -> Listen w (StateT s m) a
liftListen listen m = StateT $ \ s -> do
~((a, s'), w) <- listen (runStateT m s)
```

```
return ((a, w), s')
{-# INLINE liftListen #-}
-- | Lift a @pass@ operation to the new monad.
liftPass :: (Monad m) => Pass w m (a,s) -> Pass w (StateT s m) a
liftPass pass m = StateT $ \ s -> pass $ do
   \sim((a, f), s') <- runStateT m s
   return ((a, s'), f)
{-# INLINE liftPass #-}
{- $examples
Parser from ParseLib with Hugs:
> type Parser a = StateT String [] a
> ==> StateT (String -> [(a,String)])
For example, item can be written as:
> item = do (x:xs) <- get
         put xs
        return x
> type BoringState s a = StateT s Identity a
       ==> StateT (s -> Identity (a,s))
> type StateWithIO s a = StateT s IO a
      ==> StateT (s -> IO (a,s))
> type StateWithErr s a = StateT s Maybe a
      ==> StateT (s -> Maybe (a,s))
-}
{- $counting
A function to increment a counter.
Taken from the paper \"Generalising Monads to Arrows\",
John Hughes (<http://www.cse.chalmers.se/~rimh/>), November 1998:
> tick :: State Int Int
> tick = do n <- get
            put (n+1)
           return n
Add one to the given number using the state monad:
```

```
> plusOne :: Int -> Int
 > plusOne n = execState tick n
A contrived addition example. Works only with positive numbers:
> plus :: Int -> Int -> Int
 > plus n x = execState (sequence $ replicate n tick) x
 {- $labelling
An example from /The Craft of Functional Programming/, Simon
Thompson (<http://www.cs.kent.ac.uk/people/staff/sjt/>),
Addison-Wesley 1999: \"Given an arbitrary tree, transform it to a
tree of integers in which the original elements are replaced by
natural numbers, starting from 0. The same element has to be
replaced by the same number at every occurrence, and when we meet
an as-yet-unvisited element we have to find a \'new\' number to match
it with:\"
> data Tree a = Nil | Node a (Tree a) (Tree a) deriving (Show, Eq)
 > type Table a = [a]
> numberTree :: Eq a => Tree a -> State (Table a) (Tree Int)
 > numberTree Nil = return Nil
> numberTree (Node x t1 t2) = do
    num <- numberNode x
      nt1 <- numberTree t1
      nt2 <- numberTree t2
      return (Node num nt1 nt2)
      numberNode :: Eq a => a -> State (Table a) Int
      numberNode x = do
          table <- get
          case elemIndex x table of
              Nothing -> do
                  put (table ++ [x])
                  return (length table)
              Just i -> return i
numTree applies numberTree with an initial state:
> numTree :: (Eq a) => Tree a -> Tree Int
> numTree t = evalState (numberTree t) []
> testTree = Node "Zero" (Node "One" (Node "Two" Nil Nil) (Node "One" (
```

```
issues (4)
fork
file changes
annotate
download .zip
darcs get url
Packs built at 2015-11-20 14:15:46 UTC
```