X=V, n=3 : Operators and Kinematic Factors $\label{eq:X} {\text{E.T.}}$

January 30, 2025

(4, 1)

(Block 1) Trace = 0, Mixed Symmetry, C = mixed

$$\begin{split} O_1^{V(4,1),1} &= O_{2,1,2} + O_{3,1,3} + O_{4,1,4} \\ K_1^{V(4,1),1} &= \frac{ip_1(E(p)^3 + E(p)m_N^2 + E(p)p_1^2 - E(p)p_2^2 - E(p)p_3^2 + 2m_N^3 + 2m_Np_1^2)}{(2E(p)(E(p) + m_N))} \end{split}$$

$$\begin{split} O_2^{V(4,1),1} &= O_{1,2,1} + O_{3,2,3} + O_{4,2,4} \\ K_2^{V(4,1),1} &= \frac{ip_2(E(p)^3 + E(p)m_N^2 - E(p)p_1^2 + E(p)p_2^2 - E(p)p_3^2 + 2m_N^3 + 2m_Np_2^2)}{(2E(p)(E(p) + m_N))} \end{split}$$

$$\begin{split} O_3^{V(4,1),1} &= O_{1,3,1} + O_{2,3,2} + O_{4,3,4} \\ K_3^{V(4,1),1} &= \frac{ip_3(E(p)^3 + E(p)m_N^2 - E(p)p_1^2 - E(p)p_2^2 + E(p)p_3^2 + 2m_N^3 + 2m_Np_3^2)}{(2E(p)(E(p) + m_N))} \end{split}$$

$$\begin{split} O_4^{V(4,1),1} &= O_{1,4,1} + O_{2,4,2} + O_{3,4,3} \\ K_4^{V(4,1),1} &= p_1^2 + p_2^2 + p_3^2 \end{split}$$

(Block 2) Trace = 0, Mixed Symmetry, C = mixed

$$\begin{split} O_1^{V(4,1),2} &= O_{2,2,1} + O_{3,3,1} + O_{4,4,1} \\ K_1^{V(4,1),2} &= \frac{ip_1(E(p)^3 + E(p)m_N^2 + E(p)p_1^2 - E(p)p_2^2 - E(p)p_3^2 + 2m_N^3 + 2m_Np_1^2)}{(2E(p)(E(p) + m_N))} \end{split}$$

$$\begin{split} O_2^{V(4,1),2} &= O_{1,1,2} + O_{3,3,2} + O_{4,4,2} \\ K_2^{V(4,1),2} &= \frac{i p_2(E(p)^3 + E(p) m_N^2 - E(p) p_1^2 + E(p) p_2^2 - E(p) p_3^2 + 2 m_N^3 + 2 m_N p_2^2)}{(2E(p)(E(p) + m_N))} \end{split}$$

$$\begin{split} O_3^{V(4,1),2} &= O_{1,1,3} + O_{2,2,3} + O_{4,4,3} \\ K_3^{V(4,1),2} &= \frac{ip_3(E(p)^3 + E(p)m_N^2 - E(p)p_1^2 - E(p)p_2^2 + E(p)p_3^2 + 2m_N^3 + 2m_Np_3^2)}{(2E(p)(E(p) + m_N))} \end{split}$$

$$\begin{split} O_4^{V(4,1),2} &= O_{1,1,4} + O_{2,2,4} + O_{3,3,4} \\ K_4^{V(4,1),2} &= p_1^2 + p_2^2 + p_3^2 \end{split}$$

(Block 3) Trace = 0, Symmetric, C = -1

$$O_1^{V(4,1),3} = O_{1,1,1}$$
 $K_1^{V(4,1),3} = \frac{-ip_1^3}{E(p)}$

$$O_2^{V(4,1),3} = O_{2,2,2}$$
$$K_2^{V(4,1),3} = \frac{-ip_2^3}{E(p)}$$

$$O_3^{V(4,1),3} = O_{3,3,3}$$

$$K_3^{V(4,1),3} = \frac{-ip_3^3}{E(p)}$$

$$\begin{split} O_4^{V(4,1),3} &= O_{4,4,4} \\ K_4^{V(4,1),3} &= \frac{-E(p)(E(p)^2 + E(p)m_N)}{(E(p) + m_N)} \end{split}$$

(Block 4) Trace = 0, Mixed Symmetry, C = -1

$$\begin{split} O_1^{V(4,1),4} &= O_{1,2,2} + O_{1,3,3} + O_{1,4,4} \\ K_1^{V(4,1),4} &= \frac{ip_1(m_N^2 + p_1^2)}{E(p)} \end{split}$$

$$\begin{split} O_2^{V(4,1),4} &= O_{2,1,1} + O_{2,3,3} + O_{2,4,4} \\ K_2^{V(4,1),4} &= \frac{ip_2(m_N^2 + p_2^2)}{E(p)} \end{split}$$

$$O_3^{V(4,1),4} = O_{3,1,1} + O_{3,2,2} + O_{3,4,4}$$

$$K_3^{V(4,1),4} = \frac{ip_3(m_N^2 + p_3^2)}{E(p)}$$

$$O_4^{V(4,1),4} = O_{4,1,1} + O_{4,2,2} + O_{4,3,3}$$

$$K_4^{V(4,1),4} = \frac{(p_1^2 + p_2^2 + p_3^2)(m_N(E(p) + m_N - p_3) + m_N(E(p) + m_N + p_3) + (E(p) - p_3)(E(p) + m_N - p_3) + (E(p) + p_3)(E(p) + m_N)}{(4E(p)(E(p) + m_N))}$$

(4, 2)

(Block 1) Trace = 0, Symmetric, C = -1

$$\begin{split} O_1^{V(4,2),1} &= O_{2,3,4} + O_{2,4,3} + O_{3,2,4} + O_{3,4,2} + O_{4,2,3} + O_{4,3,2} \\ K_1^{V(4,2),1} &= \frac{6p_2p_3(E(p)^2 + E(p)m_N)}{(E(p)(E(p) + m_N))} \end{split}$$

$$\begin{split} O_2^{V(4,2),1} &= O_{1,3,4} + O_{1,4,3} + O_{3,1,4} + O_{3,4,1} + O_{4,1,3} + O_{4,3,1} \\ K_2^{V(4,2),1} &= \frac{6p_1p_3(E(p)^2 + E(p)m_N)}{(E(p)(E(p) + m_N))} \end{split}$$

$$\begin{split} O_3^{V(4,2),1} &= O_{1,2,4} + O_{1,4,2} + O_{2,1,4} + O_{2,4,1} + O_{4,1,2} + O_{4,2,1} \\ K_3^{V(4,2),1} &= \frac{6p_1p_2(E(p)^2 + E(p)m_N)}{(E(p)(E(p) + m_N))} \end{split}$$

$$\begin{split} O_4^{V(4,2),1} &= O_{1,2,3} + O_{1,3,2} + O_{2,1,3} + O_{2,3,1} + O_{3,1,2} + O_{3,2,1} \\ K_4^{V(4,2),1} &= \frac{-6ip_1p_2p_3}{E(p)} \end{split}$$

(4, 4)

(Block 1) Trace = 0, Antisymmetric, C = 1

$$\begin{split} O_1^{V(4,4),1} &= O_{2,3,4} - O_{2,4,3} - O_{3,2,4} + O_{3,4,2} + O_{4,2,3} - O_{4,3,2} \\ K_1^{V(4,4),1} &= 0 \end{split}$$

$$\begin{split} O_2^{V(4,4),1} &= O_{1,3,4} - O_{1,4,3} - O_{3,1,4} + O_{3,4,1} + O_{4,1,3} - O_{4,3,1} \\ K_2^{V(4,4),1} &= 0 \end{split}$$

$$\begin{split} O_3^{V(4,4),1} &= O_{1,2,4} - O_{1,4,2} - O_{2,1,4} + O_{2,4,1} + O_{4,1,2} - O_{4,2,1} \\ K_3^{V(4,4),1} &= 0 \end{split}$$

$$\begin{split} O_4^{V(4,4),1} &= O_{1,2,3} - O_{1,3,2} - O_{2,1,3} + O_{2,3,1} + O_{3,1,2} - O_{3,2,1} \\ K_4^{V(4,4),1} &= 0 \end{split}$$

(8, 1)

(Block 1) Trace = 0, Mixed Symmetry, C = mixed

$$\begin{split} O_1^{V(8,1),1} &= O_{2,1,2} - O_{3,1,3}/2 - O_{4,1,4}/2 \\ K_1^{V(8,1),1} &= \frac{ip_1(-E(p)^3 - E(p)m_N^2 - E(p)p_1^2 - 5E(p)p_2^2 + E(p)p_3^2 - 2m_N^3 - 2m_Np_1^2 - 6m_Np_2^2)}{(4E(p)(E(p) + m_N))} \end{split}$$

$$\begin{split} O_2^{V(8,1),1} &= O_{1,2,1} - O_{3,2,3}/2 - O_{4,2,4}/2 \\ K_2^{V(8,1),1} &= \frac{ip_2(-E(p)^3 - E(p)m_N^2 - 5E(p)p_1^2 - E(p)p_2^2 + E(p)p_3^2 - 2m_N^3 - 6m_Np_1^2 - 2m_Np_2^2)}{(4E(p)(E(p) + m_N))} \end{split}$$

$$\begin{split} O_3^{V(8,1),1} &= O_{1,3,1} + O_{2,3,2} - 2O_{4,3,4} \\ K_3^{V(8,1),1} &= \frac{ip_3(-E(p)^3 - E(p)m_N^2 - 2E(p)p_1^2 - 2E(p)p_2^2 - E(p)p_3^2 - 2m_N^3 - 3m_Np_1^2 - 3m_Np_2^2 - 2m_Np_3^2)}{(E(p)(E(p) + m_N))} \end{split}$$

$$\begin{split} O_4^{V(8,1),1} &= O_{1,4,1} + O_{2,4,2} - 2O_{3,4,3} \\ K_4^{V(8,1),1} &= p_1^2 + p_2^2 - 2p_3^2 \end{split}$$

$$\begin{split} O_5^{V(8,1),1} &= O_{3,1,3} - O_{4,1,4} \\ K_5^{V(8,1),1} &= \frac{-ip_1(E(p)^3 + 2E(p)^2m_N + E(p)m_N^2 + E(p)p_1^2 + E(p)p_2^2 + 3E(p)p_3^2 + 2m_Np_3^2)}{(2E(p)(E(p) + m_N))} \end{split}$$

$$\begin{split} O_6^{V(8,1),1} &= O_{3,2,3} - O_{4,2,4} \\ K_6^{V(8,1),1} &= \frac{-ip_2(E(p)^3 + 2E(p)^2m_N + E(p)m_N^2 + E(p)p_1^2 + E(p)p_2^2 + 3E(p)p_3^2 + 2m_Np_3^2)}{(2E(p)(E(p) + m_N))} \end{split}$$

$$O_7^{V(8,1),1} = O_{1,3,1} - O_{2,3,2}$$

$$K_7^{V(8,1),1} = \frac{ip_3(-p_1^2 + p_2^2)}{E(p)}$$

$$\begin{split} O_8^{V(8,1),1} &= O_{1,4,1} - O_{2,4,2} \\ K_8^{V(8,1),1} &= p_1^2 - p_2^2 \end{split}$$

(Block 2) Trace = 0, Mixed Symmetry, C = mixed

$$\begin{split} O_1^{V(8,1),2} &= O_{2,2,1} - O_{3,3,1}/2 - O_{4,4,1}/2 \\ K_1^{V(8,1),2} &= \frac{ip_1(-E(p)^3 - E(p)m_N^2 - E(p)p_1^2 - 5E(p)p_2^2 + E(p)p_3^2 - 2m_N^3 - 2m_Np_1^2 - 6m_Np_2^2)}{(4E(p)(E(p) + m_N))} \end{split}$$

$$\begin{split} O_2^{V(8,1),2} &= O_{1,1,2} - O_{3,3,2}/2 - O_{4,4,2}/2 \\ K_2^{V(8,1),2} &= \frac{ip_2(-E(p)^3 - E(p)m_N^2 - 5E(p)p_1^2 - E(p)p_2^2 + E(p)p_3^2 - 2m_N^3 - 6m_Np_1^2 - 2m_Np_2^2)}{(4E(p)(E(p) + m_N))} \end{split}$$

$$\begin{split} O_3^{V(8,1),2} &= O_{1,1,3} + O_{2,2,3} - 2O_{4,4,3} \\ K_3^{V(8,1),2} &= \frac{ip_3(-E(p)^3 - E(p)m_N^2 - 2E(p)p_1^2 - 2E(p)p_2^2 - E(p)p_3^2 - 2m_N^3 - 3m_Np_1^2 - 3m_Np_2^2 - 2m_Np_3^2)}{(E(p)(E(p) + m_N))} \end{split}$$

$$\begin{split} O_4^{V(8,1),2} &= O_{1,1,4} + O_{2,2,4} - 2O_{3,3,4} \\ K_4^{V(8,1),2} &= p_1^2 + p_2^2 - 2p_3^2 \end{split}$$

$$\begin{split} O_5^{V(8,1),2} &= O_{3,3,1} - O_{4,4,1} \\ K_5^{V(8,1),2} &= \frac{-ip_1(E(p)^3 + 2E(p)^2m_N + E(p)m_N^2 + E(p)p_1^2 + E(p)p_2^2 + 3E(p)p_3^2 + 2m_Np_3^2)}{(2E(p)(E(p) + m_N))} \end{split}$$

$$\begin{split} O_6^{V(8,1),2} &= O_{3,3,2} - O_{4,4,2} \\ K_6^{V(8,1),2} &= \frac{-ip_2(E(p)^3 + 2E(p)^2m_N + E(p)m_N^2 + E(p)p_1^2 + E(p)p_2^2 + 3E(p)p_3^2 + 2m_Np_3^2)}{(2E(p)(E(p) + m_N))} \end{split}$$

$$\begin{split} O_7^{V(8,1),2} &= O_{1,1,3} - O_{2,2,3} \\ K_7^{V(8,1),2} &= \frac{ip_3(-p_1^2 + p_2^2)}{E(p)} \end{split}$$

$$O_8^{V(8,1),2} = O_{1,1,4} - O_{2,2,4}$$

 $K_8^{V(8,1),2} = p_1^2 - p_2^2$

(Block 3) Trace = 0, Mixed Symmetry, C = -1

$$\begin{split} O_1^{V(8,1),3} &= O_{1,2,2} - O_{1,3,3}/2 - O_{1,4,4}/2 \\ K_1^{V(8,1),3} &= \frac{-ip_1(m_N^2 + p_1^2 + 3p_2^2)}{(2E(p))} \end{split}$$

$$\begin{split} O_2^{V(8,1),3} &= O_{2,1,1} - O_{2,3,3}/2 - O_{2,4,4}/2 \\ K_2^{V(8,1),3} &= \frac{-ip_2(m_N^2 + 3p_1^2 + p_2^2)}{(2E(p))} \end{split}$$

$$\begin{split} O_3^{V(8,1),3} &= O_{3,1,1} + O_{3,2,2} - 2O_{3,4,4} \\ K_3^{V(8,1),3} &= \frac{-ip_3(2m_N^2 + 3p_1^2 + 3p_2^2 + 2p_3^2)}{E(p)} \end{split}$$

$$\begin{split} O_4^{V(8,1),3} &= O_{4,1,1} + O_{4,2,2} - 2O_{4,3,3} \\ K_4^{V(8,1),3} &= \frac{(p_1^2 + p_2^2 - 2p_3^2)(m_N(E(p) + m_N - p_3) + m_N(E(p) + m_N + p_3) + (E(p) - p_3)(E(p) + m_N - p_3) + (E(p) + p_3)(E(p) + m_N)}{(4E(p)(E(p) + m_N))} \end{split}$$

$$\begin{split} O_5^{V(8,1),3} &= O_{1,3,3} - O_{1,4,4} \\ K_5^{V(8,1),3} &= \frac{-ip_1(m_N^2 + p_1^2 + p_2^2 + 2p_3^2)}{E(p)} \end{split}$$

$$\begin{split} O_6^{V(8,1),3} &= O_{2,3,3} - O_{2,4,4} \\ K_6^{V(8,1),3} &= \frac{-ip_2(m_N^2 + p_1^2 + p_2^2 + 2p_3^2)}{E(p)} \end{split}$$

$$\begin{split} O_7^{V(8,1),3} &= O_{3,1,1} - O_{3,2,2} \\ K_7^{V(8,1),3} &= \frac{i p_3 (-p_1^2 + p_2^2)}{E(p)} \end{split}$$

$$\begin{split} O_8^{V(8,1),3} &= O_{4,1,1} - O_{4,2,2} \\ K_8^{V(8,1),3} &= \frac{(p_1^2 - p_2^2)(m_N(E(p) + m_N - p_3) + m_N(E(p) + m_N + p_3) + (E(p) - p_3)(E(p) + m_N - p_3) + (E(p) + p_3)(E(p) + m_N + p_3) + (E(p) - p_3)(E(p) + m_N + p_3) + (E$$

(8, 2)

(Block 1) Trace = 0, Mixed Symmetry, C = mixed

$$O_1^{V(8,2),1} = O_{2,3,4} + O_{2,4,3} - O_{3,2,4} - O_{4,2,3}$$

$$K_1^{V(8,2),1} = 0$$

$$\begin{split} O_2^{V(8,2),1} &= O_{1,3,4} + O_{1,4,3} - O_{3,1,4} - O_{4,1,3} \\ K_2^{V(8,2),1} &= 0 \end{split}$$

$$\begin{split} O_3^{V(8,2),1} &= O_{1,4,2} + O_{2,4,1} - O_{4,1,2} - O_{4,2,1} \\ K_3^{V(8,2),1} &= 0 \end{split}$$

$$\begin{split} O_4^{V(8,2),1} &= O_{1,3,2} + O_{2,3,1} - O_{3,1,2} - O_{3,2,1} \\ K_4^{V(8,2),1} &= 0 \end{split}$$

$$\begin{split} O_5^{V(8,2),1} &= O_{2,3,4} - O_{2,4,3} - O_{3,2,4} - 2O_{3,4,2} + O_{4,2,3} + 2O_{4,3,2} \\ K_5^{V(8,2),1} &= 0 \end{split}$$

$$\begin{split} O_6^{V(8,2),1} &= O_{1,3,4} - O_{1,4,3} - O_{3,1,4} - 2O_{3,4,1} + O_{4,1,3} + 2O_{4,3,1} \\ K_6^{V(8,2),1} &= 0 \end{split}$$

$$\begin{split} O_7^{V(8,2),1} &= O_{1,2,4} + O_{1,4,2}/2 - O_{2,1,4} - O_{2,4,1}/2 - O_{4,1,2}/2 + O_{4,2,1}/2 \\ K_7^{V(8,2),1} &= 0 \end{split}$$

$$\begin{split} O_8^{V(8,2),1} &= O_{1,2,3} + O_{1,3,2}/2 - O_{2,1,3} - O_{2,3,1}/2 - O_{3,1,2}/2 + O_{3,2,1}/2 \\ K_8^{V(8,2),1} &= 0 \end{split}$$

(Block 2) Trace = 0, Mixed Symmetry, C = mixed

$$\begin{split} O_1^{V(8,2),2} &= O_{2,3,4} + O_{2,4,3} - O_{3,4,2} - O_{4,3,2} \\ K_1^{V(8,2),2} &= 0 \end{split}$$

$$\begin{split} O_2^{V(8,2),2} &= O_{1,3,4} + O_{1,4,3} - O_{3,4,1} - O_{4,3,1} \\ K_2^{V(8,2),2} &= 0 \end{split}$$

$$\begin{split} O_3^{V(8,2),2} &= O_{1,2,4} + O_{2,1,4} - O_{4,1,2} - O_{4,2,1} \\ K_3^{V(8,2),2} &= 0 \end{split}$$

$$\begin{split} O_4^{V(8,2),2} &= O_{1,2,3} + O_{2,1,3} - O_{3,1,2} - O_{3,2,1} \\ K_4^{V(8,2),2} &= 0 \end{split}$$

$$\begin{split} O_5^{V(8,2),2} &= O_{2,3,4} - O_{2,4,3} + 2O_{3,2,4} + O_{3,4,2} - 2O_{4,2,3} - O_{4,3,2} \\ K_5^{V(8,2),2} &= 0 \end{split}$$

$$O_6^{V(8,2),2} = O_{1,3,4} - O_{1,4,3} + 2O_{3,1,4} + O_{3,4,1} - 2O_{4,1,3} - O_{4,3,1}$$

$$K_6^{V(8,2),2} = 0$$

$$\begin{split} O_7^{V(8,2),2} &= O_{1,2,4} + 2O_{1,4,2} - O_{2,1,4} - 2O_{2,4,1} + O_{4,1,2} - O_{4,2,1} \\ K_7^{V(8,2),2} &= 0 \end{split}$$

$$\begin{split} O_8^{V(8,2),2} &= O_{1,2,3} + 2O_{1,3,2} - O_{2,1,3} - 2O_{2,3,1} + O_{3,1,2} - O_{3,2,1} \\ K_8^{V(8,2),2} &= 0 \end{split}$$