

# Chapter # 04

$$\textcircled{1} \quad \vec{V}_{\text{avg}} = \frac{\Delta d}{\Delta t} = \left( \frac{d_1 + d_2 + d_3}{t_1 + t_2 + t_3} \right)$$

$$\textcircled{2} \quad \vec{V}_{\text{ins}} = \lim_{\Delta t \rightarrow 0} \frac{\Delta d}{\Delta t} \rightarrow \begin{matrix} \text{derivative of } d \\ \text{w.r.t time} \end{matrix}$$

$$\textcircled{3} \quad \vec{a}_{\text{avg}} = \frac{\Delta V}{\Delta t}$$

$$\textcircled{4} \quad \vec{a}_{\text{ins}} = \lim_{\Delta t \rightarrow 0} \frac{\Delta V}{\Delta t}$$

$$|V_{\text{avg}}| = \sqrt{V_x^2 + V_y^2 + V_z^2}$$

$$\vec{V}_{\text{net}} = \vec{V}_1 + \vec{V}_2 + \vec{V}_3 + \dots$$

↑ sign vary  
Speed =  $\frac{V_{\text{total}}}{\text{time}}$

Equation of uniformly accelerated motions

$$1) \quad V_f = V_i + at$$

$$2) \quad S = V_i t + \frac{1}{2} a t^2$$

$$3) \quad aS = V_f^2 - V_i^2$$

Projectile motion  $\rightarrow$  2-D motion

↳ launched with an initial velocity  $V_i$  at an angle  $\theta$  w.r.t horizontal axis

↳ horizontal axis ( $x$ -axis)

↳ vertical axis ( $y$ -axis)

↳ no air resistance

↳  $g = \text{constant} = 9.8 \text{ m/s}^2$

→ horizontal motion = no acceleration

→ vertical motion =  $-g$

→ initial velocity at an angle  $\theta$   
    always  
    ↳ resolve into  
        components

①  $V_{ix} = V_i \cos \theta$  ( $\because a_x = A \cos \theta$ )  
    ②  $V_{iy} = V_i \sin \theta$  ( $\because a_y = A \sin \theta$ )

③ Always draw triangle.

④  $X = V_{ix} \cdot t$

⑤  $Y = V_{iy} \cdot t + \frac{1}{2} g t^2$  } General Case

⑥  $Y = V_{iy}t - \frac{1}{2} g t^2$  } against gravity  
    ↳ if  $V_{iy} < 0$

⑦  $Y = \frac{1}{2} g t^2$  } if projectile is dropped  
    from a height

⑧ Throw horizontally  $\Rightarrow V_y = 0$

so  $Y = \frac{1}{2} g t^2$

⑨  $a_x = 0$

⑩  $a_y = g$  or  $-g$

depends upon statement

$\Rightarrow S = V_i t + \frac{1}{2} a t^2$

$\downarrow$   
 $X = V_{ix} t + \frac{1}{2} a_{ix} t^2$

$X = V_{ix} t$

$g = -ve$   
 $g = +ve$

$\downarrow$   
 $Y = V_{iy} t + \frac{1}{2} a_{iy} t^2$

$\boxed{Y = V_{iy} t + \frac{1}{2} g t^2}$

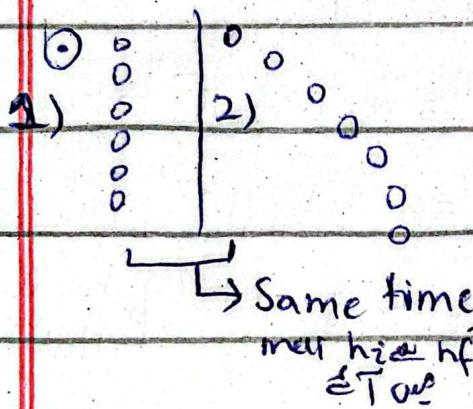
$\downarrow$   
 $Y = V_{iy} t - \frac{1}{2} g t^2$

$\downarrow$   
depends upon statement.

- ✓ ①  $y - y_i = v_{iy} t - \frac{1}{2} g t^2$  ] if launched through some specific height -  
 @ similarly  $x - x_i = v_{ix} t$  also to find initial height.
- ② Trajectory ( $\equiv$  path of particle) in projectile motion is parabolic.

$$③ \vec{v}_i = v_{ix} \hat{i} + v_{iy} \hat{j}$$

- ④ In projectile motion the horizontal motion and the vertical motion are independent of each other.



- ⑤ At highest point  $v_y = 0$   
 ⑥ Before the highest point (top)  $\Rightarrow v_y > 0$   
 ⑦ After the highest point (top)  $\Rightarrow v_y < 0$

⑧ At launch ( $t=0$ )  $\Rightarrow v_{iy} = v_{i\text{initial}}$

⑨ At time  $t$  (after launch)  $\Rightarrow v_y = v_{i\text{initial}} - gt$   
 ↴ decreases due to gravity

⑩ At launch ( $t=0$ )  $\Rightarrow v_{ix} = v_{i\cos\theta}$  ) same

⑪ At time  $t$   $\rightarrow v_{ix} = v_{i\cos\theta}$

be there is no gravity or air resistance in horizontal motion

In short  $v_{ix}$  never changes

- ⑫ Relected from a plane = its velocity assume as plane

- ⑬ Shot from plane = its velocity will be something else..

Angle  $\theta$  north of east = east w/north  
 $\rightarrow \theta$

Speedometer of car measures speed (magnitude of velocity)

if &  $v_i$  is given  $\rightarrow$  Height of Projectile:

$$H = \frac{v_i^2 \sin^2 \theta}{2g}$$

$$\therefore 2as = v_f^2 - v_i^2$$

$$a = -g$$

$$v_{fy} = 0$$

$$v_{ix} = v_i \cos \theta$$

$$S = H$$

$\rightarrow$  Time of Flight:

The time taken by the body to cover the distance from the place of its projection to place where it hits the ground at the same level is called TOF.

or Time In Air

$$T = \frac{2v_i \sin \theta}{g}$$

$$\therefore S = v_i t + \frac{1}{2} g t^2$$

$\rightarrow$  Range of Projectile:

Maximum distance which a projectile covers in the horizontal direction is called range of the projectile.

$$R = v_{ix} \cdot T$$

$$R = \frac{v_i^2 \sin 2\theta}{g}$$

## Uniform Circular Motion (UCM)

→ 2D

→ obj moves around circle at const speed

→ speed = uniform

→  $\vec{V}$  ≠ uniform bc direction changes

→  $|V|$  = uniform.

→ centrepetal acce.  $\rightarrow a = \frac{V^2}{r}$

→ 1 circle circumference in time T is

$$T = \frac{2\pi r}{V}$$

→ T = Period for exactly once

$$T = \frac{\theta}{\omega}$$

$$\text{speed } V = \frac{2\pi r}{T}$$