

Assignment 03

Group members:

21k-3881

21k-3897

21k-3911

day/date

Assignment 3 21K-3887, 21K-3897, 21K-3911

a) $X = \{B, T, C, A, B, A\}$ Member 1: Taha
 $Y = \{U, B, C, B, D, A, B\}$ Member 2: Subeh

	B	T	C	A	B	A
U	0	0	0	0	0	0
B	1	1	1	1	1	1
C	0	1	1	2	2	2
B	0	1	1	2	2	3
D	0	1	1	2	2	3
A	0	1	1	2	2	3
B	0	1	1	2	2	3

LCS: B, C, B, A

b) X : Taha LCS Y : Subeh

	T	A	h	a
S	0	0	0	0
U	0	0	0	0
b	0	0	0	0
e	0	0	0	0
h	0	0	0	0

$\therefore X + Y - LCS$

$= 8$ SubeTaha

day/date

21K-3897 21K-38911 21K-3881

C) arr[] = {7, 10, 2, 1, 20} 3897, 38911

temp[] = {1, 1, 1, 1, 1}

$\begin{matrix} j & i \\ 7, & 10, & 2, & 1, & 20 \end{matrix}$

$7 < 10$

$\Rightarrow temp[1] = temp[0] + 1$ (1, 2, 1, 1, 1)

$\begin{matrix} j & i \\ 7, & 10, & 2, & 1, & 20 \end{matrix}$

$7 < 2$

$10 < 2$

$\begin{matrix} j & i \\ 7, & 10, & 2, & 1, & 20 \end{matrix}$

$7 < 1$

$10 < 1$

$2 < 1$

~~7~~ $\begin{matrix} j & i \\ 7, & 10, & 2, & 1, & 20 \end{matrix}$

~~7~~ $7 < 20$

$temp[4] = temp[0] + 1$ (1, 2, 1, 1, 2)

$10 < 20$

$temp[4] = temp[1] + 1$ (1, 2, 1, 1, 3)

$2 < 20$ but $temp[2] + 1$ \Rightarrow ~~Temp[4]~~
 $1 < 20$ " " [3] " "

Ans: [1, 2, 1, 1, 3]

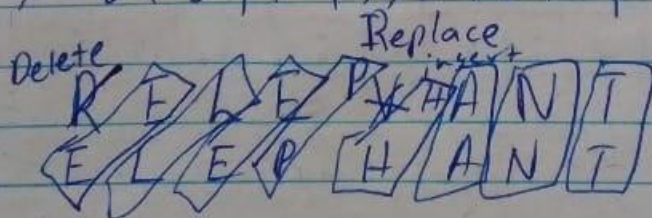
Max length ≥ 3

(d) "Levenshtein - distance"

$$D[i,j] = \min \begin{cases} D[i-1,j] + 1 & ; \text{Delete} \\ D[i,j-1] + 1 & ; \text{Insert} \\ D[i-1,j-1] + \text{cost} & ; \text{Replace} \end{cases}$$

String 1:- Elephant, String 2:- Relevant

		R	E	L	E	V	A	N	T
		1	2	3	4	5	6	7	8
E	1	1	1	2	3	4	5	6	7
L	2	2	2	1	2	3	4	5	6
E	3	3	2	2	1	2	3	4	5
P	4	4	3	3	2	2	3	4	5
H	5	5	4	4	3	3	3	4	5
A	6	6	5	5	4	4	3	4	5
N	7	7	6	6	5	5	4	3	4
T	8	8	7	7	6	6	5	4	3



Total Operations

1 Delete Operation

1 Replace "

1 Insert "

Part (c)

$$P_0 \times P_1 \times P_2 \times P_3 \times P_4 \times P_5 ; P_5 = \text{AMMAD}$$

$$P_5 = 5$$

$$\begin{array}{ccccc} A & \times & B & \times & C & \times & D & \times & E \\ p_0 \times p_1 & & p_1 \times p_2 & & p_2 \times p_3 & & p_3 \times p_4 & & p_4 \times p_5 \\ 2 \times 25 & & 25 \times 3 & & 3 \times 16 & & 16 \times 1 & & 1 \times 5 \end{array}$$

$$M[i, j] = \min \{ M[i, k] + M[k+1, j] + p_{i-1} p_k p_j \}$$

	A	B	C	D	E
A	0	150	246	173	183
B	0	0	1200	123	248
C	0	0	0	48	63
D	0	0	0	0	80
E	0	0	0	0	0

$$A \times B = 0 + 0 + 2 \times 25 \times 3 = 150$$

$$B \times C = 0 + 0 + 25 \times 3 \times 16 = 1200$$

$$C \times D = 0 + 0 + 3 \times 16 \times 1 = 48$$

$$D \times E = 0 + 0 + 16 \times 1 \times 5 = 80$$

$$ABC = (AB)C, A(BC)$$

$$\begin{array}{l} 150 + 0 + 0 + 2 \times 3 \times 16, 0 + 0 + 25 \times 16 \times 2 + 1200 \\ 246, 2000 \\ (2 \times 16) \end{array}$$

$$BCD = \underset{25 \times 16}{(BC)D}, \underset{16 \times 1}{B} \underset{1025 \times 3}{(CD)}$$

$$= 1200 + 00 + 25 \times 16 \times 1; 0 + 0 + 25 \times 3 \times 1 + 48$$

$$1600, 123$$

$$25 \times 1$$

$$CDE = \underset{3 \times 1}{(C)D} \underset{1 \times 5}{E}; \underset{3 \times 16}{C} \underset{16 \times 5}{(DE)}$$

$$48 + 00 + 3 \times 1 \times 5; 0 + 0 + 3 \times 16 \times 5 + 80$$

$$63; 320$$

$$3 \times 5$$

$$ABCD = \underset{2 \times 16}{(AB)C} \underset{16 \times 1}{D}, \underset{2 \times 25}{A} \underset{25 \times 1}{(BCD)}$$

$$246 + 0 + 0 + 2 \times 16 \times 1; 0 + 0 + 2 \times 25 \times 1 + 123$$

$$278, 173$$

$$2 \times 1$$

$$BCDE = \underset{25 \times 3}{B} \underset{3 \times 5}{(CDE)}; \underset{25 \times 1}{(BCD)} \underset{1 \times 5}{E}$$

$$0 + 0 + 25 \times 3 \times 5 + 63; 123 + 0 + 0 + 25 \times 1 \times 5$$

$$438; 248$$

$$25 \times 5$$

$$ABCDE = \underset{2 \times 1}{(ABCD)} \underset{1 \times 5}{E}, \underset{2 \times 25}{A} \underset{25 \times 5}{(BCDE)}$$

$$173 + 2 \times 1 \times 5 + 0 + 0; 0 + 0 + 2 \times 25 \times 5 + 248$$

$$183; 498$$

$$2 \times 5$$

21k-3881
21k-3891
21k-3897

f) Value = $V_i = \{1, 4, 5, 7, 4\}$
Weight = $W_i = \{1, 3, 4, 5, 2\}$
Capacity = $W = 9$

V_i	W_i	item no.	0	1	2	3	4	5	6	7	8	9
0	0	0	0	0	0	0	0	0	0	0	0	0
1	1	1	0	1	1	1	1	1	1	1	1	1
4	2	2	0	1	4	5	5	5	5	5	5	5
4	3	3	0	1	4	5	5	8	9	9	9	9
5	4	4	0	1	4	5	5	8	9	10	10	13
7	5	5	0	1	4	5	5	8	9	11	12	13

Formula:

$$V[i, w] = \max \{ V[i-1, w], V[i-1, w - w[i]] + P[i] \}$$

$$V[5, 8] = \max \{ V[4, 8], V[4, 8-5] + 7 \}$$

$$V[5, 8] = \max \{ 10, V[4, 3] + 7 \}$$

$$V[5, 8] = \max \{ 10, 5 + 7 \}$$

$$V[5, 8] = \max \{ 10, 12 \} = 12$$

$$X = \{0, 1, 1, 0, 1\} \text{ Ans}$$

DAA Assignment 3

Group Members:- 21K-3911, 21K-3897,
21K-3881

Names:- Muhammad Ammad, Sabeh Ansari, Taha Jawaid.

Question (g)

Algorithm:-

- 1) Accept names from the user.
- 2) Convert names to numbers:-
 - 2.1) Define a function `nam-to-numbers` which take a string and returns an Integer array.
 - 2.2) In the function iterate through the string and for each letter provide corresponding number ($A=1, B=2, Z=26$) and save that number in an Integer Array.
 - 2.3) After the String iteration is completed return the Integer Array.
- 3) Do the same for ~~second~~ second name.
- 4) Now take first 3 numbers from `nam1` and last 3 numbers from name 2 and combine them in a single Array named (Answer).

21k-3881
21k-3911
21k-3897

h) Length $[] = \{ 1, 2, 3, 4, 5, 6, 7, 8 \}$
Price $[] = \{ 1, 5, 8, 9, 10, 16, 18, 20 \}$

Rod length = 8

Cut	Profit
8	20
7, 1	$18 + 1 = 19$
6, 2	$16 + 5 = 21 \checkmark$
5, 3	$10 + 8 = 18$
4, 4	$9 + 9 = 18$
6, 1, 1	$16 + 1 + 1 = 18$
5, 2, 1	$10 + 5 + 1 = 16$
4, 3, 1	$9 + 8 + 1 = 18$
4, 2, 2	$9 + 5 + 5 = 19$
3, 3, 2	$8 + 8 + 5 = 21 \checkmark$
5, 1, 1, 1	$10 + 1 + 1 + 1 = 13$
4, 2, 1, 1	$9 + 5 + 1 + 1 = 16$
3, 3, 1, 1	$8 + 8 + 1 + 1 = 18$
3, 2, 2, 1	$8 + 5 + 5 + 1 = 19$
2, 2, 2, 2	$5 + 5 + 5 + 5 = 20$
4, 1, 1, 1, 1	$9 + 1 + 1 + 1 + 1 = 13$
3, 2, 1, 1, 1	$8 + 5 + 1 + 1 + 1 = 16$
2, 2, 2, 1, 1	$5 + 5 + 5 + 1 + 1 = 17$

21k-3881

21k-3911

21k-3897

3, 1, 1, 1, 1, 1

2, 2, 1, 1, 1, 1

2, 1, 1, 1, 1, 1, 1

1, 1, 1, 1, 1, 1, 1, 1

$$8 + 1 + 1 + 1 + 1 + 1 = 13$$

$$5 + 5 + 1 + 1 + 1 + 1 = 14$$

$$5 + 1 + 1 + 1 + 1 + 1 + 1 = 11$$

$$1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 = 8$$

⇒ Highest Profit of 21 in cuts 6, 2
and 3, 3, 2
Ans.

i) $S = \{1, 5, 6, 8\}$

Desired Change = 13

Possible Combinations:

$$\Rightarrow 8 + 5 = 13 \quad \leftarrow \text{Min} = 2 \text{ coins}$$

$$\Rightarrow 5 + 5 + 1 + 1 + 1 = 13$$

$$\Rightarrow 6 + 6 + 1 = 13$$

$$\Rightarrow 8 + 1 + 1 + 1 + 1 + 1 = 13$$

$$\Rightarrow 5 + 6 + 1 + 1 = 13$$

$$\Rightarrow 1 \times 13 = 13$$

$$\Rightarrow 6 + (1 \times 7) = 13$$

$$\Rightarrow 5 + (1 \times 8) = 13$$

∴ We will select 2 coins i.e. (8, 5)
to make the change 13
Ans.

