Task 1: Deriving the Private Key

```
GNU nano 4.8
                                                                                      task1.c
//K213881
#include <openssl/bn.h>
#include <stdio.h>
void printBN(char *msg, BIGNUM * a) {
    char *number_str = BN_bn2hex(a);
printf("%s %s\n", msg, number_str);
     OPENSSL_free(number_str);
int main() {
    BN_CTX *ctx = BN_CTX_new();
     BIGNUM *p = BN_new();
    BIGNUM *q = BN_new();
BIGNUM *e = BN_new();
    BIGNUM *n = BN_new();
    BIGNUM *phi = BN_new();
BIGNUM *d = BN_new();
    BIGNUM *one = BN_new();
    BN_hex2bn(&p, "F7E75FDC469067FFDC4E847C51F452DF");
BN_hex2bn(&q, "E85CED54AF57E53E092113E62F436F4F");
BN_hex2bn(&e, "OD88C3");
    BN dec2bn(&one, "1");
    BN_mul(n, p, q, ctx);
//printBN("n = ", n);
                                                                                                  task1.c
 GNU nano 4.8
     BIGNUM *p = BN_new();
     BIGNUM *q = BN_new();
     BIGNUM *e = BN_new();
     BIGNUM *n = BN new();
     BIGNUM *phi = BN_new();
     BIGNUM *d = BN_new();
     BIGNUM *one = BN new();
     BN_hex2bn(&p, "F7E75FDC469067FFDC4E847C51F452DF");
BN_hex2bn(&q, "E85CED54AF57E53E092113E62F436F4F");
BN_hex2bn(&e, "0D88C3");
     BN_dec2bn(&one, "1");
     BN_mul(n, p, q, ctx);
//printBN("n = ", n);
     BIGNUM *p1 = BN new();
     BIGNUM *q1 = BN_new();
     BN_sub(p1, p, one);
     BN_sub(q1, q, one);
BN_mul(phi, p1, q1, ctx);
BN_mod_inverse(d, e, phi, ctx);
printBN("private key d = ", d);
return 0;
```

```
seed@VM: ~/.../k213881_Assignment-2
[10/18/24]seed@VM: ~/.../k213881_Assignment-2$ nano taskl.c
[10/18/24]seed@VM: ~/.../k213881_Assignment-2$ gcc taskl.c -o taskl -lcrypto
[10/18/24]seed@VM: ~/.../k213881_Assignment-2$ ./taskl
private key d = 3587A24598E5F2A21DB007D89D18CC50ABA5075BA19A33890FE7C28A9B496AEB
[10/18/24]seed@VM: ~/.../k213881_Assignment-2$
```

Task 2: Encrypting a Message

```
GNU nano 4.8
// k213881
#include <openssl/bn.h>
#include <stdio.h>

void printBN(char *msg, BIGNUM *a) {
    char *number_str = BN_bn2hex(a);
    printf("%s %sh," msg, number_str);
    OPENSSL_free(number_str);
}

int main() {
    BM_CTX *ctx = BN_CCTX_new();
    BIGNUM *n = BN_new();
    BIGNUM *e = BN_new();
    BIGNUM *e = BN_new();
    BIGNUM *e = BN_new();
    BIGNUM *c = BN_new();
    BIGNUM *c = BN_new();
    BN_hex2bn(&n, "DCBFFE3E51F62209CE7032E2677A79864A89D4C4DDE3A4D0BC88162924F81A5");
    BN_hex2bn(&e, "010001");
    BN_hex2bn(&e, "12074f70207356372567421");
    BN_mod_exp(c, m, e, n, ctx);
    prīntBN("Ciphertext = ", c);
    return 0;
}
```

```
seed@VM:~/.../k213881_Assignment-2
[10/18/24]seed@VM:~/.../k213881_Assignment-2$ nano task2.c
[10/18/24]seed@VM:~/.../k213881_Assignment-2$ gcc task2.c -o task2 -lcrypto
[10/18/24]seed@VM:~/.../k213881_Assignment-2$ ./task2
Ciphertext = 042B5A5A00312EC413028808F16B5EE5D0710F1C027B409E4E8F3A473D859B1F
[10/18/24]seed@VM:~/.../k213881_Assignment-2$ ]
```

Task 3: Decrypting a Message

```
seed@VM: ~/.../k213881_Assignment-2
 GNU nano 4.8
                                                                                                                          task3.c
  // k213881
 #include <openssl/bn.h>
 #include <stdio.h>
  void printBN(char *msg, BIGNUM *a) {
        char *number_str = BN_bn2hex(a);
printf("%s %s\n", msg, number_str);
        OPENSSL_free(number_str);
 int main() {
        BN_CTX *ctx = BN_CTX_new();
        BIGNUM *n = BN_new();
        BIGNUM *d = BN new();
        BIGNUM *c = BN new();
        BIGNUM *m = BN_new();
       BN_hex2bn(&n, "DCBFFE3E51F62209CE7032E2677A79864A89D4C4DDE3A4D0CB81629242FB1A5");
BN_hex2bn(&d, "74D8069F5A3C182DE2E4794148AABC26AA381CD7D30D");
BN_hex2bn(&c, "80CF971F2F63782881107241DE5ABDB0E7BABBFD7C7DCB67396567EA1E2493F");
        BN_mod_exp(m, c, d, n, ctx);
        printBN("Decrypted message = ", m);
        return 0;
                                                                               seed@VM: ~/.../k213881_Assignment-2
                                                                                                                                                                           Q = - 0
[10/18/24]seed@VM:-/.../k213881_Assignment-2$ nano task3.c

[10/18/24]seed@VM:-/.../k213881_Assignment-2$ gcc task3.c -o task3 -lcrypto

[10/18/24]seed@VM:-/.../k213881_Assignment-2$ ./task3

Decrypted message = 06C9AC887E04A7V483AZE92D801102F547453CF4A13A3F151E647EC84DBAB96452

[10/18/24]seed@VM:-/.../k213881_Assignment-2$ ■
```

Task 4: Signing a Message

```
GNU nano 4.8
                                                                            task4.c
    char *number str = BN bn2hex(a);
    printf("%s %s\n", msg, number_str);
    OPENSSL_free(number_str);
int main() {
    BN_CTX *ctx = BN CTX new();
    BIGNUM *n = BN new();
    BIGNUM *d = BN new();
    BIGNUM *m = BN_new();
    BIGNUM *s = BN new();
    BN_hex2bn(\&n, "DCBFFE3E51F62209CE7032E2677A79864A89D4C4DDE3A4D0CB81629242FB1A5"); \\ BN_hex2bn(\&d, "74D8069F5A3C182DE2E4794148AABC26AA381CD7D30D"); \\
    BN hex2bn(&m, "49206f776520796f75202432303030"); // "I owe you $2000." in hex
    BN_mod_exp(s, m, d, n, ctx);
    printBN("(I owe you $2000) Signature = ", s);
    // Now change the message to "I owe you $3000." and sign again
    BN hex2bn(&m, "49206f776520796f75202433303030"); // "I owe you $3000." in hex
    BN_mod_exp(s, m, d, n, ctx);
    printBN("(I owe you $3000) Signature = ", s);
    return 0;
                                                                    [ Wrote 32 lines ]
```

Description:

In this task, the original message "I owe you \$2000." is signed using RSA, and then a modified version of the message ("I owe you \$3000.") is also signed. Upon comparing the

signatures of the two messages, the signatures are completely different. This is because RSA signatures are generated based on the exact content of the message, so even a small change, such as modifying "\$2000" to \$3000," results in a different hash value and thus a different signature. This behaviour demonstrates the integrity protection offered by digital signatures, ensuring that even minor changes to the original message can be detected, making it tamper-evident.

Task 5: Verifying a Signature

```
task5.c
GNU nano 4.8
//k213881
#include <openssl/bn.h>
#include <stdio.h>
void printBN(char *msg, BIGNUM *a) {
   char *number_str = BN_bn2hex(a);
    printf("%s %s\n", msg, number_str);
   OPENSSL free(number str);
int main() {
   BN_CTX *ctx = BN_CTX_new();
   BIGNUM *n = BN new();
   BIGNUM *e = BN_new();
   BIGNUM *s = BN new();
   BIGNUM *m verify = BN new();
   BIGNUM *expected_m = BN_new();
   BN hex2bn(&n, "AE1CD4DC432379B97FD846CE1C4720559F1233955113AA51B450F18116115");
   BN_hex2bn(&e, "010001");
   BN hex2bn(&s, "643D6F3490209C7EC9C0B2BCA36C47FA37165C0005CAB026C0542CBD6802F");
   BN hex2bn(&expected_m, "4C61756E63682061206D697373696C652E");
   printf("original signature: 643D6F3490209C7EC9C0B2BCA36C47FA37165C0005CAB026C0542CBD6802F\n");
   BN mod exp(m verify, s, e, n, ctx);
   printBN("Recovered message (original) = ", m_verify);
                                                              [ Wrote 49 lines ]
```

```
GNU nano 4.8
                                                                     task5.c
   printf("original signature: 643D6F3490209C7EC9C0B2BCA36C47FA37165C0005CAB026C0542CBD6802F\n");
   BN mod exp(m verify, s, e, n, ctx);
   printBN("Recovered message (original) = ", m_verify);
  (BN_cmp(m_verify, expected_m) == 0) {
   printf("The signature is valid for the original message.\n");
 else {
   printf("The signature is NOT valid for the original message.\n");
BIGNUM *s corrupted = BN new();
BN hex2bn(&s corrupted, "643D6F3490209C7EC9C0B2BCA36C47FA37165C0005CAB026C0542CBD6803F");
printf("Modified signature (2F -> 3F): 643D6F3490209C7EC9C0B2BCA36C47FA37165C0005CAB026C0542CBD6803F\n");
BN_mod_exp(m_verify, s_corrupted, e, n, ctx);
printBN("Recovered message (corrupted) = ", m verify);
  (BN_cmp(m_verify, expected_m) == 0) {
   printf("The corrupted signature is still valid for the message.\n");
   printf("The corrupted signature is NOT valid for the message.\n");
return 0;
```

```
| Seed@VM:-/.../k213881_Assignment-2$ nano task5.c
| 10/18/24|seed@VM:-/.../k213881_Assignment-2$; gcc task5.c -o task5 -lcrypto
| 10/18/24|seed@VM:-/.../k213881_Assignment-2$; /task5
| original signature: 643D6F3490209C7EC9C0B2BCA36C47FA37165C0005CAB026C0542CBD6802F
| Recovered message (original) = 0A3A7E027E699FBAAC4B2C6BD584E08106BE45190F9123E75F53812B2F258
| The signature is NOT valid for the original message.
| Modified signature (2F -> 3F): 643D6F3490209C7EC9C08D2BCA36C47FA37165C0005CAB026C0542CBD6803F
| Recovered message (corrupted) = 049A2CFFFFB3BAC888F5A44CCD70A2AD4A4D039903BAFB36C14F43A2B2C866
| The corrupted signature is NOT valid for the message.
| The corrupted signature is NOT valid for the message.
| The corrupted signature is NOT valid for the message.
| The corrupted signature is NOT valid for the message.
| The corrupted signature is NOT valid for the message.
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| The corrupted signature is NOT valid for the message.
| The corrupted signature is NOT valid for the message.
| The corrupted signature is NOT valid for the message.
| The corrupted signature is NOT va
```

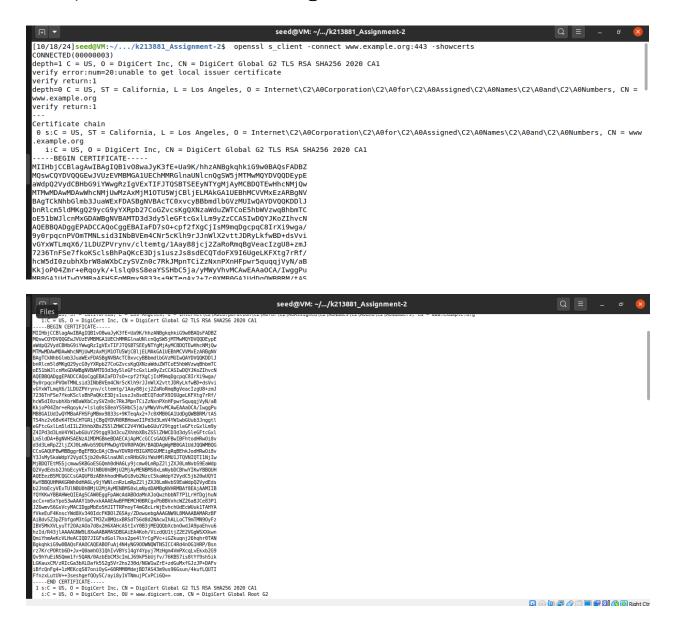
Description:

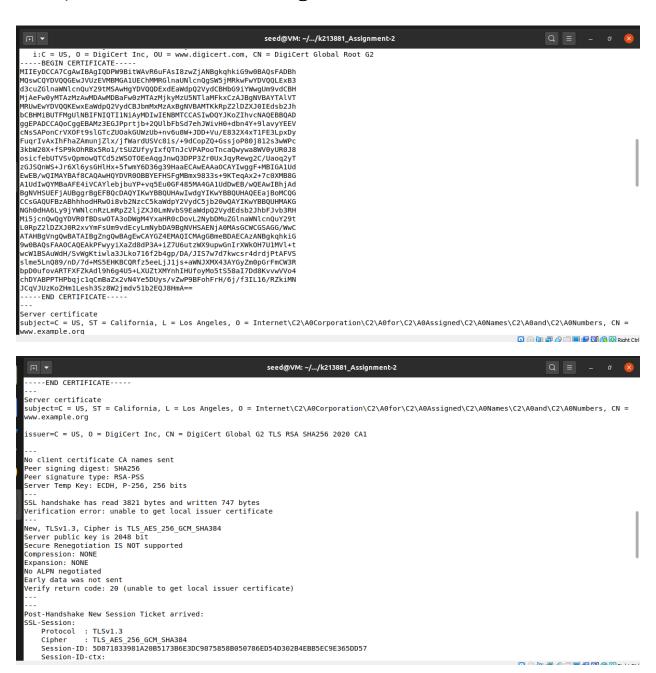
When Bob verifies Alice's signature on the message "Launch a missile." with the correct public key, the verification succeeds if the signature is unaltered. However, when the last byte of the signature changed from 2F to 3F, the verification fails. This is because even a tiny alteration in the signature disrupts the cryptographic process, causing the signature to no longer match the message. This demonstrates how RSA ensures message integrity, as any modification to the signature or message will result in verification failure, providing strong tamper detection.

Task 6: Manually Verifying an X.509 Certificate

Major steps to follow in this tasks are:

- The objective of this task is to manually authenticate an X.509 certificate by
 obtaining the public key and signature from the certificate and confirming the
 signature's validity. This process includes downloading a certificate from a website,
 extracting necessary details, and validating the certificate using the issuer's public
 key.
- X.509 Certificates utilize public key infrastructure (PKI) to confirm the legitimacy of a server or individual.
- We will retrieve a certificate from the web server using the openssl s_client command, specifically from www.example.org.
- The initial certificate (labeled 0) is the server's certificate, while the subsequent one (labeled 1) is the issuer's certificate.
- Save these two certificates into separate files: the server certificate as server_cert.pem and the issuer's certificate as issuer_cert.pem.
- Extract the public key from the issuer's certificate.
- Extract the modulus component of the public key.
- Display the entire certificate to identify the public exponent e.
- Extract the signature from the server's certificate.
- The signature will be found under the Signature Algorithm section.
- Copy the entire signature and save it to a file named signature.txt.
- Extract the main body of the server's certificate. For verification, the hash is calculated based on the certificate's body.
- The main body of the certificate will be saved as server_body.bin, which will be used to generate the hash.
- The signature is created by hashing the certificate body first, then encrypting the hash with the CA's private key.
- Check the signature. If the signature is valid, the decrypted signature will match the hash computed from the certificate body. Otherwise, the signature may be corrupted or the certificate has been altered.

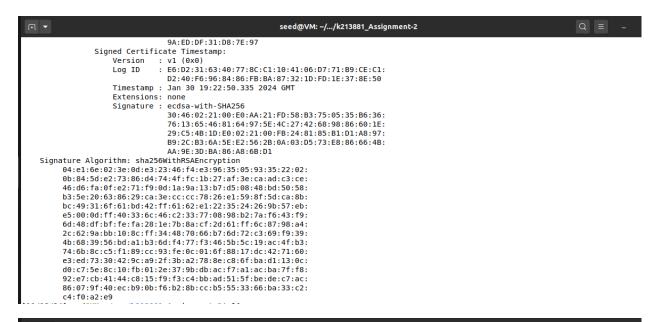




X509v3 Subject Key Identifier:

4C:FE:D0:12:4D:2E:21:CF:6B:FA:F2:F2:B8:4C:49:02:1D:31:91:8A

```
Q = - 0
                                                                                          seed@VM: ~/.../k213881 Assignment-2
 closed
Closed
[10/18/24]seed@VM:-/.../k213881_Assignment-2$ nano server_cert.pem
[10/18/24]seed@VM:-/.../k213881_Assignment-2$ nano server_cert.pem
[10/18/24]seed@VM:-/.../k213881_Assignment-2$ nano server_cert.pem
[10/18/24]seed@VM:-/.../k213881_Assignment-2$ nano issuer_cert.pem
[10/18/24]seed@VM:-/.../k213881_Assignment-2$ nano issuer_cert.pem
[10/18/24]seed@VM:-/.../k213881_Assignment-2$ openss( x509 -in issuer_cert.pem
-noout -modulus
Modulus=CCF710624FA6BB636FED905256C56D277B7A12568AF1F4F9D6E7E18FBD95ABF260411570DB1200FA270AB557385B7DB2519371950E6A41945B351BFA7BFABBC5BE2430
FES6EFC4F37D97E314F51449CBA710F216EAAB22F031221161699026BA78D9971FE37D66AB75449573CBACFFEF5D0A8AS9493E1ACB23A0FF348FC76B37C1630CDE46D6B45FE7D
 23FD90E851071E51A35FED4946547F2C88C5F4139C97153C03E8A139DC690C32C1AF16574C9447427CA2C89C7DE6D44D54AF4299A8C104C2779CD648E4CE11E02A8099F04370CF
3F766BD14C49AB245EC20D82FD46A8AB6C93CC6252427592F89AFA5E5EB2B061E51F1FB97F0998E83DFA837F4769A1
 [10/18/24]seed@VM:~/.../k213881_Assignment-2$ openssl x509 -in server_cert.pem -text -noout
      Data:
            Version: 3 (0x2)
Serial Number:
             07:5b:ce:f3:06:89:c8:ad:df:13:e5:1a:f4:af:e1:87
Signature Algorithm: sha256WithRSAEncryption
             Issuer: C = US, O = DigiCert Inc, CN = DigiCert Global G2 TLS RSA SHA256 2020 CA1
             Validity
            rs, CN =
              www.example.org
            Subject Public Key Info:
Public Key Algorithm: rsaEncryption
RSA Public-Key: (2048 bit)
                         Modulus:
00:86:85:0f:bb:0e:f9:ca:5f:d9:f5:e0:0a:32:2c:
                               33:d9:aa:0e:07:29:a8:2f:08:ad:78:bd:c2:06:bf:
f7:2d:2b:a6:a7:27:3d:53:a6:4c:c3:4b:b2:27:77:
                               20:d6:c1:54:49:b8:08:da:f9:70:a9:61:f6:b2:49:
                               9d:69:57:da:fb:6d:24:34:72:2e:47:f0:04:3f:9d:
b1:5b:e2:bc:66:31:59:32:e6:a9:7e:bf:d4:b0:d4:
                                                                                                                                                                                        seed@VM: ~/.../k213881_Assignment-2
                                                                                                                                                                                                    Q = - 0
            Not After: Mar 1 23:59:59 2025 GMT
Subject: C = US, ST = California, L = Los Angeles, 0 = Internet\C2\A0Corporation\C2\A0for\C2\A0Assigned\C2\A0Names\C2\A0Names\C2\A0Numbe
= www.example.org
 s, CN =
            Subject Public Key Info:
Public Key Algorithm: rsaEncryption
RSA Public-Key: (2048 bit)
                               00:86:85:0f:bb:0e:f9:ca:5f:d9:f5:e0:0a:32:2c:
                               33:d9:aa:0e:07:29:a8:2f:08:ad:78:bd:c2:06:bf:
f7:2d:2b:a6:a7:27:3d:53:a6:4c:c3:4b:b2:27:77:
                               20:d6:c1:54:49:b8:08:da:f9:70:a9:61:f6:b2:49:
9d:69:57:da:fb:6d:24:34:72:2e:47:f0:04:3f:9d:
                               b1:5b:e2:bc:66:31:59:32:e6:a9:7e:bf:d4:b0:d4:
64:f5:6b:ca:7b:ff:72:5b:5e:9a:d8:3f:d4:06:b2:
                               f3:c8:dc:8f:66:5a:46:84:66:a8:18:15:79:a7:08:
                               ce:05:3c:fb:39:89:ef:6d:fa:4e:71:52:7b:b7:e4:
                               a0:a4:9c:96:c0:61:3d:a4:0a:70:4d:c3:8e:cd:6e:
b3:32:6c:f2:c7:44:09:04:dd:a0:55:fd:23:a5:20:
78:b2:85:5e:d8:3b:ad:17:ff:85:c5:b9:74:8d:33:
                               b9:b8:57:6e:b5:bc:69:65:db:0b:3c:92:55:99:f4:
                                73:b4:64:24:ca:67:4c:28:99:cc:dc:67:3d:79:c7:
                               16:9c:2b:e6:ab:aa:aa:35:72:37:f6:81:2a:48:e8:
3f:4e:19:9a:bf:9e:46:aa:32:93:ff:a5:b2:5a:b4:
                               b1:2f:1e:69:84:92:1d:b0:b9:8d:af:f2:31:6c:95:
                               86:f3
                        Exponent: 65537 (0x10001)
            X509v3 extensions:
                   X509v3 Authority Key Identifier:
keyid:74:85:80:C0:66:C7:DF:37:DE:CF:BD:29:37:AA:03:1D:BE:ED:CD:17
```



seed@VM: ~/.../k213881_Assignment-2

----BEGIN CERTIFICATE-----MIIHbjCCBlagAwIBAgIQB1vO8waJyK3fE+Ua9K/hhzANBgkqhkiG9w0BAQsFADBZ MQswCQYDVQQGEwJYUJEVMBMGA1UEChMMRGlnaUNlcnQgSM5jMTMAMQYDVQQDEypE aWdpQ2VydCBHbG91YMwgRzIgVExTIFJTQSBTSEEyNTYgMjAyMCBDQTEwHhcNMjQw MTMaMDAwMDAwMhcNMjUwMzAxMjM10TUSWjCBljELMAKGA1UEBhMCVVMxEzARBgNV BAGTCKNhbGlmb3JuaWExFDASBgNVBACTC0xvcyBBbmdlbGVzMUIwQAYDVQQKDDLJ bnRlcm5ldMKgQ29ycG9yYXRpb27CoGZvcsKgQXNzaWduZWTCoE5hbWVzwqBhbmTC onktchisturing/sycs9y/xng/zh/sycs0y/xng/syckyzh/de/side/stibol/st /230 interinuctional control of the eGFtcGxlLm5ldIILZXhhbXBsZS5lZHWCC2V4YWIwbGUuY29tggtleGFtcGxlLm9y Z4IPd3d3LmV4YWIwbGUuY29tgg93d3cuZXhhbXBsZS5lZHWCD3d3dy5leGFtcGxl Lm5ldDA+BgNVHSAENzAIMDMGBmeBDAECAjApMCcGCCsGAQUFBwIBFhtodHRwOi8v d3d3LmRpZZljZXJ0LmNvbS9DUFMwDgYDVR0PAQH/BAQDAgWgMB0GA1UdJQQWMBQG CCsGAQUFBwMBBggrBgEFBQcDAjCBnwYDVR0fBIGXMIGUMEigRqBEhkJodHRw0i8v LCSGAQUFBMMBBQJFBGFBUCOJLBMMTVJNFBLGXMISUMHLIGHRGBERLJOHRWDLBW Y331MJSKBAWDPYZVYGC5jb20VRGInaUNlcnRHDG9iWXHMTRWIJJTOVNIOTIJNjTW MjBDQTEtMS5jcmxwSKBGoESGQmh0dHA6Ly9jcmx0LmRpz2ljZXJ0LmNvbS9EaWdp QZVydEdsb2JhbEcyVEXTULNBU0hBMJJUZMjAyMENBMS0XLmNybDcBhwYTKxYBBQUH AQEEe2BBMCQGCC5GAQUFB2BBhh0dHWRW03BvD2NzCSKaWdpYZydC5jb20MUQYI KwYBBQUHMAKGRWh0dHA6Ly9jYWNlcnRzLmRpZ2ljZXJ0LmNvbS9EaWdpQ2VydEds b2JhbEcyVExTUlNBU0hBMjU2MjAyMENBMS0xLmNydDAMBgNVHRMBAf8EAjAAMIIB fQYKKwYBBAHWeQIEAgSCAW0EggFpAWcAdABOdaMnXJoQwzhbbNTfP1LrHfDgjhuN acCx+mSxYpo53wAAAY1b0vxkAAAEAwBFMEMCH0BRCgxPbBBVxhcWZ26a8JCe83P1 JZ6wmv56GsVcyMACIDgpMbEo5HJITTRPnoyT4mG8cLrWjEvhchUdEcWUuk1TAHYA fVkeEuF4KnscYwd8XX340IdcFKB0lZ65Ay/ZDowuebgAAAGNW9L8MAAABAMARZBF AiBdv5Z3pZFbfgoM3tGpCTM3ZxBMQsxBRSdTS6d8d2NAcwIhALLoCT9mTMN90yFz IBV5MkXVLyuTf20AzA0a7d8x2H6XAHcA5tIxY0B3jMEQQQbXcbn0wdJA9paEhvu6

