



Usage Of Cryptography

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Credits: Mark Stamp

Agenda

- History of Cryptography
- Symmetric Encryption
- Asymmetric Crypto
- MACs and hash functions
- Digital signatures
- Certificates and PKI



Why do we need crypto

- Complex math!
- The core technology of cyberspace
 - Secret communication
 - Data confidentiality
 - Data integrity
 - Authentication
 - E-Commerce
 - Digital currency ...



<https://flic.kr/p/brdXxC>

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History of Cryptography



- Egypt, China
- אתב"ש בספר ירמיהו
- A **cipher** or cryptosystem is used to encrypt the **plaintext**
- The result of encryption is **ciphertext**
- We **decrypt** ciphertext to recover plaintext



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Key

- Need strong cipher
 - Need many different strong ciphers!
 - How to make someone to forget the cipher?
- A **key** is used to configure a cryptosystem

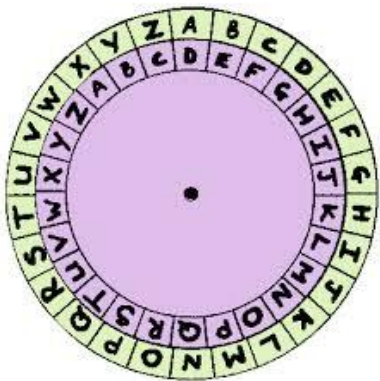


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Caesar and its attacks

- The simplest substitution cipher
- What is the key?
- How to break it?
- How to make it stronger?



Plaintext	a	b	c	d	e	f	g	h	i	j	k	l	m	n	o	p	q	r	s	t	u	v	w	x	y	z
Ciphertext	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C

Substitution cyphers and attacks

- Shift by n for some n in {0,1,2,...,25}
- Then key is n
- Example: key n = 7

Plaintext	a	b	c	d	e	f	g	h	i	j	k	l	m	n	o	p	q	r	s	t	u	v	w	x	y	z
Ciphertext	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z	A	B	C	D	E	F	G

hello → OLSSV

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Cryptanalysis I: Try Them All

- A simple substitution (shift by n) is used
- But the key is unknown
- Given ciphertext: **XIVQMREXIH**
- How to find the key?
- Only 26 possible keys - try them all!
- Exhaustive key search (brute force)
- Solution: key is n = 4

```
1: whuplqdwg
2: vgtokpcvgf
3: ufsnjobufe
4: terminated
5: sdqlhm`sd
```

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Least-Simple Simple Substitution

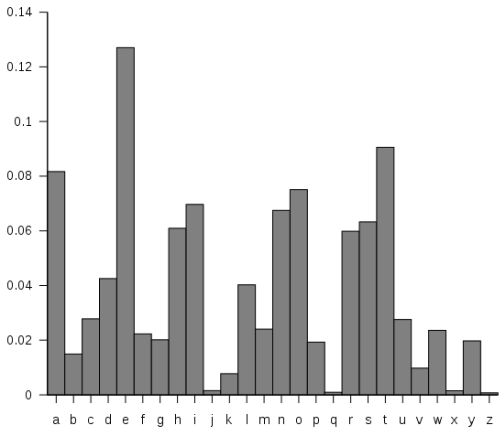
- In general, simple substitution key can be any permutation of letters
- Not necessarily a shift of the alphabet
- Then $26! > 2^{88}$ possible keys!
- A superfast computer testing 2^{40} per second would take 8.900.000 years...

Plaintext	a	b	c	d	e	f	g	h	i	j	k	l	m	n	o	p	q	r	s	t	u	v	w	x	y	z
Ciphertext	J	I	C	A	X	S	E	Y	V	D	K	W	B	Q	T	Z	R	H	F	M	P	N	U	L	G	O

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Cryptanalysis II

- Letter frequency analysis
- Letter combinations frequency
- Words frequency
- Huge key space != stronger cipher!



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Types of crypto attacks

- Cipher text only (Caesar)
- Known plaintext (Enigma, RC4)
- Chosen plaintext
- Chosen ciphertext
- [Kerckhoffs](#) (1883) Algorithm can't stay secret (Enigma, A5, DVD, [US Navy](#))
 - Security through obscurity



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Claude Shannon

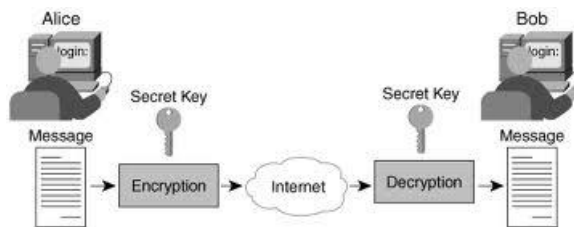
- The founder of Information Theory
- 1949 paper: [Communication Theory of Secrecy Systems](#)
- Fundamental concepts
 - **Confusion** - obscure relationship between plaintext and ciphertext
 - **Diffusion** - spread plaintext statistics through the ciphertext
- Proved that one-time pad is unbreakable



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Symmetric encryption

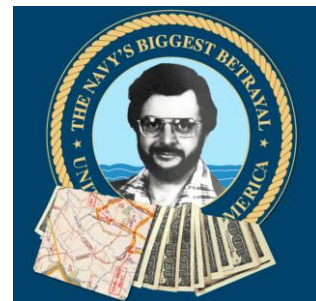
- Symmetric algorithm – the same key used for decryption and encryption
- All encryption algorithms used to be symmetric ...



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Modern symmetric encryption

- Translates the **bytes** of plaintext into ciphertext
- DES, 3-DES and now [AES](#) are standard symmetric encryption algorithms
- Problem – key distribution ($n \times n$ keys for n pairs)
- Problem – [key management](#)
- Problem – non-repudiation



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Asymmetric crypto

- Motivation: solve the key distribution problem
 - Secure banking online
- Secret communication without agreed shared key!
- **Some operations are easy to do in one direction, but hard to do in the reverse direction**
 - Scrambling an egg vs. undoing it*
 - Insulting a person vs. making him/her forget it*
 - Closing a padlock vs. opening it



*Credits to Yaron Sella for this example

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Asymmetric crypto

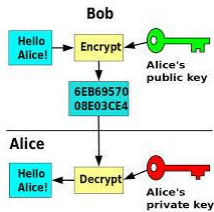
- Asymmetrical mathematical problems:
 - Assigning values to variables vs. solving equations
 - Multiplying numbers vs. factoring ($7919 * 6967 = 55171673$)(RSA)
 - Discrete Log ([Diffie Hellman](#))
 - You'll learn how they work in other courses!
- Modular calculus
 - $8 + 5 \bmod 12 = 13 \bmod 12 = 1$**



Public and Private Keys

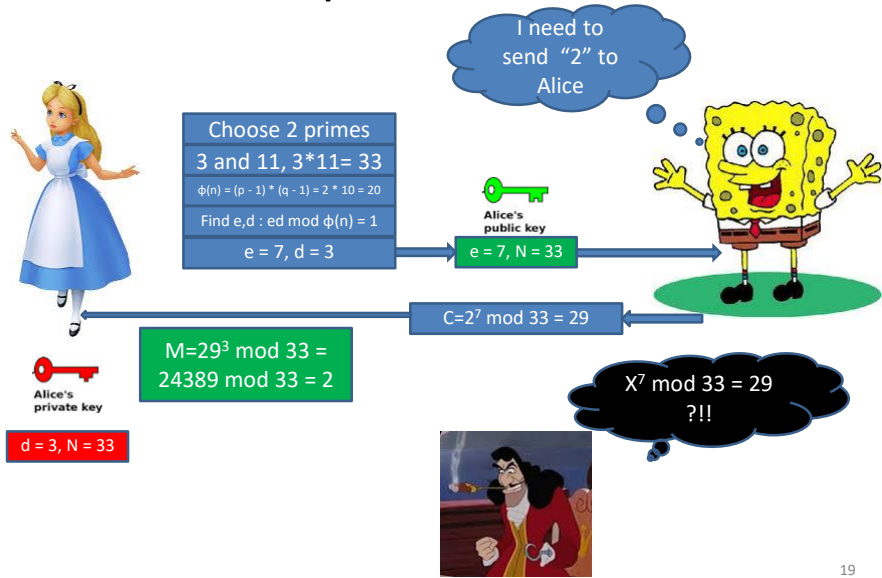
- A user generates a pair of keys: public and private.
- Public is published to the whole world and is used for encryption
- Private is secret and is used for decryption
- It is hard to get the private key from the public
- Public key cryptography is very slow , used to pass a symmetric session key

$$C = M^e \bmod N$$
$$M = C^d \bmod N$$



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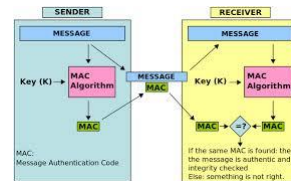
RSA simplified simulation



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Message Authentication Code (MAC)

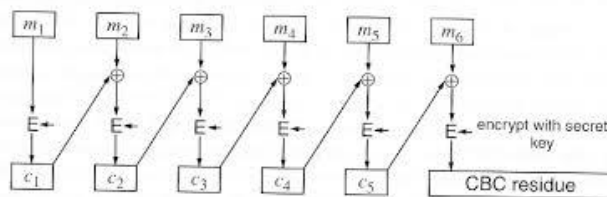
- Why do we need it?
- A number added to a message
- Uses a shared secret key
- Authentication and Integrity (no confidentiality)



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Message Authentication Code (MAC)

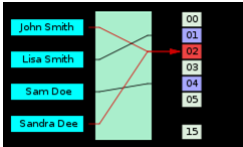
- Example – last block of AES-CBC encryption
- Any change in the plaintext must result in a different MAC!
- Can't fake the message for the given MAC
- Based on block cipher symmetric encryption and hashes



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One Way Hash Functions

- Hash function: maps a large object to a small fingerprint (e.g. length of string, first character)
 - Many collisions
 - Data $X = (X_0, X_1, X_2, \dots, X_{n-1})$, each X_i is a byte
 - Define $h(X) = X_0 + X_1 + X_2 + \dots + X_{n-1}$
 - Is this a secure cryptographic hash?
- Cryptographic hash functions practically uninvertible:
 - Easy to compute
 - Infeasible to find a message given a hash (preimage)
 - Infeasible to change the message without changing hash
 - Infeasible to find two messages with the same hash (collision resistance)



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One Way Hash Functions

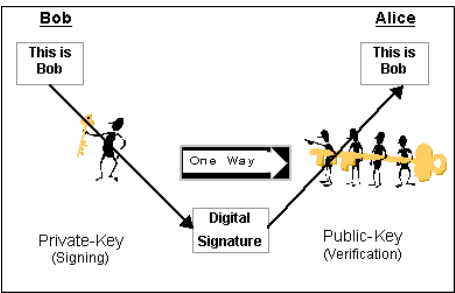
- Provide integrity (no key!)
- Hashed MAC (HMAC) – uses a key to provide also authentication
- Widely used: software packages, firmware updates, digital signatures...
- SHA (1 - deprecated, 256), MD5 – also deprecated, [see here why](#)

Fox	cryptographic hash function	DFCD 3454 BBFA 788A 751A 696C 24B9 7009 CA99 2D17
The red fox jumps over the blue dog	cryptographic hash function	0086 46BB FB7D CB22 823C ACC7 6CD1 90B1 EE6E 3ABC
The red fox jumps over the blue dog	cryptographic hash function	8F98 7558 7851 4F32 D1C6 76B1 73A9 0DA4 A2FE 4819
The red fox jumps over the blue dog	cryptographic hash function	FCD3 7FBB 5AF2 C8FF 915F D401 C0A9 799A 46AF FB45
The red fox jumps over the blue dog	cryptographic hash function	8ACA D682 D588 4C79 4BF4 1789 7B58 ACF8 92B9 6A6C

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Digital signatures

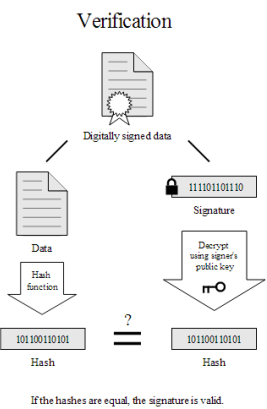
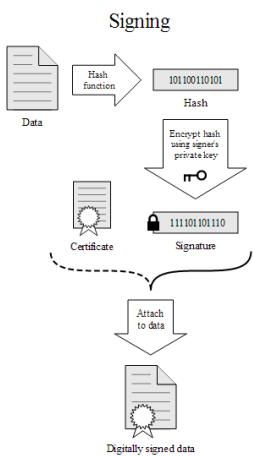
- Using the private key for encryption uniquely authenticates the sender
- Everyone can verify that Alice sent this message-signature
- Can't be reused for another message
- Can prove it was Alice who sent the message (unlike in shared secret schemes)



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Digital signing


- Authentication + integrity
- RSA
- DSA
- Used in: secure mail, official documents, software images, certificates, ...



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Certificates

- Where all public keys are kept?
- What guarantees that this is indeed Alice's public key?
- Certificate:
 - Credentials (name, organization, email)
 - Public key
 - Signed by someone you trust
 - Chain Of Trust
- X.509 is the standard format

 **Certificate Information**

This certificate is intended for the following purpose(s):

- Proves your identity to a remote computer
- Ensures software came from software publisher
- Protects software from alteration after publication
- Ensures the identity of a remote computer
- All issuance policies

* Refer to the certification authority's statement for details.

Issued to: VeriSign Class 3 Public Primary Certification Authority - G5

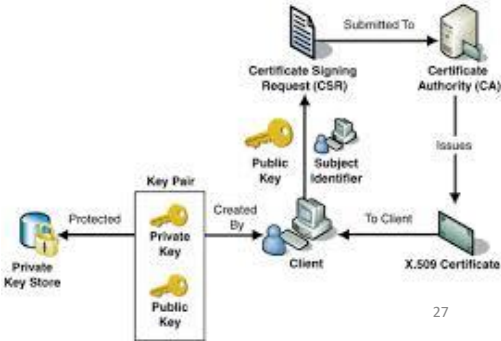
Issued by: Class 3 Public Primary Certification Authority

Valid from: 08/ 11/ 2006 **to** 08/ 11/ 2021

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Public Key Infrastructure

- In real life we need lots of certificates, who will sign all of them?
- A small amount of trusted Certificates Authorities (CA) – root CAs
- Root CA's public keys are preinstalled



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PKI challenges

- Is the name enough? (Think of a phone book)
- How does the CA verifies trustfulness of the applicant?
- What makes CA trusted
 - Stolen CA private keys
- Key revocation handling (CRL)
- Can we trust the code that verifies that the certificate content is correct?



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Questions?



<https://flic.kr/p/pqiJNt>

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Terms learnt

- Cipher, plaintext, ciphertext
- Key
- Cryptanalysis
- Brute force
- Confusion, diffusion
- Symmetric and asymmetric crypto
- Public and private key
- MAC, one way hash, HMAC
- Digital signatures
- PKI



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Summary

- Cryptography helps with Confidentiality and Integrity
- Classic crypto is easy to understand and break
- Symmetric ciphers are fast, but keys are a mess
- Asymmetric crypto solves the key management problem
- Digital signatures provide authentication and integrity



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