

```
b = 11    e = 12354    p = 7919    q = 5153    n = 40806607
```

```
----- Right to left -----
```

```
Answer = 31057402
```

```
Time = 1064 nano Seconds
```

```
----- Left to right -----
```

```
Answer = 31057402
```

```
Time = 1421 nano Seconds
```

```
----- CRT -----
```

```
Answer = 31057402
```

```
Time = 6363 nano Seconds
```

As shown in the results the fastest algorithm in my implementation is Right to left modular exponentiation then Left to right then CRT.

Time calculated is the average of running the code 50000 times.

```
1  #include <iostream>
2  #include <chrono>
3
4  using namespace std;
5  typedef long long ll;
6
7  ll Right_to_Left_Binary_Modular_Exponentiation(ll b, ll e, ll n) {
8      ll a = 1;
9      ll s = b;
10     int number_of_bits = (int)log2(e) + 1;
11     for(int i = 0 ; i < number_of_bits; i++)
12     {
13         if (e >> i & 1)
14             a = (a * s) % n;
15         s = (s * s) % n;
16     }
17     return a;
18 }
19
20
21 ll Left_to_Right_Binary_Modular_Exponentiation(ll b, ll e, ll n) {
22     ll s = b;
23     int number_of_bits = (int)log2(e) + 1;
24     for (int i = number_of_bits - 2 ; i >= 0; i--)
25     {
26         s = (s * s) % n;
27         if (e >> i & 1)
28             s = (s * b) % n;
29     }
30     return s;
31 }
32
33
```

```

34  ll Extended_GCD(ll a, ll b, ll& x, ll& y) {
35      if (b == 0) {
36          x = 1;
37          y = 0;
38          return a;
39      }
40
41      ll x1, y1, gcd = Extended_GCD(b, a % b, x1, y1);
42      x = y1;
43      lldiv_t div = std::lldiv(a, b);
44      y = x1 - div.quot * y1;
45      return gcd;
46  }
47
48  ll Modulare_Inverse(ll a, ll n) {
49      // ax ≡ 1 (mod n)
50      ll x, y;
51      Extended_GCD(a, n, x, y);
52      if (x < 0)
53          x += n;
54      return x;
55  }
56
57  ll CRT(ll b, ll e, ll p, ll q, ll n) {
58
59      ll yp = Left_to_Right_Binary_Modular_Exponentiation(b, e, p);
60      ll yq = Left_to_Right_Binary_Modular_Exponentiation(b, e, q);
61      ll xq = Modulare_Inverse(q, p);
62      ll xp = Modulare_Inverse(p, q);
63      ll y = (yp * q * xq + yq * p * xp) % n;
64      return y;
65  }
66

```

```

68  int main()
69  {
70      ll b = 11, e = 12354, p = 7919, q = 5153, n = 40806607;
71      ll ans1, ans2, ans3, time1 = 0, time2 = 0, time3 = 0;
72      for (int i = 0; i < 50000; i++) {
73
74          auto start_time = chrono::steady_clock::now();
75          ans1 = Right_to_Left_Binary_Modular_Exponentiation(b, e, n);
76          auto end_time = chrono::steady_clock::now();
77          time1 += chrono::duration_cast<chrono::nanoseconds>(end_time - start_time).count();
78
79          start_time = end_time;
80          ans2 = Left_to_Right_Binary_Modular_Exponentiation(b, e, n);
81          end_time = chrono::steady_clock::now();
82          time2 += chrono::duration_cast<chrono::nanoseconds>(end_time - start_time).count();
83
84          start_time = end_time;
85          ans3 = CRT(b, e, p, q, n);
86          end_time = chrono::steady_clock::now();
87          time3 += chrono::duration_cast<chrono::nanoseconds>(end_time - start_time).count();
88
89      }
90      time1 = time1 / 50000;
91      time2 = time2 / 50000;
92      time3 = time3 / 50000;
93

```

```
94     cout << "b = " << b << "   e = " << e;  
95     cout << "   p = " << p << "   q = " << q << "   n = " << n << endl << endl;  
96  
97     cout << "----- Right to left ----- " << endl << endl;  
98     cout << "Answer = " << ans1 << endl;  
99     cout << "Time = " << time1 << endl << endl;  
100  
101     cout << "----- Left to right ----- " << endl << endl;  
102     cout << "Answer = " << ans2 << endl;  
103     cout << "Time = " << time2 << endl << endl;  
104  
105     cout << " ----- CRT ----- " << endl << endl;  
106     cout << "Answer = " << ans3 << endl;  
107     cout << "Time = " << time3 << endl << endl;  
108  
109     return 0;  
110 }  
111
```