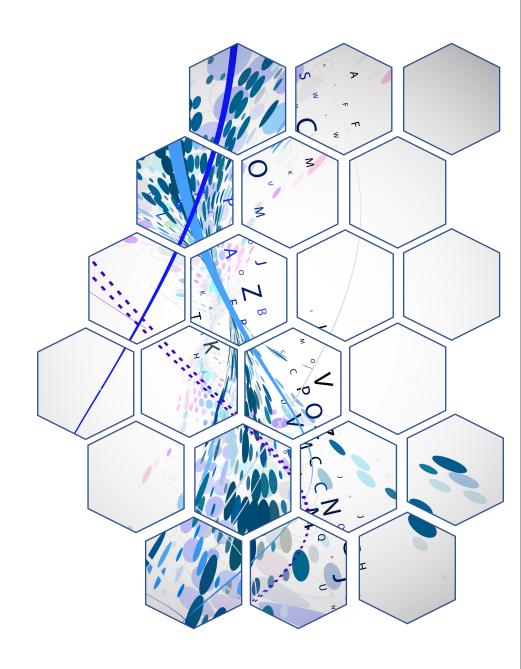
## **POLYNOMIAL**

Abstract Algebra



### **Submitted by**

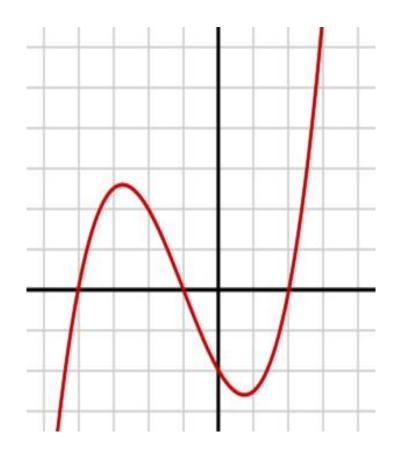
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#### **OUTLINE:**

- INTRODUCTION OF POLYNOMIALS
- TYPES OF POLYNOMIALS
- POLYNOMIAL RINGS
- IRREDUCIBLE POLYNOMIAL
- PSEUDO RANDOM GENERATOR FOR POLYNOMIAL



VIA CYCLIC PHASE

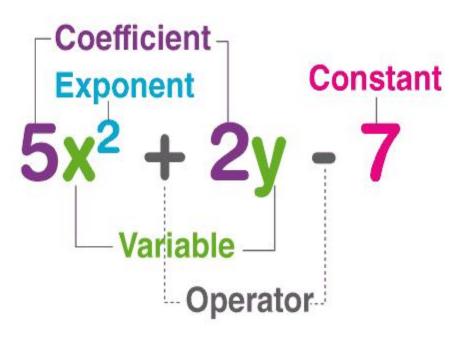


#### **POLYNOMIALS:**

- Polynomials are algebraic expressions that consist of variables and coefficients.
- Variables are also sometimes called indeterminates.
- Addition, subtraction, multiplication, and also positive integer exponents can be perfored for polynomial expressions.

#### **POLYNOMIALS**





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#### TYPES OF POLYNOMIALS

Monomials:

A monomial is a polynomial expression that contains only one term. For example 4t, 21x, 2y, 9pq.

Binomials:

A binomial is a polynomial with two, unlike terms. For example  $3x + 4x^2$ 

Trinomial:

A trinomial is a polynomial with three, unlike terms. For example,  $3x + 5x^2 - 6x^3$  and  $12pq + 4x^2 - 10$ .

#### DEGREES OF POLYNOMIAL

Zero or constant polynomial

Polynomials with 0 degree. Example: 3 or 3x0

Linear polynomial

Polynomials with 1 as the degree. Example: x + y - 4, 5m + 7n, 2p

Quadratic polynomial

Polynomials with 2 as the degree . Example : 8x2 + 7y - 9, m2 + mn - 6

Cubic polynomial

Polynomials with 3 as the degree. Example: 3x3, p3 + pq + 7

### POLYNOMIAL RINGS

A polynomial ring or polynomial algebra is a ring formed from the set of polynomials in one or more indeterminates (traditionally also called variables) with coefficients in another ring, often a field.

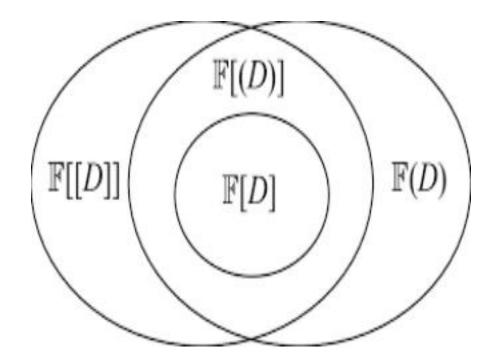


fig - Relationship among polynomial rings

## IRREDUCIBLE POLYNOMIAL

- An irreducible polynomial is a polynomial that cannot be factored into the product of two non-constant polynomials.
- An irreducible polynomial is also called a prime polynomial.

The polynomial  $x^2-2 \in Q[x]$  is irreducible since

#### **Solution:**

it cannot be factored any further over the rational numbers.

 $x^2+1$  is irreducible over the real numbers.

#### PSEUDO RANDOM GENERATOR FOR POLYNOMIAL

- Pseudorandom generators for low-degree polynomials are a particular instance of a Pseudo Random Number Generator (PRNG)
- In statistical tests, the tests are considered as evaluations of low degree polynomials.
- Efficient procedure that maps a short truly random seed to a longer pseudorandom string.

# POLYNOMIAL PSEUDO-RANDOM NUMBER GENERATOR VIA CYCLIC PHASE

```
Polynomials f(x): f(x) = fo+f_1 x + f2x^2 + fnx''; f; \in GF (p'') are assigned to a Galois field GF (0).
```

If a generic algebra A (n) is defined in GF (0) and modular arithmetic modulo p [12] is used, the algebraic field Zip is the ring of quotients modulo the prime p (at least for the multiplication operator).

```
For example, addition of two polynomials in GF (2) and Z3 (2) modulo (x^3 + x + 1) is: f(x) = x^2 + 1; f(x) = x^2 + x f(x) = \sum f(x) = f(x) + f(x) = x + 1
This is the polynomial equation .
```

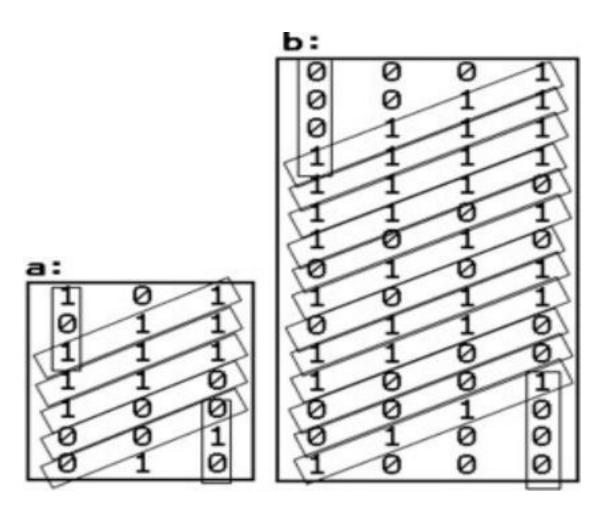


Figure: Pseudo random code generating

#### Reffenences:

- 1. Abstract Algebra: Theory and Applications Thomas W. Judson
- 2. Polynomial pseudo random number generator via cyclic phase Angelo Marchi, Alfonso Del Giudice, Antonio Liverani Faculty of Economics

# **THANK YOU**