

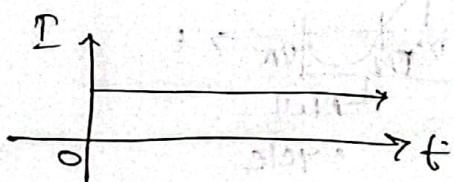
EEE

Chapter-13

SINUSOIDS AND PHASORS

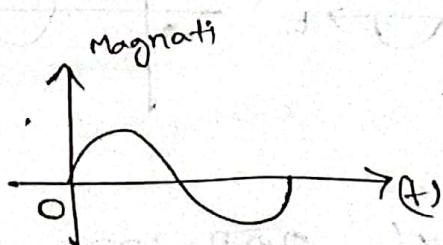
Current প্রবাহণ,

(i) DC \rightarrow Direct current



কোন যথান্বে এবং কোন সময়ের দ্রুতি না, তাহলে
প্রবাহণ এর একটি স্থায়ী মানের জন্য নির্দিষ্ট হবে।

(ii) AC \rightarrow Alternative current.



স্থায়ী প্রবাহণ এবং

কোন সময়ের জন্য কোন যথান্বে এবং কোন সময়ের জন্য নির্দিষ্ট হবে। এই যথান্বে এবং কোন সময়ের জন্য একটি স্থায়ী মানের জন্য নির্দিষ্ট হবে।

AC current \rightarrow Supplied by $\sin \omega t$



একটি



একটি গুরুতর এবং সহজে আবেগ পূরণ



একটি গুরুতর এবং

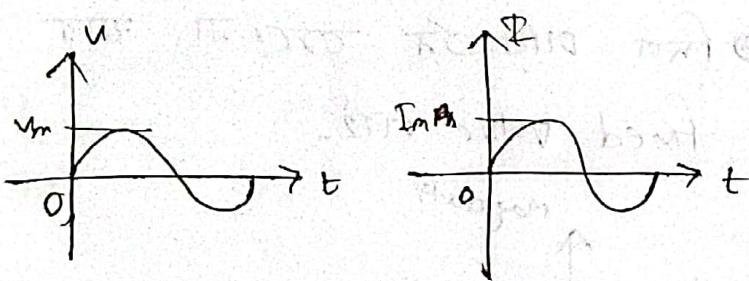
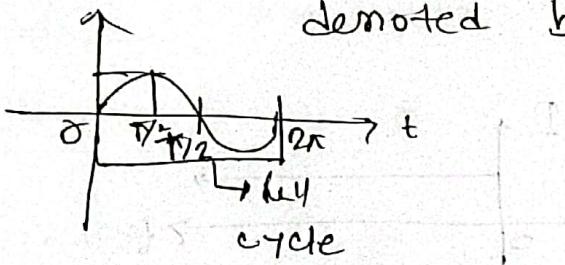
অঙ্গ এবং একটি অঙ্গ এবং একটি অঙ্গ

স্থায়ী প্রবাহণ এবং একটি অঙ্গ এবং একটি অঙ্গ

time period, എണ്ണ full wave റെ full cycle

function ഒരു സംവാദ നാൾ റിക്കോ time period എന്ത്;

denoted by T ,

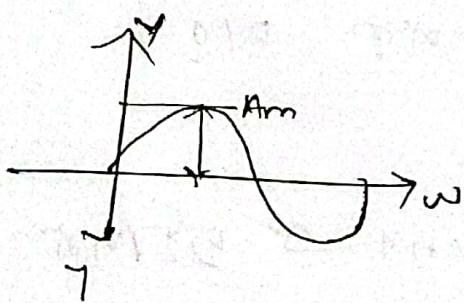


frequency, എത്ര സ്വാധീ ചെന്തുണ്ട് Complete cycle

(ചുരുക്കണം wave റെ frequency എന്ത്, denoted by f ,

$$f = \frac{1}{T} \quad , \quad \omega \rightarrow \text{angular frequency}$$

നിർവ്വാത മാറ്റൽ,



$$v(t) = Am \sin(\omega t)$$

$$Am = Am_{\max}$$

ഓരോ Amplitude റെ $V_{\max} / I_{\max} 3 \pi/2 \approx 1.57$

$$V = V_m \sin \omega t$$

$$V = V_m \sin \omega t$$

$$I = I_m \sin \omega t$$

$$0 \leq \theta$$

$$\omega = \frac{t}{T} \Rightarrow \frac{2\pi}{T} = 2\pi f = \frac{2\pi N}{t}$$

$$\theta = \omega t$$

$$\omega = \frac{2\pi}{T}$$

$$v = \frac{c}{\lambda} = \frac{V}{T}$$

c = constant (const)

v = velocity / const

λ = wavelength



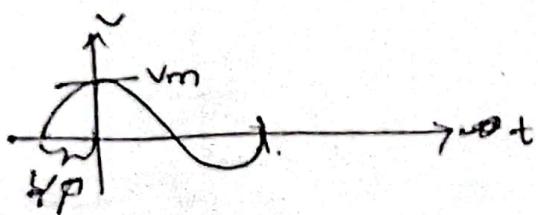
w = angular const

T = period
time period

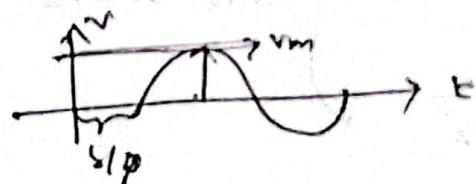
n = min/s / frequency

N = number waves/s

θ/t = constant



$$V_2 = V_m \sin(\omega t + \phi)$$



$$V_3 = V_m \sin(\omega t - \phi)$$

$\phi = 0^\circ$ or 180° at time $t = 0$ wave starts at V_m

$\phi = 0^\circ$ (starts at V_m) $\phi = 180^\circ$ (starts at 0)

$$V(t) = V_m \cos(50t + 10^\circ)$$

$$V_m = 12, T = \frac{2\pi}{\omega} = 0.025 \text{ s} \approx 36 \text{ s}$$

$$\omega = 50$$

$$\phi = 10^\circ$$

$$f = \frac{1}{T}$$

$\sin(\theta + 180^\circ) = -\sin \theta$

$$\cos(\theta + 180^\circ) = -\cos \theta$$

$$\cos(\omega t + 180^\circ)$$

$$\sin(\omega t \pm 180^\circ) = \sin \omega t$$

$$\cos(\omega t \pm 180^\circ) = -\cos \omega t$$

$$i \sin(\omega t + 90^\circ) = \cos \omega t$$

$$\cos(\omega t + 90^\circ) = -\sin \omega t$$

V_{rms} value and Average value of Voltage

$$V_{rms} = \frac{V_m}{\sqrt{2}}$$

} Sine wave

$$I_{rms} = \frac{I_m}{\sqrt{2}}$$

$$V_{rms} = \sqrt{\frac{1}{T} \int_0^T V(t) dt}$$

$$V_{avg} = \frac{2V_m}{\pi}$$

$$V_{avg} = \frac{1}{\pi} \int_0^{\pi} V_p \sin \omega t dt$$

$$V_{avg} = \frac{V_p}{\pi} \left[-\cos \omega t \right]_0^{\pi} = \pi \cdot \frac{2V_p}{\pi} = 0.637 V_p$$

$V_p \rightarrow$ peak value (V_{max})

$0.637 V_m$

Capacitor: voltage or change \rightarrow 270° खेड़ी तरीका
तरीका

voltage or lag अंतर,

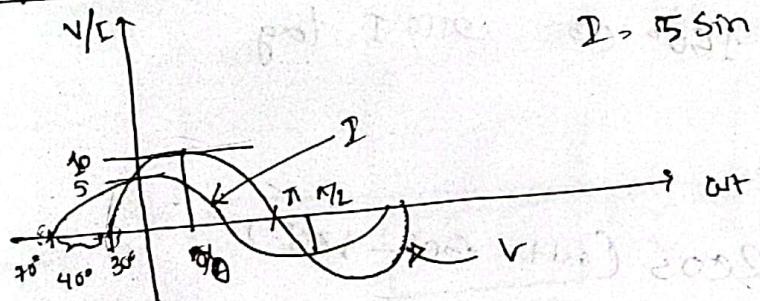
Inductor: current or change \rightarrow 270° खेड़ी तरीका

or lag अंतर,

$$V = 10 \sin(\omega t + 30^\circ)$$

$$I = 5 \sin(\omega t - 70^\circ)$$

Capacitor:



I lead V by 40° , or V lags I by 40°

अब I वाले वेव V का वेव 90° अंतर 40°

अब I वाले वेव V का अंतर 70° अंतर लगाते हैं तो V का अंतर 30°

I lead अंतर V 40° और V lead I 50°

lag अंतर 110°

capacitor और inductance σ lead / lag (तरीका)

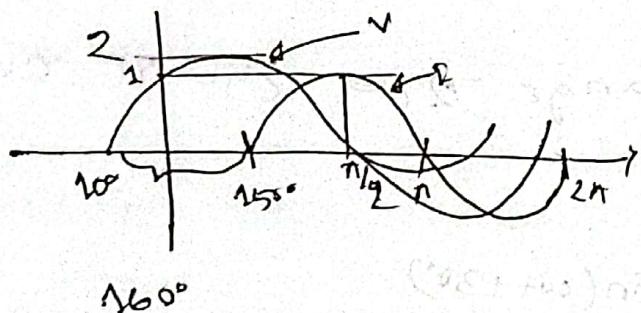
Inductance

$$I = -\sin(\omega t + 30^\circ)$$

$$V = -\sin(\omega t + 30^\circ - 180^\circ)$$

$$= \sin(\omega t - 150^\circ)$$

$$V = 2 \sin(\omega t + 10^\circ)$$



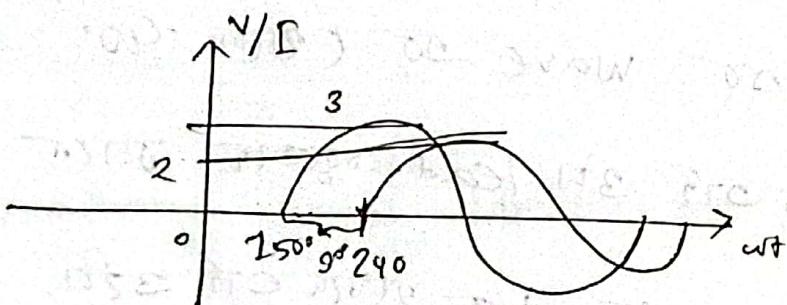
current \sim lead voltage 160° (ω), I lag

voltage 160° (θ),

$$I = -2 \cos(\omega t - 60^\circ) = 2 \cos(\omega t - 60^\circ - 180^\circ)$$

$$= 2 \cos(\omega t - 240^\circ)$$

$$V = 3 \sin(\omega t - 150^\circ)$$



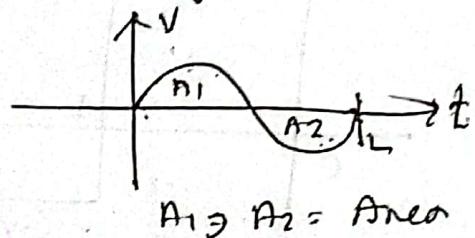
Phase measurement

$$\theta = \frac{\text{Phase shift (no of div)}}{T (\text{no of div.})} \times 360^\circ$$

Vavg derivation: $V_{avg} = \frac{2V_m}{\pi}$ (Sinusoidal wave to 250 Hz
over avg value)

Circular wave for avg.

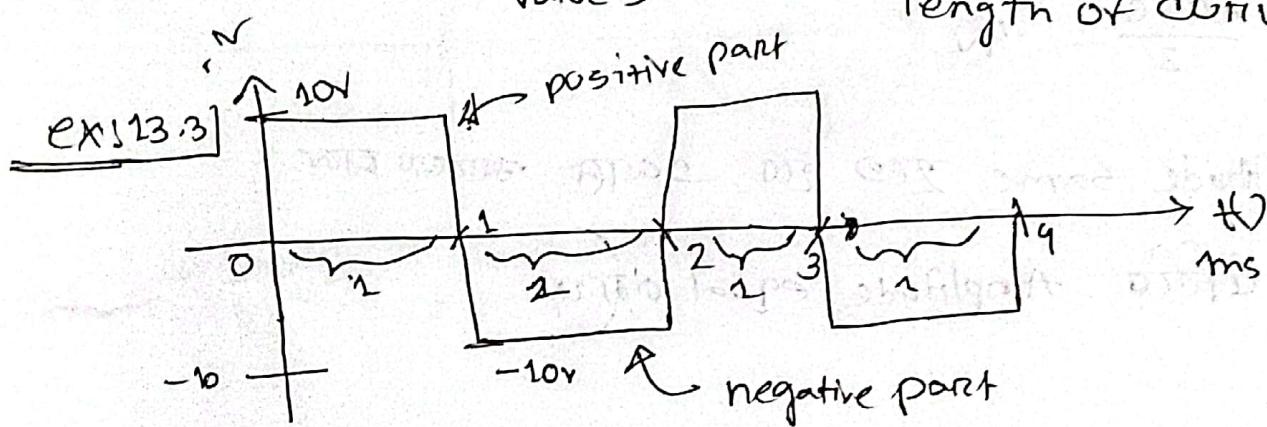
value 9



$A_1 + A_2 = \text{Area}$

$L = \text{Length}$

G_r (averaging average) = $\frac{\text{algebraic sum of areas}}{\text{length of curve}}$ (complete cycle)

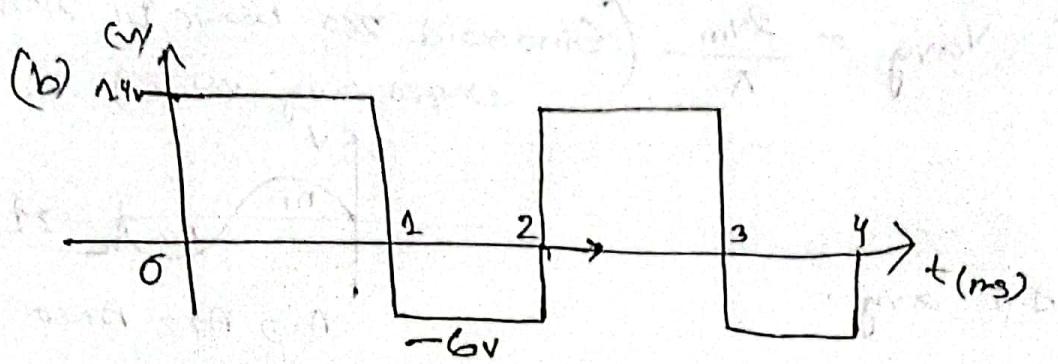


$$G_r = \frac{(10V) \times 1(1ms) + (-10V) \times 1}{2}$$

$$= \frac{10 - 10}{2} = \frac{0}{2} = 0V$$

After complete cycle of area and length ratio avg

(at avg 0V)

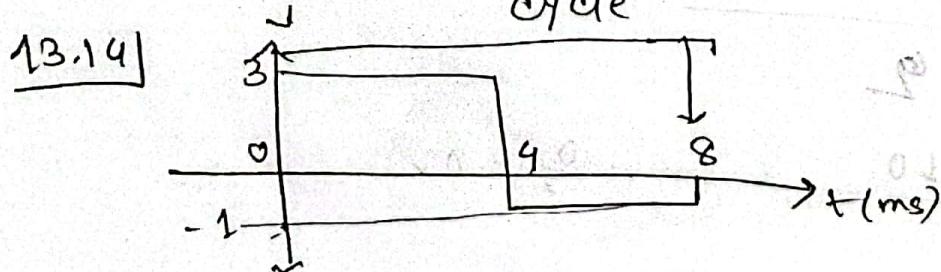


$$G_r = \frac{(14 \times 1) + (-6 \times 1)}{2}$$

$$= \frac{14 - 6}{2} = 4V$$

Amplitude same तो यह एकल मार्ग पर
तो लगभग Amplitude equal होगा.

Q8. $V_2 = V_1 + 24V$

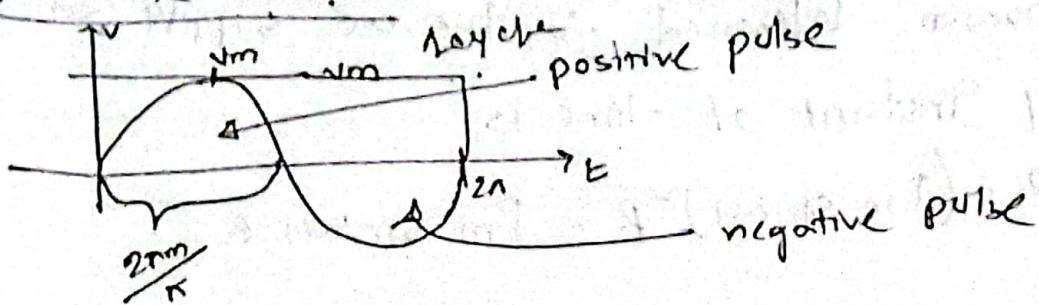


$$G_r = \frac{(3 \times 4) + (4 \times -1)}{8}$$

$$= \frac{12 - 4}{8} = 1V$$

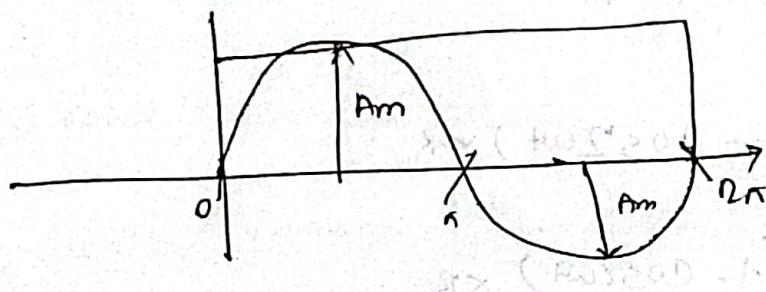


for sine wave:



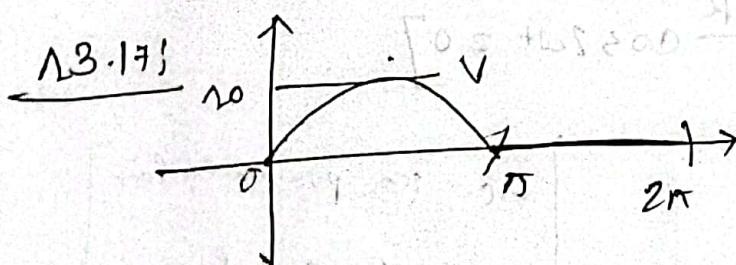
$$\text{GTR (avg)} = \frac{2Am}{\pi} = \frac{2Vm}{\pi} \quad \left[\text{from first quarter pulse area} \right]$$

Ex 13.15)



$$G(\text{avg}) = \frac{+2Am - 2Am}{2\pi}$$

$$= 0V$$



$$G(\text{avg}) = \frac{2Am + 0}{2\pi} = \frac{2 \times 10V}{2\pi}$$
$$= \frac{10}{\pi}$$

$V_{av} = DC = (\text{vertical shift index}) \times (\text{vertical sensitivity})$

v/s

RMS value / effective value

Power The power delivered by the ac supply at any instant of time is

$$P_{ac} = (I_{ac})^2 R = (I_m \sin \omega t)^2 R = I_m^2 \sin^2 \omega t R$$

$$\bar{P}_{av(ac)} = P_{dc}$$

$$P = \frac{1}{2} I_m^2 \cdot 2 \sin^2 \omega t \times R$$

$$= \frac{1}{2} I_m^2 (1 - \cos 2\omega t) \times R$$

$$= \frac{I_m^2 R}{2} (1 - \cos 2\omega t) \times R$$

$$= \frac{I_m^2 R}{2} (1 - \cos 2\omega t)$$

$$P_{ac} = \frac{I_m^2 R}{2} - \frac{I_m^2 R}{2} \cos 2\omega t$$

$$P_{ac} = \frac{I_m^2 R}{2} \quad \left[\frac{I_m^2 R}{2} \cos 2\omega t = 0 \right]$$

$$\bar{P}_{av(ac)} = P_{dc}$$

[ac is power or loss
dc is " " " " Pdc]

$$\frac{I_m^2 R}{2} = I_{dc}^2 \times R$$

$$\frac{I_m}{\sqrt{2}} = I_{dc}$$

AC circuit w/ sinusoidal current or voltage
 Equivalent
 (2πf) AC circuit value $I_{AC} = \frac{I_m}{\sqrt{2}}$

$$V_{DC} = \frac{V_m}{\sqrt{2}}$$

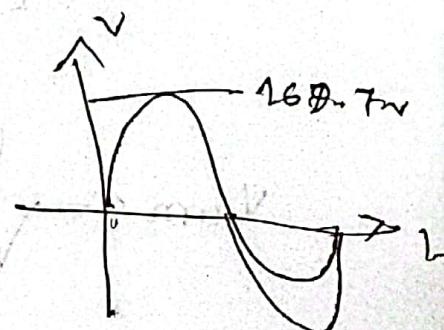
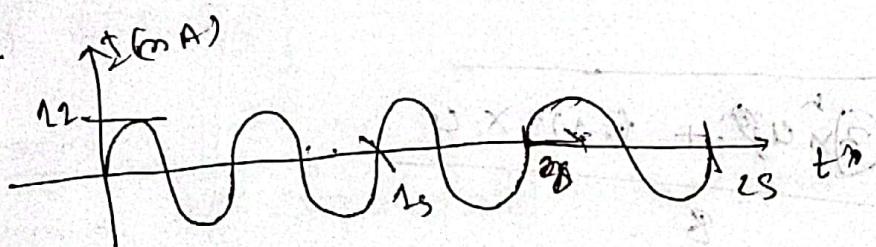
(2πf) effective value / rms value $\text{out } 169.7 \text{ V}$

r.m.s value / effective value

$$V_{eff} / V_{r.m.s} = \frac{V_m}{\sqrt{2}}$$

$$I_{eff} / I_{r.m.s} = \frac{I_m}{\sqrt{2}}$$

13.19)



$$I_{r.m.s} = \frac{I_m}{\sqrt{2}} = \frac{12}{\sqrt{2}}$$

$$= 8.484 \text{ mA}$$

$$V_{r.m.s} = \frac{169.7}{\sqrt{2}}$$

$$= 120 \text{ V}$$

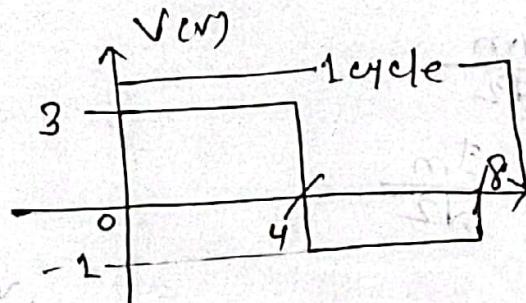
n.m.s. square wave

Square wave \Rightarrow (2πf) Area value of total square wave over the length \Rightarrow same \Rightarrow $\sqrt{A_1^2 + A_2^2}$

$$V_{n.m.s} = \sqrt{(V_m)^2 + (V_m)^2} = \sqrt{(A_1)^2 + (A_2)^2} = \sqrt{A_1^2 + A_2^2}$$

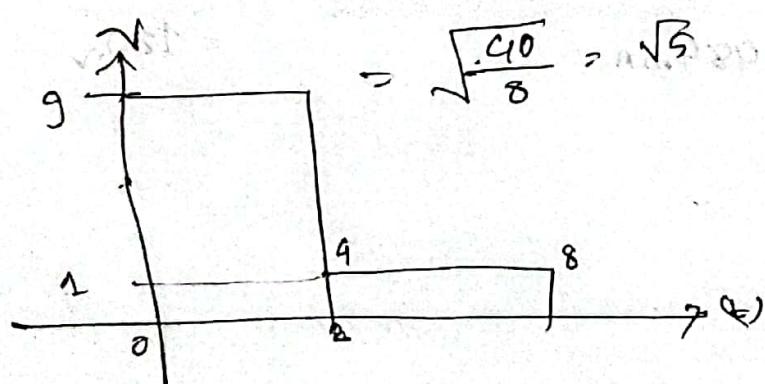
$$I_{n.m.s} = \sqrt{\frac{(I_m)^2}{2}} = \sqrt{\frac{(A_1)^2 + (A_2)^2}{2}} = \sqrt{\frac{(A_1 \times P_1) + (A_2 \times P_2)}{2}}$$

ex: 13.21



$$V_{n.m.s} = \sqrt{\frac{(3)^2 \times 4 + (-1)^2 \times 4}{8}}$$

$$\sqrt{\frac{9 \times 4 + 1 \times 4}{8}}$$



$$V_{n.m.s.} = \sqrt{\frac{V_m}{l}} = \sqrt{\frac{(L_1)^b \times P_1 + (L_2)^b \times P_2}{l}}$$

$L_1 = 493.5$
 $P_1 = 252.5$

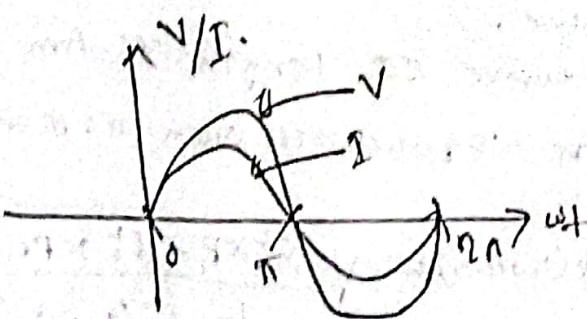
~~$I_{n.m.s.} = \sqrt{\frac{I_m}{l}} = \sqrt{(L)^b \times P}$~~

$l = \text{total length of interval}$
 complete cycle

$$I_{n.m.s.} / I_{\text{eff}} = \sqrt{\frac{\text{area}(T^m(t))}{T}}$$

[pure Inductances \Rightarrow pure Capacitor : 90° leading angle $\Rightarrow 90^\circ$ lagging angle inductor / capacitor or $I_{\text{lead}} \text{ but } 28^\circ$]

Resistance
Resistance 5Ω \Rightarrow lag / lead current occurs in



current $| V \cos \theta |$ constant phase angle $(\cos \theta)$ vs.

leading angle / lagging angle ratio

Chapter 13

Resistance

$$S = \frac{\theta}{t}$$

$A = A_m \sin \omega t$ ← normal wave formula

also given

$$V_m \rightarrow V = V_m \sin \omega t$$

$$I = I_m \sin \omega t$$

} resistance form

$$\omega = \frac{\theta}{t} = \frac{2\pi}{T}$$

$$= 2\pi n = 2\pi f$$

$$f = \frac{1}{T}$$

$$\textcircled{a} \cdot f/n = \frac{C}{\lambda} = \frac{V}{\lambda}$$

ω = angular velocity

θ = angle, t = time

T = time period

Inductor / capacitor

$$V = V_m \sin(\omega t + \phi)$$

$$I = I_m \sin(\omega t + \phi)$$

$$\text{if } V = V_m \sin(\omega t + \phi)$$

$$\text{if } V = V_m \sin(\omega t - \phi)$$

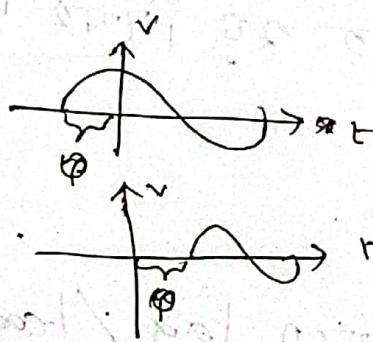
r.m.s and avg for sine wave

$$V_{r.m.s} = \sqrt{V_{eff}} = \frac{V_m}{\sqrt{2}}$$

$$I_{r.m.s} = I_{eff} = \frac{I_m}{\sqrt{2}}$$

$$V_{avg} = \frac{2V_m}{\pi}$$

square wave \rightarrow avg:



(square wave) wave \rightarrow r.m.s value.

wave go. Length \rightarrow Am (

(in square area) area (0.5 cycle)

$$A(r.m.s) = \sqrt{\frac{l_1^2 \times P_1 + l_2^2 \times P_2}{\text{length (cycle)}}}$$

Converging: $A_c(\text{average}) = \frac{\text{algebraic sum of areas}}{\text{length of curve}}$ (complete cycle)

Chapter 14

The derivative of a sine wave has the same period and frequency as the original sinusoidal wave form.

$$e(t) = E_m \sin(\omega t + \theta)$$

$$\frac{d}{dt} e(t) = \omega E_m \cos(\omega t + \theta)$$

Sinusoidal wave \Rightarrow (2πf) R, L, C, (Resistor, Inductance, Capacitor)

Resistance: resistance is, for all practical purpose, is unaffected by the frequency of the applied sinusoidal voltage. On current ... for this frequency region, the resistor in can be treated as a constant, and Ohm's Law can be applied.

$$\text{For, } V = V_m \sin \omega t$$

R \Rightarrow (2πf) frequency \Rightarrow constant \Rightarrow I = V_m / R ,
current \Rightarrow voltage \Rightarrow wave \Rightarrow point \Rightarrow current
 \Rightarrow $I = V_m / R \sin \omega t$ \Rightarrow $I = I_m \sin \omega t$

9750 2785 leading / lagging angle upto zero.

$$DC \neq I = \frac{V}{R}$$

$$I = \frac{V_m \sin \omega t}{R}$$

$$I = I_m \sin \omega t$$

$$V = IR = I_m \sin \omega t \cdot R = V_m \sin \omega t$$

$$I_m = \frac{V_m}{R} \quad \left. \begin{array}{l} \\ \end{array} \right\} \text{Ohm's Law}$$

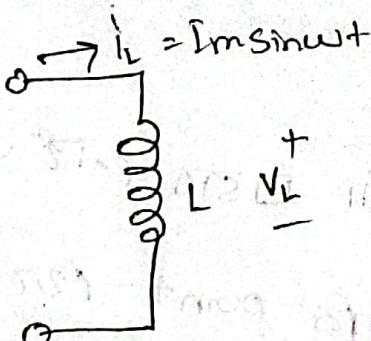
$$V_m = I_m \times R \quad \left. \begin{array}{l} \\ \end{array} \right\} \text{(AC circuit)}$$

in purely resistive circuit,

(i) Voltage, Current & peak phase same

(ii) $\text{Voltage peak's value} = \text{Current peak's value} \times \text{Resistance}$

Induction



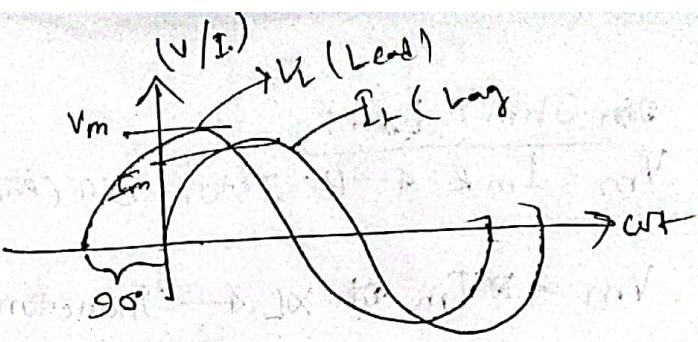
Inductance current abruptly

Change \rightarrow Induction

Current Lag $\pi/2$



$$V_L = I L \frac{di_L}{dt}$$



$$\frac{di_L}{dt} = \frac{1}{L} (I_m \sin \omega t) = \omega I_m \cos \omega t$$

$$V_L = L \frac{di_L}{dt}$$

$$V_L = L \omega I_m \cos \omega t$$

$$V_L = V_m \sin(\omega t + 90^\circ)$$

$$V_L = L \omega I_m \sin(\omega t + 90^\circ)$$

$$V_L = V_m \sin(\omega t + 90^\circ)$$

$$V_m = I_m \times \omega \times L$$

$\omega = 2\pi f$
 $\omega = \frac{2\pi}{T}$

ω = angular velocity

L = inductance

$$X_L = \omega \times L$$

$$V_m = \omega L I_m$$

$$\text{or}, V_m = X_L I_m$$

$$\text{or}, X_L = \frac{V_m}{I_m} \quad (\text{unit Ohm})$$

for inductance, V_L lead i_L by

90° , on i_L lags V_L by 90°

V_L lead 90°

i_L lag "

X_L inductor σ resistor σ ~~or~~ or not ~~or~~

$$\text{or} \cdot V = I \times R$$

$$X_L = L \times \omega$$

$$V_m = L \times X_L$$

Ohm's Law:

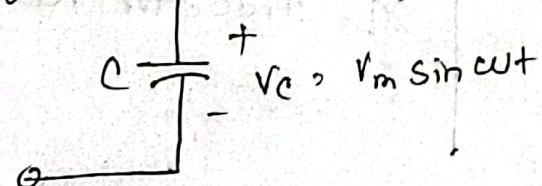
$$V_m = I_m R \leftarrow \text{Resistor } \rightarrow \text{Current}$$

$$V_m = I_m \times X_L \leftarrow \text{Inductor } \rightarrow \text{Current}$$

Inductive reactive is the opposite to the flow of current which is denoted by X_L and unit Ohm's

Capacitor

$$\rightarrow i_C = ?$$



capacitor - Voltage directly

Change \rightarrow Current \rightarrow AT

Capacitor - Voltage

lag \rightarrow

$$I_C = C \frac{dV_C}{dt}$$

$$\frac{dV_C}{dt} = \frac{d}{dt} (V_m \sin \omega t) = \omega V_m \cos \omega t \leftarrow \text{Voltage}$$

$$I_C = C (\omega V_m \cos \omega t)$$

$$I_C = C \omega V_m \cos \omega t$$

$$I_C = I_m \cos \omega t$$

$$I_C = C \omega V_m \sin (\omega t + 90^\circ)$$

$$I_C = I_m \sin (\omega t + 90^\circ)$$

C = Capacitor

V_m = maximum voltage

$$I_m = V_m \times C \times \omega$$

X_C = Capacitor reactance

$$X_C = \omega X_C$$

$$V_m = \frac{I_m}{\omega X_C}$$

$$= \frac{I_m}{\cancel{\omega} X_C}$$

$$= I_m \times X_C$$

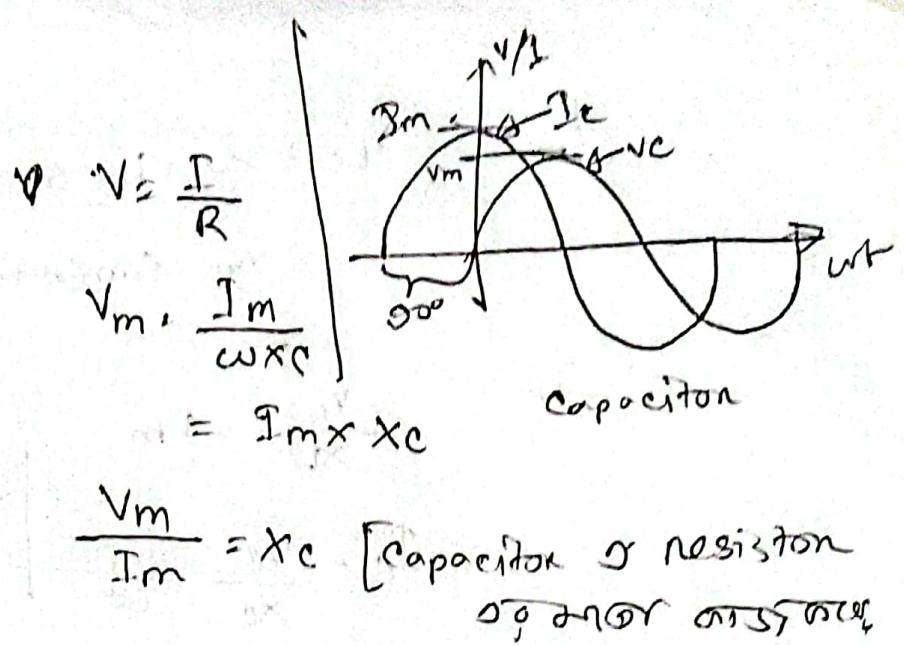
$$X_C = \frac{1}{\omega X_C}$$

X_C > Capacitor & Resistor

or या मात्रा तात्पुरता,

Capacitor & Current 90° lead वा

Voltage 90° lag वा



$$\text{or } V = \frac{I}{R}$$

$$V_m = \frac{I_m}{\omega X_C}$$

$$= I_m \times X_C$$

$$\frac{V_m}{I_m} = X_C \quad [\text{Capacitor or resistor} \text{ या मात्रा तात्पुरता}]$$

opposition

$$\frac{V_m}{I_m} = \frac{V_m}{V_m \times \omega X_C} = \frac{1}{\omega C} = X_C$$

Ideal Capacitor / Inductor या voltage / current 90° lead

या lag वा

V_2 30 sin ωt

$$L \Rightarrow V_L = L \times \omega \times I_m \sin(\omega t + 90^\circ)$$

$$\Rightarrow V_m \sin(\omega t + 90^\circ)$$

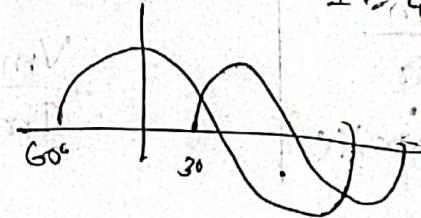
$$\frac{V_L}{X_L} \Rightarrow I_m$$

$$I_c = \frac{V_L}{X_L}$$

$$= \frac{V_c \omega c}{X_c}$$

$$I = 40 \sin(\omega t + 60^\circ)$$

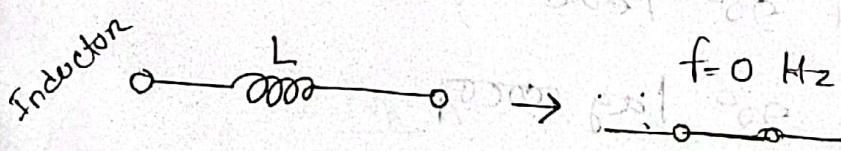
$$I_c = \frac{V_c}{X_c}$$



$$I_c \times X_c = V_c$$

$$\frac{I_c}{\omega c} = V_c$$

dc & high, low frequency effects on L and C



$$f = 0 \text{ Hz}$$

$f = \text{very high frequency}$



$f = \text{very high frequency}$

(Inductive/capacitive reactant = Resistor \gg ωR)

dc circuit \therefore frequency = zero

capacitor $f = \infty$
at $f = \text{very high frequency}$

Inductor:

$$X_L = \omega L$$

$$= 2\pi f L = 2\pi(0) L = 0$$

rectangle zero \therefore $X_L = 0$ at $f = 0$

$2\pi f \neq 0$,

inductor short circuit analogy

$$X_C = \frac{1}{\omega C}$$

$$= \frac{1}{2\pi f C}$$

$$= \frac{1}{2\pi \times 0 \times C} = \infty$$

$f \rightarrow \text{high } X_C = \text{open circuit}$

when f = very high frequency

Inductors

$$X_L = \omega L = 2\pi f L$$

f = high $\rightarrow X_L$ = high

Inductor open circuit -

→ short circuit

f → very high frequency

$$X_C = \frac{1}{\omega C}$$

$$= \frac{1}{2\pi f C}$$

when f = high open

X_C = low Ω

when Capacitor short circuit
→ short circuit Ω

Average power and power factors

$P = V I \cos \theta$ The magnitude of average power delivered

is independent of whether V leads I or I leads V .

$$P = V I = \frac{V_m}{2} I_m \cos(\theta_V - \theta_I) \quad \text{if } \theta_V \rightarrow \text{Voltage}$$

$$= \frac{V_m I_m}{2} \cos \theta$$

$$= \frac{V_m}{\sqrt{2}} \times \frac{I_m}{\sqrt{2}} \cos \theta = V_{eff} I_{eff} \cos \theta$$

Resistor \Rightarrow $\cos 0^\circ = 1$ and V \Rightarrow 0° angle difference

$$2\pi m 0^\circ \cos 0^\circ = 1$$

$$P = V_{eff} \cdot I_{eff} \cdot X_R$$

$$P = \frac{V_{eff}^2}{R} = I_{eff}^2 R$$

Induction since purely Inductive circuit $\theta_v - \theta_i = 90^\circ$

$$\Rightarrow 90^\circ, |\theta_v - \theta_i| = |90^\circ|, 90^\circ$$

$$P = \frac{I_m V_m}{2} \cos 90^\circ = 0 \text{ W}$$

Capacitor leads $\theta_v - \theta_i = 90^\circ, |\theta_v - \theta_i| = |90^\circ - 0^\circ| = 90^\circ$

$$P = \frac{I_m V_m}{2} \cos 90^\circ = 0 \text{ W}$$

power factor: V and i at 2785 , angle difference

$270^\circ - 0^\circ$ cosine of power factor.

$$F_p = \cos \theta$$

$$P = \frac{V_m I_m}{2} \cos \theta = P$$

$$P = \frac{V_m I_m}{2} F_p$$

$$\frac{2P}{V_m \times I_m} = F_p$$

Complex numbers

Rectangular form

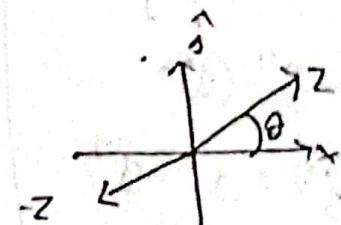
The format for the rectangular form is

$$C = x + \hat{j}y$$

$$\text{polar form} = C = z \angle \theta$$

$$-C = -z \angle \theta$$

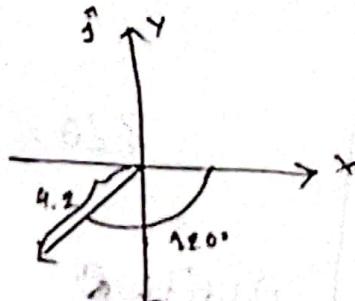
$$= z \angle \theta \pm 180^\circ$$



$$C = -4.2 \angle 60^\circ$$

$$= 4.2 \angle 60^\circ - 180^\circ$$

$$= 4.2 \angle -120^\circ$$



Rectangular to polar

$$C = x + \hat{j}y$$

$$[z = r\angle]$$

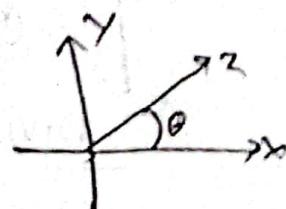
$$z = \sqrt{x^2 + y^2}$$

$$\theta = \tan^{-1} \left(\frac{y}{x} \right)$$

Polar to Rectangular

$$x = z \cos \theta$$

$$y = z \sin \theta$$



$$j = \sqrt{-1}$$

$$j^2 = \sqrt{-1} \cdot -1$$

$$\begin{aligned} j^3 &= j \cdot j \cdot -1 \\ &= -j \end{aligned}$$

$$j^4 = (1)^4$$

$$\begin{aligned} j^5 &= j^3 \cdot j^2 \\ &= -j \cdot (-1) \\ &= j \end{aligned}$$

$$\frac{1}{j} = 1 \times \frac{1}{j}$$

$$\begin{aligned} &= \frac{j}{j} \times \frac{1}{j} \\ &= \frac{j}{j^2} \end{aligned}$$

$$\frac{1}{j} = \frac{j}{-1} = -j$$

Complex conjugate

$$c = x + jy$$

$$= x - jy$$

$$\text{so } c = z \angle \theta$$

$$= z \angle -\theta$$

Reciprocal $c = x + jy$

$$= \frac{1}{x + jy}$$

$$z \angle \theta = \frac{1}{z \angle \theta}$$

Addition

$$c_1 + c_2 = (x_1 + x_2) + j(y_1 + y_2)$$

Subtraction

$$c_1 - c_2 = (x_1 - x_2) + j(y_1 - y_2)$$

multiplication

$$c_1 c_2 = (x_1 x_2 - y_1 y_2) + j(y_1 x_2 + x_1 y_2)$$

$$\frac{c_1}{c_2} = \frac{x_1 + jy_1}{x_2 + jy_2} \cdot \frac{x_1 x_2 + y_1 y_2 + j y_1 x_2 - x_1 y_2}{x_2^2 + y_2^2}$$

for Pto polar forms

মনে রাখি polar form জো angle same হবে। তা আর

জো angle difference মনে 180° ৰে কোণ যোগ কোণ বৰ্তন
অথাৎ multiplication কোণ যোগ,

Ex: $2\angle 45^\circ + 3\angle 45^\circ = 5\angle 45^\circ$

$$2\angle 0^\circ + 4\angle 180^\circ = 6\angle 0^\circ$$

multiplication

$$C_1 = Z_1 \angle \theta_1, C_2 = Z_2 \angle \theta_2$$

$$C_1 \cdot C_2 = Z_1 Z_2 \angle \theta_1 + \theta_2$$

Division: $C_1 = Z_1 \angle \theta_1, C_2 = Z_2 \angle \theta_2$

$$\frac{C_1}{C_2} = \frac{Z_1 \angle \theta_1}{Z_2 \angle \theta_2} = \frac{Z_1}{Z_2} \angle \theta_1 - \theta_2$$



Polar forms

8 Chapter - 14

Sine

Sine wave \Rightarrow formula,

$$e(t) = E_m \sin(\omega t + \theta)$$

Pure resistor \Rightarrow current

$$\omega = \frac{\theta}{t} = \frac{2\pi}{T} = 2\pi f$$

$$V = V_m \sin \omega t \quad | \quad \theta = 0$$

$$I = I_m \sin \omega t$$

$$\text{Ohm's Law: } V = I R \quad | \quad I = \frac{V}{R}$$

$$I_m = \frac{V_m}{R}$$

Pure inductor \Rightarrow current

V and I \Rightarrow angle difference $\theta = 90^\circ$.

$$V = V_m \sin \omega t \quad | \quad I = I_m \sin(\omega t + 90^\circ)$$

$$(1) \quad I = I_m \sin \omega t$$

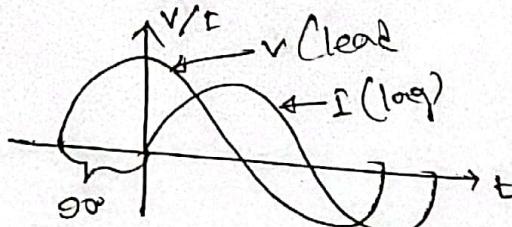
$$(2) \quad V = V_m \sin(\omega t + 90^\circ)$$

$$(3) \quad V_L = L \times \frac{di}{dt}$$

$$(4) \quad V_m = I_m \times \omega \times L$$

$$= I_m \times X_L$$

$$(5) \quad X_L = \omega L \quad | \quad (\text{inductive reactance})$$



ω = angular velocity

$$I_m = I_{max} \Rightarrow V_m = V_{max}$$

L = inductor (unit H)

X_L = Inductive reactance

(not resistor or motor)

$$X_L = \omega L$$

$$= 2\pi f L$$

$$I_m = \frac{V_m}{X_L} \quad (\text{Ohm's Law})$$

X_L (unit Ohm) Resistor

মাত্র তাৰা একই ইন্ডেক্ষন

But angle

Capacitors

$$(1) V_C = V_m \sin \omega t$$

$$(2) I_C = I_m \sin(\omega t + 90^\circ)$$

$$(3) I_m = V_m \times \omega \times C$$

$$(4) I_m = \frac{V_m}{X_C}$$

$$(5) X_C = \frac{1}{\omega C}$$

↑ (Capacitor ৰেজিস্টর

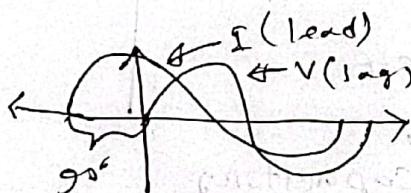
একই কিমু একই

But অংক

difference

ওজন

$$(6) X_C = \frac{1}{2\pi f C}$$



V_C = Voltage of capacitor

I_C = Current of capacitor

$I_m = I_{max}$, $V_m = V_{max}$

X_C = capacitive reactance

↳ resistance দ্বাৰা নিৰ্ভৰ

কোণ

f/n = frequency

C = capacitor (unit F)

power%

$$P = \frac{V_m I_m}{2} \cos \theta$$

$$= V_{eff} I_{eff} \cos \theta$$

$$F_p = \cos \theta$$

resistor $\theta = 0^\circ$ (v and i 0° ziffern)

$$P = \frac{V_m I_m}{2}$$

$$P = V_{eff} \cdot I_{eff}$$

pure Inductor/Capacitor

$$\theta = 90^\circ$$

$$\cos 90^\circ = 0$$

$$P = \frac{V_m I_m}{2} \times 0 = 0$$

$$F_p = P = \frac{V_m I_m}{2} \cos \theta$$

$$P = \frac{V_m I_m}{2} F_p$$

$$F_p = \frac{2P}{V_m I_m}$$

F_p = power factor

$\theta = v$ and i $\Delta\varphi$ $\Delta\theta$
angle difference

$$V_{eff} = V_{r.m.s}$$

$$= \frac{V_m}{\sqrt{2}}$$

$$I_{eff} = I_{r.m.s}$$

$$= \frac{I_m}{\sqrt{2}}$$

$$\theta = |\theta_v - \theta_i|$$

$$= 90^\circ$$

} power factor

Chapter - 15g

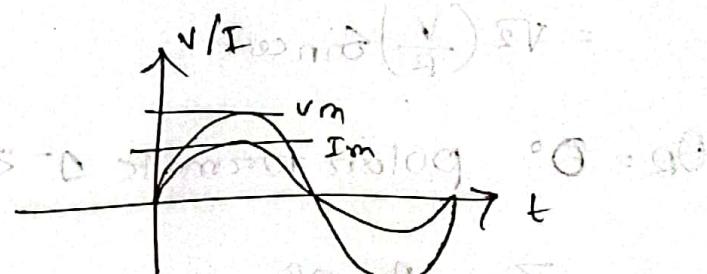
■ Series AC Circuits (Impedance and phasor form)

Resistive Elements $\varphi = 0$ (V and i in same angle difference)

for purely resistive

$$I_m = \frac{V_m}{R}$$

$$V_m = I_m R$$



$$\frac{V}{R} = V_m \sin \omega t = V \angle 0^\circ \quad [\text{where } V = \frac{V_m}{\sqrt{2}}]$$

$$(f) I_R = I_m \sin \omega t = I \angle 0^\circ \quad [\text{where } I = \frac{I_m}{\sqrt{2}}]$$

$$V = \frac{V_m}{\sqrt{2}}$$

$$\sqrt{2} V = V_m$$

$$I = \frac{I_m}{\sqrt{2}}$$

$$I \times \sqrt{2} = I_m$$

(*) Using phasor Diagram and applying Ohm's Law

$$I = \frac{V}{R} = \frac{V \angle 0^\circ}{R \angle 0^\circ}$$

($\cancel{\sqrt{2}}$) $\angle 0^\circ + 0^\circ$ angle difference 0° or 90°

$$\theta_R = 0^\circ$$

$$I = \frac{V}{R} = \frac{V \angle 0^\circ}{R \angle 0^\circ} = \frac{V}{R} \angle 0^\circ - 0^\circ = \frac{V}{R} \angle 0^\circ$$

$$I_m = \frac{V_m}{R}$$

$$= \sqrt{2} \left(\frac{V}{R} \right)$$

$$I = I_m \sin \omega t$$

$$= \sqrt{2} \left(\frac{V}{R} \right) \sin \omega t$$

$\theta_R = 0^\circ$ polar formate ଏହିରେ ପାର୍ଶ୍ଵ ଦିଶ୍ବି ପାର୍ଶ୍ଵ (proper phasor reference).

$$Z_R = R \angle 0^\circ$$

phasor relation
ship

Z_R : Impedance of a resistive element between V and I)

ଏହି Impedance କମେଟାର କୁଣ୍ଡଳୀ (କେନ୍ଦ୍ରିଯାତ୍ମିକ କମେଟାର କୁଣ୍ଡଳୀ) କିମ୍ବା କମେଟାର କୁଣ୍ଡଳୀ
~~କେବଳ~~ charge, ^{flow} କାହାରେ ଆବଶ୍ୟକ ଏହାରେ ଏହାରେ ଏହାରେ ଏହାରେ

ଏହା କମେଟାର କିମ୍ବା ରିସିଟର କିମ୍ବା ମାତ୍ର,

ଏହା ଏକ ଓନ୍ଟ ଓମ.

Z_R phason ହାତୀ,

Ex: $V_m = 100V$ $I_m = 20A$

$$V = V_m \sin \omega t \quad I = 20 \sin \omega t \\ = 100 \sin \omega t$$

$$V = 100 \sin \omega t \rightarrow (\text{phasor form})$$

$$V = \frac{V_m}{\sqrt{2}} \angle 0^\circ$$

$$V = \frac{100}{\sqrt{2}} \angle 0^\circ \quad (\text{phasor form})$$

$$V = 70.71 \angle 0^\circ$$

$$R = \frac{V}{I} = \frac{100}{20} = \frac{V_m}{I_m}$$

$$= 5 \Omega$$

$$I = \frac{V \angle 0^\circ}{Z \Omega} = \frac{V \angle 0^\circ}{R \angle 0^\circ} = \frac{70.71 \angle 0^\circ}{5 \angle 0^\circ}$$

$$= 14.14 \angle 0^\circ$$

$$\therefore I = \sqrt{2} \left(\frac{V}{R} \right) \sin \omega t$$

$$= \frac{V_m}{R} \sin \omega t$$

$$= \frac{100}{5} \sin \omega t$$

$$= 20 \sin \omega t$$

Expt 15.2 $I = 4 \sin(\omega t + 30^\circ) \quad V = ?$

$$R = 2 \Omega$$



$$I_m = \frac{V_m}{R}$$

$$4 \times 2 = V_m = 8$$

$$V = 8 \sin(\omega t + 30^\circ)$$

$$V_m = \sqrt{2} \frac{V}{R}$$

$$\frac{4 \times 2}{\sqrt{2}} = V$$

$$5.656 \angle 0^\circ = V$$

$$I = \sqrt{2} \times 4 \text{ A}$$

$$I = \frac{I_m}{\sqrt{2}} = \frac{4}{\sqrt{2}} = 2.828$$

$$I = I_m \sin(\omega t + 30^\circ)$$

$$= I \angle 0^\circ$$

$$= 2.828 \angle 0^\circ$$

$$I = \frac{V \angle 0^\circ}{R \angle 0^\circ}$$

$$V = I \angle 0^\circ \times R \angle 0^\circ$$

$$= 2.828 \angle 0^\circ \times 2 \angle 0^\circ$$

$$= 5.656 \angle 0^\circ$$

Inductor $\angle 90^\circ$ (纯感性) (pure inductor $\angle 90^\circ$)

Inductive Reactance $X_L = \omega L$

V and i angle difference $\theta = 90^\circ$

Induction $\angle 90^\circ$ Voltage lead $\angle 90^\circ$

$$V = V_m \sin \omega t$$

$$= V \angle 0^\circ$$

$$I = \frac{V \angle 0^\circ}{X_L \angle \theta_L} \Rightarrow \frac{V}{X_L} \angle 0^\circ - \theta_L$$

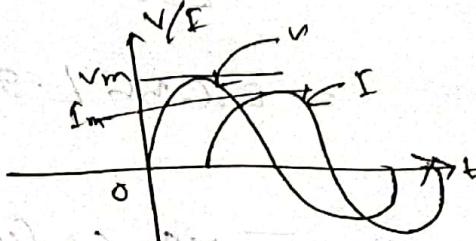
$$I \angle (90^\circ - \theta_L) = 2.828 \angle 90^\circ$$

since V leads I by 90° . I must have an angle of -90°

$$\theta_L = 90^\circ$$

$$I = \frac{V \angle 0^\circ}{Z_L \angle 90^\circ} = \frac{V \angle 0^\circ}{X_L \angle 90^\circ} I_m = \frac{V}{X_L} \angle 0^\circ - 90^\circ$$

$$I = \frac{V}{X_L} \angle -90^\circ$$



$$I = \frac{\sqrt{2}V}{X_L} \sin(\omega t - 90^\circ)$$

X_L = inductance mH , Resistor Ω or ohms . But angle $0\pi/2$

$$Z_L = X_L \angle 90^\circ + \text{impedance}$$

Z_L is Unit Ω , Ohms. It measured how much

the inductive element will "control on impedance" through the network (বাটৰ) the level of current

Exp: 15.3

$$V_m = 24V \quad \theta = 90^\circ \quad X_L = 3\Omega$$

$$I_m = 8A$$

$$V = 16.97 \angle 0^\circ$$

$$V = \frac{24}{\sqrt{2}} = 16.97V$$

$$I = 5.657 \angle -90^\circ$$

$$I = \frac{I_m}{\sqrt{2}} = 5.657 \angle -90^\circ$$

$$I = \frac{V \angle 0^\circ}{X_L 90^\circ}$$

$$I_m = \sqrt{2} \times I$$

$$\Rightarrow \frac{16.97 \angle 0^\circ}{3 \angle 90^\circ}$$

$$= 5.656 \angle -90^\circ$$

$$I = 5.656 \angle -90^\circ$$

$$I = \sqrt{2} \times I \sin(\omega t - 90^\circ)$$

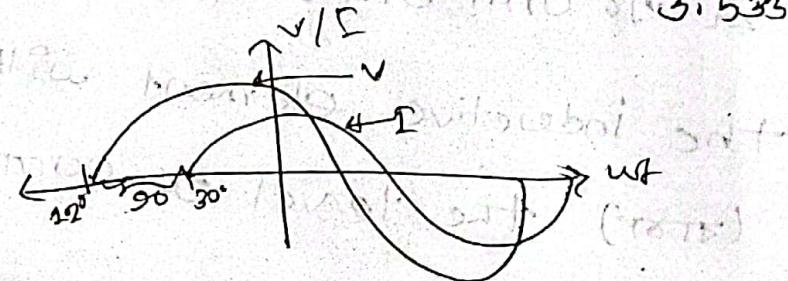
$$= \sqrt{2} (5.656) \angle -\sin(\omega t - 90^\circ)$$

$$= 8 \sin(\omega t - 90^\circ)$$

$$15.4] I = 5 \sin(\omega t + 30^\circ) \quad [I_{\max} \times \sqrt{2} = I' \quad I = I_m \frac{\sqrt{2}}{\sqrt{2}} = \frac{5}{\sqrt{2}}$$

$$X_L = 4 \Omega$$

$$I \approx 2i = V_L$$



$$3.535 \angle 30^\circ \times 4 \angle 90^\circ = V_L$$

$$14.14 \angle 120^\circ = V_L$$

$$V_L = \sqrt{2} \times (14.14) \sin(\omega t + 120^\circ)$$

$$= 100.20 \sin(\omega t + 120^\circ)$$

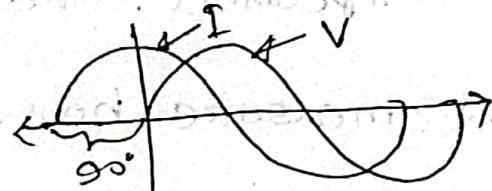
Capacitors

Capacitive Reactance)

for pure capacitor current leads voltage by 90°

angle difference between V and I ; $\theta = 90^\circ$

$$X_C = \frac{1}{\omega C}$$



$$V = V_m \sin \omega t$$

$$\text{phasor form } V = \sqrt{V_m^2} \angle 0^\circ \quad \left[V = \frac{V_m}{\sqrt{2}} \right]$$

Applying Ohm's Law and using phasor algebra.

$$I = \frac{\sqrt{V_m^2} \angle 0^\circ}{X_C \angle 90^\circ} = \frac{\sqrt{V_m^2}}{X_C} \angle 0 - 90^\circ$$

I lead V by 90° , i must have an angle 90° .

$$\text{so } \theta_C = -90^\circ$$

$$I = \frac{\sqrt{V_m^2} \angle 0^\circ}{X_C \angle -90^\circ} = \frac{\sqrt{V_m^2}}{X_C} \angle 0 - (-90^\circ)$$

$$I = \frac{\sqrt{V_m^2}}{X_C} \angle 90^\circ$$

$$I = I_m \sin(\omega t + 90^\circ)$$

$$= \left(\frac{\sqrt{2} V_m}{X_C} \right) \sin(\omega t + 90^\circ)$$

$$\boxed{Z_C = X_C \angle -90^\circ} \rightarrow \text{impedance}$$

X_C = Capacitive reactance (not Resistance or ω)
But angle ωt is increasing along with

Z_C = Impedance, and it's unit Ohm's.

It measure how much the capacitor element will "control and impede" ($\propto \omega$) the flow of current through the network.

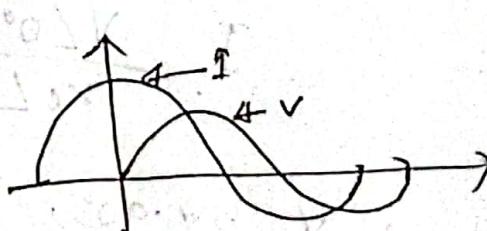
exp
15.5

$$X_C = 2\Omega$$

$$V = 15 \sin \omega t$$

$$\therefore V = \frac{15}{\sqrt{2}} \angle 0^\circ$$

$$= 10.61 \angle 0^\circ$$



$$I_C = \frac{V \angle 10.61 \angle 0^\circ}{2 \angle -90^\circ} = 5.303 \angle 0^\circ - (-90^\circ)$$

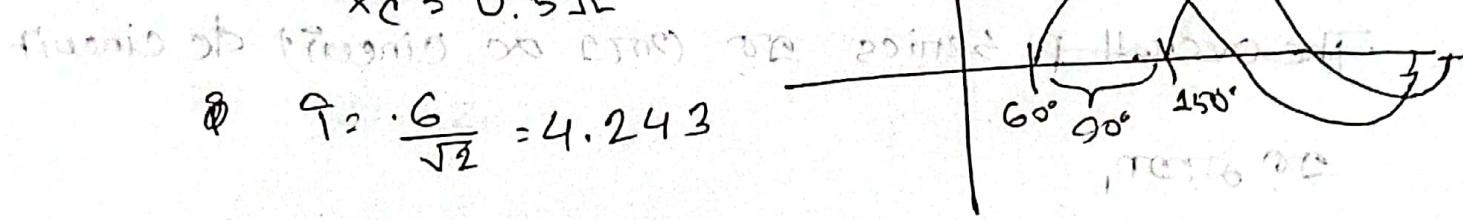
$$I = 5.303 \angle 90^\circ$$

$$I = \sqrt{2} \times (5.303) \sin(\omega t + 90^\circ)$$

$$= 7.5 \sin(\omega t + 90^\circ)$$

$$15.6] \quad i = 6 \sin(\omega t - 60^\circ)$$

$$X_C = 0.5 \Omega$$



$$\therefore \quad i = \frac{6}{\sqrt{2}} = 4.243$$

$$i = 4.243 \angle -60^\circ$$

$$Z_C = 0.5 \angle -90^\circ$$

$$i \times Z_C = \text{v}_C$$

$$4.243 \angle -60^\circ \times 0.5 \angle -90^\circ = \text{v}_C$$

$$2.121 \angle -150^\circ = \text{v}_C$$

$$\therefore \text{v}_C = \sqrt{2} (2.121) \sin(\omega t - 150^\circ)$$

$$= 3 \sin(\omega t - 150^\circ)$$

Impédance:

$$(1) Z_R = R \angle 0^\circ \text{ ohm}$$

$$(2) Z_L = X_L \angle 90^\circ \text{ ohm}$$

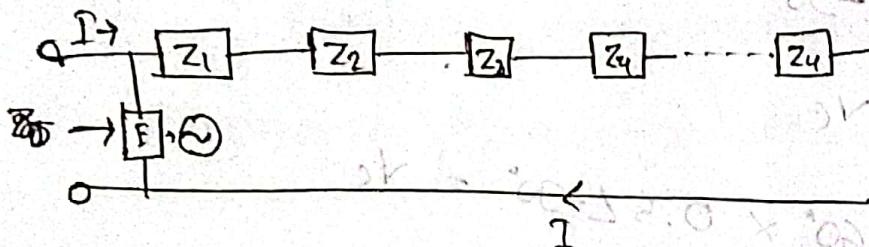
$$(3) Z_C = X_C \angle -90^\circ \text{ ohm}$$

Series Configuration

The overall p. series or (207) ac circuit dc circuit

in action,

$$Z_T(\text{total}) = z_1 + z_2 + z_3 + z_4 + \dots + z_n$$



Ans

$$I = \frac{E}{Z_T}$$

E = Supply voltage

(Ac supply)

Z_T = total impedance

The voltage across the each element can then be found by another application of Ohm's law;

$$V_1 = I z_1$$

θ_T = angle difference

$$V_2 = I z_2$$

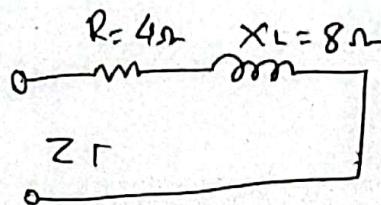
de between V and

$$E = V_1 + V_2$$

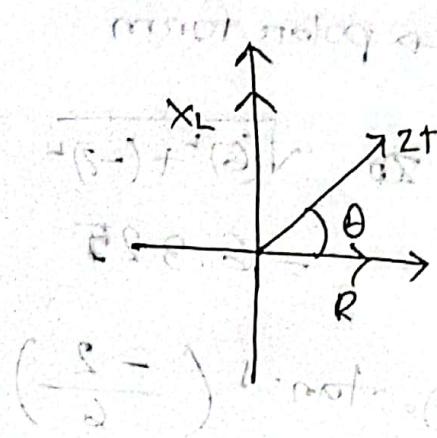
Power to the circuit (series connection)

$$P = EI \cos \theta_T$$

expg 15.7



$$\begin{aligned} Z_T &= Z_R + Z_L \\ &= R \angle 0^\circ + X_L \angle 90^\circ \\ &= R + jX_L \\ &= 4 + j8\Omega \end{aligned}$$

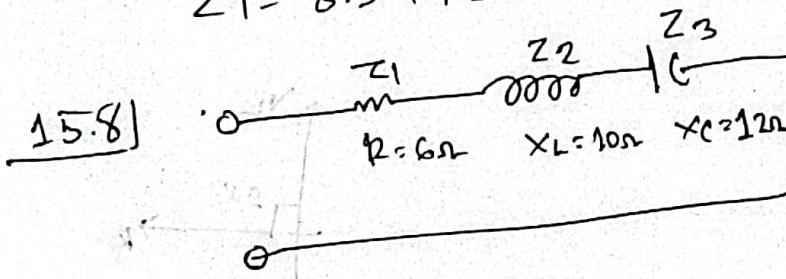


$Z_T \rightarrow$ polar form

$$Z_T = \sqrt{(4)^2 + (8)^2} = 8.944$$

$$\theta = \tan^{-1}\left(\frac{8}{4}\right) = 63.43^\circ$$

$$Z_T = 8.944 \angle 63.43^\circ$$

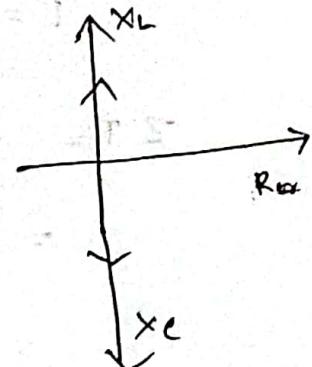


$$\begin{aligned} Z_T &= Z_1 + Z_2 + Z_3 \\ &= R \angle 0^\circ + X_L \angle 90^\circ + X_C \angle -90^\circ \end{aligned}$$

$$= R + jX_L - jX_C$$

$$= R + j(X_L - X_C)$$

$$= 6 + j(10 - 12) = 6 - j2$$



$ZT \rightarrow$ polar form

$$ZT = \sqrt{(6)^2 + (-2)^2}$$

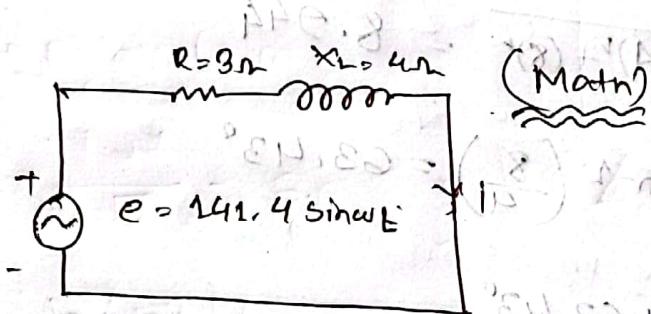
$$= 6.325$$

$$\theta = \tan^{-1} \left(\frac{-2}{6} \right)$$

$$= -18.43^\circ$$

$$ZT = 6.325 \angle -18.43^\circ$$

R-L



$$e = 141.4 \sin \omega t$$

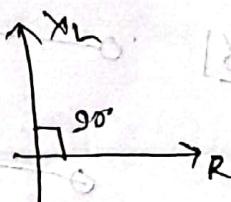
$$R = 100 \angle 0^\circ$$

$$ZT = Z_R + Z_L$$

$$= R \angle 0^\circ + X_L \angle 90^\circ$$

$$= 3 \angle 0^\circ + 4 \angle 90^\circ$$

$$= 3 + j4$$



ZT polar form $\Rightarrow (3\sqrt{9+16}) \angle \tan^{-1}\left(\frac{4}{3}\right) = 53.13$

$$Z_T = 5 \angle 53.13^\circ$$

$$I = \frac{100 \angle 0^\circ}{5 \angle 53.13^\circ}$$

$$= 20^\circ \angle -53.13^\circ$$

$$\frac{I}{Z_T} = \frac{100 \angle 0^\circ}{20 \angle -53.13^\circ}$$

$$\textcircled{1} P = EI \cos \theta_T$$

$$= E_{\text{eff}} I_{\text{eff}} \cos \theta_T$$

$$\text{E.m.f.} \rightarrow E_{\text{eff}} = \frac{E_m}{\sqrt{2}}$$

$$= \frac{141.4}{\sqrt{2}} = 100V$$

$$\textcircled{2} I_{\text{m.s.}} \rightarrow I_{\text{eff}} = \frac{I_m}{\sqrt{2}} = 20A$$

$$P = E_{\text{eff}} I_{\text{eff}} \cos \theta_T$$

$$= (100 \times 20) \cos 53.13^\circ$$

$$\approx 1200W$$

R $\angle 0^\circ$ power

$$P_R = V_R I \cos \theta_R$$

$$= (60 \times 20) \cos 50^\circ$$

$$= 1200$$

$$V_R = I Z_R$$

$$= 20 \angle -53.13^\circ \times 3 \angle 0^\circ$$

$$= 60^\circ \angle -53.13^\circ$$

$$V_L = I Z_L$$

$$= 20 \angle -53.13^\circ \times 4 \angle 90^\circ$$

$$= 80 \angle 36.87^\circ$$

(E1-E2 + Induced EMF) $\angle 0^\circ$

max. voltage $\angle 90^\circ$

$$\theta_T = (\theta_V - \theta_i)$$

$$= (0^\circ - (-53.13))$$

$$= 153.13^\circ \approx 53.13^\circ$$

$8 + 0.83j$

$8 + j0.83$

$8 + j0.83$

L $\angle 0^\circ$ power

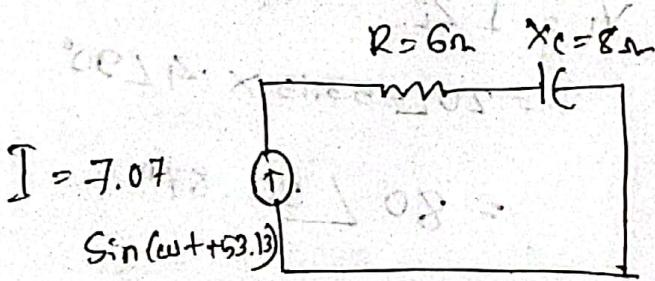
$$P_L = V_L I \cos \theta_L$$

$$\Rightarrow (80 \times 20) \cos 90^\circ$$

$$= 0$$

$$P_T = P_R + P_L = 1200 + 0 = 1200 \text{ W}$$

* R-C: Math



$$I = 7.07 \sin(\omega t + 53.13)$$

$I \rightarrow$ polar form

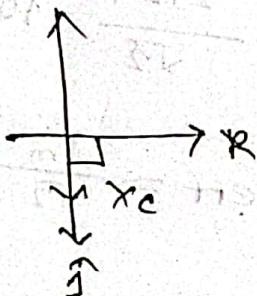
$$I = \frac{7.07}{\sqrt{2}} = 5 \text{ A}$$

$$\text{bom} \angle \theta = 53.13$$

$$Z_T = Z_R + Z_C$$

$$= 6 \angle 0^\circ + 8 \angle -90^\circ$$

$$= 6 - j8$$



$Z_T \rightarrow$ polar form

$$Z_T = 6 - j8$$

$$\sqrt{36+64} = 10$$

$$\theta = \tan^{-1} \left(\frac{-8}{6} \right) = -53.13$$

$$Z_T = 10 \angle -53.13$$

$$V_{TR2}, E = I \times Z$$

$$E = 5 \angle 53.13^\circ \times 20 \angle -53.13^\circ \\ = 50 \angle 0^\circ$$

$$V_R = \sqrt{Z_R} = 5 \angle 53.13^\circ \times 6 \angle 0^\circ$$

$$= 30 \angle 53.13^\circ$$

$$V_C = I Z_C = 5 \angle 53.13^\circ \times 8 \angle -90^\circ$$

$$= 40 \angle -36.86^\circ$$

PT_(tot+ai)

$$P_r = \Theta F_{eff} I_{eff} \cos \theta_t$$

$$\theta_r = (\theta_v - \theta_i) = (0 - 53.13^\circ) \\ = -53.13^\circ = 53.13^\circ$$

$$F_{eff} = \frac{E}{\sqrt{2}} = 50$$

$$I_{eff} = \frac{I}{\sqrt{2}} = 5$$

$$P_r = (50 \times 5) \cos 53.13^\circ$$

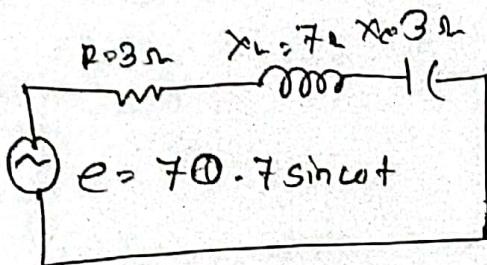
$$= 250 \cos 53.13^\circ$$

$$= 150$$

$$P_R = V_R I \cos \theta_R = 30 \times (30 \times 5) \cos 0^\circ \\ = 150 \times 15$$

$$P_C = V_C I \cos \theta_C = (40 \times 5) \cos -90^\circ = 0$$

R-L-C in Math



$e = 70.7 \sin \omega t \rightarrow$ polar form phase diagram

$$E = \frac{70.7}{\sqrt{2}} \angle 0^\circ$$
$$= 50 \angle 0^\circ$$

$$X_L = 7 \Omega, X_C = -$$

$$X_L = 7 \angle 90^\circ$$

$$X_C = 3 \angle -90^\circ$$

$$X_L = 7 \Omega, X_C = 3 \Omega, R = 3 \Omega$$

$$Z_T = Z_R + Z_L + Z_C$$

$$= R \angle 0^\circ + X_L \angle 90^\circ + X_C \angle -90^\circ$$

$$= 3 \angle 0^\circ + 7 \angle 90^\circ + 3 \angle -90^\circ$$

$$Z_T = 3 \angle 0^\circ + 3 + j7 - j3 = 3 + 4j$$

$Z_T \rightarrow$ polar form

$$Z_T = 3 + 4j$$

$$\Rightarrow \sqrt{(3)^2 + (4)^2} = 5$$

$$\tan^{-1} \left(\frac{4}{3} \right) = 53.13^\circ$$

$$Z_T = 5 \angle 53.13^\circ$$

$$I = \frac{E}{Z_T} = \frac{50 \angle 0^\circ}{5 \angle 53.13^\circ}$$
$$\Rightarrow 10 \angle -53.13^\circ$$

$$\forall V_R = I R \angle Z_R$$

$$= 10 \angle -53.13^\circ \times 3 \angle 0^\circ$$

$$= 30 \angle -53.13 + 0 = 30 \angle -53.13$$

$$V_L = I Z_L = 10 \angle -53.13 \times 7 \angle 90^\circ$$

$$= 70 \angle 36.87^\circ$$

$$V_C = I Z_C = 10 \angle -53.13 \times 3 \angle -90^\circ$$

$$= 30 \angle 143.13^\circ$$

power $\Phi = EI \cos \theta_T$

$$\theta_T = |(\theta_V - \theta_i) - |(\theta - 53.13)|$$
$$= 53.13$$

$$E_{eff} = \frac{E}{\sqrt{2}} = 50$$

$$I_{eff} = \frac{I}{\sqrt{2}} = 10$$

$$\Phi = (50 \times 10) \cos 53.13^\circ$$

$$> 300 \text{ W}$$

Power Factor

$$F_p = \cos \theta$$

$$Z_T = \frac{E}{I}$$

$$P = EI \cos \theta$$

$$\frac{P}{EI} = \cos \theta$$

$$\frac{\cancel{P}}{\cancel{EI}} \cdot \frac{I^2 R}{EI} = \cos \theta$$

$$\cancel{\frac{P}{E}} \cdot \frac{R}{\frac{EI}{I^2}} = \cos \theta$$

$$\Rightarrow \frac{R}{\frac{E}{I}} = \cos \theta$$

$$\Rightarrow \frac{R}{Z_T} = \cos \theta$$

$$\frac{R}{r Z_T} = F_p$$

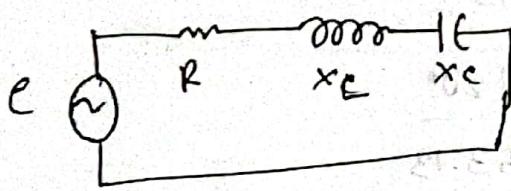
$$\boxed{F_p = \cos \theta = \frac{R}{Z_T}}$$

Voltage divider rules

ac dc circuit or voltage divider rule or

ac circuit or voltage divider rules same

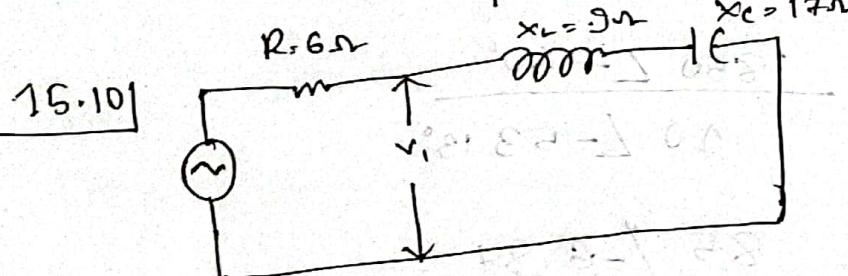
$$V_x = \frac{Z_x E}{Z_T}$$



$$Z_T = Z_R + Z_L + Z_C$$

$$e = E$$

$$V_R = \frac{Z_R \times E}{Z_T} \quad V_L = \frac{Z_L \times E}{Z_T} \quad V_C = \frac{Z_C \times E}{Z_T}$$



$$V_R = \frac{Z_R E}{Z_R + Z_C + Z_L} = \frac{6 \times 0^\circ \cdot (50 \angle 30^\circ)}{6 \angle 0^\circ + 9 \angle 90^\circ + 17 \angle -90^\circ}$$

$$= \frac{30 \angle 30^\circ}{6 + 9j - 17j}$$

$$\frac{30 \angle 30^\circ}{6 - 8j} = \frac{30 \angle 30^\circ}{20 \angle -53.13^\circ}$$

$$= 3 \angle 83.13^\circ$$

Z_T polar form

$$Z_T = 6 - 8j \quad \therefore \sqrt{(6)^2 + (8)^2} = 10$$

$$\tan^{-1}\left(\frac{-8}{6}\right) = -53.13^\circ$$

$$V_L = \frac{Z_L \times E}{Z_T} = \frac{2L90^\circ \times 50 \angle 30^\circ}{10 \angle -53.13^\circ}$$

$$= \frac{450 \angle 120^\circ}{10 \angle -53.13}$$

$$\Rightarrow 45 \angle 173.13$$

$$V_C = \frac{Z_C E}{Z_T} = \frac{1.7 \angle 90^\circ \times 50 \angle 30^\circ}{10 \angle -53.13}$$

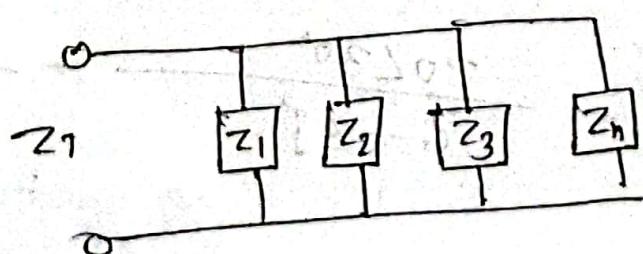
$$= \frac{850 \angle +60^\circ}{10 \angle -53.13}$$

$$\therefore 85 \angle -6.87$$

III Parallel ac circuits

... parallel σ ac circuit യൂണി ഡീ സൈറ്റ്

രണ്ട്



$$\frac{1}{Z_T} = \frac{1}{Z_1} + \frac{1}{Z_2} + \frac{1}{Z_3} + \dots + \frac{1}{Z_n}$$

$$\frac{1}{Z_T} = \frac{1}{Z_1} + \frac{1}{Z_2}$$

$$Z_T = \frac{Z_1 \times Z_2}{Z_1 + Z_2}$$

④ $I_1 = \frac{E}{Z_1}, I_2 = \frac{E}{Z_2}$

⑤ $I = I_1 + I_2$

degree: angle

$$\therefore \frac{1}{Z_R} = \frac{1}{R \angle 0^\circ} = G_R \angle 0^\circ$$

G_R = Conductance

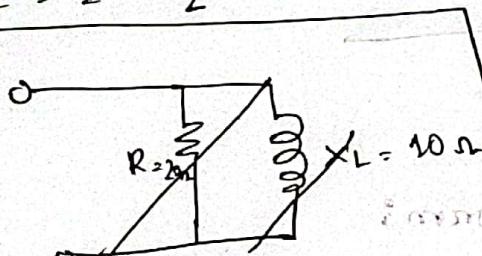
$$\therefore \frac{1}{Z_L} = \frac{1}{X_L \angle 90^\circ} = \frac{1}{X_L} \angle -90^\circ$$

$$\therefore \frac{1}{Z_C} = \frac{1}{X_C \angle -90^\circ} = \frac{1}{X_C} \angle +90^\circ$$

⑥ power for parallel circuits

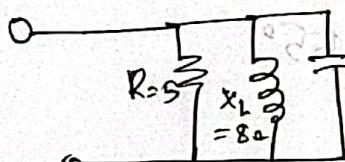
$$P = EI \cos \theta_T$$

15.12



$$Z_T = \frac{1}{Z_R} + \frac{1}{Z_L}$$

15.13



$$\frac{1}{Z_T} = \frac{1}{Z_R} + \frac{1}{Z_{X_L}} + \frac{1}{Z_{X_C}}$$

$$= \frac{1}{R \angle 0^\circ} + \frac{1}{8 \angle 90^\circ} + \frac{1}{20 \angle -90^\circ}$$

$$= \frac{(8 \angle 90^\circ \times 20 \angle -90^\circ) + (5 \angle 0^\circ \times 20 \angle -90^\circ) + (5 \angle 0^\circ \times 8 \angle 90^\circ)}{5 \angle 0^\circ \times 8 \angle 90^\circ \times 20 \angle -90^\circ}$$

$$= 160 \angle 0^\circ + 100 \angle -90^\circ + 40 \angle 90^\circ$$

$$\frac{1}{Z_T} = \frac{160 \angle 0^\circ + 100 \angle -90^\circ + 40 \angle 90^\circ}{800 \angle 0^\circ}$$

$$Z_T =$$

$$\frac{800 \angle 0^\circ}{160 \angle 0^\circ + 100 \angle 90^\circ + 40 \angle -90^\circ}$$

$$= \frac{800 \angle 0^\circ}{160 + 100j - 40j}$$

$$= \frac{800 \angle 0^\circ}{160 + 60j}$$

$160 + 60j$ to polar form:

$$\sqrt{(160)^2 + (60)^2}$$

$$= 170.88$$

$$\theta = \tan^{-1} \left(\frac{-60}{160} \right) = 20.55^\circ$$

$$160 + 60j \text{ polar form } 170.88 \angle -20.55^\circ$$

$$Z_T = \frac{800 \angle 0^\circ}{170.88 \angle -20.55^\circ}$$

$$= 4.68 \angle +20.55^\circ$$

Q. power factor for parallel

$$F_p = \cos \theta$$

$$P = EI \cos \theta$$

$$\text{or, } P = EI F_p$$

$$\text{or, } \frac{P}{EI} = F_p$$

$$\text{or, } F_p = \frac{P}{R \times E \times I}$$

$$= \frac{E}{RC}$$

$$= \frac{1}{R} \times \frac{E}{I}$$

$$= G_R \times \frac{1}{I}$$

$$= G_R \times \frac{1}{ZT} = \frac{G_R}{ZT}$$

$$F_p = G_R \times ZT$$

$$= \frac{ZT}{R}$$

current Divider Rule:

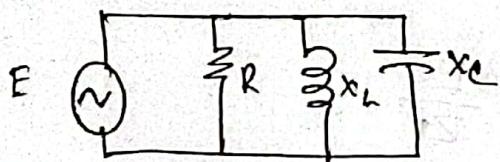
current divider rule is same for ac & dc.

and dc circuit.

$$I_1 = \frac{Z_2 I_T}{Z_1 + Z_2}, \quad I_2 = \frac{Z_1 I_T}{Z_1 + Z_2}$$

maths part

R-C-Lg 15.71



$$\text{Q. } E = \sqrt{2} (100) \sin(\omega t + 53.13^\circ) = 100 \angle 53.13^\circ$$

$$P = 70.7 \sin \omega t$$

$$X_L = 1.43 \Omega, R = 3.33 \Omega, X_C = 3.33 \Omega$$

$$\frac{1}{Z_T} = \frac{1}{Z_R} + \frac{1}{Z_C} + \frac{1}{Z_L}$$

$$= \frac{1}{R \angle 0^\circ} + \frac{1}{X_C \angle -90^\circ} + \frac{1}{X_L \angle 90^\circ}$$

$$= \frac{1}{3.33 \angle 0^\circ} + \frac{1}{3.33 \angle -90^\circ} + \frac{1}{1.43 \angle 90^\circ}$$

$$= 0.3 \angle 0^\circ + 0.3 \angle (-90^\circ) + 0.7 \angle 90^\circ$$

$$= 0.3 \angle 0^\circ + 0.3 \angle 90^\circ + 0.7 \angle -90^\circ$$

$$= 0.3 + 0.3j - 0.7j$$

$$\frac{1}{Z_T} = 0.3 - 0.4j$$

$$\frac{1}{Z_T} \text{ goes polar form } 0.3 - 0.4j$$

$$\sqrt{(0.3)^2 + (0.4)^2} = 0.5$$

$$\Theta = \tan^{-1} \left(\frac{-0.4}{0.3} \right) = -53.13^\circ$$

$$\Rightarrow \frac{1}{Z_T} = 0.5 \angle -53.13^\circ$$

$$\Rightarrow \frac{1}{0.5 \angle -53.13^\circ} = Z_T$$

$$\Rightarrow 2 \angle -(-53.13) = Z_T$$

$$\Rightarrow 2 \angle 53.13 = Z_T$$

$$I = \frac{E}{Z_T} = \frac{100 \angle 53.13^\circ}{2 \angle 53.13^\circ} = 50 \angle 0^\circ$$

I_{R_2} \cdot $I_R \times E$

$$\text{for } I_{R_1} \quad I_{R_1} = \frac{Z_L \times I_R \times E}{Z_T} = \frac{1.43 \angle 90^\circ \times 3.33 \angle 90^\circ \times 50 \angle 0^\circ}{2 \angle 53.13^\circ}$$

$$= +19.05 \angle -53.13^\circ$$

$$\text{For } I_R: I_R = \frac{E}{Z_R}$$

$$= \frac{100 \angle 53.13^\circ}{3.33 \angle 0^\circ}$$

$$\Rightarrow 30 \angle 53.13^\circ$$

$$\text{For } I_L, I_L = \frac{E}{Z_L}$$

$$= \frac{100 \angle 53.13^\circ}{1.43 \angle 90^\circ}$$

$$= 70 \angle -36.87^\circ$$

$$\text{For } I_C: \frac{E}{Z_C} = \frac{100 \angle 53.13^\circ}{3.33 \angle -90^\circ}$$

$$= 70 \angle 143.13^\circ$$

formulas

(1) Resistor $\theta = 0^\circ$

- $I_m = \frac{V_m}{R}$, $V = \frac{V_m}{\sqrt{2}}$, $I = \frac{I_m}{\sqrt{2}}$
- $I = I_m \sin \omega t = V \angle 0^\circ$ [$I' = \frac{I_m}{\sqrt{2}}$]
- $V = V_m \sin \omega t = V \angle 0^\circ$ [$V' = \frac{V_m}{\sqrt{2}}$]
- $Z_R = R \angle 0^\circ$
- $I = \frac{V \angle 0^\circ}{R \angle 0^\circ} = \frac{V}{R} \angle 0^\circ = \frac{V}{R} \angle 0^\circ$
- $I_m = \frac{\sqrt{2} V}{R}$
- $I = \sqrt{2} \left(\frac{V}{R} \right) \sin \omega t$

(2) Inductor: pure inductor or angle difference 90°

Ques 85 $\theta = 90^\circ$

- $X_L = \omega L$ (inductive reactant)
- $Z_L = X_L \angle 90^\circ$ (Impedance)
- $V = V_m \sin \omega t = V \angle 0^\circ$
- $I = I_m \sin(\omega t - 90^\circ) = I \angle -90^\circ$
- $I = \frac{V}{Z_L} = \frac{V \angle 0^\circ}{X_L \angle 90^\circ} = \frac{V \angle 0^\circ}{\sqrt{2} X_L}$
- $I = \frac{\sqrt{2} V}{X_L} \sin(\omega t - 90^\circ)$

Capacitive: pure capacitance σ v and i by angle difference 90° .

- $X_C = \frac{1}{\omega C}$ (capacitive reactance)

- $Z_C = X_C \angle -90^\circ$ (impedance)

- $V = V_m \sin \omega t = V \angle 0^\circ$

- $I = \frac{V}{Z_C} = \frac{V \angle 0^\circ}{X_C \angle -90^\circ} = \frac{V}{X_C} \angle 90^\circ$

- $I = I_m \sin(\omega t + 90^\circ)$

- $I = \frac{\sqrt{2} V_m}{X_C} \sin(\omega t + 90^\circ)$

Impedances

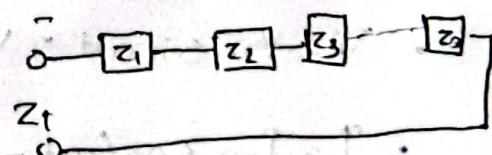
- $Z_R = R \angle 0^\circ$

- $Z_L = X_L \angle 90^\circ$

- $Z_C = X_C \angle -90^\circ$

* element of total circuit series σ Z_T :

- $Z_T = Z_1 + Z_2 + Z_3 + \dots + Z_n$



Z_T (Total)

- $I = \frac{E}{Z_T}$

Supply voltage $\rightarrow E$

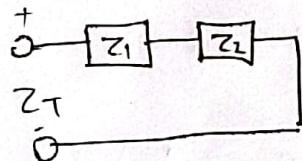
$Z_T \rightarrow$ Total Impedance

$$V_1 = I Z_1$$

$$V_2 = I Z_2$$

$$E = V_1 + V_2$$

voltage divider rules:



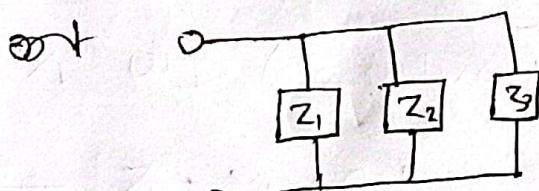
$$V_1 = I Z_1$$

$$V_1 = \frac{E Z_1}{Z_1 + Z_2} = \frac{Z_1 E}{Z_T}$$

$$V_2 = \frac{E Z_2}{Z_1 + Z_2} = \frac{Z_2 E}{Z_T}$$

power

parallel:



$$\frac{1}{Z_T} = \frac{1}{Z_1} + \frac{1}{Z_2} + \frac{1}{Z_3}$$

$$\frac{1}{Z_T} = \frac{Z_2 Z_3 + Z_1 Z_3 + Z_1 Z_2}{Z_1 Z_2 Z_3}$$

$$Z_T = \frac{Z_1 Z_2 Z_3}{Z_2 Z_3 + Z_1 Z_3 + Z_1 Z_2}$$

$$\cdot I_1 = \frac{E}{Z_1}, I_2 = \frac{E}{Z_2}$$

$$\cdot I = I_1 + I_2$$

$$\cdot \frac{1}{Z_R} = \frac{1}{R} \angle 0^\circ = \frac{1}{R}$$

$$\cdot \frac{1}{Z_L} = \frac{1}{X_L \angle 90^\circ} = \frac{1}{X_L} \angle -90^\circ$$

$$\cdot \frac{1}{Z_C} = \frac{1}{X_C \angle -90^\circ} = \frac{1}{X_C} \angle 90^\circ$$

Current Divider rule

$$I_1 = \frac{Z_2 I_T}{Z_1 + Z_2}, \quad I_2 = \frac{Z_1 I_T}{Z_1 + Z_2}$$

Power

$$P = EI \cos \theta_T$$

$$E = E_{\text{eff}} = E_{\text{r.m.s.}} = \frac{E_m}{\sqrt{2}}$$

$$I = I_{\text{eff}} = I_{\text{r.m.s.}} = \frac{I_m}{\sqrt{2}}$$

θ_T = angle difference between V and i.

Power factor

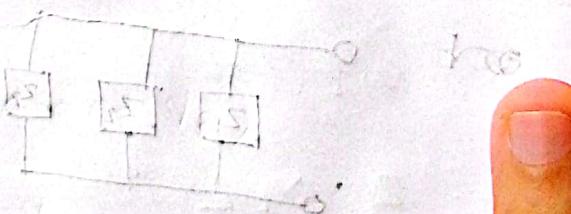
$$F_P = \cos \theta$$

$$P = EI \cos \theta$$

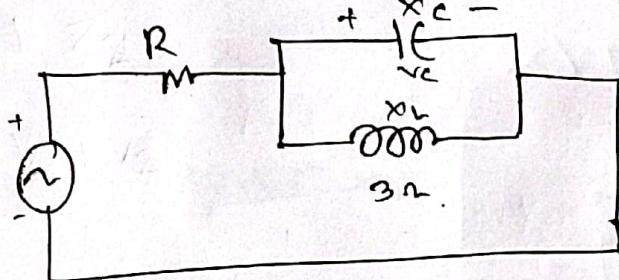
$$\frac{P}{EI} = \cos \theta \quad \frac{P}{EI} = F_P$$

$$F_P = \cos \theta = \frac{R}{Z_T} \quad [\text{series}]$$

$$F_P = \cos \theta = \frac{Z_T}{R} \quad [\text{parallel}]$$



Chapter - 16



$$E = 120V \angle 0^\circ, X_L = 3 \angle 90^\circ, X_C = 2 \angle -90^\circ$$

$$X_L = 3\Omega, X_C = 2\Omega, Z_R = 1 \angle 0^\circ$$

$$Z_L = 3 \angle 90^\circ, Z_C = 2 \angle -90^\circ, Z_R = 1 \angle 0^\circ$$

(a) Calculate Z_T :

$$Z_T = Z_R + Z_C \parallel Z_L$$

$$Z_T = \frac{Z_C \times Z_L}{Z_C + Z_L}$$

$$= \frac{2 \angle -90^\circ \times 3 \angle 90^\circ}{(2 \angle -90^\circ + 3 \angle 90^\circ)}$$

$$= \frac{6 \angle 0^\circ}{-2j + 3j} = \frac{6 \angle 0^\circ}{j}$$

$= 2\hat{j} + 3\hat{j}$ in polar form

$$\sqrt{(2)^2 + (3)^2} = 3.61$$

$\tan^{-1}(3)$

$$Z_T = 1 \angle 0^\circ + 6 \angle -90^\circ$$

$$= 1 \hat{x} - 6 \hat{y}$$

$1 - 6\hat{y}$ o. polar form,

$$\sqrt{(1)^2 + (-6)^2} = \sqrt{1+36} = 6.083$$

$$\theta = \tan^{-1}\left(\frac{-6}{1}\right) = -80.53^\circ$$

$$Z_T = 6.083 \angle -80.53^\circ$$

(b) Determine I_{sg}

$$I_s = \frac{E}{Z_T} = \frac{120 \angle 0^\circ}{6.083 \angle -80.53^\circ}$$

$$= 19.74 \angle 80.53^\circ$$

(c) $V_R = I Z_R$ (Calculate V_C and V_R)

$$= 19.74 \angle 80.53^\circ \times 1 \angle 0^\circ$$

$$= 19.74 \angle 80.53^\circ$$

$$\cancel{V_C = I Z_C} = \cancel{V_C = I (Z_T + Z_L)}$$

$$\cancel{V_C = V_{out}}$$

$$V_C \rightarrow E - V$$

$$V_C = I_S (Z_C || Z_L)$$

$$= 19.74 \angle 80.53^\circ \times 2'$$

$$= 19.74 \angle 80.53^\circ \times 6 \angle -90^\circ$$

$$= 118.44 \angle -9.47^\circ$$

(d) Find I_C

$$I_C = \frac{V_C}{Z_C} = \frac{118.44 \angle -9.47^\circ}{2 \angle -90^\circ}$$

$$= 59.22 \angle 80.53^\circ$$

(e) Total power P

~~$$P = P_R + P_C + P_L$$~~

$$= I_{eff} \times V_{eff} \cos 0^\circ + I_{eff} R_{eff} \cos 90^\circ +$$



$$= I_{eff} V_{eff} \times 1 + 0 + 0$$

$$R_{eff} (85\Omega)$$

$$I_{eff} = 19.74 \angle 80.53^\circ *$$

$$V_{eff} = 19.74 \angle 80.53^\circ$$

$$P = I_{\text{eff}} \times E_{\text{eff}}$$

$$\rightarrow 19.74 / 80.53 \times 19.74 / 80.53$$

$$= 389.67 / 161.06$$

=

$$P = I_{\text{eff}} \times E_{\text{eff}}$$

$$= (19.74) \times (19.74)$$

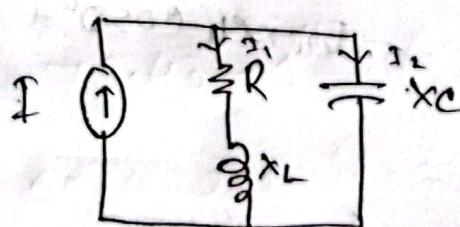
$$= 389.67 \text{ W}$$

(f) Calculate F_P :

$$F_P = \cos \theta = \cos 80.54^\circ$$

$$= 0.168 \text{ leading}$$

16.2 | exp)



$$R = 3 \Omega, X_L = 4 \Omega, X_C = 8 \Omega$$

$$I = 50 \angle 30^\circ$$

$$2R = 3 \angle 0^\circ, 2X_L = 4 \angle 90^\circ, 2X_C = 8 \angle -90^\circ$$

(a) calculated by using current dividend rule

$$Z' = Z_R + Z_L = 3 \angle 0^\circ + 4 \angle 90^\circ = 3 + 4j$$

$$I_1 = \frac{Z_C \times I}{Z_C + Z_1} = \frac{8L - 90^\circ \times 50L 30^\circ}{-8\hat{j} + 3 + 4\hat{j}}$$

$$= \frac{400L - 60^\circ}{3 - 4\hat{j}}$$

$$3 - 4i \text{ to polar form: } \sqrt{3^2 + (-4)^2}, \theta = \tan^{-1} \left(\frac{-4}{3} \right) = -53.13^\circ$$

$$I_1 = \frac{400 \angle -60^\circ}{5 \angle -53.13^\circ} \rightarrow 80 \angle -6.87^\circ$$

(5) Calculate I_2 (current divider rules)

(5) Calculate z^2 (conjugate)

$$T_2 = \frac{Z_1 \times I}{Z_1 + Z_C} = 5153.13^\circ$$

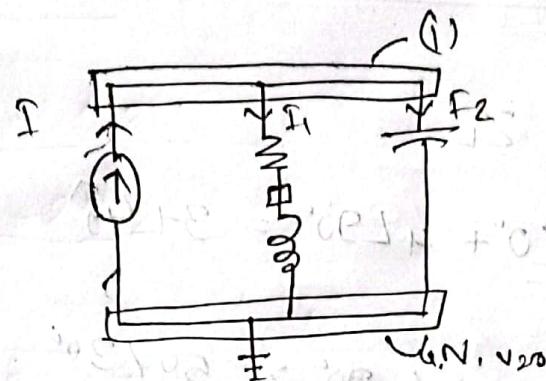
$$= \frac{5 \angle 53.13 \times 50 \angle 30^\circ}{3 - 4\hat{j}}$$

$$= \frac{250 \angle 83.13}{5 \angle -53.13}$$

$$= 50 \angle 136.26^\circ$$

$$\sqrt{(3)^2 + (4)^2} = 5$$

(C) Verify KVL at one node



At NODE 1

$$I = I_1 + I_2$$

$$50 \angle 30^\circ = 80 \angle -6.87^\circ + 50 \angle 136.26^\circ$$

$80 \angle -6.87^\circ$ का तारीफ़ फॉर्म:

$$X = 80 \cos(-6.87^\circ) = 79.43$$

$$Y = 80 \sin(-6.87^\circ) = -9.57$$

$$I_1 = 79.43 - j 9.57$$

I_2 का तारीफ़ फॉर्म

$$X = 50 \cos(136.26^\circ) = -36.12$$

$$Y = 50 \sin(136.26^\circ) = 34.57$$

$$I_2 = -36.12 + 34.57 j$$



$$I = I_1 + I_2$$

$$= 79.43 - 9.57 \hat{J} \rightarrow -36.12 + 34.57 \hat{J}$$

$$\approx 43.31 + 25 \hat{J}$$

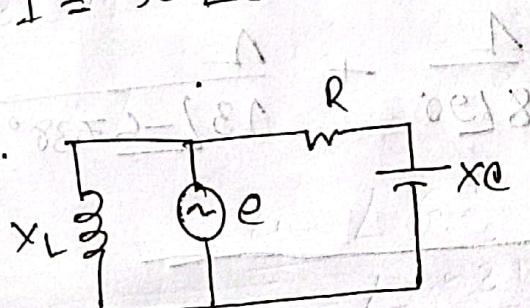
I in polar form

$$\sqrt{(43.31)^2 + (25)^2} = 50$$

$$\theta = \tan^{-1} \left(\frac{25}{43.31} \right) = 30^\circ$$

$$\theta = 30^\circ \quad (43.31 \hat{J})$$

$$I = 50 \angle 30^\circ$$



16.3

$$E = 20 \angle 20^\circ, R = 5 \Omega; X_C = 12 \Omega, X_L = 8 \Omega$$

(a) V_C (Voltage Divider rule)

$$V_C = \frac{E \times Z_C}{Z_C + Z_R} = \frac{20 \angle 20^\circ \times 12 \angle -90^\circ}{5 \angle 0^\circ + 12 \angle -90^\circ}$$

$$240 \angle -70^\circ$$

$$\underline{\text{5-12}\hat{J} \text{ polar form}} \quad \sqrt{5^2 + 12^2} = 13, \quad \theta = \tan^{-1} \left(\frac{-12}{5} \right) \\ = -67.4^\circ$$

$$N_C = \frac{240 \angle -70^\circ}{13 \angle -67.38^\circ}$$

$$= 18.48 \angle -2.62$$

(b) Calculate Current I_s

$$\frac{1}{Z_T} = \frac{1}{Z_L} + \frac{1}{Z_R + Z_C}$$

$$= \frac{1}{8 \angle 90^\circ} + \frac{1}{23 \angle -67.38^\circ}$$

$$= 0.125 \angle -90^\circ + 0.077 \angle 67.38^\circ$$

$$= -0.125 \hat{j} + 0.077 \angle 67.38^\circ$$

$0.077 \angle 67.38^\circ$ കു രാജീവഫോൺ ട്ലാസ്റ്റിക്

$$X = 0.077 \cos(67.38^\circ) = 0.03$$

$$Y = 0.077 \sin(67.38^\circ) = 0.071$$

$$\frac{1}{Z_T} = -0.125 \hat{j} + 0.03 + 0.071 \hat{j}$$

$$= -0.048 \hat{j} + 0.03$$

• $\frac{1}{Z_T}$ കു polar form:

$$\sqrt{(0.048)^2 + (0.03)^2} = 0.06$$

$$\theta = \tan^{-1} \left(\frac{-0.048}{0.03} \right) = -58^\circ$$

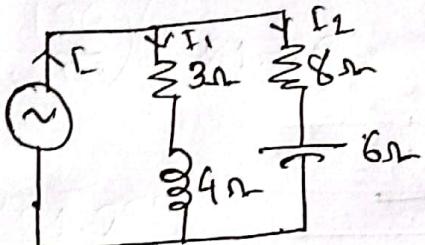
$$\frac{1}{Z_T} = 0.06 \angle -58^\circ$$

$$I = \frac{E}{Z_T}$$

$$= 20 \angle 20^\circ \times 0.06 \angle -58^\circ$$

$$= 1.2 \angle -38^\circ$$

16.4



$$E = 100 \angle 0^\circ, R_1 = 3 \Omega, R_2 = 8 \Omega$$

$$X_L = 4 \Omega, X_C = 6 \Omega$$

(a) Calculate the current I_s :

$$Z_R = 3 \angle 0^\circ, Z_{R_2} = 8 \angle 0^\circ, Z_L = 4 \angle 90^\circ, Z_C = 6 \angle -90^\circ$$

$$Z_1 = Z_{R_1} + Z_L = 3 \angle 0^\circ + 4 \angle 90^\circ$$

$$= 3 + 4j = 5 \angle 53.13^\circ$$

$$Z_2 = Z_{R_2} + Z_C = 8 \angle 0^\circ + 6 \angle -90^\circ = 8 - 6j$$

$$= 10 \angle -36.87^\circ$$

$$Z_T = \frac{Z_1 \times Z_2}{Z_1 + Z_2}$$

$$= \frac{5 \angle 53.13^\circ \times 10 \angle -36.87^\circ}{3 + 4j + 8 - 6j}$$

$$= \frac{50 \angle 16.26^\circ}{11 - 2j}$$

$11 - 2j$ in polar form:

$$\sqrt{(11)^2 + (-2)^2} = \sqrt{125} = 5\sqrt{5} = 11.18$$

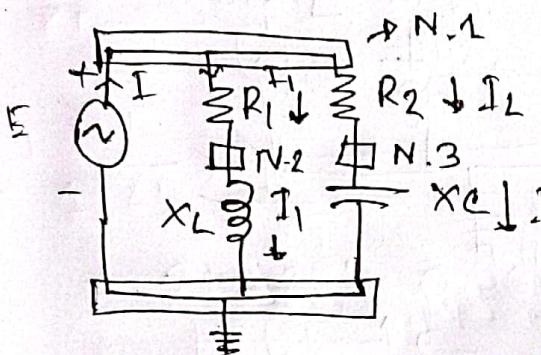
$$\theta = \tan^{-1} \left(\frac{-2}{11} \right) = -10.30^\circ$$

$$Z_T = \frac{50 \angle 16.26^\circ}{11.18 \angle -10.30^\circ}$$

$$= 4.46 \angle 26.56^\circ \quad 4.472 \angle 26.56^\circ$$

$$T = \frac{E}{Z_T} = \frac{100 \angle 0^\circ}{4.472 \angle 26.56^\circ} = 22.36 \angle -26.56^\circ$$

(b) Find the voltage V_{ab}



$$E = 100 \angle 0^\circ$$

$$Z_{R_1} = 3 \angle 0^\circ$$

$$Z_{R_2} = 8 \angle 0^\circ$$

$$Z_L = 4 \angle 90^\circ$$

$$Z_C = 6 \angle -90^\circ$$

NODE 1 $E = 100 \angle 0^\circ$

NODE 2

$$I_1 = \frac{V_2 - V_o}{Z_L}$$

NODE -3

$$I_2 = \frac{V_3 - V_o}{Z_C}$$

$$\Rightarrow \frac{E - V_2}{Z_{R_1}} = \frac{V_2}{Z_L}$$

$$\frac{E - V_3}{Z_{R_2}} = \frac{V_3}{Z_C}$$

$$\Rightarrow Z_L E - V_2 Z_L = V_2 Z_{R_1}$$

$$Z_C E - V_3 Z_C = V_3 Z_{R_2}$$

$$\Rightarrow Z_L E = V_2 (Z_L + Z_{R_1})$$

$$Z_C E = V_3 (Z_C + Z_{R_2})$$

$$\Rightarrow \frac{E Z_L}{Z_L + Z_{R_1}} = V_2 \quad (1)$$

$$\frac{Z_C E}{Z_C + Z_{R_2}} = V_3 \quad (2)$$

$$V_{ab} = V_3 - V_2 \quad (3)$$

for (i), $V_2 = \frac{E \times Z_L}{Z_R + Z_L}$

$$= \frac{100 \angle 0^\circ \times 4 \angle 90^\circ}{3 \angle 0^\circ + 4 \angle 90^\circ}$$
$$= \frac{400 \angle 90^\circ}{3 + 4j}$$

$$= \frac{400 \angle 90^\circ}{5 \angle 53.13^\circ}$$

$$= 80 \angle 90^\circ - 53.13^\circ$$
$$= 80 \angle 36.87^\circ$$

$$(95+35)\text{eV} = 80 \times 80 \times \cos(36.87^\circ) = 64$$

$$Y = 80 \sin(36.87^\circ) = 48$$

$$V_2 = 64 + 48j \quad (iv)$$

(iii) $\rightarrow 8V - 8V$

for (i), $V_3 = \frac{EX2c}{Z_C + Z_{R_2}}$

$$= \frac{100 \angle 0^\circ \times 6 \angle -90^\circ}{6 \angle -90^\circ + 8 \angle 0^\circ}$$

$$= \frac{600 \angle -90^\circ}{-6j + 8}$$

$$= \frac{600 \angle -90^\circ}{10 \angle -36.87^\circ}$$

$$= 60 \angle -53.13^\circ$$

$60 \angle -53.13^\circ$ in rectangular form

$$x = 60 \cos(-53.13) = 36$$

$$y = 60 \sin(-53.13) = -48$$

$$V_3 = 36 - 48j \quad (iv)$$

for (ii),

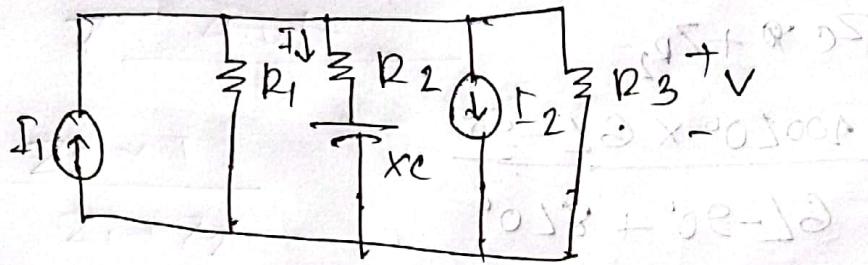
$$V_{AB} = V_3 - V_2 \rightarrow V_{AB} = V_2 - V_3$$

$$= 36 - 48j - 64 = -64 + 48j$$

$$\begin{aligned} V_{AB} &= V_2 - V_3 = 64 + 48j - 36 + 48j \\ &= 28 + 96j \\ &= 100 \angle 73.74^\circ \end{aligned}$$

(Ans.)

16.6

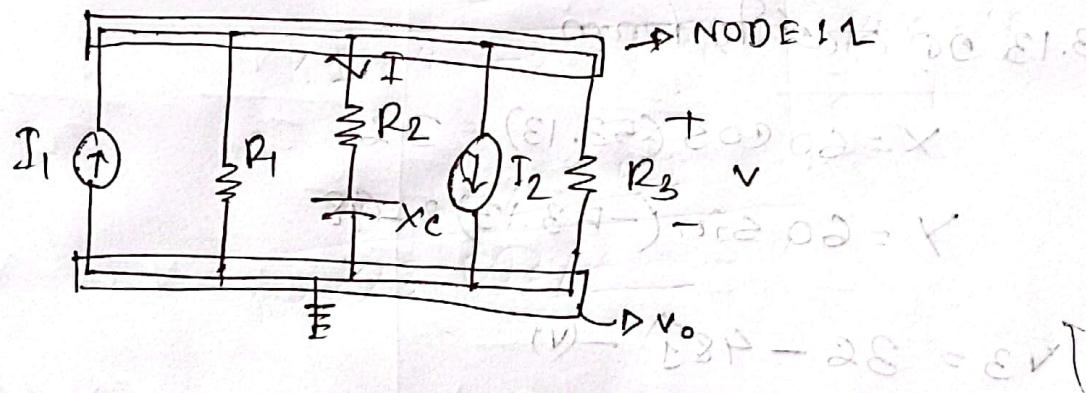


$$I_1 = 6 \angle 20^\circ, Z_{R1} = 2 \angle 0^\circ, Z_{R2} = 10 \angle 0^\circ$$

$$Z_{R3} = 6.8 \angle 0^\circ, Z_C = 20 \angle -90^\circ$$

$$I_2 = 4 \angle 0^\circ$$

(a) Determine the current I_T



$$I_T = 6 \angle 20^\circ - 4 \angle 0^\circ$$

$$6 \angle 20^\circ \text{ in rectangular form } x = 6 \cos 20^\circ = 5.698$$

$$y = 6 \sin 20^\circ = 2.052$$

$$I_T = 5.698 + 2.052 \angle 0^\circ - 4 \angle 0^\circ$$

$$= 1.698 + 2.052 \angle 0^\circ = 2.626 \angle 1.402^\circ$$

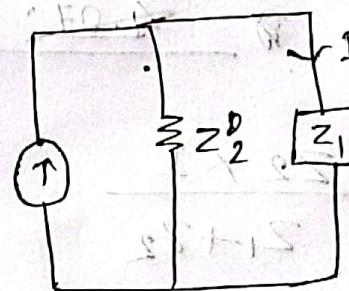
$$= 2.625 \angle 51.34^\circ$$

① NODE 1:

$$I_1 = I' + I'' + I_2 + I'''$$

$$I_1 - I_2 = I' + I'' + I'''$$

$$2.625 \angle 51.34^\circ = I' + I'' + I'''$$



$$\cdot Z_1 = Z_{R_2} + Z_C$$

$$= 10 \angle 0^\circ + 20 \angle -90^\circ$$

$$= 10 - 20j$$

$$= 22.36 \angle -63.43^\circ$$

$$Z_2 = \frac{Z_{R_1} \times Z_{R_3}}{Z_{R_1} + Z_{R_3}}$$

$$= \frac{2 \angle 0^\circ \times 6.8 \angle 0^\circ}{2 \angle 0^\circ + 6.8 \angle 0^\circ}$$

$$= \frac{13.6 \angle 0^\circ}{8.8 \angle 0^\circ} = 1.545 \angle 0^\circ$$

$$\approx 1.55 \angle 0^\circ = 1.55$$

~~$$I = \frac{Z_2 \times I_T}{Z_2 + Z_1 \angle 51.34^\circ}$$~~

$$= \frac{1.55 \angle 0^\circ \times 2.625 \angle 51.34^\circ}{1.55 \angle 0^\circ + 10 - 20j}$$

$$I = \frac{Z_2 \times I}{Z_1 + Z_2}$$

$$= \frac{1.54520^\circ \times (2.626 \angle 51.402^\circ)}{1.54520^\circ + 10 - 20j}$$

$$= \frac{4.057 \angle 51.402^\circ}{1.54520^\circ + 10 - 20j}$$

$$= \frac{4.057 \angle 51.402^\circ}{(1.54520^\circ + 10 - 20j) \times 10^3}$$

$$= \frac{4.057 \angle 51.402^\circ}{10^3 \times 23.093 \angle -60.004^\circ}$$

$$\Rightarrow 0.176 \angle 111.406^\circ$$

$$(b) V = I Z_2$$

$$\Rightarrow (0.176 \angle 111.406^\circ) \times (22.36 \angle -63.483^\circ)$$

$$= 3.6 \angle 3.936^\circ \quad 3.936 \angle 47.971^\circ$$

$$= 3.6 \angle 3.936^\circ \quad 3.936 \angle 47.971^\circ$$