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1 // Assignment 9 - Convex Hull
2 // You can solve it using Graham's Scan
3
4 typedef pair<int, int> Point;
5
6 class Solution {
7 public:
8     /* Helper function to calculate the orientation of three points (p, q, r)
9     0 -> p, q, r and collinear,
10    1 -> clockwise,
11    2 -> counterclockwise
12    */
13    int orientation(const Point& p, const Point& q, const Point& r) {
14        int val = (q.second - p.second) * (r.first - q.first) -
15                (q.first - p.first) * (r.second - q.second);
16        if (val == 0)
17            return 0;
18        return (val > 0) ? 1 : 2;
19    }
20
21    // Function to compute the square of the distance between two points
22    int distance(const Point& p1, const Point& p2) {
23        return (p1.first - p2.first) * (p1.first - p2.first) +
24                (p1.second - p2.second) * (p1.second - p2.second);
25    }
26
27    vector<vector<int>> outerTrees(vector<vector<int>>& trees) {
28        // Graham's scan convex hull algorithm
29        vector<Point> points;
30        for (const auto& tree : trees) {
31            points.emplace_back(tree[0], tree[1]);
32        }
33
34        // Step 1: Find the point with the lowest y-coordinate (or leftmost in
35        // case of tie)
36        Point start = *min_element(
37            points.begin(), points.end(), [](const Point& p1, const Point& p2) {
38                return (p1.second < p2.second) ||
39                       (p1.second == p2.second && p1.first < p2.first);
40            });
41
42        // Step 2: Sort points based on polar angle with 'start' point
43        auto polar_angle = [&start](const Point& p) {
44            return atan2(p.second - start.second, p.first - start.first);
45        };
46
47        sort(points.begin(), points.end(),
48            [&start, &polar_angle, this](const Point& p1, const Point& p2) {
49                double angle1 = polar_angle(p1);
50                double angle2 = polar_angle(p2);
51                if (angle1 == angle2) {
52                    return distance(start, p1) < distance(start, p2);
53                }
54                return angle1 < angle2;
55            });
56
57        // Step 3: Initialize the convex hull with the first three points
58        vector<Point> hull = {start};
59
60        for (size_t i = 1; i < points.size(); ++i) {
61            while (hull.size() > 1 &&
62                orientation(hull[hull.size() - 2], hull.back(), points[i]) ==
63                1) {
64                hull.pop_back(); // Pop last point if we turn clockwise or if
65                                // collinear
66            }
67            hull.push_back(points[i]);
68        }
69    }

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70     for (size_t i = points.size() - 1; i >= 0; --i) {
71         if (orientation(start, hull.back(), points[i]) == 0) {
72             hull.push_back(points[i]);
73         }
74         if (i == 0)
75             break;
76     }
77
78     vector<vector<int>> result;
79     unordered_set<string> unique_points;
80
81     for (const auto& p : hull) {
82         string point_str = to_string(p.first) + "," + to_string(p.second);
83         if (unique_points.find(point_str) == unique_points.end()) {
84             result.push_back({p.first, p.second});
85             unique_points.insert(point_str);
86         }
87     }
88
89     return result;
90 }
91 };

```