

ABSTRACT

MAGNETOMETER-LESS STATE-ESTIMATION OF A UNICYCLE MODEL MOBILE ROBOT USING A CASCADED KALMAN FILTER FRAMEWORK

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OF A UNICYCLE MODEL MOBILE ROBOT
USING A CASCADED KALMAN FILTER FRAMEWORK**

BY

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Here's where you acknowledge folks who helped.

DEDICATION

To all of the fluffy kitties.

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CHAPTER 1

INTRODUCTION

This section will cover background information on mobile robot kinematic models, IMU state estimation, Kalman Filtering methods, and cascading KF framework.

1.1 Motivation

Talk about the development of miniature robots. Talk about our spherical robot design. The small size of the robot makes it difficult to use a magnetometer due to the close proximity of the motors and sensors. Using an external sensor is clunky or not realistic.

1.2 Literature Review

This section should go over the papers I have gone over. This includes NMNI, NDZTA, Song 2018 on the cascaded KF framework, as well as other papers using external sensors to get more robust heading.

1.3 Objective

To tackle these challenges, this thesis aims to find a novel way to estimate a mobile robots states using only a 6DOF IMU with a unicycle model wheeled mobile robot. The thesis will

have an algorithm with only a 6DOF IMU as well as having the option to add an additional sensor to provide more robust localization.

CHAPTER 2

METHODS

This part will be an overview of the overall framework of the algorithm. It will first discuss preprocessing methods. These methods involve NMNI, NDZTA, and error compensation in the gyroscope and accelerometer. Afterwards it will discuss the first and second kalman filter models, then the optional block containing the additional sensor to improve the performance of the filter.

2.1 IMU Preprocessing

Here I will first talk about what an IMU is, 6DOF vs. 9DOF, how each sensor works, and the inherent errors in each sensor.

It will then cover the planned signal processing methods for each sensor on the IMU and go in depth about each algorithms implementation.

2.1.1 Accelerometer Signal Processing

This subsection talks about the preprocessing methods that will take place on the accelerometer data coming from the IMU as well as the numerical integration methods used for displacement calculation.

2.1.1.1 Displacement Measurement from Acceleration Data

Euler integration, trapezoidal, RK4. (Better integration = better data) Don't think I really need to explain this right now.

2.1.1.2 No Displacement Zero Translational Accumulation (NDZTA)

Sci-hub Link: <https://sci-hub.live/https://ieeexplore.ieee.org/document/9268038>

Removing the noise in accelerometer data during stationary points in time is done by finding a way to have the system understand when it is stationary. The No Displacement Zero Translation Accumulation (NDZTA) algorithm accounts for this by calculating a threshold value that indicates whether the system is in motion or not. Figure 2.1 illustrates the logic of the algorithm.

First a low pass filter is applied to the accelerometer data to eliminate the inherent high frequency noise. After the filter is applied, a maximum value is collected from a sampling window during an initial static position. This maximum value becomes the threshold that helps the system realize it is not in motion. Now the displacement is calculated based on this found threshold which signifies the boundary between static and dynamic motions. The algorithm works by comparing the real-time acceleration data a with the threshold a_{th} to decide if displacement calculation is needed. This comparison is demonstrated in equations 2.1 and 2.2.

$$a > a_{th}, \text{ Sensor is in motion. Carryout displacement calculation} \quad (2.1)$$

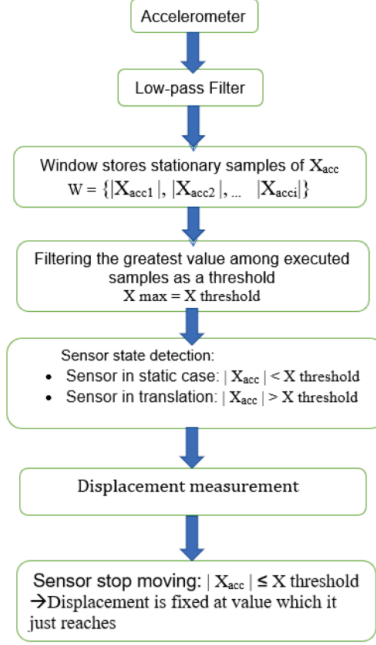


Figure 2.1: NDZTA flow

$$a \leq a_{th}, \text{ Sensor is static. Set } acc = vel = pos = 0 \quad (2.2)$$

Note that the displacement calculation has many errors due to noise in the sensor signals and numerical integration causing the error to grow. In order to eliminate the error, the NDZTA algorithm proposes a method composed of these 3 main steps.

Step 1: Threshold Calculation

Step 2: Motion Detection

Step 3: Displacement Measurement

During each detection of the static case, the threshold value is updated depending on equation 2.3.

Equation 2.3 here!

some conditional statement that I cannot remember.

2.1.2 Gyroscope Signal Processing

This subsection talks about the preprocessing methods that will take place on the gyroscope data coming from the IMU.

2.1.2.1 Bias Compensation

Don't think I need to really explain this right now.

2.1.2.2 No Motion No Integration (NMNI)

Sci-hub link: <https://sci-hub.live/https://ieeexplore.ieee.org/document/9247295>

<https://sci-hub.live/https://www.sciencedirect.com/science/article/abs/pii/S0924424721001540>

To find roll, pitch, and yaw angles, the angular rate data from the gyroscope is numerically integrated. Due to multiple different error sources, noise and drift problems will cause the gyroscope data to vary.

To compensate for these errors, the No Motion No Integration (NMNI) algorithm is used. This algorithm only allows numerical integration when dynamic motion is detected. Similar to the NDZTA algorithm discussed in previous sections, this algorithm finds the maximum value within sampled data during an initial window of static motion. This max value is set

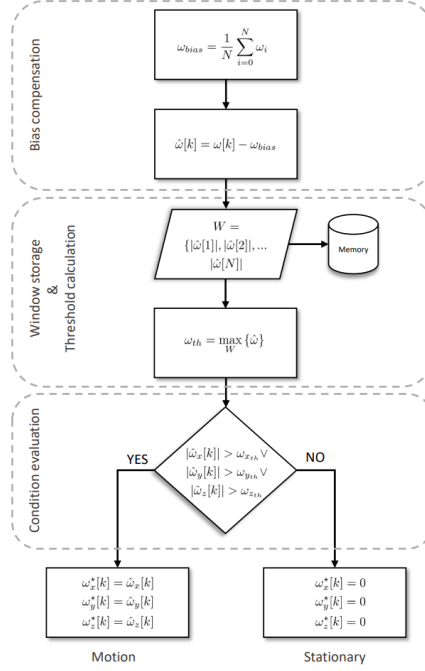


Figure 2.2: NMNI flow

as a threshold value, and the real-time data collected by the gyroscope is compared with the threshold value to determine if the system is in static or dynamic motion. The overall logic of the algorithm can be seen in figure 2.2 below.

Maybe enter equations here too. But seems redundant.

2.2 First KF: Course Correction Extended Kalman Filter

This section covers the first Kalman Filter in the cascaded Kalman Filter framework. This Kalman Filter uses the unicycle kinematic model as the process model, and gets bias compensated feedback position data from the accelerometer as the measurement model.

2.2.1 Process Model

Kinematic model follows the common unicycle model for wheeled-mobile robots (WMRs). This thesis is assuming 2D planar motion so the states are x , y , and θ .

$$x = z = [x, y, \theta]^T \quad (2.3)$$

$$f = \begin{bmatrix} v\cos(\theta) & 0 \\ v\sin(\theta) & 0 \\ 0 & w \end{bmatrix} \quad (2.4)$$

where v and w are the linear and angular velocity of the mobile robot.

$$F = \begin{bmatrix} 1 & 0 & -v\sin(\theta) \\ 0 & 1 & v\cos(\theta) \\ 0 & 0 & 1 \end{bmatrix} \quad (2.5)$$

2.2.2 Measurement Model

The measurement model here is identity because the states can be directly accessed with minimal calculations. Going into this system will be the corrected and compensated position and orientation data that is found from our second KF. These are then used to estimate the states taking into account the robots kinematic constraints along with the sensor measurements.

Add equations on how pose is found using sensor data

$$h = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad (2.6)$$

$$H = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad (2.7)$$

2.3 Second KF: Bias Estimation Kalman Filter

This section covers the second Kalman Filter in the cascaded Kalman Filter framework. This Kalman filter uses the gyroscope model as the process model, and uses the accelerometer data as the measurement model to estimate our states as well as correction terms to compensate for sensor errors.

2.3.1 Process Model

This states are orientation error ($\delta\phi$), velocity error (δv), gyroscope bias (b_g), and accelerometer bias (b_a).

$$\mathbf{x}_2 = [\delta\phi^T, \delta v^T, \mathbf{b}_g^T, \mathbf{b}_a^T]^T \quad (2.8)$$

$$f = \begin{bmatrix} \mathbf{0}_{3 \times 3} & \mathbf{0}_{3 \times 3} & -\mathbf{C}_b^n & \mathbf{0}_{3 \times 3} \\ \mathbf{S} & \mathbf{0}_{3 \times 3} & \mathbf{0}_{3 \times 3} & \mathbf{C}_b^n \\ \mathbf{0}_{3 \times 3} & \mathbf{0}_{3 \times 3} & -\beta_g \mathbf{I}_{3 \times 3} & \mathbf{0}_{3 \times 3} \\ \mathbf{0}_{3 \times 3} & \mathbf{0}_{3 \times 3} & \mathbf{0}_{3 \times 3} & -\beta_a \mathbf{I}_{3 \times 3} \end{bmatrix} \quad (2.9)$$

C (don't know if definition is correct) is a rotation matrix. S is a skew symmetric matrix of acceleration representing vector cross product. β are the Markov process time constants that model our biases.

$$\mathbf{C}_b^n = \begin{bmatrix} \cos(\phi_D) & -\sin(\phi_D) & 0 \\ \sin(\phi_D) & \cos(\phi_D) & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad (2.10)$$

$$\mathbf{S} = \begin{bmatrix} 0 & -a_D & a_E \\ a_D & 0 & -a_N \\ -a_E & a_N & 0 \end{bmatrix} \quad (2.11)$$

2.3.2 Measurement Model

Measurements are course angle error and velocity measurements. Course angle error is found by taking the difference between the KF estimated heading angle from the gyro and unicycle model and the estimated heading found from using the previous and current position data that provides the heading for the robot to linearly move from the previous point to the current point.

$$\delta\theta = \theta_{est} - \theta_{acc} \quad (2.12)$$

where θ_{est} is the heading estimated by the kalman filter and θ_{acc} is the heading found from the position data.

COMMENT

But doesn't heading from kinematics come from acc and gyro already? So instead, take the improved heading from fusing kinematics with acc and gyro, and pass to gyro KF instead of heading error.

So first KF takes x, y, θ as measurement and outputs θ into KF2. KF2 then takes in v and θ to estimate errors to correct/compensate sensor measurements and vel and orientation errors. These improvements of measurement errors and state errors should improve x, y, θ and improve estimates in the first KF. Those will be the states that we care more about.

But if we are just going to use the states estimated by the first KF, why don't we just find orientations and pass it to first KF rather than find errors, then externally correct them then pass them to the first KF.

COMMENT

$$z_2 = [\delta\theta, \mathbf{v}]^T \quad (2.13)$$

$$h = \begin{bmatrix} \begin{bmatrix} \tan(\phi_N)\cos(\phi_D) & \tan(\phi_N)\sin(\phi_D) & -1 \end{bmatrix} & \mathbf{0}_{1 \times 3} & \mathbf{0}_{1 \times 3} & \mathbf{0}_{1 \times 3} \\ \mathbf{0}_{3 \times 3} & \mathbf{I}_{3 \times 3} & \mathbf{0}_{3 \times 3} & \mathbf{0}_{3 \times 3} \end{bmatrix} \quad (2.14)$$

2.4 Estimation with Additional Sensor

This sensor should be one that can give position data. GPS, camera, encoder. From this extra sensor, you can set up a cost function that models the error in the measurements

and minimize it using gradient descent or something to hopefully get the best estimate in position/heading.

CHAPTER 3

FUTURE WORK

The work left involves simulating the entire framework of the algorithm. Currently the preprocessing methods are implemented on to the KF blocks and are simulated separately. In the future they need to be combined and the performance needs to be analyzed.

Afterwards, how the optional sensor is to be implemented into the algorithm needs to be figured out. (Thinking of optimizing a cost function between sensor and position from accelerometer to provide best position estimate then feeding that into the KF.)

Finally, implementation on a physical system is left. The planned robot for implementation is the Sphero-mini.

3.1 Simulation

Specifications of simulation. Errors modeled, results of simulation.

3.2 Physical Implementation

Sphero-mini's specifications. Sensors. Workspace specifications. Results.