

**Swinburne University of Technology***School of Science, Computing and Engineering Technologies***FINAL EXAM COVER SHEET**

**Subject Code:** COS30008  
**Subject Title:** Data Structures & Patterns  
**Due date:** June 7, 2022, 18:00  
**Lecturer:** Dr. Markus Lumpe

**Your name:** \_\_\_\_\_ **Your student id:** \_\_\_\_\_

Check Tutorial	Mon 10:30	Mon 14:30	Tues 08:30	Tues 10:30	Tues 12:30	Tues 14:30	Tues 16:30	Wed 08:30	Wed 10:30	Wed 12:30	Wed 14:30

Marker's comments:

Problem	Marks	Time Estimate in minutes	Obtained
1	132	30	
2	56	10	
3	60	15	
4	10+88=98	45	
5	50	20	
Total	396	120	

This test requires approx. 2 hours and accounts for 50% of your overall mark.

```
1
2 // COS30008, Final Exam, 2022
3
4 #pragma once
5
6 #include <stdexcept>
7 #include <algorithm>
8
9 using namespace std;
10
11 template<typename T>
12 class TernaryTreePrefixIterator;
13
14 template<typename T>
15 class TernaryTree
16 {
17 public:
18
19     using TTree = TernaryTree<T>;
20     using TSubTree = TTree*;
21
22 private:
23
24     T fKey;
25     TSubTree fSubTrees[3];
26
27     // private default constructor used for declaration of NIL
28     TernaryTree() :
29         fKey(T())
30     {
31         for ( size_t i = 0; i < 3; i++ )
32         {
33             fSubTrees[i] = &NIL;
34         }
35     }
36
37 public:
38
39     using Iterator = TernaryTreePrefixIterator<T>;
40
41     static TTree NIL;           // sentinel
42
43     // getters for subtrees
44     const TTree& getLeft() const { return *fSubTrees[0]; }
45     const TTree& getMiddle() const { return *fSubTrees[1]; }
46     const TTree& getRight() const { return *fSubTrees[2]; }
47
48     // add a subtree
49     void addLeft( const TTree& aTTree ) { addSubTree( 0, aTTree ); }
```

```

50 void addMiddle( const TTree& aTTree ) { addSubTree( 1, aTTree ); }
51 void addRight( const TTree& aTTree ) { addSubTree( 2, aTTree ); }
52
53 // remove a subtree, may through a domain error
54 const TTree& removeLeft() { return removeSubTree( 0 ); }
55 const TTree& removeMiddle() { return removeSubTree( 1 ); }
56 const TTree& removeRight() { return removeSubTree( 2 ); }
57
58 ///////////////////////////////////////////////////
59 // Problem 1: TernaryTree Basic Infrastructure
60
61 private:
62
63 // remove a subtree, may throw a domain error [22]
64 const TTree& removeSubTree( size_t aSubtreeIndex )
65 {
66     if (fSubTrees[aSubtreeIndex]->empty())
67     {
68         throw domain_error("Subtree is NIL");
69     }
70     if (aSubtreeIndex > 2)
71     {
72         throw out_of_range("Illegal subtree index");
73     }
74     const TTree& index = const_cast<TTree&>(*fSubTrees
75         [aSubtreeIndex]);
76     fSubTrees[aSubtreeIndex] = &NIL;
77     return index;
78 }
79 // add a subtree; must avoid memory leaks; may throw domain error [18]
80 void addSubTree( size_t aSubtreeIndex, const TTree& aTTree )
81 {
82     if (empty())
83     {
84         throw domain_error("Operation not supported");
85     }
86     if (aSubtreeIndex > 2)
87     {
88         throw out_of_range("Illegal subtree index");
89     }
90     if (!fSubTrees[aSubtreeIndex]->empty())
91     {
92         throw domain_error("Subtree is not NIL");
93     }
94     fSubTrees[aSubtreeIndex] = const_cast<TTree*>(& aTTree);
95 }
96
97 public:

```

```
98
99     TernaryTree(const T& aKey) :fKey(aKey)
100     {
101         for (int i = 0; i < 3; i++)
102         {
103             fSubTrees[i] = &NIL;
104         }
105     }
106
107     // destructor (free sub-trees, must not free empty trees) [14]
108     ~TernaryTree()
109     {
110         if (!empty())
111         {
112             for (int i = 0; i < 3; i++)
113             {
114                 if (!fSubTrees[i]->empty())
115                 {
116                     delete fSubTrees[i];
117                 }
118             }
119         }
120     }
121
122     // return key value, may throw domain_error if empty [2]
123     const T& operator*() const
124     {
125         if (empty())
126         {
127             throw domain_error("Tree is empty");
128         }
129         return fKey;
130     }
131
132     // returns true if this ternary tree is empty [4]
133     bool empty() const { return this == &NIL; }
134
135     // returns true if this ternary tree is a leaf [10]
136     bool leaf() const
137     {
138         for (int i = 0; i < 3; i++)
139         {
140             if (!fSubTrees[i]->empty()) return false;
141         }
142         return true;
143     }
144
145     // return height of ternary tree, may throw domain_error if empty [48]
146     size_t height() const
```

```

147     {
148         if (empty())
149         {
150             throw domain_error("Operation not supported");
151         }
152         if (leaf()) return 0;
153         size_t height[3] = {};
154
155         for (int i = 0; i < 3; i++)
156         {
157             height[i] = fSubTrees[i]->empty() ? 0 : fSubTrees[i]->height
158                 ();
159         }
160         return *max_element(height, height + 3) + 1;
161     }
162     //////////////////////////////////////
163     // Problem 2: TernaryTree Copy Semantics
164
165     // copy constructor, must not copy empty ternary tree
166     TernaryTree( const TTree& aOtherTTree )
167     {
168         for (int i = 0; i < 3; i++)
169         {
170             fSubTrees[i] = &NIL;
171         }
172         *this = aOtherTTree;
173     }
174
175     // copy assignment operator, must not copy empty ternary tree
176     // may throw a domain error on attempts to copy NIL
177     TTree& operator=(const TTree& aOtherTTree)
178     {
179         if (this != &aOtherTTree)
180             if (!aOtherTTree.empty())
181             {
182                 this->~TernaryTree();
183                 fKey = aOtherTTree.fKey;
184                 for (size_t i = 0; i < 3; i++)
185                 {
186                     if (!aOtherTTree.fSubTrees[i]->empty())
187                     {
188                         fSubTrees[i] = aOtherTTree.fSubTrees[i]->clone();
189                     }
190                     else
191                     {
192                         fSubTrees[i] = &NIL;
193                     }
194                 }

```

```
195         }
196         else
197         {
198             throw domain_error("NIL as source not permitted.");
199         }
200         return *this;
201     }
202
203     // clone ternary tree, must not copy empty trees
204     TSubTree clone() const
205     {
206         if (empty())
207         {
208             throw domain_error("NIL as source not permitted.");
209         }
210         return new TTree(*this);
211     }
212
213     //////////////////////////////////////
214     // Problem 3: TernaryTree Move Semantics
215
216     // TTree r-value constructor
217     TernaryTree( T&& aKey ): fKey(std::move(aKey))
218     {
219         for (int i = 0; i < 3; i++)
220         {
221             fSubTrees[i] = &NIL;
222         }
223     }
224
225     // move constructor, must not copy empty ternary tree
226     TernaryTree( TTree&& aOtherTTree )
227     {
228         for (int i = 0; i < 3; i++)
229         {
230             fSubTrees[i] = &NIL;
231         }
232         *this = move(aOtherTTree);
233     }
234
235     // move assignment operator, must not copy empty ternary tree
236     TTree& operator=( TTree&& aOtherTTree )
237     {
238         if (this != &aOtherTTree)
239         {
240             if (!aOtherTTree.empty())
241             {
242                 this->~TernaryTree();
243                 fKey = std::move(aOtherTTree.fKey);
```

```
244         for (int i = 0; i < 3; i++)
245         {
246             if (!aOtherTTree.fSubTrees[i]->empty()) fSubTrees[i] =
247                 const_cast<TSubTree>(&aOtherTTree.removeSubTree(i));
248             else fSubTrees[i] = &NIL;
249         }
250     else
251     {
252         throw std::domain_error("NIL as source not permitted.");
253     }
254 }
255 }
256
257 ///////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////
258 // Problem 4: TernaryTree Prefix Iterator
259
260 // return ternary tree prefix iterator positioned at start
261 Iterator begin() const
262 {
263     return Iterator(this).begin();
264 }
265
266 // return ternary prefix iterator positioned at end
267 Iterator end() const
268 {
269     return Iterator(this).end();
270 }
271 };
272
273 template<typename T>
274 TernaryTree<T> TernaryTree<T>::NIL;
275
```

```
1
2 // COS30008, Final Exam, 2022
3
4 #pragma once
5
6 #include "TernaryTree.h"
7
8 #include <stack>
9
10 template<typename T>
11 class TernaryTreePrefixIterator
12 {
13 private:
14     using TTree = TernaryTree<T>;
15     using TTreeNode = TTree*;
16     using TTreeStack = std::stack<const TTree*>;
17
18     const TTree* fTTree;           // ternary tree
19     TTreeStack fStack;             // traversal stack
20
21 public:
22
23     using Iterator = TernaryTreePrefixIterator<T>;
24
25     Iterator operator++(int)
26     {
27         Iterator old = *this;
28
29         ++(*this);
30
31         return old;
32     }
33
34     bool operator!=( const Iterator& aOtherIter ) const
35     {
36         return !(*this == aOtherIter);
37     }
38
39     //////////////////////////////////////
40     // Problem 4: TernaryTree Prefix Iterator
41
42 private:
43
44     // push subtree of aNode [30]
45     void push_subtrees( const TTree* aNode )
46     {
47         if (!(*aNode).getRight().empty())
48         {
49             fStack.push(const_cast<TTreeNode>(&(*aNode).getRight()));
```



```

50     }
51     if (!(*aNode).getMiddle().empty())
52     {
53         fStack.push(const_cast<TTreeNode>(&(*aNode).getMiddle()));
54     }
55     if (!(*aNode).getLeft().empty())
56     {
57         fStack.push(const_cast<TTreeNode>(&(*aNode).getLeft())); 5;
58     }
59 }
60
61 public:
62
63     // iterator constructor [12]
64     TernaryTreePrefixIterator( const TTree* aTTree ): fTTree(aTTree),      ↗
65     {
66         fStack()
67         {
68             if (!(*fTTree).empty())
69             {
70                 fStack.push(const_cast<TTreeNode>(&(*fTTree)));
71             }
72         }
73         // iterator dereference [8]
74         const T& operator*() const
75         {
76             return **fStack.top();
77         }
78         // prefix increment [12]
79         Iterator& operator++()
80         {
81             TTreeNode lPopped = const_cast<TTreeNode>(&(*fStack.top()));
82             fStack.pop();
83             push_subtrees(lPopped);
84             return *this;
85         }
86
87         // iterator equivalence [12]
88         bool operator==( const Iterator& aOtherIter ) const
89         {
90             return fTTree == aOtherIter.fTTree && fStack.size() ==      ↗
91                 aOtherIter.fStack.size();
92         }
93         // auxiliaries [4,10]
94         Iterator begin() const
95         {
96             Iterator temp = *this;

```

---

```
97         temp.fStack = TTreeStack();
98         temp.fStack.push(const_cast<TTreeNode>(temp.fTTree));
99         return temp;
100     }
101     Iterator end() const
102     {
103         Iterator temp = *this;
104         temp.fStack = TTreeStack();
105         return temp;
106     }
107 };
108
```

**Problem 5****(50 marks)**

Answer the following questions in one or two sentences:

- a. How can we construct a tree where all nodes have the same degree? [4]

**5a)**

- b. What is the difference between l-value and r-value references? [6]

**5b)**

- c. What is a key concept of an abstract data types? [4]

**5c)**

- d. How do we define mutual dependent classes in C++? [4]

**5d)**

- e. What must a value-based data type define in C++? [2]

**5e)**

f. What is an object adapter? [6]

5f)

g. What is the difference between copy constructor and assignment operator and how do we guarantee safe operation? [8]

5g)

h. What is the best-case, average-case, and worse-case for a lookup in a binary tree? [6]

5h)

i. What are reference data members and how do we initialize them? [2]

5i)

j. You are given  $n-1$  numbers out of  $n$  numbers. How do we find the missing number  $n_k$ ,  $1 \leq k \leq n$ , in linear time? [8]

5j)