

C++ によるデリバティブ・ライブラリ構築の基礎

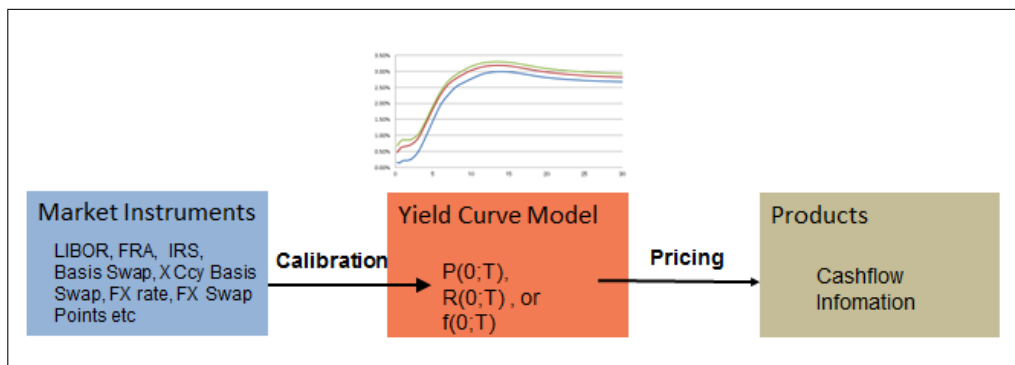
6. イールドカーブ

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1 イールドカーブの構築

マーケットでトレードされている流動性のある商品の価値をイールドカーブでプライシングを行い、その価値がマーケットでトレードされている価値になるように、イールドカーブの情報を逆算する。



(Figure 1) イールドカーブモデル、プライシング、及びカリブレーション

2 キャッシュフローのプライシング

$D(T)$ を現在 (時点 0) における時点 T のディスカウント・ファクターをする。

2.1 ビュレット (Bullet) ・キャッシュフロー

時点 T における金額を A とすれば、現在価値 V は

$$V = D(T) * A$$

である。

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2.2 固定金利のキャッシュフロー

元本 N 、年率表示の金利を r 、利息期間のスタート時刻を年で T_s 、利息期間のエンド時刻を年で T_e とする。

$$V = N \cdot r \cdot (T_e - T_s) \cdot D(T_e)$$

2.3 変動金利のキャッシュフロー

現在まだ決まっていない、利息期間 $[T_s, T_e]$ の変動金利の現在価値を考える。この変動金利は時点 T_s で決まり、時点 T_e に支払われる。利息期間のスタート時点で N 単位のキャッシュをこの変動金利で運用すると、フィクシングした金利を L とすれば、エンド時点の T_e では $1 + L(T_e - T_s)$ となっている。これらのキャッシュフローは、

$$\begin{cases} \text{時点 } T_s : & -N \\ \text{時点 } T_e : & N \cdot (1 + L \cdot (T_e - T_s)) \end{cases} \quad (1)$$

である。これらのキャッシュフローの総現在価値はゼロであるから、変動金利の現在価値を V をすれば、

$$0 = N (D(T_e) - D(T_s)) + V$$

これより、まだ決まっていない変動金利キャッシュフローの現在価値 V は

$$V = N (D(T_s) - D(T_e)) \quad (2)$$

と計算できる。

利息期間が $[T_s, T_e]$ である現在の変動金利のフォワードレート F を算出しておこう。 F はフォワードレートの定義から

$$V = N \cdot K \cdot (T_e - T_s) \cdot D(T_e)$$

が成り立つような K であるから、(2) より

$$F = \frac{1}{T_e - T_s} \left(\frac{D(T_s)}{D(T_e)} - 1 \right) \quad (3)$$

よって、(3) から、フォワードレート F を計算して、これがあたかも固定レートのように現在価値を計算しても同じことである。つまり、

$$V = N \cdot F \cdot (T_e - T_s) \cdot D(T_e) \quad (4)$$

3 Forward declaration (前方宣言)

関数を定義とは別に宣言できたのと同様に、クラスも定義なしに宣言できる。この宣言を **Forward declaration** (前方宣言) という。

```
class Matirx;
```

は `Matrix` という名前はクラス型であることをプログラムに教えている。この `Matrix` 型は、定義がまだ明らかではないので、不完全型 (incomplete type) という。不完全型は次の 2 つの場合に使われる。

- ある型に対するポインタや参照を定義するときは、その型は不完全であってもよい。
- ある関数を（定義ではなく）宣言するときに用いるパラメータの型や戻り値の型は不完全型でよい。

次の場合は、クラスは定義されていなくてはならない。

- ある型のオブジェクトをつかうコードを書くときや、ポインタや参照からクラスのメンバにアクセスするとき
- クラス定義で、データメンバの型（クラス）を宣言するとき

よって、あるクラス定義で、同じクラス型のデータメンバを持つことはできない。しかし、同じクラスのポインタや参照はメンバーにすることができる。

4 Cast

浮動小数点数の割り算をおこないたいときがある。

```
int i, j;
double slope = i / j;
```

この場合、Cast で陽な型変換をおこなう。

4.1 Old-style cast

```
double slope = (double) (i) / j;
```

4.2 Static cast

```
double slope = static_cast<double> (i) / j;
```

4.3 Dynamic cast

4.3.1 ポインタ型の Dynamic cast

`dynamic_cast<T *>(e)`、ここで `T` はあるクラス型の派生クラスで `e` はベースクラスを指すポインタである。

```
if (Derived *dp = dynamic_cast<Derived *> (bp))
{
    // dp が指す Derived オブジェクトを使う
}
else
{
    // bp が指すオブジェクトを使う
}
```

もし上で、`bp` が `Derived` のオブジェクトを指しているのであれば、キャストで `dp` は `bp` が指している `Derived` オブジェクトを指すように初期化される。そうでなければ、キャストの結果は `0(null pointer)` となる。

4.3.2 参照型の Dynamic cast

`dynamic_cast<T &>(e)`、ここで `T` はあるクラス型の派生クラスで `e` はベースクラスを指すポインタである。

参照型の `Dynamic cast` がポインタ型の `Dynamic cast` と違うところは、エラー処理である。もし、ダイナミックキャストが失敗したら、キャストは `std::bad_cast` という例外を投げる。

5 コード

5.1 UTMModelBase.h

```
#ifndef UT_MODEL_BASE_H
#define UT_MODEL_BASE_H
#include <string>
/////////////////////////////////////////////////////////////////
/////////////////////////////////////////////////////////////////
// UTMModelBase
//
// The base class for all models.
//
class UTMModelBase
{
public:
    static std::string const ourClassTag;

    // Friend class.
    // Make UTSolveForModelComponent a friend so that model can be calibrated.
    friend class UTMModelFactory;

    friend class UTSolveForModelComponent;

    // Destructor.
    virtual ~UTMModelBase() {}

    // Constructor.
    UTMModelBase() {}

    // Clone.
    virtual UTMModelBase* clone() const = 0;

    // Functions.
    virtual std::string classTag() const = 0;
    virtual double df(double time) const = 0;
    virtual double forwardRate(double startTime, double endTime) const = 0;

    // Return a reference to the ith sub-model
```

```

        virtual const UTMModelBase* subModel(unsigned long i) const;

private:
    // solver in the calibration only use this.
    virtual void setComponent(unsigned int i, double component) = 0;
};
/////////////////////////////////////////////////////////////////
/////////////////////////////////////////////////////////////////
#endif // UT_MODEL_BASE_H

```

5.2 UTMModelBase.cpp

```

#include "UTModelBase.h"
using namespace std;

const string UTMModelBase::ourClassTag = "Model Base";

/////////////////////////////////////////////////////////////////
/////////////////////////////////////////////////////////////////
const UTMModelBase* UTMModelBase::subModel(unsigned long i) const
{
    return nullptr;
}

```

5.3 UTMModelYieldCurve.h

```

#ifndef UT_MODEL_YIELD_CURVE_H
#define UT_MODEL_YIELD_CURVE_H

#include <string>
#include <vector>

#include "UTModelBase.h"

/////////////////////////////////////////////////////////////////
/////////////////////////////////////////////////////////////////
class UTMModelYieldCurve : public UTMModelBase
{
public:
    enum UT_InterpolateType
    {
        UT_FWD_RATE = 0,
        UT_ZERO_RATE = 1,
        UT_MINUS_LOG_DF = 2
    }

```

```

};

enum UT_InterpolationMethod
{
    UT_FLAT = 0,
    UT_CUBIC_SPLINE = 1,
    UT_LINEAR = 2
};

static std::string const ourClassTag;

// Destructor.
virtual ~UTModelYieldCurve();

// Defalut Constructor: construct the default flat yield curve at 3%
UTModelYieldCurve();

// Constructor with user specified flat rate
UTModelYieldCurve(double flatRate);

//Cinstructor with user specified yield curve
UTModelYieldCurve(
    const std::vector<double>&    timeLine,
    const std::vector<double>&    rates,
    UT_InterpolateeType interpolateeType = UT_FWD_RATE,
    UT_InterpolationMethod interpolationMethod = UT_FLAT);

//Clone
virtual UTModelBase* clone() const;

// Functions.
virtual std::string classTag() const { return ourClassTag; }

// Return the discount factor given a date
virtual double df( double time) const;
// Return the forward rate given two dates
virtual double forwardRate(double startTime, double endTime) const;
// Return minus log of DF
double lnDf(double time) const;

private:

// solver in the calibration only use this.
virtual void setComponent(unsigned int i, double component) { myRates[i] = component; }

//Yield Curve
std::vector<double> myTimeLine;

```

```

        std::vector<double> myRates;
        UT_InterpolateeType myInterpolatee;
        UT_InterpolationMethod myInterpolationMethod;
    };
#endif // UT_MODEL_YIELD_CURVE_H

```

5.4 UTMModelYieldCurve.cpp

```

#include "UTModelYieldCurve.h"

using namespace std;

////////////////////////////////////
////////////////////////////////////
// Static data.
// The class tag
const string UTMModelYieldCurve::ourClassTag = "Yield Curve Model";

////////////////////////////////////
////////////////////////////////////
UTModelYieldCurve::~UTModelYieldCurve()
{
}

////////////////////////////////////
//Default constructor: Default yield curve of flat 3%
UTModelYieldCurve::UTModelYieldCurve()
    : UTMModelBase(),
      myTimeLine(1, 1.0), myRates(1, 0.03), myInterpolatee(UT_FWD_RATE), myInterpolation-
Method(UT_FLAT)
{
}

////////////////////////////////////
UTModelYieldCurve::UTModelYieldCurve(double flatRate)
    : UTMModelBase(),
      myTimeLine(1, 1.0), myRates(1, flatRate), myInterpolatee(UT_FWD_RATE), myInterpolation-
Method(UT_FLAT)
{
}

////////////////////////////////////
UTModelYieldCurve::UTModelYieldCurve(const vector<double>&    timeLine,
        const vector<double>&    rates,

```

```

        UT_InterpolateType interpolateeType,
        UT_InterpolationMethod interpolationMethod)
    : UTModelBase(),
      myTimeLine(timeLine), myRates(rates), myInterpolatee(interpolateeType), myInterpolation-
Method(interpolationMethod)
{
}

////////////////////////////////////
UTModelBase* UTModelYieldCurve::clone() const
{
    return new UTModelYieldCurve(*this);
}

////////////////////////////////////
double UTModelYieldCurve::df(double time) const
{
    return exp(-1.0 * lnDf(time));
}

////////////////////////////////////
double UTModelYieldCurve::forwardRate(double startTime, double endTime) const
{
    double rtn = df(startTime) / df(endTime) - 1.0;
    return rtn / (endTime - startTime);
}

////////////////////////////////////
double UTModelYieldCurve::lnDf(double time) const
{
    //Assuming piecewise flat forward rate interpolation..
    if (time < 0.0)
    {
        return 0.0;
    }

    // Get the size of the time line.
    auto gridSize = myTimeLine.size();
    double previousTime = 0.0;
    double currentTime = 0.0;
    double sum = 0.0;
    unsigned int i = 0;
    for (i = 0; i < gridSize; ++i)

```



```

{
    currentTime = myTimeLine[i];
    if (currentTime <= time)
    {
        sum += myRates[i] * (currentTime - previousTime);
        previousTime = currentTime;
    }
    else
    {
        //This means interpolation
        return sum + myRates[i] * (time - previousTime);
    }
}

//This means extrapolation (i.e., input time > last grid point of time)
return sum + myRates[i-1] * (time - previousTime);
}

////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////
////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////

```

5.5 UTValuationEngineProduct.h

```

#ifndef UT_VALUATION_ENGINE_PRODUCT_H
#define UT_VALUATION_ENGINE_PRODUCT_H

#include <memory>
#include <vector>

// Forward declaration
class UTModelBase;
class UTModelYieldCurve;
class UTProductBase;
class UTProductLinearBase;
class UTProductCashflowBase;
class UTProductCashflowBullet;
class UTProductCashflowRateFixed;
class UTProductCashflowRateFloat;
////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////
////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////
class UTValuationEngineProductBase
{
public:

```

```

// Destructor.
virtual ~UTValuationEngineProductBase() {};
// Constructor.
UTValuationEngineProductBase(const UTModelBase & model);

// Calculates the PV of the Product and accumulate it in the ResultPV object.
virtual void calculatePV( double& result ) = 0;
// Accessors
const UTModelBase & modelBase() const { return myModelBase; }

protected:
    const UTModelBase & myModelBase;
};

////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////
class UTValuationEngineAnalyticProductLinear : public UTValuationEngineProductBase
{
public:
    // Destructor.
    virtual ~UTValuationEngineAnalyticProductLinear() {};
    // Constructor.
    UTValuationEngineAnalyticProductLinear(const UTModelBase & model, const UTProductLin-
earBase & product);

    // Accessor
    const UTProductLinearBase& linearProduct() const { return myProductLinear; }

    // Calculates the PV of the Product and accumulate it in the ResultPV object.
    virtual void calculatePV(double& result);

private:
    // Private functions
    unsigned int size() const { return mySubValuationEngines.size(); }
    UTValuationEngineProductBase& subValuationEngine(unsigned int i) { return *(mySubValua-
tionEngines[i]); }
    const UTValuationEngineProductBase& subValuationEngine(unsigned int i) const { return *(my-
SubValuationEngines[i]); }

    const UTProductLinearBase & myProductLinear;
    // This valuation engine contains lots of 'smaller' valuation engines: one for each (undetermined)
sub-product in the product linear
    std::vector<std::unique_ptr<UTValuationEngineProductBase> > mySubValuationEngines;
};

////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////

```

```

class UTValuationEngineProductCashflowBase : public UTValuationEngineProductBase
{
public:

    // Destructor.
    virtual ~UTValuationEngineProductCashflowBase() {};

    // Constructor.
    UTValuationEngineProductCashflowBase(const UTModelBase & model, const UTProductCash-
flowBase & product);

protected:

    // Accessors
    const UTProductCashflowBase & productCashFlowBase() const { return myProductCashFlow-
Base; }

    //member
    double myValue;
private:
    const UTProductCashflowBase & myProductCashFlowBase;
};

////////////////////////////////////
////////////////////////////////////
// A yield curve model is used to value the following cashflows.
//
// UTProductCashflowBullet
// UTProductCashflowRateFixed
// UTProductCashflowRateFloat

class UTValuationEngineAnalyticYieldCurveProductCashflowBullet : public UTValuationEnginePro-
ductCashflowBase
{
public:

    // Destructor.
    virtual ~UTValuationEngineAnalyticYieldCurveProductCashflowBullet() {}

    // Constructor.
    UTValuationEngineAnalyticYieldCurveProductCashflowBullet(
        const UTModelYieldCurve & model,
        const UTProductCashflowBullet & cashFlow);
private:
    // References to the model and the cashflow.
    const UTModelYieldCurve & myModel;

```

```

const UTProductCashflowBullet & myProductCashflow;

// Calculated values.
double myPayment;
double myPaymentDf;
};

////////////////////////////////////
class UTValuationEngineAnalyticYieldCurveProductCashflowRateFixed : public UTValuationEngineProductCashflowBase
{
public:

// Destructor.
virtual ~UTValuationEngineAnalyticYieldCurveProductCashflowRateFixed() {}
// Constructor.
UTValuationEngineAnalyticYieldCurveProductCashflowRateFixed(
    const UTMModelYieldCurve & model,
    const UTProductCashflowRateFixed & cashFlow);

private:

// References to the model and the cashflow.
const UTMModelYieldCurve & myModel;
const UTProductCashflowRateFixed & myProductCashflow;

// Calculated values.
double myFlowPayment;
double myFlowPaymentDf;
double myRate;
};

////////////////////////////////////
class UTValuationEngineAnalyticYieldCurveProductCashflowRateFloat : public UTValuationEngineProductCashflowBase
{
public:

// Destructor.
virtual ~UTValuationEngineAnalyticYieldCurveProductCashflowRateFloat() {}
// Constructor.
UTValuationEngineAnalyticYieldCurveProductCashflowRateFloat(
    const UTMModelYieldCurve & model,
    const UTProductCashflowRateFloat & cashFlow);

private:

```

```

// References to the model and the cashflow.
const UTMModelYieldCurve & myModel;
const UTPProductCashflowRateFloat & myProductCashflow;

// Calculated values.
double myFlowPayment;
double myFlowPaymentDf;
double myFlowPaymentWithZeroSpread;
double myFlowValueWithZeroSpread;
double myForwardRate;
};

////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////
////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////
#endif // UT_VALUATION_ENGINE_PRODUCT_H

```

5.6 UTValuationEngineProduct.cpp

```

#include "UTEnum.h"
#include "UTValuationEngineProduct.h"
#include "UTValuationEngineFactory.h"
#include "UTProductCashflow.h"
#include "UTProductSwap.h"
#include "UTModelYieldCurve.h"

using namespace std;

////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////
////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////
//UTValuationEngineProductBase
//
UTValuationEngineProductBase::UTValuationEngineProductBase(const UTMModelBase & model)
    : myModelBase(model)
{
}

////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////
////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////
//UTValuationEngineProductCashflowBase
//
UTValuationEngineProductCashflowBase::UTValuationEngineProductCashflowBase(
    const UTMModelBase & model,
    const UTPProductCashflowBase & product)
:

```

```

        UTValuationEngineProductBase(model),
        myProductCashFlowBase(product)
    {
    }

////////////////////////////////////
void UTValuationEngineProductCashflowBase::calculatePV( double& resultPv )
{
    // Accumulate only Pv
    resultPv += myValue;
}

////////////////////////////////////
////////////////////////////////////
//UTValuationEngineAnalyticYieldCurveProductLinear
//
UTValuationEngineAnalyticProductLinear::UTValuationEngineAnalyticProductLinear(const    UT-
ModelBase& model, const UTProductLinearBase & product)
:
    UTValuationEngineProductBase(model),
    myProductLinear(product)
{
    unsigned long iSize = myProductLinear.size();
    mySubValuationEngines.resize(myProductLinear.size());
    for (unsigned long i = 0; i < myProductLinear.size(); ++i)
        mySubValuationEngines[i] = unique_ptr<UTValuationEngineProductBase>(UTValuationEngineFactory::new
*myProductLinear.underlying(i));
}

////////////////////////////////////
// Calculates the PV of the Product and accumulate it
void
UTValuationEngineAnalyticProductLinear::calculatePV(double& resultPv)
{
    // Loops though each sub-valuation engine to accumulate the PV of each component or leg (or
sub-product...)
    for (unsigned int i = 0; i < size(); ++i)
    {
        subValuationEngine(i).calculatePV(resultPv);
    }
}

////////////////////////////////////

```

```

////////////////////////////////////
// UTValuationEngineAnalyticYieldCurveProductCashflowBullet
//
UTValuationEngineAnalyticYieldCurveProductCashflowBullet::UTValuationEngineAnalyticYieldCurveProductCashfl
    const UTModelYieldCurve & model,
    const UTProductCashflowBullet & cashFlow)
: UTValuationEngineProductCashflowBase(model, cashFlow),
  myModel(model),
  myProductCashflow(cashFlow)
{
    // The payment date and payment.
    double payTime = myProductCashflow.paymentTime();
    myPayment = myProductCashflow.amount();

    // The value is signed by whether we pay (-) or receive (+).
    if (myProductCashflow.payReceive() == UT_PayReceive::UT_PAY)
    {
        myPayment *= -1.0;
    }

    // Check the payment date is after the value date.
    if (payTime >= 0.0)
    {
        // Get the discount factor from the curve.
        myPaymentDf = myModel.df(payTime);
        myValue = myPayment * myPaymentDf;
    }
    else
    {
        myPaymentDf = 1.0;
        myValue = 0.0;
    }
}

////////////////////////////////////
////////////////////////////////////
//
// UTValuationEngineAnalyticYieldCurveProductCashflowRateFixed
//
UTValuationEngineAnalyticYieldCurveProductCashflowRateFixed::UTValuationEngineAnalyticYieldCurveProductC
    const UTModelYieldCurve & model,
    const UTProductCashflowRateFixed & cashFlow)

```

```

: UTValuationEngineProductCashflowBase(model, cashFlow),
myModel(model),
myProductCashflow(cashFlow)
{
    // The rate is just a fixed coupon.
    myRate = myProductCashflow.coupon();

    // The payment
    const double paymentTime = myProductCashflow.paymentTime();
    myFlowPayment = myProductCashflow.notional() * myProductCashflow.accrued() * myRate;

    // The value is signed by whether we pay (-) or receive (+).
    if (myProductCashflow.payReceive() == UT_PayReceive::UT_PAY)
    {
        myFlowPayment *= -1.0;
    }

    // Check the payment date is after the value date.
    if (paymentTime >= 0.0)
    {
        // Get the discount factor from the curve.
        myFlowPaymentDf = myModel.df(paymentTime);
        myValue = myFlowPayment * myFlowPaymentDf;
    }
    else
    {
        myFlowPaymentDf = 1.0;
        myValue = 0.0;
    }
}

////////////////////////////////////
////////////////////////////////////
//
// UTValuationEngineAnalyticYieldCurveProductCashflowRateFloat
//
UTValuationEngineAnalyticYieldCurveProductCashflowRateFloat::UTValuationEngineAnalyticYieldCurveProductCa
    const UTModelYieldCurve & model,
    const UTProductCashflowRateFloat & cashFlow)
:
    UTValuationEngineProductCashflowBase(model, cashFlow),
    myModel(model),
    myProductCashflow(cashFlow)

```



```

{
    const double paymentTime = myProductCashflow.paymentTime();

    // If the payment date is STRICTLY before the model value date, do NOT take it into account
    if (paymentTime <
    {
        myFlowPaymentDf = 1.0;
        myFlowPayment = 0.0;
        myFlowPaymentWithZeroSpread = 0.0;
        myForwardRate = 0.0;
    }
    else
        // The payment date is on or after the value date, take the payment into account
        {
            // Calculate the (forward) value of the libor index (payment forward measure).
            myForwardRate = myModel.forwardRate(myProductCashflow.startTime(), myProduct-
Cashflow.endTime());
            // The payment, and its 'derivatives' w.r.t. the spread.
            double adjustedNotional = myProductCashflow.notional() * myProductCashflow.accrued();
            myFlowPayment = adjustedNotional * (myForwardRate + myProductCashflow.spread());
            myFlowPaymentWithZeroSpread = adjustedNotional * myForwardRate;

            // Get the discount factor from the curve.
            myFlowPaymentDf = myModel.df(paymentTime);
        }

    // The value is signed by whether we pay (-) or receive (+).
    if (myProductCashflow.payReceive() == UT_PayReceive::UT_PAY)
    {
        myFlowPayment *= -1.0;
        myFlowPaymentWithZeroSpread *= -1.0;
    }

    myValue = myFlowPayment * myFlowPaymentDf;
    myFlowValueWithZeroSpread = myFlowPaymentWithZeroSpread * myFlowPaymentDf;
}

////////////////////////////////////
////////////////////////////////////

```

5.7 UTValuationEngineFactory.h

```

#ifndef UT_VALUATION_ENGINE_FACTORY_H
#define UT_VALUATION_ENGINE_FACTORY_H

```

```

#include <memory>
#include <vector>

#include "UTValuationEngineProduct.h"

////////////////////////////////////
////////////////////////////////////
// Create the appropriate valuation engine by model, product and method
class UTValuationEngineFactory
{
public:
    // Generic Valuation Engine for analytic method
    static std::unique_ptr<UTValuationEngineProductBase> newValuationEngineAnalytic(const
UTModelBase& model, const UTPProductBase& product, bool bThrow = false);

    // Valuation Engine for Analytic + YieldCurveModel
    static std::unique_ptr<UTValuationEngineProductBase> newValuationEngineAnalyticYield-
Curve(const UTModelYieldCurve& model, const UTPProductBase& product, bool bThrow = false);

};

#endif // UT_VALUATION_ENGINE_FACTORY_H

```

5.8 UTValuationEngineFactory.cpp

```

#include "UTValuationEngineFactory.h"
#include "UTValuationEngineProduct.h"
#include "UTProductCashflow.h"
#include "UTProductSwap.h"
#include "UTModelYieldCurve.h"

using namespace std;

////////////////////////////////////
unique_ptr<UTValuationEngineProductBase> UTValuationEngineFactory::newValuationEngineAnalytic(const
UTModelBase& model, const UTPProductBase& product, bool bThrow)
{
    if (model.classTag() == "Yield Curve Model")
    {
        return newValuationEngineAnalyticYieldCurve(dynamic_cast<const UTModelYieldCurve&>(model),
product, bThrow);
    }
    else
    {
        if (bThrow)

```

```

        {
            throw runtime_error("UTValuationEngineRegistry::The input model cannot value the
product analytically.");
        }
    }

    return nullptr;
}

////////////////////////////////////
unique_ptr<UTValuationEngineProductBase> UTValuationEngineFactory::newValuationEngineAnalyticYieldCurve(c
UTModelYieldCurve& model, const UTProductBase& product, bool bThrow)
{
    unique_ptr<UTValuationEngineProductBase> pValuationEngine(nullptr);
    if (product.classTag() == "Vanilla Leg")
    {
        pValuationEngine.reset(new UTValuationEngineAnalyticProductLinear(model, dy-
namic_cast<const UTProductLinearBase&>(product)));
    }
    else if (product.classTag() == "Vanilla Swap")
    {
        pValuationEngine.reset(new UTValuationEngineAnalyticProductLinear(model, dy-
namic_cast<const UTProductLinearBase&>(product)));
    }
    else if (product.classTag() == "Product Cashflow Bullet")
    {
        pValuationEngine.reset(new UTValuationEngineAnalyticYieldCurveProductCashflowBul-
let(model, dynamic_cast<const UTProductCashflowBullet&>(product)));
    }
    else if (product.classTag() == "Product Cashflow Rate Fixed")
    {
        pValuationEngine.reset(new UTValuationEngineAnalyticYieldCurveProductCashflowRate-
Fixed(model, dynamic_cast<const UTProductCashflowRateFixed&> (product)));
    }
    else if (product.classTag() == "Product Cashflow Rate Float")
    {
        pValuationEngine.reset(new UTValuationEngineAnalyticYieldCurveProductCashflowRate-
Float(model, dynamic_cast<const UTProductCashflowRateFloat&> (product)));
    }
    else
    {

```

```

        if (bThrow)
        {
            throw runtime_error("UTValuationEngineFactory::The input product cannot be valued
by Yield curve model analytically.");
        }
    }

    return pValuationEngine;
}

////////////////////////////////////
////////////////////////////////////

```

5.9 UTModelFactory.h

```

#ifndef UT_MODEL_FACTORY_H
#define UT_MODEL_FACTORY_H

#include <vector>

#include "UTModelYieldCurve.h"
#include "UTProductCashflow.h"
#include "UTBisection.h"

////////////////////////////////////
////////////////////////////////////
// UTModelFactory
//
class UTModelFactory
{
public:
    // Destructor.
    virtual ~UTModelFactory() {}

    // Constructor.
    UTModelFactory() {}

    // Creates a 'calibrated' yield curve model
    static std::unique_ptr<UTModelYieldCurve> newModelYieldCurve(
        const std::vector<double> & swapMaturities,
        const std::vector<double> & swapRates,
        const UTModelYieldCurve::UT_InterpolationMethod& interpMethod = UTModelYield-
Curve::UT_FLAT,
        const UTModelYieldCurve::UT_InterpolateeType& interpolateeType = UTModelYield-
Curve::UT_FWD_RATE );

```

```

};

/////////////////////////////////////////////////////////////////
/////////////////////////////////////////////////////////////////
//Helper Class for model calibration
class UTSolveForModelComponent : public UTBisection
{
    // Object for this class: Calibration of the given model
public:

    virtual ~UTSolveForModelComponent() {}
    UTSolveForModelComponent(UTModelBase &model, const UTProductBase& product, double
target, unsigned int componentNumber)
        : UTBisection(),
        myModel(model),
        myProduct(product),
        myTarget(target),
        myComponentNumber(componentNumber){}

    // Overloaded penalty function
    virtual double error (double x);

private:

    UTModelBase &    myModel;
    const UTProductBase& myProduct;
    double myTarget;
    unsigned int myComponentNumber;
};

/////////////////////////////////////////////////////////////////
/////////////////////////////////////////////////////////////////
#endif // UT_MODEL_FACTORY_H

```

5.10 UTModelFactory.cpp

```

#include <memory>

#include "UTEnum.h"
#include "UTModelFactory.h"
#include "UTProductSwap.h"
#include "UTValuationEngineFactory.h"
#include "UTBisection.h"

using namespace std;

/////////////////////////////////////////////////////////////////

```

```

////////////////////////////////////
unique_ptr<UTModelYieldCurve>
UTModelFactory::newModelYieldCurve(
const vector<double> & swapMaturities,
const vector<double> & swapRates,
const UTModelYieldCurve::UT.InterpolationMethod& interpMethod,
const UTModelYieldCurve::UT.InterpolateeType& interpolateeType)
{
    // Check the size of the 2 vectors
    if (swapMaturities.size() != swapRates.size())
    {
        throw runtime_error("UTModelFactory: The size of swap maturities and rates should be the
same.");
    }

    // Create a temporal yield curve model with inputed interp method
    unique_ptr<UTModelYieldCurve> pYieldCurveModel(new UTModelYieldCurve(swapMaturities,
swapRates, interpolateeType, interpMethod));

    //We are assuming that the swap maturities and rates are ordered correctly...
    for (unsigned int i = 0; i < swapMaturities.size(); ++i)
    {
        // create product.
        // Assuming the swap convention is like JPY swaps..
        UTProductSwapVanilla vanillaSwap(0, swapMaturities[i], swapRates[i], 0.5, 0.5, 10000.0,
UT_PayReceive:: UT_RECEIVE);
        UTSolveForModelComponent solver(*pYieldCurveModel, vanillaSwap, 0.0,i);
        double rate = solver.root(-0.1, 1.0);
    }

    // Calibration is done! So return the calibrated model
    return pYieldCurveModel;
}

////////////////////////////////////
////////////////////////////////////
double
UTSolveForModelComponent::error(double x)
{
    // Pricing
    myModel.setComponent(myComponentNumber,x);

    // Usually Calibration is done to analytic prices...

```

```

        unique_ptr<UTValuationEngineProductBase>pricer(UTValuationEngineFactory::newValuationEngineAnalytic(m
myProduct));

        double pv = 0.0;
        pricer->calculatePV(pv);
        return pv - myTarget;
    }
    //////////////////////////////////////
    //////////////////////////////////////

```

5.11 UTBisection.h

```

#ifndef UT_BISECTION_H
#define UT_BISECTION_H

#include <float.h>
#include <cmath>

    //////////////////////////////////////
    //////////////////////////////////////
    // Polymorphism solution
    class UTBisection
    {
    public:
        //
        // f(x) is the value of the function at abscissa x whose zeros we are looking for.
        // The error function must be overloaded.
        virtual double error(double x) = 0;
        //
        // Virtual destructor.
        virtual ~UTBisection(){}
        //
        // NOTE: this root finder only considers convergence in the abscissa, i.e. it iterates until further
progress in the argument
        // is smaller than absoluteAccuracy.
        //
        double root(double lowerBound, double upperBound, double absoluteAccuracy = 15 *
DBL_EPSILON, unsigned long maxIterations = (DBL_DIG * 10) / 3);
    };
    //////////////////////////////////////
    //////////////////////////////////////
#endif // UT_BISECTION_H

```

5.12 UTBisection.cpp

```
#include <stdexcept>

#include "UTBisection.h"

using namespace std;

////////////////////////////////////
////////////////////////////////////
double UTBisection::root(double x1, double x2, double accuracy, unsigned long maxIterations)
{
    double f1 = error(x1);
    double f2 = error(x2);

    double xmid, fmid;
    for (unsigned long i = 0; i < maxIterations; ++i)
    {
        xmid = 0.5 * (x1 + x2);
        fmid = error(xmid);
        if (fmid == 0.0)
        {
            return xmid;
        }
        else if (f1*fmid < 0.0)
        {
            x2 = xmid;
            f2 = fmid;
        }
        else
        {
            x1 = xmid;
            f1 = fmid;
        }

        if (fabs(x2 - x1) <= accuracy || fmid == 0.0)
            return 0.5 * (x2 + x1);
    }

    throw runtime_error("UTBisection: Root search did not converge.");

    // Should never get here
    return 0.0;
}
```


5.13 UTest.h

```
#ifndef UT_TEST_H
#define UT_TEST_H

void pricingTest();
void yieldCurveCalibration();
////////////////////////////////////
////////////////////////////////////
#endif // UT_NEWTON_H
```

5.14 UTest.cpp

```
#include<iostream>
#include<fstream>
#include<string>

#include "UTEnum.h"
#include "UTProductSwap.h"
#include "UTModelYieldCurve.h"
#include "UTValuationEngineFactory.h"
#include "UTModelFactory.h"
#include "UTest.h"

using namespace std;

void yieldCurveCalibration()
{
    vector<double> swapRates{ 0.01, 0.03, 0.05 };
    vector<double> swapMaturities{ 1.0, 3.0, 5.0 };

    //Model generation
    auto yieldCurve = UTModelFactory::newModelYieldCurve(swapMaturities, swapRates);

    // Products
    UTProductSwapVanilla vanillaSwap1(0, 1.0, 0.01, 0.5, 0.5, 10000.0, UT_PayReceive::UT_RECEIVE);
    UTProductSwapVanilla vanillaSwap2(0, 3.0, 0.03, 0.5, 0.5, 10000.0, UT_PayReceive::UT_RECEIVE);
    UTProductSwapVanilla vanillaSwap3(0, 5.0, 0.05, 0.5, 0.5, 10000.0, UT_PayReceive::UT_RECEIVE);

    //Pricing Test
    auto pricer1 = UTValuationEngineFactory::newValuationEngineAnalyticYieldCurve(*yieldCurve,
vanillaSwap1);
    double pv = 0.0;
    pricer1->calculatePV(pv);
```

```

    cout << "the PV of 1st swap is " << pv << ".\n";

    auto pricer2 = UTValuationEngineFactory::newValuationEngineAnalyticYieldCurve(*yieldCurve,
vanillaSwap2);
    pv = 0.0; //reset of pv
    pricer2->calculatePV(pv);
    cout << "the PV of the 2nd swap is " << pv << ".\n";

    auto pricer3 = UTValuationEngineFactory::newValuationEngineAnalyticYieldCurve(*yieldCurve,
vanillaSwap3);
    pv = 0.0;
    pricer3->calculatePV(pv);
    cout << "the PV of the 3rd swap is " << pv << ".\n";
}

void pricingTest()
{
    // Products
    UTProductSwapVanilla vanillaSwap(0, 10, 0.03, 0.5,0.5, 10000.0, UT_PayReceive::UT_RECEIVE);
    UTProductLegVanilla fixedLeg(UT_FixedFloat::UT_FIXED, 0, 10, 0.03, 0.5, 10000.0,
UT_PayReceive::UT_RECEIVE);
    UTProductLegVanilla floatLeg(UT_FixedFloat::UT_FLOAT, 0, 10, 0.0, 0.5, 10000.0, UT_PayReceive::UT_PAY);

    //Model
    UTModelYieldCurve yieldCurve;

    //Pricing
    auto pricerFixedLeg(UTValuationEngineFactory::newValuationEngineAnalyticYieldCurve(yieldCurve,
fixedLeg));

    double pv = 0.0;
    pricerFixedLeg->calculatePV(pv);
    cout << "the PV of the fixed leg is " << pv << ".\n";

    auto pricerFloatLeg(UTValuationEngineFactory::newValuationEngineAnalyticYieldCurve(yieldCurve,
floatLeg));
    pv = 0.0; //reset of pv
    pricerFloatLeg->calculatePV(pv);
    cout << "the PV of the float leg is " << pv << ".\n";

    auto pricerSwap(UTValuationEngineFactory::newValuationEngineAnalyticYieldCurve(yieldCurve,
vanillaSwap));
    pv = 0.0;
    pricerSwap->calculatePV(pv);
    cout << "the PV of the swap is " << pv << ".\n";
}

```

5.15 UTMMain.cpp

```
#include<iostream>

#include "UTTest.h"
#include "UTProductSwap.h"
#include "UTModelYieldCurve.h"

using namespace std;

int main()
{
    try
    {
        //Put your test routine
        yieldCurveCalibration();
    }
    catch (runtime_error err)
    {
        cout << err.what();
    }

    // The final input to stop the routine
    double tmp;
    cin >> tmp;
    return 0;
}
```

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