

Aliasing

• Suppose we use a sampling frequency of Fs Hz
• This is good for input frequencies up to Fs/2 Hz
• What happens to higher frequencies?
• They should not be there – should have been filtered out.
• Assume a sine-wave of frequency F > Fs/2 remains.
• After sampling, it becomes a sine-wave of freq Fs – F.

(Assume Fs/2 < F < Fs)
• Example: If Fs = 8 kHz & F = 5 kHz, we get 3 kHz.
• It's the wrong frequency.
• If it's a harmonic within a musical note, will be out of tune.
• And it goes down when it's supposed to be going up.

Demonstration of aliasing

Simple experiment in Task 1

Do not use 'resample' for this experiment.

Listen to this demo.

Generates C-major piano scale over 4 octaves (orig file)

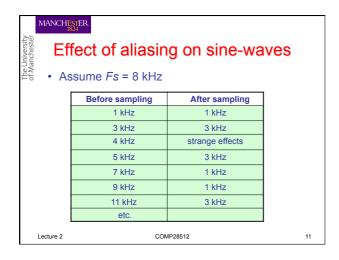
From 261.6 Hz (middle C) up to 2093 Hz

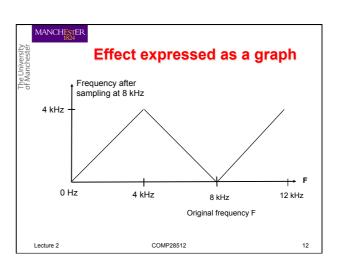
Down-sampled (no filtering) to Fs = 2kHz (aliased file).

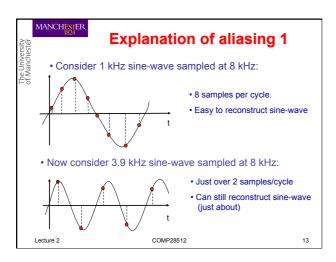
Two wav files: orig & aliased.

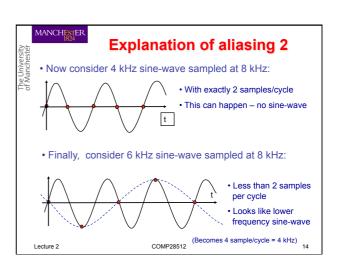
Observe in aliased file:

(1) out of tune harmonics > 1 kHz
(2) Note starts decreasing as fundamental freq goes above 1kHz

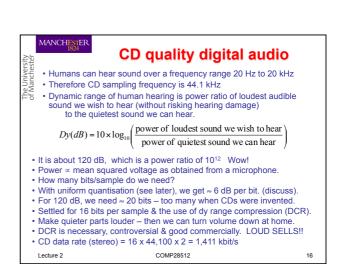








MANCHESTER Decibel (dB) scale • I can shout twice as loud as you! • Power of my sound in Watts is twice your power • My voice is 3 dB louder than yours Power ratio (dB) = $10 \times \log_{10} \left(\frac{\text{Power of my voice (Watts)}}{\text{Power of your voice (Watts)}} \right)$ $=10 \times \log_{10}(2) = 10 \times 0.3 = 3 \text{ dB}$ Power ratio dB Power ratio dB 0 1000 30 10000 40 3 1/2 -3 10⁵ 50 1010 6 100 4 10 10 10¹² 120 100 20 COMP28512 Lecture 2



**MANCHESTER

Telephone quality digital speech

**Band-limited from 300 Hz – 3.4 kHz – narrow-band.
(or 50 Hz – 3.4 kHz)

**Loses naturalness but not intelligibility (in principle)

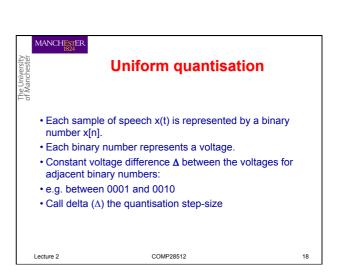
**In practice, sometimes cannot distinguish "S" from "F"!

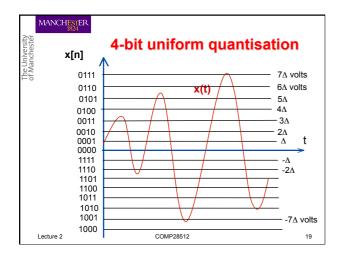
**Sampled at 8 kHz with 8 bits per sample

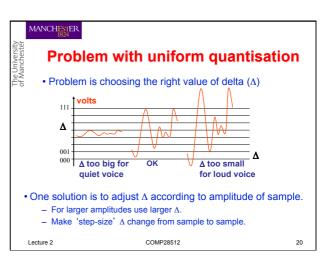
**64 kbit/s bit-rate, but needs non-uniform quantization

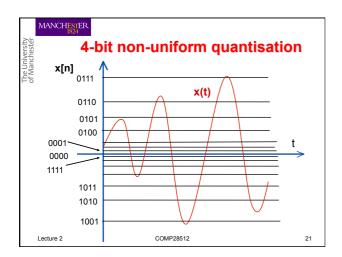
- mu-law or A-law

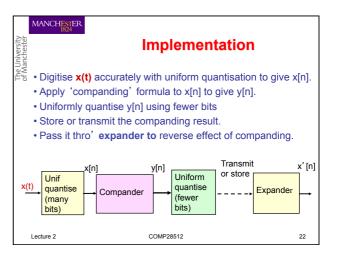
- known as the ITU-G711 standard











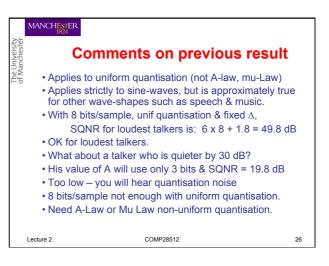
Effect of compander & expander

• Compander increases smaller amplitudes of x[n] & reduces larger ones.
• Uniform quantiser is then applied with fixed Δ.
• Expander decreases smaller amplitudes of x[n] & also Δ, & increases larger ones along with Δ.
• Effect is non-uniform quantisation as illustrated before.

• Famous companding formulas: A-law & Mu-law (G711)
• These normally require 8-bits per sample.
• Companding is like 'compression', but it is done for coding purposes, not for listening to directly.

MANCHESTER More on quantisation error • Uniform quantisation produces error in each sample. • Random in range $\pm \Delta/2$ (assuming no overflow). When samples are converted back to analogue form, error is heard as 'white noise' sound added to x(t). · 'Noise' is an unwanted signal. · White noise is spread evenly across all frequencies. · Sounds like a waterfall or the sea. • Not a car or house alarm, or a car revving its engine. • Error in each sample has uniform probability between $\pm \Delta/2$. • Mean square value (MSV) of noise is: $\Delta^2/12$ (famous result) · MSV is a measure of power COMP28512

Signal-to-quantisation noise ratio (SQNR) $SQNR = 10 \log_{10} \left(\frac{\text{signal power}}{\text{quantisation noise power}} \right) \quad \text{in decibels (dB.)}$ For a sine-wave of amplitude A, its MSV is A²/2. $\therefore \quad SQNR = 10 \log_{10} \left(\frac{A^2 / 2}{\Delta^2 / 12} \right) \quad dB$ With NB bits/sample unif quantisation & step size Δ , what is max possible value of A? Answer: $(2^{NB} / 2) \times \Delta$ $\therefore \quad SQNR = 10 \times \log_{10} \left(\frac{(2^{2 \times NB} / 8) \times \Delta^2}{\Delta^2 / 12} \right) = 10 \times \log_{10} (1.5 \times 2^{2 \times NB}) \quad dB$ $= 10 \times \log_{10} (1.5) + 20 \times NB \times \log_{10} (2) \approx 1.8 + 6 \times NB \quad dB$ $= 6 \quad dB \quad per \quad bit + 1.8$ (Another famous result) Lecture 2



MANCHESTER

Agriculture William CD recordings with 16 bits/sample

• Max SQNR = 6x16 + 1.8 = 97.8 dB.

• This is for LOUDest music.

• What abt quiet passages that we can just hear?

• Lower by 120 dB maybe?

• SQNR = -22.2 dB??

- Signal power less than quant noise power by a long way.

• Must apply DRC to CD recordings with 16 bits/sample.

• Do we really want 120 dB in our homes/cars or through ear-phones connected to mobile phones?

Speech & music on mobile phones

• 64 kbits/second still too high for mobile telephony
• Need to encode speech at around 13 kb/s or lower.
• How can we do this?
• If we sample at 8 kHz, have <2 bits/sample. No good.
• If we reduce sampling rate, bandwidth will be too low.
• What can we do?
• LPC coding (See Workshop 1 - next)
• 1.411 Mbits/s CD quality too high for music,
• Need mp3 coding
• Come to Workshop 3 (next month)

Summary

Digitising analogue signals: sampling & quantisation
Effect of aliasing
Dynamic range required for speech & music
Uniform quantisation noise power: Δ²/12
SQNR = 6m + 1.8 dB (m bits)
Non-uniform quantisation (A-Law & mu-Law).

A question

• What are similarities & differences difference between companding & compression as defined in this lecture?

• Answer: Both reduce high amplitudes and/or increase small amplitudes.

• Companding does this sample by sample for the purpose of digitising the signal. The companding is reversed before we listen to the signal.

• Compression does this gradually over many samples to reduce loud sections and/or increase quiet sections. It does not work sample by sample and the compression is not reversed before we listen to it.