

Equivalence of Finite State Automata and Regular Grammar

- FSA accepts Regular Language
- Regular Grammar generates Regular Language
- We will show
 - 1. Conversion of RG to FSA (NFA)
 - 2. Conversion of FSA(DFA) to RG

Conversion of RG to FSA(NFA)

- Given RG $G=(N,T,P,S)$ construct NFA $M=(Q,\Sigma,\delta,q_0,F)$
- Such that $L(G)=L(M)$ or $L(M)=L(G)$
- Construction
- $Q=NU\{q_f\}$: q_f is new non terminal symbol for final state
- $\Sigma=T$
- $q_0=S$
- $F=\{q_f\}$
- Now definition of δ -
- 1. If $A \rightarrow aB$ is a rule in P the $\delta(A,a)$ contains B
- 2. If $A \rightarrow a$ is a rule in P the $\delta(A,a)$ contains q_f

Conversion of RG to FSA(NFA)

Given RG

1. $S \rightarrow aS$
2. $S \rightarrow aA$
3. $A \rightarrow bA$
4. $A \rightarrow b$

$$L(G) = \{a^m b^n \mid m, n \geq 1\}$$

Construct NFA M

1. $\delta(S, a)$ contains S
2. $\delta(S, a)$ contains A
3. $\delta(A, b)$ contains A
4. $\delta(A, b)$ contains q_f

