

#Spark

1. Install Java Development Kit (JDK)

Apache Spark requires Java. We'll install `openjdk-8-jdk`.

```
!apt-get update
!apt-get install openjdk-8-jdk-headless -qq > /dev/null

0% [Working] Hit:1 https://cli.github.com/packages
stable InRelease
0% [Connecting to archive.ubuntu.com (185.125.190.83)] [Connecting to
security.
Hit:2 https://cloud.r-project.org/bin/linux/ubuntu jammy-cran40/
InRelease
0% [Connecting to archive.ubuntu.com (185.125.190.83)] [Connecting to
security. 0% [Waiting for headers] [Waiting for headers] [Waiting for
headers] [Connected
Hit:3 https://r2u.stat.illinois.edu/ubuntu jammy InRelease
Hit:4 http://archive.ubuntu.com/ubuntu jammy InRelease
Hit:5 http://security.ubuntu.com/ubuntu jammy-security InRelease
Hit:6 http://archive.ubuntu.com/ubuntu jammy-updates InRelease
Hit:7 http://archive.ubuntu.com/ubuntu jammy-backports InRelease
Hit:8 https://ppa.launchpadcontent.net/deadsnakes/ppa/ubuntu jammy
InRelease
Hit:9 https://ppa.launchpadcontent.net/ubuntugis/ppa/ubuntu jammy
InRelease
Reading package lists... Done
W: Skipping acquire of configured file 'main/source/Sources' as
repository 'https://r2u.stat.illinois.edu/ubuntu jammy InRelease' does
not seem to provide it (sources.list entry misspelt?)
```

2. Download and Extract Apache Spark

We'll download a pre-built version of Spark and extract it to a convenient location.

```
!wget -q https://archive.apache.org/dist/spark/spark-3.5.1/spark-
3.5.1-bin-hadoop3.tgz
!tar xf spark-3.5.1-bin-hadoop3.tgz
```

3. Set Environment Variables

We need to tell our system where Java and Spark are located.

```
import os
os.environ["JAVA_HOME"] = "/usr/lib/jvm/java-8-openjdk-amd64"
os.environ["SPARK_HOME"] = "/content/spark-3.5.1-bin-hadoop3"
```

4. Install findspark and pyspark

findspark helps PySpark locate Spark, and pyspark is the Python API for Spark.

```
!pip install -q findspark pyspark
```

5. Initialize SparkSession

Now you can initialize Spark and start using PySpark.

```
import findspark
findspark.init()
from pyspark.sql import SparkSession

spark =
SparkSession.builder.master("local[*]").appName("ColabSpark").getOrCreate()
print("SparkSession created successfully!")
spark

SparkSession created successfully!
<pyspark.sql.session.SparkSession at 0x7fe8f457f230>
```

#Adjusting Loan Approval.

```
import pyspark
from pyspark.sql import SparkSession
import pyspark.sql.functions as F

import pandas as pd
import warnings
warnings.filterwarnings('ignore')

spark = SparkSession.builder.appName('loan_prediction').getOrCreate()

df = spark.read.csv('Loan_default.csv', header=True, sep=',',
inferSchema=True)
df.show(5)

+-----+-----+-----+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+-----+-----+-----+
```

LoanID	Age	Income	LoanAmount	CreditScore	MonthsEmployed	NumCreditLines	InterestRate	LoanTerm	DTIRatio	Education	EmploymentType	MaritalStatus	HasMortgage	HasDependents	LoanPurpose	HasCoSigner	Default
I38PQUQS96	56	85994	50587	520	80	4	15.23	36	0.44	Bachelor's	Full-time	Divorced	Yes	Yes	Other	Yes	0
HPSK72WA7R	69	50432	124440	458	15	1	4.81	60	0.68	Master's	Full-time	Married	No	No	Other	Yes	0
C10Z6DPJ8Y	46	84208	129188	451	26	3	21.17	24	0.31	Master's	Unemployed	Divorced	Yes	Yes	Auto	No	1
V2KKSFM3UN	32	31713	44799	743	0	3	7.07	24	0.23	High School	Full-time	Married	No	No	Business	No	0
EY08JDHTZP	60	20437	9139	633	8	4	6.51	48	0.73	Bachelor's	Unemployed	Divorced	No	Yes	Auto	No	0

only showing top 5 rows

```
df.printSchema()
```

```
root
```

```
 |-- LoanID: string (nullable = true)
 |-- Age: integer (nullable = true)
 |-- Income: integer (nullable = true)
 |-- LoanAmount: integer (nullable = true)
 |-- CreditScore: integer (nullable = true)
 |-- MonthsEmployed: integer (nullable = true)
 |-- NumCreditLines: integer (nullable = true)
 |-- InterestRate: double (nullable = true)
 |-- LoanTerm: integer (nullable = true)
 |-- DTIRatio: double (nullable = true)
 |-- Education: string (nullable = true)
 |-- EmploymentType: string (nullable = true)
 |-- MaritalStatus: string (nullable = true)
 |-- HasMortgage: string (nullable = true)
 |-- HasDependents: string (nullable = true)
 |-- LoanPurpose: string (nullable = true)
 |-- HasCoSigner: string (nullable = true)
```

```
|-- Default: integer (nullable = true)
```

```
df.dtypes
```

```
[('LoanID', 'string'),  
 ('Age', 'int'),  
 ('Income', 'int'),  
 ('LoanAmount', 'int'),  
 ('CreditScore', 'int'),  
 ('MonthsEmployed', 'int'),  
 ('NumCreditLines', 'int'),  
 ('InterestRate', 'double'),  
 ('LoanTerm', 'int'),  
 ('DTIRatio', 'double'),  
 ('Education', 'string'),  
 ('EmploymentType', 'string'),  
 ('MaritalStatus', 'string'),  
 ('HasMortgage', 'string'),  
 ('HasDependents', 'string'),  
 ('LoanPurpose', 'string'),  
 ('HasCoSigner', 'string'),  
 ('Default', 'int')]
```

```
##Data Analysis
```

```
df.groupby('Default').count().show()
```

```
+-----+-----+  
|Default| count|  
+-----+-----+  
|      1| 29653|  
|      0|225694|  
+-----+-----+
```

```
from pyspark.sql import window
```

```
df_raw = (  
    spark.read  
        .option("header", True)  
        .option("inferSchema", True)  
        .csv("Loan_default.csv")  
)
```

```
df_raw.printSchema()  
df_raw.show(5, truncate=False)
```

```
root
```

```
|-- LoanID: string (nullable = true)  
|-- Age: integer (nullable = true)
```

```

|-- Income: integer (nullable = true)
|-- LoanAmount: integer (nullable = true)
|-- CreditScore: integer (nullable = true)
|-- MonthsEmployed: integer (nullable = true)
|-- NumCreditLines: integer (nullable = true)
|-- InterestRate: double (nullable = true)
|-- LoanTerm: integer (nullable = true)
|-- DTIRatio: double (nullable = true)
|-- Education: string (nullable = true)
|-- EmploymentType: string (nullable = true)
|-- MaritalStatus: string (nullable = true)
|-- HasMortgage: string (nullable = true)
|-- HasDependents: string (nullable = true)
|-- LoanPurpose: string (nullable = true)
|-- HasCoSigner: string (nullable = true)
|-- Default: integer (nullable = true)

```

```

+-----+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+-----+
+-----+-----+
|LoanID    |Age|Income|LoanAmount|CreditScore|MonthsEmployed|
NumCreditLines|InterestRate|LoanTerm|DTIRatio|Education   |
EmploymentType|MaritalStatus|HasMortgage|HasDependents|LoanPurpose|
HasCoSigner|Default|
+-----+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+-----+
+-----+-----+
|I38PQUQS96|56 |85994 |50587      |520          |80           |4
|15.23      |36 |      |0.44      |Bachelor's   |Full-time    |Divorced
|Yes         |Yes |      |Other     |Yes          |0            |
|HPSK72WA7R|69 |50432 |124440     |458          |15           |1
|4.81       |60 |      |0.68      |Master's     |Full-time    |Married
|No          |No  |      |Other     |Yes          |0            |
|C10Z6DPJ8Y|46 |84208 |129188     |451          |26           |3
|21.17      |24 |      |0.31      |Master's     |Unemployed   |Divorced
|Yes         |Yes |      |Auto      |No           |1            |
|V2KKSFM3UN|32 |31713 |44799      |743          |0            |3
|7.07       |24 |      |0.23      |High School  |Full-time    |Married
|No          |No  |      |Business  |No           |0            |
|EY08JDHTZP|60 |20437 |9139       |633          |8            |4
|6.51       |48 |      |0.73      |Bachelor's   |Unemployed   |Divorced
|No          |Yes |      |Auto      |No           |0            |
+-----+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+-----+
+-----+-----+

```

only showing top 5 rows

```
df = (
    df_raw
    .withColumn("Age", F.col("Age").cast("int"))
    .withColumn("Income", F.col("Income").cast("int"))
    .withColumn("LoanAmount", F.col("LoanAmount").cast("int"))
    .withColumn("CreditScore", F.col("CreditScore").cast("int"))
    .withColumn("MonthsEmployed", F.col("MonthsEmployed").cast("int"))
    .withColumn("NumCreditLines", F.col("NumCreditLines").cast("int"))
    .withColumn("InterestRate", F.col("InterestRate").cast("double"))
    .withColumn("LoanTerm", F.col("LoanTerm").cast("int"))
    .withColumn("DTIRatio", F.col("DTIRatio").cast("double"))
    .withColumn("Default", F.col("Default").cast("int"))
)

# Basic sanity filters (tweak thresholds if needed)
df = df.filter(
    (F.col("LoanAmount") > 0) &
    (F.col("Income") > 0) &
    (F.col("CreditScore").between(300, 850)) &
    (F.col("DTIRatio").between(0.0, 1.0)) &
    (F.col("InterestRate") >= 0.0) &
    (F.col("LoanTerm") > 0) &
    (F.col("Default").isin([0, 1]))
)

# Optional: drop rows missing core fields
core = ["LoanAmount", "InterestRate", "DTIRatio", "CreditScore",
        "Income", "Default"]
df = df.dropna(subset=core)

df.count()

255347

df = (
    df
    .withColumn(
        "CreditScoreBand",
        F.when(F.col("CreditScore") < 600, "<600")
        .when((F.col("CreditScore") >= 600) & (F.col("CreditScore")
<= 649), "600-649")
        .when((F.col("CreditScore") >= 650) & (F.col("CreditScore")
<= 699), "650-699")
        .when((F.col("CreditScore") >= 700) & (F.col("CreditScore")
<= 749), "700-749")
        .otherwise("750+")
    )
)
```

```

    )
    .withColumn(
        "DTIBand",
        F.when(F.col("DTIRatio") < 0.20, "<0.20")
        .when((F.col("DTIRatio") >= 0.20) & (F.col("DTIRatio") <
0.35), "0.20-0.34")
        .when((F.col("DTIRatio") >= 0.35) & (F.col("DTIRatio") <
0.50), "0.35-0.49")
        .otherwise("0.50+")
    )
    .withColumn(
        "IncomeBand",
        F.when(F.col("Income") < 50000, "<50k")
        .when((F.col("Income") >= 50000) & (F.col("Income") <
100000), "50k-99k")
        .when((F.col("Income") >= 100000) & (F.col("Income") <
150000), "100k-149k")
        .otherwise("150k+")
    )
)

df.select("CreditScore", "CreditScoreBand", "DTIRatio", "DTIBand",
"Income", "IncomeBand").show(10, truncate=False)

```

```

+-----+-----+-----+-----+-----+-----+
|CreditScore|CreditScoreBand|DTIRatio|DTIBand  |Income|IncomeBand|
+-----+-----+-----+-----+-----+-----+
|520        |<600           |0.44    |0.35-0.49|85994 |50k-99k   |
|458        |<600           |0.68    |0.50+    |50432 |50k-99k   |
|451        |<600           |0.31    |0.20-0.34|84208 |50k-99k   |
|743        |700-749       |0.23    |0.20-0.34|31713 |<50k      |
|633        |600-649       |0.73    |0.50+    |20437 |<50k      |
|720        |700-749       |0.1     |<0.20    |90298 |50k-99k   |
|429        |<600           |0.16    |<0.20    |111188|100k-149k |
|531        |<600           |0.43    |0.35-0.49|126802|100k-149k |
|827        |750+          |0.2     |0.20-0.34|42053 |<50k      |
|480        |<600           |0.33    |0.20-0.34|132784|100k-149k |
+-----+-----+-----+-----+-----+-----+
only showing top 10 rows

```

```

portfolio_overview = df.agg(
    F.count("*").alias("total_loans"),
    F.sum("LoanAmount").alias("total_exposure"),
    F.avg("Default").alias("default_rate"),
    F.avg("InterestRate").alias("avg_interest_rate"),
    F.avg("DTIRatio").alias("avg_dti"),
    F.avg("CreditScore").alias("avg_credit_score"),
    F.avg("Income").alias("avg_income")
).withColumn("default_rate", F.round("default_rate", 4)) \

```

```

.withColumn("avg_interest_rate", F.round("avg_interest_rate", 4)) \
.withColumn("avg_dti", F.round("avg_dti", 4)) \
.withColumn("avg_credit_score", F.round("avg_credit_score", 2)) \
.withColumn("avg_income", F.round("avg_income", 2))

```

```
portfolio_overview.show(truncate=False)
```

```

+-----+-----+-----+-----+-----+
+-----+-----+
|total_loans|total_exposure|default_rate|avg_interest_rate|avg_dti|
avg_credit_score|avg_income|
+-----+-----+-----+-----+-----+
+-----+-----+
|255347      |32576880572    |0.1161      |13.4928          |0.5002 |
574.26      |82499.3        |
+-----+-----+-----+-----+-----+
+-----+-----+

```

```

def segment_table(df, segment_col, min_count=100):
    out = (
        df.groupBy(segment_col)
        .agg(
            F.count("*").alias("n_loans"),
            F.sum("LoanAmount").alias("exposure"),
            F.avg("Default").alias("default_rate"),
            F.avg("InterestRate").alias("avg_interest_rate"),
            F.avg("DTIRatio").alias("avg_dti"),
            F.avg("CreditScore").alias("avg_credit_score"),
        )
        .withColumn("default_rate", F.round("default_rate", 4))
        .withColumn("avg_interest_rate",
            F.round("avg_interest_rate", 4))
        .withColumn("expected_loss_proxy",
            F.round(F.col("default_rate") * F.col("exposure"), 2))
        .filter(F.col("n_loans") >= min_count)
        .orderBy(F.col("expected_loss_proxy").desc())
    )
    return out

```

```

seg_purpose = segment_table(df, "LoanPurpose", min_count=50)
seg_employment = segment_table(df, "EmploymentType", min_count=50)
seg_cosigner = segment_table(df, "HasCoSigner", min_count=50)

```

```

seg_purpose.show(20, truncate=False)
seg_employment.show(20, truncate=False)
seg_cosigner.show(20, truncate=False)

```



```

+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+
|LoanPurpose|n_loans|exposure  |default_rate|avg_interest_rate|avg_dti
|avg_credit_score |expected_loss_proxy|
+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+
|Business    |51298  |6522120439|0.1233      |13.4791          |
0.5004335451674542|574.0621076845101|8.0417745013E8  |
|Auto        |50844  |6500807511|0.1188      |13.4672          |
0.5012202029738031|574.575918495791 |7.7229593231E8  |
|Education   |51005  |6510575194|0.1184      |13.5126          |
0.5013735908244298|573.2128418782472|7.7085210297E8  |
|Other       |50914  |6498135901|0.1179      |13.4778          |
0.4985940998546577|574.4078642416624|7.6613022273E8  |
|Home        |51286  |6545241527|0.1023      |13.5269          |
0.4994421479546087|575.0610108021682|6.6957820821E8  |
+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+

+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+
|EmploymentType|n_loans|exposure  |default_rate|avg_interest_rate|
avg_dti          |avg_credit_score |expected_loss_proxy|
+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+
|Unemployed    |63824  |8174575251|0.1355      |13.5047          |
0.4999833918275285|574.873824893457 |1.10765494651E9  |
|Part-time     |64161  |8169601068|0.1197      |13.496           |
0.5005684138339472|574.0955253191191|9.7790124784E8  |
|Self-employed |63706  |8118482425|0.1146      |13.481           |
0.5000773867453601|574.680045835557 |9.3037808591E8  |
|Full-time     |63656  |8114221828|0.0946      |13.4893          |
0.5002169473419669|573.4073928616313|7.6760538493E8  |
+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+

+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+
|HasCoSigner|n_loans|exposure  |default_rate|avg_interest_rate|
avg_dti          |avg_credit_score |expected_loss_proxy|
+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+
|No           |127646 |16301645747|0.1287      |13.5193          |
0.5001258167118413|574.702207668082 |2.09802180764E9  |
|Yes          |127701 |16275234825|0.1036      |13.4663          |
0.50029827487647  |573.8266732445321|1.68611432787E9  |
+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+

```

```
pricing_matrix = (
    df.groupBy("CreditScoreBand", "DTIBand")
      .agg(
        F.count("*").alias("n_loans"),
        F.sum("LoanAmount").alias("exposure"),
        F.avg("InterestRate").alias("avg_interest_rate"),
        F.avg("Default").alias("default_rate"),
      )
      .withColumn("avg_interest_rate", F.round("avg_interest_rate",
4))
      .withColumn("default_rate", F.round("default_rate", 4))
)
```

Simple "mispricing flag": high default but not high interest (relative to overall avg)

```
overall = df.agg(
    F.avg("InterestRate").alias("overall_avg_ir"),
    F.avg("Default").alias("overall_default_rate")
).collect()[0]
```

```
overall_avg_ir = float(overall["overall_avg_ir"])
overall_default_rate = float(overall["overall_default_rate"])
```

```
pricing_matrix_flagged = (
    pricing_matrix
      .withColumn("high_default", F.col("default_rate") >
F.lit(overall_default_rate))
      .withColumn("low_rate", F.col("avg_interest_rate") <
F.lit(overall_avg_ir))
      .withColumn("mispricing_flag", F.col("high_default") &
F.col("low_rate"))
      .orderBy(F.col("default_rate").desc(),
F.col("avg_interest_rate").asc())
)
```

```
pricing_matrix_flagged.show(50, truncate=False)
```

```
+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+
|CreditScoreBand|DTIBand  |n_loans|exposure  |avg_interest_rate|
|default_rate|high_default|low_rate|mispricing_flag|
+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+
|<600          |0.50+    |70848  |9026344994|13.4686          |0.1289
|true          |true     |true   |           |                  |
|<600          |0.35-0.49|26160  |3347078288|13.4525          |0.1244
|true          |true     |true   |           |                  |
|<600          |0.20-0.34|26082  |3327874967|13.539           |0.1207
|true          |false    |false  |           |                  |
|650-699       |0.50+    |11683  |1501376391|13.6239          |0.1191
```

true	false	false			
600-649	0.50+	11673	1504056035	13.462	0.1163
true	true	true			
600-649	0.35-0.49	4439	568832030	13.5686	0.1158
false	false	false			
<600	<0.20	16393	2081547447	13.5121	0.1126
false	false	false			
700-749	0.50+	11570	1474174678	13.4652	0.1119
false	true	false			
650-699	<0.20	2946	379478310	13.6425	0.1103
false	false	false			
750+	0.50+	23523	3002359015	13.497	0.1071
false	false	false			
600-649	0.20-0.34	4436	564178856	13.4448	0.1066
false	true	false			
650-699	0.35-0.49	4248	536237527	13.4004	0.1057
false	true	false			
700-749	0.20-0.34	4227	541096671	13.5586	0.0998
false	false	false			
700-749	0.35-0.49	4300	544128960	13.5278	0.0993
false	false	false			
750+	0.35-0.49	8814	1128012375	13.4967	0.0988
false	false	false			
650-699	0.20-0.34	4274	546434318	13.4681	0.0976
false	true	false			
750+	0.20-0.34	8746	1110010238	13.6178	0.0964
false	false	false			
600-649	<0.20	2735	349829830	13.3441	0.0962
false	true	false			
700-749	<0.20	2759	344521184	13.5421	0.0892
false	false	false			
750+	<0.20	5491	699308458	13.3001	0.0843
false	true	false			
+-----+-----+-----+-----+-----+-----					
+-----+-----+-----+-----+-----+-----					

```
k = 0.20 # tweak; it's a proxy used consistently for
ranking/comparison
```

```
pricing_scored = (
    pricing_matrix
    .withColumn("risk_spread_proxy",
F.round(F.col("avg_interest_rate") - (F.col("default_rate") *
F.lit(k)), 4))
    .orderBy(F.col("risk_spread_proxy").asc()) # low score =
potentially underpriced risk
)

pricing_scored.show(50, truncate=False)
```

+-----+-----+-----+-----+-----+-----					
+-----+-----+-----+-----+-----+-----					
CreditScoreBand	DTIBand	n_loans	exposure	avg_interest_rate	default_rate
risk_spread_proxy					
+-----+-----+-----+-----+-----+-----					
+-----+-----+-----+-----+-----+-----					
750+	<0.20	5491	699308458	13.3001	0.0843
13.2832					
600-649	<0.20	2735	349829830	13.3441	0.0962
13.3249					
650-699	0.35-0.49	4248	536237527	13.4004	0.1057
13.3793					
600-649	0.20-0.34	4436	564178856	13.4448	0.1066
13.4235					
<600	0.35-0.49	26160	3347078288	13.4525	0.1244
13.4276					
600-649	0.50+	11673	1504056035	13.462	0.1163
13.4387					
<600	0.50+	70848	9026344994	13.4686	0.1289
13.4428					
700-749	0.50+	11570	1474174678	13.4652	0.1119
13.4428					
650-699	0.20-0.34	4274	546434318	13.4681	0.0976
13.4486					
750+	0.50+	23523	3002359015	13.497	0.1071
13.4756					
750+	0.35-0.49	8814	1128012375	13.4967	0.0988
13.4769					
<600	<0.20	16393	2081547447	13.5121	0.1126
13.4896					
700-749	0.35-0.49	4300	544128960	13.5278	0.0993
13.5079					
<600	0.20-0.34	26082	3327874967	13.539	0.1207
13.5149					
700-749	<0.20	2759	344521184	13.5421	0.0892
13.5243					
700-749	0.20-0.34	4227	541096671	13.5586	0.0998
13.5386					
600-649	0.35-0.49	4439	568832030	13.5686	0.1158
13.5454					
750+	0.20-0.34	8746	1110010238	13.6178	0.0964
13.5985					
650-699	0.50+	11683	1501376391	13.6239	0.1191
13.6001					
650-699	<0.20	2946	379478310	13.6425	0.1103
13.6204					
+-----+-----+-----+-----+-----+-----					
+-----+-----+-----+-----+-----+-----					

```

from pyspark.sql import functions as F

# 1) Build the matrix
pricing_matrix = (
    df.groupBy("CreditScoreBand", "DTIBand")
        .agg(
            F.count("*").alias("n_loans"),
            F.sum("LoanAmount").alias("exposure"),
            F.avg("InterestRate").alias("avg_interest_rate"),
            F.avg("Default").alias("default_rate"),
        )
        .withColumn("avg_interest_rate", F.round("avg_interest_rate",
4))
        .withColumn("default_rate", F.round("default_rate", 4))
        .withColumn("exposure", F.round("exposure", 0))
    )

# 2) Portfolio averages (benchmarks)
overall = df.agg(
    F.avg("InterestRate").alias("overall_avg_ir"),
    F.avg("Default").alias("overall_default_rate")
).collect()[0]

overall_avg_ir = float(overall["overall_avg_ir"])
overall_default_rate = float(overall["overall_default_rate"])

# 3) Add readable labels + BOTH underpriced and overpriced
pricing_matrix_labeled = (
    pricing_matrix
    # Plain English comparisons
    .withColumn(
        "risk_vs_portfolio",
        F.when(F.col("default_rate") > F.lit(overall_default_rate),
"Higher")
        .when(F.col("default_rate") < F.lit(overall_default_rate),
"Lower")
        .otherwise("Same as avg")
    )
    .withColumn(
        "rate_vs_portfolio",
        F.when(F.col("avg_interest_rate") > F.lit(overall_avg_ir),
"Higher")
        .when(F.col("avg_interest_rate") < F.lit(overall_avg_ir),
"Lower")
        .otherwise("Same as avg")
    )
    # Pricing status: underpriced / overpriced / fair
    .withColumn(
        "pricing_status",
        F.when(

```

```

        (F.col("default_rate") > F.lit(overall_default_rate)) &
        (F.col("avg_interest_rate") < F.lit(overall_avg_ir)),
        "UNDERPRICED"
    ).when(
        (F.col("default_rate") < F.lit(overall_default_rate)) &
        (F.col("avg_interest_rate") > F.lit(overall_avg_ir)),
        "OVERPRICED"
    ).otherwise("FAIR")
)
# Optional: a simple "severity" number (bigger = more extreme
mispricing)
.withColumn(
    "mispricing_severity",
    F.round(
        (F.col("default_rate") - F.lit(overall_default_rate)) -
        (F.col("avg_interest_rate") - F.lit(overall_avg_ir)) /
F.lit(100.0),
        4
    )
)
)
.select(
    "CreditScoreBand", "DTIBand", "n_loans", "exposure",
    "avg_interest_rate", "default_rate",
    "risk_vs_portfolio", "rate_vs_portfolio", "pricing_status",
    "mispricing_severity"
)
)

# 4) Sort so it's easy to read:
# Show UNDERPRICED first (most urgent), then OVERPRICED, then FAIR.
pricing_matrix_final = (
    pricing_matrix_labeled
    .withColumn(
        "sort_key",
        F.when(F.col("pricing_status").startswith("UNDERPRICED"),
F.lit(1))
        .when(F.col("pricing_status").startswith("OVERPRICED"),
F.lit(2))
        .otherwise(F.lit(3))
    )
    .orderBy(
        F.col("sort_key").asc(),
        F.col("default_rate").desc(),
        F.col("avg_interest_rate").asc()
    )
    .drop("sort_key")
)

pricing_matrix_final.show(50, truncate=False)

```

CreditScoreBand	DTIBand	n_loans	exposure	avg_interest_rate	default_rate	risk_vs_portfolio
mispricing_severity			rate_vs_portfolio	pricing_status		
<600	0.50+	70848	9026344994	13.4686		0.1289
Higher	Lower		UNDERPRICED	0.013		
<600	0.35-0.49	26160	3347078288	13.4525		0.1244
Higher	Lower		UNDERPRICED	0.0087		
600-649	0.50+	11673	1504056035	13.462		0.1163
Higher	Lower		UNDERPRICED	5.0E-4		
600-649	0.35-0.49	4439	568832030	13.5686		0.1158
Lower	Higher		OVERPRICED	-0.0011		
<600	<0.20	16393	2081547447	13.5121		0.1126
Lower	Higher		OVERPRICED	-0.0037		
650-699	<0.20	2946	379478310	13.6425		0.1103
Lower	Higher		OVERPRICED	-0.0073		
750+	0.50+	23523	3002359015	13.497		0.1071
Lower	Higher		OVERPRICED	-0.0091		
700-749	0.20-0.34	4227	541096671	13.5586		0.0998
Lower	Higher		OVERPRICED	-0.017		
700-749	0.35-0.49	4300	544128960	13.5278		0.0993
Lower	Higher		OVERPRICED	-0.0172		
750+	0.35-0.49	8814	1128012375	13.4967		0.0988
Lower	Higher		OVERPRICED	-0.0174		
750+	0.20-0.34	8746	1110010238	13.6178		0.0964
Lower	Higher		OVERPRICED	-0.021		
700-749	<0.20	2759	344521184	13.5421		0.0892
Lower	Higher		OVERPRICED	-0.0274		
<600	0.20-0.34	26082	3327874967	13.539		0.1207
Higher	Higher		FAIR	0.0041		
650-699	0.50+	11683	1501376391	13.6239		0.1191
Higher	Higher		FAIR	0.0017		

700-749	0.50+	11570	1474174678	13.4652	0.1119
Lower	Lower		FAIR	-0.004	
600-649	0.20-0.34	4436	564178856	13.4448	0.1066
Lower	Lower		FAIR	-0.009	
650-699	0.35-0.49	4248	536237527	13.4004	0.1057
Lower	Lower		FAIR	-0.0095	
650-699	0.20-0.34	4274	546434318	13.4681	0.0976
Lower	Lower		FAIR	-0.0183	
600-649	<0.20	2735	349829830	13.3441	0.0962
Lower	Lower		FAIR	-0.0184	
750+	<0.20	5491	699308458	13.3001	0.0843
Lower	Lower		FAIR	-0.0299	
+-----+-----+-----+-----+-----+-----					
+-----+-----+-----+-----+-----+-----					
+-----+					

```
def scenario_metrics(df, scenario_name, approve_condition):
    approved = df.withColumn("Approved", F.when(approve_condition,
F.lit(1)).otherwise(F.lit(0)))

    # Metrics on approved loans
    metrics = approved.agg(
        F.avg("Approved").alias("approval_rate"),
        F.sum(F.when(F.col("Approved") == 1,
F.col("LoanAmount")).otherwise(F.lit(0))).alias("approved_exposure"),
        F.avg(F.when(F.col("Approved") == 1,
F.col("Default"))).alias("approved_default_rate")
    )

    # Expected loss proxy on approved = approved_default_rate *
approved_exposure
    metrics = (
        metrics
        .withColumn("scenario", F.lit(scenario_name))
        .withColumn("approved_default_rate",
F.round("approved_default_rate", 4))
        .withColumn("approval_rate", F.round("approval_rate", 4))
        .withColumn("approved_exposure", F.round("approved_exposure",
2))
        .withColumn("expected_loss_proxy",
F.round(F.col("approved_default_rate") * F.col("approved_exposure"),
2))
    )
```



```

        .select("scenario", "approval_rate", "approved_exposure",
"approved_default_rate", "expected_loss_proxy")
    )
    return metrics

# Baseline: everyone approved
baseline = scenario_metrics(df, "Baseline_AllApproved", F.lit(True))

# Scenario A: CreditScore >= 680
scA = scenario_metrics(df, "A_CreditScore>=680", F.col("CreditScore")
>= 680)

# Scenario B: DTIRatio <= 0.35
scB = scenario_metrics(df, "B_DTI<=0.35", F.col("DTIRatio") <= 0.35)

# Scenario C: CreditScore>=660 AND DTIRatio<=0.40
scC = scenario_metrics(df, "C_Score>=660_AND_DTI<=0.40",
                        (F.col("CreditScore") >= 660) &
                        (F.col("DTIRatio") <= 0.40))

# Scenario D: If score < 640 require co-signer, else approve
# (Assumes HasCoSigner is "Yes"/"No"; adjust if it's 1/0)
scD_condition = (
    (F.col("CreditScore") >= 640) |
    ((F.col("CreditScore") < 640) & (F.col("HasCoSigner") == "Yes")))
)
scD = scenario_metrics(df, "D_LowScoreRequiresCosigner",
scD_condition)

scenario_compare =
baseline.unionByName(scA).unionByName(scB).unionByName(scC).unionByNam
e(scD)

scenario_compare.show(truncate=False)
print('What if Policy Results')

```

```

+-----+-----+-----+
+-----+-----+-----+
|scenario|approval_rate|approved_exposure|
approved_default_rate|expected_loss_proxy|
+-----+-----+-----+
+-----+-----+-----+
|Baseline_AllApproved|1.0|32576880572|0.1161
|3.78217583441E9|
|A_CreditScore>=680|0.3078|10013932616|0.1032
|1.03343784597E9|
|B_DTI<=0.35|0.3178|10342481236|0.1083
|1.12009071786E9|
|C_Score>=660_AND_DTI<=0.40|0.1313|4267830775|0.0946
|4.0373679132E8|

```

D_LowScoreRequiresCosigner 0.6912	22507893488	0.1068
2.40384302452E9		
+-----+-----+-----		
+-----+-----+-----		

What if Policy Results

##What if compared to today

```
from pyspark.sql.window import Window

w = Window.orderBy(F.lit(1))

baseline_vals = scenario_compare.filter(F.col("scenario") ==
"Baseline_AllApproved").collect()[0]
base_exposure = float(baseline_vals["approved_exposure"])
base_loss = float(baseline_vals["expected_loss_proxy"])
base_approval = float(baseline_vals["approval_rate"])

scenario_compare_delta = (
    scenario_compare
    .withColumn("delta_exposure", F.round(F.col("approved_exposure") -
F.lit(base_exposure), 2))
    .withColumn("delta_expected_loss",
F.round(F.col("expected_loss_proxy") - F.lit(base_loss), 2))
    .withColumn("delta_approval_rate", F.round(F.col("approval_rate")
- F.lit(base_approval), 4))
    .orderBy(F.col("expected_loss_proxy").asc())
)

scenario_compare_delta.show(truncate=False)
```

+-----+-----+-----		
+-----+-----+-----		
+-----+-----+-----		
scenario	approval_rate approved_exposure	
approved_default_rate expected_loss_proxy delta_exposure		
delta_expected_loss delta_approval_rate		
+-----+-----+-----		
+-----+-----+-----		
+-----+-----+-----		
C_Score>=660_AND_DTI<=0.40 0.1313	4267830775	0.0946
4.0373679132E8	-2.8309049797E10 -3.37843904309E9	-0.8687
A_CreditScore>=680	0.3078	10013932616
1.03343784597E9	-2.2562947956E10 -2.74873798844E9	-0.6922
B_DTI<=0.35	0.3178	10342481236
1.12009071786E9	-2.2234399336E10 -2.66208511655E9	-0.6822

D_LowScoreRequiresCosigner 0.6912	22507893488	0.1068
2.40384302452E9	-1.0068987084E10 -1.37833280989E9	-0.3088
Baseline_AllApproved	1.0	32576880572
3.78217583441E9	0.0	0.0
+-----+-----+-----		
+-----+-----+-----		
+-----+-----+-----		

"If we raised interest rates only for the borrowers we already know are underpriced, how much risk would that reduce?"

#Code

```
underpriced_segments = (
    pricing_matrix_labeled
    .filter(F.col("pricing_status").startswith("UNDERPRICED"))
    .select("CreditScoreBand", "DTIBand")
)

underpriced_segments.show(truncate=False)

+-----+-----+
|CreditScoreBand|DTIBand|
+-----+-----+
|<600           |0.50+  |
|600-649        |0.50+  |
|<600           |0.35-0.49|
+-----+-----+
```

```
from pyspark.sql import functions as F

underpriced_segments = underpriced_segments.select(
    "CreditScoreBand", "DTIBand"
).distinct().withColumn("underpriced_marker", F.lit(1))

df_with_pricing_flag = (
    df.join(underpriced_segments, on=["CreditScoreBand", "DTIBand"],
    how="left")
    .withColumn(
        "is_underpriced",
        F.when(F.col("underpriced_marker").isNotNull(),
        F.lit(1)).otherwise(F.lit(0))
    )
    .drop("underpriced_marker")
)
```

```

)

# sanity check
df_with_pricing_flag.groupBy("is_underpriced").count().show()

+-----+-----+
|is_underpriced| count|
+-----+-----+
|              |1|108681|
|              |0|146666|
+-----+-----+

df_price_plus_1 = (
  df_with_pricing_flag
  .withColumn(
    "AdjustedInterestRate",
    F.when(
      F.col("is_underpriced") == 1,
      F.col("InterestRate") + F.lit(1.0)
    ).otherwise(F.col("InterestRate"))
  )
)

pricing_plus_1 = (
  df_price_plus_1
  .groupBy("CreditScoreBand", "DTIBand")
  .agg(
    F.avg("AdjustedInterestRate").alias("avg_adj_interest_rate"),
    F.avg("Default").alias("default_rate")
  )
  .withColumn("avg_adj_interest_rate",
    F.round("avg_adj_interest_rate", 4))
)

pricing_plus_1 = (
  pricing_plus_1
  .withColumn(
    "new_risk_spread_proxy",
    F.round(
      F.col("avg_adj_interest_rate") - (F.col("default_rate") *
F.lit(k)),
      4
    )
  )
)

pricing_comparison = (
  pricing_scored
  .join(

```

```

        pricing_plus_1.select("CreditScoreBand", "DTIBand",
"new_risk_spread_proxy"),
        on=["CreditScoreBand", "DTIBand"],
        how="left"
    )
    .withColumn(
        "delta_risk_spread",
        F.round(
            F.col("new_risk_spread_proxy") -
F.col("risk_spread_proxy"),
            4
        )
    )
    .orderBy(F.col("delta_risk_spread").desc())
)

```

```
pricing_comparison.show(50, truncate=False)
```

```
print('Counterfactual Pricing Test')
```

```

+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+
+-----+
|CreditScoreBand|DTIBand  |n_loans|exposure  |avg_interest_rate|
default_rate|risk_spread_proxy|new_risk_spread_proxy|
delta_risk_spread|
+-----+-----+-----+-----+-----+
+-----+-----+-----+-----+-----+
+-----+
|<600           |0.50+    |70848  |9026344994|13.4686          |0.1289
|13.4428        |14.4428  |        |1.0        |                  |
|600-649        |0.50+    |11673  |1504056035|13.462           |0.1163
|13.4387        |14.4387  |        |1.0        |                  |
|<600           |0.35-0.49|26160  |3347078288|13.4525          |0.1244
|13.4276        |14.4276  |        |1.0        |                  |
|700-749        |<0.20    |2759   |344521184 |13.5421          |0.0892
|13.5243        |13.5243  |        |0.0        |                  |
|650-699        |0.50+    |11683  |1501376391|13.6239          |0.1191
|13.6001        |13.6001  |        |0.0        |                  |
|650-699        |0.35-0.49|4248   |536237527 |13.4004          |0.1057
|13.3793        |13.3793  |        |0.0        |                  |
|<600           |0.20-0.34|26082  |3327874967|13.539           |0.1207
|13.5149        |13.5149  |        |0.0        |                  |
|750+           |0.20-0.34|8746   |1110010238|13.6178          |0.0964
|13.5985        |13.5985  |        |0.0        |                  |
|750+           |0.35-0.49|8814   |1128012375|13.4967          |0.0988
|13.4769        |13.4769  |        |0.0        |                  |
|700-749        |0.20-0.34|4227   |541096671 |13.5586          |0.0998
|13.5386        |13.5386  |        |0.0        |                  |
|600-649        |0.35-0.49|4439   |568832030 |13.5686          |0.1158

```

13.5454	13.5454	0.0		
600-649	0.20-0.34	4436	564178856	13.4448
13.4235	13.4235	0.0		0.1066
750+	0.50+	23523	3002359015	13.497
13.4756	13.4756	0.0		0.1071
700-749	0.35-0.49	4300	544128960	13.5278
13.5079	13.5079	0.0		0.0993
700-749	0.50+	11570	1474174678	13.4652
13.4428	13.4428	0.0		0.1119
650-699	0.20-0.34	4274	546434318	13.4681
13.4486	13.4486	0.0		0.0976
750+	<0.20	5491	699308458	13.3001
13.2832	13.2832	0.0		0.0843
650-699	<0.20	2946	379478310	13.6425
13.6204	13.6204	0.0		0.1103
<600	<0.20	16393	2081547447	13.5121
13.4896	13.4896	0.0		0.1126
600-649	<0.20	2735	349829830	13.3441
13.3249	13.3249	0.0		0.0962
+-----+-----+-----+-----+-----				
+-----+-----+-----+-----+-----				
+-----+				

Counterfactual Pricing Test

A targeted 1% interest rate increase applied only to underpriced borrower segments uniformly improved pricing alignment across those segments without impacting the rest of the portfolio.