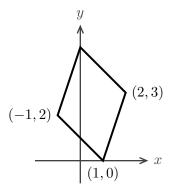
Areas and Determinants

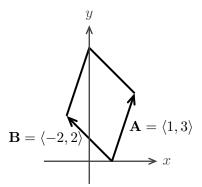
1. Compute
$$\begin{vmatrix} 6 & 5 \\ 1 & 2 \end{vmatrix}$$
.

Answer:
$$\begin{vmatrix} 6 & 5 \\ 1 & 2 \end{vmatrix} = 6 \cdot 2 - 5 \cdot 1 = 7.$$

2. Compute the area of the parallelogram shown.



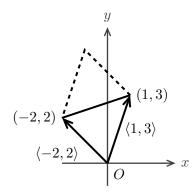
Answer: The area is given by the determinant of the vectors determining the parallelogram.



Area =
$$|\det(\mathbf{A}, \mathbf{B})| = \left|\det\begin{pmatrix} 1 & 3 \\ -2 & 2 \end{pmatrix}\right| = 2 + 6 = 8.$$

3. Find the area of the triangle with vertices (0,0), (-2,2) and (1,3).

Answer: The triangle is half a parallelogram. So the area is $\begin{vmatrix} 1 \\ 2 \end{vmatrix} \det \begin{pmatrix} 1 & 3 \\ -2 & 2 \end{vmatrix} = 2$.



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