TECHNICAL UNIVERSITY OF DENMARK

Course name Introduction to programming and data processing

Course Number 02633 (02631, 02692, 02694)

AIDS ALLOWED ALL AIDS EXAM DURATION 2 HOURS

Weighting All exercises have equal weight

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SUBMISSION DETAILS

You must hand in your solution electronically:

- 1. You can upload your solutions individually on CodeJudge (dtu.codejudge.net/prog-jun16/assignment) under Afleveringer/Exam. When you hand in a solution on CodeJudge, the test example given in the assignment description will be run on your solution. If your solution passes this single test, it will appear as Submitted. This means that your solution passes on this single test example. You can upload to CodeJudge as many times as you like during the exam.
- 2. You must upload your solutions on CampusNet. Each assignment must be uploaded as one separate .py file, given the same name as the function in the assignment:
 - (a) normalWeight.py
 - (b) danceClass.py
 - (c) survivalTemperature.py
 - (d) greenEyes.py
 - (e) bestBuy.py

The files must be handed in separately (not as a zip-file) and must have these exact filenames.

After the exam, your solutions will be automatically evaluated on CodeJudge on a range of different tests, to check that they work correctly in general. The assessment of you solution is based only on how many of the automated tests it passes.

- Make sure that your code follows the specifications exactly.
- Each solution shall not contain any additional code beyond the specified function.
- Remember, you can check if your solutions follow the specifications by uploading them to CodeJudge.
- Note that all vectors and matrices used as input or output must be numpy arrays.

Assignment A Normal weight

The body mass index (BMI) is defined as

$$\mathtt{BMI} = \frac{w}{h^2}$$

where w is body weight (mass) in kilograms, and h is the height in metres. A person is categorized as being of normal weight if his BMI falls in range from 18.5 to 25 kg m⁻², both endpoints included.

■ Problem definition

Write a function normalWeight that takes height in meters as input. The function should return a vector representing the normal weight range, given as the smallest and the largest weight in whole kilograms, which when converted to BMI fall into normal range.

■ Solution template

```
def normalWeight(h):
    #insert your code
    return w
```

Input

h Height in meters (decimal number).

Output

w Interval for normal weight in kilograms (vector with 2 elements).

Example

Say a height is given as h = 1.73. The weight limits of the normal range can be calculated as

$$w_{\text{lower}} = 18.5 \cdot 1.73^2 = 55.3687$$
 and $w_{\text{upper}} = 25 \cdot 1.73^2 = 74.8225$. (1)

We need weight in whole kilograms, so numbers should be rounded. To ensure that weight falls into the normal range, the lower limit should be rounded up and the upper limit should be rounded down. The final output of the function is the vector [56, 74].

Assignment B Dance class

A dance class is considered valid if all of the following conditions are met:

- there is no less than 10 participants,
- there is no more than 30 participants,
- when the participants are in dance couples (one male and one female), there is no more than 3 unpaired (only male or only female) participants.

For registration purposes a vector is used with number 0 corresponding to the male and 1 to female participant.

■ Problem definition

Write a function named danceClass that takes a vector corresponding to registered participants as input and returns a string valid or invalid indicating whether the dance class is valid or not.

■ Solution template

```
def danceClass(v):
    #insert your code
    return s
```

Input

v Class registration (vector containing zeros and ones).

Output

s Class validity (string).

Example

Say we have following vector as input

```
[\ 1\ \ 1\ \ 1\ \ 0\ \ 0\ \ 1\ \ 0\ \ 1\ \ 1\ \ 1\ \ 0\ ].
```

There are 11 registered participants (elements in the vector). Number 11 is neither smaller than 10, nor larger than 30, so the first two conditions are met. There are 7 female participants (ones in the vector) and 4 male participants (zeros in the vector). This makes 4 male-female couples, and leaves 3 unpaired female participants. Number 3 is not larger than 3, so last condition is also met. The function should return valid.

Assignment C Survival temperature

To survive in cold temperatures, humans must either maintain a sufficiently high metabolic rate, or regulate heat loss by covering their body with clothes made of insulating material. The expression giving the lowest temperature for survival T in degrees Celsius as a function of metabolic heat production M in W m⁻² and a thermal conductance (for clothes and tissue) g in mol m⁻² s⁻¹ is

$$T = 36 - \frac{(0.9M - 12)(g + 0.95)}{27.8g}.$$
 (2)

The reasonable range for metabolic heat production is from 50 W m $^{-2}$ for sleep to 500 W m $^{-2}$ for heavy activity, e.g. sports. The reasonable range for thermal conductance is from 0.04 mol m $^{-2}$ s $^{-1}$ for winter sleeping bag to 0.45 mol m $^{-2}$ s $^{-1}$ for no clothing.

■ Problem definition

Write a function named survivalTemperature that takes a vector of values for the metabolic heat production M and a vector of values of the thermal conductance g as input. The function should return a matrix T of size $N_M \times N_g$, where N_M is the number of elements of M and N_g is number of elements in g. Elements of T should be the lowest survival temperature for the corresponding values from M and g. If some of the input values from M and g fall outside the reasonable range for that input, the function should not return a matrix, but instead a string RangeError.

■ Solution template

def survivalTemperature(M,g):

#insert your code

return T

Input

M Values for metabolic heat production M (vector with N_M elements).

g Values for thermal conductance g (vector with N_g elements).

Output

Values for survival temperature T ($N_M \times N_q$ matrix) or an error string.

Example

Consider following input

$$M = [50 \ 200 \ 300], \quad g = [0.20 \ 0.14]. \tag{3}$$

We have $N_M = 3$, $N_q = 2$, and the resulting 3×2 matrix should be

$$T = \begin{bmatrix} 29.1745 & 26.7580 \\ 1.2518 & -11.0504 \\ -17.3633 & -36.2559 \end{bmatrix}, \tag{4}$$

where, for example, element (2,1) of matrix T is computed as

$$T_{(2,1)} = 36 - \frac{(0.9 \cdot 200 - 12)(0.20 + 0.95)}{27.8 \cdot 0.20} = 1.2518.$$
 (5)

Assignment D Green eyes

The following chart gives probabilities (in percents) for child eye colors based on the eye colors of the parents.

	Parents	Child • • •		
		(brown)	(\mathtt{blue})	(\mathtt{green})
• + •	(brown + brown)	75	6	19
ullet + $ullet$	$(\mathtt{brown} + \mathtt{blue})$	50	50	0
ullet + $ullet$	$(\mathtt{brown} + \mathtt{green})$	50	12	38
ullet + $ullet$	$(\mathtt{blue} + \mathtt{blue})$	0	99	1
ullet + $ullet$	$(\mathtt{blue} + \mathtt{green})$	0	50	50
ullet + $ullet$	$(\mathtt{green} + \mathtt{green})$	0	25	75

■ Problem definition

Write a function greenEyes that takes two strings representing eye colors of the parents (in any order) as input. The strings are expected to be written in lower case as in the table above. The function should return the probability (in percents) of the child eye color being green.

■ Solution template

def greenEyes(p1,p2):
 #insert your code
 return P

Input

p1 Eye color of one parent (string).

p2 Eye color of second parent (string).

Output

P The probability in percent of the child eye color being green (number).

Example

Consider following input

$$p1 = green, \quad p2 = brown.$$
 (6)

According to the table, the green and brown combination (brown+green) gives the 38 percent probability for a child having green eyes. Thus, the number 38 should be returned.

Assignment E Best buy

A shopper is given a sum of money and a shopping list. He will start at the top of the list, and will be buying items one by one as long as he has enough money to buy the next item. When he does not have enough money to buy the next item, he will go home.

Problem definition

Write a function bestBuy which takes a vector containing prices of the items at the shopping list and a number representing the som of money the shopper is given as input. The function should return a total number of items bought by the shopper, before he returned home.

■ Solution template

```
def bestBuy(p,m):
    #insert your code
    return n
```

Input

p Prices of items (vector of positive numbers).

m Available money (positive number).

Output

n Number of bought items (whole number).

Example

Say we have a following input

$$p = [5 \ 4 \ 6 \ 2 \ 9 \ 1 \ 1 \ 4], \quad m = 16. \tag{7}$$

The spending looks like this

number of bought items	0	1	2	3
money left	16	11	7	1
price of next item	5	4	6	2

After 3 bought items the shopper has spent 5 + 4 + 6 = 15 money and has 16 - 15 = 1 money left, which is not enough to buy the next item on the list which costs 2 money. He returns home with 3 items, and function should return 3.

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