

```
In [1]: import tensorflow as tf
```

```
In [2]: # 0D张量只包含一个数字，有0个维度，又称为标量
rank_0_tensor = tf.constant(4)
print(rank_0_tensor)
```

```
tf.Tensor(4, shape=(), dtype=int32)
```

```
In [3]: # 1D张量包含一个一维数组，可以看作由0D张量组成的数组，有1个维度，又称为向量
rank_1_tensor = tf.constant([2.0, 3.0, 4.0])
print(rank_1_tensor)
```

```
tf.Tensor([2. 3. 4.], shape=(3,), dtype=float32)
```

```
In [4]: # 2D张量可以看作由1D张量组成的数组，有2个维度，又称为矩阵
rank_2_tensor = tf.constant([[1, 2],
                             [3, 4],
                             [5, 6]], dtype=tf.float16)

print(rank_2_tensor)
```

```
tf.Tensor(
[[1. 2.]
 [3. 4.]
 [5. 6.]], shape=(3, 2), dtype=float16)
```

```
In [5]: # 3D张量可以看作由2D张量组成的数组，有3个维度
```

```
rank_3_tensor = tf.constant([
    [[0, 1, 2, 3, 4],
     [5, 6, 7, 8, 9]],
    [[10, 11, 12, 13, 14],
     [15, 16, 17, 18, 19]],
    [[20, 21, 22, 23, 24],
     [25, 26, 27, 28, 29]],
])

print(rank_3_tensor)
```

```
tf.Tensor(
[[[ 0  1  2  3  4]
  [ 5  6  7  8  9]]

 [[10 11 12 13 14]
  [15 16 17 18 19]]

 [[20 21 22 23 24]
  [25 26 27 28 29]]], shape=(3, 2, 5), dtype=int32)
```

## 1.标量运算

·向量运算

·矩阵运算

```
In [6]: #标量运算:对张量实施逐元素运算，包括加、减、乘、除、乘方以及三角函数、指数、对数等常见

a = tf.constant([[1, 2],
                 [3, 4]])
```

```
b = tf.constant([[0,0],
                 [1,0]])
```

```
print(a + b)
print(a - b)
print(a * b)
print(a / b)
```

```
tf.Tensor(
[[1 2]
 [4 4]], shape=(2, 2), dtype=int32)
tf.Tensor(
[[1 2]
 [2 4]], shape=(2, 2), dtype=int32)
tf.Tensor(
[[0 0]
 [3 0]], shape=(2, 2), dtype=int32)
tf.Tensor(
[[inf inf]
 [ 3. inf]], shape=(2, 2), dtype=float64)
```

### 1.标量运算

## 2.向量运算

### 3.矩阵运算

In [7]:

```
# 向量运算: 只在一个特定轴上运算, 将一个向量映射到一个标量或者另外一个向量
A= tf.constant([[2,20,30,3,6],
                [1,1,1,1,1]])
```

```
print(tf.math.reduce_sum(A))
print(tf.math.reduce_max(A))
```

```
B = tf.constant([[2,20,30,3,6],
                 [3,11,16,1,8],
                 [14,45,23,5,27]])
```

```
print(tf.math.reduce_sum(B,0))#沿0轴 (列方向), 求和
print(tf.math.reduce_sum(B,1))#沿1轴(行方向), 求和
print(tf.math.reduce_max(B,0))# 沿0轴, 求最大值
print(tf.math.reduce_max(B,1))# 沿1轴, 求最大值
```

```
tf.Tensor(66, shape=(), dtype=int32)
tf.Tensor(30, shape=(), dtype=int32)
tf.Tensor([19 76 69 9 41], shape=(5,), dtype=int32)
tf.Tensor([ 61  39 114], shape=(3,), dtype=int32)
tf.Tensor([14 45 30 5 27], shape=(5,), dtype=int32)
tf.Tensor([30 16 45], shape=(3,), dtype=int32)
```

In [8]:

```
# 矩阵运算:矩阵必须是二维的, 包括矩阵乘法、矩阵转置、矩阵逆、矩阵行列式、矩阵求特征值、
A= tf.constant([[2,20,30,3,6],
                [1,1,1,1,1]])
```

```
#矩阵转置
```

```
A_trans = tf.linalg.matrix_transpose(A)
print(A_trans)
```

```
B= tf.constant([[2,20,30,3,6],
                 [3,11,16,1,8],
                 [14,45,23,5,27]])
```

```
#矩阵点积
```

```
print(tf.linalg.matmul(B, A_trans))
```

```
tf.Tensor(
[[ 2  1]
 [20  1]
 [30  1]
 [ 3  1]
 [ 6  1]], shape=(5, 2), dtype=int32)
tf.Tensor(
[[1349  61]
 [ 757  39]
 [1795 114]], shape=(3, 2), dtype=int32)
```

## 2、低阶API

- .tf.constant():提供了常量的声明功能
- .tf.Variable():提供了变量的声明功能
- .tf.reshape():提供了多阶Tensor的形状变换功能
- .tf.math.reduce\_mean():提供了对Tensor求平均值的功能
- .tf.random.normal():随机生成一个Tensor, 其值符合正态分布
- .tf.random.uniform():随机生成一个Tensor, 其值符合均匀分布
- .tf.transpose():提供了矩阵的转置功能
- .tf.math.argmax():提供了返回一个数组内最大值对应索引的功能
- .tf.expand\_dims():在输入的Tensor中增加一个维度
- .tf.concat():将多个Tensor在同一个维度上进行连接
- .tf.bitcast():提供了数据类型转换功能

```
In [9]: # tf.constant() 提供了常量的声明功能
a=tf.constant(7)
print(a)
print(a.numpy())
```

```
tf.Tensor(7, shape=(), dtype=int32)
7
```

```
In [16]: # tf.Variable():提供了变量的声明功能
```

```
#声明一个Python变量
a1 = 7
print('a1= ', a1)
#声明一个0阶Tensor变量
a2 = tf.Variable(7)
print('a2= ', a2)
#声明一个1阶Tensor变量, 即数组
a3 = tf.Variable([0,1,2])
print('a3= ', a3)
print(a1, a2, a3)
```

```
a1= 7
a2= <tf.Variable 'Variable:0' shape=() dtype=int32, numpy=7>
a3= <tf.Variable 'Variable:0' shape=(3,) dtype=int32, numpy=array([0, 1, 2])> /n
7 <tf.Variable 'Variable:0' shape=() dtype=int32, numpy=7> <tf.Variable 'Variable:0' s
hape=(3,) dtype=int32, numpy=array([0, 1, 2])>
```

```
In [17]: # tf.reshape():提供了多阶Tensor的形状变换功能
```

```
a = tf.Variable([[0,1,2],[3,4,5]])
print(a)
# 对a的形状进行变换, 变换为(3,2)
a1 = tf.reshape(a, [3,2])
```

```
print(a1)
print(a1.shape)
```

```
<tf.Variable 'Variable:0' shape=(2, 3) dtype=int32, numpy=
array([[0, 1, 2],
       [3, 4, 5]])>
tf.Tensor(
[[0 1]
 [2 3]
 [4 5]], shape=(3, 2), dtype=int32)
(3, 2)
```

In [18]:

```
# tf.math.reduce_mean():提供了对Tensor求平均值的功能，输出数据类型会根据输入数据类型来
# input_tensor:配置输入的Tensor
# axis:配置按行求平均值或按列求平均值，默认是全行全列求平均值
# keepdims:配置输出结果是否保持二维矩阵特性
# name:配置操作的名称
```

```
a = tf.constant([1,2.,3,4,5,6,7.])

#输入数据类型是float32，输出数据类型也是float32
print(a.dtype)
print(tf.math.reduce_mean(a))
b = tf.constant([[1,2,1],[5,2,10]])

#输入数据类型是int32，输出数据类型也是int32
print(b.dtype)

#虽然平均值为3.5，但是由于上面确定了输出类型为整型，因此强制赋值为整数3
print(tf.math.reduce_mean(b))
```

```
<dtype: 'float32'>
tf.Tensor(4.0, shape=(), dtype=float32)
<dtype: 'int32'>
tf.Tensor(3, shape=(), dtype=int32)
```

In [20]:

```
# tf.random.normal():随机生成一个Tensor，其值符合正态分布。使用该API时有如下参数需要配
# shape:配置生成Tensor的维度
# mean:配置正态分布的中心值
# stddev:配置正态分布的标准差
# seed:配置正态分布的随机生成粒子
# dtype:配置生成Tensor的数据类型
```

```
a = tf.random.normal(shape=[2,3], mean=2)
print(a)# a为Tensor类型，是一个2维张量Tensor
print(type(a))# type()方法是Python的原生方法，查看Tensor对象a的类型，是一个Tensor
print(a.dtype)#由于a是Tensor类型，因此可以使用Tensor对象的dtype属性
print(a.numpy())# a转换成numpy的array数组类型，就是普通的数组类型
print(type(a.numpy()))
```

```
tf.Tensor(
[[3.093015  0.83826673 0.6251465 ]
 [3.308845  3.5064597  2.4058805 ]], shape=(2, 3), dtype=float32)
<class 'tensorflow.python.framework.ops.EagerTensor'>
<dtype: 'float32'>
[[3.093015  0.83826673 0.6251465 ]
 [3.308845  3.5064597  2.4058805 ]]
<class 'numpy.ndarray'>
```

In [24]:

```
# tf.random.uniform():随机生成一个Tensor，其值符合均匀分布。有如下参数需要配置：
# shape:配置生成Tensor的维度
# minval: 配置随机生成数值的最小值
# maxval:配置随机生成数值的最大值
# seed:配置正态分布的随机生成粒子
```

```
# dtype:配置生成Tensor的数据类型

a = tf.random.uniform(shape=[2,3],minval=1,maxval=10,seed=8,dtype=tf.int32)
print(a.numpy())
print('*'*20)
print(a.numpy())
```

```
<bound method _EagerTensorBase.numpy of <tf.Tensor: shape=(2, 3), dtype=int32, numpy=
array([[4, 1, 4],
       [2, 5, 9]])>>
*****
[[4 1 4]
 [2 5 9]]
```

In [25]:

```
# tf.transpose():提供了矩阵的转置功能。使用该API时配置的参数如下:
# a:输入需要转置的矩阵
# perm:配置转置后矩阵的形状
# conjugate:当输入矩阵是复数时, 需要配置为
# Truename:配置本次操作的名称

#定义x为一个3维张量, 形状是(2,2,3)
x = tf.constant([[[1,2,3],
                  [4,5,6]],
                 [[7,8,9],
                  [10,11,12]]])
#转置后的形状是(2,3,2)
a = tf.transpose(x,perm=[0,2,1])
print(a.numpy())
```

```
[[[ 1  4]
   [ 2  5]
   [ 3  6]]

  [[ 7 10]
   [ 8 11]
   [ 9 12]]]
```

In [26]:

```
# tf.math.argmax():提供了返回一个数组内最大值对应索引的功能。使用该API时有如下参数可以
# input: 配置输入的数组
# axis:配置计算的维度
# output_type:配置输出的格式
# name:配置操作的名称

a = tf.constant([1,2,3,4,5])
x = tf.math.argmax(a)
print(x.numpy())
```

4

In [27]:

```
# tf.expand_dims():在输入的Tensor中增加一个维度, 比如t是一个维度为[2]的Tensor, 那么tf.
# 使用这个API时需要配置如下参数:
# input:配置输入的Tensor
# axis:配置需要添加维度的下标, 比如[2, 1]需要在2和1之间添加, 则配置值为1
# name:配置输出Tensor的名称

#初始化一个维度为(3,1)的Tensor
a = tf.constant([[1],[2],[3]])
print(a.shape)
print(a)
# 为a增加一个维度, 使其维度变成(1,3,1)
b = tf.expand_dims(a,0)
print(b.shape)
print(b)
```

```
(3, 1)
tf.Tensor(
[[1]
 [2]
 [3]], shape=(3, 1), dtype=int32)
(1, 3, 1)
tf.Tensor(
[[[1]
 [2]
 [3]]], shape=(1, 3, 1), dtype=int32)
```

In [33]:

```
# tf.concat():将多个Tensor在同一个维度上进行连接,使用该API时需要进行如下参数配置:
# values:配置Tensor的列表或者是一个单独的Tensor
# axis:配置按行或按列连接,axis=0表示按行连接,axis=1表示按列连接
# name:配置运算操作的名称

a1 = tf.constant([[2,3,4],[4,5,6],[2,3,4]])
a2 = tf.constant([[1,2,2],[6,7,9],[2,3,2]])
print('原始矩阵:')
print('a1=',a1.numpy())
print('a2=',a2.numpy())
#按行进行连接
print('按行进行连接:axis=0')
b = tf.concat([a1,a2], axis=0)
print(b.numpy())

#按列进行连接
print('按列进行连接:axis=1')
b = tf.concat([a1,a2], axis=1)
print(b.numpy())
```

```
原始矩阵:
a1= [[2 3 4]
 [4 5 6]
 [2 3 4]]
a2= [[1 2 2]
 [6 7 9]
 [2 3 2]]
按行进行连接:axis=0
[[2 3 4]
 [4 5 6]
 [2 3 4]
 [1 2 2]
 [6 7 9]
 [2 3 2]]
按列进行连接:axis=1
[[2 3 4 1 2 2]
 [4 5 6 6 7 9]
 [2 3 4 2 3 2]]
```

In [34]:

```
# tf.bitcast():提供了数据类型转换功能:
# type:配置转换后的数据类型,可选择的类型包括:
# tf.bfloat16, tf.half, tf.float32, tf.float64 (加tf.+类型)

#a原本是浮点类型float32类型
a = tf.constant(32.0)
#将a转换成整型int32
b = tf.bitcast(a,type=tf.int32)
print(a.dtype)
print(b.dtype)
```

```
<dtype: 'float32'>
<dtype: 'int32'>
```

### 3、Tensorflow高阶API(tf.keras)

```
In [47]: from sklearn import datasets
import numpy as np

#从sklearn中导入数据集
x_train = datasets.load_iris().data #导入iris数据集的输入
y_train = datasets.load_iris().target #导入iris数据集的标签

np.random.seed(120) #设置随机种子, 让每次结果都一样, 方便对照
np.random.shuffle(x_train) #使用shuffle()方法, 让输入x_train乱序
np.random.seed(120) #设置随机种子, 让每次结果都一样, 方便对照
np.random.shuffle(y_train) #使用shuffle()方法, 让输入y_train乱序

#tf.random.set_seed(120) #让tensorflow中的种子数设置为120'''
```

```
In [48]: # 模型创建(Sequential方法):实例化模型对象,
# 方法是: tf.keras.Sequential()
import tensorflow as tf
#创建模型对象的实例
#model = tf.keras.Sequential()
model = tf.keras.models.Sequential([
    tf.keras.layers.Dense(3, activation='softmax',
                           kernel_regularizer=tf.keras.regularizers.l2())
])
```

```
In [49]: '''# 模型创建(Sequential方法):组建网络层

# 示例代码:实现三个全连接神经网络层级的集成, 构建一个全连接神经网络模型
import tensorflow as tf
#使用add()方法集成神经网络层级
model.add(tf.keras.layers.Dense(256, activation="relu"))
model.add(tf.keras.layers.Dense(128, activation="relu"))
model.add(tf.keras.layers.Dense(2, activation="softmax"))'''
```

```
Out[49]: '# 模型创建(Sequential方法):组建网络层\n\n# 示例代码:实现三个全连接神经网络层级的集成, 构建一个全连接神经网络模型\nimport tensorflow as tf\n#使用add()方法集成神经网络层级\nmodel.add(tf.keras.layers.Dense(256, activation="relu"))\nmodel.add(tf.keras.layers.Dense(128, activation="relu"))\nmodel.add(tf.keras.layers.Dense(2, activation="softmax"))'
```

Sequential().compile():提供了神经网络模型的编译功能, 需要定义三个参数:

- loss:用来配置模型的损失函数, 可以通过名称调用tf.losses (API中已经定义好的loss函数)
- optimizer:用来配置模型的优化器, 可以调用tf.keras.optimizers (API配置模型所需要的优化器)
- metrics:用来配置模型评价的方法, 如accuracy、mse等

```
In [50]: # 编译模型
model.compile(optimizer=tf.keras.optimizers.SGD(lr=0.1),
              loss=tf.keras.losses.SparseCategoricalCrossentropy(from_logits=False),
              metrics=["sparse_categorical_accuracy"])
```

```
C:\Users\A\anaconda3\lib\site-packages\keras\optimizer_v2\gradient_descent.py:102: Use
rWarning: The `lr` argument is deprecated, use `learning_rate` instead.
super(SGD, self).__init__(name, **kwargs)
```

```
In [51]: # 模型训练
```

```
#使用model.fit()方法来执行训练过程，
model.fit(
    x_train, y_train,
    batch_size=32,
    epochs=100,
    validation_split=0.2,
    validation_freq=20)
```

```
Epoch 1/100
4/4 [=====] - 0s 2ms/step - loss: 1.0306 - sparse_categorical
_accuracy: 0.5417
Epoch 2/100
4/4 [=====] - 0s 2ms/step - loss: 0.9619 - sparse_categorical
_accuracy: 0.6083
Epoch 3/100
4/4 [=====] - 0s 3ms/step - loss: 1.0652 - sparse_categorical
_accuracy: 0.6583
Epoch 4/100
4/4 [=====] - 0s 2ms/step - loss: 0.7098 - sparse_categorical
_accuracy: 0.6833
Epoch 5/100
4/4 [=====] - 0s 3ms/step - loss: 0.8163 - sparse_categorical
_accuracy: 0.6583
Epoch 6/100
4/4 [=====] - 0s 3ms/step - loss: 1.0491 - sparse_categorical
_accuracy: 0.6500
Epoch 7/100
4/4 [=====] - 0s 2ms/step - loss: 0.8715 - sparse_categorical
_accuracy: 0.6333
Epoch 8/100
4/4 [=====] - 0s 2ms/step - loss: 0.7782 - sparse_categorical
_accuracy: 0.7000
Epoch 9/100
4/4 [=====] - 0s 4ms/step - loss: 1.2221 - sparse_categorical
_accuracy: 0.6000
Epoch 10/100
4/4 [=====] - 0s 3ms/step - loss: 0.5530 - sparse_categorical
_accuracy: 0.7667
Epoch 11/100
4/4 [=====] - 0s 2ms/step - loss: 0.5949 - sparse_categorical
_accuracy: 0.7083
Epoch 12/100
4/4 [=====] - 0s 3ms/step - loss: 0.5465 - sparse_categorical
_accuracy: 0.7917
Epoch 13/100
4/4 [=====] - 0s 7ms/step - loss: 0.7197 - sparse_categorical
_accuracy: 0.6500
Epoch 14/100
4/4 [=====] - 0s 4ms/step - loss: 0.8596 - sparse_categorical
_accuracy: 0.6167
Epoch 15/100
4/4 [=====] - 0s 10ms/step - loss: 0.6518 - sparse_categorical
_accuracy: 0.7667
Epoch 16/100
4/4 [=====] - 0s 3ms/step - loss: 0.8912 - sparse_categorical
_accuracy: 0.6333
Epoch 17/100
4/4 [=====] - 0s 3ms/step - loss: 0.5538 - sparse_categorical
_accuracy: 0.8167
Epoch 18/100
4/4 [=====] - 0s 2ms/step - loss: 0.5209 - sparse_categorical
_accuracy: 0.7833
Epoch 19/100
4/4 [=====] - 0s 3ms/step - loss: 0.6197 - sparse_categorical
_accuracy: 0.6833
Epoch 20/100
4/4 [=====] - 0s 85ms/step - loss: 0.5462 - sparse_categorical
_accuracy: 0.7167 - val_loss: 0.4783 - val_sparse_categorical_accuracy: 0.8333
Epoch 21/100
```



4/4 [=====] - 0s 2ms/step - loss: 0.4707 - sparse\_categorical  
\_accuracy: 0.8333  
Epoch 22/100  
4/4 [=====] - 0s 2ms/step - loss: 0.5747 - sparse\_categorical  
\_accuracy: 0.7500  
Epoch 23/100  
4/4 [=====] - 0s 2ms/step - loss: 0.5052 - sparse\_categorical  
\_accuracy: 0.7417  
Epoch 24/100  
4/4 [=====] - 0s 3ms/step - loss: 0.5326 - sparse\_categorical  
\_accuracy: 0.8333  
Epoch 25/100  
4/4 [=====] - 0s 3ms/step - loss: 0.6479 - sparse\_categorical  
\_accuracy: 0.8333  
Epoch 26/100  
4/4 [=====] - 0s 4ms/step - loss: 0.4549 - sparse\_categorical  
\_accuracy: 0.9083  
Epoch 27/100  
4/4 [=====] - 0s 3ms/step - loss: 0.4777 - sparse\_categorical  
\_accuracy: 0.8667  
Epoch 28/100  
4/4 [=====] - 0s 2ms/step - loss: 0.4313 - sparse\_categorical  
\_accuracy: 0.9083  
Epoch 29/100  
4/4 [=====] - 0s 2ms/step - loss: 0.5341 - sparse\_categorical  
\_accuracy: 0.7583  
Epoch 30/100  
4/4 [=====] - 0s 3ms/step - loss: 0.5056 - sparse\_categorical  
\_accuracy: 0.8250  
Epoch 31/100  
4/4 [=====] - 0s 4ms/step - loss: 0.5137 - sparse\_categorical  
\_accuracy: 0.7833  
Epoch 32/100  
4/4 [=====] - 0s 2ms/step - loss: 0.4074 - sparse\_categorical  
\_accuracy: 0.8667  
Epoch 33/100  
4/4 [=====] - 0s 4ms/step - loss: 0.4537 - sparse\_categorical  
\_accuracy: 0.8083  
Epoch 34/100  
4/4 [=====] - 0s 2ms/step - loss: 0.4198 - sparse\_categorical  
\_accuracy: 0.9167  
Epoch 35/100  
4/4 [=====] - 0s 2ms/step - loss: 0.6320 - sparse\_categorical  
\_accuracy: 0.6333  
Epoch 36/100  
4/4 [=====] - 0s 2ms/step - loss: 0.5572 - sparse\_categorical  
\_accuracy: 0.7750  
Epoch 37/100  
4/4 [=====] - 0s 3ms/step - loss: 0.5676 - sparse\_categorical  
\_accuracy: 0.7167  
Epoch 38/100  
4/4 [=====] - 0s 3ms/step - loss: 0.5682 - sparse\_categorical  
\_accuracy: 0.7333  
Epoch 39/100  
4/4 [=====] - 0s 3ms/step - loss: 0.5107 - sparse\_categorical  
\_accuracy: 0.7167  
Epoch 40/100  
4/4 [=====] - 0s 12ms/step - loss: 0.5591 - sparse\_categorical  
\_accuracy: 0.7500 - val\_loss: 0.6830 - val\_sparse\_categorical\_accuracy: 0.7000  
Epoch 41/100  
4/4 [=====] - 0s 3ms/step - loss: 0.5818 - sparse\_categorical  
\_accuracy: 0.8000  
Epoch 42/100  
4/4 [=====] - 0s 3ms/step - loss: 0.3993 - sparse\_categorical  
\_accuracy: 0.8667  
Epoch 43/100  
4/4 [=====] - 0s 3ms/step - loss: 0.4115 - sparse\_categorical  
\_accuracy: 0.9083  
Epoch 44/100

4/4 [=====] - 0s 2ms/step - loss: 0.4853 - sparse\_categorical  
\_accuracy: 0.7750  
Epoch 45/100  
4/4 [=====] - 0s 2ms/step - loss: 0.4163 - sparse\_categorical  
\_accuracy: 0.8833  
Epoch 46/100  
4/4 [=====] - 0s 2ms/step - loss: 0.4727 - sparse\_categorical  
\_accuracy: 0.8000  
Epoch 47/100  
4/4 [=====] - 0s 3ms/step - loss: 0.4674 - sparse\_categorical  
\_accuracy: 0.8167  
Epoch 48/100  
4/4 [=====] - 0s 3ms/step - loss: 0.4536 - sparse\_categorical  
\_accuracy: 0.8917  
Epoch 49/100  
4/4 [=====] - 0s 2ms/step - loss: 0.4905 - sparse\_categorical  
\_accuracy: 0.9000  
Epoch 50/100  
4/4 [=====] - 0s 2ms/step - loss: 0.4394 - sparse\_categorical  
\_accuracy: 0.8250  
Epoch 51/100  
4/4 [=====] - 0s 2ms/step - loss: 0.6971 - sparse\_categorical  
\_accuracy: 0.6333  
Epoch 52/100  
4/4 [=====] - 0s 4ms/step - loss: 0.5546 - sparse\_categorical  
\_accuracy: 0.8000  
Epoch 53/100  
4/4 [=====] - 0s 3ms/step - loss: 0.4602 - sparse\_categorical  
\_accuracy: 0.7750  
Epoch 54/100  
4/4 [=====] - 0s 3ms/step - loss: 0.5039 - sparse\_categorical  
\_accuracy: 0.7833  
Epoch 55/100  
4/4 [=====] - 0s 1ms/step - loss: 0.3859 - sparse\_categorical  
\_accuracy: 0.9250  
Epoch 56/100  
4/4 [=====] - 0s 2ms/step - loss: 0.3940 - sparse\_categorical  
\_accuracy: 0.9083  
Epoch 57/100  
4/4 [=====] - 0s 2ms/step - loss: 0.3844 - sparse\_categorical  
\_accuracy: 0.9417  
Epoch 58/100  
4/4 [=====] - 0s 2ms/step - loss: 0.4611 - sparse\_categorical  
\_accuracy: 0.8250  
Epoch 59/100  
4/4 [=====] - 0s 3ms/step - loss: 0.4397 - sparse\_categorical  
\_accuracy: 0.8667  
Epoch 60/100  
4/4 [=====] - 0s 11ms/step - loss: 0.4033 - sparse\_categorical  
\_accuracy: 0.9167 - val\_loss: 0.3977 - val\_sparse\_categorical\_accuracy: 0.9667  
Epoch 61/100  
4/4 [=====] - 0s 4ms/step - loss: 0.4098 - sparse\_categorical  
\_accuracy: 0.8667  
Epoch 62/100  
4/4 [=====] - 0s 3ms/step - loss: 0.4387 - sparse\_categorical  
\_accuracy: 0.8333  
Epoch 63/100  
4/4 [=====] - 0s 3ms/step - loss: 0.4040 - sparse\_categorical  
\_accuracy: 0.8667  
Epoch 64/100  
4/4 [=====] - 0s 2ms/step - loss: 0.5888 - sparse\_categorical  
\_accuracy: 0.8250  
Epoch 65/100  
4/4 [=====] - 0s 2ms/step - loss: 0.3751 - sparse\_categorical  
\_accuracy: 0.9500  
Epoch 66/100  
4/4 [=====] - 0s 2ms/step - loss: 0.3872 - sparse\_categorical  
\_accuracy: 0.9167  
Epoch 67/100

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4/4 [=====] - 0s 3ms/step - loss: 0.5178 - sparse_categorical
_accuracy: 0.7417
Epoch 68/100
4/4 [=====] - 0s 3ms/step - loss: 0.4354 - sparse_categorical
_accuracy: 0.8333
Epoch 69/100
4/4 [=====] - 0s 3ms/step - loss: 0.3686 - sparse_categorical
_accuracy: 0.9417
Epoch 70/100
4/4 [=====] - 0s 2ms/step - loss: 0.3792 - sparse_categorical
_accuracy: 0.9250
Epoch 71/100
4/4 [=====] - 0s 2ms/step - loss: 0.4358 - sparse_categorical
_accuracy: 0.8333
Epoch 72/100
4/4 [=====] - 0s 4ms/step - loss: 0.4314 - sparse_categorical
_accuracy: 0.8583
Epoch 73/100
4/4 [=====] - 0s 3ms/step - loss: 0.3735 - sparse_categorical
_accuracy: 0.9500
Epoch 74/100
4/4 [=====] - 0s 3ms/step - loss: 0.4658 - sparse_categorical
_accuracy: 0.8000
Epoch 75/100
4/4 [=====] - 0s 2ms/step - loss: 0.5149 - sparse_categorical
_accuracy: 0.7333
Epoch 76/100
4/4 [=====] - 0s 2ms/step - loss: 0.4693 - sparse_categorical
_accuracy: 0.8250
Epoch 77/100
4/4 [=====] - 0s 3ms/step - loss: 0.5652 - sparse_categorical
_accuracy: 0.7250
Epoch 78/100
4/4 [=====] - 0s 3ms/step - loss: 0.3974 - sparse_categorical
_accuracy: 0.9167
Epoch 79/100
4/4 [=====] - 0s 2ms/step - loss: 0.3948 - sparse_categorical
_accuracy: 0.9333
Epoch 80/100
4/4 [=====] - 0s 13ms/step - loss: 0.3998 - sparse_categorical
l_accuracy: 0.8917 - val_loss: 0.4344 - val_sparse_categorical_accuracy: 0.8000
Epoch 81/100
4/4 [=====] - 0s 3ms/step - loss: 0.3705 - sparse_categorical
_accuracy: 0.9417
Epoch 82/100
4/4 [=====] - 0s 3ms/step - loss: 0.4268 - sparse_categorical
_accuracy: 0.9083
Epoch 83/100
4/4 [=====] - 0s 3ms/step - loss: 0.3839 - sparse_categorical
_accuracy: 0.9500
Epoch 84/100
4/4 [=====] - 0s 2ms/step - loss: 0.4830 - sparse_categorical
_accuracy: 0.8167
Epoch 85/100
4/4 [=====] - 0s 2ms/step - loss: 0.4201 - sparse_categorical
_accuracy: 0.9000
Epoch 86/100
4/4 [=====] - 0s 3ms/step - loss: 0.4669 - sparse_categorical
_accuracy: 0.8250
Epoch 87/100
4/4 [=====] - 0s 2ms/step - loss: 0.5585 - sparse_categorical
_accuracy: 0.7917
Epoch 88/100
4/4 [=====] - 0s 3ms/step - loss: 0.4020 - sparse_categorical
_accuracy: 0.8917
Epoch 89/100
4/4 [=====] - 0s 2ms/step - loss: 0.5704 - sparse_categorical
_accuracy: 0.7167
Epoch 90/100
```

```

4/4 [=====] - 0s 2ms/step - loss: 0.4474 - sparse_categorical
_accuracy: 0.8333
Epoch 91/100
4/4 [=====] - 0s 2ms/step - loss: 0.4752 - sparse_categorical
_accuracy: 0.8333
Epoch 92/100
4/4 [=====] - 0s 2ms/step - loss: 0.4194 - sparse_categorical
_accuracy: 0.8917
Epoch 93/100
4/4 [=====] - 0s 3ms/step - loss: 0.3423 - sparse_categorical
_accuracy: 0.9750
Epoch 94/100
4/4 [=====] - 0s 4ms/step - loss: 0.3820 - sparse_categorical
_accuracy: 0.9333
Epoch 95/100
4/4 [=====] - 0s 3ms/step - loss: 0.3612 - sparse_categorical
_accuracy: 0.9500
Epoch 96/100
4/4 [=====] - 0s 2ms/step - loss: 0.3614 - sparse_categorical
_accuracy: 0.9750
Epoch 97/100
4/4 [=====] - 0s 2ms/step - loss: 0.4358 - sparse_categorical
_accuracy: 0.8583
Epoch 98/100
4/4 [=====] - 0s 2ms/step - loss: 0.3838 - sparse_categorical
_accuracy: 0.9250
Epoch 99/100
4/4 [=====] - 0s 3ms/step - loss: 0.3695 - sparse_categorical
_accuracy: 0.9417
Epoch 100/100
4/4 [=====] - 0s 33ms/step - loss: 0.4284 - sparse_categorical
l_accuracy: 0.8833 - val_loss: 0.4003 - val_sparse_categorical_accuracy: 0.9000

```

Out[51]: <keras.callbacks.History at 0x1e45a22d8e0>

In [52]: `# 打印出网络结构和参数统计`  
`model.summary()`

Model: "sequential\_12"

Layer (type)	Output Shape	Param #
dense_22 (Dense)	(None, 3)	15

=====  
 Total params: 15  
 Trainable params: 15  
 Non-trainable params: 0  
 =====

In [54]: `#保存模型`  
`model.save(filepath='demo_model')#文件夹(将模型保存此文件夹)`

INFO:tensorflow:Assets written to: demo\_model/assets

In [58]: `#模型加载`  
`model = tf.keras.models.load_model("demo_model")`  
`#模型预测`  
`model.predict(x_train)`

Out[58]: array([[3.14646736e-02, 8.80347610e-01, 8.81876498e-02],  
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[9.15064037e-01, 8.48172456e-02, 1.18659424e-04],  
[9.50267851e-01, 4.97112647e-02, 2.09455648e-05],  
[1.06419828e-02, 5.97191811e-01, 3.92166197e-01],  
[9.43122625e-01, 5.68432026e-02, 3.41363993e-05]], dtype=float32)
```

In [ ]:

## 4、图像处理工具PIL

In [ ]: